42. Let U have a discrete uniform distribution on the integers a and b where $a < b$. Prove the variance is

$$\text{Var}(U) = \frac{(b-a+1)^2 - 1}{12}$$