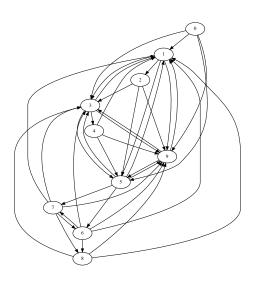
Boost.Graph Cookbook 1: Basics

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1 Introduction

This is 'Boost.Graph Cookbook 1: Basics' (formerly: 'A well-connected C++14 Boost.Graph tutorial'), version 3.0.

1.1 Why this tutorial

I needed this tutorial already in 2006, when I started experimenting with Boost.Graph. More specifically, I needed a tutorial that:

- Orders concepts chronologically
- Increases complexity gradually
- Shows complete pieces of code

What I had were the book [8] and the Boost.Graph website, both did not satisfy these requirements.

1.2 Tutorial style

Readable for beginners This tutorial is aimed at the beginner programmer. This tutorial is intended to take the reader to the level of understanding the book [8] and the Boost.Graph website require. It is about basic graph manipulation, not the more advanced graph algorithms.

High verbosity This tutorial is intended to be as verbose, such that a beginner should be able to follow every step, from reading the tutorial from beginning to end chronologically. Especially in the earlier chapters, the rationale behind the code presented is given, including references to the literature. Chapters marked with '\(\bigsim\)' are optional, less verbose and bring no new information to the storyline.

Repetitiveness This tutorial is intended to be as repetitive, such that a beginner can spot the patterns in the code snippets their increasing complexity. Extending code from this tutorial should be as easy as extending the patterns.

Index In the index, I did first put all my long-named functions there literally, but this resulted in a very sloppy layout. Instead, the function 'do_something' can be found as 'Do something' in the index. On the other hand, STL and Boost functions like 'std::do_something' and 'boost::do_something' can be found as such in the index.

1.3 Coding style

Concept For every concept, I will show

- a function that achieves a goal, for example 'create empty undirected graph'
- a test case of that function, that demonstrates how to use the function, for example 'create_empty_undirected_graph_test'

C++14 All coding snippets are taken from compiled and tested C++14 code. I chose to use C++14 because it was available to me on all local and remote computers. Next to this, it makes code even shorter then just C++11.

Coding standard I use the coding style from the Core C++ Guidelines. At the time of this writing, the Core C++ Guidelines were still in early development, so I can only hope the conventions I then chose to follow are still Good Ideas.

No comments in code It is important to add comments to code. In this tutorial, however, I have chosen not to put comments in code, as I already describe the function in the tutorial its text. This way, it prevents me from saying the same things twice.

Trade-off between generic code and readability It is good to write generic code. In this tutorial, however, I have chosen my functions to have no templated arguments for conciseness and readability. For example, a vertex name is std::string, the type for if a vertex is selected is a boolean, and the custom vertex type is of type 'my_custom_vertex'. I think these choices are reasonable and that the resulting increase in readability is worth it.

Long function names I enjoy to show concepts by putting those in (long-named) functions. These functions sometimes border the trivial, by, for example, only calling a single Boost.Graph function. On the other hand, these functions have more English-sounding names, resulting in demonstration code that is readable. Additionally, they explicitly mention their return type (in a simpler way), which may be considered informative.

Long function names and readability Due to my long function names and the limitation of ≈ 50 characters per line, sometimes the code does get to look a bit awkward. I am sorry for this.

Use of auto I prefer to use the keyword auto over doubling the lines of code for using statements. Often the 'do' functions return an explicit data type, these can be used for reference. Sometime I deduce the return type using decltype and a function with the same return type. When C++17 gets accessible, I will use 'decltype(auto)'. If you really want to know a type, you can use the 'get_type_name' function (chapter 11.1).

Explicit use of namespaces On the other hand, I am explicit in the namespaces of functions and classes I use, so to distinguish between types like 'std::array' and 'boost::array'. Some functions (for example, 'get') reside in the namespace of the graph to work on. In this tutorial, this is in the global namespace. Thus, I will write 'get', instead of 'boost::get', as the latter does not compile.

Use of STL algorithms I try to use STL algorithms wherever I can. Also you should prefer algorithm calls over hand-written for-loops ([9] chapter 18.12.1, [7] item 43). Sometimes using these algorithms becomes a burden on the lines of code. This is because in C++11, a lambda function argument (use by the algorithm) must have its data type specified. It may take multiple lines of 'using' statements being able to do so. In C++14 one can use 'auto' there as well. So, only if it shortens the number of lines significantly, I use raw for-loops, even though you shouldn't.

Re-use of functions The functions I develop in this tutorial are re-used from that moment on. This improves to readability of the code and decreases the number of lines.

Tested to compile All functions in this tutorial are tested to compile using Travis CI in both debug and release mode.

Tested to work All functions in this tutorial are tested, using the Boost.Test library. Travis CI calls these tests after each push to the repository.

Availability The code, as well as this tutorial, can be downloaded from the GitHub at www.github.com/richelbilderbeek/boost_graph_cookbook_1.

1.4 License

This tutorial is licensed under Creative Commons license 4.0. All C++ code is licensed under GPL 3.0.



Figure 1: Creative Commons license 4.0

1.5 Feedback

This tutorial is not intended to be perfect yet. For that, I need help and feedback from the community. All referenced feedback is welcome, as well as any constructive feedback.

I have tried hard to strictly follow the style as described above. If you find I deviated from these decisions somewhere, I would be grateful if you'd let know. Next to this, there are some sections that need to be coded or have its code improved.

1.6 Acknowledgements

These are users that improved this tutorial and/or the code behind this tutorial, in chronological order:

- m-dudley, http://stackoverflow.com/users/111327/m-dudley
- E. Kawashima
- mat69, https://www.reddit.com/user/mat69
- danielhj, https://www.reddit.com/user/danieljh
- sehe, http://stackoverflow.com/users/85371/sehe

- cv and me, http://stackoverflow.com/users/2417774/cv-and-he
- mywtfmp3

1.7 Outline

The chapters of this tutorial are also like a well-connected graph. To allow for quicker learners to skim chapters, or for beginners looking to find the patterns.

The distinction between the chapter is in the type of edges and vertices. They can have:

- no properties: see chapter 2
- have a bundled property: see chapter 4

Pivotal chapters are chapters like 'Finding the first vertex with ...', as this opens up the door to finding a vertex and manipulating it.

All chapters have a rather similar structure in themselves, as depicted in figure 2.

There are also some bonus chapters, that I have labeled with a '▶'. These chapters are added I needed these functions myself and adding them would not hurt. Just feel free to skip them, as there will be less theory explained.

2 Building graphs without properties

Boost.Graph is about creating graphs. In this chapter we create the simplest of graphs, in which edges and nodes have no properties (e.g. having a name).

Still, there are two types of graphs that can be constructed: undirected and directed graphs. The difference between directed and undirected graphs is in the edges: in an undirected graph, an edge connects two vertices without any directionality, as displayed in figure 3. In a directed graph, an edge goes from a certain vertex, its source, to another (which may actually be the same), its target. A directed graph is shown in figure 4.

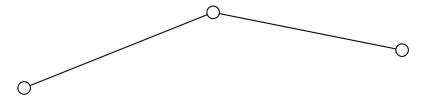


Figure 3: Example of an undirected graph

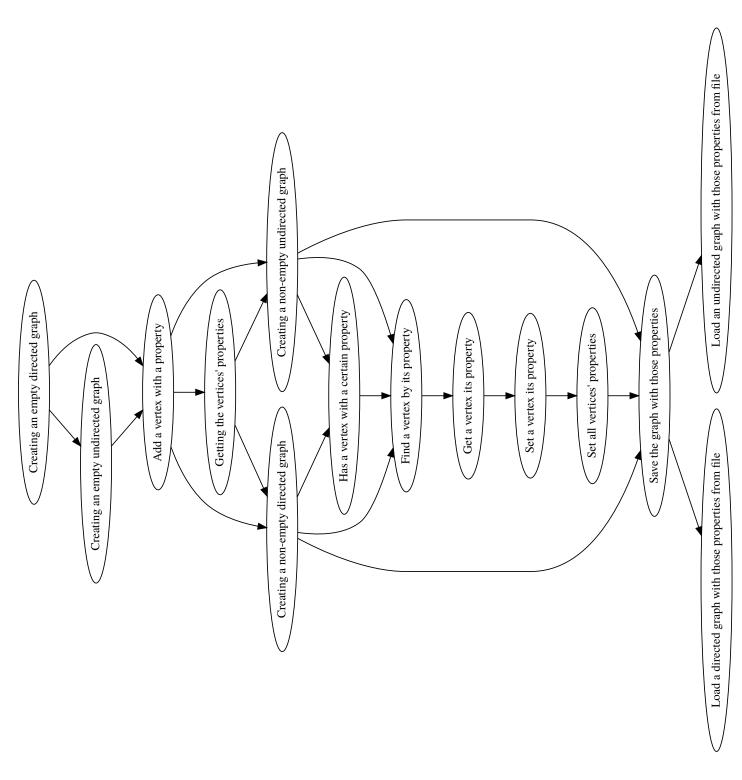


Figure 2: The relations between sub-chapters

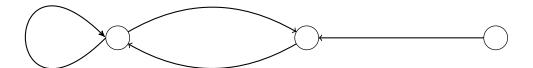


Figure 4: Example of a directed graph

In this chapter, we will build two directed and two undirected graphs:

- An empty (directed) graph, which is the default type: see chapter 2.1
- An empty (undirected) graph: see chapter 2.2
- A two-state Markov chain, a directed graph with two vertices and four edges, chapter 2.14
- K_2 , an undirected graph with two vertices and one edge, chapter 2.15

Creating an empty graph may sound trivial, it is not, thanks to the versatility of the Boost.Graph library.

In the process of creating graphs, some basic (sometimes bordering trivial) functions are encountered:

- Counting the number of vertices: see chapter 2.3
- Counting the number of edges: see chapter 2.4
- Adding a vertex: see chapter 2.5
- Getting all vertices: see chapter 2.7
- Getting all vertex descriptors: see chapter 2.8
- Adding an edge: see chapter 2.9
- Getting all edges: see chapter 2.11
- Getting all edge descriptors: see chapter 2.13

These functions are mostly there for completion and showing which data types are used.

The chapter also introduces some important concepts:

- Vertex descriptors: see chapter 2.6
- Edge insertion result: see chapter 2.10
- Edge descriptors: see chapter 2.12

After this chapter you may want to:

- Building graphs with named vertices: see chapter ??
- Building graphs with bundled vertices: see chapter 4
- Building graphs with custom vertices: see chapter ??
- Building graphs with a graph name: see chapter 8

2.1 Creating an empty (directed) graph

Let's create an empty graph!

Algorithm 1 shows the function to create an empty graph.

Algorithm 1 Creating an empty (directed) graph

```
#include <boost/graph/adjacency_list.hpp>
boost::adjacency_list <>
create_empty_directed_graph() noexcept
{
   return {};
}
```

The code consists out of an #include and a function definition. The #include tells the compiler to read the header file 'adjacency_list.hpp'. A header file (often with a '.h' or '.hpp' extension) contains class and functions declarations and/or definitions. The header file 'adjacency_list.hpp' contains the boost::adjacency_list class definition. Without including this file, you will get compile errors like 'definition of boost::adjacency_list unknown'. The function 'create_empty_directed_graph' has:

- a return type: The return type is 'boost::adjacency_list<>>', that is a 'boost::adjacency_list' with all template arguments set at their defaults
- a noexcept specification: the function should not throw³, so it is preferred to mark it noexcept ([10] chapter 13.7).

²In practice, these compiler error messages will be longer, bordering the unreadable ³if the function would throw because it cannot allocate this little piece of memory, you are already in big trouble

• a function body: all the function body does is implicitly create its return type by using the '{}'. An alternative syntax would be 'return boost::adjacency list<>()', which is needlessly longer

Algorithm 2 demonstrates the 'create_empty_directed_graph' function. This demonstration is embedded within a Boost.Test unit test case. It includes a Boost.Test header to allow to use the Boost.Test framework. Additionally, a header file is included with the same name as the function⁴. This allows use to be able to use the function. The test case creates an empty graph and stores it. Instead of specifying the data type explicitly, 'auto' is used (this is preferred, [10] chapter 31.6), which lets the compiler figure out the type itself.

Algorithm 2 Demonstration of 'create_empty_directed_graph'

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph.h"

BOOST_AUTO_TEST_CASE(test_create_empty_directed_graph)
{
   const auto g = create_empty_directed_graph();
   BOOST_CHECK(boost::is_directed(g));
}
```

Congratulations, you've just created a boost::adjacency_list with its default template arguments. The boost::adjacency_list is the most commonly used graph type, the other is the boost::adjacency_matrix. We do not do anything with it yet, but still, you've just created a graph, in which:

- The out edges and vertices are stored in a std::vector
- The edges have a direction
- The vertices, edges and graph have no properties
- The edges are stored in a std::list

It stores its edges, out edges and vertices in a two different STL⁵ containers. std::vector is the container you should use by default ([10] chapter 31.6, [11] chapter 76), as it has constant time look-up and back insertion. The std::list is used for storing the edges, as it is better suited at inserting elements at any position.

I use const to store the empty graph as we do not modify it. Correct use of const is called const-correct. Prefer to be const-correct ([9] chapter 7.9.3, [10] chapter 12.7, [7] item 3, [3] chapter 3, [11] item 15, [2] FAQ 14.05, [1] item 8, [4] 9.1.6).

⁴I do not think it is important to have creative names

⁵Standard Template Library, the standard library

2.2 Creating an empty undirected graph

Let's create another empty graph! This time, we even make it undirected! Algorithm 3 shows how to create an undirected graph.

Algorithm 3 Creating an empty undirected graph

```
#include <boost/graph/adjacency_list.hpp>
boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::undirectedS
>
create_empty_undirected_graph() noexcept
{
   return {};
}
```

This algorithm differs from the 'create_empty_directed_graph' function (algorithm 1) in that there are three template arguments that need to be specified in the creation of the boost::adjacency_list:

- the first 'boost::vecS': select (that is what the 'S' means) that out edges are stored in a std::vector. This is the default way.
- the second 'boost::vecS': select that the graph vertices are stored in a std::vector. This is the default way.
- 'boost::undirectedS': select that the graph is undirected. This is all we needed to change. By default, this argument is boost::directed

Algorithm 4 demonstrates the 'create_empty_undirected_graph' function.

Algorithm 4 Demonstration of 'create empty undirected graph'

```
#include <boost/test/unit_test.hpp>
#include "create_empty_undirected_graph.h"

BOOST_AUTO_TEST_CASE(test_create_empty_undirected_graph)
{
    const auto g = create_empty_undirected_graph();
    BOOST_CHECK(boost::is_undirected(g));
}
```

Congratulations, with algorithm 4, you've just created an undirected graph in which:

- The out edges and vertices are stored in a std::vector
- The graph is undirected
- Vertices, edges and graph have no properties
- Edges are stored in a std::list

2.3 Counting the number of vertices

Let's count all zero vertices of an empty graph!

Algorithm 5 Count the number of vertices

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
int get_n_vertices(const graph& g) noexcept
{
   const int n{
      static_cast<int>(boost::num_vertices(g))
   };
   assert(static_cast<unsigned long>(n)
      == boost::num_vertices(g)
   );
   return n;
}
```

The function 'get_n_vertices' takes the result of boost::num_vertices, converts it to int and checks if there was conversion error. We do so, as one should prefer using signed data types over unsigned ones in an interface ([4] chapter 9.2.2). To do so, in the function body its first statement, the unsigned long produced by boost::num_vertices get converted to an int using a static_cast. Using an unsigned integer over a (signed) integer for the sake of gaining that one more bit ([9] chapter 4.4) should be avoided. The integer 'n' is initialized using list-initialization, which is preferred over the other initialization syntaxes ([10] chapter 17.7.6).

The assert checks if the conversion back to unsigned long re-creates the original value, to check if no information has been lost. If information is lost, the program crashes. Use assert extensively ([9] chapter 24.5.18, [10] chapter 30.5, [11] chapter 68, [6] chapter 8.2, [5] hour 24, [4] chapter 2.6).

The function 'get_n_vertices' is demonstrated in algorithm 6, to measure the number of vertices of both the directed and undirected graph we are already able to create.

Algorithm 6 Demonstration of the 'get n vertices' function

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_n_vertices.h"

BOOST_AUTO_TEST_CASE(test_get_n_vertices)
{
    const auto g = create_empty_directed_graph();
    BOOST_CHECK(get_n_vertices(g) == 0);

    const auto h = create_empty_undirected_graph();
    BOOST_CHECK(get_n_vertices(h) == 0);
}
```

Note that the type of graph does not matter here. One can count the number of vertices of every graph, as all graphs have vertices. Boost.Graph is very good at detecting operations that are not allowed, during compile time.

2.4 Counting the number of edges

Let's count all zero edges of an empty graph!

This is very similar to the previous chapter, only it uses boost::num_edges instead:

Algorithm 7 Count the number of edges

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
int get_n_edges(const graph& g) noexcept
{
   const int n{
      static_cast<int>(boost::num_edges(g))
   };
   assert(static_cast<unsigned long>(n)
      = boost::num_edges(g)
   );
   return n;
}
```

This code is similar to the 'get_n_vertices' function (algorithm 5, see rationale there) except 'boost::num_edges' is used, instead of 'boost::num_vertices',

which also returns an unsigned long.

The function 'get_n_edges' is demonstrated in algorithm 8, to measure the number of edges of an empty directed and undirected graph.

