

- ▶ Jonathan Dushoff, McMaster University

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Tessa Wessels, Faces on a Train

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Outline

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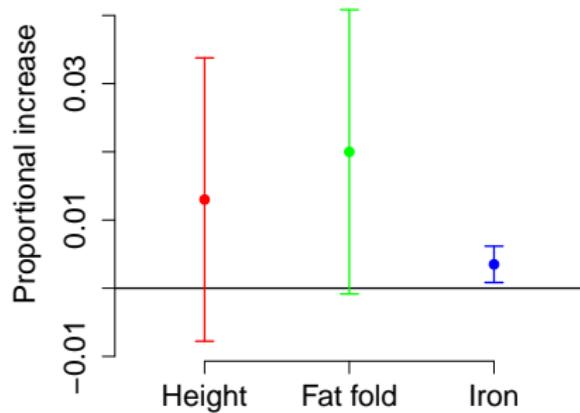
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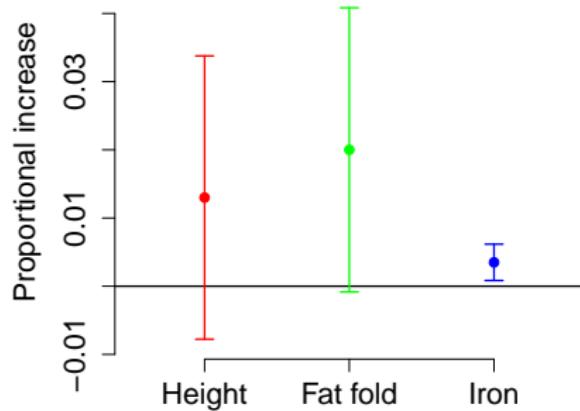
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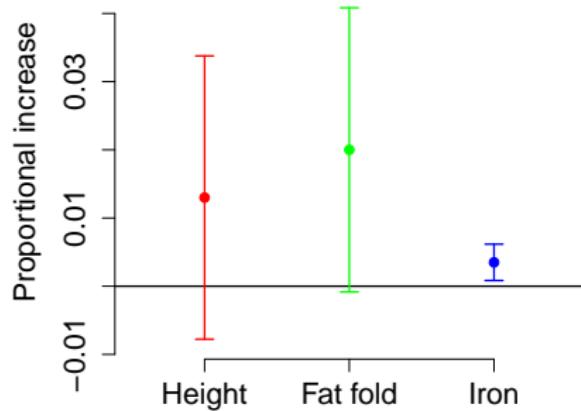
