

$$\begin{array}{ccc}
 * & \xrightarrow{\quad q \quad} & F(X/\sim) \\
 & \searrow f & \downarrow \tilde{f}_* \\
 & & F(Y)
 \end{array}$$