Algorithm 8 Demonstration of the 'get n edges' function

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_n_edges.h"

BOOST_AUTO_TEST_CASE(test_get_n_edges)
{
    const auto g = create_empty_directed_graph();
    BOOST_CHECK(get_n_edges(g) == 0);

    const auto h = create_empty_undirected_graph();
    BOOST_CHECK(get_n_edges(h) == 0);
}
```

2.5 Adding a vertex

Empty graphs are nice, now its time to add a vertex!

To add a vertex to a graph, the boost::add_vertex function is used as shows in algorithm 9:

Algorithm 9 Adding a vertex to a graph

The static_assert at the top of the function checks during compiling if the function is called with a non-const graph. One can freely omit this static_assert: you will get a compiler error anyways, be it a less helpful one.

Note that boost::add_vertex (in the 'add_vertex' function) returns a vertex descriptor, which is ignored for now. Vertex descriptors are looked at in more details at the chapter 2.6, as we need these to add an edge. To allow for this already, 'add_vertex' also returns a vertex descriptor.

Algorithm 10 shows how to add a vertex to a directed and undirected graph.

Algorithm 10 Demonstration of the 'add vertex' function

```
#include <boost/test/unit_test.hpp>
#include "add_vertex.h"
#include "create_empty_directed_graph.h"

BOOST_AUTO_TEST_CASE(test_add_vertex)
{
    auto g = create_empty_undirected_graph();
    add_vertex(g);
    BOOST_CHECK(boost::num_vertices(g) == 1);

    auto h = create_empty_directed_graph();
    add_vertex(h);
    BOOST_CHECK(boost::num_vertices(h) == 1);
}
```

This demonstration code creates two empty graphs, adds one vertex to each and then asserts that the number of vertices in each graph is one. This works for both types of graphs, as all graphs have vertices.

2.6 Vertex descriptors

A vertex descriptor is a handle to a vertex within a graph.

Vertex descriptors can be obtained by dereferencing a vertex iterator (see chapter 2.8). To do so, we first obtain some vertex iterators in chapter 2.7).

Vertex descriptors are used to:

- add an edge between two vertices, see chapter 2.9
- obtain properties of vertex a vertex, for example the vertex its out degrees (chapter 3.1), the vertex its name (chapter ??), or a custom vertex property (chapter ??)

In this tutorial, vertex descriptors have named prefixed with 'vd_', for example 'vd_1'.

2.7 Get the vertex iterators

You cannot get the vertices. This may sound unexpected, as it must be possible to work on the vertices of a graph. Working on the vertices of a graph is done through these steps:

- Obtain a vertex iterator pair from the graph
- Dereferencing a vertex iterator to obtain a vertex descriptor

'vertices' (not 'boost::vertices') is used to obtain a vertex iterator pair, as shown in algorithm 11. The first vertex iterator points to the first vertex (its descriptor, to be precise), the second points to beyond the last vertex (its descriptor, to be precise). In this tutorial, vertex iterator pairs have named prefixed with 'vip_', for example 'vip_1'.

Algorithm 11 Get the vertex iterators of a graph

```
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
std::pair <
   typename graph::vertex_iterator,
   typename graph::vertex_iterator
>
get_vertex_iterators(const graph& g) noexcept
{
   return vertices(g);
}
```

This is a somewhat trivial function, as it forwards the function call to 'vertices' (not 'boost::vertices').

These vertex iterators can be dereferenced to obtain the vertex descriptors. Note that 'get_vertex_iterators' will not be used often in isolation: usually one obtains the vertex descriptors immediately. Just for your reference, algorithm 12 demonstrates of the 'get_vertices' function, by showing that the vertex iterators of an empty graph point to the same location.

Algorithm 12 Demonstration of 'get_vertex_iterators'

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_vertex_iterators.h"

BOOST_AUTO_TEST_CASE(test_get_vertex_iterators)
{
    const auto g = create_empty_undirected_graph();
    const auto vip_g = get_vertex_iterators(g);
    BOOST_CHECK(vip_g.first == vip_g.second);

    const auto h = create_empty_directed_graph();
    const auto vip_h = get_vertex_iterators(h);
    BOOST_CHECK(vip_h.first == vip_h.second);
}
```

2.8 Get all vertex descriptors

Vertex descriptors are the way to manipulate those vertices. Let's go get the all!

Vertex descriptors are obtained from dereferencing vertex iterators. Algorithm 13 shows how to obtain all vertex descriptors from a graph.

Algorithm 13 Get all vertex descriptors of a graph

```
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph_traits.hpp>

template <typename graph>
std::vector<
    typename boost::graph_traits<graph>::vertex_descriptor
>
get_vertex_descriptors(const graph& g) noexcept
{
    using vd = typename graph::vertex_descriptor;

    std::vector<vd> vds(boost::num_vertices(g));
    const auto vis = vertices(g);
    std::copy(vis.first, vis.second, std::begin(vds));
    return vds;
}
```

This is the first more complex piece of code. In the first lines, some 'using' statements allow for shorter type names⁶.

The std::vector to serve as a return value is created at the needed size, which is the number of vertices.

The function 'vertices' (not boost::vertices!) returns a vertex iterator pair. These iterators are used by std::copy to iterator over. std::copy is an STL algorithm to copy a half-open range. Prefer algorithm calls over hand-written for-loops ([9] chapter 18.12.1, [7] item 43).

In this case, we copy all vertex descriptors in the range produced by 'vertices' to the std::vector.

This function will not be used in practice: one iterates over the vertices directly instead, saving the cost of creating a std::vector. This function is only shown as an illustration.

Algorithm 14 demonstrates that an empty graph has no vertex descriptors:

Algorithm 14 Demonstration of 'get_vertex_descriptors'

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_vertex_descriptors.h"

BOOST_AUTO_TEST_CASE(test_get_vertex_descriptors)
{
    const auto g = create_empty_undirected_graph();
    const auto vds_g = get_vertex_descriptors(g);
    BOOST_CHECK(vds_g.empty());

    const auto h = create_empty_directed_graph();
    const auto vds_h = get_vertex_descriptors(h);
    BOOST_CHECK(vds_h.empty());
}
```

Because all graphs have vertices and thus vertex descriptors, the type of graph is unimportant for this code to compile.

2.9 Add an edge

To add an edge to a graph, two vertex descriptors are needed. A vertex descriptor is a handle to the vertex within a graph (vertex descriptors are looked at in more details in chapter 2.6). Algorithm 15 adds two vertices to a graph, and connects these two using boost::add edge:

⁶which may be necessary just to create a tutorial with code snippets that are readable

Algorithm 15 Adding (two vertices and) an edge to a graph

```
#include <type_traits>
#include <typename graph/adjacency_list.hpp>

template <typename graph>
typename boost::graph_traits<graph>::edge_descriptor
add_edge(graph& g) noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);
    const auto vd_a = boost::add_vertex(g);
    const auto vd_b = boost::add_vertex(g);
    const auto aer = boost::add_edge(
        vd_a, vd_b, g
);
    assert(aer.second);
    return aer.first;
}
```

Algorithm 15 shows how to add an isolated edge to a graph (instead of allowing for graphs with higher connectivities). First, two vertices are created, using the function 'boost::add_vertex'. 'boost::add_vertex' returns a vertex descriptor (which I prefix with 'vd'), both of which are stored. The vertex descriptors are used to add an edge to the graph, using 'boost::add_edge'. 'boost::add_edge' returns a std::pair, consisting of an edge descriptor and a boolean success indicator. The success of adding the edge is checked by an assert statement. Here we assert that this insertion was successful. Insertion can fail if an edge is already present and duplicates are not allowed.

A demonstration of add_edge is shown in algorithm 16, in which an edge is added to both a directed and undirected graph, after which the number of edges and vertices is checked.

Algorithm 16 Demonstration of 'add edge'

```
#include <boost/test/unit_test.hpp>
#include "add_edge.h"
#include "create_empty_directed_graph.h"

BOOST_AUTO_TEST_CASE(test_add_edge)
{
    auto g = create_empty_undirected_graph();
    add_edge(g);
    BOOST_CHECK(boost::num_vertices(g) == 2);
    BOOST_CHECK(boost::num_edges(g) == 1);

auto h = create_empty_directed_graph();
    add_edge(h);
    BOOST_CHECK(boost::num_vertices(h) == 2);
    BOOST_CHECK(boost::num_vertices(h) == 2);
    BOOST_CHECK(boost::num_edges(h) == 1);
}
```

The graph type is unimportant: as all graph types have vertices and edges, edges can be added without possible compile problems.

2.10 boost::add edge result

When using the function 'boost::add_edge', a 'std::pair<edge_descriptor,bool>' is returned. It contains both the edge descriptor (see chapter 2.12) and a boolean, which indicates insertion success.

In this tutorial, boost::add_edge results have named prefixed with 'aer_', for example 'aer_1'.

2.11 Getting the edge iterators

You cannot get the edges directly. Instead, working on the edges of a graph is done through these steps:

- Obtain an edge iterator pair from the graph
- Dereference an edge iterator to obtain an edge descriptor

'edges' (not boost::edges!) is used to obtain an edge iterator pair. The first edge iterator points to the first edge (its descriptor, to be precise), the second points to beyond the last edge (its descriptor, to be precise). In this tutorial, edge iterator pairs have named prefixed with 'eip_', for example 'eip_1'. Algorithm 17 shows how to obtain these:

Algorithm 17 Get the edge iterators of a graph

```
#include <boost/graph/adjacency_list.hpp>
template <typename graph>
std::pair <
   typename graph::edge_iterator,
   typename graph::edge_iterator
>
get_edge_iterators(const graph& g) noexcept
{
   return edges(g);
}
```

This is a somewhat trivial function, as all it does is forward to function call to 'edges' (not boost::edges!) These edge iterators can be dereferenced to obtain the edge descriptors. Note that this function will not be used often in isolation: usually one obtains the edge descriptors immediately.

Algorithm 18 demonstrates 'get_edge_iterators' by showing that both iterators of the edge iterator pair point to the same location, when the graph is empty.

Algorithm 18 Demonstration of 'get edge iterators'

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_edge_iterators.h"

BOOST_AUTO_TEST_CASE(test_get_edge_iterators)
{
    const auto g = create_empty_undirected_graph();
    const auto eip_g = get_edge_iterators(g);
    BOOST_CHECK(eip_g.first == eip_g.second);

auto h = create_empty_directed_graph();
    const auto eip_h = get_edge_iterators(h);
    BOOST_CHECK(eip_h.first == eip_h.second);
}
```

2.12 Edge descriptors

An edge descriptor is a handle to an edge within a graph. They are similar to vertex descriptors (chapter 2.6).

Edge descriptors are used to obtain the name, or other properties, of an edge In this tutorial, edge descriptors have named prefixed with 'ed_', for example 'ed 1'.

2.13 Get all edge descriptors

Obtaining all edge descriptors is similar to obtaining all vertex descriptors (algorithm 13), as shown in algorithm 19:

Algorithm 19 Get all edge descriptors of a graph

```
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include "boost/graph/graph_traits.hpp"

template <typename graph>
std::vector<
    typename boost::graph_traits<graph>::edge_descriptor
> get_edge_descriptors(const graph& g) noexcept
{
    using boost::graph_traits;
    using ed = typename graph_traits<graph>::
        edge_descriptor;
    std::vector<ed> v(boost::num_edges(g));
    const auto eip = edges(g);
    std::copy(eip.first, eip.second, std::begin(v));
    return v;
}
```

The only difference is that instead of the function 'vertices' (not boost::vertices!), 'edges' (not boost::edges!) is used.

Algorithm 20 demonstrates the 'get_edge_descriptor', by showing that empty graphs do not have any edge descriptors.

Algorithm 20 Demonstration of get edge descriptors

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_edge_descriptors.h"

BOOST_AUTO_TEST_CASE(test_get_edge_descriptors)
{
    const auto g = create_empty_directed_graph();
    const auto eds_g = get_edge_descriptors(g);
    BOOST_CHECK(eds_g.empty());

    const auto h = create_empty_undirected_graph();
    const auto eds_h = get_edge_descriptors(h);
    BOOST_CHECK(eds_h.empty());
}
```

2.14 Creating a directed graph

Finally, we are going to create a directed non-empty graph!

2.14.1 Graph

This directed graph is a two-state Markov chain, with two vertices and four edges, as depicted in figure 5:

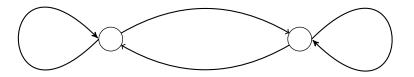


Figure 5: The two-state Markov chain

Note that directed graphs can have edges that start and end in the same vertex. These are called self-loops.

2.14.2 Function to create such a graph

To create this two-state Markov chain, the following code can be used:

Algorithm 21 Creating the two-state Markov chain as depicted in figure 5

```
#include <cassert>
#include "create_empty_directed_graph.h"

boost::adjacency_list <>
create_markov_chain() noexcept
{
   auto g = create_empty_directed_graph();
   const auto vd_a = boost::add_vertex(g);
   const auto vd_b = boost::add_vertex(g);
   boost::add_edge(vd_a, vd_a, g);
   boost::add_edge(vd_a, vd_b, g);
   boost::add_edge(vd_b, vd_a, g);
   boost::add_edge(vd_b, vd_a, g);
   boost::add_edge(vd_b, vd_b, g);
   return g;
}
```

Instead of typing the complete type, we call the 'create_empty_directed_graph' function, and let auto figure out the type. The vertex descriptors (see chapter 2.6) created by two boost::add_vertex calls are stored to add an edge to the graph. Then boost::add_edge is called four times. Every time, its return type (see chapter 2.10) is checked for a successful insertion.

Note that the graph lacks all properties: nodes do not have names, nor do edges.

2.14.3 Creating such a graph

Algorithm 22 demonstrates the 'create_markov_chain_graph' function and checks if it has the correct amount of edges and vertices:

Algorithm 22 Demonstration of the 'create markov chain'

```
#include <boost/test/unit_test.hpp>
#include "create_markov_chain.h"

BOOST_AUTO_TEST_CASE(test_create_markov_chain)
{
   const auto g = create_markov_chain();
   BOOST_CHECK(boost::num_vertices(g) == 2);
   BOOST_CHECK(boost::num_edges(g) == 4);
}
```

2.14.4 The .dot file produced

Running a bit ahead, this graph can be converted to a .dot file using the 'save_graph_to_dot' function (algorithm 55). The .dot file created is displayed in algorithm 23:

Algorithm 23 .dot file created from the 'create_markov_chain_graph' function (algorithm 21), converted from graph to .dot file using algorithm 55

```
digraph G {
0;
1;
0->0;
0->1;
1->0;
1->1;
1->1;
```

From the .dot file one can already see that the graph is directed, because:

- The first word, 'digraph', denotes a directed graph (where 'graph' would have indicated an undirected graph)
- The edges are written as '->' (where undirected connections would be written as '-')

2.14.5 The .svg file produced

The .svg file of this graph is shown in figure 6:

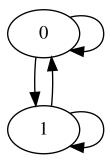


Figure 6: .svg file created from the 'create_markov_chain' function (algorithm 21) its .dot file and converted from .dot file to .svg using algorithm 136

This figure shows that the graph in directed, as the edges have arrow heads. The vertices display the node index, which is the default behavior.

2.15 Creating K_2 , a fully connected undirected graph with two vertices

Finally, we are going to create an undirected non-empty graph!

2.15.1 Graph

To create a fully connected undirected graph with two vertices (also called K_2), one needs two vertices and one (undirected) edge, as depicted in figure 7.



Figure 7: K_2 : a fully connected undirected graph with two vertices

2.15.2 Function to create such a graph

To create K_2 , the following code can be used:

Algorithm 24 Creating K_2 as depicted in figure 7

```
#include "create_empty_undirected_graph.h"

boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::undirectedS

create_k2_graph() noexcept
{
   auto g = create_empty_undirected_graph();
   const auto vd_a = boost::add_vertex(g);
   const auto vd_b = boost::add_vertex(g);
   boost::add_edge(vd_a, vd_b, g);
   return g;
}</pre>
```

This code is very similar to the 'add_edge' function (algorithm 15). Instead of typing the graph its type, we call the 'create_empty_undirected_graph' function and let auto figure it out. The vertex descriptors (see chapter 2.6) created by two boost::add_vertex calls are stored to add an edge to the graph. From boost::add_edge its return type (see chapter 2.10), it is only checked that insertion has been successful.

Note that the graph lacks all properties: nodes do not have names, nor do edges.

2.15.3 Creating such a graph

Algorithm 25 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 25 Demonstration of 'create k2 graph'

```
#include <boost/test/unit_test.hpp>
#include "create_k2_graph.h"

BOOST_AUTO_TEST_CASE(test_create_k2_graph)
{
   const auto g = create_k2_graph();
   BOOST_CHECK(boost::num_vertices(g) == 2);
   BOOST_CHECK(boost::num_edges(g) == 1);
}
```

2.15.4 The .dot file produced

Running a bit ahead, this graph can be converted to the .dot file as shown in algorithm 26:

Algorithm 26 .dot file created from the 'create_k2_graph' function (algorithm 24), converted from graph to .dot file using algorithm 55

```
graph G {
0;
1;
0--1;
}
```

From the .dot file one can already see that the graph is undirected, because:

- The first word, 'graph', denotes an undirected graph (where 'digraph' would have indicated a directional graph)
- The edge between 0 and 1 is written as '-' (where directed connections would be written as '->', '<-' or '<>')

2.15.5 The .svg file produced

Continuing to running a bit ahead, this .dot file can be converted to the .svg as shown in figure 8:

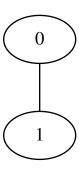


Figure 8: .svg file created from the 'create_k2_graph' function (algorithm 24) its .dot file, converted from .dot file to .svg using algorithm 136

Also this figure shows that the graph in undirected, otherwise the edge would have one or two arrow heads. The vertices display the node index, which is the default behavior.

2.16 \triangleright Creating K_3 , a fully connected undirected graph with three vertices

This is an extension of the previous chapter

2.16.1 Graph

To create a fully connected undirected graph with two vertices (also called K_2), one needs two vertices and one (undirected) edge, as depicted in figure 9.

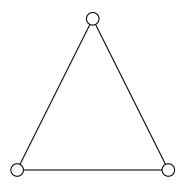


Figure 9: K_3 : a fully connected graph with three edges and vertices

2.16.2 Function to create such a graph

To create K_3 , the following code can be used:

Algorithm 27 Creating K_3 as depicted in figure 9

