

5. Let \mathcal{A} be a Borel field on a sample space \mathcal{S} , and let $A \in \mathcal{A}$. Define

$$\mathcal{A}_B = \{C : C \in B \cap A\}.$$

Prove \mathcal{A}_B is a Borel field.