

97. Let X_1, \dots, X_n be a random sample from an exponential(θ) population. Let $X_{(1)} < X_{(2)} < \dots < X_{(n)}$ represent the order statistics of the sample. Define the sample range $R = X_{(n)} - X_{(1)}$ and the mid-range $V = (X_{(1)} + X_{(n)})/2$
- (a) Find the joint distribution of $X_{(1)}$ and $X_{(n)}$.
 - (b) Use bivariate transformation methods to find the joint distribution of (R, V) .
 - (c) Find expressions for the marginals of R and V .