```
#include <cassert>
#include "create_empty_undirected_graph.h"
#include "create k3 graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
create k3 graph() noexcept
  auto g = create_empty_undirected_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto vd c = boost::add_vertex(g);
  boost::add edge(vd a, vd b, g);
  boost::add\_edge(vd\_b, vd\_c, g);
  boost::add edge(vd c, vd a, g);
  return g;
}
```

2.16.3 Creating such a graph

Algorithm 28 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 28 Demonstration of 'create_k3_graph'

```
#include <boost/test/unit_test.hpp>
#include "create_k3_graph.h"

BOOST_AUTO_TEST_CASE(test_create_k3_graph)
{
   const auto g = create_k3_graph();
   BOOST_CHECK(boost::num_edges(g) == 3);
   BOOST_CHECK(boost::num_vertices(g) == 3);
}
```

2.16.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 29:

Algorithm 29 .dot file created from the 'create_k3_graph' function (algorithm 27), converted from graph to .dot file using algorithm 55

```
graph G {
0;
1;
2;
0--1;
1--2;
2--0;
}
```

2.16.5 The .svg file produced

Continuing to running a bit ahead, this .dot file can be converted to the .svg as shown in figure 10:

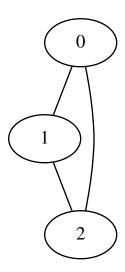


Figure 10: .svg file created from the 'create_k3_graph' function (algorithm 27) its .dot file, converted from .dot file to .svg using algorithm 136

2.17 Creating a path graph

A path graph is a linear graph without any branches

2.17.1 Graph

Here I show a path graph with four vertices (see figure 11):



Figure 11: A path graph with four vertices

2.17.2 Function to create such a graph

To create a path graph, the following code can be used:

Algorithm 30 Creating a path graph as depicted in figure 11

```
#include "create empty undirected graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
create path graph (const size t n vertices) noexcept
  auto g = create empty undirected graph();
  if (n_vertices == 0) return g;
  auto vd 1 = boost :: add vertex(g);
  if (n vertices == 1) return g;
  for (size t i=1; i!=n vertices; ++i)
    auto vd_2 = boost :: add_vertex(g);
    boost::add_edge(vd_1, vd_2, g);
    vd_1 = vd_2;
  }
  return g;
```

2.17.3 Creating such a graph

Algorithm 31 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 31 Demonstration of 'create path graph'

```
#include <boost/test/unit_test.hpp>
#include "create_path_graph.h"

BOOST_AUTO_TEST_CASE(test_create_path_graph)
{
   const auto g = create_path_graph(4);
   BOOST_CHECK(boost::num_edges(g) == 3);
   BOOST_CHECK(boost::num_vertices(g) == 4);
}
```

2.17.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 32:

Algorithm 32 .dot file created from the 'create_path_graph' function (algorithm 30), converted from graph to .dot file using algorithm 55

```
graph G {
0;
1;
2;
3;
0--1;
1--2;
2--3;
}
```

2.17.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 12:

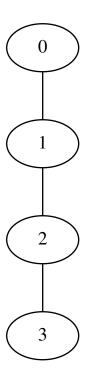


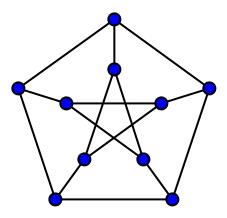
Figure 12: .svg file created from the 'create_path_graph' function (algorithm 30) its .dot file, converted from .dot file to .svg using algorithm 136

2.18 ► Creating a Peterson graph

A Petersen graph is the first graph with interesting properties.

2.18.1 Graph

To create a Petersen graph, one needs five vertices and five undirected edges, as depicted in figure 13.



 $\label{eq:figure 13: A Petersen graph (from https://en.wikipedia.org/wiki/Petersen_graph)} \\$

2.18.2 Function to create such a graph

To create a Petersen graph, the following code can be used:

Algorithm 33 Creating Petersen graph as depicted in figure 13

```
#include <cassert>
#include <vector>
#include "create empty undirected graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
create petersen graph() noexcept
  using vd = decltype(create_empty_undirected_graph())::
     vertex descriptor;
  auto g = create empty undirected graph();
  std :: vector < vd > v; //Outer
  for (int i=0; i!=5; ++i) {
    v.push_back(boost::add_vertex(g));
  std::vector<vd> w; //Inner
  for (int i=0; i!=5; ++i) {
    w.push back(boost::add vertex(g));
  //Outer ring
  for (int i=0; i!=5; ++i) {
    boost:: add edge(v[i], v[(i + 1) \% 5], g);
  //Spoke
  for (int i=0; i!=5; ++i) {
    boost::add_edge(v[i], w[i], g);
  //Inner pentagram
  for (int i=0; i!=5; ++i) {
    boost::add_edge(w[i], w[(i + 2) % 5], g);
  return g;
}
```

2.18.3 Creating such a graph

Algorithm 34 demonstrates how to use 'create_petersen_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 34 Demonstration of 'create_k3_graph'

```
#include <boost/test/unit_test.hpp>
#include "create_petersen_graph.h"

BOOST_AUTO_TEST_CASE(test_create_petersen_graph)
{
   const auto g = create_petersen_graph();
   BOOST_CHECK(boost::num_edges(g) == 15);
   BOOST_CHECK(boost::num_vertices(g) == 10);
}
```

2.18.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 35:

Algorithm 35 .dot file created from the 'create_petersen_graph' function (algorithm 33), converted from graph to .dot file using algorithm 55

```
graph G {
0;
1;
2;
3;
4;
5;
6;
7;
8;
9;
0--1;
1--2 ;
2--3;
3--4;
4--0;
0--5;
1--6;
2--7;
3--8;
4--9;
5--7;
6--8;
7--9;
8--5;
9--6;
}
```

2.18.5 The .svg file produced

This .dot file can be converted to the .svg as shown in figure 14:

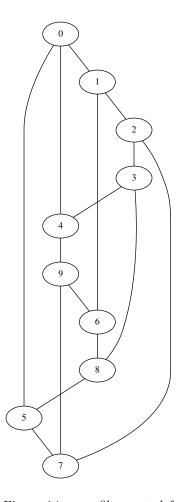


Figure 14: .svg file created from the 'create_petersen_graph' function (algorithm 33) its .dot file, converted from .dot file to .svg using algorithm 136

3 Working on graphs without properties

Now that we can build a graph, there are some things we can do.

- Getting the vertices' out degrees: see chapter 3.1
- Create a direct-neighbour subgraph from a vertex descriptor
- Create all direct-neighbour subgraphs from a graphs
- Saving a graph without properties to .dot file: see chapter 3.11
- $\bullet\,$ Loading an undirected graph without properties from . dot file: see chapter 3.13

 Loading a directed graph without properties from .dot file: see chapter 3.12

3.1 Getting the vertices' out degree

Let's measure the out degree of all vertices in a graph!

The out degree of a vertex is the number of edges that originate at it.

The number of connections is called the 'degree' of the vertex. There are three types of degrees:

- in degree: the number of incoming connections, using 'in_degree' (not 'boost::in_degree')
- out degree: the number of outgoing connections, using 'out_degree' (not 'boost::out degree')
- degree: sum of the in degree and out degree, using 'degree' (not 'boost::degree')

Algorithm 36 shows how to obtain these:

Algorithm 36 Get the vertices' out degrees

```
#include <boost/graph/adjacency_list.hpp>
#include <vector>

template <typename graph>
std::vector<int> get_vertex_out_degrees(
    const graph& g
) noexcept
{
    using vd = typename graph::vertex_descriptor;

    std::vector<int> v(boost::num_vertices(g));
    const auto vip = vertices(g);
    std::transform(vip.first, vip.second, std::begin(v),
        [&g](const vd& d) {
        return out_degree(d,g);
    }
    );
    return v;
}
```

The structure of this algorithm is similar to 'get_vertex_descriptors' (algorithm 13), except that the out degrees from the vertex descriptors are stored. The out degree of a vertex iterator is obtained from the function 'out_degree' (not boost::out_degree!).

Albeit that the K_2 graph and the two-state Markov chain are rather simple, we can use it to demonstrate 'get_vertex_out_degrees' on, as shown in algorithm 37.

Algorithm 37 Demonstration of the 'get vertex out degrees' function

```
#include <boost/test/unit test.hpp>
#include "create k2 graph.h"
#include "create_markov_chain.h"
#include "get vertex out degrees.h"
BOOST AUTO TEST CASE(test get vertex out degrees)
  const auto g = create_k2_graph();
  const std::vector<int> expected_out_degrees_g{1,1};
  const std::vector<int> vertex out degrees g{
    get vertex out degrees(g)
  BOOST CHECK (expected out degrees g
    = vertex_out_degrees_g
  const auto h = create markov chain();
  const std::vector<int> expected out degrees h\{2,2\};
  const std::vector<int> vertex out degrees h{
    get_vertex_out_degrees(h)
  };
 BOOST CHECK (expected out degrees h
    = vertex out degrees h
  );
}
```

It is expected that K_2 has one out-degree for every vertex, where the two-state Markov chain is expected to have two out-degrees per vertex.

3.2 Is there an edge between two vertices?

If you have two vertex descriptors, you can check if these are connected by an edge:

Algorithm 38 Check if there exists an edge between two vertices

```
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph_traits.hpp>

template <typename graph>
bool has_edge_between_vertices(
   const typename boost::graph_traits<graph>::
        vertex_descriptor& vd_1,
   const typename boost::graph_traits<graph>::
        vertex_descriptor& vd_2,
   const graph& g
) noexcept
{
   return edge(vd_1, vd_2, g).second;
}
```

This code uses the function 'edge' (not boost::edge: it returns a pair consisting of an edge descriptor and a boolean indicating if it is a valid edge descriptor. The boolean will be true if there exists an edge between the two vertices and false if not.

The demo shows that there is an edge between the two vertices of a K_2 graph, but there are no self-loops (edges that original and end at the same vertex).

Algorithm 39 Demonstration of the 'has edge between vertices' function

```
#include <boost/test/unit_test.hpp>
#include "create_k2_graph.h"
#include "has_edge_between_vertices.h"

BOOST_AUTO_TEST_CASE(test_has_edge_between_vertices)
{
   const auto g = create_k2_graph();
   const auto vd_1 = *vertices(g).first;
   const auto vd_2 = *(++vertices(g).first);
   BOOST_CHECK( has_edge_between_vertices(vd_1, vd_2, g));
   BOOST_CHECK(!has_edge_between_vertices(vd_1, vd_1, g));
}
```

3.3 Get the edge between two vertices

If you have two vertex descriptors, you can use these to find the edge between them.

Algorithm 40 Get the edge between two vertices

```
#include <boost/graph/adjacency list.hpp>
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
get edge between vertices (
  \mathbf{const} \ \mathbf{typename} \ \mathbf{boost} :: \mathbf{graph\_traits} {<} \mathbf{graph} > ::
       vertex descriptor& vd from,
  \mathbf{const} \ \mathbf{typename} \ \mathbf{boost} :: \mathbf{graph\_traits} {<} \mathbf{graph} > ::
       vertex descriptor& vd to,
  const graph& g
  const auto er = edge(vd from, vd to, g);
   if (!er.second)
     std::stringstream msg;
     \operatorname{msg} << \operatorname{\__func}_{-} << ": \; \; "
        << "no_edge_between_these_vertices"</pre>
     throw std::invalid argument(msg.str());
  return er.first;
}
```

This code does assume that there is an edge between the two vertices.

The demo shows how to get the edge between two vertices, deleting it, and checking for success.

Algorithm 41 Demonstration of the 'get edge between vertices' function

```
#include <boost/test/unit_test.hpp>
#include "create_k2_graph.h"
#include "get_edge_between_vertices.h"

#oclude "has_edge_between_vertices.h"

BOOST_AUTO_TEST_CASE(test_get_edge_between_vertices)
{
    auto g = create_k2_graph();
    const auto vd_1 = *vertices(g).first;
    const auto vd_2 = *(++vertices(g).first);
    BOOST_CHECK(has_edge_between_vertices(vd_1, vd_2, g));
    const auto ed = get_edge_between_vertices(vd_1, vd_2, g);
    boost::remove_edge(ed, g);
    BOOST_CHECK(boost::num_edges(g) == 0);
}
```

3.4 Create a direct-neighbour subgraph from a vertex descriptor

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the 'create direct neighbour subgraph' code:

Algorithm 42 Get the direct-neighbour subgraph from a vertex descriptor

```
#include <map>
#include <boost/graph/adjacency_list.hpp>
template < typename graph, typename vertex descriptor >
graph create direct neighbour subgraph (
  const vertex_descriptor& vd,
  const graph& g
{
  graph h;
  std::map<vertex_descriptor, vertex_descriptor> m;
    const auto vd_h = boost::add_vertex(h);
    m.insert(std::make pair(vd,vd h));
  //Copy\ vertices
    const auto vdsi = boost::adjacent_vertices(vd, g);
    for (auto i = vdsi.first; i != vdsi.second; ++i)
      \mathbf{if} (m. find (*i) == m. end ())
        const auto vd h = boost::add vertex(h);
        m. insert (std::make_pair(*i, vd_h));
  //Copy\ edges
    const auto eip = edges(g);
    const auto j = eip.second;
    for (auto i = eip.first; i!=j; ++i)
      const auto vd from = source(*i, g);
      const auto vd_to = target(*i, g);
      if (m. find (vd from) = std :: end (m)) continue;
      if (m. find (vd to) = std::end(m)) continue;
      boost::add edge(m[vd from],m[vd to], h);
  return h;
}
```

This demonstration code shows that the direct-neighbour graph of each vertex of a K_2 graphs is ... a K_2 graph!

Algorithm 43 Demo of the 'create direct neighbour subgraph' function

Note that this algorithm works on both undirected and directional graphs. If the graph is directional, only the out edges will be copied. To also copy the vertices connected with inward edges, use 3.5

3.5 Create a direct-neighbour subgraph from a vertex descriptor including inward edges

Too bad, this algorithm does not work yet.

${\bf Algorithm~44~Get~the~direct-neighbour~subgraph~from~a~vertex~descriptor}$

```
#include <boost/graph/adjacency list.hpp>
#include <unordered map>
#include <vector>
template <typename graph>
graph create direct neighbour subgraph including in edges
    const typename graph::vertex descriptor&vd, const
       graph& g)
{
    using vertex descriptor = typename graph::
       vertex descriptor;
    using edge_descriptor = typename graph::
       edge descriptor;
    using vpair = std::pair < vertex descriptor,
       vertex descriptor >;
    std::vector<vpair> conn edges;
    std::unordered_map<vertex_descriptor,</pre>
       vertex descriptor > m;
    vertex descriptor vd h = 0;
    m.insert(std::make pair(vd, vd h++));
    for (const edge_descriptor ed : boost::
       make iterator range(edges(g))) {
      const auto vd from = source(ed, g);
      const auto vd to = target (ed, g);
      if (vd = vd from) {
        conn edges.emplace back(vd from, vd to);
        m.insert(std::make_pair(vd_to, vd_h++));
      if (vd = vd to) {
        conn edges.emplace back(vd from, vd to);
        m.insert(std::make pair(vd from, vd h++));
    }
    for (vpair& vp : conn edges) {
      vp.first = m[vp.first];
      vp.second = m[vp.second];
    return graph (conn edges.begin (), conn edges.end (), m.
       size());
```

3.6 Creating all direct-neighbour subgraphs from a graph without properties

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph without properties:

Algorithm 45 Create all direct-neighbour subgraphs from a graph without properties

```
#include <vector>
#include "create direct neighbour subgraph.h"
template <typename graph>
std::vector<graph> create all direct neighbour subgraphs(
  const graph& g
  noexcept
{
  using vd = typename graph::vertex descriptor;
  std::vector<graph> v(boost::num vertices(g));
  const auto vip = vertices(g);
  std::transform(
    {\tt vip.first}\ ,\ {\tt vip.second}\ ,
    std::begin(v),
    [&g](const vd& d)
      return create direct neighbour subgraph (
      );
    }
  );
  return v;
```

This demonstration code shows that all two direct-neighbour graphs of a K_2 graphs are ... K_2 graphs!

Algorithm 46 Demo of the 'create_all_direct_neighbour_subgraphs' function

3.7 Are two graphs isomorphic?

You may want to check if two graphs are isomorphic. That is: if they have the same shape.

Algorithm 47 Check if two graphs are isomorphic

```
#include <boost/graph/isomorphism.hpp>

template <typename graph1, typename graph2>
bool is_isomorphic(
   const graph1 g,
   const graph2 h
) noexcept
{
   return boost::isomorphism(g,h);
}
```

This demonstration code shows that a K_3 graph is not equivalent to a 3-vertices path graph:

Algorithm 48 Demo of the 'is isomorphic' function

```
#include <boost/test/unit_test.hpp>
#include "create_path_graph.h"
#include "create_k3_graph.h"
#include "is_isomorphic.h"

BOOST_AUTO_TEST_CASE(test_is_isomorphic)
{
   const auto g = create_path_graph(3);
   const auto h = create_k3_graph();
   BOOST_CHECK( is_isomorphic(g,g));
   BOOST_CHECK(!is_isomorphic(g,h));
}
```

3.8 Count the number of connected components in an directed graph

A directed graph may consist out of two components, that are connected within each, but unconnected between them. Take for example, a graph of two isolated edges, with four vertices.

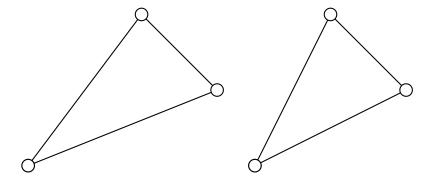


Figure 15: Example of a directed graph with two components

This algorithm counts the number of connected components:

Algorithm 49 Count the number of connected components

```
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/strong_components.hpp>

template <typename graph>
int count_directed_graph_connected_components(
    const graph& g
) noexcept
{
    std::vector<int> c(boost::num_vertices(g));
    const int n = boost::strong_components(g,
        boost::make_iterator_property_map(
        std::begin(c),
        get(boost::vertex_index, g)
    )
    );
    return n;
}
```

The complexity of this algorithm is O(|V| + |E|).

This demonstration code shows that two solitary edges are correctly counted as being two components:

Algorithm 50 Demo of the 'count_directed_graph_connected_components' function

