

Engineering Economy Ch. 2 Engineering, Hydraulics & Eng. Mgmt., McGraw-Hill, 1992.

Eng Eco - compare alternatives & select most economic.

- need common money units
- time
- interest - time value of money

Discount factor -

Based on i - interest rate

n - # years

P = Present amount

A = annual amount

F = future amount

Table 2.1.1

• Future from present amount

$$F = P(1+i)^n$$

Single-payment compound amount

$$F/P = (1+i)^n = (F/P, i\%, n)$$

P/F = single payment present worth

• Annual from future amount

Uniform annual series sinking fund

$$A/F = \frac{i}{(1+i)^n - 1} = (A/F, i\%, n)$$

F/A = Series compound amount

• Annual from present amount

capital recovery factor

$$A/P = \frac{i(1+i)^n}{(1+i)^n - 1} = (A/P, i\%, n)$$

P/A = Series present worth factor

• Uniform Gradient Series

$$\left| \begin{array}{c} P \\ A_1 \\ A_2 \\ \vdots \\ A_n \end{array} \right|_{i\%}$$

Benefit-Cost Analysis

Costs often initial (capital) & annual (O&M)

Benefits usually annual (ODM)

$$PVB = b_0 + \frac{b_1}{(1+i)} + \frac{b_2}{(1+i)^2} + \dots + \frac{b_n}{(1+i)^n}$$

$$PVC = c_0 + \frac{c_1}{(1+i)} + \frac{c_2}{(1+i)^2} + \dots + \frac{c_n}{(1+i)^n}$$

We want $PVB > PVC$

$$\text{or } \frac{PVB}{PVC} > 1$$

$$\frac{PVB}{PVC} = \frac{B}{C}$$

Consider multiple alternatives, what if several have $\frac{PVB}{PVC} > 1$?

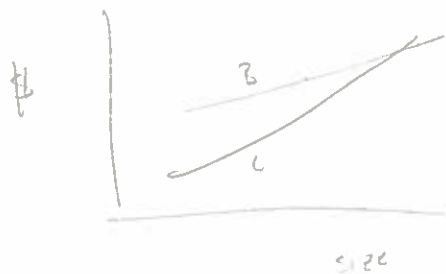
Optimum - when $\Delta PV B = \Delta PV C$
 marginal value of B. marginal value of C

Must compare Alternatives to each other
 Start with lowest cost

$$\Delta PV B = \Delta b_0 + \frac{\Delta b_1}{(1+i)} + \frac{\Delta b_2}{(1+i)^2} - \dots + \frac{\Delta b_n}{(1+i)^n}$$

$$\Delta PV C = \Delta c_0 + \frac{\Delta c_1}{(1+i)} + \frac{\Delta c_2}{(1+i)^2} - \dots + \frac{\Delta c_n}{(1+i)^n}$$

$$\frac{\Delta PV C}{\Delta PV B} = \frac{\Delta B}{\Delta C} = \frac{PV C(A_1) - PV C(A_2)}{PV B(A_1) - PV B(A_2)}$$



