

# Norwegian University of Science and Technology

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## **Assignment Title**

Assignment 2

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Using the A\* Algorithm

## **Course**

TDT4136 Introduction to Artificial Intelligence

## **Semester**

FALL 2018

## **Date Submitted**

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## **Submitted by**

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## Part 1: Grids with Obstacles

### 1.1

I wrote the algorithm and rest of the application by myself. I used the A\*-wikipedia-page (pseudo code) as inspiration for the algorithm: [https://en.wikipedia.org/wiki/A\\*\\_search\\_algorithm](https://en.wikipedia.org/wiki/A*_search_algorithm).

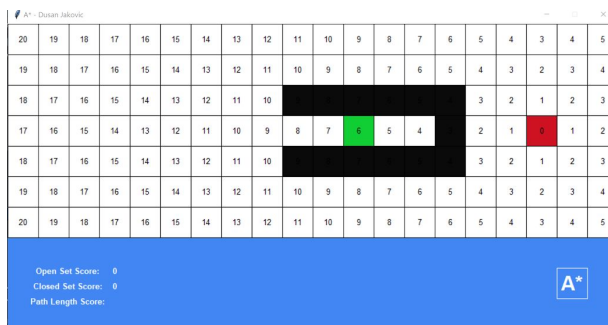
I used the graphics.py library to make the program visual.

The source code can be found under “Source Code: Part 1” at the last pages

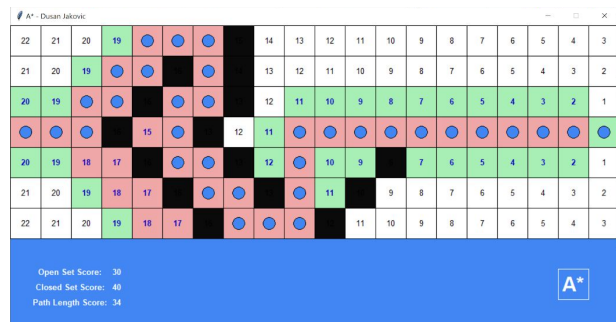
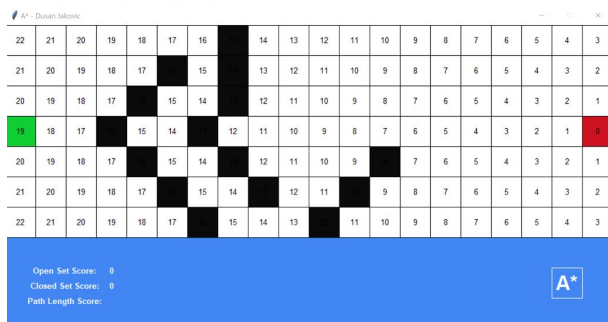
### 1.2

All the cells have a value in them, which represent the h-value of the cell. The green cell is the start and the red one is the end/goal. When the program runs, the cells which are in the open set will be represented with a lighter shade of green, while the cells in the closed set will be represented with a lighter red. A blue dot without fill will represent the cell that is currently visited/evaluated. When the algorithm executes, the path will be drawn by a dots. If the path isn't found, the program will return a message that the path couldn't be reached.

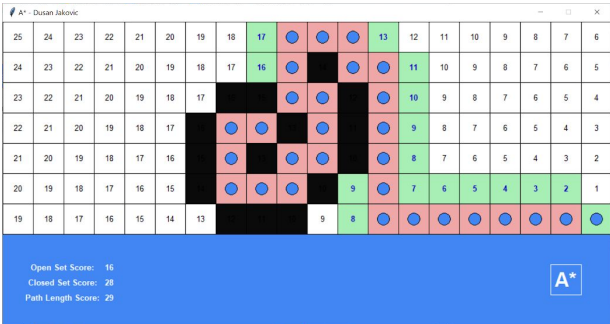
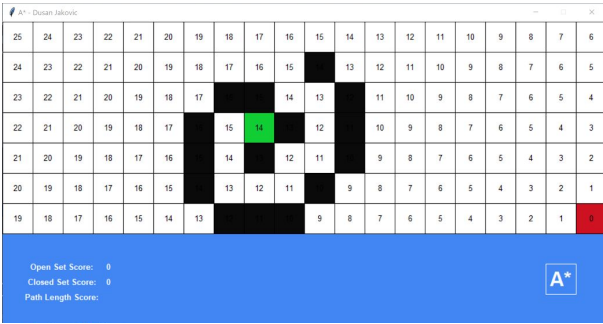
#### board-1-1



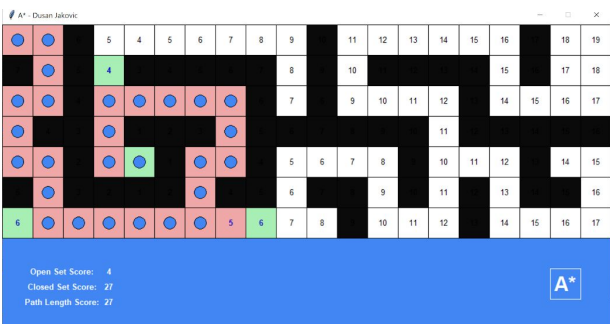
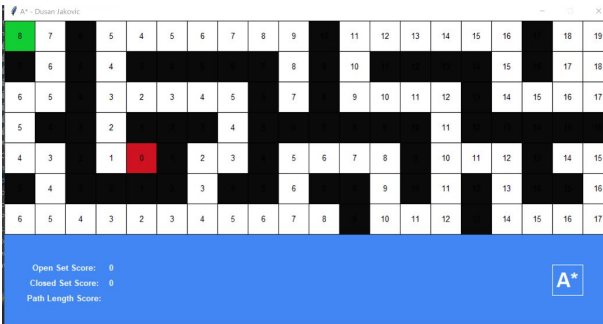
#### board-1-2