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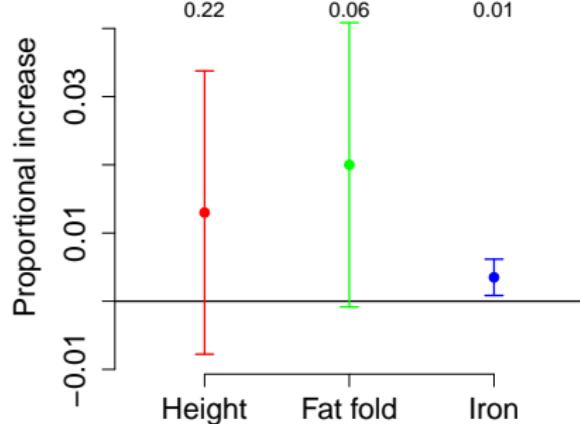
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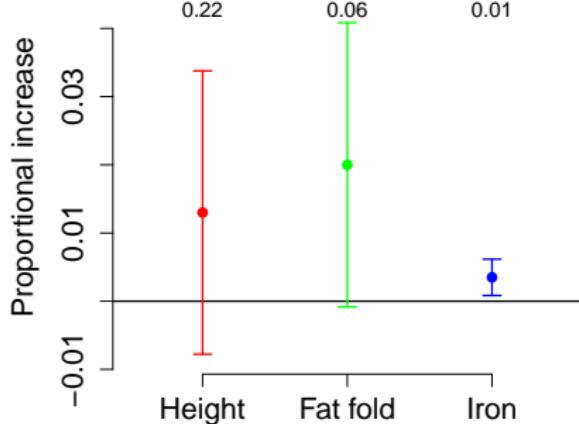
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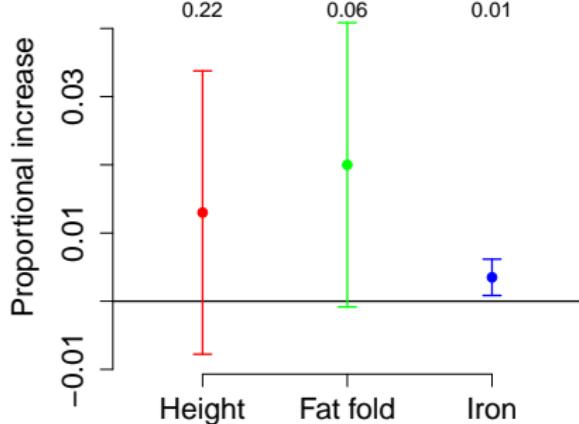
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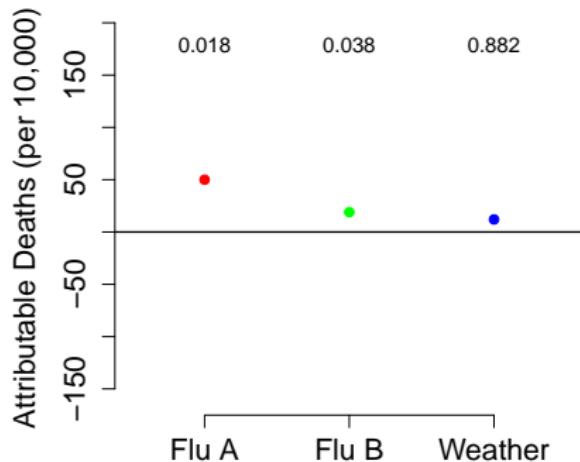
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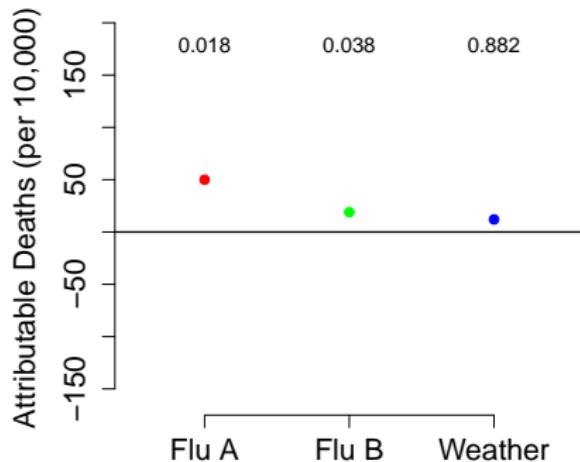
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Annualized flu deaths