```
#include <boost/test/unit test.hpp>
#include "create_empty_directed_graph.h"
#include "add edge.h"
#include "count directed graph connected components.h"
BOOST AUTO TEST CASE(
   test count directed graph connected components)
  auto g = create empty directed graph();
  BOOST CHECK (count directed graph connected components (g
     ) = 0);
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto vd c = boost :: add vertex(g);
  boost::add edge(vd a, vd b, g);
  boost::add edge(vd b, vd c, g);
  boost::add edge(vd c, vd a, g);
  BOOST CHECK (count directed graph connected components (g
  const auto vd d = boost::add vertex(g);
  const auto vd_e = boost::add_vertex(g);
  \mathbf{const} \ \mathbf{auto} \ vd\_f = boost :: add\_vertex(g);
  boost::add edge(vd d, vd e, g);
  boost::add edge(vd e, vd f, g);
  boost::add_edge(vd_f, vd_d, g);
  BOOST CHECK (count directed graph connected components (g
     ) = 2);
}
```

3.9 Count the number of connected components in an undirected graph

An undirected graph may consist out of two components, that are connect within each, but unconnected between them. Take for example, a graph of two isolated edges, with four vertices.

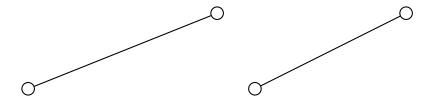


Figure 16: Example of an undirected graph with two components

This algorithm counts the number of connected components:

Algorithm 51 Count the number of connected components

```
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/isomorphism.hpp>
#include <boost/graph/connected_components.hpp>

template <typename graph>
int count_undirected_graph_connected_components(
    const graph& g
) noexcept
{
    std::vector<int> c(boost::num_vertices(g));
    return boost::connected_components(g,
        boost::make_iterator_property_map(
        std::begin(c),
        get(boost::vertex_index, g)
    )
    );
}
```

The complexity of this algorithm is O(|V| + |E|).

This demonstration code shows that two solitary edges are correctly counted as being two components:

Algorithm 52 Demo of the 'count_undirected_graph_connected_components' function

3.10 Count the number of levels in an undirected graph

Graphs can have a hierarchical structure. From a starting vertex, the number of levels can be counted. A graph of one vertex has zero levels. A graph with one edge has one level. A linear graph of three vertices and two edges has one or two levels, depending on the starting vertex.

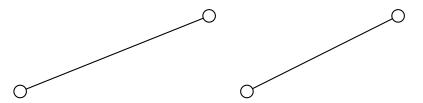


Figure 17: Example of an undirected graph with two components

This algorithm counts the number of levels in an undirected graph, starting at a certain vertex.

It does so, by collecting the neighbours of the traversed vertices. Each sweep, all neighbours of traversed neighbours are added to a set of known vertices. As long as vertices can be added, the algorithm continues. If no vertices can be added, the number of level equals the number of sweeps.

Algorithm 53 Count the number of levels in an undirected graph

```
#include <set>
#include <vector>
#include <boost/graph/adjacency list.hpp>
// Collect all neighbours
// If there are no new neighbours, the level is found
template <typename graph>
int count undirected graph levels (
  typename boost::graph traits<graph>::vertex descriptor
  const graph& g
  noexcept
  int level = 0;
  // This does not work:
  // \ \mathit{std} :: \mathit{set} < \mathit{boost} :: \mathit{graph\_traits} < \mathit{graph} > ::
      vertex descriptor > s;
  std :: set < int > s;
  s.insert(vd);
  while (1)
    //How\ many\ nodes\ are\ known\ now
    const auto sz_before = s.size();
    const auto t = s;
    for (const auto v: t)
       const auto neighbours = boost::adjacent_vertices(v,
       for (auto n = neighbours.first; n != neighbours.
          second; ++n
         s.insert(*n);
    }
    //Have new nodes been discovered?
    if (s.size() == sz_before) break;
    //Found new nodes, thus an extra level
    ++level;
  return level;
                               58
```

This demonstration code shows the number of levels from a certain vertex, while adding edges to form a linear graph. The vertex, when still without edges, has zero levels. After adding one edge, the graph has one level, etc.

Algorithm 54 Demo of the 'count undirected graph levels' function

```
#include <boost/test/unit test.hpp>
#include "create empty undirected graph.h"
#include "add edge.h"
#include "count undirected graph levels.h"
BOOST AUTO TEST CASE(test count undirected graph levels)
  auto g = create_empty_undirected graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto vd c = boost::add vertex(g);
  const auto vd d = boost::add_vertex(g);
  BOOST CHECK(count undirected graph levels(vd a, g) =
     0);
  boost::add edge(vd a, vd b, g);
  BOOST CHECK(count undirected graph levels(vd a, g) =
     1);
  boost::add edge(vd b, vd c, g);
  BOOST CHECK(count undirected graph levels (vd a, g) =
      2);
  boost::add edge(vd c, vd d, g);
  BOOST CHECK(count undirected graph levels (vd a, g) =
     3);
}
```

3.11 Saving a graph to a .dot file

Graph are easily saved to a file, thanks to Graphviz. Graphviz (short for Graph Visualization Software) is a package of open-source tools for drawing graphs. It uses the DOT language for describing graphs, and these are commonly stored in (plain-text) .dot files (I show .dot file of every non-empty graph created, e.g. chapters 2.14.4 and 2.15.4)

Algorithm 55 Saving a graph to a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>

template <typename graph>
void save_graph_to_dot(
   const graph& g,
   const std::string& filename
) noexcept
{
   std::ofstream f(filename);
   boost::write_graphviz(f,g);
}
```

All the code does is create an std::ofstream (an output-to-file stream) and use boost::write_graphviz to write the DOT description of our graph to that stream. Instead of 'std::ofstream', one could use std::cout (a related output stream) to display the DOT language on screen directly.

Algorithm 56 shows how to use the 'save graph to dot' function:

Algorithm 56 Demonstration of the 'save graph to dot' function

```
#include <boost/test/unit_test.hpp>
#include "create_k2_graph.h"
#include "create_markov_chain.h"
#include "save_graph_to_dot.h"

BOOST_AUTO_TEST_CASE(test_save_graph_to_dot)
{
    const auto g = create_k2_graph();
    save_graph_to_dot(g, "create_k2_graph.dot");

    const auto h = create_markov_chain();
    save_graph_to_dot(h, "create_markov_chain.dot");
}
```

When using the 'save_graph_to_dot' function (algorithm 55), only the structure of the graph is saved: all other properties like names are not stored. Algorithm ?? shows how to do so.

3.12 Loading a directed graph from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph is loaded, as shown in algorithm 57:

Algorithm 57 Loading a directed graph from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty directed graph.h"
#include "is regular file.h"
boost::adjacency list <>
load directed graph from dot (
  const std::string& dot filename
  if (!is regular file(dot filename))
    std::stringstream msg;
    msg << __func__ << ":_file_',"
      << dot filename << "', not found"</pre>
    throw std::invalid argument(msg.str());
  }
  std::ifstream f(dot_filename.c_str());
  auto g = create empty directed graph();
  boost::dynamic_properties dp(
    boost::ignore other properties
  );
  boost::read graphviz(f,g,dp);
  return g;
```

In this algorithm, first it is checked if the file to load exists, using the 'is_regular_file' function (algorithm 137), after which an std::ifstream is opened. Then an empty directed graph is created, which saves us writing down the template arguments explicitly. Then, a boost::dynamic_properties is created with the 'boost::ignore_other_properties' in its constructor (using a default constructor here results in the run-time error 'property not found: node_id', see chapter 12.5). From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 58 shows how to use the 'load_directed_graph_from_dot' function:

Algorithm 58 Demonstration of the 'load_directed_graph_from_dot' function

```
#include <boost/test/unit test.hpp>
#include "create markov chain.h"
#include "load_directed_graph_from_dot.h"
#include "save_graph_to dot.h"
BOOST AUTO TEST CASE(test load directed graph from dot)
  using boost::num edges;
  using boost::num vertices;
  const auto g = create markov chain();
  const std::string filename{
    "create markov chain.dot"
  };
  save graph to dot(g, filename);
  const auto h = load_directed_graph from dot(filename);
  BOOST CHECK(num\_edges(g) == num\_edges(h));
  BOOST CHECK(num vertices(g) = num vertices(h));
}
```

This demonstration shows how the Markov chain is created using the 'create_markov_chain_graph' function (algorithm 21), saved and then loaded. The loaded graph is then checked to be a two-state Markov chain.

3.13 Loading an undirected graph from a .dot file

Loading an undirected graph from a .dot file is very similar to loading a directed graph from a .dot file, as shown in chapter 3.12. Algorithm 59 show how to do so:

Algorithm 59 Loading an undirected graph from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty undirected graph.h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
load undirected graph from dot (
  const std::string& dot filename
{
  if (!is regular file(dot filename))
    std::stringstream msg;
    msg << __func__ << ":_file_',"
      << dot filename << "', not found"</pre>
    throw std::invalid argument(msg.str());
  std::ifstream f(dot_filename.c_str());
  auto g = create_empty_undirected_graph();
  boost::dynamic_properties p(
    boost::ignore other properties
  );
  boost::read graphviz(f,g,p);
  return g;
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 3.12 describes the rationale of this function

Algorithm 60 shows how to use the 'load_undirected_graph_from_dot' function:

Algorithm 60 Demonstration of the 'load_undirected_graph_from_dot' function

This demonstration shows how the K_2 graph is created using the 'create_k2_graph' function (algorithm 24), saved and then loaded. The loaded graph is checked to be a K_2 graph.

4 Building graphs with bundled vertices

Up until now, the graphs created have had edges and vertices without any properties. In this chapter, graphs will be created, in which the vertices can have a bundled 'my_bundled_vertex' type⁷. The following graphs will be created:

- An empty directed graph that allows for bundled vertices: see chapter 62
- An empty undirected graph that allows for bundled vertices: see chapter 4.2
- A two-state Markov chain with bundled vertices: see chapter 4.6
- K_2 with bundled vertices: see chapter 4.7

In the process, some basic (sometimes bordering trivial) functions are shown:

- Create the vertex class, called 'my_bundled_vertex': see chapter 4.1
- Adding a 'my bundled vertex': see chapter 4.4

 $^{^7\}mathrm{I}$ do not intend to be original in naming my data types

• Getting the vertices 'my bundled vertex'-es: see chapter 4.5

These functions are mostly there for completion and showing which data types are used.

4.1 Creating the bundled vertex class

Before creating an empty graph with bundled vertices, that bundled vertex class must be created. In this tutorial, it is called 'my_bundled_vertex'. 'my_bundled_vertex' is a class that is nonsensical, but it can be replaced by any other class type.

Here I will show the header file of 'my_bundled_vertex', as the implementation of it is not important:

Algorithm 61 Declaration of my bundled vertex

```
#include <string>
#include <iosfwd>
#include <boost/property map/dynamic property map.hpp>
struct my bundled vertex
  explicit my bundled vertex(
    const std::string& name = "",
    const std::string& description = "",
    {f const\ double\ x=0.0},
    const double y = 0.0
  ) noexcept;
  std::string m name;
  std::string m description;
  double m x;
  double m y;
};
std::ostream& operator<<(std::ostream& os, const
   my bundled vertex& e) noexcept;
bool operator == (const my_bundled_vertex& lhs, const
   my bundled vertex& rhs) noexcept;
bool operator!=(const my bundled vertex& lhs, const
   my bundled vertex& rhs) noexcept;
```

'my bundled vertex' is a class that has multiple properties:

- It has four public member variables: the double 'm_x' ('m_' stands for member), the double 'm_y', the std::string m_name and the std::string m_description. These variables must be public
- It has a default constructor

- It is copyable
- It is comparable for equality (it has operator==), which is needed for searching

'my_bundled_vertex' does not have to have the stream operators defined for file I/O, as this goes via the public member variables.

4.2 Create the empty directed graph with bundled vertices

Algorithm 62 Creating an empty directed graph with bundled vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_vertex.h"

boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::directedS,
   my_bundled_vertex
>
create_empty_directed_bundled_vertices_graph() noexcept
{
   return {};
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is directed (due to the boost::directedS)
- The vertices have one property: they have a bundled type, that is of data type 'my bundled vertex'
- The edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'my_bundled_vertex'. This can be read as: "vertices have the bundled property 'my_bundled_vertex". Or simply: "vertices have a bundled type called my_bundled_vertex".

4.3 Create the empty undirected graph with bundled vertices

Algorithm 63 Creating an empty undirected graph with bundled vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_vertex.h"

boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::undirectedS,
   my_bundled_vertex
>
create_empty_undirected_bundled_vertices_graph() noexcept
{
   return {};
}
```

This code is very similar to the code described in chapter 4.2, except that the directness (the third template argument) is undirected (due to the boost::undirectedS).

4.4 Add a bundled vertex

Adding a bundled vertex is very similar to adding a named vertex (chapter ??).

Algorithm 64 Add a bundled vertex

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_vertex.h"

template <typename graph, typename bundled_vertex>
typename boost::graph_traits<graph>::vertex_descriptor
add_bundled_vertex(const bundled_vertex& v, graph& g)
    noexcept

{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);
    return boost::add_vertex(v, g);
}
```

When having added a new (abstract) vertex to the graph, the vertex descriptor is used to set the 'my bundled vertex' in the graph.

4.5 Getting the bundled vertices' my vertexes⁸

When the vertices of a graph have any bundled 'my_bundled_vertex', one can extract these as such:

Algorithm 65 Get the bundled vertices' my vertexes

```
#include <vector>
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/graph traits.hpp>
#include <boost/graph/properties.hpp>
#include "my bundled vertex.h"
template <typename graph>
std::vector<my bundled vertex> get my bundled vertexes(
  const graph& g
  noexcept
  using vd = typename graph::vertex descriptor;
  std::vector<my bundled vertex> v(boost::num vertices(g)
      );
  const auto vip = vertices(g);
  std::transform(vip.first, vip.second, std::begin(v),
    [\&g](\mathbf{const} \ vd\& \ d) \ \{ \ \mathbf{return} \ g[d]; \ \}
  );
  return v;
}
```

The 'my_bundled_vertex' bundled in each vertex is obtained from a vertex descriptor and then put into a std::vector.

The order of the 'my_bundled_vertex' objects may be different after saving and loading.

When trying to get the vertices' my_bundled_vertex from a graph without these, you will get the error 'formed reference to void' (see chapter 12.1).

4.6 Creating a two-state Markov chain with bundled vertices

4.6.1 Graph

Figure 18 shows the graph that will be reproduced:

 $^{^8{\}rm the~name~'my_vertexes'}$ is chosen to indicate this function returns a container of my_vertex

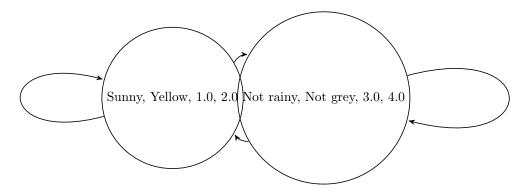


Figure 18: A two-state Markov chain where the vertices have bundled properties and the edges have no properties. The vertices' properties are nonsensical

4.6.2 Function to create such a graph

Here is the code creating a two-state Markov chain with bundled vertices:

Algorithm 66 Creating the two-state Markov chain as depicted in figure 18

```
#include "add bundled vertex.h"
#include "create_empty_directed_bundled_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my\_bundled\_vertex
create bundled vertices markov chain() noexcept
  auto g
    = create_empty_directed_bundled_vertices_graph();
  const my_bundled_vertex a("Sunny",
    "Yellow" ,1.0,2.0
  const my_bundled_vertex b("Not_rainy",
    "Not_grey",3.0,4.0
  );
  const auto vd_a = add_bundled_vertex(a, g);
  const auto vd_b = add_bundled_vertex(b, g);
  boost::add edge(vd a, vd a, g);
  boost::add edge(vd a, vd b, g);
  boost::add\_edge(vd\_b,\ vd\_a,\ g);
  boost::add_edge(vd_b, vd_b, g);
  return g;
}
```

4.6.3 Creating such a graph

Here is the demo:

Algorithm 67 Demo of the 'create_bundled_vertices_markov_chain' function (algorithm 66)

4.6.4 The .dot file produced

```
Algorithm 68 .dot file created from the 'create_bundled_vertices_markov_chain' function (algorithm 66), converted from graph to .dot file using algorithm 81 digraph G {
    O[label="Sunny",comment="Yellow",width=1,height=2];
    1[label="Not$$$SPACE$$$rainy",comment="Not$$$SPACE$$$grey",width=3,height=4];
    0->0;
```

1->1 ; }

0->1 ; 1->0 ;

4.6.5 The .svg file produced

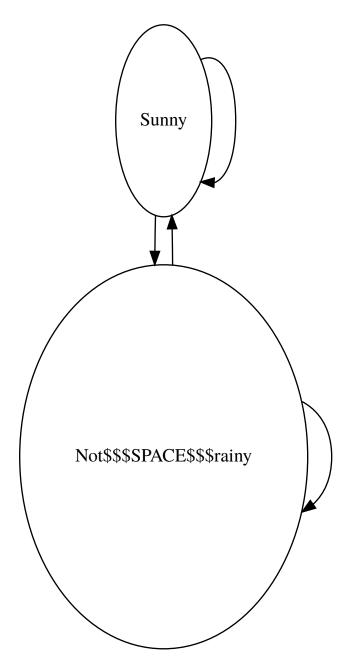


Figure 19: .svg file created from the 'create_bundled_vertices_markov_chain' function (algorithm 66) its .dot file, converted from .dot file to .svg using algorithm 136

4.7 Creating K_2 with bundled vertices

4.7.1 Graph

We reproduce the K_2 with named vertices of chapter $\ref{eq:chapter}$, but with our bundled vertices instead, as show in figure 20:

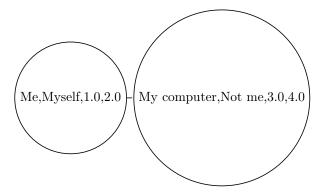


Figure 20: K_2 : a fully connected graph with two bundled vertices

4.7.2 Function to create such a graph

Algorithm 69 Creating K_2 as depicted in figure ??