marginal
value



Ex. 2.2.2

Consumer Behavior

Utility function - describes level of satisfaction to user for each alternative

Select between commodities w_1, \dots, w_n

$$u = f(w_1, w_2, \dots, w_n)$$

$$n=2 \quad u = f(w_1, w_2)$$

$$\text{marginal utility: } du = \frac{df}{dw_1} dw_1 + \frac{df}{dw_2} dw_2$$

- $\frac{dw_2}{dw_1} = \text{marginal rate of substitution}$

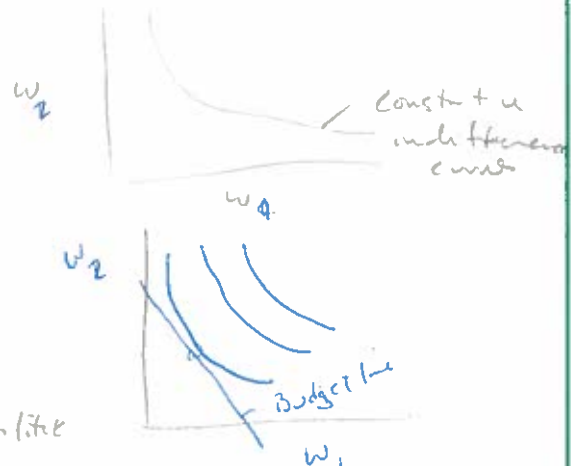
Maximization of Utility - user desire

$$\text{Budget constraint } B^0 = p_1 w_1 + p_2 w_2$$

price price

Max utility when ratio of marginal utilities
 = ratio of prices

$$\frac{dw_2}{dw_1} = \frac{p_1}{p_2}$$



Demand function - quantity consumer will buy as function of price & income



① substitution effect $p \uparrow Q \downarrow$

② income effect

Elasticity of demand = proportionate rate
of change in quantity demanded
by proportionate rate of price change

$$\epsilon_{11} = \frac{\partial w_1 / w_1}{\partial p_1 / p_1} = \frac{p_1}{w_1} \frac{\partial w_1}{\partial p_1}$$

high elasticity > -1 necessity

more
negative
↓

$$\epsilon_{11} > -1 \quad p_1 \uparrow, w_1 \uparrow$$

$$\epsilon_{11} < -1 \quad p_1 \uparrow, w_1 \downarrow$$

$$\epsilon_{11} = -1 \quad p_1 \uparrow, w_1 \text{ constant}$$

$$\frac{\partial(p_1 w_1)}{\partial p_1} = w_1 (1 + \epsilon_{11})$$

Cross price elasticity $\epsilon_{21} = \frac{p_1}{w_2} \frac{\partial w_2}{\partial p_1}$

Theory of the Firm — used for hydro systems

Firm — technical unit which produces commodities

Theory of Firm

- allocation of resources for production
- determine level of production
- response to change in price for inputs & outputs

Production function

$$\underset{\substack{\uparrow \\ \text{product}}}{q} = f(\underset{\substack{\uparrow \\ \text{inputs}}}{x_1, x_2, \dots, x_n})$$

assume technical efficiency
max output from each
combination

Ex. $q = \text{corn}$ $x_1 = \text{irrigation H}_2\text{O}$ $x_2 = \text{fertilizer}$

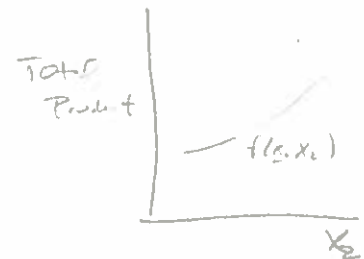
$$q = f(x_1, x_2)$$

Input, output levels → rate of use or production/time

Long run → all inputs vary

Short run → one is fixed

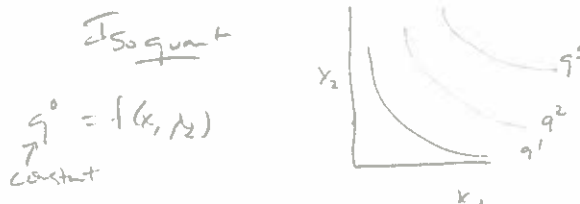
Total Product $TP(x_2) = q = f(\underset{\substack{\uparrow \\ \text{fixed}}}{x_1}, x_2)$



Average Product $AP(x_2) = \frac{q}{x_2} = \frac{f(x_1, x_2)}{x_2}$

Marginal Product $MP(x_2) = \frac{\partial q}{\partial x_2} = \frac{\partial f(x_1, x_2)}{\partial x_2}$