board-1-3



board-1-4



## Part 2: Grids with Different cell Costs

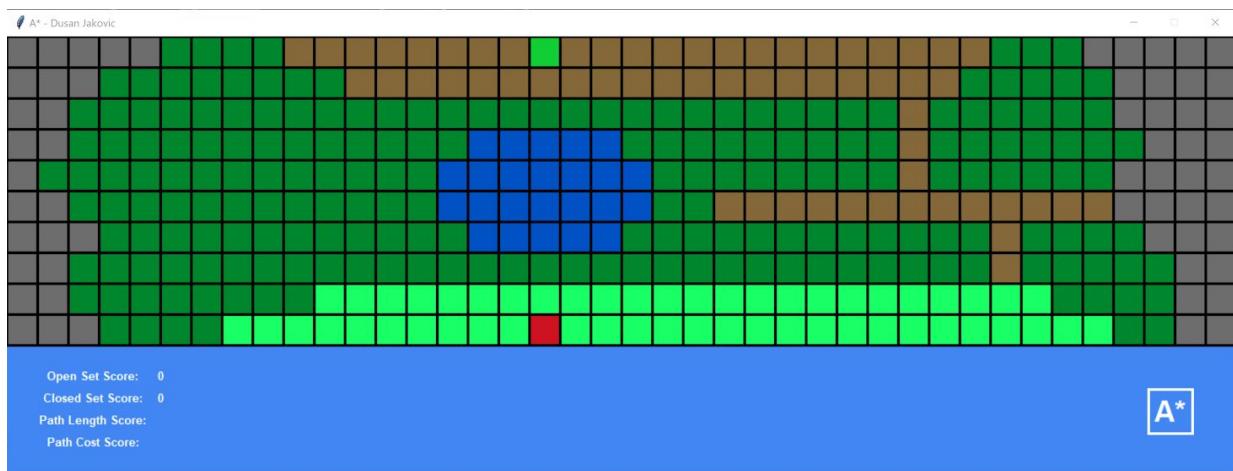
### 2.1

The visual part is slightly changed to make it a bit more visible: the open set and closed set are represented with red and green outline, instead of fill...I also added a “Path Cost Score”, which is the total cost of the path - considering the cost of each cell.

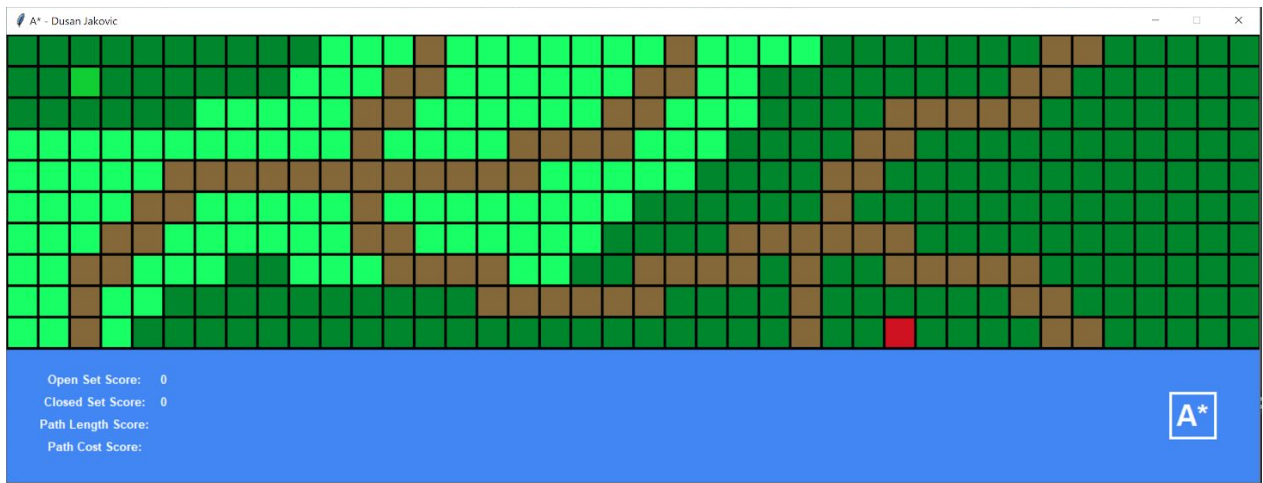
The source code can be found under “Source Code: Part 2” at the last pages

### 2.2

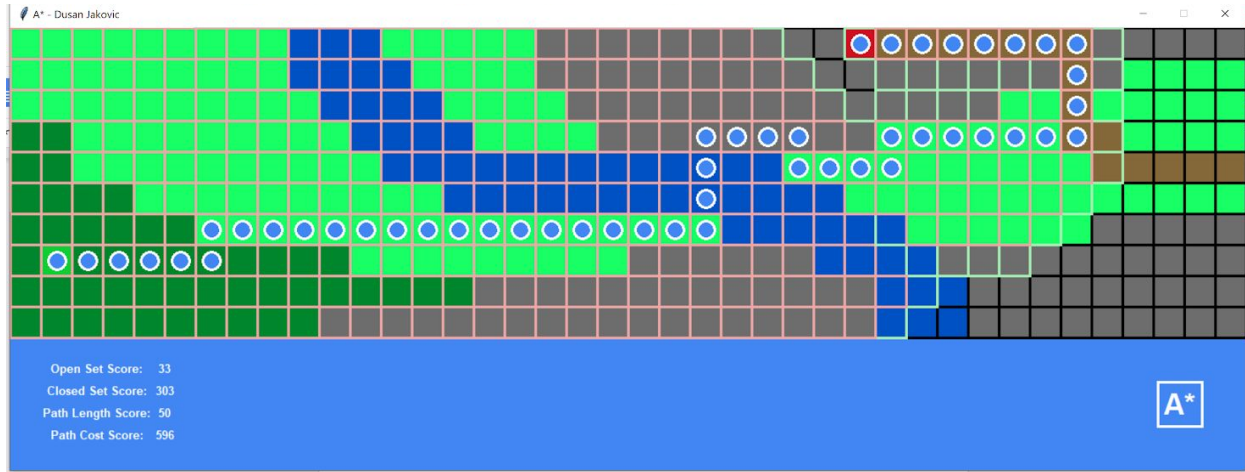
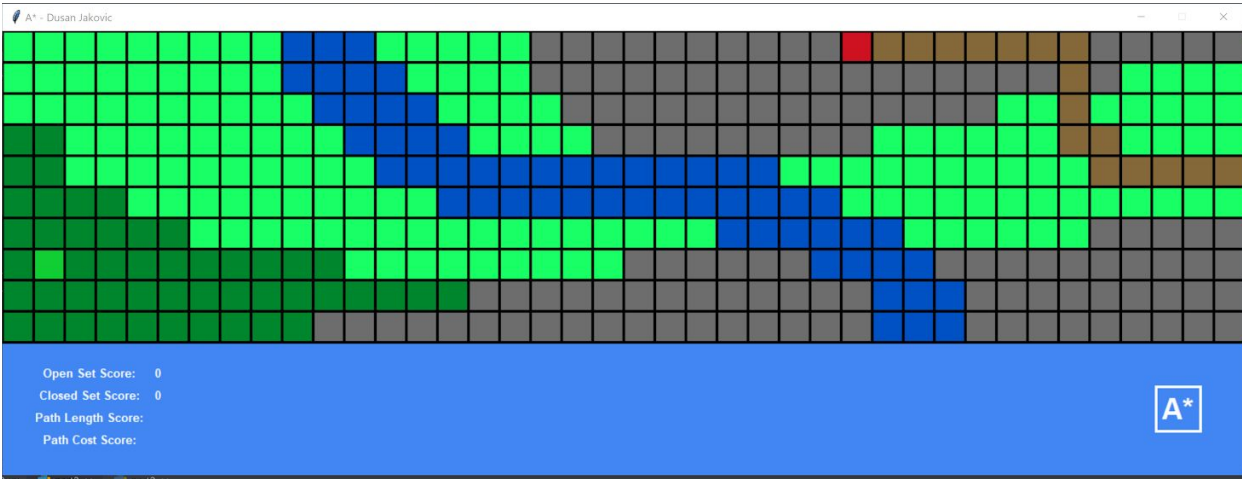
#### board-2-1