```
#include "create empty undirected bundled vertices graph.
   h"
#include "add bundled vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex
create bundled vertices k2 graph() noexcept
  auto g = create empty undirected bundled vertices graph
     ();
  const my_bundled_vertex a(
    "Me", "Myself", 1.0, 2.0
  );
  const my bundled vertex b(
    "My_computer", "Not_me", 3.0, 4.0
  );
  const auto vd a = add bundled vertex(a, g);
  const auto vd b = add bundled vertex(b, g);
  boost::add edge(vd a, vd b, g);
  return g;
}
```

Most of the code is a slight modification of the 'create_named_vertices_k2_graph' function (algorithm ??). In the end, (references to) the my_bundled_vertices are obtained and set with two bundled my_bundled_vertex objects.

4.7.3 Creating such a graph

Demo:

Algorithm 70 Demo of the 'create_bundled_vertices_k2_graph' function (algorithm 69)

```
#include <boost/test/unit test.hpp>
#include "create bundled vertices k2 graph.h"
#include "has bundled vertex with my vertex.h"
BOOST AUTO TEST CASE(
   test_create_bundled_vertices_k2_graph)
{
  const auto g = create_bundled_vertices_k2_graph();
  BOOST CHECK(boost::num edges(g) = 1);
  BOOST CHECK(boost::num vertices(g) = 2);
  BOOST CHECK(has bundled vertex with my vertex(
    \label{eq:my_bundled_vertex} \verb|my_bundled_vertex| ("Me", "Myself", 1.0, 2.0) , g) \\
  );
  BOOST CHECK(has bundled vertex with my vertex(
    my_bundled_vertex("My_computer", "Not_me", 3.0, 4.0), g)
  );
}
```

4.7.4 The .dot file produced

Algorithm 71 .dot file created from the 'create_bundled_vertices_k2_graph'

function (algorithm 69), converted from graph to .dot file using algorithm 55

graph G {
0[label="Me",comment="Myself",width=1,height=2];
1[label="My\$\$\$SPACE\$\$\$computer",comment="Not\$\$\$SPACE\$\$\$me",width=3,height=4];
0--1;
}

4.7.5 The .svg file produced

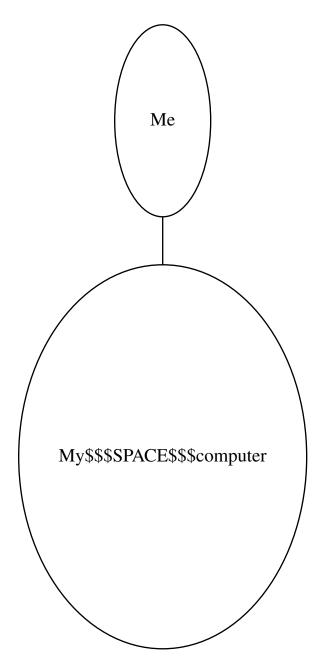


Figure 21: .svg file created from the 'create_bundled_vertices_k2_graph' function (algorithm 69) its .dot file, converted from .dot file to .svg using algorithm 136

5 Working on graphs with bundled vertices

When using graphs with bundled vertices, their state gives a way to find a vertex and working with it. This chapter shows some basic operations on graphs with bundled vertices.

- Check if there exists a vertex with a certain 'my_bundled_vertex': chapter 5.1
- Find a vertex with a certain 'my_bundled_vertex': chapter 5.2
- Get a vertex its 'my_bundled_vertex' from its vertex descriptor: chapter
 5.3
- Set a vertex its 'my_bundled_vertex' using its vertex descriptor: chapter 5.4
- Setting all vertices their 'my_bundled_vertex'-es: chapter 5.5
- \bullet Storing an directed/undirected graph with bundled vertices as a .dot file: chapter 5.6
- Loading a directed graph with bundled vertices from a .dot file: chapter 5.7
- \bullet Loading an undirected directed graph with bundled vertices from a .dot file: chapter 5.8

5.1 Has a bundled vertex with a my bundled vertex

Before modifying our vertices, let's first determine if we can find a vertex by its bundled type ('my_bundled_vertex') in a graph. After obtain the vertex iterators, we can dereference each these to obtain the vertex descriptors and then compare each vertex its 'my bundled vertex' with the one desired.

Algorithm 72 Find if there is vertex with a certain my bundled vertex

```
#include <string>
#include <boost/graph/properties.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
bool has_bundled_vertex_with_my_vertex(
    const my_bundled_vertex& v,
    const graph& g
) noexcept
{
    using vd = typename graph::vertex_descriptor;

    const auto vip = vertices(g);
    return std::find_if(vip.first, vip.second,
        [&v, &g](const vd& d)
        {
        return g[d] == v;
        }
    ) != vip.second;
}
```

This function can be demonstrated as in algorithm 73, where a certain my_bundled_vertex cannot be found in an empty graph. After adding the desired my_bundled_vertex, it is found.

Algorithm 73 Demonstration of the 'has_bundled_vertex_with_my_vertex' function

Note that this function only finds if there is at least one bundled vertex with that my_bundled_vertex: it does not tell how many bundled vertices with that my_bundled_vertex exist in the graph.

5.2 Find a bundled vertex with a certain my bundled vertex

Where STL functions work with iterators, here we obtain a vertex descriptor (see chapter 2.6) to obtain a handle to the desired vertex. Algorithm 74 shows how to obtain a vertex descriptor to the first vertex found with a specific 'my bundled vertex' value.

Algorithm 74 Find the first vertex with a certain my bundled vertex

```
#include <cassert>
\#include <boost/graph/graph_traits.hpp>
\#include <boost/graph/properties.hpp>
#include "has bundled vertex with my vertex.h"
#include "my bundled vertex.h"
template <typename graph, typename bundled vertex t>
\textbf{typename} \hspace{0.2cm} boost:: graph\_traits < graph>:: vertex\_descriptor
find_first_bundled_vertex_with_my_vertex(
  const bundled vertex t& v,
  const graph& g
  using vd = typename graph::vertex descriptor;
  const auto vip = vertices(g);
  const auto i = std::find if(
    vip.first, vip.second,
    [\&v, \&g](const vd d) \{ return g[d] = v; \}
  if (i == vip.second)
    std::stringstream msg;
    msg << __func__ << ":"
      << "could_not_find_my_bundled_vertex_'"</pre>
      <<\ v\ <<\ "\ "
    throw std::invalid argument(msg.str());
  return *i;
}
```

With the vertex descriptor obtained, one can read and modify the vertex and the edges surrounding it. Algorithm 75 shows some examples of how to do so

 ${\bf Algorithm~75~Demonstration~of~the~`find_first_bundled_vertex_with_my_vertex'} \\ {\bf function}$

```
#include <boost/test/unit_test.hpp>
#include "create_bundled_vertices_k2_graph.h"
#include "find_first_bundled_vertex_with_my_vertex.h"

BOOST_AUTO_TEST_CASE(
    test_find_first_bundled_vertex_with_my_vertex)
{
    const auto g = create_bundled_vertices_k2_graph();
    const auto vd =
        find_first_bundled_vertex_with_my_vertex(
        my_bundled_vertex("Me","Myself",1.0,2.0),
        g
    );
    BOOST_CHECK(out_degree(vd,g) == 1);
    BOOST_CHECK(in_degree(vd,g) == 1);
}
```

5.3 Get a bundled vertex its 'my bundled vertex'

To obtain the 'my bundled vertex' from a vertex descriptor is simple:

Algorithm 76 Get a bundled vertex its my vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
my_bundled_vertex get_my_bundled_vertex(
    const typename boost::graph_traits<graph>::
        vertex_descriptor&vd,
    const graph&g
) noexcept
{
    return g[vd];
}
```

One can just use the graph as a property map and let it be looked-up.

To use 'get_bundled_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 77 shows a simple example.

Algorithm 77 Demonstration if the 'get_bundled_vertex_my_vertex' function

5.4 Set a bundled vertex its my vertex

If you know how to get the 'my_bundled_vertex' from a vertex descriptor, setting it is just as easy, as shown in algorithm 78.

Algorithm 78 Set a bundled vertex its my vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
void set_my_bundled_vertex(
    const my_bundled_vertex& v,
    const typename boost::graph_traits<graph>::
        vertex_descriptor& vd,
    graph& g
) noexcept
{
    static_assert(!std::is_const<graph>::value, "graph,
        cannot_be_const");
    g[vd] = v;
}
```

To use 'set_bundled_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 79 shows a simple example.

Algorithm 79 Demonstration if the 'set_bundled_vertex_my_vertex' function

```
#include <boost/test/unit test.hpp>
#include "add bundled vertex.h"
#include "create empty undirected bundled vertices graph.
   h"
#include "find_first_bundled_vertex_with_my_vertex.h"
#include "get_my_bundled_vertex.h"
#include "set my bundled vertex.h"
BOOST AUTO TEST CASE(test set my bundled vertex)
  auto g = create empty undirected bundled vertices graph
  const my bundled vertex old name{"Dex"};
  add bundled vertex (old name, g);
  const auto vd =
     find first bundled vertex with my vertex (old name, g)
  BOOST CHECK(get my bundled vertex(vd, g) = old name);
  const my bundled vertex new name{"Diggy"};
  set my bundled vertex (new name, vd, g);
  BOOST CHECK(get my bundled vertex(vd, g) = new name);
```

5.5 Setting all bundled vertices' my vertex objects

When the vertices of a graph are 'my_bundled_vertex' objects, one can set these as such:

Algorithm 80 Setting the bundled vertices' 'my bundled vertex'-es

```
#include <string>
#include <vector>
#include <boost/graph/graph traits.hpp>
#include <boost/graph/properties.hpp>
#include "my bundled vertex.h"
template <typename graph>
void set_my_bundled_vertexes(
  graph&g,
  const std::vector<my bundled vertex>& my vertexes
  noexcept
  static_assert(!std::is_const<graph>::value,
    "graph_cannot_be_const"
  );
  auto my vertexes begin = std::begin(my vertexes);
  //const auto my\_vertexes\_end = std :: end(my\_vertexes);
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (
    auto i = vip.first;
    i!=j; ++i,
    ++my_vertexes_begin
    //assert(my\ vertexes\ begin\ !=\ my\ vertexes\ end);
    g[*i] = *my_vertexes_begin;
}
```

5.6 Storing a graph with bundled vertices as a .dot

If you used the 'create_bundled_vertices_k2_graph' function (algorithm 69) to produce a K_2 graph with vertices associated with 'my_bundled_vertex' objects, you can store these with algorithm 81:

Algorithm 81 Storing a graph with bundled vertices as a .dot file

This code looks small, because we call the 'make_bundled_vertices_writer' function, which is shown in algorithm 82:

Algorithm 82 The 'make bundled vertices writer' function

```
template <typename graph>
inline bundled_vertices_writer<graph>
make_bundled_vertices_writer(
   const graph& g
)
{
   return bundled_vertices_writer<
      graph
   >(g);
}
```

Also this function is forwarding the real work to the 'bundled_vertices_writer', shown in algorithm 83:

Algorithm 83 The 'bundled_vertices_writer' function

```
#include <ostream>
#include "graphviz encode.h"
#include "is_graphviz_friendly.h"
template <
  typename graph
class bundled_vertices_writer {
public:
  bundled vertices writer (
    graph g
    : m_g{g}
  template <class vertex descriptor>
  void operator()(
    std::ostream& out,
    const vertex_descriptor& vd
  ) const noexcept {
    out
      << "[label=\""
        << graphviz encode(</pre>
           m_g[vd].m_name
      << "\", comment=\""
        << graphviz encode(</pre>
           m_g[vd].m_description
      <<\stackrel{'}{\quad} "\setminus", width="
        << m_g[vd].m_x
      << ", height="
        << m g[vd].m y
      << "]"
  }
private:
  graph m g;
};
```

Here, some interesting things are happening: the writer needs the bundled property maps to work with and thus copies the whole graph to its internals. I have chosen to map the 'my_bundled_vertex' member variables to Graphviz

attributes (see chapter 13.2 for most Graphviz attributes) as shown in table 1:

my_bundled_vertex variable	C++ data type	Graphviz data type	Graphviz attribute
m_name	std::string	string	label
m_description	std::string	string	comment
m_x	double	double	width
m_y	double	double	height

Table 1: Mapping of my_bundled_vertex member variable and Graphviz attributes

Important in this mapping is that the C++ and the Graphviz data types match. I also chose attributes that matched as closely as possible.

The writer also encodes the std::string of the name and description to a Graphviz-friendly format. When loading the .dot file again, this will have to be undone again.

5.7 Loading a directed graph with bundled vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with bundled vertices is loaded, as shown in algorithm 84:

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty directed bundled vertices graph.h"
#include "graphviz decode.h"
#include "is_regular_file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  my bundled vertex
load_directed_bundled_vertices_graph_from_dot(
  const std::string& dot filename
  if (!is regular file(dot filename))
    std::stringstream msg;
    \mathrm{msg} \, << \, \__\mathrm{func}\__{\,-} \, << \, ": \, \_\, \mathrm{file}\, \_\, `"
      << dot filename << "', not, found"</pre>
    throw std::invalid argument(msg.str());
  std::ifstream f(dot filename.c str());
  auto g = create empty directed bundled vertices graph()
  boost::dynamic_properties dp(boost::
      ignore_other_properties);
  dp.property("label",get(&my_bundled_vertex::m_name, g))
  dp.property("comment", get(&my bundled vertex::
     m description, g));
  dp.property("width", get(&my_bundled_vertex::m_x, g));
  \tt dp.property("height", get(\&my\_bundled\_vertex::m\_y, g));\\
  boost::read graphviz(f,g,dp);
  //Decode \ vertices
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i)
    g[*i].m name = graphviz decode(g[*i].m name);
    g[*i].m description = graphviz decode(g[*i].
        m description);
                               90
  return g;
}
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created, to save typing the typename explicitly.

Then a boost::dynamic_properties is created with its default constructor, after which we set it to follow the same mapping as in the previous chapter. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

At the moment the graph is created, all 'my_bundled_vertex' their names and description are in a Graphviz-friendly format. By obtaining all vertex iterators and vertex descriptors, the encoding is made undone.

Algorithm 85 shows how to use the 'load_directed_bundled_vertices_graph_from_dot' function:

Algorithm 85 Demonstration of the 'load_directed_bundled_vertices_graph_from_dot' function

```
#include <boost/test/unit test.hpp>
#include "create bundled vertices markov chain.h"
#include "load directed bundled vertices graph from dot.h
#include "save bundled vertices graph to dot.h"
#include "get my bundled vertexes.h"
BOOST AUTO TEST CASE(
   test load directed bundled vertices graph from dot)
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled vertices markov chain();
  const std::string filename{
    "create bundled vertices markov chain.dot"
  };
  save bundled vertices graph to dot(g, filename);
  const auto h
    = load_directed_bundled_vertices_graph_from_dot(
       filename);
  BOOST CHECK(num edges(g) = num edges(h));
  BOOST CHECK(num vertices(g) = num vertices(h));
  BOOST_CHECK(get_my_bundled_vertexes(g) ==
     get my bundled vertexes(h));
}
```

This demonstration shows how the Markov chain is created using the 'create bundled vertices markov chain' function (algorithm 66), saved and then

loaded. The loaded graph is checked to be the same as the original.

5.8 Loading an undirected graph with bundled vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with bundled vertices is loaded, as shown in algorithm 86:

 $\bf Algorithm~86$ Loading an undirected graph with bundled vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_bundled_vertices_graph.
   h"
#include "graphviz decode.h"
#include "is_regular_file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex
load_undirected_bundled_vertices_graph_from_dot(
  const std::string& dot filename
  if (!is regular file(dot filename))
    std::stringstream msg;
    \mathrm{msg} \; << \; \_\_\mathrm{func}\_\_ \; << \; ": \_ \, \mathrm{file} \, \_ \, , \, "
      << dot filename << "', not_found"</pre>
    throw std::invalid argument(msg.str());
  std::ifstream f(dot filename.c str());
  auto \ g = create\_empty\_undirected\_bundled\_vertices\_graph
      ();
  boost::dynamic properties dp(boost::
      ignore_other_properties);
  dp.property("label",get(&my_bundled vertex::m name, g))
  dp.property("comment", get(&my bundled vertex::
      m description, g));
  dp.property("width", get(&my_bundled_vertex::m_x, g));
  dp.property("height", get(&my_bundled_vertex::m_y, g));
  boost::read_graphviz(f,g,dp);
  //Decode vertices
  const auto vip = vertices(g);
  \label{eq:const} \textbf{const} \ \ \textbf{auto} \ \ \textbf{j} \ = \ vip \, . \, second \, ;
  for (auto i = vip.first; i!=j; ++i)
    g[*i].m name = graphviz decode(g[*i].m name);
    g[*i].m description = gr \mathfrak{P}hviz decode(g[*i]).
        m description);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 5.7 describes the rationale of this function.

Algorithm 87 shows how to use the 'load_undirected_bundled_vertices_graph_from_dot' function:

Algorithm 87 Demonstration of the 'load_undirected_bundled_vertices_graph_from_dot' function

```
#include <boost/test/unit_test.hpp>
#include "create_bundled_vertices_k2_graph.h"
#include "load undirected bundled vertices graph from dot
    . h"
#include "save_bundled_vertices_graph_to_dot.h"
#include "get my bundled vertexes.h"
BOOST AUTO TEST CASE(
   test load undirected bundled vertices graph from dot)
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled vertices k2 graph();
  const std::string filename{
    "create_bundled_vertices_k2_graph.dot"
  };
  save bundled vertices graph to dot(g, filename);
  const auto h
    = load undirected bundled vertices graph from dot(
       filename);
  BOOST CHECK(get my bundled vertexes(g)
    == get my bundled vertexes(h)
  );
}
```

This demonstration shows how K_2 with bundled vertices is created using the 'create_bundled_vertices_k2_graph' function (algorithm 69), saved and then loaded. The loaded graph is checked to be the same as the original.

6 Building graphs with bundled edges and vertices

Up until now, the graphs created have had only bundled vertices. In this chapter, graphs will be created, in which both the edges and vertices have a bundled

'my_bundled_edge' and 'my_bundled_edge' type⁹.

- \bullet An empty directed graph that allows for bundled edges and vertices: see chapter 6.2
- \bullet An empty undirected graph that allows for bundled edges and vertices: see chapter 6.3
- A two-state Markov chain with bundled edges and vertices: see chapter 6.6
- K_3 with bundled edges and vertices: see chapter 6.7

In the process, some basic (sometimes bordering trivial) functions are shown:

- Creating the 'my bundled edge' class: see chapter 6.1
- Adding a bundled 'my_bundled_edge': see chapter 6.4

These functions are mostly there for completion and showing which data types are used.

6.1 Creating the bundled edge class

In this example, I create a 'my_bundled_edge' class. Here I will show the header file of it, as the implementation of it is not important yet.

⁹I do not intend to be original in naming my data types

Algorithm 88 Declaration of my_bundled_edge

```
#include <string>
#include <iosfwd>
class my bundled edge
public:
  explicit my bundled edge (
    const std::string& name = "",
    const std::string& description = "",
    const double width = 1.0,
    const double height = 1.0
  ) noexcept;
  std::string m_name;
  std::string m description;
  double m width;
  double m_height;
};
std::ostream& operator<<(std::ostream& os, const
   my bundled edge& e) noexcept;
bool operator == (const my_bundled_edge& lhs, const
   my bundled edge& rhs) noexcept;
bool operator!=(const my bundled edge& lhs, const
   my bundled edge& rhs) noexcept;
```

my_bundled_edge is a class that has multiple properties: two doubles 'm_width' ('m_' stands for member) and 'm_height', and two std::strings m_name and m_description.'my_bundled_edge' is copyable, but cannot trivially be converted to a 'std::string.' 'my_bundled_edge' is comparable for equality (that is, operator== is defined).

'my_bundled_edge' does not have to have the stream operators defined for file I/O, as this goes via the public member variables.

6.2 Create an empty directed graph with bundled edges and vertices

Algorithm 89 Creating an empty directed graph with bundled edges and vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_edge.h"
#include "my_bundled_vertex.h"

boost::adjacency_list <
    boost::vecS,
    boost::vecS,
    boost::directedS,
    my_bundled_vertex,
    my_bundled_edge
>
create_empty_directed_bundled_edges_and_vertices_graph()
    noexcept
{
    return {};
}
```

This code is very similar to the code described in chapter ??, except that there is a new, fifth template argument:

```
boost::property<boost::edge_bundled_type_t, my_edge>
```

This can be read as: "edges have the property 'boost::edge_bundled_type_t', which is of data type 'my_bundled_edge". Or simply: "edges have a bundled type called my_bundled_edge".

