

1. IMPLEMENTATION OF 8-PUZZLE

```
import numpy as np
import heapq

class PuzzleState:
    def __init__(self, board, moves=0):
        self.board = board
        self.blank_pos = self.find_blank(board)
        self.moves = moves

    def find_blank(self, board):
        return tuple(map(tuple, np.where(board == 0)))

    def get_neighbors(self):
        neighbors = []
        x, y = self.blank_pos
        directions = [(-1, 0), (1, 0), (0, -1), (0, 1)] # Up, Down, Left, Right

        for dx, dy in directions:
            nx, ny = x + dx, y + dy
            if 0 <= nx < 3 and 0 <= ny < 3:
                new_board = self.board.copy()
                new_board[x, y], new_board[nx, ny] = new_board[nx, ny], new_board[x, y]
                neighbors.append(PuzzleState(new_board, self.moves + 1))
        return neighbors

    def is_goal(self):
        return np.array_equal(self.board, np.array([[1, 2, 3], [4, 5, 6], [7, 8, 0]]))

    def heuristic(self):
        return np.sum(np.abs(np.argmax(self.board) - np.argmax(np.array([[1, 2, 3], [4, 5, 6], [7, 8, 0]]).flatten())))

    def __lt__(self, other):
        return (self.moves + self.heuristic()) < (other.moves + other.heuristic())

def a_star_solver(initial_board):
    initial_state = PuzzleState(initial_board)
    open_set = []
    heapq.heappush(open_set, initial_state)
    visited = set()

    while open_set:
        current = heapq.heappop(open_set)
```

```
if current.is_goal():
    return current.moves

visited.add(tuple(map(tuple, current.board)))

for neighbor in current.get_neighbors():
    if tuple(map(tuple, neighbor.board)) not in visited:
        heapq.heappush(open_set, neighbor)

return -1 # No solution found

if __name__ == "__main__":
    # Initial configuration (0 represents the blank space)
    initial_board = np.array([[1, 2, 3],
                             [4, 0, 5],
                             [7, 8, 6]])

    result = a_star_solver(initial_board)
    if result != -1:
        print(f"Solved in {result} moves!")
    else:
        print("No solution exists.")
```

8/10/24
Tuesday

Lab 2

(10)

③ Solve 8 puzzle problems, Implement Iterative Deepening Search algorithms.

1 Initialization:

- Represent the puzzle as a 3×3 grid with 0 as the empty space.
- Define the goal state where tiles are ordered from 1 to 8 with 0 in the bottom-right corner.
- Define valid moves for the empty space: up, down, left, right.

2 Check Goal:

- Compare the current puzzle state with the goal state.

3 Get Empty Position:

- Location the position of the empty space (0).

4 Move the Empty Space:

- Try moving the empty space in all directions and generate new valid states.

5 Depth - Limited Search (DLS):

- Explore states up to a given depth limit.
- If the goal isn't reached with the limit backtrace and try new paths.

6 Iterative Deepening Search (IDS)

- Start with depth 0 and incrementally increase the depth limit.

- Perform DLS for each limit until the goal state is found.

7 Print Solution:

- Once the goal is found, print the sequence of steps reaching from

the initial state to the Goal State

output:

Solution found in 14 steps.

Steps to reach the goal:

Step 0:

9 1 2 3

Step 3:

1, 2, 3
4, 0, 5
6, 7, 8

1, 2, 3
4, 5, 0
6, 7, 8

1, 2, 3
4, 5, 8
6, 0, 7

Step 4:

Step 5:

Step 6:

1, 2, 3
4, 5, 8
0, 6, 7

1, 2, 3
0, 5, 8
4, 6, 7

1, 2, 3
5, 0, 8
4, 6, 7

Step 6:

Step 7:

Step 8:

1, 2, 3
5, 0, 8
4, 6, 7

1, 2, 3
5, 6, 8
4, 6, 7

1, 2, 3
5, 6, 8
4, 7, 0

Step 9:

Step 10:

Step 11:

1, 2, 3
5, 6, 0
4, 7, 8

1, 2, 3
5, 0, 6
4, 7, 8

1, 2, 3
0, 5, 6
4, 7, 8

Step 12:

Step 13:

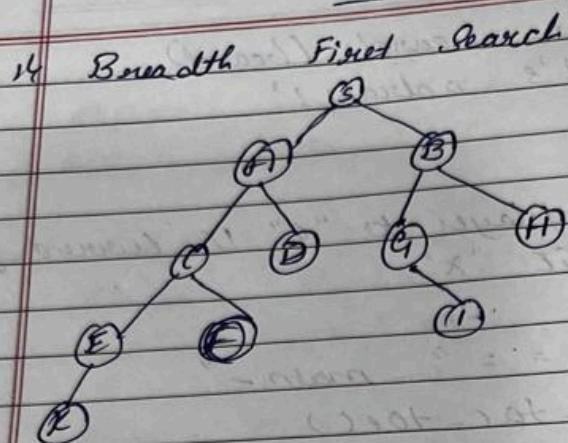
Step 14:

1, 2, 3
4, 5, 6
0, 7, 8

1, 2, 3
4, 5, 6
7, 0, 8

1, 2, 3
4, 5, 6
7, 8, 0

Lab - 2



Frontier:

$S \leftarrow [S]$

$A \leftarrow [A | B | C]$

$B \leftarrow [B | C | D | G]$

$C \leftarrow [C | D | G | H]$

$D \leftarrow [D | G | H | E]$

$E \leftarrow [G | H | E | F]$

$F \leftarrow [H | E | F | I]$

$G \leftarrow [E | F | I]$

$H \leftarrow [F | I | K]$

Explored:

