

Citadel Protocol Specification

Dusk

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1 Protocol overview

Citadel is a Self-Sovereign Identity (SSI) protocol built on top of Dusk that allows users of a given service to manage their digital identities in a fully transparent manner. More specifically, every user can know which information about them is shared with other parties, and accept or deny any request for personal information.

1.1 The parties involved

Citadel involves three (potentially different) parties:

- The *user* is the person who interacts with the wallet and requests licenses in order to claim their right to make use of services.
- The *Service Provider* (SP) is the entity that offers a service to users. Upon verification that a service request from a user is correct, it provides such service.
- The *License Provider* (LP) is the entity that receives requests for licenses from users, and upon acceptance, issues them. The LP can be the same SP entity or a different one.

1.2 The elements involved

Below there is the list of the elements involved in the protocol. The details of their structure and their role are explained in the following sections.

- A *request* is a set of information that the user sends to the network in order to inform the LP that they are requesting a license. It includes an stealth address where the license will be sent to.
- A *license* is an asset that represents the right of a user to use a certain service. In particular, a license contains a set of attributes that are associated to the requirements needed to make use of that service.
- A *session* is a set of public values sent by the user to the network that are associated with the initiation of the use of a service.
- A *session cookie* is a set of values that allows the SP to verify that a license was used to open a session in their service.

1.3 Properties

Citadel satisfies the following properties:

- **Ownership:** a user of a service is able to prove ownership of a license that allows them to use such a service, without leaking any secret information.
- **Membership:** our solution gives the possibility to revoke licenses. Users can prove ownership of a valid license, that has not been revoked, so it is still member of a given set of licenses.
- **Unlinkability:** nobody in the network can link any activity of the users with other activities done in the network.
- **Attribute Blinding:** the user is capable of deciding which information they want to leak to the SP, blinding the attributes and providing only the desired information.
- **Decentralized License Usage:** when using the licenses, all the participants of the network learn that a given license has been used, without learning any secret information about the license or the user that owns it. This prevents a malicious user of reusing a license that is not allowed to be used again, with different SP.

1.4 Protocol intuition

The basic workflow of our protocol is as follows: users can request licenses to LPs, another entity that the user needs to trust. As soon as the LP gets the request, it can be verified and the LP can decide to issue a license for that user in the Blockchain, using a cryptographic approach that makes all the data private to anyone but the user. The user can later decide to use the license to access a given service provided by a third party, the SP. By means of a zero-knowledge proof, the user will prove in a decentralized manner to the whole network that they can use a given license, without revealing any secret information. The user will finally send a set of cryptographic elements, the session cookie, to the SP. The SP will verify this session cookie using public information stored on the Blockchain, and will grant the service upon successful verification.

2 Cryptographic primitives

In this section, we detail the cryptographic primitives used in Citadel. We briefly introduce Merkle trees, the commitment scheme, encryption scheme, proof system, elliptic curves and hash functions used, specifying at each step the concrete parameters with which each of the primitives is instantiated.

Notation. Throughout the document, we use the following conventions. Given a set S , we denote sampling an element x uniformly at random from S by $x \leftarrow S$. Any group \mathbb{G} used is of a large prime order, and we assume that the discrete logarithm problem is hard in \mathbb{G} . If two elements are denoted by the same letter in upper case and lower case, e.g. a, A , this often signifies the fact that A is a public key corresponding to the secret key a .

2.1 Elliptic curves

BLS12-381 [2] and Jubjub [3] are the elliptic curves used. More precisely, let

$$\begin{aligned} q &= 4002409555221667393417789825735904156556882819939007885332058136 \\ &\quad 124031650490837864442687629129015664037894272559787, \\ p &= 5243587517512619047944774050818596583769055250052763782260365869 \\ &\quad 9938581184513. \end{aligned}$$

