

Lab 8. - Open Channel Flow

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Course Website

<http://54.243.252.9/ce-3105-webroot/>

Readings

1. [V-Notch Weir Theory](#)
2. [Hydraulic Jump Theory](#)
3. [Hydraulic Jump Calculator](#)
4. [V-Notch Weir Calculator](#)
5. [B-16 Hydraulic Demonstration Channel \(User Manual\)](#)
6. [Barnes, 1967 USGS Water Supply Paper 1849](#) A collection of photographs and

computed Manning's n

7. <https://www.usgs.gov/centers/sawsc/science/mannings-roughness-coefficients-south-carolina-streams#overview>
8. https://pubs.usgs.gov/ds/668/pdf/DataSeries_668_2.pdf

Videos

1. [Laboratory 8 Instructional Video by Dr. Uddameri](#)

Introduction

Open channel flow is critical for understanding the hydraulics of natural and engineered systems such as rivers, canals, and drainage channels. This laboratory investigates steady uniform flow, head loss models, and hydraulic jumps in open channels. Using a recirculating flume equipped with depth gauges, a digital distance gauge, and calibrated discharge measurements, students will determine Manning's roughness coefficient for a rock bed and analyze alternate and sequent depths in a hydraulic jump. This experiment emphasizes the application of fundamental hydraulics principles to real-world flow conditions.

Purpose

To examine behavior in open channels, in particular determining Manning's n for a portion of a channel, and creating and observing the alternate and sequent depths in a hydraulic jump.

Background/Theory

Open channel flow - free surface, gravity driven.

From pg. 1 of [Sturm, T. Open Channel Hydraulics, 1 st Ed.](#)

Open channel hydraulics is the study of the physics of fluid flow in conveyances in which the flowing fluid forms a free surface and is driven by gravity. The primary

Note

The gravity "drive" is mostly true - I would say such flows are dominated by momentum conditions, mostly with gravity influence. Open flow can go uphill (adverse to gravitational drive) but not for much distance (as one will run out of momentum)

Common examples of open channels:

- rivers, streams, brooks, creeks, cricks (Applacian meaning small stream), billabongs, bourns, wadis, and many more localized terms for small streams
- ditches, canals, aqueducts, storm sewers, sanitary sewers

From pg. 1 of [Sturm, T. Open Channel Hydraulics, 1 st Ed.](#)

other cases such as density-stratified flows. Natural open channels include brooks, streams, rivers, and estuaries. Artificial open channels are exemplified by storm sewers, sanitary sewers, and culverts flowing partly full, as well as drainage ditches, irrigation canals, aqueducts, and flood diversion channels. Applications of

Applications of open channel flow principles

- Culvert design, bridge design, spillway design
- Floodway analysis, and nuisance flooding prediction
- Fate and transport of yummy/yucky stuff (dissolved and/or suspended)
- Surge estimation and coastal flooding from cyclonic storms ([hurricane, typhoon](#))

From pg. 1 of [Sturm, T. Open Channel Hydraulics, 1 st Ed.](#)

ditches, irrigation canals, aqueducts, and flood diversion channels. Applications of open channel hydraulics range from the design of artificial channels for beneficial purposes such as irrigation, drainage, water supply, and wastewater conveyance to the analysis of flooding in natural waterways to delineate floodplains and assess flood damages for a flood of specified frequency. Principles of open channel hydraulics also are utilized to describe the transport and fate of environmental contaminants, including those carried by sediments in motion, as well as to predict flood surges caused by dam breaks or hurricanes.

Natural and man-made open channels are of interest to engineers. The Manning's equation is a fundamental equation governing open channel flow and is given by

$$Q = \frac{K_n}{n} A R^{2/3} S^{1/2}$$

Where K_n is the conversion factor (1 for SI and 1.49 for English units); n is the Manning's roughness coefficient, A is the cross-sectional area and R is the hydraulic radius which is given as:

$$R = \frac{A}{P_W}$$

where P_W is the wetted perimeter.

Steady-Uniform Flow

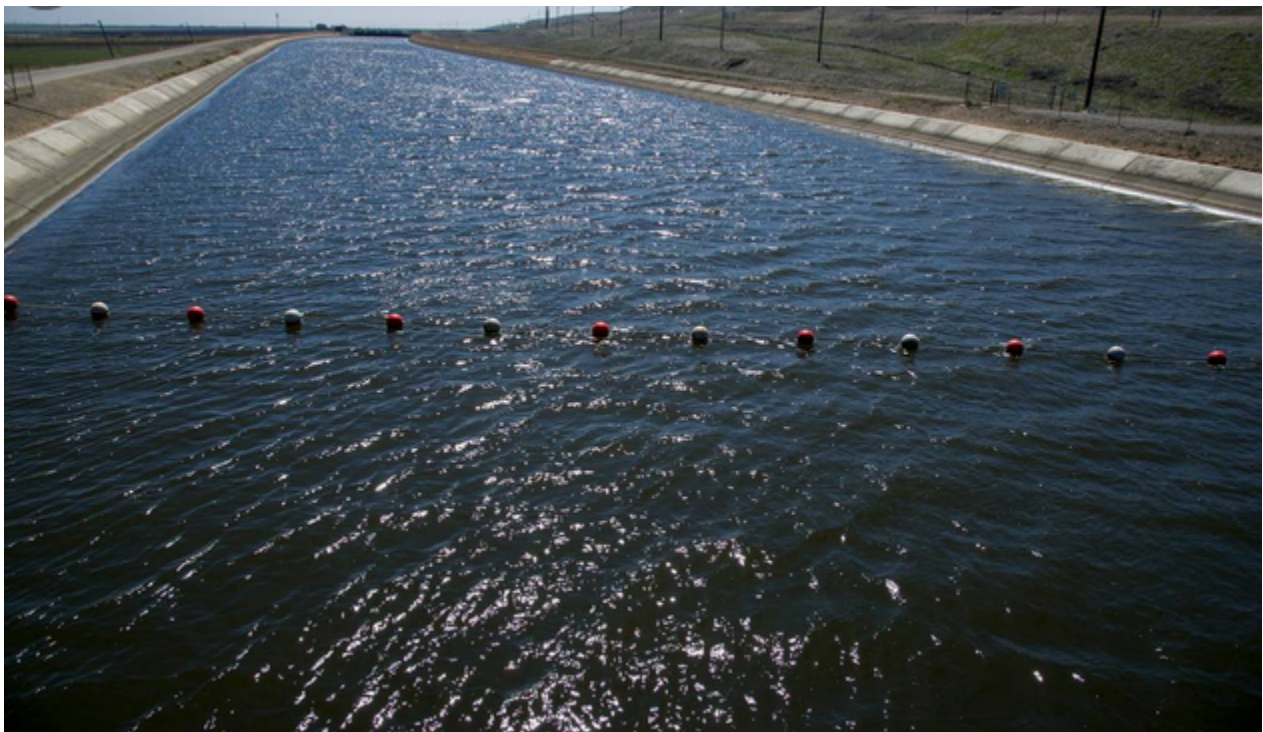
Uniform flow occurs when the average velocities in successive cross sections of a channel are the same. This occurs only when the cross section is constant. Non-uniform flow results from gradual or sudden changes in the cross sectional area. If the water surface is parallel to the channel bottom, flow is uniform and the water surface is at normal depth y_n

