

⊗

Panel Data - $t=4, i=2$

Time Individual

t	i	$D1$	$D2$	$D3$	Constant	y	x
1	1	$D1_1$	$D2_1$	$D3_1$	1		
2	1	$D1_1$	$D2_1$	$D3_1$	1		
3	1	$D1_1$	$D2_1$	$D3_1$	1		
4	1	$D1_1$	$D2_1$	$D3_1$	1		
1	2	$D1_2$	$D2_2$	$D3_2$	1		
2	2	$D1_2$	$D2_2$	$D3_2$	1		
3	2	$D1_2$	$D2_2$	$D3_2$	1		
4	2	$D1_2$	$D2_2$	$D3_2$	1		

t_j Note 1: $\text{Constant}_{it} = 1 \quad \forall i, t$

t_j Note 2: Fixed effects: $\begin{cases} D1_{it} = D1_i \\ D2_{it} = D2_i \\ D3_{it} = D3_i \end{cases} \quad \forall i, t$
(time-invariant)

t_j Note 3: $D1_i + D2_i + D3_i = 1 \quad \forall i$

(Since they are binary indicators for 1 state-specific variable (e.g. province) \rightarrow For each observation, exactly 1 of them equals 1, others equal 0)

t_j Therefore: $D1_i + D2_i + D3_i = \text{Constant}_{it} (=1) \quad \forall i, t$

If we write

$$y_{it} = \beta_0 \times \text{Constant}_{it} + \beta_1 x_{it} + \gamma_1 D1_i + \gamma_2 D2_i + \gamma_3 D3_i + u_{it}$$

$\text{Constant}_{it} = 1 = D1_i + D2_i + D3_i \quad \forall i, t$
 \rightarrow perfect multicollinearity!