Note that both are prime numbers, with bit-lengths 381 and 255, respectively. The curve BLS12-381 is the curve over \mathbb{F}_q defined by the equation

$$E : Y^2 = X^3 + 4.$$

We have that $E(\mathbb{F}_q)$ has different subgroups $\mathbb{G}_1, \mathbb{G}_2$ such that $\#\mathbb{G}_1 = \#\mathbb{G}_2 = p$. This curve is pairing-friendly (with embedding degree $k = 12$), so pairings are efficiently computable. More precisely, Citadel makes use of the bilinear group

$$\mathbb{B} = (p, \mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_T, e : \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}_T).$$

By instantiating the zk-SNARK with the bilinear group \mathbb{B} , we are able to prove statements about satisfiability of arithmetic circuits over \mathbb{F}_p , the so-called *scalar field* of E .

Furthermore, we are interested in proving certain operations with the zk-SNARK, like the correct verification of a Schnorr signature σ . Note that σ is an element of a certain elliptic curve J , but is represented as two coordinates in the base field \mathbb{F}_s of J . Therefore, the verification can be best represented as arithmetic constraints modulo s . While it is possible to represent any NP statement using arithmetic modulo p to plug it into the zk-SNARK, this incurs into a significant efficiency loss if not done carefully. The natural thing is to set $s = p$. Therefore, the signature scheme must be instantiated with an elliptic curve over \mathbb{F}_p . For this, let

$$d = -\frac{10240}{10241} \bmod p.$$

Citadel uses the Jubjub curve, defined by the equation

$$J : -X^2 + Y^2 = 1 + dX^2Y^2,$$

over \mathbb{F}_p . In particular, it uses a subgroup \mathbb{J} of order

$$t = \begin{array}{l} 6554484396890773809930967563523245729705921265872317281365359162 \\ 392183254199, \end{array}$$

which is a 252-bit prime.

The primes and groups defined here will be used through the rest of the document.

2.2 Digital signatures

The Schnorr Sigma protocol [15] is used, compiled with the Fiat–Shamir transformation [5, 14], as a signature scheme. In particular, Citadel makes use of the standard scheme as well as a double-key version to be able to delegate computations later in the protocol. Let $G, G' \leftarrow \mathbb{J}$.

The single-key signature scheme is as follows.

- *Setup*. Sample a secret key $\mathbf{sk} \leftarrow \mathbb{F}_t$ and set the corresponding public key $\mathbf{pk} = \mathbf{sk}G$. Output $(\mathbf{sk}, \mathbf{pk})$.
- *Sign*. On input a message m and a secret key \mathbf{sk} , sample $r \leftarrow \mathbb{F}_t$ and compute $R = rG$. Compute the challenge $c = H(R, \mathbf{pk}, m)$, and set

$$u = r - c\mathbf{sk}.$$

Output the signature $\sigma = (R, u)$.

- *Verify*. On input a public key \mathbf{pk} , message m and signature $\sigma = (R, u)$, compute $c = H(R, \mathbf{pk}, m)$ and check whether the following equality holds:

$$R = uG + c\mathbf{pk},$$

If so, accept the signature, otherwise reject.

The double-key signature scheme is as follows.

- *Setup*. Sample a secret key $\mathbf{sk} \leftarrow \mathbb{F}_t$ and set the corresponding public key $(\mathbf{pk}, \mathbf{pk}') = (\mathbf{sk}G, \mathbf{sk}G')$. Output $(\mathbf{sk}, (\mathbf{pk}, \mathbf{pk}'))$.
- *Sign*. On input a message m and a secret key \mathbf{sk} , sample $r \leftarrow \mathbb{F}_t$ and compute $(R, R') = (rG, rG')$. Compute the challenge $c = H(R, R', \mathbf{pk}, m)$, and set

$$u = r - c\mathbf{sk}.$$

Output the signature $\sigma = (R, R', u)$.

- *Verify*. On input a public key \mathbf{pk} , message m and signature $\sigma = (R, R', u)$, compute $c = H(R, R', \mathbf{pk}, m)$ and check whether the following equalities hold:

$$\begin{aligned} R &= uG + c\mathbf{pk}, \\ R' &= uG' + c\mathbf{pk}'. \end{aligned}$$

If so, accept the signature, otherwise reject.

