

16. Let  $\mathcal{S}$  be a sample space of an experiment, and  $\mathcal{B}$  the smallest Borel field of sets in  $\mathcal{S}$ . Let  $A$  and  $B$  be any two sets in  $\mathcal{B}$  such that  $P(B) > 0$ . Then the conditional probability of  $A$  given that  $B$  has occurred is

$$P(A|B) = \frac{P(A \cap B)}{P(B)}.$$

Prove the probability function  $P(\cdot|B)$  satisfies Kolmogorov's Axioms.