

2 sum
 array = [5, 2, 11, 7, 15] tar = 9
 return [1, 3]

① BF
 all pairs \rightarrow sum = tar
 for (i=0 to n) ↑
 first = arr[i]
 for (j=i+1 to n) ↑
 second = arr[j]
 sum = first + second
 if (sum = tar) ↑
 return arr
 y y y
 $O(n^2)$

② Better
 sorting $\rightarrow O(n \log n)$
 [2 5 7 11 15]
 ↑ ↑
 smallest largest
 sum = smallest + largest = 17
 17 > 9
 largest --
 [2 5 7 11 15]
 ↑ ↑
 smallest largest
 sum = 2 + 11 = 13
 13 > 9
 largest --
 [2 5 7 11 15]
 ↑ ↑
 smallest largest
 sum = 2 + 7 = 9
 target $\rightarrow O(n)$
 Total TC: $O(n \log n)$

③ Optimized
 hashing
 arr = [5 2 11 7 15]
 tar = 9
 pair sum = first + second = tar
 5 2 11 7 15 element | id
 ↑ 5 0
 first
 second = 9 - 5 = 4
 4 not there
 5 2 11 7 15 element | id
 ↑ 5 0
 first 2 1
 second = 7
 store 2 in um
 5 2 11 7 15 element | id
 ↑ 5 0
 first 2 1
 11 2
 second = -2
 store 11 in um
 5 2 11 7 15 element | id
 ↑ 5 0
 first 2 1
 11 2
 second = 2
 2 exists in um
 make pair of 2 ka index
 and 2 ka index
 that is your result

Pseudo code

unordered_map <i, i> m
 for (i=0 to n) ↑ $\leftarrow TC = O(n)$
 first = arr[i]
 sec = tar - first
 if (m.find(sec) != m.end()) ↑
 return [i, m[sec]]
 y
 m[first] = i;
 Key Value
 y

we consider that
 find function takes
 constant time for
 practical solutions

TC: $O(n)$