Used for design of long open channels with the goal to have the water surface slope equal to the bed slope. Heres a couple of pictures,

First a Central Aridzona Project canal



And the Central Valley Project (Callyfornia) canal I grew up swimmin' in.



The line of floaty balls means you are approaching one of these:



Even though swimmin' in the canals is illegal, the operators dont want to turn a bunch of kids into fish food, so they put up the balls.

Note

Despite the obvious Darwinian advantage of grinding up kids - dead meat does not pay taxes; support old folks; nor serve as a supply of harvestable kidneys. Hence we try to save them.

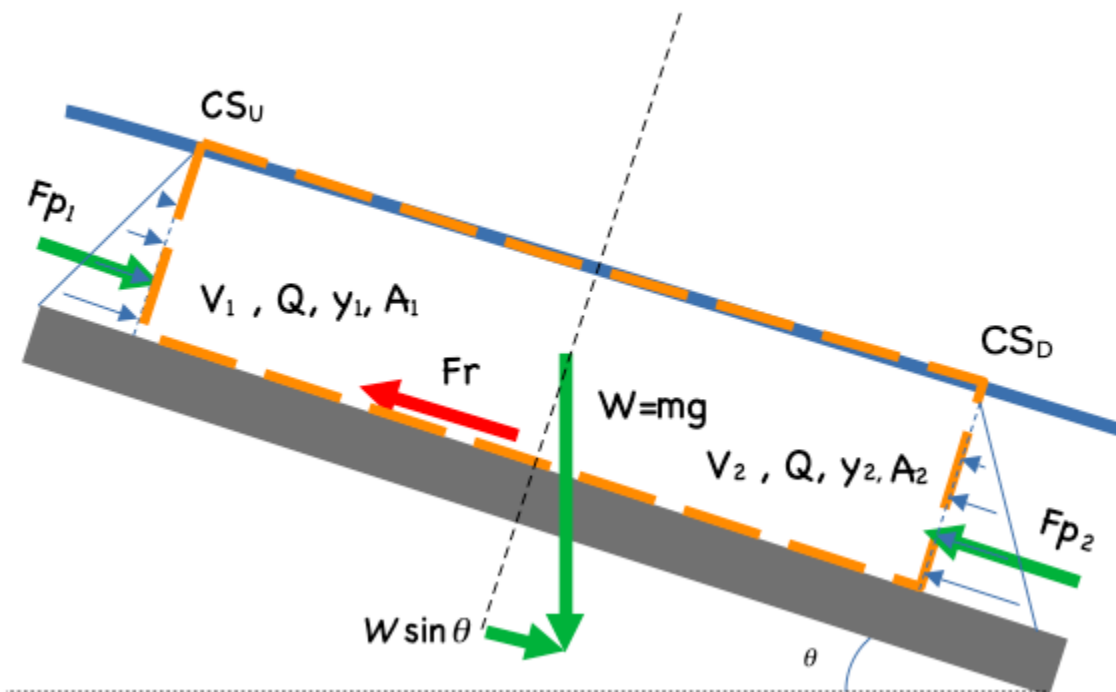
In these applications the resistance to flow is balanced by a driving force provided by gravity.

Resistance is a consequence of cross-section shape, soil, vegetation, materials (in engineered channels). In pipelines the resistance was understood by laboratory experimenters by the 1930's. In open channels interest started later

