Hierarchical Indexing

Up to this point we've been focused primarily on one-dimensional and two-dimensional data, stored in Pandas Series and DataFrame objects, respectively. Often it is useful to go beyond this and store higher-dimensional data—that is, data indexed by more than one or two keys. Early Pandas versions provided Panel and Panel4D objects that could be thought of as 3D or 4D analogs to the 2D DataFrame, but they were somewhat clunky to use in practice. A far more common pattern for handling higher-dimensional data is to make use of *hierarchical indexing* (also known as *multi-indexing*) to incorporate multiple index *levels* within a single index. In this way, higher-dimensional data can be compactly represented within the familiar one-dimensional Series and two-dimensional DataFrame objects. (If you're interested in true *N*-dimensional arrays with Pandas-style flexible indices, you can look into the excellent Xarray package (https://xarray.pydata.org/).)

In this chapter, we'll explore the direct creation of MultiIndex objects; considerations when indexing, slicing, and computing statistics across multiply indexed data; and useful routines for converting between simple and hierarchically indexed representations of data.

We begin with the standard imports:

```
In [1]: import pandas as pd
import numpy as np
```

A Multiply Indexed Series

Let's start by considering how we might represent two-dimensional data within a one-dimensional Series . For concreteness, we will consider a series of data where each point has a character and numerical key.

The Bad Way

Suppose you would like to track data about states from two different years. Using the Pandas tools we've already covered, you might be tempted to simply use Python tuples as keys:

```
Out[2]: (California, 2010) 37253956
(California, 2020) 39538223
(New York, 2010) 19378102
(New York, 2020) 20201249
(Texas, 2010) 25145561
(Texas, 2020) 29145505
dtype: int64
```

With this indexing scheme, you can straightforwardly index or slice the series based on this tuple index:

But the convenience ends there. For example, if you need to select all values from 2010, you'll need to do some messy (and potentially slow) munging to make it happen:

This produces the desired result, but is not as clean (or as efficient for large datasets) as the slicing syntax we've grown to love in Pandas.

The Better Way: The Pandas MultiIndex

Fortunately, Pandas provides a better way. Our tuple-based indexing is essentially a rudimentary multi-index, and the Pandas MultiIndex type gives us the types of operations we wish to have. We can create a multi-index from the tuples as follows:

```
In [5]: index = pd.MultiIndex.from_tuples(index)
```

The MultiIndex represents multiple *levels* of indexing—in this case, the state names and the years—as well as multiple *labels* for each data point which encode these levels.

If we reindex our series with this MultiIndex , we see the hierarchical representation of the data:

```
In [6]: pop = pop.reindex(index)
        pop
Out[6]: California
                     2010
                             37253956
                     2020
                             39538223
        New York
                     2010
                             19378102
                     2020
                             20201249
        Texas
                     2010
                             25145561
                             29145505
                     2020
        dtype: int64
```

Here the first two columns of the Series representation show the multiple index values, while the third column shows the data. Notice that some entries are missing in the first column: in this multi-index representation, any blank entry indicates the same value as the line above it.

Now to access all data for which the second index is 2020, we can use the Pandas slicing notation:

The result is a singly indexed Series with just the keys we're interested in. This syntax is much more convenient (and the operation is much more efficient!) than the home-spun tuple-based multi-indexing solution that we started with. We'll now further discuss this sort of indexing operation on hierarchically indexed data.

MultiIndex as Extra Dimension

dtype: int64

You might notice something else here: we could easily have stored the same data using a simple DataFrame with index and column labels. In fact, Pandas is built with this equivalence in mind. The unstack method will quickly convert a multiply indexed Series into a conventionally indexed DataFrame:

```
In [8]: pop_df = pop.unstack()
pop_df
```

Out[8]:

```
    2010
    2020

    California
    37253956
    39538223

    New York
    19378102
    20201249

    Texas
    25145561
    29145505
```

