

3 Sum

nums = [-1, 0, 1, 2, -1, -4]

we need to find

a, b, c where

$$a + b + c = 0$$

$$-1 + 0 + 1 = 0 \text{ (triplet)}$$

$$2 + -1 + -1 = 0$$

we need to find unique triplets

$$i \neq j \neq k$$

should not be the same

number must be at three different indices

① Brute force

find all possible combinations

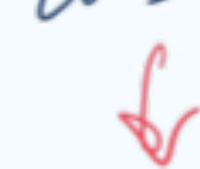
```
for (i = 0 to n) ↑
```

```
  for (j = i + 1 to n) ↑
```

```
    for (k = j + 1 to n) ↑
```

```
      if (a + b + c == 0) ↑
```

as store



will store in set

not in unordered because

we want it to be

sorted even though if

there are duplicates

we know all the

permutations since it'll

be the same after being

sorted

TC: $O(n^3 \times \log(\text{unique triplets}))$

because we use set

② Better (Hashing)

$$a + b + c = 0$$

$$a = -(b + c) = \text{target}$$

```
for (i = 0 to n) ↑
```

```
  tar = -nums[i]
```

```
  set<int> s;
```

```
  for (j = i + 1 to n) ↑
```

```
    tofind = tar - nums[j]
```

```
    if (s.find(tofind) != s.end()) ↑
```

found

y

```
    s.insert(nums[j])
```

y

y

TC: $O(n^2 \times \log(\text{unique triplets}))$

③ Optimized (2 pointer approach)

① nums \Rightarrow sort

[-4, -1, -1, 0, 1, 2]

[-4 | -1 | -1 | 0 | 1 | 2]

↑ ↑

↑

$$\text{sum} = -4 + (-1) + 2 = -3 \uparrow$$

we need to increase sum

so j++

[-4 | -1 | -1 | 0 | 1 | 2]

↑

↑

↑

j \neq k so we need to increase i now

```
for (i = 0 to n) ↑
```

```
  if (i > 0 && nums[i] == nums[i - 1]) (continue; // to avoid repeated values in sorted array)
```

```
  j = i + 1, k = n - 1
```

```
  while (j < k) ↑
```

```
    sum = nums[i] + nums[j] + nums[k]
```

```
    if (sum < 0)
```

```
      j++
```

```
    else if (sum > 0)
```

```
      k--
```

```
    else ↑
```

```
      nums[i], nums[j], nums[k] → ans
```

```
      while (j < k && nums[j] == nums[j + 1])
```

```
        j++
```

// to avoid repeated values

y

y

y

TC: $O(n \log n + n^2)$