The signature scheme is existentially unforgeable under chosen-message attacks under the discrete logarithm assumption, in the random oracle model [10, Section 12.5.1]. While the Schnorr signature scheme is widely known, the double-key version has not been used before, to the best of our knowledge. In Citadel, as it happens in the Phoenix transaction model [4], this is leveraged to allow for delegation of proof computations without the need to share one's secret key with the helper.

2.3 Hash functions

Citadel uses hash functions H mostly in the case where given y , we want to prove knowledge of x such that $H(x) = y$. We will do so with PlonK, which requires statements to be written as arithmetic constraints modulo a large prime number p . Most hash function evaluations do not naturally translate to this language, incurring in a big efficiency loss. To avoid this, the Poseidon hash function [8] $H : \mathfrak{F}_p \rightarrow \mathbb{F}_p$, where \mathfrak{F}_p is the set of tuples of \mathbb{F}_p -elements of any length, will be used whenever we compute a hash of which we need to produce a proof. This is because Poseidon is purposefully designed to work with modular arithmetic.

2.4 Encryption schemes

A symmetric encryption scheme [11] based on Poseidon is also used, as described below.

Poseidon is built by applying the sponge construction [1] to a permutation $\pi : \mathbb{F}_p^t \rightarrow \mathbb{F}_p^t$, for $t = r + c$, where

- r is the *rate*, i.e. the amount of \mathbb{F}_p -elements of the input that can be processed in a call to π .
- c is the *capacity*, which is a part of the permutation that is never output by the hash, and is required for security.

The permutation π is composed of linear (matrix multiplication over \mathbb{F}_p) and non-linear (S-boxes) operations. Some rounds are *full rounds*, and apply S-boxes to the whole input, and others are *partial rounds*, in which an S-box is applied to a single \mathbb{F}_p -element.

In this case, Citadel uses POSEIDON-128 to target 128-bit security. Following the recommendations of [8], parameters are set as $r = 4$ and $c = 1$, so that a hash in the Merkle tree can be computed with a single call to the permutation. Internally, a permutation performs $R_F = 8$ full rounds and $R_P = 59$ partial rounds, and uses $S(x) = x^5$ as the S-box.

The encryption scheme [11] is a variation of the one-time pad encryption in the field. It uses Poseidon as a pseudorandom function to extend an agreed-upon symmetric key and encrypt the message. Therefore, the encryption scheme is perfectly secure under the random oracle model.

Concretely, the encryption works as follows. Given a message in \mathbb{F}_q^ℓ , each \mathbb{F}_q -component is added to the corresponding component of the key. The key is obtained using Poseidon by extending the symmetric-encryption key, which is an elliptic curve point, to obtain a key with the same size of the message. The initialization vector contains the two coordinates of the key and a nonce, it is passed to the Poseidon iteration which extends the key and outputs the ciphertext. The sender sends the encryption along with the nonce and the information needed to compute the key, so the receiver can use Poseidon with the same key and nonce to decrypt the message.

2.5 Commitments

As commitment scheme, Citadel uses the Pedersen commitment [13], which we now describe.

- *Setup*. Sample and output the commitment key $\text{ck} = (G, G') \leftarrow \mathbb{J}^2$.
- *Commit*. On input a value v , sample randomness $r \leftarrow \mathbb{F}_t$ and output

$$c = \text{Com}_{\text{ck}}(v; r) = vG + rG'.$$

- *Open*. Reveal v, r . With these, anyone can recompute the commitment and check if it matches c .

This scheme is perfectly hiding, and computationally binding under the discrete logarithm assumption.

2.6 Proof systems

Citadel uses the zk-SNARK PlonK [7] as its proof system. PlonK allows anyone to prove satisfiability of any arithmetic circuit modulo a prime. Since arithmetic circuit satisfiability is an NP-complete problem, this proof system will allow us to prove any statement in NP. PlonK makes use of the KZG polynomial commitment scheme [9], as described in [7]. This requires instantiating PlonK over a pairing-friendly group, which is described in Section 2.1.

