

# CRACKING the CODING INTERVIEW

189 PROGRAMMING QUESTIONS & SOLUTIONS



**GAYLE LAAKMANN McDOWELL**

*Author of Cracking the PM Interview and Cracking the Tech Career*

**6<sup>TH</sup>**  
**EDITION**



**CRACKING**  
*the*  
**CODING INTERVIEW**

**6TH EDITION**

**ALSO BY GAYLE LAAKMANN McDOWELL**

**CRACKING THE PM INTERVIEW**

HOW TO LAND A PRODUCT MANAGER JOB IN TECHNOLOGY

**CRACKING THE TECH CAREER**

INSIDER ADVICE ON LANDING A JOB AT GOOGLE, MICROSOFT, APPLE, OR ANY TOP TECH COMPANY

# **CRACKING**

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# **CODING INTERVIEW**

***6th Edition***

189 Programming Questions and Solutions

**GAYLE LAAKMANN McDOWELL**  
**Founder and CEO, CareerCup.com**

CareerCup, LLC  
Palo Alto, CA

CRACKING THE CODING INTERVIEW, SIXTH EDITION

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*For Davis and Tobin,  
and all the things that bring us joy in life.*

# Introduction

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Join us at [www.CrackingTheCodingInterview.com](http://www.CrackingTheCodingInterview.com) to download the complete solutions, contribute or view solutions in other programming languages, discuss problems from this book with other readers, ask questions, report issues, view this book's errata, and seek additional advice.

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Dear Reader,

Let's get the introductions out of the way.

I am not a recruiter. I am a software engineer. And as such, I know what it's like to be asked to whip up brilliant algorithms on the spot and then write flawless code on a whiteboard. I know because I've been asked to do the same thing—in interviews at Google, Microsoft, Apple, and Amazon, among other companies.

I also know because I've been on the other side of the table, asking candidates to do this. I've combed through stacks of resumes to find the engineers who I thought might be able to actually pass these interviews. I've evaluated them as they solved—or tried to solve—challenging questions. And I've debated in Google's Hiring Committee whether a candidate did well enough to merit an offer. I understand the full hiring circle because I've been through it all, repeatedly.

And you, reader, are probably preparing for an interview, perhaps tomorrow, next week, or next year. I am here to help you solidify your understanding of computer science fundamentals and then learn how to apply those fundamentals to crack the coding interview.

The 6th edition of *Cracking the Coding Interview* updates the 5th edition with 70% more content: additional questions, revised solutions, new chapter introductions, more algorithm strategies, hints for all problems, and other content. Be sure to check out our website, [CrackingTheCodingInterview.com](http://CrackingTheCodingInterview.com), to connect with other candidates and discover new resources.

I'm excited for you and for the skills you are going to develop. Thorough preparation will give you a wide range of technical and communication skills. It will be well worth it, no matter where the effort takes you!

I encourage you to read these introductory chapters carefully. They contain important insight that just might make the difference between a "hire" and a "no hire."

**And remember—interviews are hard!** In my years of interviewing at Google, I saw some interviewers ask "easy" questions while others ask harder questions. But you know what? Getting the easy questions doesn't make it any easier to get the offer. Receiving an offer is not about solving questions flawlessly (very few candidates do!). Rather, it is about answering questions *better than other candidates*. So don't stress out when you get a tricky question—everyone else probably thought it was hard too. It's okay to not be flawless.

Study hard, practice—and good luck!

Gayle L. McDowell

Founder/CEO, [CareerCup.com](http://CareerCup.com)

Author of *Cracking the PM Interview* and *Cracking the Tech Career*

# Introduction

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## Something's Wrong

We walked out of the hiring meeting frustrated—again. Of the ten candidates we reviewed that day, none would receive offers. Were we being too harsh, we wondered?

I, in particular, was disappointed. We had rejected one of *my* candidates. A former student. One I had referred. He had a 3.73 GPA from the University of Washington, one of the best computer science schools in the world, and had done extensive work on open-source projects. He was energetic. He was creative. He was sharp. He worked hard. He was a true geek in all the best ways.

But I had to agree with the rest of the committee: the data wasn't there. Even if my emphatic recommendation could sway them to reconsider, he would surely get rejected in the later stages of the hiring process. There were just too many red flags.