Demo:

```
Algorithm
                 90
                                                    the
                         Demonstration
                                                             'cre-
ate \_empty \_directed \_bundled \_edges \_and \_vertices \_graph' function
#include <boost/test/unit_test.hpp>
#include "
   create empty directed bundled edges and vertices graph
    . h"
BOOST AUTO TEST CASE(
    test\_create\_empty\_directed\_bundled\_edges\_and\_vertices\_graph
{
  const auto g =
      create empty directed bundled edges and vertices graph
      ();
  BOOST CHECK(boost::num edges(g) = 0);
  BOOST CHECK(boost::num vertices(g) = 0);
```

6.3 Create an empty undirected graph with bundled edges and vertices

Algorithm 91 Creating an empty undirected graph with bundled edges and vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_edge.h"
#include "my_bundled_vertex.h"

boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::undirectedS,
   my_bundled_vertex,
   my_bundled_edge
>
create_empty_undirected_bundled_edges_and_vertices_graph
   () noexcept
{
   return {};
}
```

This code is very similar to the code described in chapter 6.2, except that the directness (the third template argument) is undirected (due to the boost::undirectedS).

Demo:

```
Algorithm
                 92
                         Demonstration
                                            of
                                                    the
                                                              'cre-
ate empty undirected bundled edges and vertices graph' function
#include <boost/test/unit test.hpp>
#include "
   create\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph
    . h " \,
BOOST AUTO TEST CASE(
   test\_create\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph
{
  const auto g
        create\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph
 BOOST CHECK(boost::num\_edges(g) == 0);
  BOOST\_CHECK(boost::num\_vertices(g) == 0);
}
```

6.4 Add a bundled edge

Adding a bundled edge is very similar to adding a named edge (chapter ??).

Algorithm 93 Add a bundled edge

```
#include <cassert>
#include <sstream>
#include <stdexcept>
#include <boost/graph/adjacency list.hpp>
#include "my bundled edge.h"
#include "has edge between vertices.h"
{\bf template}\ {<} {\bf typename}\ {\rm graph}\ ,\ {\bf typename}\ {\rm bundled\_edge}{>}
typename boost::graph traits<graph>::edge descriptor
add bundled edge (
  \mathbf{const} \ \mathbf{typename} \ \mathbf{boost} :: \mathbf{graph\_traits} {<} \mathbf{graph} > ::
      vertex descriptor& vd from,
  const typename boost::graph traits<graph>::
      vertex_descriptor& vd_to,
  const bundled edge& edge,
  graph& g
  static_assert(!std::is_const<graph>::value, "graph_
      cannot_be_const");
  if (has edge between vertices (vd from, vd to, g))
    std::stringstream msg;
    msg << __func__ << ":_already_an_edge_there";</pre>
    throw std::invalid argument(msg.str());
  const auto aer = boost::add edge(vd from, vd to, g);
  assert (aer.second);
  g[aer.first] = edge;
  return aer. first;
}
```

When having added a new (abstract) edge to the graph, the edge descriptor is used to set the my_edge in the graph.

Here is the demo:

Algorithm 94 Demo of 'add bundled edge'

```
#include <boost/test/unit test.hpp>
#include "add_bundled_edge.h"
#include "add_bundled_vertex.h"
#include "
   create empty directed bundled edges and vertices graph
   . h"
BOOST_AUTO_TEST_CASE(test_add_bundled_edge)
  auto g =
     create_empty_directed_bundled_edges_and_vertices_graph
  const auto vd_from = add_bundled_vertex(
     my bundled vertex("From"), g);
  const auto vd to = add bundled vertex (my bundled vertex
     ("To"), g);
  add_bundled_edge(vd_from, vd_to, my_bundled_edge("X"),
 BOOST\_CHECK(boost::num\_vertices(g) == 2);
 BOOST CHECK(boost::num edges(g) = 1);
```

6.5 Getting the bundled edges my edges

When the edges of a graph are 'my_bundled_edge' objects, one can extract these all as such:

Algorithm 95 Get the edges' my bundled edges

```
#include <vector>
#include <boost/graph/adjacency list.hpp>
#include "my_bundled_edge.h"
template <typename graph>
std::vector<my bundled edge> get my bundled edges(
  const graph& g
) noexcept
  using ed = typename boost::graph traits<graph>::
     edge descriptor;
  std::vector<my bundled edge> v(boost::num edges(g));
  const auto eip = edges(g);
  std::transform(eip.first, eip.second, std::begin(v),
    [\&g](const ed e) \{ return g[e]; \}
  );
  return v;
}
```

The 'my_bundled_edge' object associated with the edges are obtained from the graph its property map and then put into a std::vector.

Note: the order of the my_bundled_edge objects may be different after saving and loading.

When trying to get the edges' my_bundled_edge objects from a graph without bundled edges objects associated, you will get the error 'formed reference to void' (see chapter 12.1).

6.6 Creating a Markov-chain with bundled edges and vertices

6.6.1 Graph

Figure 22 shows the graph that will be reproduced:

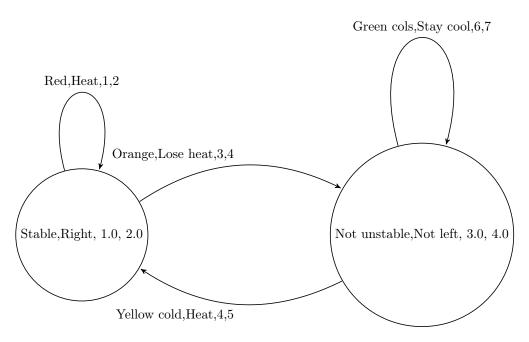


Figure 22: A two-state Markov chain where the edges and vertices have bundled properties. The edges' and vertices' properties are nonsensical

6.6.2 Function to create such a graph

Here is the code creating a two-state Markov chain with bundled edges and vertices:

Algorithm 96 Creating the two-state Markov chain as depicted in figure 22

```
#include <cassert>
#include "
   create empty directed bundled edges and vertices graph
#include "add bundled edge.h"
#include "add bundled vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my bundled vertex,
  my bundled edge
create bundled edges and vertices markov chain()
  auto g
       create_empty_directed_bundled_edges_and_vertices_graph
  const auto va = my bundled vertex("Stable", "Right"
      ,1.0,2.0);
  const auto vb = my bundled vertex("Not_unstable", "Not_
      left",3.0,4.0);
  const auto vd_a = add_bundled_vertex(va, g);
  const auto vd b = add bundled vertex(vb, g);
  const auto e aa = my bundled edge("Red", "Heat", 1.0, 2.0)
  const auto e ab = my bundled edge("Orange", "Lose_heat"
      ,3.0,4.0);
  const auto e ba = my bundled edge("Yellow_cold", "Heat"
      ,5.0,6.0);
  const auto e bb = my bundled edge("Green_cold", "Stay_
     cool'', 7.0, 8.0);
  add bundled edge(vd a, vd a, e aa, g);
  add_bundled_edge(vd_a, vd_b, e_ab, g);
  add bundled edge (vd b, vd a, e ba,
  add bundled edge(vd b, vd b, e bb,
  return g;
```

6.6.3 Creating such a graph

Here is the demo:

```
Algorithm 97 Demo of the 'create bundled edges and vertices markov chain'
function (algorithm 96)
#include <boost/test/unit test.hpp>
#include "create bundled edges and vertices markov chain.
#include "get my bundled edges.h"
#include "my bundled vertex.h"
BOOST AUTO TEST CASE(
    test create bundled edges and vertices markov chain)
  const auto g =
      create bundled edges and vertices markov chain();
  const std::vector<my bundled edge> edge my edges{
    get my bundled edges(g)
  };
  const std::vector<my bundled edge> expected my edges{
    my bundled edge ("Red", "Heat", 1.0, 2.0),
    my bundled edge ("Orange", "Lose_heat", 3.0, 4.0),
     \  \, \text{my bundled edge}(\,\text{"Yellow\_cold"}\,,\text{"Heat"}\,,5.0\,,6.0)\;,
    my\_bundled\_edge("Green\_cold", "Stay\_cool", 7.0, 8.0)
  BOOST CHECK(edge my edges = expected my edges);
```

6.6.4 The .dot file produced

```
Algorithm
                      .dot
                                      created
                                                from
                                                         the
                                                                 'cre-
ate bundled edges and vertices markov chain'
                                                function
                                                           (algorithm
96), converted from graph to .dot file using algorithm 55
digraph G {
0[label="Stable",comment="Right",width=1,height=2];
1[label="Not$$$PACE$$$unstable",comment="Not$$$SPACE$$$left",width=3,height=4];
0->0 [label="Red",comment="Heat",width=1,height=2];
0->1 [label="Orange",comment="Lose$$$SPACE$$$heat",width=3,height=4];
1->0 [label="Yellow$$$SPACE$$$cold",comment="Heat",width=5,height=6];
1->1 [label="Green$$$SPACE$$$cold",comment="Stay$$$SPACE$$$cool",width=7,height=8];
```

6.6.5 The .svg file produced

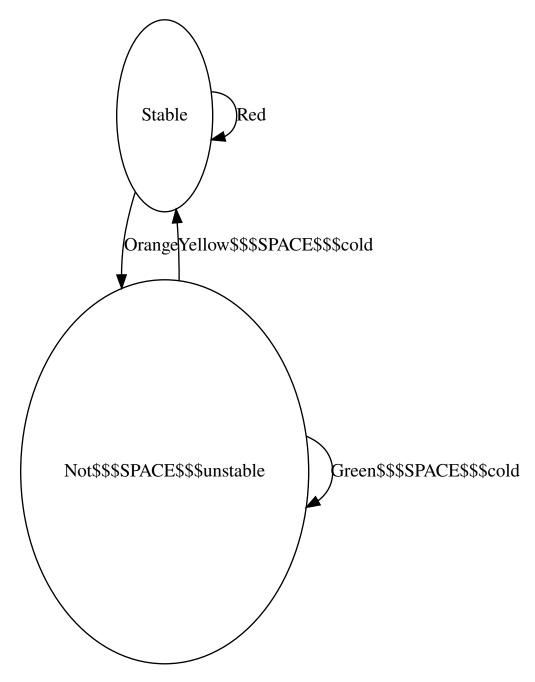


Figure 23: .svg file created from the 'create_bundled_edges_and_vertices_markov_chain' function (algorithm ??) its .dot file, converted from .dot file to .svg using algorithm 136

6.7 Creating K_3 with bundled edges and vertices

Instead of using edges with a name, or other properties, here we use a bundled edge class called 'my_bundled_edge'.

6.7.1 Graph

We reproduce the K_3 with named edges and vertices of chapter $\ref{eq:chapter}$, but with our bundled edges and vertices instead:

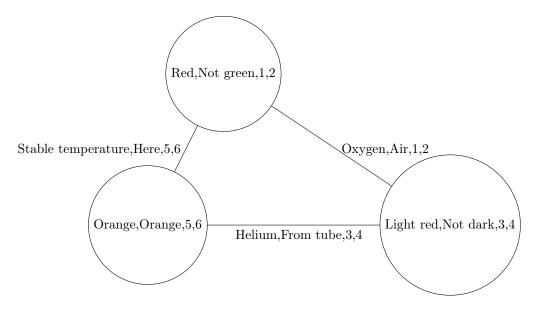


Figure 24: K_3 : a fully connected graph with three named edges and vertices

Algorithm 99 Creating K_3 as depicted in figure ??

```
#include "
   create empty undirected bundled edges and vertices graph
    . h"
#include "add_bundled_edge.h"
#include "add bundled vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my_bundled_vertex,
  my\_bundled\_edge
create bundled edges and vertices k3 graph()
  auto g
        create empty undirected bundled edges and vertices graph
  const auto vd a = add bundled vertex(
    my bundled vertex("Red", "Not_green", 1.0, 2.0),
    g
  );
  const auto vd b = add bundled vertex(
    my bundled vertex("Light_red", "Not_dark", 3.0, 4.0),
    g
  );
  const auto vd c = add bundled vertex(
    my_bundled_vertex("Orange", "Orangy", 5.0,6.0),
    g
  );
  add bundled edge (vd a, vd b,
    my bundled edge ("Oxygen", "Air", 1.0, 2.0),
    g
  );
  add bundled edge(vd b, vd c,
    my_bundled_edge("Helium", "From_tube", 3.0, 4.0),
  );
  add_bundled_edge(vd_c, vd_a,
    my_bundled_edge("Stable_temperature", "Here", 5.0, 6.0),
    g
  );
  return g;
                             110
}
```

Most of the code is a slight modification of algorithm ??. In the end, the my_edges and my_vertices are obtained as the graph its property_map and set with the 'my_bundled_edge' and 'my_bundled_vertex' objects.

6.7.3 Creating such a graph

Here is the demo:

```
function (algorithm 99)

#include <boost/test/unit_test.hpp>
#include "create_bundled_edges_and_vertices_k3_graph.h"

BOOST_AUTO_TEST_CASE(
    test_create_bundled_edges_and_vertices_k3_graph)
```

Algorithm 100 Demo of the 'create bundled edges and vertices k3 graph'

6.7.4 The .dot file produced

```
Algorithm
               101
                       .dot
                               file
                                      created
                                                 from
                                                          the
                                                                 'cre-
ate bundled edges and vertices markov chain'
                                                 function
                                                           (algorithm
99), converted from graph to .dot file using algorithm 55
O[label="Red",comment="Not$$$SPACE$$$green",width=1,height=2];
1[label="Light$$$SPACE$$$red",comment="Not$$$$PACE$$$dark",width=3,height=4];
2[label="Orange",comment="Orangy",width=5,height=6];
0--1 [label="Oxygen",comment="Air",width=1,height=2];
1--2 [label="Helium",comment="From$$$$PACE$$$tube",width=3,height=4];
2--0 [label="Stable$$$PACE$$$temperature",comment="Here",width=5,height=6];
}
```

6.7.5 The .svg file produced

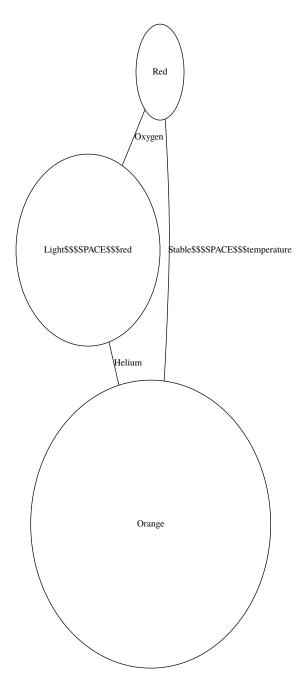


Figure 25: .svg file created from the 'create_bundled_edges_and_vertices_k3_graph' function (algorithm ??) its .dot file, converted from .dot file to .svg using algorithm 136

7 Working on graphs with bundled edges and vertices

7.1 Has a my bundled edge

Before modifying our edges, let's first determine if we can find an edge by its bundled type ('my_bundled_edge') in a graph. After obtaining a my_bundled_edge map, we obtain the edge iterators, dereference these to obtain the edge descriptors and then compare each edge its my_bundled_edge with the one desired.

Algorithm 102 Find if there is a bundled edge with a certain my bundled edge

```
#include <boost/graph/properties.hpp>
#include "my_bundled_edge.h"

template <typename graph>
bool has_bundled_edge_with_my_edge(
    const my_bundled_edge& e,
    const graph& g
) noexcept
{
    using ed = typename boost::graph_traits<graph>::
        edge_descriptor;
    const auto eip = edges(g);
    return std::find_if(eip.first, eip.second,
        [&e, &g](const ed& d)
        {
            return g[d] == e;
        }
        ) != eip.second;
}
```

This function can be demonstrated as in algorithm 103, where a certain 'my_bundled_edge' cannot be found in an empty graph. After adding the desired my_bundled_edge, it is found.

 ${\bf Algorithm} \ \overline{\bf 103} \ {\bf Demonstration} \ {\bf of} \ {\bf the} \ {\bf `has_bundled_edge_with_my_edge'} \\ {\bf function}$

Note that this function only finds if there is at least one edge with that my_bundled_edge: it does not tell how many edges with that my_bundled_edge exist in the graph.

7.2 Find a my bundled edge

Where STL functions work with iterators, here we obtain an edge descriptor (see chapter 2.12) to obtain a handle to the desired edge. Algorithm 104 shows how to obtain an edge descriptor to the first edge found with a specific my_bundled_edge value.

Algorithm 104 Find the first bundled edge with a certain my_bundled_edge

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include "has_bundled_edge_with_my edge.h"
#include "has custom edge with my edge.h"
#include "my bundled edge.h"
template <typename graph>
typename boost::graph_traits<graph>::edge_descriptor
find first bundled edge with my edge (
  const my bundled edge& e,
  const graph& g
  using ed = typename boost::graph traits<graph>::
     edge descriptor;
  const auto eip = edges(g);
  const auto i = std::find if(
    eip.first, eip.second,
    [\&e, \&g](const ed d) \{ return g[d] = e; \}
  if (i == eip.second)
    std::stringstream msg;
    msg << __func__ << ":"
      << "could_not_find_my bundled edge_'"</pre>
      << e << " '"
    throw std::invalid argument(msg.str());
  return *i;
}
```

With the edge descriptor obtained, one can read and modify the edge and the vertices surrounding it. Algorithm 105 shows some examples of how to do so.