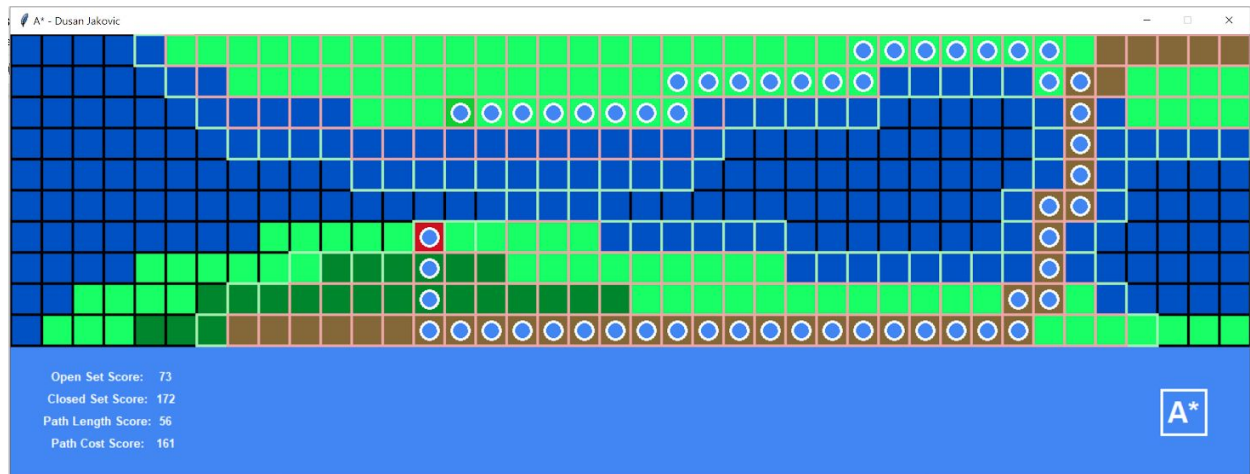
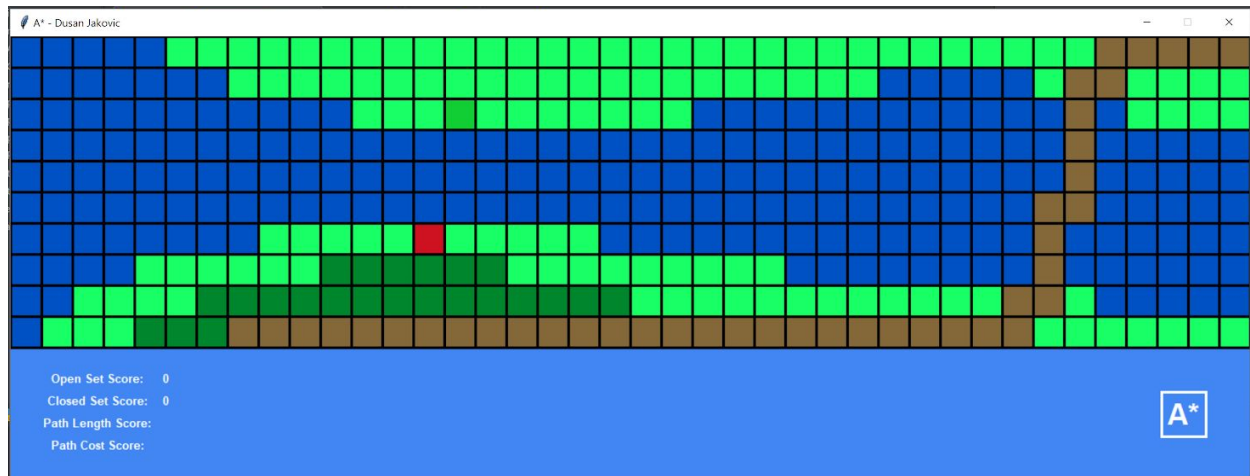
board-2-2



board-2-3



## board-2-4





## Part 3: Comparison with BFS and Dijkstra's Algorithm

### 3.1

The visual part of the program is the same as in the previous part (part 2). I consider this sufficient enough for an answer to 3.1.