Although he was quite intelligent, he struggled to solve the interview problems. Most successful candidates could fly through the first question, which was a twist on a well-known problem, but he had trouble developing an algorithm. When he came up with one, he failed to consider solutions that optimized for other scenarios. Finally, when he began coding, he flew through the code with an initial solution, but it was riddled with mistakes that he failed to catch. Though he wasn't the worst candidate we'd seen by any measure, he was far from meeting the "bar." Rejected.

When he asked for feedback over the phone a couple of weeks later, I struggled with what to tell him. Be smarter? No, I knew he was brilliant. Be a better coder? No, his skills were on par with some of the best I'd seen.

Like many motivated candidates, he had prepared extensively. He had read K&R's classic C book, and he'd reviewed CLRS' famous algorithms textbook. He could describe in detail the myriad of ways of balancing a tree, and he could do things in C that no sane programmer should ever want to do.

I had to tell him the unfortunate truth: those books aren't enough. Academic books prepare you for fancy research, and they will probably make you a better software engineer, but they're not sufficient for interviews. Why? I'll give you a hint: Your interviewers haven't seen red-black trees since *they* were in school either.

To crack the coding interview, you need to prepare with *real* interview questions. You must practice on *real* problems and learn their patterns. It's about developing a fresh algorithm, not memorizing existing problems.

**Cracking the Coding Interview** is the result of my first-hand experience interviewing at top companies and later coaching candidates through these interviews. It is the result of hundreds of conversations with candidates. It is the result of the thousands of questions contributed by candidates and interviewers. And it's the result of seeing so many interview questions from so many firms. Enclosed in this book are 189 of the best interview questions, selected from thousands of potential problems.

## My Approach

The focus of **Cracking the Coding Interview** is algorithm, coding, and design questions. Why? Because while you can and will be asked behavioral questions, the answers will be as varied as your resume. Likewise, while many firms will ask so-called "trivia" questions (e.g., "What is a virtual function?"), the skills developed through practicing these questions are limited to very specific bits of knowledge. The book will briefly touch on some of these questions to show you what they're like, but I have chosen to allocate space to areas where there's more to learn.

### My Passion

Teaching is my passion. I love helping people understand new concepts and giving them tools to help them excel in their passions.

My first official experience teaching was in college at the University of Pennsylvania, when I became a teaching assistant for an undergraduate computer science course during my second year. I went on to TA for several other courses, and I eventually launched my own computer science course there, focused on hands-on skills.

As an engineer at Google, training and mentoring new engineers were some of the things I enjoyed most. I even used my "20% time" to teach two computer science courses at the University of Washington.

Now, years later, I continue to teach computer science concepts, but this time with the goal of preparing engineers at startups for their acquisition interviews. I've seen their mistakes and struggles, and I've developed techniques and strategies to help them combat those very issues.

***Cracking the Coding Interview*, *Cracking the PM Interview*, *Cracking the Tech Career*, and *CareerCup*** reflect my passion for teaching. Even now, you can often find me "hanging out" at [CareerCup.com](http://CareerCup.com), helping users who stop by for assistance.

Join us.

Gayle L. McDowell

## The Interview Process

At most of the top tech companies (and many other companies), algorithm and coding problems form the largest component of the interview process. Think of these as problem-solving questions. The interviewer is looking to evaluate your ability to solve algorithmic problems you haven't seen before.

Very often, you might get through only one question in an interview. Forty-five minutes is not a long time, and it's difficult to get through several different questions in that time frame.

You should do your best to talk out loud throughout the problem and explain your thought process. Your interviewer might jump in sometimes to help you; let them. It's normal and doesn't really mean that you're doing poorly. (That said, of course not needing hints is even better.)

At the end of the interview, the interviewer will walk away with a gut feel for how you did. A numeric score might be assigned to your performance, but it's not actually a quantitative assessment. There's no chart that says how many points you get for different things. It just doesn't work like that.