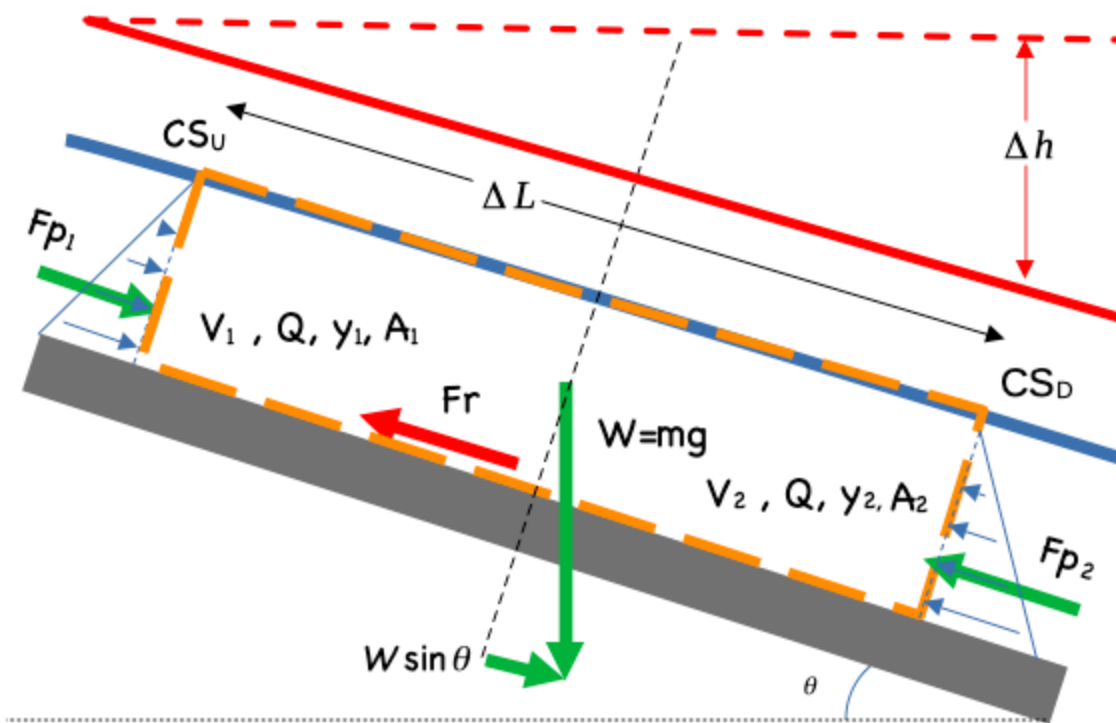
Note

Obviously people have built working open channels much earlier, but techniques of design were empirical passed down by secret societies who wore wizard hats and flew on brooms!

Consider a generic force balance diagram over a short section of channel, ΔL long:



Now insert the Energy Grade Line (EGL)



In the case of uniform flow the flow depths are the same at each end of the section, the section length is such that the end areas are about the same, hence the upstream and downstream pressure force are the same, and the remaining forces are gravity (drive) and friction:

$$W \sin \theta = \rho g A \Delta L \sin \theta = Fr$$

Note

In the above expression Fr is the frictional shear force, not the Froude number. Use the principle of algebraic substitution, and give friction any name you want in the drawing, except Elroy

If friction is stipulated to be generated only by the shear force induced at the solid-liquid interface (and not at the free surface) then the expression becomes

$$\rho g A \Delta L \sin \theta = \tau_0 P \Delta L$$

where P is the wetted perimeter

Divide by $P\Delta L$ to obtain

$$\frac{\rho g A \Delta L \sin \theta}{P \Delta L} = \tau_0$$

observe the hydraulic radius, $R_h = \frac{A}{P}$ appears

$$\rho g R_h \sin \theta = \tau_0$$

The boundary shear stress is the factor that expresses the resistance properties of the fluid (wasser) and the solid material (conduit wall). A usual simplification is to observe that the angle is usuall pretty small so that

$$\sin \theta \approx S_0$$

In pipe flow (CE 3305) the shear stress was something like

$$\tau_0 = \frac{f \rho V^2}{8}$$

Or more usefully (in that context)

$$f = \frac{8 \tau_0}{\rho V^2}$$

And one either looked up a value in the Moody chart or applied Swammee-Jain equations to find f for various Reynolds numbers and material relative roughness.

Returning to our situation we have

$$\frac{\Delta h}{\Delta L} = \frac{\tau_0}{\rho g R} = \frac{\frac{f \rho V^2}{8}}{\rho g R} = \frac{f}{4R} \frac{V^2}{2g}$$

So now we need some way to express f .

Head Loss Models

Chezy Correlation

$$V = \left(\frac{8g}{f}\right)^{1/2} \sqrt{RS_0} = C\sqrt{RS_0}$$

and the value C is the Chezy coefficient.

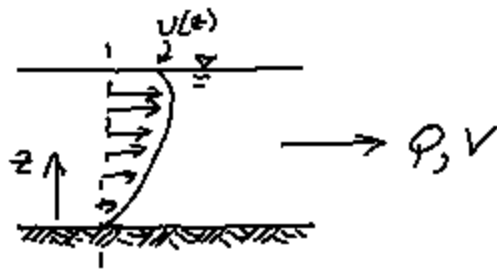
Manning Correlation

Manning several years before his football career developed a similar correlation but observed that the hydraulic radius varied by the $2/3$ power as

$$V = CR^{2/3}S_0^{1/2}$$

There is meaningful theory to relate surface roughness to the " C " values

Velocity Distributions



A vertical velocity profile is not a "straight" line but diminishes as one approaches the channel bottom.

The usual "shape" of the profile is logarithmic (turbulent) or parabolic (laminar). In practice, using arithmetic scales are practically indistinguishable

$$\text{Shear Velocity} \\ U_* = \sqrt{\frac{\tau_0}{\rho}}$$

Logarithmic Profile
at a smooth
wall is

$$\frac{U(z)}{U_*} = \frac{1}{K} \ln \frac{U_* z}{\nu} + A_s$$

↑
Von Karman
Constant

Can be related to pipe roughness values as

$$n = K_n \left(\frac{f}{8g} \right)^{1/2} R^{1/6} \quad \begin{aligned} K_n &= 1.0 \text{ SI} \\ &= 1.49 \text{ US Customary} \end{aligned}$$

In some cases one can relate material properties to estimate f from a Moody chart to estimate n .

$$f_{\text{open channel}} \approx \left(\frac{P}{B} \right)^{1/2} \left[\frac{1}{\frac{B}{D} + 0.3} + 0.9 \right]^{-1} f_{\text{moody}}$$

More typical is a table look-up

From here one can relate the friction factor back to Manning's n or the Chezy coefficient:

The resistance is affected by

- unsteadiness of flow (Re)
- Fr
- material roughness ($\frac{k_s}{D}$) ($\frac{V}{\sqrt{gD}}$)

" n " value lumps all these relationships into a single term, that is obtained by a classification scheme.