Below is a summary the efficiency of PlonK, for a circuit with n multiplication gates and ℓ public inputs.

- *Proving time:* $O(n)$ group and field operations.
- *Verification time:* $O(1 + \ell)$ group and field operations.
- *Proof size:* $O(1)$ group and field elements.

PlonK is sound in the algebraic group model [6], and statistically zero-knowledge. A complete and explicit description of the scheme can be found in [7, Section 8].

2.7 Merkle trees

A *Merkle tree* [12] is a tree that contains at every vertex the hash of its children vertices. More precisely, we consider a perfect k -ary tree of height h . The single vertex at level 0 is called the *root* of the tree, and the k^h vertices at level h are called the *leaves*. Given a vertex in level i , the k vertices in level $i + 1$ that are adjacent to it are called its *children*. Two vertices are each other's *sibling* if they are children of the same vertex.

To each vertex in the tree, we will recursively associate a value, starting from the leaves.¹ Let H be a hash function.

- Level h : leaves are initialized to a null value. Through the lifetime of the tree, they will progressively be filled from left to right with values.
- Level $0 \leq i < h$: each vertex has k children c_1, \dots, c_k at level $i + 1$. We set the value of the vertex to $H(c_1, \dots, c_k)$.

The tree is updated every time a new value is written into a leaf, by updating the $h + 1$ elements in the path from the new value to the root. In particular, this means that the root changes after every update. A nice feature of Merkle trees is that, given a root r , it is easy to prove that a value x is in a leaf of a tree with root r . The proof works as follows:

- *Prove.* For $i = h, \dots, 1$, let x_i be the vertex that is in level i and is in the unique path from x to the root. Let $y_{i,1}, \dots, y_{i,k-1}$ be the $k - 1$ siblings of x_i . Output

$$(x, (y_{1,1}, \dots, y_{1,k-1}), \dots, (y_{h,1}, \dots, y_{h,k-1})).$$

- *Verify.* Parse input as $(x_h, (y_{1,1}, \dots, y_{1,k-1}), \dots, (y_{h,1}, \dots, y_{h,k-1}))$, where x_h is the purported value and $y_{i,1}, \dots, y_{i,k-1}$ are the purported siblings at level i . For $i = h - 1, \dots, 0$, compute²

$$x_i = H(x_{i+1}, y_{i+1,1}, \dots, y_{i+1,k-1}).$$

This allows for proving membership in a set of size k^h by sending $O(kh)$ values. This proof is sound provided that the hash function is collision resistant [10, Section 5.6.2]. For our application, we will set $k = 4$ and $h = 17$.

3 Protocol

3.1 Keys

Let $G, G' \leftarrow \mathbb{J}$ be two generators for the subgroup \mathbb{J} of order t of the Jubjub elliptic curve. In Citadel, each party involved in the protocol holds a pair of static keys with the following structure:

- *Secret key:* $\text{sk} = (a, b)$, where $a, b \leftarrow \mathbb{F}_t$.
- *Public key:* $\text{pk} = (A, B)$, where $A = aG$ and $B = bG$.

We use the subindices $\text{user}, \text{SP}, \text{LP}$ to indicate the owner of the keys, e.g. pk_{user} denotes the public key of the user.

¹We will often abuse notation and write the vertex to refer to the value associated with the vertex.

²To be precise, the prover also has to send $\lceil \log_2 k \rceil$ bits for each level, specifying the position of x_i with respect to its siblings, so that the verifier knows in which order to arrange the inputs of the hash.

3.2 Protocol flow

In this section, we describe the workflow of Citadel in detail. Citadel includes two subprotocols, the license request protocol, and the service request protocol. They are depicted in Figure 1.