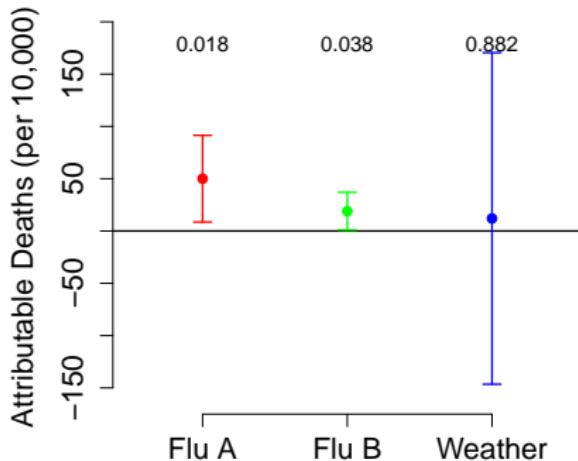
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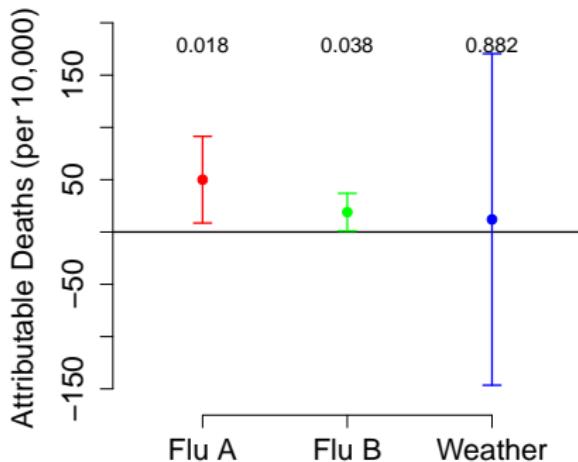
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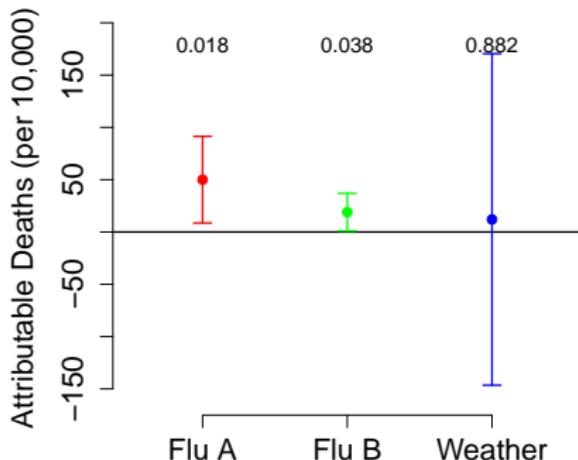
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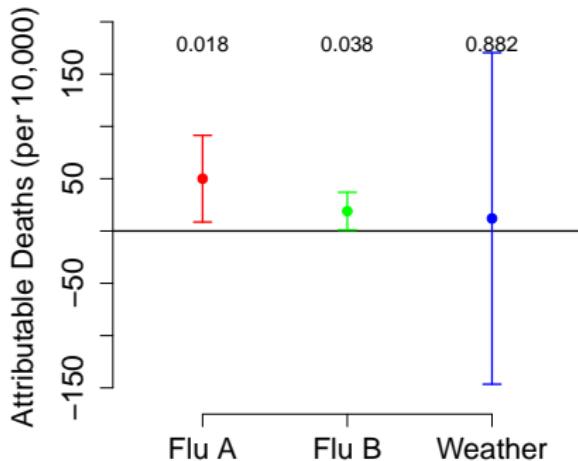