In certain situations its numerical value is stipulated by regulatory documents.

i.e. TCEQ stipulates $n=0.013$ for new wastewater pipes

The usual way to specify Manning's n is by a table lookup such as <http://54.243.252.9/toolbox/Databases/ManningN/ManningsN.html>

or tables similar to those in our book

TABLE 4-1

Values of the Manning's Roughness Coefficient n

| Type of Channel and Description | Minimum | Normal | Maximum |
|--|---------|--------|---------|
| A. Closed Conduits Flowing Partly Full | | | |
| A-1. Metal | | | |
| a. Brass, smooth | 0.009 | 0.010 | 0.013 |
| b. Steel | | | |
| 1. Lockbar and welded | 0.010 | 0.012 | 0.014 |
| 2. Riveted and spiral | 0.013 | 0.016 | 0.017 |
| c. Cast iron | | | |
| 1. Coated | 0.010 | 0.013 | 0.014 |
| 2. Uncoated | 0.011 | 0.014 | 0.016 |
| d. Wrought iron | | | |
| 1. Black | 0.012 | 0.014 | 0.015 |
| 2. Galvanized | 0.013 | 0.016 | 0.017 |
| e. Corrugated metal | | | |
| 1. Subdrain | 0.017 | 0.019 | 0.021 |
| 2. Storm drain | 0.021 | 0.024 | 0.030 |
| A-2. Nonmetal | | | |
| a. Lucite | 0.008 | 0.009 | 0.010 |
| b. Glass | 0.009 | 0.010 | 0.013 |
| c. Cement | | | |
| 1. Neat, surface | 0.010 | 0.011 | 0.013 |
| 2. Mortar | 0.011 | 0.013 | 0.015 |
| d. Concrete | | | |
| 1. Culvert, straight and free of debris | 0.010 | 0.011 | 0.013 |
| 2. Culvert with bends, connections, and some debris | 0.011 | 0.013 | 0.014 |
| 3. Finished | 0.011 | 0.012 | 0.014 |
| 4. Sewer with manholes, inlet, etc., straight | 0.013 | 0.015 | 0.017 |
| 5. Unfinished, steel form | 0.012 | 0.013 | 0.014 |
| 6. Unfinished, smooth wood form | 0.012 | 0.014 | 0.016 |
| 7. Unfinished, rough wood form | 0.015 | 0.017 | 0.020 |
| e. Wood | | | |
| 1. Stave | 0.010 | 0.012 | 0.014 |
| 2. Laminated, treated | 0.015 | 0.017 | 0.020 |
| f. Clay | | | |
| 1. Common drainage tile | 0.011 | 0.013 | 0.017 |
| 2. Vitrified sewer | 0.011 | 0.014 | 0.017 |
| 3. Vitrified sewer with manholes, inlet, etc. | 0.013 | 0.015 | 0.017 |
| 4. Vitrified subdrain with open joint | 0.014 | 0.016 | 0.018 |
| g. Brickwork | | | |
| 1. Glazed | 0.011 | 0.013 | 0.015 |
| 2. Lined with cement mortar | 0.012 | 0.015 | 0.017 |
| h. Sanitary sewers coated with sewage slimes, with bends and connections | 0.012 | 0.013 | 0.016 |
| i. Paved invert, sewer, smooth bottom | 0.016 | 0.019 | 0.020 |
| j. Rubble masonry, cemented | 0.018 | 0.025 | 0.030 |

| Type of Channel and Description | Minimum | Normal | Maximum |
|---|---------|--------|---------|
| B. Lined or Built-up Channels | | | |
| B-1. Metal | | | |
| a. Smooth steel surface | | | |
| 1. Unpainted | 0.011 | 0.012 | 0.014 |
| 2. Painted | 0.012 | 0.013 | 0.017 |
| b. Corrugated | 0.021 | 0.025 | 0.030 |
| B-2. Nonmetal | | | |
| a. Cement | | | |
| 1. Neat, surface | 0.010 | 0.011 | 0.013 |
| 2. Mortar | 0.011 | 0.013 | 0.015 |
| b. Wood | | | |
| 1. Planed, untreated | 0.010 | 0.012 | 0.014 |
| 2. Planed, creosoted | 0.011 | 0.012 | 0.015 |
| 3. Unplaned | 0.011 | 0.013 | 0.015 |
| 4. Plank with battens | 0.012 | 0.015 | 0.018 |
| 5. Lined with roofing paper | 0.010 | 0.014 | 0.017 |
| c. Concrete | | | |
| 1. Trowel finish | 0.011 | 0.013 | 0.015 |
| 2. Float finish | 0.013 | 0.015 | 0.016 |
| 3. Finished, with gravel on bottom | 0.015 | 0.017 | 0.020 |
| 4. Unfinished | 0.014 | 0.017 | 0.020 |
| 5. Gunite, good section | 0.016 | 0.019 | 0.023 |
| 6. Gunite, wavy section | 0.018 | 0.022 | 0.025 |
| 7. On good excavated rock | 0.017 | 0.020 | |
| 8. On irregular excavated rock | 0.022 | 0.027 | |
| d. Concrete bottom float finished with sides of | | | |
| 1. Dressed stone in mortar | 0.015 | 0.017 | 0.020 |
| 2. Random stone in mortar | 0.017 | 0.020 | 0.024 |
| 3. Cement rubble masonry, plastered | 0.016 | 0.020 | 0.024 |
| 4. Cement rubble masonry | 0.020 | 0.025 | 0.030 |
| 5. Dry rubble or riprap | 0.020 | 0.030 | 0.035 |
| e. Gravel bottom with sides of | | | |
| 1. Formed concrete | 0.017 | 0.020 | 0.025 |
| 2. Random stone in mortar | 0.020 | 0.023 | 0.026 |
| 3. Dry rubble or riprap | 0.023 | 0.033 | 0.036 |
| f. Brick | | | |
| 1. Glazed | 0.011 | 0.013 | 0.015 |
| 2. In cement mortar | 0.012 | 0.015 | 0.018 |
| g. Masonry | | | |
| 1. Cemented rubble | 0.017 | 0.025 | 0.030 |
| 2. Dry rubble | 0.023 | 0.032 | 0.035 |
| h. Dressed ashlar | 0.013 | 0.015 | 0.017 |
| i. Asphalt | | | |
| 1. Smooth | 0.013 | 0.013 | |
| 2. Rough | 0.016 | 0.016 | |
| j. Vegetal lining | 0.030 | ... | 0.500 |
| C. Excavated or Dredged | | | |
| a. Earth, straight and uniform | | | |
| 1. Clean, recently completed | 0.016 | 0.018 | 0.020 |