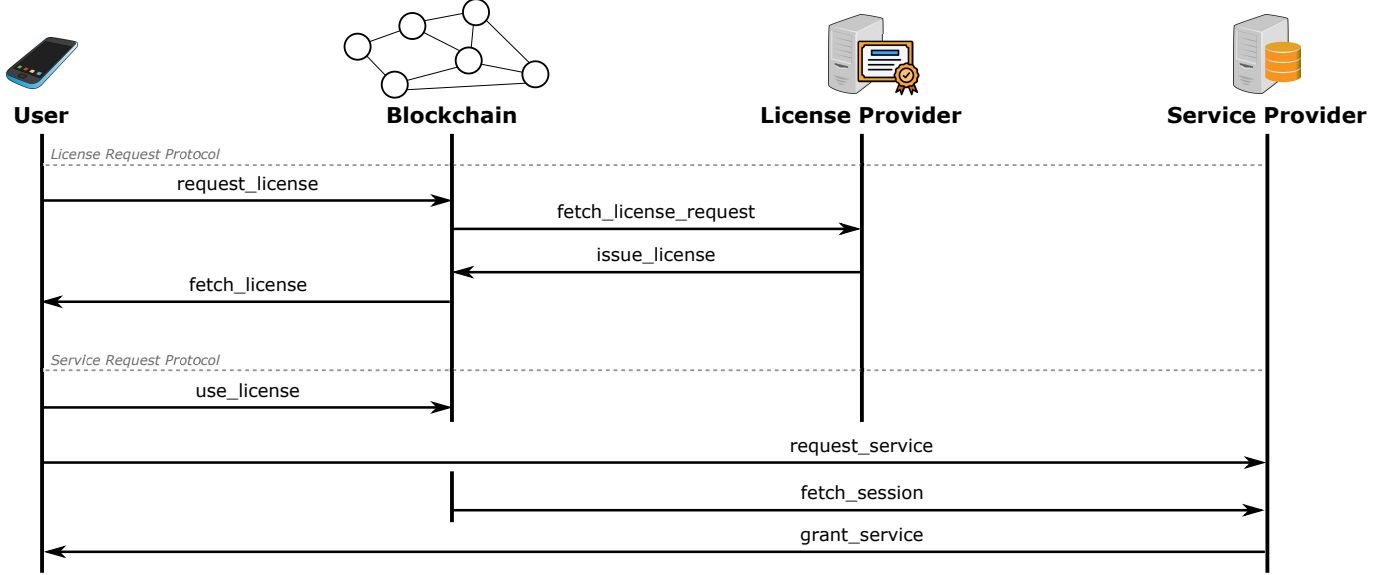


Figure 1: Overview of the protocol messages exchanged between the user, Dusk’s network, the LP and the SP.

3.2.1 (user) request_license()

1. Compute a license stealth address (lpk, R_{lic}) belonging to the user, using the user’s own public key, as follows.
 - 1.1. Sample r uniformly at random from \mathbb{F}_t .
 - 1.2. Compute a symmetric Diffie–Hellman key $k = rA_{user}$.
 - 1.3. Compute a one-time public key $lpk = H^{Poseidon}(k)G + B_{user}$.
 - 1.4. Compute $R_{lic} = rG$.
2. Compute the license secret key $lsk = H^{Poseidon}(k) + b_{user}$ and an additional key $k_{lic} = H^{Poseidon}(lsk)G$.
3. Compute the request stealth address (rpk, R_{req}) using the LP’s public key, as follows.
 - 3.1. Sample r uniformly at random from \mathbb{F}_t .
 - 3.2. Compute a symmetric Diffie–Hellman key $k_{req} = rA_{LP}$.
 - 3.3. Compute a one-time public key $rpk = H^{Poseidon}(k_{req})G + B_{LP}$.
 - 3.4. Compute $R_{req} = rG$.
4. Encrypt data using the key k_{req} : $enc = Enc_{k_{req}}((lpk, R_{lic}) || k_{lic}; nonce)$.
5. Send the following request to the network: $req = ((rpk, R_{req}), enc, nonce)$.

