

## Level 2 Stars, Workshop 2

David Alexander

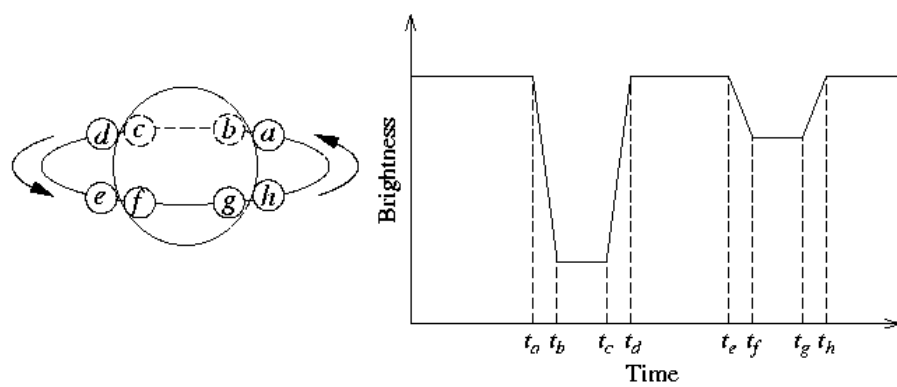
### **Binary stars**

- a) Assuming circular orbits, demonstrate that Keplers third law is the relation between the angular frequency and the mutual gravitational attraction of two stars in a binary system.

[Recall that Keplers third law is  $P^2 = \frac{4\pi^2 a^3}{G(m_1 + m_2)}$ , where  $P$  is the orbital period,  $a$  is the combination of the semi-major axes for the orbits of the two stars, and  $m_1$  and  $m_2$  are the individual masses of the two stars]

- b) Given that the Earth orbits the Sun in one year at a distance of 1 AU, calculate the orbital period of the system if the Earth was replaced with a solar mass star?
- c) How will the inclination angle (to your line of sight) of a visual binary system affect the mass measured using Keplers third law? How will the mass ratio of the two stars be affected by the inclination angle?
- d) An analysis of the spectrum (the spectrum is shown on the next page) of an eclipsing, double line, spectroscopic binary with a period of 8.6 years shows that the maximum Doppler shift of the Hydrogen Balmer H $\alpha$  (6562.8Å) line is  $\Delta\lambda_s = 0.72 \text{ Å}$  for the smaller star and only  $\Delta\lambda_l = 0.068 \text{ Å}$  for the companion. From the sinusoidal shapes of the radial velocity curves, it is also apparent that the orbits are nearly circular.
- Calculate the mass ratio of the two stars.
  - Assuming that the inclination of the system is  $90^\circ$ , calculate the velocity in km/s and radius of the orbits in AU of the two stars.
  - Calculate the sum of the masses of the two stars in units of solar masses.
  - Calculate the masses of the two individual stars in units of solar masses.
- e) From the light curve (see the figure below) of the eclipsing spectroscopic binary in part (d), it is found that  $t_b - t_a = 11.7$  hours, and  $t_d - t_b = 164$  days. Calculate the radii of the two stars in units of solar radii.

[1 AU =  $1.50 \times 10^{11}$  m,  $M_\odot = 1.99 \times 10^{30}$  kg,  $R_\odot = 6.96 \times 10^8$  m,  $L_\odot = 3.85 \times 10^{26}$  W, 1 eV =  $1.60 \times 10^{-19}$  J]



**Fig: Eclipsing binary light curve**