

88. Consider the gamma(α, β) distribution.

(a) Prove the moment generating function is given by

$$M(t) = \left(\frac{1}{1 - \beta t} \right)^\alpha, \quad t < \frac{1}{\beta}$$

(b) Use the MGF to find the mean of the gamma distribution.