3.2.2 (LP) fetch_license_request()

The LP checks continuously the network to detect any incoming license requests addressed to them:

1. Compute $\tilde{k}_{req} = a_{LP}R_{req}$.

2. Check if $\text{rpk} \stackrel{?}{=} H^{\text{Poseidon}}(\tilde{k}_{\text{req}})G + B_{\text{LP}}$.
3. Decrypt enc using nonce and \tilde{k}_{req} : $((\text{lpk}, R_{\text{lic}}), k_{\text{lic}}) = \text{Dec}_{\tilde{k}_{\text{req}}}(\text{enc}; \text{nonce})$.

3.2.3 (LP) issue_license()

1. Upon receiving a request from a user, define a set of attributes associated to the license, collect them (e.g. by concatenation) in a variable attr_data , and compute a digital signature as follows:

$$\text{sig}_{\text{lic}} = \text{sign_single_key}_{\text{sk}_{\text{LP}}}(\text{lpk}, \text{attr_data}).$$

2. Encrypt the signature and the attributes using the license key:

$$\text{enc} = \text{Enc}_{k_{\text{lic}}}(\text{sig}_{\text{lic}} || \text{attr_data}; \text{nonce}).$$

3. Send the following license to the network:

$$\text{lic} = ((\text{lpk}, R_{\text{lic}}), \text{enc}, \text{nonce}).$$

3.2.4 (user) fetch_license()

In order to receive the license, the user must scan all incoming transactions the following way:

1. Compute $\tilde{k}_{\text{lic}} = H^{\text{Poseidon}}(\text{lsk})G$.
2. Check if $\text{lpk} \stackrel{?}{=} H^{\text{Poseidon}}(\tilde{k}_{\text{lic}})G + B_{\text{user}}$.
3. Decrypt enc using nonce and \tilde{k}_{lic} : $(\text{sig}_{\text{lic}}, \text{attr_data}) = \text{Dec}_{\tilde{k}_{\text{lic}}}(\text{enc}; \text{nonce})$.

3.2.5 (user) use_license()

When willing to use a license, the user must open a session with an specific SP by executing a call to the license contract. The user performs the following steps:

1. Create a zero-knowledge proof π using the gadget depicted in Figure 2.
2. Issue a transaction that calls the license contract, which includes π . Notice that here, the user signs session_hash using lsk . Likewise, the user here will need to compute $\text{lpk}' = \text{lsk}G'$.
3. The network validators execute the license smart contract, which verifies π . Upon success, the following session will be added to a shared list of sessions:

$$\text{session} = \{\text{session_hash}, \text{session_id}, \text{com}_0^{\text{hash}}, \text{com}_1, \text{com}_2\},$$

where $\text{session_hash} = H^{\text{Poseidon}}(\text{pk}_{\text{SP}} || r_{\text{session}})$, and r_{session} is sampled uniformly at random from \mathbb{F}_t .

3.2.6 (user) request_service()

To request a service to the SP, the user establishes communication with it using a secure channel, and provides the session cookie that follows:

$$\text{sc} = \{\text{pk}_{\text{SP}}, r_{\text{session}}, \text{session_id}, \text{pk}_{\text{LP}}, \text{attr_data}, c, s_0, s_1, s_2\}$$

3.2.7 (SP) fetch_session()

Receive a session from the list of sessions, where $\text{session.session_id} = \text{sc.session_id}$.

3.2.8 (SP) grant_service()

Grant or deny the service upon verification of the following steps:

1. Check whether the values $(attr_data, pk_{LP}, c)$ included in the `sc` are correct.
2. Check whether the opening $(pk_{SP}, r_{session})$ included in the `sc` matches the `session_hash` found in the `session`.
3. Check whether the openings $((pk_{LP}, s_0), (attr_data, s_1), (c, s_2))$ included in the `sc` match the commitments $(com_0^{hash}, com_1, com_2)$ found in the `session`.