The source code can be found in the the zipped folder “code”

File: part2 (The code for BFS and Dijkstra is commented out)

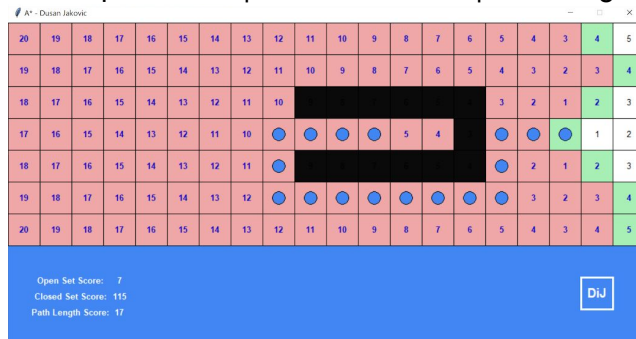
### 3.2

#### board-1-1

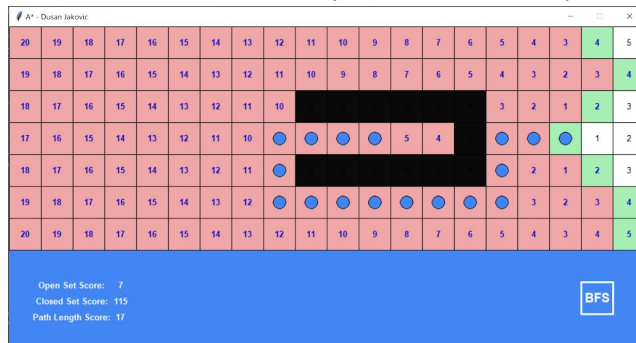
**A\*:** Open Set: 18 | Closed Set: 28 | Path length: 17 | Path Cost = Path Length



**BFS:** Open Set: 7 | Closed Set: 115 | Path length: 17 | Path Cost = Path Length

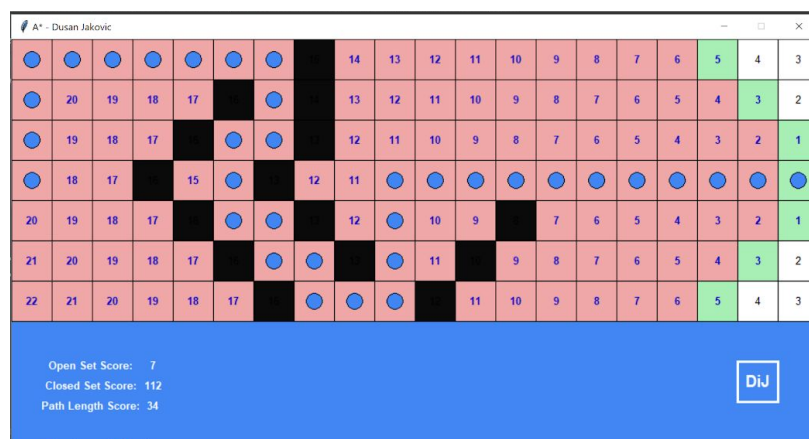
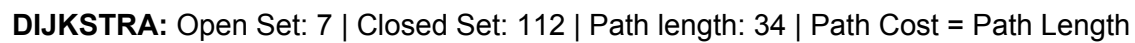