Naturally, the stack method provides the opposite operation:

```
In [9]:
        pop_df.stack()
Out[9]: California
                     2010
                              37253956
                     2020
                              39538223
        New York
                     2010
                              19378102
                     2020
                              20201249
        Texas
                     2010
                              25145561
                     2020
                              29145505
        dtype: int64
```

Seeing this, you might wonder why would we would bother with hierarchical indexing at all. The reason is simple: just as we were able to use multi-indexing to manipulate two-dimensional data within a one-dimensional Series , we can also use it to manipulate data of three or more dimensions in a Series or DataFrame . Each extra level in a multi-index represents an extra dimension of data; taking advantage of this property gives us much more flexibility in the types of data we can represent. Concretely, we might want to add another column of demographic data for each state at each year (say, population under 18); with a MultiIndex this is as easy as adding another column to the DataFrame :

Out[10]:

		total	under18
California	2010	37253956	9284094
California	2020	39538223	8898092
New York	2010	19378102	4318033
New fork	2020	20201249	4181528
Tayaa	2010	25145561	6879014
Texas	2020	29145505	7432474

In addition, all the ufuncs and other functionality discussed in <u>Operating on Data in Pandas (03.03-Operations-in-Pandas.ipynb)</u> work with hierarchical indices as well. Here we compute the fraction of people under 18 by year, given the above data:

This allows us to easily and quickly manipulate and explore even high-dimensional data.

Methods of MultiIndex Creation

The most straightforward way to construct a multiply indexed Series or DataFrame is to simply pass a list of two or more index arrays to the constructor. For example:

The work of creating the MultiIndex is done in the background.

Similarly, if you pass a dictionary with appropriate tuples as keys, Pandas will automatically recognize this and use a MultiIndex by default:

```
In [13]: data = {('California', 2010): 37253956,
                  ('California', 2020): 39538223,
                  ('New York', 2010): 19378102,
                  ('New York', 2020): 20201249,
                  ('Texas', 2010): 25145561,
                  ('Texas', 2020): 29145505}
         pd.Series(data)
Out[13]: California
                      2010
                              37253956
                      2020
                              39538223
         New York
                      2010
                              19378102
                      2020
                              20201249
         Texas
                      2010
                              25145561
                      2020
                              29145505
         dtype: int64
```

Nevertheless, it is sometimes useful to explicitly create a MultiIndex; we'll look at a couple of methods for doing this next.

Explicit MultiIndex Constructors

For more flexibility in how the index is constructed, you can instead use the constructor methods available in the pd.MultiIndex class. For example, as we did before, you can construct a MultiIndex from a simple list of arrays giving the index values within each level:

Or you can construct it from a list of tuples giving the multiple index values of each point:

You can even construct it from a Cartesian product of single indices:

Similarly, you can construct a MultiIndex directly using its internal encoding by passing levels (a list of lists containing available index values for each level) and codes (a list of lists that reference these labels):

Any of these objects can be passed as the index argument when creating a Series or DataFrame, or be passed to the reindex method of an existing Series or DataFrame.

MultiIndex Level Names

Sometimes it is convenient to name the levels of the MultiIndex. This can be accomplished by passing the names argument to any of the previously discussed MultiIndex constructors, or by setting the names attribute of the index after the fact:

```
In [18]: pop.index.names = ['state', 'year']
         pop
Out[18]: state
                      year
         California
                      2010
                              37253956
                      2020
                              39538223
         New York
                      2010
                              19378102
                              20201249
                      2020
         Texas
                      2010
                              25145561
                      2020
                              29145505
         dtype: int64
```

With more involved datasets, this can be a useful way to keep track of the meaning of various index values.

