

MSDS spring2020

Deep learning and data mining Robert Azencott

HW2

1 Describe your Data set and the associated classification task

i suggest to reduce the number of classes to the 3 largest classes C1 C2 C3 of sizes $\text{siz1} > \text{siz2} > \text{siz3}$

if siz3 is much smaller than siz2 and siz1 , inflate C3 artificially by adjoining to C3 one or two or even three copies of itself to get a better balanced classification problem

- indicate the number of cases N in the data set (after reduction of number of classes to 3)
- present in words the distinct classes C1 C2 C3 involved and their sizes
- Select a training set and a test set ; give the size of each class within the training set and within the test set ; give the proportions of cases in each class for the test set and for the training set; these two proportions should be similar for each class

2 Define the MLP architecture of an Automatic Classifier with $r=3$ classes

- select an MLP architecture with three layers L1, H, L2, extended by a Softmax function and its final output layer OUT

$L1 \Rightarrow H \Rightarrow L2 \Rightarrow \text{softmax} \Rightarrow \text{OUT}$

of respective dimensions

$p = \dim(L1) = \# \text{ descriptors}, h = \dim(H), \dim(L2) = 3; \dim(\text{OUT}) = 3$

- select a response function (either the sigmoid function or the RELU function) to be set for all neurons
- the goal of the MLP classifier is to provide for each input vector X_k an output probability vector OUT_k very close to the binary vector encoding the true class of the input X_k
- explain precisely what is the part played by the softmax function, and how the final classification of X_k is computed from OUT_k

3. Select 2 tentative sizes h for the hidden layer

To estimate one small but plausible value for h , namely $h = h_{95} < p$, apply PCA analysis to your training set of input vectors to generate p eigenvalues ordered in decreasing order

Plot this decreasing sequence of eigenvalues in yr report

Compute the smallest number " h_{95} " of eigenvalues preserving 95% of the total sum of eigenvalues

To estimate one larger plausible value h_L for the size h , proceed as follows

- apply PCA analysis to the set of M_j input vectors corresponding to the class C_j , with $j=1,2,3$ to generate M_j eigenvalues in decreasing order, and compute the smallest number " U_j " of eigenvalues preserving 95% of the total sum of these M_j eigenvalues;

- then define $h_L = U_1 + U_2 + U_3$.

3. for each one of the 2 values $h = h_{95}$, $h = h_L$ implement automatic training

- use gradient descent to minimize $avCRE$ = average CROSS ENTROPY error between computed and true values of the probability OUT_k

- explain precisely what is $aCRE$ during training and after each epoch

- indicate which software environment you will use for HW2

- indicate precisely which software functions you are choosing to implement MLP learning with $aCRE$ loss function;

- list clearly what are the options offered for this task, namely for initialization of the weights, for batch learning, for the successive gradient descent steps sizes $\epsilon(n)$, for stopping the learning, for intermediary outputs to monitor learning quality

- indicate your selections for batch size B , for time dependent gradient descent step size, for gradient descent algorithm, for stopping the learning, for *random* initialization of weights and thresholds

automatic learning typically implements successive steps

- at STEP($n-1$) select a new batch BAT_n containing B cases, and apply the learning rule to update the last vector of weights and thresholds $W(n-1)$ into a new vector W_n which includes both thresholds and weights.

- compute the batch average cross-entropy error $bavCRE_n$ by running the MLP parametrized by W_n on the current Batch BAT_n , and compute the vector G_n = gradient of $BACRE_n$ at step n by the formula $G_n = (1/\epsilon(n)) [W(n+1) - W(n)]$

- compute and plot the curve $n \rightarrow \text{baCREn}$
- compute and plot the curve $n \rightarrow \|W(n+1) - W(n)\| / \|W_n\|$
- compute the gradient norm $\|G_n\| = (1/\varepsilon(n)) \|W(n+1) - W(n)\|$ and the (fixed) dimension D of the gradient vector G_n ,
- plot the curve $n \rightarrow \|G_n\| / d$ where d is the square root of D
- comment on these three curves

4 Performance analysis

Do the following after each $\text{Epoch}(m)$, $m = 1, 2, \dots$

denote $\text{MLP}(m)$ the MLP classifier parametrized by the last weight vector computed during $\text{Epoch}(m)$

compute the performance indicator $\text{trainPER}(m)$ = percentage of correct classifications computed by $\text{MLP}(m)$ on the whole training set and the similar indicator $\text{testPER}(m)$ computed on the whole test set

on the same graph plot the two curves $\text{trainPER}(m)$ and $\text{testPER}(m)$ versus m ; compare the two curves to select the best epoch $\text{Epoch}(m^*)$ after which the learning should be stopped to avoid overfit

after the last epoch $\text{Epoch}(m^*)$ compute and interpret the 3×3 confusion matrix of $\text{MLP}(m^*)$

5 Impact of various learning options

Evaluate experimentally the impact on final performance of various factors such as changes in batch size, initialization, gradient descent step size, dimension h of H

6 Analysis of the hidden layer behaviour after completion of automatic learning

- call h^* the best of the two values h_{95} and h_L from the point of view of performance evaluations
- fix h^* and m^* and $\text{MLP}^* = \text{MLP}(m^*)$; perform and interpret a PCA analysis on the hidden layer activity vectors $H(1) \dots H(k) \dots H(N)$ generated by all the training inputs $X(k)$

- display and compare the average hidden neurons activity profiles PROF1 , PROF2, PROF3
where PROFj is the average of the $H(k)$ over all cases case(k) belonging to class j

- list the hidden neurons which achieve best DIFFERENTIATION between class C1 versus C2 ;
- do the same for C1 versus C3 , and then for C2 versus C3; interpret these results