Rather, your interviewer will make an assessment of your performance, usually based on the following:

- Analytical skills: Did you need much help solving the problem? How optimal was your solution? How long did it take you to arrive at a solution? If you had to design/architect a new solution, did you structure the problem well and think through the tradeoffs of different decisions?
- Coding skills: Were you able to successfully translate your algorithm to reasonable code? Was it clean and well-organized? Did you think about potential errors? Did you use good style?
- Technical knowledge / Computer Science fundamentals: Do you have a strong foundation in computer science and the relevant technologies?
- Experience: Have you made good technical decisions in the past? Have you built interesting, challenging projects? Have you shown drive, initiative, and other important factors?
- Culture fit / Communication skills: Do your personality and values fit with the company and team? Did you communicate well with your interviewer?

The weighting of these areas will vary based on the question, interviewer, role, team, and company. In a standard algorithm question, it might be almost entirely the first three of those.

### ► Why?

This is one of the most common questions candidates have as they get started with this process. Why do things this way? After all,

1. Lots of great candidates don't do well in these sorts of interviews.

2. You could look up the answer if it did ever come up.
3. You rarely have to use data structures such as binary search trees in the real world. If you did need to, you could surely learn it.
4. Whiteboard coding is an artificial environment. You would never code on the whiteboard in the real world, obviously.

These complaints aren't without merit. In fact, I agree with all of them, at least in part.

At the same time, there is reason to do things this way for some—not all—positions. It's not important that you agree with this logic, but it is a good idea to understand why these questions are being asked. It helps offer a little insight into the interviewer's mindset.

### **False negatives are acceptable.**

This is sad (and frustrating for candidates), but true.

From the company's perspective, it's actually acceptable that some good candidates are rejected. The company is out to build a great set of employees. They can accept that they miss out on some good people. They'd prefer not to, of course, as it raises their recruiting costs. It is an acceptable tradeoff, though, provided they can still hire enough good people.

They're far more concerned with false positives: people who do well in an interview but are not in fact very good.

### **Problem-solving skills are valuable.**

If you're able to work through several hard problems (with some help, perhaps), you're probably pretty good at developing optimal algorithms. You're smart.

Smart people tend to do good things, and that's valuable at a company. It's not the only thing that matters, of course, but it is a really good thing.

### **Basic data structure and algorithm knowledge is useful.**

Many interviewers would argue that basic computer science knowledge is, in fact, useful. Understanding trees, graphs, lists, sorting, and other knowledge does come up periodically. When it does, it's really valuable.

Could you learn it as needed? Sure. But it's very difficult to know that you should use a binary search tree if you don't know of its existence. And if you do know of its existence, then you pretty much know the basics.

Other interviewers justify the reliance on data structures and algorithms by arguing that it's a good "proxy." Even if the skills wouldn't be that hard to learn on their own, they say it's reasonably well-correlated with being a good developer. It means that you've either gone through a computer science program (in which case you've learned and retained a reasonably broad set of technical knowledge) or learned this stuff on your own. Either way, it's a good sign.

There's another reason why data structure and algorithm knowledge comes up: because it's hard to ask problem-solving questions that *don't* involve them. It turns out that the vast majority of problem-solving questions involve some of these basics. When enough candidates know these basics, it's easy to get into a pattern of asking questions with them.

## **Whiteboards let you focus on what matters.**

It's absolutely true that you'd struggle with writing perfect code on a whiteboard. Fortunately, your interviewer doesn't expect that. Virtually everyone has some bugs or minor syntactical errors.

The nice thing about a whiteboard is that, in some ways, you can focus on the big picture. You don't have a compiler, so you don't need to make your code compile. You don't need to write the entire class definition and boilerplate code. You get to focus on the interesting, "meaty" parts of the code: the function that the question is really all about.

That's not to say that you should just write pseudocode or that correctness doesn't matter. Most interviewers aren't okay with pseudocode, and fewer errors are better.

Whiteboards also tend to encourage candidates to speak more and explain their thought process. When a candidate is given a computer, their communication drops substantially.

## **But it's not for everyone or every company or every situation.**

The above sections are intended to help you understand the thought process of the company.

My personal thoughts? For the right situation, when done well, it's a reasonable judge of someone's problem-solving skills, in that people who do well tend to be fairly smart.

However, it's often not done very well. You have bad interviewers or people who just ask bad questions.

