93. Let $X_1, X_2, ..., X_n$ be a random sample from a population with mean $\mu$ and variance $\sigma^2 < \infty$. Prove

(a) $\mathrm{Var}(\bar{X}) = \sigma^2/n$ and

(b) $\mathrm{E}[S^2] = \sigma^2$