**DIJKSTRA:** Open Set: 7 | Closed Set: 115 | Path length: 17 | Path Cost = Path Length



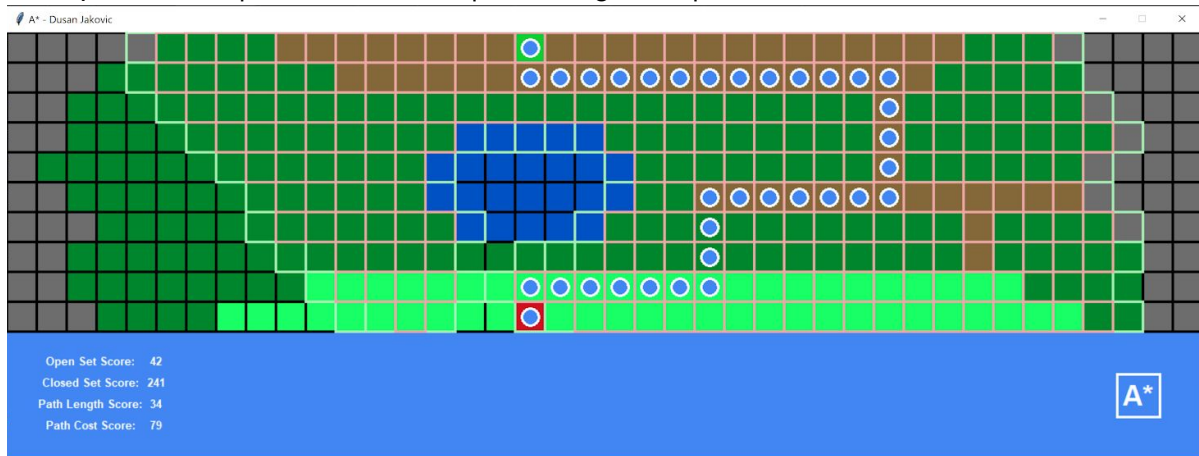


**A\*:** Open Set: 30 | Closed Set: 40 | Path length: 34 | Path Cost = Path Length

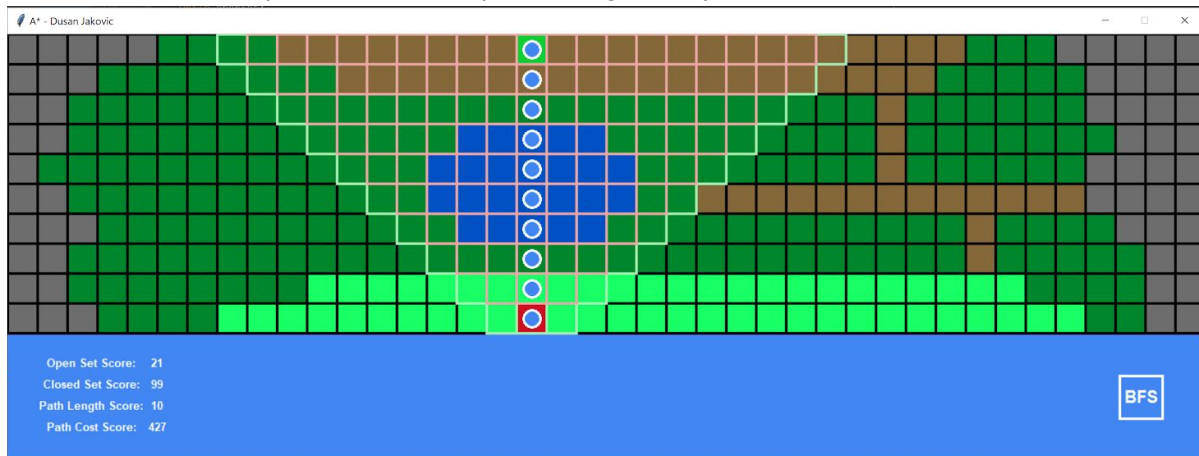


## Board-2-1

**A\*:** Open Set: 42 | Closed Set: 241 | Path length: 34 | Path Cost: 79



**BFS:** Open Set: 21 | Closed Set: 99 | Path length: 10 | Path Cost: 427

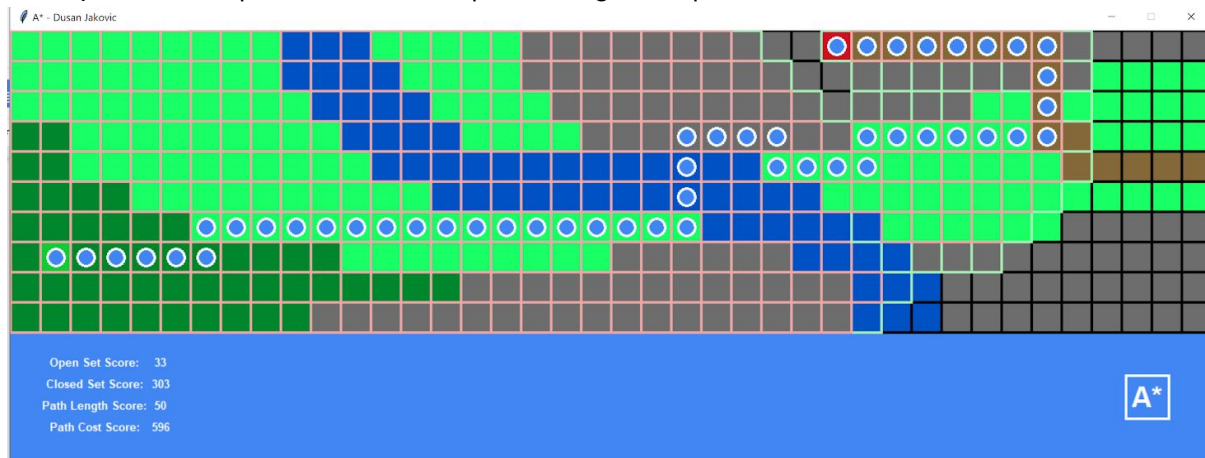


**Dijkstra:** Open Set: 74 | Closed Set: 95 | Path length: 40 | Path Cost: 103



## Board-2-3

**A\*:** Open Set: 33 | Closed Set: 303 | Path length: 50 | Path Cost: 596



**BFS:** Open Set: 11 | Closed Set: 318 | Path length: 38 | Path Cost: 896



**DIJKSTRA:** Open Set: 63 | Closed Set: 281 | Path length: 54 | Path Cost: 741



### 3.3 Board 1-1 and 1-2

Looking at the results, it's clear that A\* is the most efficient, as expected. The final paths are all the same, but the amount of open and closed set differ quite a lot between A\* and the two other.

Looking at the first board; A\* has 4 times less cells in the closed set compared to BFS and Dijkstra. A\* has double the amount of cells in the open set than the two other algorithms. The differences between these three are similar in the other boards as well. A\* star has more cells in the open set and less in the closed set, whilst the other two are the opposite. BFS and Dijkstra are identical in these cases.

### 3.3 Board 2-1 and 2-3

As in the previous comparison, A\* star is the winner by looking at the path cost. The A\* star algorithm may have bigger open set or closed set, or a longer path (length) than BFS/Dijkstra, but it will eventually find a optimal path.

BFS will always find the shortest path, but that has an extreme effect on the cost. Dijkstra may evaluate less cells than A\* but the cost is slightly higher.