It's also not appropriate for all companies. Some companies should value someone's prior experience more or need skills with particular technologies. These sorts of questions don't put much weight on that.

It also won't measure someone's work ethic or ability to focus. Then again, almost no interview process can really evaluate this.

This is not a perfect process by any means, but what is? All interview processes have their downsides.

I'll leave you with this: it is what it is, so let's do the best we can with it.

## **► How Questions are Selected**

Candidates frequently ask what the "recent" interview questions are at a specific company. Just asking this question reveals a fundamental misunderstanding of where questions come from.

At the vast majority of companies, there are no lists of what interviewers should ask. Rather, each interviewer selects their own questions.

Since it's somewhat of a "free for all" as far as questions, there's nothing that makes a question a "recent Google interview question" other than the fact that some interviewer who happens to work at Google just so happened to ask that question recently.

The questions asked this year at Google do not really differ from those asked three years ago. In fact, the questions asked at Google generally don't differ from those asked at similar companies (Amazon, Facebook, etc.).

There are some broad differences across companies. Some companies focus on algorithms (often with some system design worked in), and others really like knowledge-based questions. But within a given category of question, there is little that makes it "belong" to one company instead of another. A Google algorithm question is essentially the same as a Facebook algorithm question.

## ► It's All Relative

If there's no grading system, how are you evaluated? How does an interviewer know what to expect of you? Good question. The answer actually makes a lot of sense once you understand it.

Interviewers assess you relative to other candidates on that same question by the same interviewer. It's a relative comparison.

For example, suppose you came up with some cool new brainteaser or math problem. You ask your friend Alex the question, and it takes him 30 minutes to solve it. You ask Bella and she takes 50 minutes. Chris is never able to solve it. Dexter takes 15 minutes, but you had to give him some major hints and he probably would have taken far longer without them. Ellie takes 10—and comes up with an alternate approach you weren't even aware of. Fred takes 35 minutes.

You'll walk away saying, "Wow, Ellie did really well. I'll bet she's pretty good at math." (Of course, she could have just gotten lucky. And maybe Chris got unlucky. You might ask a few more questions just to really make sure that it wasn't good or bad luck.)

Interview questions are much the same way. Your interviewer develops a feel for your performance by comparing you to other people. It's not about the candidates she's interviewing *that week*. It's about all the candidates that she's ever asked this question to.

For this reason, getting a hard question isn't a bad thing. When it's harder for you, it's harder for everyone. It doesn't make it any less likely that you'll do well.

## ► Frequently Asked Questions

### I didn't hear back immediately after my interview. Am I rejected?

No. There are a number of reasons why a company's decision might be delayed. A very simple explanation is that one of your interviewers hasn't provided their feedback yet. Very, very few companies have a policy of not responding to candidates they reject.

If you haven't heard back from a company within 3 - 5 business days after your interview, check in (politely) with your recruiter.

### Can I re-apply to a company after getting rejected?

Almost always, but you typically have to wait a bit (6 months to a 1 year). Your first bad interview usually won't affect you too much when you re-interview. Lots of people get rejected from Google or Microsoft and later get offers from them.



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## Behind the Scenes

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Most companies conduct their interviews in very similar ways. We will offer an overview of how companies interview and what they're looking for. This information should guide your interview preparation and your reactions during and after the interview.

Once you are selected for an interview, you usually go through a screening interview. This is typically conducted over the phone. College candidates who attend top schools may have these interviews in-person.

Don't let the name fool you; the "screening" interview often involves coding and algorithms questions, and the bar can be just as high as it is for in-person interviews. If you're unsure whether or not the interview will be technical, ask your recruiting coordinator what position your interviewer holds (or what the interview might cover). An engineer will usually perform a technical interview.

Many companies have taken advantage of online synchronized document editors, but others will expect you to write code on paper and read it back over the phone. Some interviewers may even give you "homework" to solve after you hang up the phone or just ask you to email them the code you wrote.

You typically do one or two screening interviewers before being brought on-site.

In an on-site interview round, you usually have 3 to 6 in-person interviews. One of these is often over lunch. The lunch interview is usually not technical, and the interviewer may not even submit feedback. This is a good person to discuss your interests with and to ask about the company culture. Your other interviews will be mostly technical and will involve a combination of coding, algorithm, design/architecture, and behavioral/experience questions.