Furthermore, the SP might want to prevent the user from using the license more than once (e.g. this is a single-use license, like entering a concert). This is done through the computation of `session_id`. The deployment of this part of the circuit has two different possibilities:

- By setting $c = 0$ (or directly remove this input from the circuit), the license can be used only once.
- If the SP requests the user to set a custom value for c (e.g. the date of an event), the license can be reused only under certain conditions.

3.3 Circuits

3.3.1 License circuit

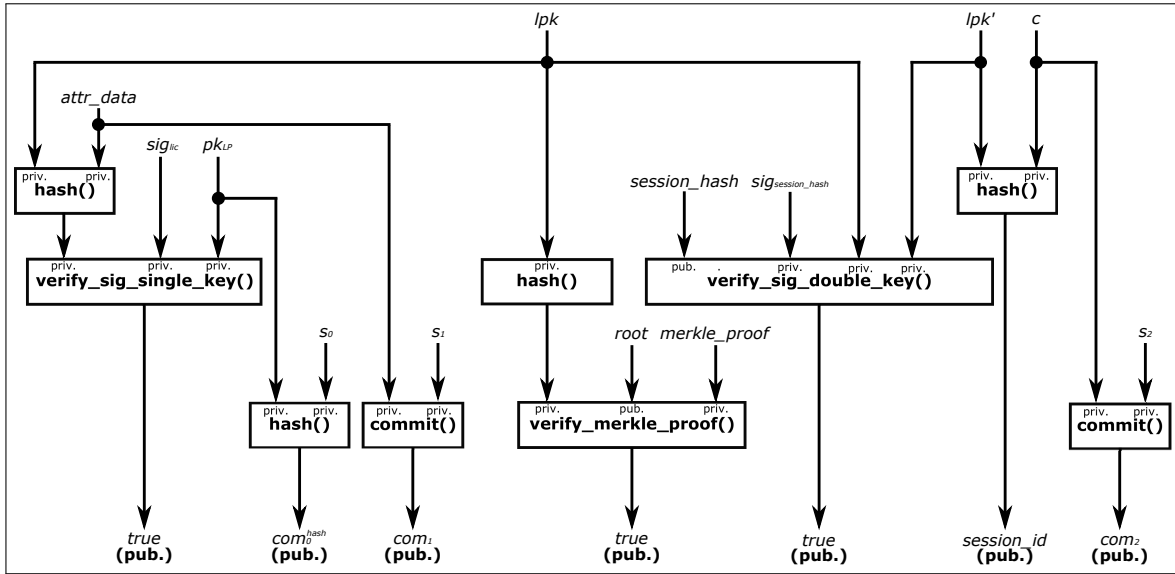


Figure 2: Arithmetic circuit for proving a license's ownership.

4 Implementation details

4.1 Elements structure

Here we describe the elements involved in Citadel. How they are used in the protocol is described in Section 3.

- *Request*: the structure of a request includes the encryption of a stealth address belonging to the user and where the license has to be sent to, and a symmetric key shared between the user and the LP.

Element	Type	Description
$(\text{rpk}, R_{\text{req}})$	StealthAddress	Stealth address for the LP.
enc	PoseidonCipher[6]	Encryption of a symmetric keys and of user's stealth address where the license has to be sent to.
nonce	BlsScalar	Randomness needed to compute enc.

- *License*: asset that represents the right of a user to use a given service. A license has the following structure:

Element	Type	Description
$(\text{lpk}, R_{\text{lic}})$	StealthAddress	License stealth address of the user.
enc	PoseidonCipher[4]	Encryption of the data of some user attributes and signature of these data.
nonce	BlsScalar	Randomness needed to compute enc.

- *SessionCookie*: a session cookie is a secret value only known to the user and the SP. It contains a set of openings to a given set of commitments. The structure is as follows:

Element	Type	Description
pk_{SP}	JubJubAffine	Public key of the SP.
r_{session}	BlsScalar	Randomness for computing the session hash.
session_id	BlsScalar	ID of a session opened using a license.
pk_{LP}	JubJubAffine	Public key of the LP.
attr_data	JubJubScalar	Specific data concerning the attributes of the user.
c	JubJubScalar	Challenge value.
s_0	JubJubScalar	Randomness used to compute $\text{com}_0^{\text{hash}}$.
s_1	BlsScalar	Randomness used to compute com_1 .
s_2	BlsScalar	Randomness used to compute com_2 .