MultiIndex for Columns

In a DataFrame, the rows and columns are completely symmetric, and just as the rows can have multiple levels of indices, the columns can have multiple levels as well. Consider the following, which is a mock-up of some (somewhat realistic) medical data:

Out[19]:

	subject		Bob		Guido		Sue
	type	HR	Temp	HR	Temp	HR	Temp
year	visit						
2013	1	30.0	38.0	56.0	38.3	45.0	35.8
	2	47.0	37.1	27.0	36.0	37.0	36.4
2014	1	51.0	35.9	24.0	36.7	32.0	36.2
	2	49.0	36.3	48.0	39.2	31.0	35.7

This is fundamentally four-dimensional data, where the dimensions are the subject, the measurement type, the year, and the visit number. With this in place we can, for example, index the top-level column by the person's name and get a full <code>DataFrame</code> containing just that person's information:

```
In [20]: health_data['Guido']
Out[20]: type HR Temp
```

		r) po	••••	·omp
	year	visit		
2013	1	56.0	38.3	
	2	27.0	36.0	
2014	1	24.0	36.7	
	2	48.0	39.2	

Indexing and Slicing a MultiIndex

Indexing and slicing on a MultiIndex is designed to be intuitive, and it helps if you think about the indices as added dimensions. We'll first look at indexing multiply indexed Series, and then multiply indexed DataFrame objects.

Multiply Indexed Series

Consider the multiply indexed Series of state populations we saw earlier:

```
In [21]:
         pop
Out[21]: state
                      year
         California
                      2010
                               37253956
                      2020
                               39538223
         New York
                      2010
                               19378102
                      2020
                               20201249
          Texas
                      2010
                               25145561
                      2020
                               29145505
          dtype: int64
```

We can access single elements by indexing with multiple terms:

```
In [22]: pop['California', 2010]
```

Out[22]: 37253956

The MultiIndex also supports *partial indexing*, or indexing just one of the levels in the index. The result is another Series , with the lower-level indices maintained:

Partial slicing is available as well, as long as the MultiIndex is sorted (see the discussion in <u>Sorted and Unsorted Indices</u>):

In [24]: pop.loc['California':'New York']

Out[24]: state year

California 2010 37253956 2020 39538223

New York 2010 19378102

2020 20201249

dtype: int64

With sorted indices, partial indexing can be performed on lower levels by passing an empty slice in the first index:

In [25]: pop[:, 2010]

Out[25]: state

California 37253956 New York 19378102 Texas 25145561

dtype: int64

Other types of indexing and selection (discussed in <u>Data Indexing and Selection (03.02-Data-Indexing-and-Selection.ipynb)</u>) work as well; for example, selection based on Boolean masks:

In [26]: pop[pop > 22000000]

Out[26]: state year

California 2010 37253956 2020 39538223 Texas 2010 25145561

2020 29145505

dtype: int64

Selection based on fancy indexing also works:

In [27]: pop[['California', 'Texas']]

Out[27]: state year

California 2010 37253956 2020 39538223 Texas 2010 25145561 2020 29145505

dtype: int64

Multiply Indexed DataFrames

A multiply indexed DataFrame behaves in a similar manner. Consider our toy medical DataFrame from before:

In [28]: health_data Out[28]: Guido Sue subject **Bob** type HR Temp HR Temp HR Temp visit year 1 30.0 38.0 56.0 38.3 45.0 35.8 2013 **2** 47.0 37.1 27.0 36.0 37.0 36.4 1 51.0 35.9 24.0 36.7 32.0 36.2 2014 2 49.0 36.3 48.0 39.2 31.0 35.7

Remember that columns are primary in a DataFrame, and the syntax used for multiply indexed Series applies to the columns. For example, we can recover Guido's heart rate data with a simple operation:

In [29]: health_data['Guido', 'HR'] Out[29]: year visit 2013 1 56.0 2 27.0 2014 1 24.0 48.0 2 Name: (Guido, HR), dtype: float64

Also, as with the single-index case, we can use the loc, iloc, and ix indexers introduced in <u>Data Indexing and Selection (03.02-Data-Indexing-and-Selection.ipynb)</u>. For example:

2 47.0

37.1

These indexers provide an array-like view of the underlying two-dimensional data, but each individual index in loc or iloc can be passed a tuple of multiple indices. For example:

Working with slices within these index tuples is not especially convenient; trying to create a slice within a tuple will lead to a syntax error:

You could get around this by building the desired slice explicitly using Python's built-in slice function, but a better way in this context is to use an IndexSlice object, which Pandas provides for precisely this situation. For example:

As you can see, there are many ways to interact with data in multiply indexed Series and DataFrame s, and as with many tools in this book the best way to become familiar with them is to try them out!