| Type of Channel and Description | Minimum | Normal | Maximum |
|--|---------|--------|---------|
| 2. Clean, after weathering | 0.018 | 0.022 | 0.025 |
| 3. Gravel, uniform section, clean | 0.022 | 0.025 | 0.030 |
| 4. With short grass, few weeds | 0.022 | 0.027 | 0.033 |
| b. Earth, winding and sluggish | | | |
| 1. No vegetation | 0.023 | 0.025 | 0.030 |
| 2. Grass, some weeds | 0.025 | 0.030 | 0.033 |
| 3. Dense weeds or aquatic plants in deep channels | 0.030 | 0.035 | 0.040 |
| 4. Earth bottom and rubble sides | 0.028 | 0.030 | 0.035 |
| 5. Stony bottom and weedy banks | 0.025 | 0.035 | 0.040 |
| 6. Cobble bottom and clean sides | 0.030 | 0.040 | 0.050 |
| c. Dragline excavated or dredged | | | |
| 1. No vegetation | 0.025 | 0.028 | 0.033 |
| 2. Light brush on banks | 0.035 | 0.050 | 0.060 |
| d. Rock cuts | | | |
| 1. Smooth and uniform | 0.025 | 0.035 | 0.040 |
| 2. Jagged and irregular | 0.035 | 0.040 | 0.050 |
| e. Channels not maintained, weeds and brush uncut | | | |
| 1. Dense weeds, high as flow depth | 0.050 | 0.080 | 0.120 |
| 2. Clean bottom, brush on sides | 0.040 | 0.050 | 0.080 |
| 3. Same, highest stage of flow | 0.045 | 0.070 | 0.110 |
| 4. Dense brush, high stage | 0.080 | 0.100 | 0.140 |
| D. Natural Streams | | | |
| D-1. Minor streams (top width at flood stage < 100 ft) | | | |
| a. Streams on plain | | | |
| 1. Clean, straight, full stage, no rifts or deep pools | 0.025 | 0.030 | 0.033 |
| 2. Same as above, but more stones and weeds | 0.030 | 0.035 | 0.040 |
| 3. Clean, winding, some pools and shoals | 0.033 | 0.040 | 0.045 |
| 4. Same as above, but some weeds and stones | 0.035 | 0.045 | 0.050 |
| 5. Same as above, lower stages, more ineffective slopes and sections | 0.040 | 0.048 | 0.055 |
| 6. Same as 4, but more stones | 0.045 | 0.050 | 0.060 |
| 7. Sluggish reaches, weedy, deep pools | 0.050 | 0.070 | 0.080 |
| 8. Very weedy reaches, deep pools, or floodways with heavy stand of timber and underbrush | 0.075 | 0.100 | 0.150 |
| b. Mountain streams, no vegetation in channel, banks usually steep, trees and brush along banks submerged at high stages | | | |
| 1. Bottom: gravels, cobbles, and few boulders | 0.030 | 0.040 | 0.050 |
| 2. Bottom: cobbles with large boulders | 0.040 | 0.050 | 0.070 |
| D-2. Flood plains | | | |
| a. Pasture, no brush | | | |
| 1. Short grass | 0.025 | 0.030 | 0.035 |

TABLE 4-1 (Continued)

| Type of Channel and Description | Minimum | Normal | Maximum |
|---|---------|--------|---------|
| 2. High grass | 0.030 | 0.035 | 0.050 |
| b. Cultivated areas | | | |
| 1. No crop | 0.020 | 0.030 | 0.040 |
| 2. Mature row crops | 0.025 | 0.035 | 0.045 |
| 3. Mature field crops | 0.030 | 0.040 | 0.050 |
| c. Brush | | | |
| 1. Scattered brush, heavy weeds | 0.035 | 0.050 | 0.070 |
| 2. Light brush and trees, in winter | 0.035 | 0.050 | 0.060 |
| 3. Light brush and trees, in summer | 0.040 | 0.060 | 0.080 |
| 4. Medium to dense brush, in winter | 0.045 | 0.070 | 0.110 |
| 5. Medium to dense brush, in summer | 0.070 | 0.100 | 0.160 |
| d. Trees | | | |
| 1. Dense willows, summer, straight | 0.110 | 0.150 | 0.200 |
| 2. Cleared land with tree stumps, no sprouts | 0.030 | 0.040 | 0.050 |
| 3. Same as above, but with heavy growth of sprouts | 0.050 | 0.060 | 0.080 |
| 4. Heavy stand of timber, a few down trees, little undergrowth, flood stage below branches | 0.080 | 0.100 | 0.120 |
| 5. Same as above, but with flood stage reaching branches | 0.100 | 0.120 | 0.160 |
| D-3. Major streams (top width at flood stage > 100 ft). The n value is less than that for minor streams of similar description, because banks offer less effective resistance. | | | |
| a. Regular section with no boulders or brush | 0.025 | ... | 0.060 |
| b. Irregular and rough section | 0.035 | ... | 0.100 |

or by comparison with photographs of channels

1. Barnes, 1967 (A classic reference document) https://pubs.usgs.gov/wsp/wsp_1849/pdf/wsp_1849.pdf
2. <https://www.usgs.gov/centers/sawsc/science/mannings-roughness-coefficients-south-carolina-streams#overview>
3. https://pubs.usgs.gov/ds/668/pdf/DataSeries_668_2.pdf

and many others.

Normal Flow Calculations

$$Q = VA = \frac{K_n}{n} AR^{2/3} S_0^{1/2}$$

where S_0 is the bed slope, S_f is the slope of the energy grade line (called the friction slope).

Typical cases:

1. Know y_0 or y_n , shape, S_0, n , compute Q directly.
2. Know y_0 , shape, Q, n , compute S_0 directly.
3. Know shape, Q, n, S_0 compute y_0 iteratively.

Steady-Rapid Varied Flow

Momentum is a property of moving things and is the product of mass and velocity.

Angular momentum is the similar property in rotating geometries. It takes an external force to change the momentum of an object.

Note

Except at faster than light travel (FTL) when impulse-momentum no longer applies; instead ones survival depends largely on the skill of the scriptwriter. As engineers we wear the red shirts and are usually sacrificed, although Scottish engineers seem to last many episodes!

