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KUNWAR DUSHYANT SINGH EE22BTECH11031

Question 12.13.3.17

Bag I contains 3 black and 2 white balls, Bag II contains 2 black and 4 white balls. A bag and a ball is selected at random. Determine the probability of selecting a black ball.

Solution:

Random variable	Value	Definition
X	0	Bag 1
	1	Bag 2
Y	0	White ball
	1	Black ball

TABLE I DISTRIBUTION

Probablity of chosing Bag

$$Pr(X = 0) = \frac{1}{2}$$
 (1)
 $Pr(X = 1) = \frac{1}{2}$ (2)

$$\Pr(X = 1) = \frac{1}{2} \tag{2}$$

(3)

Conditional Probabilty,

$$\Pr(Y = 1 | X = 0) = \frac{3}{5} \tag{4}$$

$$\Pr(Y = 1|X = 1) = \frac{1}{3} \tag{5}$$

(6)

Probablity of black balls

$$Pr(Y = 1) = Pr(Y = 1|X = 0) Pr(X = 0)$$
 (7)

+
$$Pr(Y = 1|X = 1) Pr(X = 1)$$
 (8)

$$\Pr(Y=1) = \frac{3}{10} + \frac{1}{6} \tag{9}$$

$$=\frac{7}{15}\tag{10}$$