The distribution of questions between the above topics varies between companies and even teams due to company priorities, size, and just pure randomness. Interviewers are often given a good deal of freedom in their interview questions.

After your interview, your interviewers will provide feedback in some form. In some companies, your interviewers meet together to discuss your performance and come to a decision. In other companies, interviewers submit a recommendation to a hiring manager or hiring committee to make a final decision. In some companies, interviewers don't even make the decision; their feedback goes to a hiring committee to make a decision.

Most companies get back after about a week with next steps (offer, rejection, further interviews, or just an update on the process). Some companies respond much sooner (sometimes same day!) and others take much longer.

If you have waited more than a week, you should follow up with your recruiter. If your recruiter does not respond, this does *not* mean that you are rejected (at least not at any major tech company), and almost any

other company). Let me repeat that again: not responding indicates nothing about your status. The intention is that all recruiters should tell candidates once a final decision is made.

Delays can and do happen. Follow up with your recruiter if you expect a delay, but be respectful when you do. Recruiters are just like you. They get busy and forgetful too.

## ► The Microsoft Interview

Microsoft wants smart people. Geeks. People who are passionate about technology. You probably won't be tested on the ins and outs of C++ APIs, but you will be expected to write code on the board.

In a typical interview, you'll show up at Microsoft at some time in the morning and fill out initial paper work. You'll have a short interview with a recruiter who will give you a sample question. Your recruiter is usually there to prep you, not to grill you on technical questions. If you get asked some basic technical questions, it may be because your recruiter wants to ease you into the interview so that you're less nervous when the "real" interview starts.

Be nice to your recruiter. Your recruiter can be your biggest advocate, even pushing to re-interview you if you stumbled on your first interview. They can fight for you to be hired—or not!

During the day, you'll do four or five interviews, often with two different teams. Unlike many companies, where you meet your interviewers in a conference room, you'll meet with your Microsoft interviewers in their office. This is a great time to look around and get a feel for the team culture.

Depending on the team, interviewers may or may not share their feedback on you with the rest of the interview loop.

When you complete your interviews with a team, you might speak with a hiring manager (often called the "as app", short for "as appropriate"). If so, that's a great sign! It likely means that you passed the interviews with a particular team. It's now down to the hiring manager's decision.

You might get a decision that day, or it might be a week. After one week of no word from HR, send a friendly email asking for a status update.

If your recruiter isn't very responsive, it's because she's busy, not because you're being silently rejected.

### Definitely Prepare:

"Why do you want to work for Microsoft?"

In this question, Microsoft wants to see that you're passionate about technology. A great answer might be, "I've been using Microsoft software as long as I can remember, and I'm really impressed at how Microsoft manages to create a product that is universally excellent. For example, I've been using Visual Studio recently to learn game programming, and its APIs are excellent." Note how this shows a passion for technology!

### What's Unique:

You'll only reach the hiring manager if you've done well, so if you do, that's a great sign!

Additionally, Microsoft tends to give teams more individual control, and the product set is diverse. Experiences can vary substantially across Microsoft since different teams look for different things.

### ► The Amazon Interview

Amazon's recruiting process typically begins with a phone screen in which a candidate interviews with a specific team. A small portion of the time, a candidate may have two or more interviews, which can indicate either that one of their interviewers wasn't convinced or that they are being considered for a different team or profile. In more unusual cases, such as when a candidate is local or has recently interviewed for a different position, a candidate may only do one phone screen.

The engineer who interviews you will usually ask you to write simple code via a shared document editor. They will also often ask a broad set of questions to explore what areas of technology you're familiar with.

Next, you fly to Seattle (or whichever office you're interviewing for) for four or five interviews with one or two teams that have selected you based on your resume and phone interviews. You will have to code on a whiteboard, and some interviewers will stress other skills. Interviewers are each assigned a specific area to probe and may seem very different from each other. They cannot see the other feedback until they have submitted their own, and they are discouraged from discussing it until the hiring meeting.