In the context of hydraulics many phenomenon which cannot be analyzed using the energy equation succumb nicely to momentum. The primary advantage of the momentum equation are that details of internal (to the control volume) flow patterns are irrelevant, only the external forces and momentum fluxes need to be considered. The momentum balance was used earlier to solve the head loss caused by a bridge pier and this is a typical application of momentum balances.

It matters greatly in computational hydraulics in unsteady flow.

Hydraulic Jump

A [hydraulic jump](#) occurs:

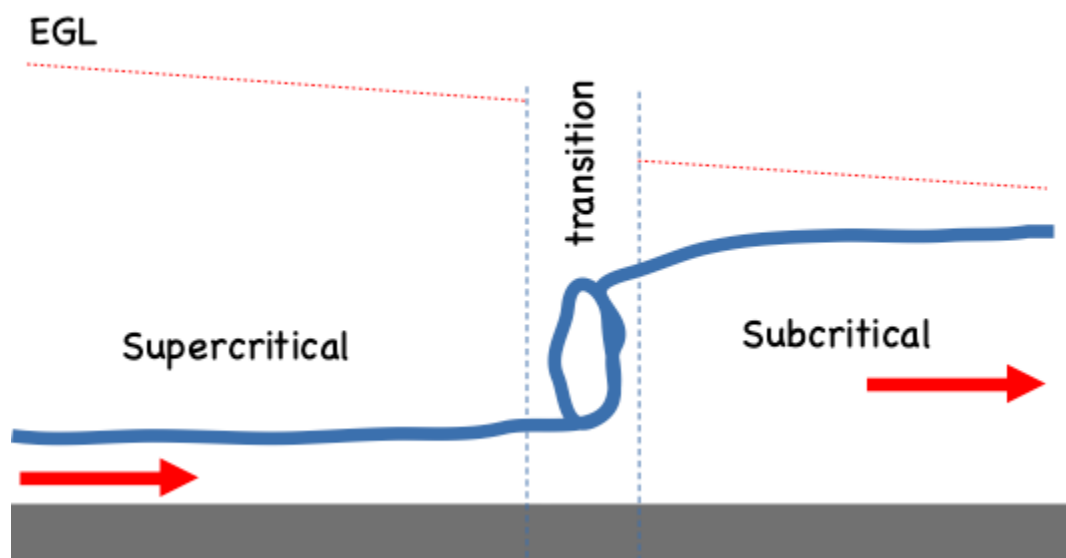
1. when you startle a sugary liquid, it jumps and spills.
2. when flow transitions for supercritical flow to subcritical flow over a short distance.
3. when a lowrider activates the car hydraulics and hops.

well for this lab its the second answer.

Note

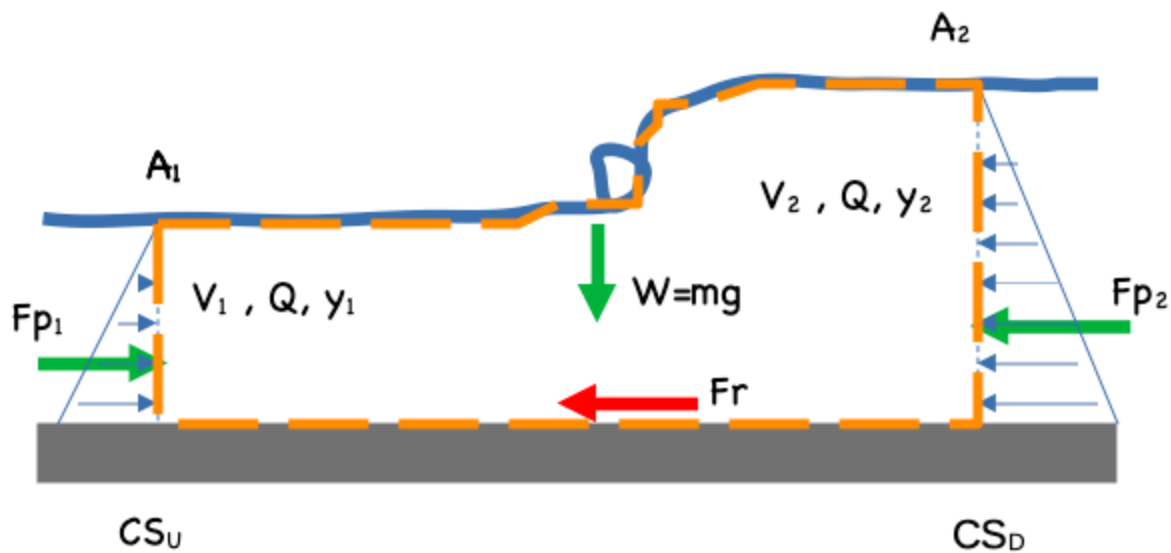
The highest lowrider hop 414.65 cm (163.25 in) and was achieved by Robert White (USA) at the Los Magnificos car show in Austin, Texas, USA on 21 November 2015. The hop was made by a converted school bus called the Honeybadger.

Here's a useful sketch. Supercritical flow upstream meets subcritical downstream. Downstream controls the flow, Q is same but the downstream velocity is exchanged for flow depth, a bit of energy is lost in the transition. The jump itself is quite turbulent and has a practical value in chemical mixing as well as energy dissipation.



Engineering design is typically concerned with forcing jumps in armored channel sections otherwise the energy will chew away at the channel and destroy things.

A control volume around the jump might look like



The jumps occur over a short distance, so the friction term is usually small compared to the other forces and change in momentum flux.