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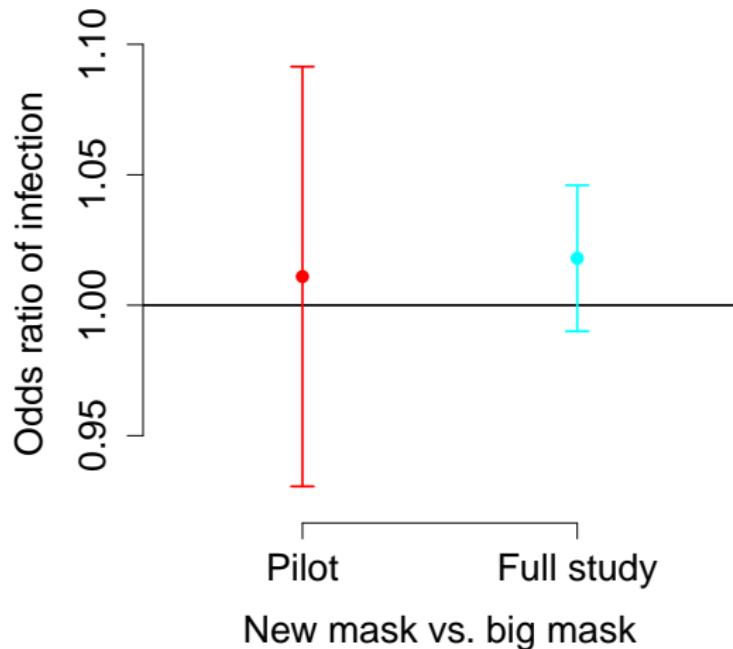
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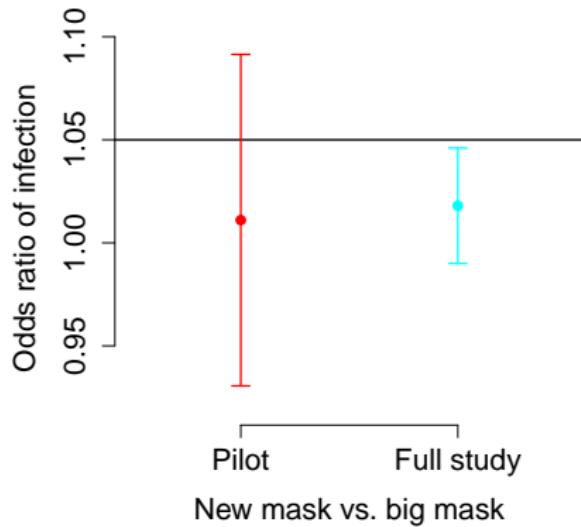
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Study results

