Mathematical Methods II Weekly problem set 8

(1) Find the general solution of the 2D Laplace equation

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0.$$

(2) Find the most general solution of the equation

$$ck\frac{\partial^2 u}{\partial x^2} + (c^2 + k^2)\frac{\partial^2 u}{\partial x \partial y} + ck\frac{\partial^2 u}{\partial y^2} = 6ck(2x^2 + y)$$

given that $u(x,y) = 2 + (c/k)^2([c/k] - 1)$ where the line x = 1 interects the line y = c/k.