Ex 2.4.1 calculate MP



Rational operation
→ where $MP(x_1) \neq MP(x_2)$
are > 0

Rate of Technical Substitution $RTS = (\text{slope of isoquant})$

$$= -\frac{dx_2}{dx_1} = \frac{MP(x_1)}{MP(x_2)}$$

Rat

Optimal Inputs - 2 variable

$$\text{Cost function } C = \underset{\substack{\uparrow \\ \text{price}}}{r_1} x_1 + \underset{\substack{\uparrow \\ \text{price}}}{r_2} x_2$$

$$\frac{dx_2}{dx_1} = -\frac{r_1}{r_2} \Rightarrow \text{PTS} = -\frac{dx_2}{dx_1} = \frac{r_1}{r_2} = \frac{MP(x_1)}{MP(x_2)}$$

$$\text{rearrange } \frac{MP(x_1)}{r_1} = \frac{MP(x_2)}{r_2} \quad \frac{MP}{\text{dollarcost}} \quad \text{same for all inputs at optimum}$$

Expansion Path - crossing isocosts + optimal combinations $g(x_1, x_2) = 0$

Cost in Short Run - 2 variable

x_1 fixed x_2 variable

$$q = f(x_1, x_2)$$

$$g(x_1, x_2) = 0$$

$$C = r_1 x_1 + r_2 x_2$$

Costs associated w/ x_1 are fixed cost FC

Total variable cost - spent on x_2

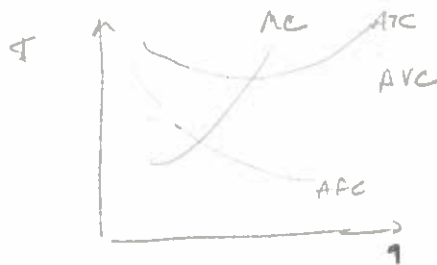
$$\text{Total Cost} = TVC + TFC$$

$$\text{Average Total Cost } ATC = \frac{TC}{q}$$

$$AFC = \frac{TFC}{q}$$

$$AVC = \frac{TVC}{q}$$

$$\text{Marginal cost } MC = \frac{\Delta TVC}{\Delta q}$$



$$\text{Total Revenue } TR = pq$$

$$MP = \Delta TR / \Delta q$$

Profit maximized when

$$MR = MC$$

Costs in Long Run - all variables

Long run AVC = envelope of short-run AC curves



Demand Curve commodity

Demand for w_j depends on P_j , other product prices, & budget B^0

$$D_i = D_i(P_1, P_2, \dots, P_n, B^0)$$

only P_j variable

$$D_i = D_i(P_j)$$

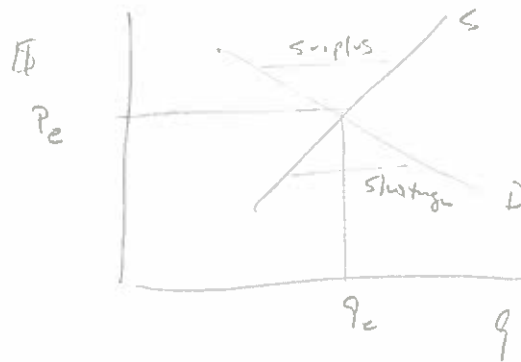
$$\text{Aggregate demand } D = \sum_i D_i(P)$$

$$\text{Marginal revenue } MP = \frac{d(TR)}{dq} = P \quad \text{if } TR = PQ$$

$$\underline{MR \text{ curve} = \text{Demand Curve}}$$

Supply function = part of MC above AVC

$$\text{Long run optimum} \Rightarrow MC = P$$



Benefit-Cost Analysis

I. Project Evaluation

A. Feasibility Tests

- 1. Engineering feasibility - performs function?**
- 2. Economic feasibility - benefits > costs?**
- 3. Financial feasibility - sufficient funds?**
- 4. Political feasibility - approval secured?**
- 5. Social feasibility - users in favor?**
- 6. Environmental feasibility - No laws broken?**

B. Economic Feasibility

- 1. Need for government in w.r. planning**
 - a. Overcome allocation deficiencies**
 - b. Coordinate multi project systems**
 - c. Provide financial resources**
- 2. Problems with govt.**
 - a. Lack of market incentives**
 - b. Political motivation - "pork barrel"**
- 3. Solution - B/C analysis**
 - a. Force objective evaluation**
 - b. Encourage improved fund allocation**

