APPROACH for Minimum Enclosing Circle:

- Input: image containing only single white object, and black background
- For the purpose of finding count and locating the objects, the code from HW1 was used.

```
# CODE FROM HW1 TO FIND AND LABEL THE OBJECTS

def code_from_hw1(image):
    """

Input:
    image: Binary color 2d image matrix.

Output:
    count: the number of objects detected.
    obj_id: a 2d map indicating which pixel belongs to which object.
    0 indicated, its a black pixel
    i in {1,2,3,...,count} denotes that the pixel belongs to object i."""
```

• Firstly, just for the sake of fast convergence, the center is initialized to the center of the **bounding box** found using ((minx+maxx)/2, (miny+maxy)/2). Furthermore, the bounding box was found using the following function.

```
def min bounding box(image):
    Input:
        image: Binary color 2d image matrix. Should consist
       of only one object comprising of white pixels.
   Output:
       min x, max x, min y, max y:
            the 4 required parameters for unique bounding box.
   m,n = image.shape
   min x,min y = image.shape
   max_x, max_y = 0,0
   for x in range(m):
        for y in range(n):
            if image[x,y]==1:
                min x = min(x, min_x)
                min y = min(y, min y)
                max_x = max(x, max_x)
                max_y = max(y, max_y)
   return min_x, max_x, min_y, max_y
```

For a given center, the radius is calculated by finding the furthest white pixel belonging
to the object followed by its distance from the center. The code has been optimized by
only considering the points within the bounding box for finding the max distance or the
radius.

- We use the BFS algorithm to traverse through the neighboring pixels of this center, to search for a smaller possible circle.
- We initialize a gueue with ((minx+maxx)/2, (miny+maxy)/2, radius).
- For visited markings, we just use a copy of the image, and mark the visited white pixels as black.
- Consider the pseudocode below for the traversal.
- While (queue is not empty):
 - \circ x,y,r = pop an element from the queue
 - o If unvisited white neighbor pixel (x1,y1) exist at top/bottom/left/right:
 - Set that pixel (x1,y1) as visited
 - Calculate the radius r1 considering x1,y1 as the center
 - If r1<r:
 - Add this pixel for review to the queue (x1,y1,r1)
- This way, we traverse over possible small circles, and find the one having minimum radius, since a circle having minimum area would be the circle having minimum radius.
- Moreover, the jaccard similarity (Q2) is computed using the following function.

```
def jaccard score(mask1, mask2):
    Input:
        mask1 and mask2 are the two binary
        image masks consisting of white
        and black pixels only.
    Output:
        The computed jaccard similarity
        between the two masks passed as
       the input.
    m,n = mask1.shape
    intersect = 0
    union = 0
    for i in range(m):
        for j in range(n):
            if mask1[i,j]==1 and mask2[i,j]==1:
                intersect+=1
            if mask1[i,j]==1 or mask2[i,j]==1:
                union+=1
    return intersect/union
```

CODE: (To be run as python <code_file_path> <image_path>)

Library Imports

```
import cv2
import numpy as np
import math
import sys
from collections import deque
```

