

56. Let  $U$  have a uniform distribution on the integers  $a$  and  $b$  where  $a < b$ . Prove the variance is

$$\text{Var}(U) = \frac{(b-a)^2}{12}$$