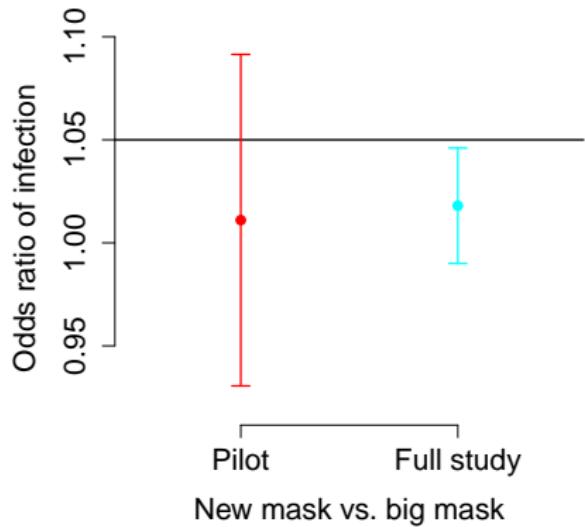


Non-inferiority trial



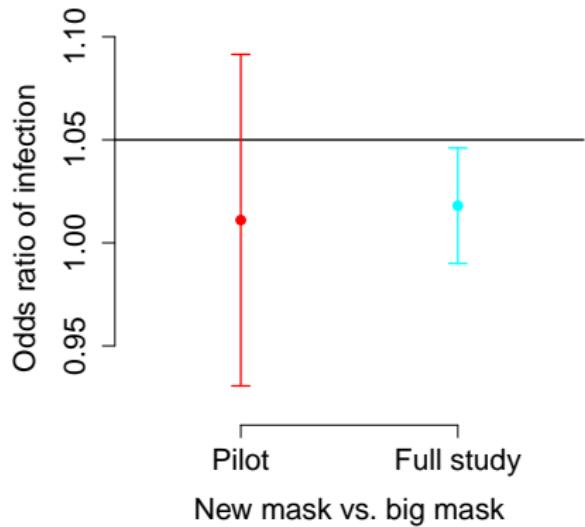
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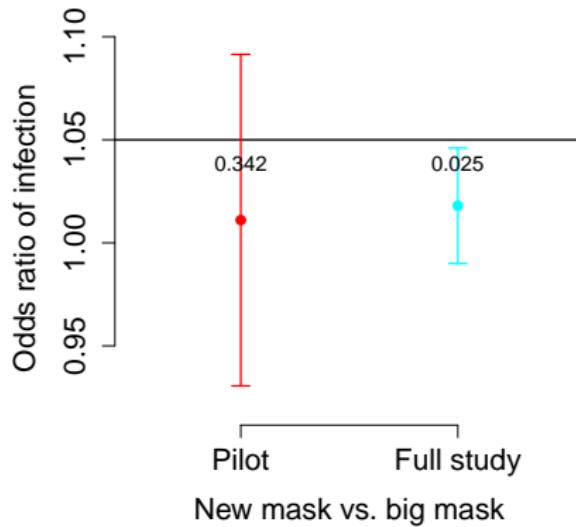
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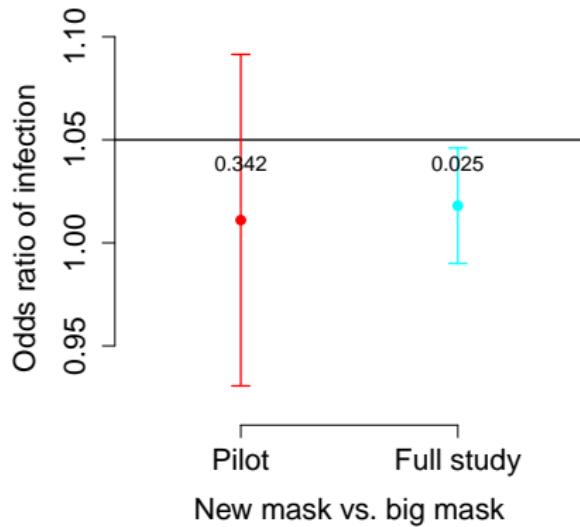
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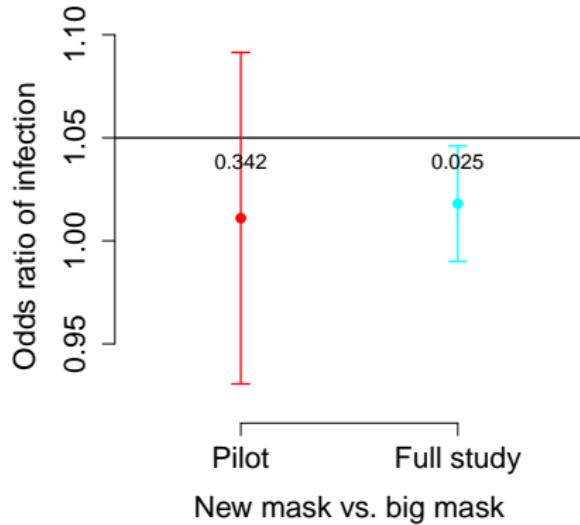
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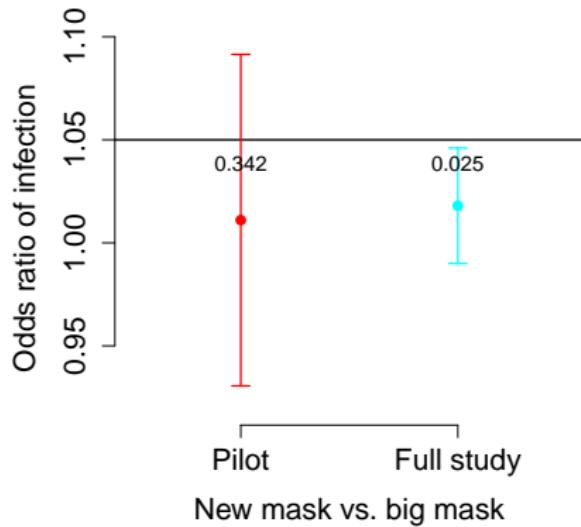
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 - ▶ The difference between the observed effect and the standard we chose