Conservation of momentum is

$$\sum F_x = Fp_1 - Fp_2 - Fr = \rho Q(V_2 - V_1)$$

The pressure forces assume hydrostatic distributions so that

$$Fp = p_i A_i = \rho g \bar{h}_i A_i$$

where \bar{h}_i is the depth to the centroid of the cross section ($\frac{y}{2}$)

Making the substitutions and neglecting the friction term yields

$$(\rho g \bar{h}_1 A_1) - (\rho g \bar{h}_2 A_2) = \rho Q(V_2 - V_1)$$

Rearrangement gives

$$(\rho g \bar{h}_1 A_1) + \rho Q V_1 = (\rho g \bar{h}_2 A_2) + \rho Q V_2$$

Divide by ρg

$$(h_1 A_1) + \frac{Q^2}{gA_1} = (h_2 A_2) + \frac{Q^2}{gA_2}$$

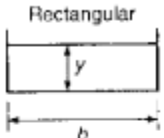
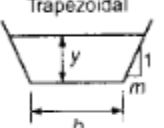
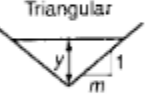

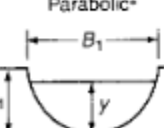
The result above is called the momentum function, and interestingly looks similar to the specific energy function with the section geometry explicitly part of the balance.

$$M_1 = M_2$$

The balance is at the two sections implies that the two different depths have the same momentum function, and these are called the alternate (upstream) and sequent (downstream) depths.

The function itself is dependent on section geometry a few analytical examples are:

TABLE 3-1
Momentum function for channels of different shapes (y = flow depth)

| | |
|--|--|
|  <p>Rectangular</p> | $by^2/2 + Q^2/(gb^y)$ |
|  <p>Trapezoidal</p> | $by^2/2 + my^3/3 + Q^2/[gy(b + my)]$ |
|  <p>Triangular</p> | $my^3/3 + Q^2/(gmy^2)$ |
|  <p>Circular¹</p> | $[3 \sin(\theta/2) - \sin^3(\theta/2) - 3(\theta/2) \cos(\theta/2)] d^3/24 + Q^2/[gd^3(\theta - \sin \theta)/8]$ |
|  <p>Parabolic²</p> | $(4/15)\zeta y^{5/2} + 1.5Q^2/(g\zeta y^{3/2})$ |

¹ $\theta = 2 \cos^{-1}[1 - 2(y/d)]$

² $\zeta = B_1/y_1^2$

For other cross sections, numerical methods are employed.

Laboratory Apparatus

The apparatus is a recirculating water flume (photo below), width 1 ft, comprising a supply tank (in the flume base) a head tank, two pumps, rectangular channel with side rails, depth gauges, total head tubes, bed tappings and downstream control gate.

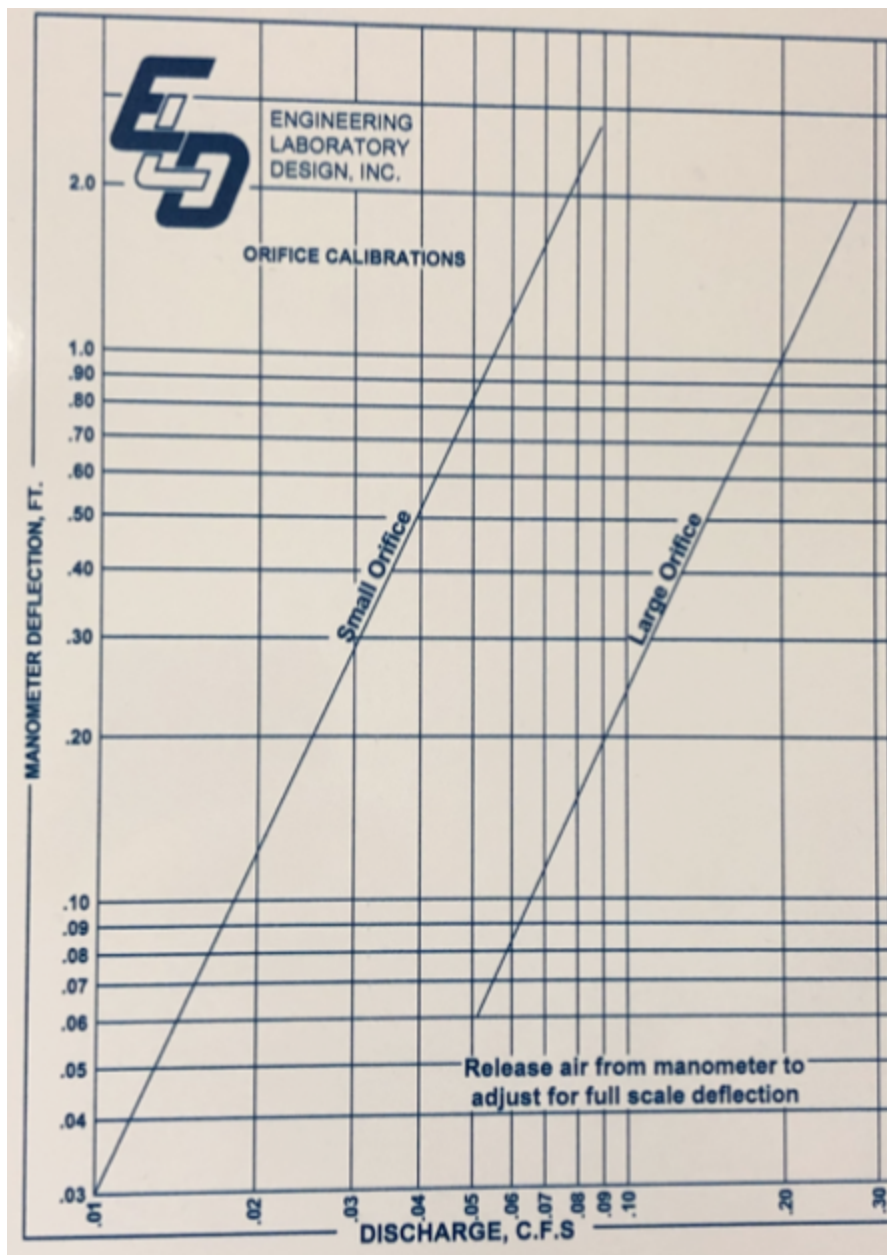


Two parts of the experiment are :

1. measure depth and flow over a rock bed (already in the flume) and determine Manning's n for the rock bed and compare to literature values, and
2. create a hydraulic jump (by using the tail-race valve), stabilizing it, then measuring the alternate and sequent depths and comparing these to calculated values based on the discharge.

Discharge Measurements

The flowrate is determined using the calibration chart below.



