

51. An interesting property of the negative binomial distribution is that $\text{Var}(X) \geq E[X]$, a property referred to as over-dispersion. Prove the negative binomial distribution is over-dispersed. Are there any restrictions on r or p for which it is not over-dispersed?