Outline

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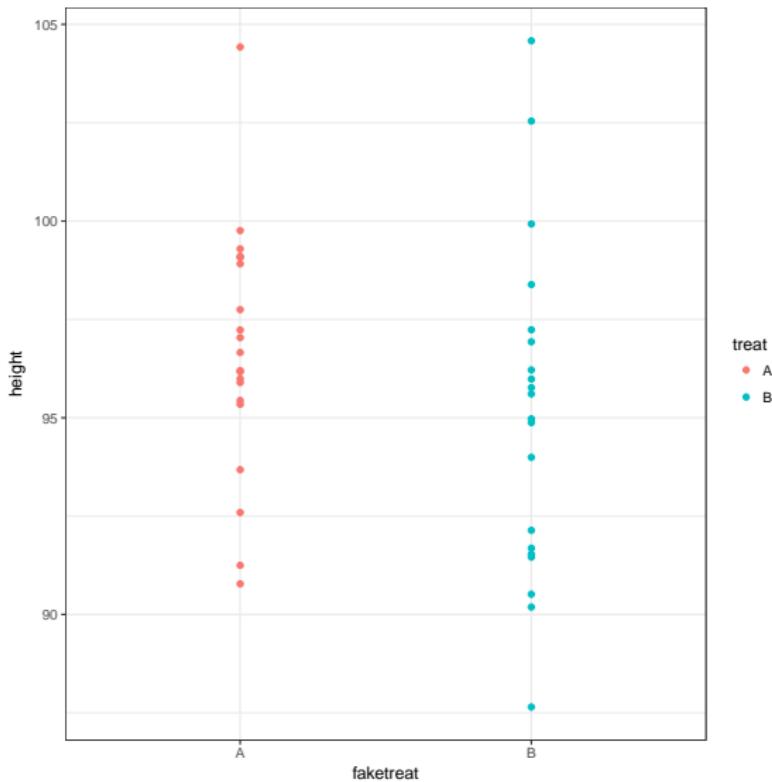
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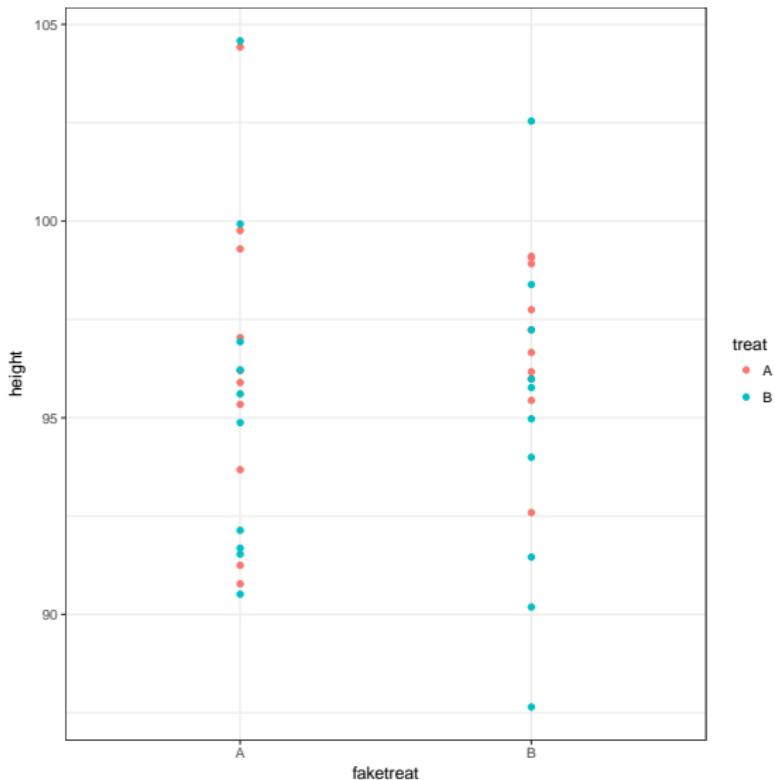
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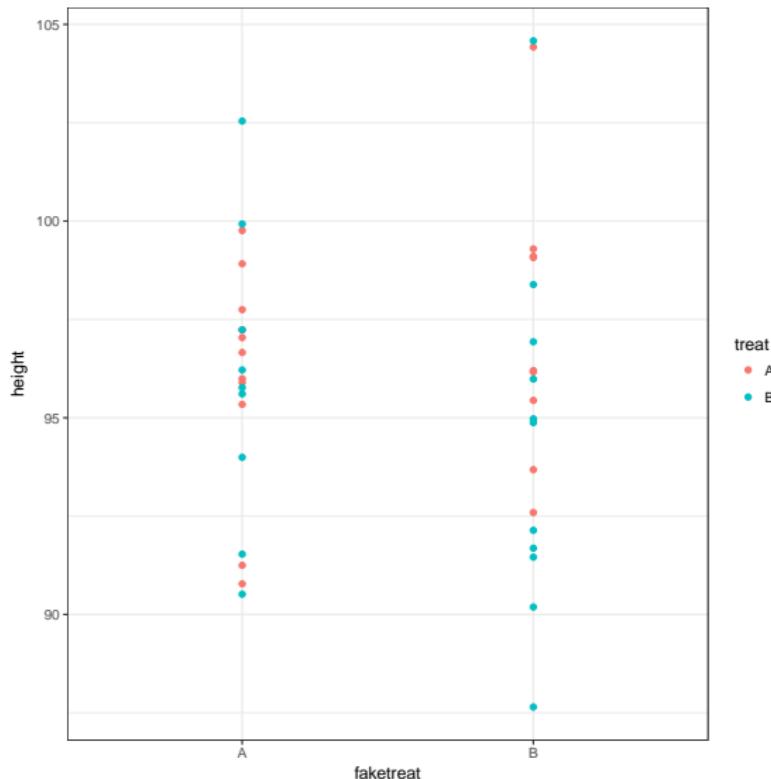
Height measurements