C. Defining Benefits and Costs

1. First define goal(s) and alternative actions

- a. Benefits measure effectiveness of action**
- b. Costs measure effectiveness of sacrificed action**

2. Differences in B/C analysis and private firm analysis:

- a. Public viewpoint incorporates all costs and all benefits. External economies/diseconomies need evaluating.**
- b. Discount rate may be lower than that used by private firms.**
- c. Government planner should try to evaluate true economic worth of input and output.**
- d. Govt. planner must derive equivalent market values through demand analysis.**

D. Benefit-Cost Categories - 4 main classes:

1. Tangible (market) benefits - those resulting from consequences to private parties which can be assigned monetary value.

a. Primary benefits - value obtained from project-produced goods and services.

Direct benefits - accrued to those who put project output to its intended use.

*reduce flood damage
from increasing
value of electric power*

Indirect benefits - realized economic consequences of technological external effects.

*low flow thru water quality
also benefits
navigation*

Land-enhancement benefits - when more productive land use is made possible (other than direct benefits)

b. Secondary benefits - value added to activities influenced by the project through economic rather than technological linkages.

“Stemming-from” benefits - linkages that increase the net income of those who process project output. *cotton used for clothing - each processor*

“Induced-by” benefits - result from backward production linkages that increase income for those providing goods and services. *farm implement sales to save the cotton*

c. Employment benefits - increased employment from new jobs created.

d. Public benefits - other goals achieved and evaluated by value judgements or relative desirability. *economic substitution, income, education, better environmental quality*

2. Intangible (extramarket) Benefits - cannot be assigned monetary value, eg. health improvements, env. aesthetics, historic preservation.

3. Project Construction - requires private parties to bear costs as well as realize benefits.

Benefits - costs = net benefit

a. Associated costs - private investment to produce or utilize project output.

purchase machinery for new crops

b. Induced costs - adverse consequences of project construction, eg. cost of downstream flood control.

4. Cost of Project Installation - placed in denominator of B/C ratio. Includes construction cost, O&M, and replacement.

II. Benefit-Cost Measurement - use "with-and-without" principle.

built or not built

A. Direct Primary Benefits

- 1. Market value of output**
- 2. Cost of producing output by alternative (least-costly)**

B. Indirect Primary Benefits

- 1. Develop checklist of potential project technological external effects and assess each one; then sum results for total benefit.**
- 2. Estimate on the basis of % of direct benefits.**

C. Land-Enhancement Benefits

- 1. Develop substantial evidence that land use will change.**
- 2. Evaluate extent of change.**

D. Secondary Benefits

- 1. National - include with primary benefits.**
- 2. Regional, state or local - additional B/C ratio.**
- 3. Include explanation of secondary benefits in planning reports.**

E. Employment Benefits

- 1. Wages paid to those otherwise unemployed.**
- 2. Increase in wages to those underemployed.**
- 3. New investment opportunity**
- 4. Input-output analysis**

F. Income-Redistribution Benefits - Establish, by tax bracket,

- 1. Cost of project among those providing funds to pay for project**
- 2. Money spent on installation, and**
- 3. Tangible efficiency benefits.**

G. Other Public Benefits - depends on type of benefit.

Improved facilities, property taxes

H. Intangible benefits - Documentation. *if not valued*

I. Associated and Induced Costs - depends on type.

For investment to utilize output

adverse consequences

J. Project Installation Costs - Includes construction, engineering/administration, right-of-way, easements, relocations, etc.

K. O&M, Replacement - Includes personnel, equipment, supplies, energy costs, etc.

III. Value of Benefit-Cost Analysis

A. Project formulation

B. Adequacy of Measurement

C. Reasons for Using B/C

1. Restrains abuse of political process

2. Promotes scientific understanding of physical and social problems

3. Helps broaden repayment base

4. Helps obtain dependable repayment contracts

5. Helps make public districts and special taxes more palatable.