

Level 2 Stars, Workshop 5

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Getting the Energy Out

- a) For the proton-proton chain the typical energy of a photon is ~ 5 MeV. At the centre of the Sun the core temperature is $T \sim 1.57 \times 10^7$ K. Compare the energy of the photons produced in the proton-proton chain to the mean energy of photons produced at the core of the Sun from black-body radiation. What do you learn from this comparison?
- b) Briefly describe the four dominant sources of opacity in stars. What source of opacity dominates in the atmosphere of the Sun ($T \sim 5,800$ K)?
- c) Calculate the initial intensity (i.e., the undiminished intensity) of the emission from a star with a measured intensity of $I_\lambda = 10^{-15} \text{ W m}^{-2}$ which is observed through a column of uniformly distributed material with an opacity of $\kappa = 0.030 \text{ m}^2 \text{ kg}^{-1}$, density of $\rho = 2.0 \times 10^{-4} \text{ kg m}^{-3}$, and length of $s = 10^6 \text{ m}$. Is the material optically thin or optically thick?
- d) A hypothetical star has the following stellar-core properties: fully ionised hydrogen gas, a radius of $r = 2.0 \times 10^8 \text{ m}$, a temperature of $T = 10^7 \text{ K}$, and gas pressure of $P = 10^{15} \text{ N m}^{-2}$.
 - i. What is the dominant form of opacity (κ) in the stellar core? Explain your reasoning.
 - ii. Calculate the opacity at the stellar core, assuming that all other forms of opacity are negligible.
 - iii. Estimate the time it takes for a photon to escape the core, assuming that the pressure is well characterized by the ideal gas law and that the time taken for the scattering of a photon is 10^{-8} sec . Give your answer in years.

$[m_H = 1.67 \times 10^{-27} \text{ kg}; e_c = 1.60 \times 10^{-19} \text{ C}; \epsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}; k = 1.38 \times 10^{-23} \text{ J K}^{-1}; \sigma_T = 6.65 \times 10^{-29} \text{ m}^2; h = 6.63 \times 10^{-34} \text{ J s}; c = 3.00 \times 10^8 \text{ m s}^{-1}]$