$[S]$

$[S | A]$

$[S | A | B]$

$[S | A | B | C | D]$

$[S | A | B | C | D | G]$

$[S | A | B | C | D | G | H]$

$[S | A | B | C | D | G | H]$

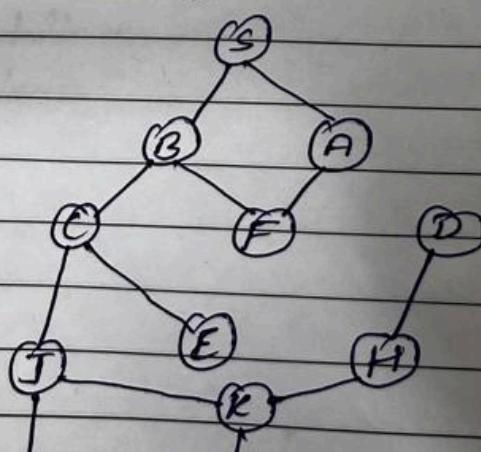
$[S | A | B | C | D | G | H | K]$

Output:

$S \rightarrow A \rightarrow B \rightarrow C \rightarrow D \rightarrow G \rightarrow H \rightarrow K$

②

Perform DFS



Frontier

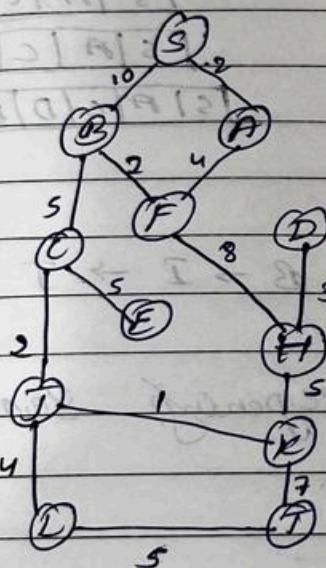
[S]
[B A]
[B F]
[B H]
[B D K]
[B D J I]

Explorred:

[S]
[S A]
[S F]
[B D H]
[B D H K]

output: S → B → F → H → K → T

③ Perform uniform cost search.

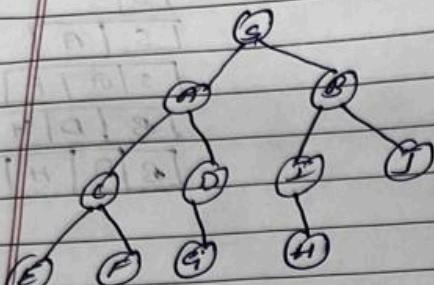


S(0)	A(2)	B(10)	F(6)	H(14)	C(15)
E(19)	D(17)	J(17)	E(20)	L(21)	T(26)

S(0)	A(2)	F(6)	I(10)	H(14)	C(15)
T(17)	E(19)	T(26)			

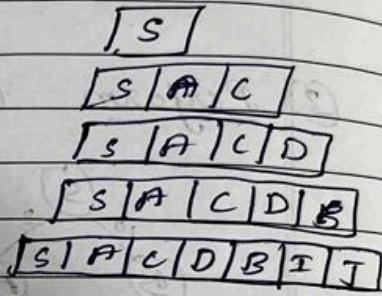
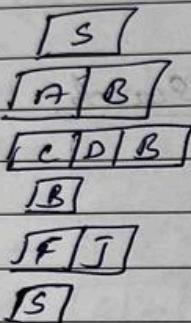
$$S \rightarrow A \rightarrow F \rightarrow H \rightarrow K \rightarrow T = \\ 2 + 4 + 8 + 5 + 7 = 26$$

④ Depth Limited Search



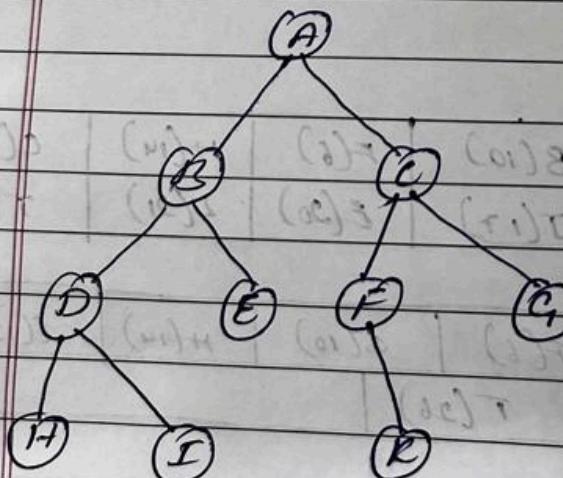
Frontier

Explored:



S → A → C → D → B → I → J

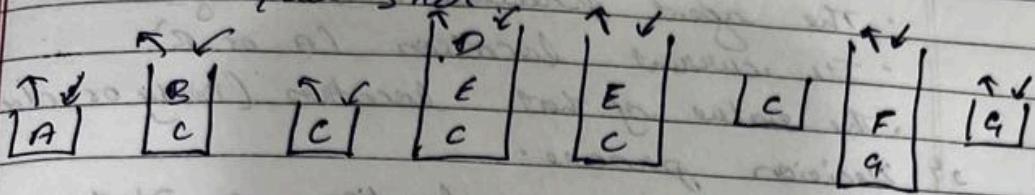
⑤ Perform iterative Deepening Search



Iterative 0: $A \rightarrow$ if we not goal state:
 $\rho_0 \rightarrow$ level 1

Iterative 1: $A \rightarrow B \rightarrow C$ do not goal state:
 $\rho_0 \rightarrow$ level 2

Iterative 2: $A \rightarrow B \rightarrow C \rightarrow D \rightarrow E \rightarrow F \rightarrow G \rightarrow$
goal state



O/P: $A \rightarrow B \rightarrow D \rightarrow E \rightarrow C \rightarrow F \rightarrow G$