Algorithm 105 Demonstration of the 'find_first_bundled_edge_with_my_edge' function

```
#include <boost/test/unit test.hpp>
#include "create bundled edges and vertices k3 graph.h"
#include "find first bundled edge with my edge.h"
BOOST AUTO TEST CASE(
   test find first bundled edge with my edge)
{
  const auto g
    = create bundled edges and vertices k3 graph();
  const auto ed
    = find first bundled edge with my edge (
    my bundled edge ("Oxygen", "Air", 1.0, 2.0),
  );
  BOOST CHECK(boost::source(ed,g)
    != boost :: target (ed,g)
  );
}
```

7.3 Get an edge its my_bundled_edge

To obtain the my_bundled_edge from an edge descriptor, one needs to pull out the my_bundled_edges map and then look up the my_edge of interest.

Algorithm 106 Get a vertex its my bundled vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include "my_bundled_edge.h"

template <typename graph>
my_bundled_edge get_my_bundled_edge(
   const typename boost::graph_traits<graph>::
        edge_descriptor& ed,
   const graph& g
) noexcept
{
   return g[ed];
}
```

To use 'get_my_bundled_edge', one first needs to obtain an edge descriptor. Algorithm 107 shows a simple example.

Algorithm 107 Demonstration if the 'get my bundled edge' function

```
#include <boost/test/unit test.hpp>
#include "add_bundled_edge.h"
#include "add bundled vertex.h"
#include "
   create empty undirected bundled edges and vertices graph
    . h "
#include "find first bundled edge with my edge.h"
#include "get_my_bundled_edge.h"
BOOST AUTO TEST CASE(test get my bundled edge)
  auto g
       create empty undirected bundled edges and vertices graph
  const my bundled edge edge{"Dex"};
  const auto vd a = add bundled vertex(
    my bundled vertex("A"), g
  );
  const auto vd_b = add_bundled_vertex(
    my bundled vertex("B"), g
  add bundled edge(vd a, vd b, edge, g);
  const auto ed
    = find_first_bundled_edge_with_my_edge(edge, g);
  BOOST CHECK(get my bundled edge(ed,g) = edge);
}
```

7.4 Set an edge its my_bundled_edge

If you know how to get the my_bundled_edge from an edge descriptor, setting it is just as easy, as shown in algorithm 108.

Algorithm 108 Set a bundled edge its my_bundled_edge from its edge descriptor

```
#include <boost/graph/properties.hpp>
#include "my_bundled_edge.h"

template <typename graph>
void set_my_bundled_edge(
   const my_bundled_edge& name,
   const typename boost::graph_traits<graph>::
        edge_descriptor& ed,
        graph& g
) noexcept
{
   static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);
   g[ed] = name;
}
```

To use 'set_bundled_edge_my_edge', one first needs to obtain an edge descriptor. Algorithm 109 shows a simple example.

Algorithm 109 Demonstration if the 'set bundled edge my edge' function

```
#include <boost/test/unit_test.hpp>
#include "add bundled edge.h"
#include "add bundled vertex.h"
#include "
   create empty undirected bundled edges and vertices graph
    .h"
#include "find first bundled edge with my edge.h"
#include "get my bundled edge.h"
#include "set my bundled edge.h"
BOOST AUTO TEST CASE(test set my bundled edge)
  auto g
        create empty undirected bundled edges and vertices graph
        ();
  const auto vd a = add bundled vertex (my bundled vertex {
      "A" } , g);
  const auto vd b = add bundled vertex(my bundled vertex{
      "B" \} , g);
  const my bundled edge old edge {"Dex"};
  add bundled edge(vd a, vd b, old edge, g);
  const auto vd
    = find_first_bundled_edge_with_my_edge(old_edge,g);
  BOOST CHECK (get my bundled edge (vd, g)
    == old edge
  );
  const my bundled edge new edge{"Diggy"};
  set my bundled edge (new edge, vd, g);
  BOOST CHECK (get my bundled edge (vd,g)
    = new edge
  );
}
```

7.5 Storing a graph with bundled edges and vertices as a .dot

If you used the 'create_bundled_edges_and_vertices_k3_graph' function (algorithm 99) to produce a K_3 graph with edges and vertices associated with my_bundled_edge and my_bundled_vertex objects, you can store these my_bundled_edges and my_bundled_vertex-es additionally with algorithm 110:

Algorithm 110 Storing a graph with bundled edges and vertices as a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "make_bundled_vertices_writer.h"
#include "make bundled edges writer.h"
template <typename graph>
void save_bundled_edges_and_vertices_graph_to_dot(
  const graph& g,
  const std::string& filename
  std::ofstream f(filename);
  boost::write graphviz(
    f,
    g,
    make_bundled_vertices_writer(g),
    make_bundled_edges_writer(g)
  );
}
```

7.6 Load a directed graph with bundled edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with bundled edges and vertices is loaded, as shown in algorithm 111:

 $\bf Algorithm~111~{\rm Loading~a~directed~graph~with~bundled~edges~and~vertices~from~a~.dot~file$

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create\_empty\_directed\_bundled\_edges\_and\_vertices\_graph
    . h "
#include "is regular file.h"
#include "graphviz decode.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my_bundled_vertex,
  my\_bundled\_edge
load directed bundled edges and vertices graph from dot (
  const std::string& dot filename
  if (!is regular file(dot filename))
    std::stringstream msg;
    msg << func << ": file;"
      << dot filename << "'_not_found"</pre>
    throw std::invalid argument(msg.str());
  }
  std::ifstream f(dot filename.c str());
  auto g =
     create empty directed bundled edges and vertices graph
      ();
  boost::dynamic properties dp(boost::
     ignore other properties);
  dp.property("label", get(&my_bundled_vertex::m_name, g))
  dp.property("comment", get(&my_bundled_vertex::
     m description, g));
  dp.property("width", get(&my_bundled_vertex::m_x, g));
  dp.property("height", get(&my_bundled_vertex::m_y, g));
  dp.property("edge id",get(&my bundled edge::m name, g))
  dp.property("label",get(&my_bundled_edge::m_name, g));
  dp.property("comment", get(&my_bundled_edge::
     m description, g));
  dp.property("width", get(& bundled edge::m width, g))
  dp.property("height", get(&my bundled edge::m height, g
  boost::read graphviz(f,g,dp);
  //Decode vertices
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label' to the edge name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

 $Algorithm\ 112\ shows\ how\ to\ use\ the\ `load_directed_bundled_edges_and_vertices_graph_from_dot' function:$

Algorithm 112 Demonstration of the 'load directed bundled edges and vertices graph from dot'function

```
#include <boost/test/unit test.hpp>
#include "create bundled edges and vertices markov chain.
   h"
#include "get sorted bundled vertex my vertexes.h"
#include "
   load directed bundled edges and vertices graph from dot
    . h"
#include "save bundled edges and vertices graph to dot.h"
BOOST AUTO TEST CASE(
   test load directed bundled edges and vertices graph from dot
{
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled edges and vertices markov chain();
  const std::string filename{
    "create bundled edges and vertices markov chain.dot"
  save bundled edges and vertices graph to dot(g,
     filename);
  const auto h
       load directed bundled edges and vertices graph from dot
      filename
    );
  BOOST\_CHECK(num\_edges(g) == num\_edges(h));
  BOOST CHECK(num vertices(g) == num vertices(h));
  BOOST\_CHECK(\,get\_sorted\_bundled\_vertex\_my\_vertexes(\,g\,)
    = get sorted bundled vertex my vertexes(h)
  );
}
```

This demonstration shows how the Markov chain is created using the 'create_bundled_edges_and_vertices_markov_chain' function (algorithm 96), saved and then loaded.

7.7 Load an undirected graph with bundled edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with bundled edges and vertices is loaded, as shown in algorithm 113:

 $\bf Algorithm~113~{\rm Loading}$ an undirected graph with bundled edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create_empty_undirected_bundled_edges_and_vertices_graph
    . h "
#include "is regular file.h"
#include "graphviz decode.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex,
  my\_bundled\_edge
load undirected bundled edges and vertices graph from dot
  const std::string& dot filename
  if (!is regular file(dot filename))
    std::stringstream msg;
    \mathrm{msg} \; << \; \_\_\mathrm{func}\_\_ \; << \; ": \_ \, \mathrm{file} \, \_ \, , \, "
      << dot filename << "'.not_found"</pre>
    throw std::invalid_argument(msg.str());
  std::ifstream f(dot filename.c str());
      create empty undirected bundled edges and vertices graph
  boost::dynamic properties dp(boost::
      ignore other properties);
  dp.property("label",get(&my_bundled_vertex::m_name, g))
  dp.property("comment", get(&my_bundled_vertex::
      m description, g));
  dp.property("width", get(&my_bundled_vertex::m_x, g));
  \tt dp.property("height", get(\&my\_bundled\_vertex::m\_y, g));\\
  dp.property("edge_id",get(&my_bundled_edge::m_name, g))
  dp.property("label",get(&my_bundled_edge::m_name, g));
  dp.property("comment", get(&my_bundled_edge::
      m description, g));
                             126
  dp.property("width", get(&my bundled edge::m width, g))
  dp.property("height", get(&my_bundled_edge::m_height, g
  boost::read graphviz(f,g,dp);
  //Decode vertices
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 7.6 describes the rationale of this function.

Algorithm 114 shows how to use the 'load_undirected_bundled_vertices_graph_from_dot' function:

Algorithm 114 Demonstration of the 'load_undirected_bundled_edges_and_vertices_graph_from_dot'fundirec

```
#include <boost/test/unit_test.hpp>
#include "create bundled edges and vertices k3 graph.h"
#include "get sorted bundled vertex my vertexes.h"
#include "
   load undirected bundled edges and vertices graph from dot
   . h"
#include "save bundled edges and vertices graph to dot.h"
BOOST AUTO TEST CASE(
   test load undirected bundled edges and vertices graph from dot
{
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled edges and vertices k3 graph();
  const std::string filename{
    "create bundled edges and vertices k3 graph.dot"
  save bundled edges and vertices graph to dot(g,
     filename);
  const auto h
       load undirected bundled edges and vertices graph from dot
      filename
 BOOST CHECK(num edges(g) = num edges(h));
 BOOST CHECK(num vertices(g) = num vertices(h));
  BOOST_CHECK(get_sorted_bundled_vertex_my_vertexes(g)
    == get_sorted_bundled_vertex_my_vertexes(h)
  );
}
```

This demonstration shows how K_2 with bundled vertices is created using the 'create_bundled_vertices_k2_graph' function (algorithm ??), saved and then loaded. The loaded graph is checked to be a graph similar to the original.

8 Building graphs with a graph name

Up until now, the graphs created have had no properties themselves. Sure, the edges and vertices have had properties, but the graph itself has had none. Until now.

In this chapter, graphs will be created with a graph name of type std::string

- An empty directed graph with a graph name: see chapter
- An empty undirected graph with a graph name: see chapter
- A two-state Markov chain with a graph name: see chapter
- K_3 with a graph name: see chapter

In the process, some basic (sometimes bordering trivial) functions are shown:

- Getting a graph its name: see chapter
- Setting a graph its name: see chapter

8.1 Create an empty directed graph with a graph name property

Algorithm 115 shows the function to create an empty directed graph with a graph name.

Algorithm 115 Creating an empty directed graph with a graph name

```
#include <boost/graph/adjacency_list.hpp>
boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::directedS,
   boost::no_property,
   boost::no_property,
   boost::property <
      boost::graph_name_t,std::string
   >
   create_empty_directed_graph_with_graph_name() noexcept
   {
      return {};
}
```

This boost::adjacency list is of the following type:

- the first 'boost::vecS': select (that is what the 'S' means) that out edges are stored in a std::vector. This is the default way.
- the second 'boost::vecS': select that the graph vertices are stored in a std::vector. This is the default way.
- 'boost::directedS': select that the graph is directed. This is the default selectedness
- the first 'boost::no_property': the vertices have no properties. This is the default (non-)property
- the second 'boost::no_property': the vertices have no properties. This is the default (non-)property
- 'boost::property
boost::graph_name_t, std::string>': the graph itself has a single property: its boost::graph_name has type std::string

Algorithm 116 demonstrates the 'create_empty_directed_graph_with_graph_name' function.

8.2 Create an empty undirected graph with a graph name property

Algorithm 117 shows the function to create an empty undirected graph with a graph name.

Algorithm 117 Creating an empty undirected graph with a graph name

```
#include <boost/graph/adjacency_list.hpp>
boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::no_property,
   boost::no_property,
   boost::property <
      boost::graph_name_t,std::string
   >
   create_empty_undirected_graph_with_graph_name() noexcept
   {
      return {};
}
```

This code is very similar to the code described in chapter 115, except that the directness (the third template argument) is undirected (due to the boost::undirectedS).

 $Algorithm\ 118\ demonstrates\ the\ `create_empty_undirected_graph_with_graph_name' function.$

Algorithm 118 Demonstration of 'create empty undirected graph with graph name'

8.3 Get a graph its name property

Algorithm 119 Get a graph its name

```
#include <string>
#include <boost/graph/properties.hpp>

template <typename graph>
std::string get_graph_name(
    const graph& g
) noexcept
{
    return get_property(
        g, boost::graph_name
    );
}
```

Algorithm 120 demonstrates the 'get_graph_name' function.

Algorithm 120 Demonstration of 'get graph name'

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph_with_graph_name.h"
#include "get_graph_name.h"

#include "set_graph_name.h"

BOOST_AUTO_TEST_CASE(test_get_graph_name)
{
    auto g = create_empty_directed_graph_with_graph_name();
    const std::string name{"Dex"};
    set_graph_name(name, g);
    BOOST_CHECK(get_graph_name(g) == name);
}
```

8.4 Set a graph its name property

Algorithm 121 Set a graph its name

```
#include <cassert>
#include <string>
#include <boost/graph/properties.hpp>

template <typename graph>
void set_graph_name(
    const std::string& name,
    graph& g
) noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);
    get_property(g, boost::graph_name) = name;
}
```

Algorithm 122 demonstrates the 'set graph name' function.

Algorithm 122 Demonstration of 'set graph name'

```
#include <boost/test/unit_test.hpp>
#include "create_empty_directed_graph_with_graph_name.h"
#include "get_graph_name.h"
#include "set_graph_name.h"

BOOST_AUTO_TEST_CASE(test_set_graph_name)
{
    auto g = create_empty_directed_graph_with_graph_name();
    const std::string name{"Dex"};
    set_graph_name(name, g);
    BOOST_CHECK(get_graph_name(g) == name);
}
```

8.5 Create a directed graph with a graph name property

8.5.1 Graph

See figure 5.

8.5.2 Function to create such a graph

Algorithm 123 shows the function to create an empty directed graph with a graph name.

Algorithm 123 Creating a two-state Markov chain with a graph name

```
#include <cassert>
#include "create_empty_directed_graph_with_graph_name.h"
#include "set graph name.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::no property,
  boost::no_property,
  boost::property<boost::graph name t, std::string>
create markov chain with graph name() noexcept
  auto g = create_empty_directed_graph_with_graph_name();
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  boost::add edge(vd a, vd a, g);
  boost::add_edge(vd_a, vd_b, g);
  boost::add edge(vd b, vd a, g);
  boost::add edge(vd b, vd b, g);
  set_graph_name("Two-state_Markov_chain", g);
  return g;
```

8.5.3 Creating such a graph

Algorithm 124 demonstrates the 'create_markov_chain_with_graph_name' function.

Algorithm 124 Demonstration of 'create markov chain with graph name'

```
#include <boost/test/unit_test.hpp>
#include "create_markov_chain_with_graph_name.h"
#include "get_graph_name.h"

BOOST_AUTO_TEST_CASE(
    test_create_markov_chain_with_graph_name)
{
    const auto g = create_markov_chain_with_graph_name();
    BOOST_CHECK(boost::num_vertices(g) == 2);
    BOOST_CHECK(boost::num_edges(g) == 4);
    BOOST_CHECK(get_graph_name(g) == "Two-state_Markov_chain");
}
```

8.5.4 The .dot file produced

Algorithm 125 .dot file created from the 'create_markov_chain_with_graph_name' function (algorithm 123), converted from graph to .dot file using algorithm 55