## Source Code: Part 1

The source code may be a bit messy because everything is inside one file. A\* is the default method that is used. BFS and Dijkstra are commented out in the code

```
from graphics import *
import time

square_size = 10

walking_space = 1
obstacle_type = 1
start_point = 10
goal_point = 10

openSet = []
closedSet = []
start = 1
goal = 1
cellGrid = []
path = []

# The Map File
filepath = "mazeboard.txt"

win = GraphWin("A* Search", 1000, 400)
win.setBackground(color_rgb(66, 134, 240))

openSet_text = Text(Point(100,405), "Open Set Score")
openSet_text.setTextColor(color="white")
openSet_text.setSize(10)
openSet_text.setStyle("bold")
openSet_text.draw(win)

openSet_score = Text(Point(175,405), "Open Set", (1))
openSet_score.setTextColor(color="white")
openSet_score.setSize(10)
openSet_score.setStyle("bold")
openSet_score.draw(win)

closedSet_text = Text(Point(100,430), "Closed Set Score")
closedSet_text.setTextColor(color="white")
closedSet_text.setSize(10)
closedSet_text.setStyle("bold")
closedSet_text.draw(win)

closedSet_score = Text(Point(175,430), "Closed Set", (1))
closedSet_score.setTextColor(color="white")
closedSet_score.setSize(10)
closedSet_score.setStyle("bold")
closedSet_score.draw(win)

pathLength_text = Text(Point(100,455), "Path Length Score")
pathLength_text.setTextColor(color="white")
pathLength_text.setSize(10)
pathLength_text.setStyle("bold")
pathLength_text.draw(win)

pathLength_text = Text(Point(175,455), "Path Length", (1))
pathLength_text.setTextColor(color="white")
pathLength_text.setSize(10)
pathLength_text.setStyle("bold")
pathLength_text.draw(win)

a_rect = Rectangle(Point(900, 400), Point(950, 450))
a_rect.setOutline(color="white")
a_rect.setWidth(5)
a_rect.draw(win)

Astar_text = Text(Point(925,425), "A*")
Astar_text.setSize(25)
# Astar_text = Text(Point(925,425), "BFS")
# Astar_text.setSize(25)
# Astar_text = Text(Point(925,425), "Dijkstra")
# Astar_text.setSize(25)
Astar_text.setTextColor(color="white")
Astar_text.setTextBackgroundColor(color_rgb(66, 134, 240))
Astar_text.setStyle("bold")
Astar_text.draw(win)

# For updating cellGrid, keeps track of already updated cells. Updates only if not already updated
open_update = []
closed_update = []

# Cell class that contains coordinates, type, h-value, h-score, f-value, neighbors and the parent
# It includes methods
# - addNeighbors() to add 0-4 neighbors to each cell
# - getNeighbors() return 0-4 neighbors
# - rectangle() represents the cell on the grid
# - hScoreText() is the cell's h-value
class Cell():
    def __init__(self, i, j, type):
        self.i = i
        self.j = j
        self.g = 0
        self.h = 0
        self.f = 0
        self.type = type
        self.parent = None
        self.neighbors = []

    def addNeighbors(self, i, j):
        if i < cellGrid[0][0] - 1:
            if cellGrid[i + 1][j].type != obstacle_type:
                self.neighbors.append(cellGrid[i + 1][j])
        if i > 0:
            if cellGrid[i - 1][j].type != obstacle_type:
                self.neighbors.append(cellGrid[i - 1][j])
        if j < cellGrid[i][0] - 1:
            if cellGrid[i][j + 1].type != obstacle_type:
                self.neighbors.append(cellGrid[i][j + 1])
        if j > 0:
            if cellGrid[i][j - 1].type != obstacle_type:
                self.neighbors.append(cellGrid[i][j - 1])

    def getNeighbors(self):
        return self.neighbors

    def rectangle(self, i, j):
        rect = Rectangle(Point(i * square_size, j * square_size), Point((i + 1) * square_size, (j + 1) * square_size))
        if self.type is walking_space:
            rect.setFill(color="white")
        if self.type is obstacle_type:
            rect.setFill(color_rgb(10, 10, 10))
        if self.type is start_point:
            rect.setFill(color_rgb(10, 200, 10))
        if self.type is goal_point:
            rect.setFill(color_rgb(200, 10, 10))
        return rect

    def hScoreText(self, i, j):
        hScoreText = Text(Point((i + 0.5) * square_size, (j + 0.5) * square_size), str(self.h))
        hScoreText.setSize(10)
        hScoreText.setTextColor(color="white")
        hScoreText.setStyle("bold")
        hScoreText.draw(win)
```

```

        displayScore = manhattan(self, goal)
        text = Text(Point(cellGrid[i][j].x * square_size + square_size / 2,
                           cellGrid[i][j].y * square_size + square_size / 2), displayScore)
        text.setSize(16)
        return text

# Manhattan heuristic function
def manhattan(point, point2):
    return abs(point.x - point2.x) + abs(point.y - point2.y)

# Parse map into grid array specified by the text file
def parseMap():
    with open(filePath) as mapFile:
        mapArray = mapFile.readlines()
    return mapArray

# TODO: Create up for this in parseMap function
# Populate elements with cells specified in map
map = parseMap()
for i in range(map.__len__()):
    subGrid = []
    cellGrid.append(subGrid)
    for j in range(map[i].__len__() - 1):
        if map[i][j] == obstacle_type:
            subGrid.append(Cell(i, j, obstacle_type))
        elif map[i][j] == start_point:
            c = Cell(i, j, start_point)
            start = c
            subGrid.append(c)
        elif map[i][j] == goal_point:
            c = Cell(i, j, goal_point)
            goal = c
            subGrid.append(c)
        else:
            c = Cell(i, j, walking_space)
            subGrid.append(c)
    openSet.append(start)

# Give the cells neighbors
def create_neighbors():
    for i in range(cellGrid.__len__()):
        for j in range(cellGrid[i].__len__() - 1):
            cellGrid[i][j].addNeighbors(i, j)

# Draw the board with the cells
def draw_board():
    for y in range(cellGrid.__len__()):
        for x in range(cellGrid[y].__len__() - 1):
            cell = cellGrid[y][x]
            rect = cell.rectangle(y, x)
            rect.draw(win)
            text = cell.hScoreText(y, x)
            text.draw(win)
    win.getMouse()

# Updates the board by the number of seconds specified by the argument
def update_board(seconds_per_update):
    # #
    current = min(openSet, key=lambda c: c.f)
    # BF
    # current = min(openSet)
    # DIJKSTRA
    # current = min(openSet, key=lambda c: c.g)
    for i in openSet:
        if i not in open_update:
            rect = i.rectangle(i.x, i.y)
            rect.setFill(color_rgb(167, 239, 180))
            rect.draw(win)
            open_update.append(i)
            text = i.hScoreText(i.x, i.y)
            text.setOutline(color_rgb(19, 10, 200))
            text.setStyle("bold")
            text.draw(win)
            dot = Circle(Point(current.x * square_size + square_size / 2, current.y * square_size + square_size / 2), 10)
            dot.setOutline(color_rgb(19, 10, 200))
            dot.draw(win)
        for i in closedSet:
            if i not in closed_update:
                rect = i.rectangle(i.x, i.y)
                rect.setFill(color_rgb(239, 167, 180))
                rect.draw(win)
                closed_update.append(i)
                text = i.hScoreText(i.x, i.y)
                text.setOutline(color_rgb(19, 10, 200))
                text.setStyle("bold")
                text.draw(win)
            openSet_score.setText(openSet.__len__())
            closedSet_score.setText(closedSet.__len__())
            time.sleep(seconds_per_update)

# Draw the path after the final path is found
def draw_path(final_path):
    for i in final_path:
        dot = Circle(Point(i.x * square_size + square_size / 2,
                           (i.y * square_size + square_size / 2), 10)
        dot.setFill(color_rgb(66, 174, 244))
        dot.draw(win)

# As algorithm tries find the shortest path, it updates the open board set,
# which updates the board as long as the algorithm runs
def aStar():
    while openSet:
        update_board(1)
        # #
        current = min(openSet, key=lambda c: c.f)
        # BF
        # current = min(openSet)
        # DIJKSTRA
        # current = min(openSet, key=lambda c: c.g)
        if current == goal:
            while current.parent:
                path.append(current)
                current = current.parent
            pathlength_text.setText(path.__len__())
            print("Cost: %s" % pathlength_text.getText())
            return path[::-1]
        openSet.remove(current)
        closedSet.append(current)

        neighbors = current.neighbors
        for neighbor in neighbors:
            if neighbor not in closedSet:
                tempG = current.g + 1
                if neighbor in openSet:
                    if tempG < neighbor.g:
                        neighbor.g = tempG
                        neighbor.parent = current
                else:
                    neighbor.h = manhattan(neighbor, goal)
                    neighbor.f = neighbor.g + neighbor.h
                    neighbor.parent = current
                    openSet.append(neighbor)

# Print ValueError if not a path found
def print_value_error():
    print("CHECK IF THE GOAL/END-POINT IS REACHABLE")

# Run the algorithm
def run():

