

107. Let  $X_1, \dots, X_n$  be IID with geometric( $\theta$ ) distribution

$$P_\theta(X = x) = \theta(1 - \theta)^{x-1}, \quad x = 1, 2, \dots, 0 < \theta < 1$$

Show that  $\sum_{i=1}^n X_i$  is sufficient for  $\theta$  and find the family of distributions of  $\sum_{i=1}^n X_i$ . Is the family complete?