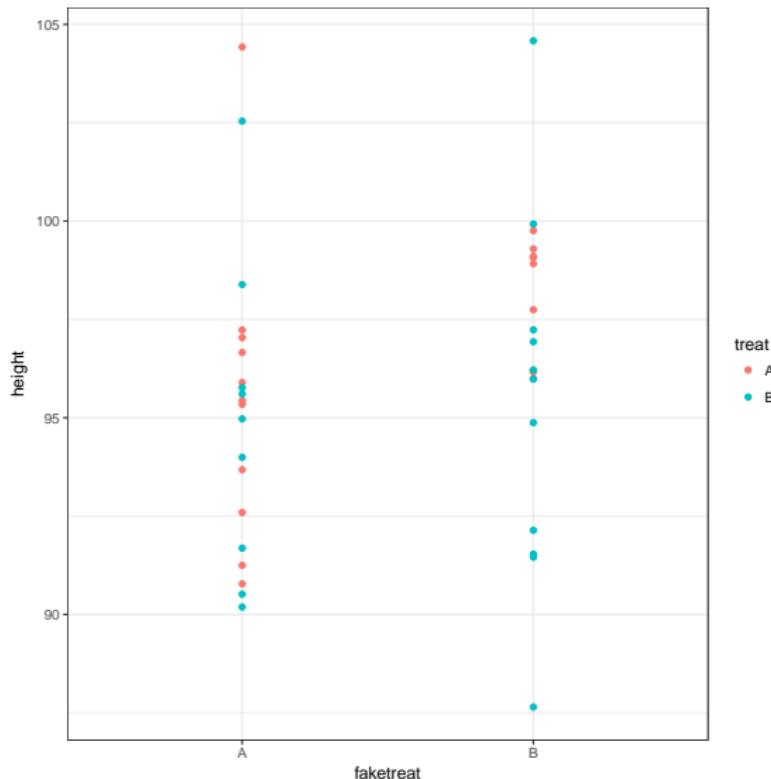
Scrambled measurements



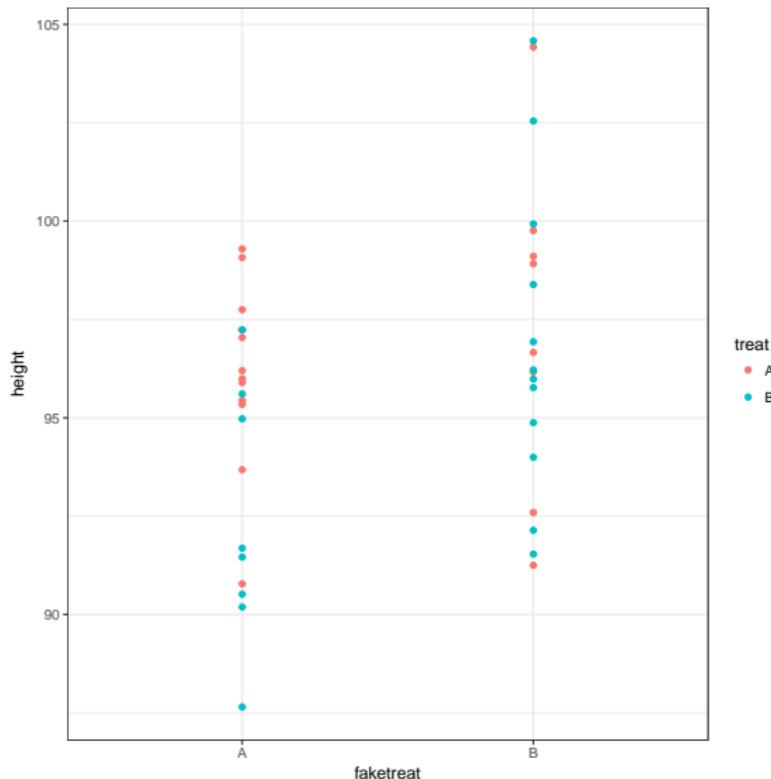
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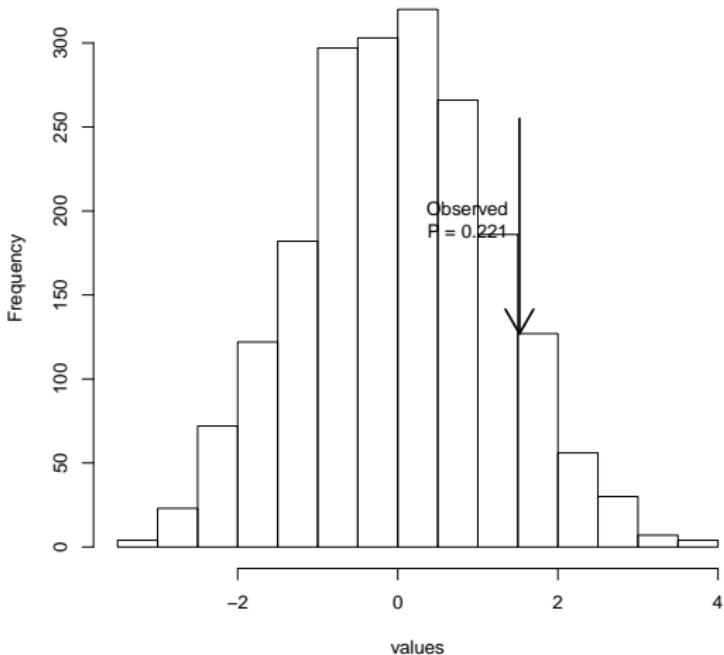
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The null distribution



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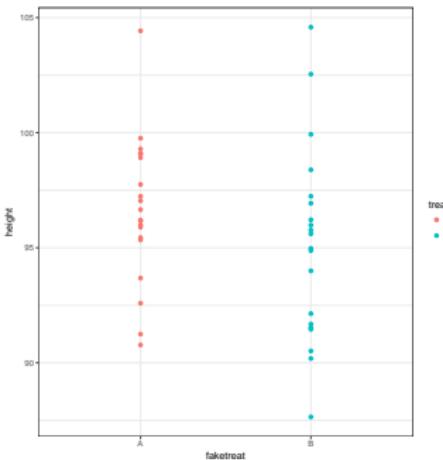