```

```

draw_board()
create_neighbours()
astar()
draw_path(path)
win.getMouse()

run()

```

## Source Code: Part 2

The source code may be a bit messy because everything is inside one file. A\* is the default method that is used. BFS and Dijkstra are commented out in the code. Comment out win.update\* to skip the animation of the algorithm. It may take some seconds to complete with the animation “turned on”, because the drawing solution for updating isn’t the most optimal one.

```

from graphics import *
import time

square_size = 10

road_type = 0
grass_type = 1
forest_type = 2
mountain_type = 3
water_type = 4
start_point = 0
goal_point = 0

openSet = []
closedSet = []
start = 0
goal = 0
cellGrid = []
path = []

filepath = "map100x100.png"

#GUI
win = GraphWin("A* Search", 1400, 500, background="white")
win.setBackground(color_rgb(66, 134, 244))

openSet_text = Text(Point(100,385), "Open Set Score")
openSet_text.setTextColor(color="black")
openSet_text.setSize(10)
openSet_text.setStyle("bold")
openSet_text.draw(win)

openSet_score = Text(Point(175,405), "Open Set Score: 0")
openSet_score.setTextColor(color="white")
openSet_score.setSize(10)
openSet_score.setStyle("bold")
openSet_score.draw(win)

closedSet_text = Text(Point(100,410), "Closed Set Score")
closedSet_text.setTextColor(color="black")
closedSet_text.setSize(10)
closedSet_text.setStyle("bold")
closedSet_text.draw(win)

closedSet_score = Text(Point(175,430), "Closed Set Score: 0")
closedSet_score.setTextColor(color="white")
closedSet_score.setSize(10)
closedSet_score.setStyle("bold")
closedSet_score.draw(win)

pathLength_text = Text(Point(100,435), "Path Length Score")
pathLength_text.setTextColor(color="black")
pathLength_text.setSize(10)
pathLength_text.setStyle("bold")
pathLength_text.draw(win)

pathLength_text = Text(Point(175,455), "Path Length Score: 0")
pathLength_text.setTextColor(color="white")
pathLength_text.setSize(10)
pathLength_text.setStyle("bold")
pathLength_text.draw(win)

pathCost_text = Text(Point(100,460), "Path Cost Score")
pathCost_text.setTextColor(color="black")
pathCost_text.setSize(10)
pathCost_text.setStyle("bold")
pathCost_text.draw(win)

pathCost_text = Text(Point(175,480), "Path Cost Score: 0")
pathCost_text.setTextColor(color="white")
pathCost_text.setSize(10)
pathCost_text.setStyle("bold")
pathCost_text.draw(win)

a_rect = Rectangle(Point(100,400),Point(130,400))
a_rect.setOutline(color="black")
a_rect.setWidth(1)
a_rect.draw(win)

white_rect = Rectangle(Point(90,400),Point(140,400))
white_rect.setOutline(color="white")
white_rect.setFill(color="white")
white_rect.draw(win)

Astar_text = Text(Point(100,455), "A*")
Astar_text.setSize(25)
Astar_text = Text(Point(100,455), "BFS")
Astar_text.setSize(15)
Astar_text = Text(Point(100,455), "Dijkstra")
Astar_text.setSize(15)
Astar_text.setTextColor(color="white")
Astar_text.setTextColor(color="black")
Astar_text.setStyle("bold")
Astar_text.draw(win)

#for updating cell score
#keeps track of already updated cells, updates only if cell score is less
open_update = []
closed_update = []

def cell(i, j, type, score):
    cell.i = i
    cell.j = j
    cell.g = 0
    cell.h = 0
    cell.f = 0
    cell.cost = 0