Rearranging Multi-Indexes

24.0 32.0

1 51.0

2014

One of the keys to working with multiply indexed data is knowing how to effectively transform the data. There are a number of operations that will preserve all the information in the dataset, but rearrange it for the purposes of various computations. We saw a brief example of this in the stack and unstack methods, but there are many more ways to finely control the rearrangement of data between hierarchical indices and columns, and we'll explore them here.

Sorted and Unsorted Indices

Earlier I briefly mentioned a caveat, but I should emphasize it more here. *Many of the MultiIndex slicing operations will fail if the index is not sorted.* Let's take a closer look.

We'll start by creating some simple multiply indexed data where the indices are *not lexographically sorted*:

```
In [34]:
         index = pd.MultiIndex.from_product([['a', 'c', 'b'], [1, 2]])
         data = pd.Series(np.random.rand(6), index=index)
         data.index.names = ['char', 'int']
         data
Out[34]: char
               int
                       0.280341
               1
               2
                       0.097290
               1
                       0.206217
         C
                2
                       0.431771
         b
               1
                       0.100183
                       0.015851
         dtype: float64
```

If we try to take a partial slice of this index, it will result in an error:

```
In [35]: try:
          data['a':'b']
except KeyError as e:
          print("KeyError", e)
```

KeyError 'Key length (1) was greater than MultiIndex lexsort depth (0)'

Although it is not entirely clear from the error message, this is the result of the MultiIndex not being sorted. For various reasons, partial slices and other similar operations require the levels in the MultiIndex to be in sorted (i.e., lexographical) order. Pandas provides a number of convenience routines to perform this type of sorting, such as the sort_index and sortlevel methods of the DataFrame . We'll use the simplest, sort index , here:

```
In [36]:
         data = data.sort index()
         data
Out[36]: char
                int
                       0.280341
                1
                2
                       0.097290
                       0.100183
          b
                1
                2
                       0.015851
          c
                1
                       0.206217
                       0.431771
          dtype: float64
```

With the index sorted in this way, partial slicing will work as expected:

Stacking and Unstacking Indices

As we saw briefly before, it is possible to convert a dataset from a stacked multi-index to a simple two-dimensional representation, optionally specifying the level to use:

```
In [38]:
          pop.unstack(level=0)
Out[38]:
           state California New York
                                       Texas
           year
           2010
                 37253956 19378102 25145561
           2020
                 39538223 20201249 29145505
In [39]:
          pop.unstack(level=1)
Out[39]:
               year
                        2010
                                  2020
               state
           California 37253956 39538223
           New York 19378102 20201249
              Texas 25145561 29145505
```

The opposite of unstack is stack, which here can be used to recover the original series:

```
In [40]:
         pop.unstack().stack()
Out[40]:
         state
                      year
          California
                               37253956
                      2010
                      2020
                               39538223
         New York
                      2010
                               19378102
                      2020
                               20201249
          Texas
                      2010
                               25145561
                      2020
                               29145505
          dtype: int64
```

Index Setting and Resetting

Another way to rearrange hierarchical data is to turn the index labels into columns; this can be accomplished with the reset_index method. Calling this on the population dictionary will result in a DataFrame with state and year columns holding the information that was formerly in the index. For clarity, we can optionally specify the name of the data for the column representation:

Out[41]:

	state	year	population
0	California	2010	37253956
1	California	2020	39538223
2	New York	2010	19378102
3	New York	2020	20201249
4	Texas	2010	25145561
5	Texas	2020	29145505

A common pattern is to build a MultiIndex from the column values. This can be done with the set_index method of the DataFrame, which returns a multiply indexed DataFrame:

Out[42]:

population

state	year	
California	2010	37253956
	2020	39538223
New York	2010	19378102
	2020	20201249
Texas	2010	25145561
	2020	29145505

In practice, this type of reindexing is one of the more useful patterns when exploring real-world datasets.