```
digraph G {
name="Two-state Markov chain";
0;
1;
0->0;
0->1;
1->0;
1->1;
}
```

8.5.5 The .svg file produced

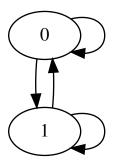


Figure 26: .svg file created from the 'create_markov_chain_with_graph_name' function (algorithm 123) its .dot file, converted from .dot file to .svg using algorithm 136

8.6 Create an undirected graph with a graph name property

8.6.1 Graph

See figure 7.

8.6.2 Function to create such a graph

Algorithm 126 shows the function to create K2 graph with a graph name.

Algorithm 126 Creating a K2 graph with a graph name

```
#include "create empty undirected graph with graph name.h
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::no_property ,
  boost::no property,
  boost::property<boost::graph name t, std::string>
create k2 graph with graph name() noexcept
  auto \ g = create\_empty\_undirected\_graph\_with\_graph\_name
      ();
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  boost::add edge(vd a, vd b, g);
  get_property(g,boost::graph_name) = "K2";
  return g;
}
```

8.6.3 Creating such a graph

Algorithm 127 demonstrates the 'create_k2_graph_with_graph_name' function.

Algorithm 127 Demonstration of 'create_k2_graph_with_graph_name'

```
#include <boost/test/unit_test.hpp>
#include "create_k2_graph_with_graph_name.h"
#include "get_graph_name.h"

BOOST_AUTO_TEST_CASE(test_create_k2_graph_with_graph_name)
{
    const auto g = create_k2_graph_with_graph_name();
    BOOST_CHECK(boost::num_vertices(g) == 2);
    BOOST_CHECK(boost::num_edges(g) == 1);
    BOOST_CHECK(get_graph_name(g) == "K2");
}
```

8.6.4 The .dot file produced

Algorithm 128 .dot file created from the 'create_k2_graph_with_graph_name' function (algorithm 126), converted from graph to .dot file using algorithm 55

```
graph G {
name="K2";
0;
1;
0--1;
}
```

8.6.5 The .svg file produced

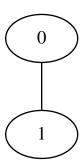


Figure 27: .svg file created from the 'create_k2_graph_with_graph_name' function (algorithm 126) its .dot file, converted from .dot file to .svg using algorithm 136

9 Working on graphs with a graph name

9.1 Storing a graph with a graph name property as a .dot file

This works:

Algorithm 129 Storing a graph with a graph name as a .dot file

```
#include <string>
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get graph name.h"
\mathbf{template} \ <\!\!\mathbf{typename} \ \mathbf{graph}\!\!>
void save graph with graph name to dot(
  const graph& g,
  const std::string& filename
  std::ofstream f(filename);
  boost::write graphviz(
    f,
    g,
    boost::default writer(),
    boost::default_writer(),
    //Unsure\ if\ this\ results\ in\ a\ graph
    //that can be loaded correctly
     //from \ a \ . dot \ file
    [\&g](std::ostream\&os) {
       os << "name=\""
         << get_graph_name(g)
         << "\";\n";
  );
}
```

9.2 Loading a directed graph with a graph name property from a .dot file

This will result in a directed graph with a name:

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "is regular file.h"
boost::adjacency_list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::no_property,
  boost::no property,
  boost::property<
    boost::graph_name_t, std::string
>
load_directed_graph_with_graph_name_from_dot(
  const std::string& dot filename
  using graph = boost::adjacency_list<</pre>
    boost :: vecS,
    boost :: vecS,
    boost::directedS,
    boost::no_property,
    boost::no_property,
    boost::property<
      boost::graph name t, std::string
  >;
  if (!is_regular_file(dot_filename))
    std::stringstream msg;
    msg << __func__ << ":_file_',"
      << dot filename << "'onot_found"</pre>
    throw std::invalid_argument(msg.str());
  }
  graph g;
  boost::ref property map<graph*,std::string>
  graph name{
    get_property(g,boost::graph_name)
  boost::dynamic_properties dp{
    boost::ignore_other_properties
  dp.property("name",graph_name);
  std::ifstream f(dot_filename.c_str());
  boost::read graphviz(f,g,dp);
  return g;
```

9.3 Loading an undirected graph with a graph name property from a .dot file $\frac{1}{2}$

This will result in an undirected graph with a name:

 $\bf Algorithm~131$ Loading an undirected graph with a graph name from a .dot file

```
#include <fstream>
#include <string>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_graph_with_graph_name.h
#include "is_regular_file.h"
boost::adjacency_list<
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::no property,
  boost::no_property,
  boost::property<
    boost::graph_name_t, std::string
  >
load_undirected_graph_with_graph_name_from_dot(
  const std::string& dot filename
{
  using graph = boost::adjacency list<
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::no property,
    boost::no_property,
    boost::property<
       boost::graph name t, std::string
  if (!is regular file(dot filename))
    std::stringstream msg;
    \mathrm{msg} \; << \; \_ \mathrm{func} \_ \; << \; ": \, \_ \, \mathrm{file} \, \_ \, , \, "
      << dot_filename << "',not_found"</pre>
    throw std::invalid_argument(msg.str());
  graph g;
  boost::ref_property_map<graph*,std::string>
  graph\_name\{
    get_property(g,boost::graph_name)
  };
  boost::dynamic properties 144){
    boost::ignore other properties
  };
  dp.property("name",graph_name);
  std::ifstream f(dot filename.c str());
  boost::read graphviz(f,g,dp);
  return g;
```

10 Other graph functions

Some functions that did not fit in.

10.1 Encode a std::string to a Graphviz-friendly format

You may want to use a label with spaces, comma's and/or quotes. Saving and loading these, will result in problem. This function replaces these special characters by a rare combination of ordinary characters.

Algorithm 132 Encode a std::string to a Graphviz-friendly format

```
#include <boost/algorithm/string/replace.hpp>

std::string graphviz_encode(std::string s) noexcept
{
   boost::algorithm::replace_all(s,",",","$$$COMMA$$$");
   boost::algorithm::replace_all(s,",","$$$SPACE$$$");
   boost::algorithm::replace_all(s,"\"","$$$QUOTE$$$");
   return s;
}
```

10.2 Decode a std::string from a Graphviz-friendly format

This function undoes the 'graphviz_encode' function (algorithm 132) and thus converts a Graphviz-friendly std::string to the original human-friendly std::string.

 ${\bf Algorithm~133~Decode~a~std::string~from~a~Graphviz-friendly~format~to~a~human-friendly~format}$

```
#include <boost/algorithm/string/replace.hpp>

std::string graphviz_decode(std::string s) noexcept
{
   boost::algorithm::replace_all(s,"$$$COMMA$$$",",");
   boost::algorithm::replace_all(s,"$$$SPACE$$$","\"");
   boost::algorithm::replace_all(s,"$$$QUOTE$$$","\"");
   return s;
}
```

10.3 Check if a std::string is Graphviz-friendly

There are pieces where I check if a std::string is Graphviz-friendly. This is done only where it matters. If it is tested not to matter, 'is_graphviz_friendly' is absent.

Algorithm 134 Check if a std::string is Graphviz-friendly

```
#include "graphviz_encode.h"
bool is_graphviz_friendly(const std::string& s) noexcept
{
   return graphviz_encode(s) == s;
}
```

11 Misc functions

These are some function I needed for creating this tutorial. Although they are not important for working with graphs, I used these heavily. These functions may be compiler-dependent, platform-dependent and/or there may be superior alternatives. I just add them for completeness.

11.1 Getting a data type as a std::string

This function will only work under GCC. I found this code at: http://stackoverflow.com/questions/1055452/c-get-name-of-type-in-template. Thanks to 'm-dudley' (Stack Overflow user page at http://stackoverflow.com/users/111327/m-dudley).

Algorithm 135 Getting a data type its name as a std::string

```
#include < cstdlib >
#include <string>
#include <typeinfo>
#include <cxxabi.h>
template < typename T >
std::string get type name() noexcept
  std::string tname = typeid(T).name();
  int status = -1;
  char * const demangled name{
    abi::__cxa_demangle(
      tname.c_str(), NULL, NULL, &status
  };
  if(status == 0) {
    tname = demangled name;
    std::free(demangled name);
  }
  return tname;
```

11.2 Convert a .dot to .svg

All illustrations in this tutorial are created by converting .dot to a .svg ('Scalable Vector Graphic') file. This function assumes the program 'dot' is installed, which is part of Graphviz.

```
#include <cassert>
#include <string>
#include <iostream>
#include <sstream>
#include <stdexcept>
#include "has dot.h"
#include "is regular file.h"
#include "is_valid_dot_file.h"
void convert dot to svg(
  const std::string& dot filename,
  const std::string& svg filename
{
  if (!has dot())
    std::stringstream msg;
    msg << func << ":_'dot'_cannot_be_found._"
      << "type_'sudo_apt-get_install_graphviz'_in_the_</pre>
           command_line"
    throw std::runtime error(msg.str());
  if (!is valid dot file(dot filename))
    std::stringstream msg;
    msg << func << ": _file _'" << dot filename
      << " 'Jis_not_a_valid_DOT_language"</pre>
    throw std::invalid argument(msg.str());
  std::stringstream cmd;
  \label{eq:cmd} \mbox{cmd} << \mbox{"dot}\mbox{$\downarrow$-Tsvg\_"$} << \mbox{dot filename} << \mbox{"$\mbox{$\downarrow$-}o\_"$} <<
      svg filename;
  const int error {
    std::system(cmd.str().c_str())
  };
  if (error)
    std::cerr << __func__ << ":warning:_command_'"
<< cmd.str() << "',_resulting_in_error_"
      << error;
  if (!is regular file(svg filename))
     std::stringstream msg;
    msg << \_\_func\_\_ << ": \_falffed\_to\_create\_SVG\_output\_
         file_',"
      << svg_filename << "'"</pre>
    throw std::runtime error(msg.str());
}
```

'convert_dot_to_svg' makes a system call to the program 'dot' to convert the .dot file to an .svg file.

11.3 Check if a file exists

Not the most smart way perhaps, but it does only use the STL.

Algorithm 137 Check if a file exists

```
#include <fstream>
bool is_regular_file(const std::string& filename)
    noexcept
{
    std::fstream f;
    f.open(filename.c_str(),std::ios::in);
    return f.is_open();
}
```

12 Errors

Some common errors.

12.1 Formed reference to void

This compile-time error occurs when you create a graph without a certain property, then subsequently reading that property, as in algorithm 138:

Algorithm 138 Creating the error 'formed reference to void'

```
#include "create_k2_graph.h"
#include "get_vertex_names.h"

void formed_reference_to_void() noexcept
{
    get_vertex_names(create_k2_graph());
}
```

In algorithm 138 a graph is created with vertices of no properties. Then the names of these vertices, which do not exists, are tried to be read. If you want to read the names of the vertices, supply a graph that has this property.

12.2 No matching function for call to 'clear out edges'

This compile-time error occurs when you want to clear the outward edges from a vertex in an undirected graph.

Algorithm 139 Creating the error 'no matching function for call to clear out edges'

```
#include "create_k2_graph.h"

void no_matching_function_for_call_to_clear_out_edges()
    noexcept
{
    auto g = create_k2_graph();
    const auto vd = *vertices(g).first;
    boost::clear_in_edges(vd,g);
}
```

In algorithm 139an undirected graph is created, a vertex descriptor is obtained, then itsout edges are tried to be cleared. Either use a directed graph (which has out edges), or use the 'boost::clear vertex' function instead.

12.3 No matching function for call to 'clear_in_edges'

See chapter 12.2.

12.4 Undefined reference to boost::detail::graph::read graphviz new

You will have to link against the Boost.Graph and Boost.Regex libraries. In Qt Creator, this is achieved by adding these lines to your Qt Creator project file:

$$LIBS += -lboost graph - lboost regex$$

12.5 Property not found: node id

When loading a graph from file (as in chapter 3.13) you will be using boost::read_graphviz. boost::read_graphviz needs a third argument, of type boost::dynamic_properties. When a graph does not have properties, do not use a default constructed version, but initialize with 'boost::ignore_other_properties' as a constructor argument instead. Algorithm 140 shows how to trigger this run-time error.

Algorithm 140 Creating the error 'Property not found: node id'

```
#include <cassert>
#include <fstream>
#include "is regular file.h"
#include "create empty undirected graph.h"
#include "create k2 graph.h"
#include "save_graph_to_dot.h"
void property_not_found_node_id() noexcept
  const std::string dot filename{"
     property_not_found_node_id.dot"};
  //Create a file
    const auto g = create k2 graph();
    save graph to dot(g, dot filename);
    assert (is regular file (dot filename));
  //Try to read that file
  std::ifstream f(dot_filename.c_str());
  auto g = create_empty_undirected_graph();
  //Line\ below\ should\ have\ been
  // boost::dynamic_properties dp(boost::
      ignore\_other\_properties);
  boost::dynamic properties dp; //Error
  try {
    boost::read graphviz(f,g,dp);
  catch (std::exception&) {
    return; //Should get here
  assert (! "Should_not_get_here");
```

12.6 Stream zeroes

```
When loading a graph from a .dot file, in operator>>, I encountered reading zeroes, where I expected an XML formatted string:

std::istream& ribi::cmap::operator>>(std::istream& is, my_class& any_class) noex

{

std::string s;
```

```
is >> s; //s has an XML format
  assert(s != "0");
  any class = my \ class(s);
  return is;
}
  This was because I misconfigured the reader. I did (heavily simplified code):
graph load from dot(const std::string& dot filename)
  std::ifstream f(dot filename.c str());
  graph g;
  boost::dynamic properties dp;
  dp.property("node_id", get(boost::vertex_custom_type, g));
  dp.property("label", get(boost::vertex custom type, g));
  boost::read graphviz(f,g,dp);
  return g;
}
  Where it should have been:
graph load from dot(const std::string& dot filename)
  std::ifstream f(dot_filename.c_str());
  graph g;
  boost::dynamic_properties dp(boost::ignore_other_properties);
  dp.property("label", get(boost::vertex custom type, g));
  boost::read_graphviz(f,g,dp);
  return g;
}
  The explanation is that by setting the boost::dynamic property 'node id'
to 'boost::vertex custom type', operator>> will receive the node indices.
  An alternative, but less clean solution, is to let operator>> ignore the node
indices:
std::istream& ribi::cmap::operator>>(std::istream& is, my_class& any_class) noex
  std::string s;
  is >> s; //s has an XML format
  if (!is xml(s)) { //Ignore node index
    any_class_class = my_class();
  else {
    any_class_class = my_class(s);
  return is;
}
```

13 Appendix

13.1 List of all edge, graph and vertex properties

The following list is obtained from the file 'boost/graph/properties.hpp'.

Edge	Graph	Vertex
edge_all	graph_all	vertex_all
edge_bundle	graph_bundle	vertex_bundle
edge_capacity	graph_name	vertex_centrality
edge_centrality	graph_visitor	vertex_color
edge_color		vertex_current_degree
edge_discover_time		vertex_degree
edge_finished		vertex_discover_time
edge_flow		vertex_distance
$edge_global$		vertex_distance2
edge_index		vertex_finish_time
edge_local		vertex_global
edge_local_index		vertex_in_degree
edge_name		vertex_index
$edge_owner$		vertex_index1
edge_residual_capacity		vertex_index2
edge_reverse		vertex_local
edge_underlying		vertex_local_index
edge_update		vertex_lowpoint
edge_weight		vertex_name
edge_weight2		vertex_out_degree
		vertex_owner
		vertex_potential
		vertex_predecessor
		vertex_priority
		vertex_rank
		vertex_root
		vertex_underlying
		vertex_update

13.2 Graphviz attributes

List created from www.graphviz.org/content/attrs, where only the attributes that are supported by all formats are listed:

Edge	Graph	Vertex
arrowhead	_background	color
arrowsize	bgcolor	colorscheme
arrowtail	center	comment
color	charset	distortion
colorscheme	color	fillcolor
comment	colorscheme	fixedsize
decorate	comment	fontcolor
dir	concentrate	fontname
fillcolor	fillcolor	fontsize
fontcolor	fontcolor	gradientangle
fontname	fontname	height
fontsize	fontpath	image
gradientangle	fontsize	imagescale
headclip	forcelabels	label
headlabel	gradientangle	labelloc
headport	imagepath	layer
label	label	margin
labelangle	labeljust	nojustify
labeldistance	labelloc	orientation
labelfloat	landscape	penwidth
labelfontcolor	layerlistsep	peripheries
labelfontname	layers	pos
labelfontsize	layerselect	regular
layer	layersep	samplepoints
nojustify	layout	shape
penwidth	margin	shapefile
pos	nodesep	sides
style	nojustify	skew
tailclip	orientation	sortv
taillabel	outputorder	style
tailport	pack	width
weight	packmode	xlabel
xlabel	pad	Z
	page	
	pagedir	
	penwidth	
	quantum	
	ratio	
	rotate	
	size	
	sortv	
	splines	
	style	
	viewport	

References

- [1] Eckel Bruce. Thinking in c++, volume 1. 2002.
- [2] Marshall P Cline, Greg Lomow, and Mike Girou. C++ FAQs. Pearson Education, 1998.
- [3] Jarrod Hollingworth, Bob Swart, and Jamie Allsop. C++ Builder 5 Developer's Guide with Cdrom. Sams, 2000.
- [4] John Lakos. Large-scale C++ software design, volume 10. Addison-Wesley Reading, 1996.
- [5] Jesse Liberty. Sams teach yourself C++ in 24 hours. Sams Publishing, 2001.
- [6] Steve McConnell. Code complete. Pearson Education, 2004.
- [7] Scott Meyers. Effective C++: 55 specific ways to improve your programs and designs. Pearson Education, 2005.
- [8] Jeremy G Siek, Lie-Quan Lee, and Andrew Lumsdaine. Boost Graph Library: User Guide and Reference Manual, The. Pearson Education, 2001.
- [9] Bjarne Stroustrup. The C++ Programming Language (3rd edition). 1997.
- [10] Bjarne Stroustrup. The C++ Programming Language (4th edition). 2013.
- [11] Herb Sutter and Andrei Alexandrescu. C++ coding standards: 101 rules, guidelines, and best practices. Pearson Education, 2004.

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