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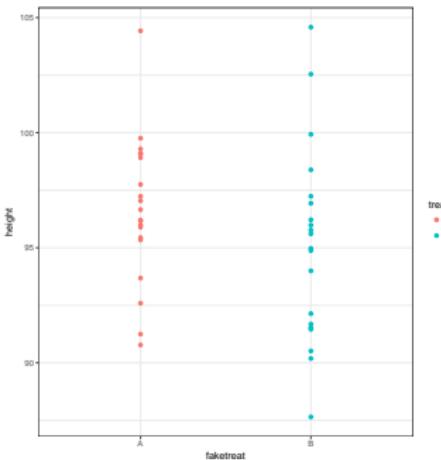
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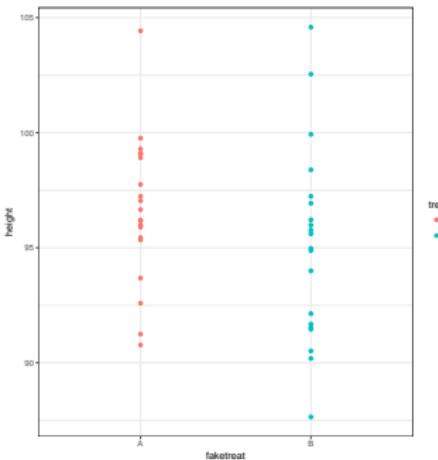
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Cape Town weather

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Tessa Wessels, Faces on a Train

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