- *Session*: a session is a public struct known by all the validators. The structure is as follows:

Element	Type	Description
session_hash	BlsScalar	Hash of the SP's public key together with r_{session} .
session_id	BlsScalar	ID of a session opened using a given license.
$\text{com}_0^{\text{hash}}$	BlsScalar	Hash of the public key of the LP with s_0 .
com_1	JubJubExtended	Pedersen commitment of the attributes data using s_1 .
com_2	JubJubExtended	Pedersen commitment of the c value using s_2 .

- *CitadelProverParameters*: a prover needs some auxiliary parameters to compute the proof that proves the ownership of a license. Some of the items of this table are related to the session and session cookie elements. The structure is as follows:

Element	Type	Description
lpk	JubJubAffine	License public key of the user.
lpk'	JubJubAffine	A variation of the license public key of the user computed with a different generator.
sig _{lic}	Signature	Signature of the license attributes data.
com ₀ ^{hash}	BlsScalar	Hash of the public key of the LP with s ₀ .
com ₁	JubJubExtended	Pedersen commitment of the attributes data using s ₁ .
com ₂	JubJubExtended	Pedersen commitment of the c value using s ₂ .
session_hash	BlsScalar	Hash of the SP's public key together with r _{session} .
sig_session_hash	SignatureDouble	Signature of the session hash signed by the user.
merkle_proof	Opening	Membership proof of the license in the Merkle tree of licenses.

4.2 Application layer

In the previous subsection, we explained how a user sends a ZKP onchain to use a license. In this process, the network validates that an unknown license has been used, and a session is opened. When the user communicates offchain with the SP, they provide a session cookie to verify that the session is opened onchain and the arguments are correct. One of these arguments, the attribute data `attr_data`, is what defines the license (e.g., a ticket token, a set of personal information...), and this data is leaked to the SP. However, some use cases could require attribute data to be verified according to some conditions, for instance, leaking the information only partially. We now introduce a scheme to perform several attribute verifications offchain.

In our scheme, each SP decides which requirements the users need to meet, and provides a circuit that performs such checks. Then, when the user wants to use a service, will provide the session cookie as explained in the generic protocol, with the difference that **shall not include** the opening to `com1`. Instead, will provide a ZKP computed out of the circuit required by the SP. For this to work, an agreement between the different involved parties is needed, i.e. both LPs and SPs will need to agree on the language (or encoding) used to create the attributes of the license. In such regard, the value `attr_data` used in the license becomes the hash of some specific attributes, as follows:

$$\text{attr_data} = H^{\text{Poseidon}}(\text{attr}_0, \text{attr}_1, \dots, \text{attr}_N, r_{\text{attr}}),$$

where r_{attr} has to be a random value known by the user and the LP. For instance, the public key stored in their ID card.

The SP will accept the service if the user provides a valid session cookie and a valid proof out of the following sample circuit, where the value `com1` included in the public inputs must be equal to the value `session.com1`:

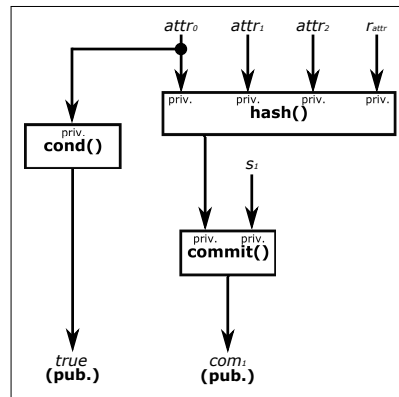


Figure 3: Arithmetic circuit for proving attributes off-chain.

The above circuit from Figure 3 can include as many conditions as desired for the attributes.

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