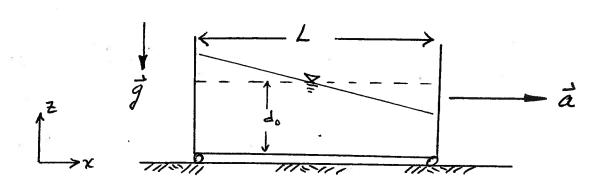


COURSE (E.3305

Application #1 Unitorn Linear Acceleration (EVIER'S EQUATION EXAMPLE 1

A rectangular container of water is subject to constant acceleration. Determine the shape of the free surface



Solution

Fundamental Equation: Ga = Gg - Vp

In component form:

$$\varphi a_x = \varphi g_x - \frac{\partial \varphi}{\partial x}$$

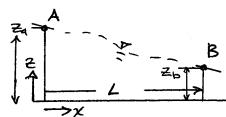
Caz = 69z - 24

Substitute and simplify

$$\frac{\partial b}{\partial x} = -ga_x \quad ; \quad \frac{\partial b}{\partial z} = -gg_z$$

The simplify to obtain observation of the shape of the sh To find shape consider two foints on the free surface: pa = po (both on free surface)

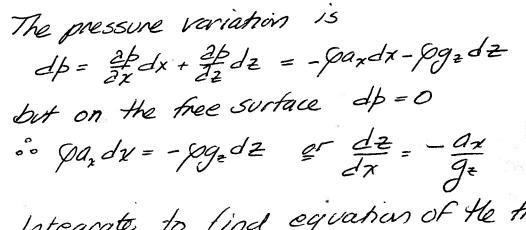
Observe: $g_x = 0$



$$b_{A} = b(0, \Xi_{A}) = b(L, \Xi_{b})$$

NGINEER!

COURSE (63305 SHEET 2 OF 4



Integrate to find equation of the free Surface.

$$\int dz = -\frac{q_x}{g_z} \int dx \implies Z = -\frac{q_x}{g_z} x + C$$

To evaluate the constant of integration consider the depth at x=4/2. Suppose this depth is do. Then $Z_{42} = -\frac{q_x(L)}{g_z(\frac{L}{2})} + C = d_0 \Rightarrow C = d_0 + \frac{q_x L}{g_z 2}$

Finally He equation of the free surface is given by $Z = d_0 + \frac{a_x L}{g_z^2} - \frac{a_x}{g_z^2} X$

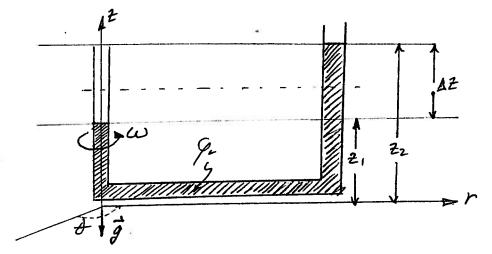
ENGINEERS

COURSE (63345 SHEET 3 OF 4





A U-tube manameter is rotated about an axis coincident with one of the arms. At equilibrium, what is He difference in height of He Huid In He two arms of He manometer?



Solution Fundamental equation of motion 99-76= pa

In component form:

$$ar = -w^2r$$

Substitute and simplify

$$-\frac{\partial b}{\partial r} = -\rho \omega^2 r \quad j - \frac{\partial b}{\partial \theta} = 0 \quad j - \frac{\partial b}{\partial z} = \rho g_z$$

Pressure variation 20



Page 87 EULES BX I

course **43305** sheet **4** of **4**

Integrate to find p(r, t, z)

Sdp = Sqw2rdr - Sqq2d2 = 9w2r2 - 9922+l,+l2

Find constants from known pressure at liquid

$$er=0, z=z, p=0 \Rightarrow gg_zz, = l, +lz$$
 (A)

$$er=R_1 = Z_2, p=0 \implies gg_z = 2 = 9\omega^2 R^2 + C_1 + C_2$$
 (B)

(B)-(A) Gives

$$g_{2}(z_{2}-z_{1}) = g\omega^{2}R^{2} + c_{1}+c_{2}-(c_{1}+c_{2})$$

$$= 0$$

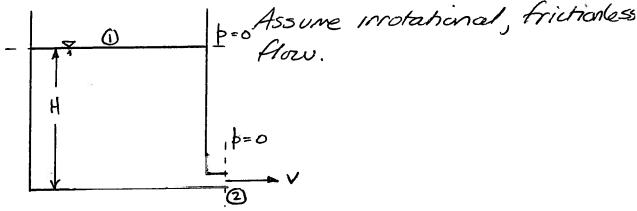
 $\int_{2}^{\infty} \frac{g\omega^{2}R^{2}}{2} = gg_{z}\Delta z \implies \Delta z = \frac{\omega^{2}R^{-1}}{2g_{z}}$



BEENOULL'S EXICOURSE CE3305 SHEET 1 OF 3

Application of Bernoulli's Equation

A tank with water drains through a small hole to the atmosphere as shown. Determine He speed of He flow in He small hole.



Solution 1/8 + 2, + \frac{V_1^2}{2q} = \frac{p_2}{8} + 2_2 + \frac{V_2}{2q} \(\begin{array}{c} \begin{array} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{

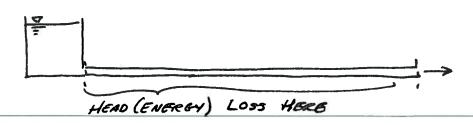
p,=p2=0 z,=H; Z2=0

V, x 0 (Fluid is in motion, but relative to the moving free surface the Speed is nagligible)

V2 = 129H

" PRETTY CLASSICAL" EXAMPLE

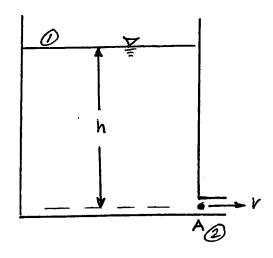
USED LATER ON IN PIPELINES AS:







Velocity in the outlet pipe from reservoir is 16 ft/sec and h=15 ft. Assume irrotational frictionless flow. What is the pressure at A?



Solution
$$\frac{f}{f} + \frac{1}{2}, + \frac{1}{f} = \frac{f^2}{g} + \frac{1}{f^2} + \frac{1}{2g} \quad (Bernoulli's Eqn.)$$

$$h = \frac{f^2}{g} + \frac{V_2^2}{2g}$$

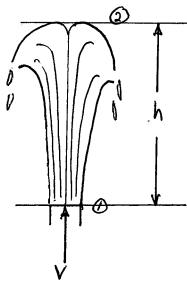
$$(h - \frac{V_2^2}{2g}) y = f^2$$

$$(4.01)^2$$

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COURSE (63305 SHEET 3 OF 3

Water issues vertically from a fountain. The water relocity at the exit is 20 H/sec. Assure irrotational flow. How high will the fountain 90?



$$\frac{p_1}{y} + z_1 + \frac{V^2}{2g} = \frac{p_2}{8} + z_2 + \frac{V^2}{2g}$$

$$p_1 = p_2 = 0 \quad \text{gage}$$

$$z_1 = 0; \quad z_2 = h$$

$$V_2 \approx 0 \quad \text{at pop of jet}$$

$$\int_{ag}^{2} = h$$

$$h = \frac{(20H/sec)^2}{2(32.2H/sec^2)} = \frac{6.21 \, \text{ft}}{}$$