

79. Let $X \sim \text{Poisson}(\theta)$ and $Y \sim \text{Poisson}(\lambda)$, independent. We used the MGF to show the distribution of $S = X + Y$ is $\text{Poisson}(\theta + \lambda)$.
- (a) Use a bivariate transformation to find the joint PMF of (S, T) where $T = X$. Use the joint PMF of (S, T) to find the PMF of S .
 - (b) Prove that the conditional distribution of $T = X$ given $S = s$ is binomial with probability of success $p = \theta/(\theta + \lambda)$.