• Module Functions

```
# CODE FROM HW1 TO FIND AND LABEL THE OBJECTS

def code_from_hw1(image):
    """
    Input:
    image: Binary color 2d image matrix.
```

```
Output:
       count: the number of objects detected.
       obj_id: a 2d map indicating which pixel belongs to which object.
            0 indicated, its a black pixel
                i in {1,2,3,...,count} denotes that the pixel belongs to
object i.
   # accumulator to count objects
   count = 0
   # dimensions of the image
   m,n = image.shape
   # object id array
   obj id = np.zeros((m,n))
   # iterate through the pixels
   for a in range(m):
       for b in range(n):
            # if unvisited white pixel found
            if image[a,b]==1:
                # increment the counter to denote new object
                count+=1
                # find all neighboring white pixels and mark
                # them as visited by setting them to black
                queue = deque(((a,b),))
                image[a,b]=0
                obj id[a,b]=count
                # similar to BFS technique
                while len(queue)>0:
                    i,j = queue.popleft()
                    if i>0 and image[i-1,j]==1:
                        image[i-1,j]=0
```

```
obj id[i-1,j]=count
                        queue.append((i-1,j))
                    if j>0 and image[i,j-1]==1:
                        image[i,j-1]=0
                        obj id[i,j-1]=count
                        queue.append((i,j-1))
                    if i<m-1 and image[i+1,j]==1:</pre>
                        image[i+1,j]=0
                        obj id[i+1,j]=count
                        queue.append((i+1,j))
                    if j< n-1 and image[i,j+1]==1:
                        image[i,j+1]=0
                        obj id[i,j+1]=count
                        queue.append((i,j+1))
    # return the final count and object id matrix
    return count, obj id
def calc radius(image, min x, max x, min y, max y, x, y):
    Input:
        image: Binary color 2d image matrix.
        min_x, max_x, min_y, max_y: from the bounding box (for computation
optimization)
         x, y: current center of the circle for which radius needs to be
calculated
    Output:
        r: the distance of the given center from the furthest
            white pixel within the specified bounding box.
    r = 0
    for i in range(min x, max x+1):
       for j in range(min_y, max_y+1):
            if image[i,j]==1:
                dist = math.sqrt((i-x)**2 + (j-y)**2)
```

```
r = max(r, dist)
   return r
def min bounding box(image):
   Input:
       image: Binary color 2d image matrix. Should consist
       of only one object comprising of white pixels.
   Output:
       min x, max x, min y, max y:
            the 4 required parameters for unique bounding box.
   m,n = image.shape
   min x, min y = image.shape
   max x, max y = 0,0
   for x in range(m):
       for y in range(n):
            if image[x,y]==1:
                min_x = min(x, min_x)
                min y = min(y, min y)
                max_x = max(x, max_x)
                \max y = \max(y, \max y)
   return min x, max x, min y, max y
def min enclosing circle(image):
   Input:
       image: Binary color 2d image matrix. Should consist
       of only one object comprising of white pixels.
   Output:
       x,y,r: The center coordinates and the radius for the
            calculated minimum enclosing circle.
```

```
# to ensure original image is not lost
image = image.copy()
m,n = image.shape
# original copy (will use 'image' as visited array for BFS)
img = image.copy()
# finding the bounding box
min x, max x, min y, max y = min bounding box(image)
x = (\min x + \max x) //2
y = (\min y + \max y) //2
r = math.sqrt( (max x-min x)**2 + (max y-min y)**2 )//2
queue = deque([(x,y,r),])
image[x,y]=0
# similar to BFS technique
while len(queue)>0:
    i,j,r_cur = queue.popleft()
    if r cur<r:</pre>
        r = r cur
        x = i
        y = j
    if i>0 and image[i-1,j]==1:
        image[i-1,j]=0
        r nxt = calc radius(img, min x, max x, min y, max y, i-1, j)
        if r nxt<r cur:</pre>
            queue.append((i-1,j,r nxt))
    if j>0 and image[i,j-1]==1:
        image[i,j-1]=0
        r_nxt = calc_radius(img, min_x, max_x, min_y, max_y, i, j-1)
        if r nxt<r cur:</pre>
            queue.append((i,j-1,r nxt))
    if i<m-1 and image[i+1,j]==1:</pre>
```

```
image[i+1,j]=0
            r_nxt = calc_radius(img, min_x, max_x, min_y, max_y, i+1, j)
            if r nxt<r cur:</pre>
                queue.append((i+1,j,r_nxt))
        if j<n-1 and image[i,j+1]==1:</pre>
            image[i,j+1]=0
            r nxt = calc radius(img, min_x, max_x, min_y, max_y, i, j+1)
            if r nxt<r cur:</pre>
                queue.append((i,j+1,r nxt))
    return x,y,r
def jaccard score(mask1, mask2):
    Input:
       mask1 and mask2 are the two binary
        image masks consisting of white
        and black pixels only.
    Output:
        The computed jaccard similarity
        between the two masks passed as
        the input.
    m,n = mask1.shape
    intersect = 0
    union = 0
    for i in range(m):
        for j in range(n):
            if mask1[i,j]==1 and mask2[i,j]==1:
                intersect+=1
            if mask1[i,j]==1 or mask2[i,j]==1:
                union+=1
    return intersect/union
```