```



```

        self.costSoFar = cost
        self.type = typ
        self.parent = None
        self.neighbors = []

    def addNeighbors(self, i, j):
        if j < cellGrid[i].__len__() - 1:
            self.neighbors.append(cellGrid[i][j+1])
        if j > 0:
            self.neighbors.append(cellGrid[i][j-1])
        if i < cellGrid.__len__() - 1:
            self.neighbors.append(cellGrid[i+1][j])
        if i > 0:
            self.neighbors.append(cellGrid[i-1][j])

    def getNeighbors(self):
        return self.neighbors

    def rectangle(self, i, j):
        rect = Rectangle(Point(i * square_size, j * square_size),
                           Point((i+1) * square_size, (j+1) * square_size))
        rect.setWidth(i)
        if self.type is grass_type:
            rect.setFill(color_rgb(25, 255, 100))
        if self.type is forest_type:
            rect.setFill(color_rgb(0, 135, 45))
        if self.type is water_type:
            rect.setFill(color_rgb(0, 0, 150))
        if self.type is mountain_type:
            rect.setFill(color_rgb(100, 100, 100))
        if self.type is road_type:
            rect.setFill(color_rgb(132, 104, 30))
        if self.type is start_point:
            rect.setFill(color_rgb(15, 200, 50))
        if self.type is goal_point:
            rect.setFill(color_rgb(200, 10, 10))
        return rect

    def hScoreText(self, i, j):
        displayScore = manhattan_with_cost(self, goal)
        text = Text(Point(cellGrid[i][j].x * square_size + square_size / 2,
                           cellGrid[i][j].y * square_size + square_size / 2), displayScore)
        text.setSize(16)
        return text

    def fScoreText(self, i, j):
        text = Text(Point(cellGrid[i][j].x * square_size + square_size / 2,
                           cellGrid[i][j].y * square_size + square_size / 2), self.f)
        text.setSize(16)
        return text

# Euclidean method for finding the heuristic cost
def euclidean(point1, point2):
    return abs(point1.x - point2.x) + abs(point1.y - point2.y)

# This euclidean method is used to show the cost
# current cell to the goal, including the cost for the given cell
def manhattan_with_cost(point, point2):
    return abs(point.x - point2.x) + abs(point.y - point2.y) + point.cost

# Parse map into grid array
def parseMap():
    with open(filepath) as mapFile:
        mapArray = mapFile.readlines()
    return mapArray

map = parseMap()

# POPULATING THE GRID
# Populate elements with Cell
for i in range(map.__len__()):
    subGrid = []
    cellGrid.append(subGrid)
    for j in range(map[i].__len__() - 1):
        if map[i][j] == grass_type:
            subGrid.append(Cell(i, j, grass_type, 0))
        elif map[i][j] == forest_type:
            subGrid.append(Cell(i, j, forest_type, 0))
        elif map[i][j] == water_type:
            subGrid.append(Cell(i, j, water_type, 0))
        elif map[i][j] == mountain_type:
            subGrid.append(Cell(i, j, mountain_type, 0))
        elif map[i][j] == road_type:
            subGrid.append(Cell(i, j, road_type, 0))
        elif map[i][j] == start_point:
            c = Cell(i, j, start_point, 0)
            start = c
            subGrid.append(c)
        elif map[i][j] == goal_point:
            c = Cell(i, j, goal_point, 0)
            goal = c
            subGrid.append(c)

openSet.append(start)

# Give neighbors
def create_neighbors(i, j):
    for i in range(cellGrid.__len__()):
        for j in range(cellGrid[i].__len__()):
            cellGrid[i][j].addNeighbors(i, j)

def draw_board():
    for y in range(cellGrid.__len__()):
        for x in range(cellGrid[y].__len__()):
            cell = cellGrid[y][x]
            rect = cell.rectangle(i, j)
            rect.draw(win)
    win.getMouse()

def update_Grid(second_per_update):
    # #
    current = min(openSet, key=lambda o: o.f)
    # BFS
    # current = openSet[0]
    # Dijkstra
    # current = min(openSet, key=lambda o: o.g)
    for i in openSet:
        if i not in open_update:
            rect = i.rectangle(i.x, i.y)
            rect.setOutline(color_rgb(144, 230, 180))
            rect.setWidth(1)
            rect.draw(win)
            open_update.append(i)
            #text = i.fScoreText(i.x, i.y)
            #text.setOutline(color_rgb(150, 10, 100))
            #text.setStyle("bold")
            #text.draw(win)
            dot = Circle(Point(current.x * square_size + square_size / 2, current.y * square_size + square_size / 2), 10)
            dot.setOutline(color_rgb(50, 134, 140))
            dot.setWidth(1)
            dot.draw(win)
        for i in closeSet:
            if i not in closed_update:
                rect = i.rectangle(i.x, i.y)
                rect.setOutline(color_rgb(132, 104, 30))
                rect.setWidth(1)
                rect.draw(win)
                closed_update.append(i)
                #text = i.fScoreText(i.x, i.y)
                #text.setOutline(color_rgb(150, 10, 100))

```

```

        #text.setStyle("bold")
        #text.draw()

        openSet_score.setText(openSet_score())
        closedSet_score.setText(closedSet_score())
        # remove update method-call to skip animation
        win.update()
        time.sleep(0.0001)

def draw_path(final_path):
    for i in final_path:
        dot = Circle(Point((i.x * square_size + square_size / 2),
                           (i.y * square_size + square_size / 2)), 10)
        dot.setFill(color_rgb(66, 134, 244))
        dot.setOutline("blue")
        dot.setOutlineWidth(1)
        dot.draw(win)

def aStar():
    while openSet:
        update_board()
        # A* START
        current = min(openSet, key=lambda o: o.f)
        # SE
        # current = openSet[0]
        # DIJKSTRA
        # current = min(openSet, key=lambda o: o.g)
        if current == goal:
            while current.parent:
                path.append(current)
                current = current.parent
            path.append(current)
            pathLength_text.setText(str(len(path)))
            #initialized as 1 because goal is in the path
            path_cost = 1
            for cell in path:
                path_cost += cell.costToGo
            pathCost_text.setText(str(path_cost))
            print("GOAL REACHED!")
            return path[::-1]

        openSet.remove(current)
        closedSet.append(current)

        # If current.parent
        current.cost = current.parent.cost + current.cost

        neighbors = current.neighbors
        for neighbor in neighbors:
            if neighbor not in closedSet:
                tempG = current.g + current.cost
                if neighbor in openSet:
                    if tempG < neighbor.g:
                        neighbor.g = tempG
                        neighbor.parent = current
                else:
                    neighbor.h = manhattan(neighbor.goal)
                    neighbor.f = neighbor.g + neighbor.h + current.cost
                    neighbor.parent = current
                    openSet.append(neighbor)

    raise ValueError("NO PATH FOUND")
    #CHECK IF THE GOAL/END-POINT IS "REACHABLE"

def run():
    draw_board()
    create_neighbors()
    aStar()
    draw_path(path)
    win.getMouse()

run()

```