

Model evaluation and comparison

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MMED 2019

► Discuss model types and model goals

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- ► Discuss the value of simulation for validating models

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 - Put the Goodness of fit test in its place

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Outline

Conceptual models

Prediction

Model Validation

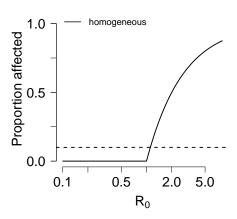
Model Evaluation
Goodness of fit
Capturing patterns
Going beyond

Conclusion

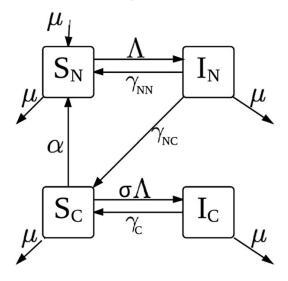


Disease thresholds

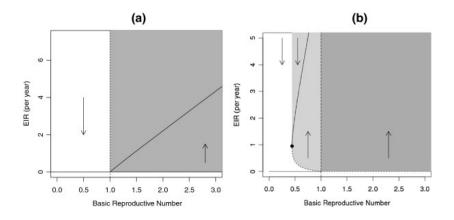
endemic equilibrium



Effects of clinical immunity



Bistability



Outline

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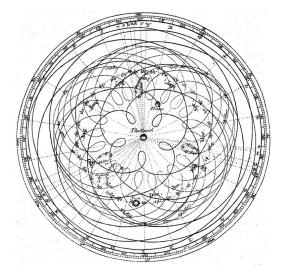
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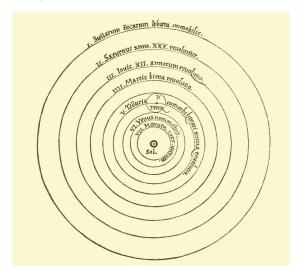
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Ptolemy v. Copernicus

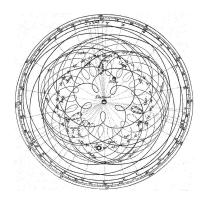


Ptolemy v. Copernicus

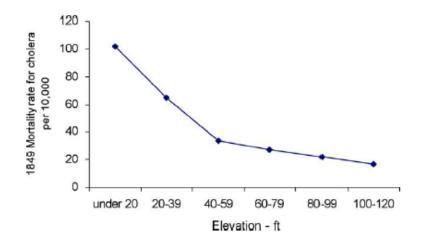


Ptolemy v. Copernicus





Where will we see cholera cases?



12/51

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Model Validation

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- Precision

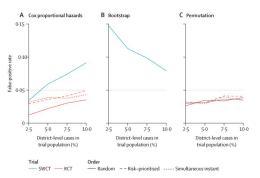
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- ► Bias?

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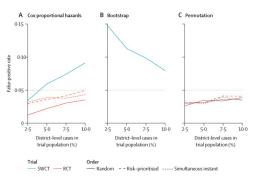
16/51

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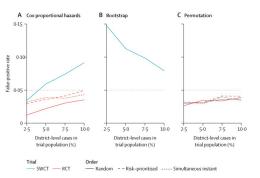
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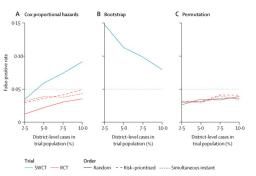
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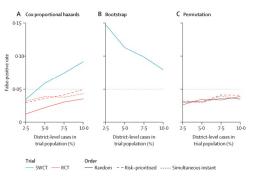
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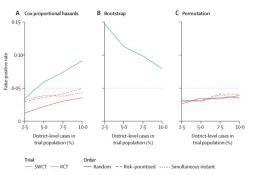
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▶ Does your model match the real world?



Does your model match the real world?

•



- Does your model match the real world?
 - ► * No!



- Does your model match the real world?
 - ➤ * No!
- How well does your model match the real world?



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 - ➤ * No!
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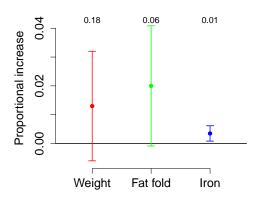


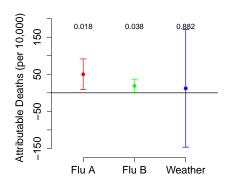
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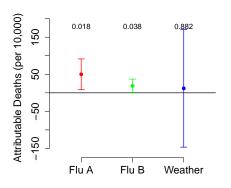


Vitamin study

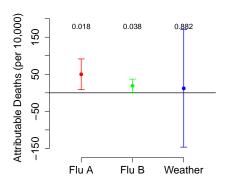




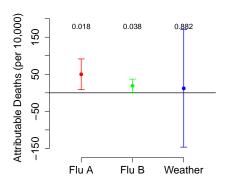
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Low P values



High P values



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► Does your model make predictions *outside* the range on which you calibrated it?

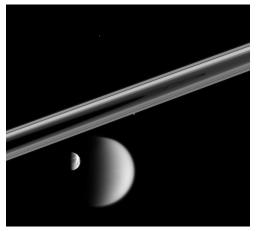
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Predicting way out of sample



Essentially, all models are wrong, but some are useful.

- Box and Draper (1987), Empirical Model Building ...



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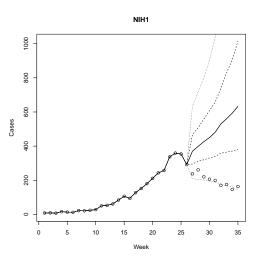


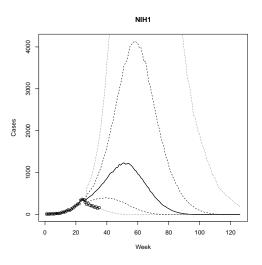
► How well can you do? Which details are important?

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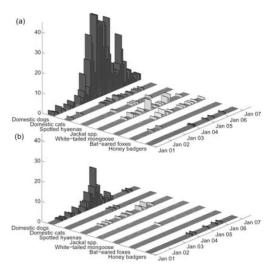




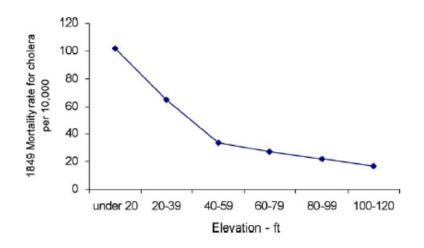
Generating hypotheses



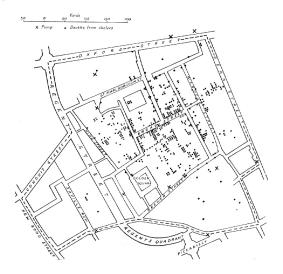
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Testing hypotheses



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Hard questions



Answers are not always easy

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Dynamic models

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