The y-axis is the difference of the manometers readings (ΔH) and the x-axis is the flowrate (Q). The following equation belongs to the "Large Orifice" line on the chart.

$$\log_{10}(Q) = \frac{\log_{10}(\Delta H) - 1.47}{2.096}$$

Flow Depth Measurements

Flow depth measurements are made using a digital distance gage (a ruler widda digital readout) if the battery is dead, you will still use the device but make manual

measurements using a ruler from different device settings.

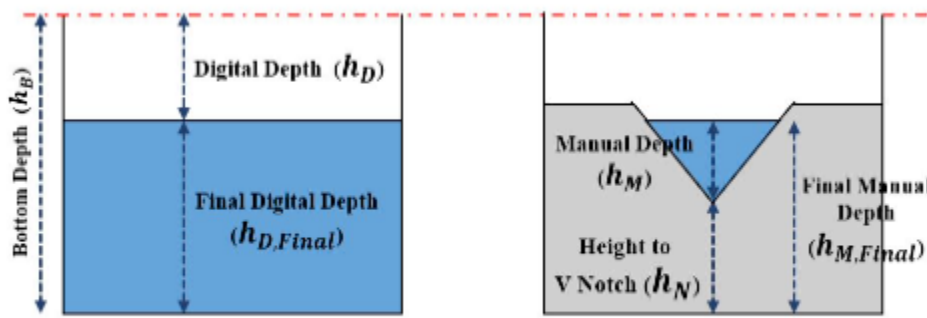


Figure 6: Manual Digital Depth

The digital device reports distance from the rail top to the pointer setting (h_D , in our case depth to water. The total depth of the channel is $h_b = 44$ mm. The flow depth is the difference in these readings.

$$h_{flow} = h_b - h_D$$

A second reading is made when the V-notch weir is in place. It is used to check the pump flow calibration (it needs to be removed to create a stable hydraulic jump).

$$h_{flow@weir} = h_M + h_{notch}$$

A Suggested Procedure

Part 1 This part is to validate the flow calibration chart and equation. 0. Set the slope to 1-percent.

1. Ensure flume tailgate is down.
2. Close the red valves for both pumps.
3. Start the pumps.
4. Move the depth logger to the same elevation as the height of V notch and reset the value to zero.
5. Make sure the manometer valves corresponding to the selected orifice(s) is(are) open.

6. Ensure the manometers are free of air bubbles.
7. Open the red valve(s) to let flow into the flume.
8. Move the depth logger till it touches the top of the water level. Measure the height.
Record this measurement.
9. Record the manometer readings for each pump.
10. Repeat the procedure for 4 different flowrates keeping the slope constant. Use the red valves to adjust flowrates.

Part2 This can be conducted with the weir in place

1. Move the depth logger to top of one of the rocks and reset the value to zero.
2. Make sure the manometer valves corresponding to the selected orifice is/are open
3. Ensure the manometers are free of air bubbles.
4. Open the Orifice to let flow into the flume
5. Move the depth logger till it touches the top of the water level. Measure the height
6. Repeat the procedure for 2 other flowrates keep the slope constant
7. Repeat the above steps for a total of 3 different **slopes**

Part 3 This part will create a stable hydraulic jump. It is easiest to remove the weir.

1. Shut down the pumps, close the red valves, and remove the weir - everything else can be left as-is.
2. Set the slope to 4-percent (its going to look steep, but the machine can handle it!)
3. Start the pumps (you can try with just a single pump if you wish).
4. Raise the tailgate a lot!
5. Zero the depth gage to the channel bottom.
6. Open the red valve(s) to start the flow.
7. Raise the headgate to just above the water height.
8. Lower the tailgate a little bit at a time - you will likely observe two jumps, one near the head gate and one after the rocks. The stable one is the one at the head gate.
9. Lower the headgate until it just touches the water surface - you are forcing supercritical depth at this location. You should be able to create a stable jump about 0.5 to 1-foot from the head gate, and the water surface after the jump should be fairly established at the rocks.

10. Record the manometer readings for the pump(s)
11. Measure the flow depth before the jump (halfway between the headgate and the jump should do). This is the alternate depth.
12. Measure the flow depth after the jump where the surface waves have dissipated (probably at the rocks). This is the sequent depth.

Deliverables

1. Experimental Protocol

Each group must submit a detailed, step-by-step protocol to ensure the experimental procedures are clearly documented and reproducible. The protocol should include:

1. Preparation:

- Steps for setting up the flume, including adjusting slopes and ensuring proper calibration of measurement devices.
- Confirmation of clear manometer tubes and operational pumps.

2. Measurements:

- Instructions for measuring flow depths using the digital distance gauge.
- Procedure for recording flow rates from the manometer readings.
- Steps for stabilizing and measuring alternate and sequent depths during the hydraulic jump analysis.

3. Safety and Maintenance:

- Guidelines for handling equipment safely and ensuring proper water circulation.

2. Laboratory Report

The laboratory report should include the following sections:

1. Title Page: Include the lab title, group members, date, and course information.
2. Abstract: Provide a concise summary of the objectives, methods, results, and conclusions.
3. Introduction: Outline the purpose of the lab, focusing on the significance of Manning's

equation and hydraulic jumps in open channel flow.

4. Apparatus and Methods:

- Description of the recirculating flume and its components (e.g., pumps, digital gauge, manometer, tailgate).
- Detailed summary of procedures for each part of the experiment, emphasizing flow measurement and hydraulic jump stabilization.

5. Data and Results:

- Present depth and flow measurements in tabular form.
- Include plots for Manning's roughness coefficient calculations and a comparison to literature values.
- Graphically represent alternate and sequent depths with the corresponding flow conditions.

6. Analysis:

- Discuss how measured Manning's coefficients compare to reference values for the rock bed.
- Evaluate the observed alternate and sequent depths relative to theoretical predictions.
- Address any discrepancies and potential sources of error.

7. Discussion:

- Highlight the practical significance of the findings in hydraulic design applications.
- Interpret the relationship between flow dynamics and channel characteristics.
- Evaluate the precision of measurements, including comparisons of depth readings from manual and digital methods (if applicable).

8. Conclusion: Summarize the key results and their implications for open channel hydraulics.

9. Appendices: Include raw data, calibration charts, and detailed calculations.

End of Section