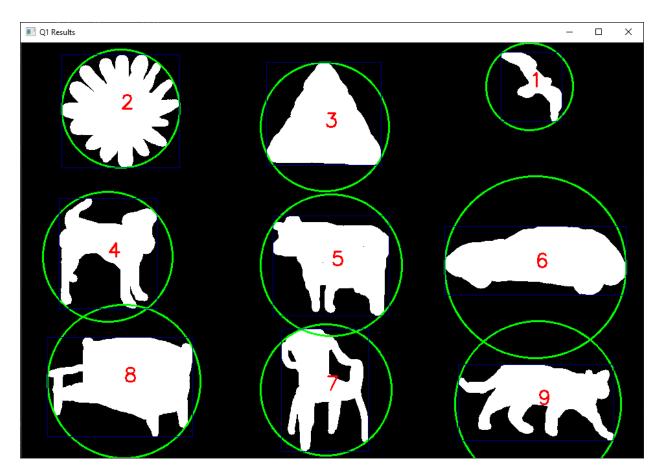
• The Main Driving Code

```
if name ==" main ":
    # input the image to np array
   image = cv2.imread(sys.argv[1], cv2.IMREAD GRAYSCALE)
   # threshold to convert to binary image
   image[image<128] = 0
   image[image>=128] = 1
   # get the objects
   count, object id = code from hw1(image.copy())
   boxes = []
   circles = []
   for i in range(1,count+1):
        img = np.zeros(image.shape)
        # image containing only object 'i'
        img[object id==i] = 1
        # get minimum bounding boxes
       box = min bounding box(img)
       boxes.append(box)
        # get minimum enclosing circles
        circle = min enclosing circle(img)
        circles.append(circle)
        # get circle mask for jackard similarity
       circle mask = np.zeros(image.shape)
       min_x, max_x, min_y, max_y = box
       x c, y c, r = circle
        for x in range(min_x, max_x+1):
            for y in range(min y, max y+1):
                within circle = (((x-x c)**2 + (y-y c)**2) \le r*r)
                if within circle:
                    circle mask[x,y] = 1
        # calculate jaccard similarity
```

```
jaccard = jaccard score(img, circle mask)
       # print the results
                     print(f"Center:({x_c},{y_c}), Radius:{r}, Jaccard
Score:{jaccard}")
   # read a color instance of the image
   img = cv2.imread(sys.argv[1])
   # add the enclosing circles to the image
   for i in range(count):
       x,y,r = circles[i]
       x=int(x)
       y=int(y)
       r=int(r)
       img = cv2.circle(img, (y,x), r, (0,255,0), 2)
   # add the enclosing boxes to the image
   for i in range(count):
       x1,x2,y1,y2 = boxes[i]
       img = cv2.rectangle(img, (y1, x1), (y2, x2), (150,0,0), 1)
   # add text to identify object by id
   for i in range(count):
       x,y,r = circles[i]
       x=int(x)
       y=int(y)
       img = cv2.putText(img, str(1+i), (y, x), cv2.FONT HERSHEY SIMPLEX,
1, (0,0,255), 2)
   # display the results
   cv2.imshow('Q1 Results', img)
   cv2.waitKey(0)
```

RESULTS:

Q1: Enclosing Circles Visualized



Centers and Radii of Enclosing Circles and Q2:Jaccard Similarities

1.	Center: (67,784), Score: 0.3383947939262473	Radius: 67.00746227100382,	Jaccard
2.	Center: (101,153), Score: 0.7409113593612039	Radius:91.7877987534291,	Jaccard
3.	Center: (129,468), Score: 0.6591141129348936	Radius:99.84988733093293,	Jaccard
4.	Center: (329,133), Score: 0.5165750258984779	Radius:100.4987562112089,	Jaccard
5.	Center: (342,478), Score: 0.6300254452926208	Radius:109.04127658827184,	Jaccard

Center: (345,793), Radius:140.1748907615055, Jaccard Score:0.6999006066422182
 Center: (534,470), Radius:101.04454463255303, Jaccard Score:0.5296036535638559
 Center: (521,158), Radius:118.6086000254619, Jaccard Score:0.647756371174247
 Center: (556,797), Radius:128.16005617976296, Jaccard Score:0.5391245743473326