The "bar raiser" interviewer is charged with keeping the interview bar high. They attend special training and will interview candidates outside their group in order to balance out the group itself. If one interview seems significantly harder and different, that's most likely the bar raiser. This person has both significant experience with interviews and veto power in the hiring decision. Remember, though: just because you seem to be struggling more in this interview doesn't mean you're actually doing worse. Your performance is judged relative to other candidates; it's not evaluated on a simple "percent correct" basis.

Once your interviewers have entered their feedback, they will meet to discuss it. They will be the people making the hiring decision.

While Amazon's recruiters are usually excellent at following up with candidates, occasionally there are delays. If you haven't heard from Amazon within a week, we recommend a friendly email.

#### **Definitely Prepare:**

Amazon cares a lot about scale. Make sure you prepare for scalability questions. You don't need a background in distributed systems to answer these questions. See our recommendations in the System Design and Scalability chapter.

Additionally, Amazon tends to ask a lot of questions about object-oriented design. Check out the Object-Oriented Design chapter for sample questions and suggestions.

#### **What's Unique:**

The Bar Raiser is brought in from a different team to keep the bar high. You need to impress both this person and the hiring manager.

Amazon tends to experiment more with its hiring process than other companies do. The process described here is the typical experience, but due to Amazon's experimentation, it's not necessarily universal.

### ► The Google Interview

There are many scary rumors floating around about Google interviews, but they're mostly just that: rumors. The interview is not terribly different from Microsoft's or Amazon's.

A Google engineer performs the first phone screen, so expect tough technical questions. These questions may involve coding, sometimes via a shared document. Candidates are typically held to the same standard and are asked similar questions on phone screens as in on-site interviews.

On your on-site interview, you'll interview with four to six people, one of whom will be a lunch interviewer. Interviewer feedback is kept confidential from the other interviewers, so you can be assured that you enter each interview with blank slate. Your lunch interviewer doesn't submit feedback, so this is a great opportunity to ask honest questions.

Interviewers are typically not given specific focuses, and there is no "structure" or "system" as to what you're asked when. Each interviewer can conduct the interview however she would like.

Written feedback is submitted to a hiring committee (HC) of engineers and managers to make a hire / no-hire recommendation. Feedback is typically broken down into four categories (Analytical Ability, Coding, Experience, and Communication) and you are given an overall score from 1.0 to 4.0. The HC usually does not include any of your interviewers. If it does, it was purely by random chance.

To extend an offer, the HC wants to see at least one interviewer who is an "enthusiastic endorser." In other words, a packet with scores of 3.6, 3.1, 3.1 and 2.6 is better than all 3.1s.

You do not necessarily need to excel in every interview, and your phone screen performance is usually not a strong factor in the final decision.

If the hiring committee recommends an offer, your packet will go to a compensation committee and then to the executive management committee. Returning a decision can take several weeks because there are so many stages and committees.

#### **Definitely Prepare:**

As a web-based company, Google cares about how to design a scalable system. So, make sure you prepare for questions from System Design and Scalability.

Google puts a strong focus on analytical (algorithm) skills, regardless of experience. You should be very well prepared for these questions, even if you think your prior experience should count for more.

#### **What's Different:**

Your interviewers do not make the hiring decision. Rather, they enter feedback which is passed to a hiring committee. The hiring committee recommends a decision which can be—though rarely is—rejected by Google executives.

### **► The Apple Interview**

Much like the company itself, Apple's interview process has minimal bureaucracy. The interviewers will be looking for excellent technical skills, but a passion for the position and the company is also very important. While it's not a prerequisite to be a Mac user, you should at least be familiar with the system.

The interview process usually begins with a recruiter phone screen to get a basic sense of your skills, followed up by a series of technical phone screens with team members.

Once you're invited on campus, you'll typically be greeted by the recruiter who provides an overview of the process. You will then have 6-8 interviews with members of the team with which you're interviewing, as well as key people with whom your team works.

You can expect a mix of one-on-one and two-on-one interviews. Be ready to code on a whiteboard and make sure all of your thoughts are clearly communicated. Lunch is with your potential future manager and appears more casual, but it is still an interview. Each interviewer usually focuses on a different area and is discouraged from sharing feedback with other interviewers unless there's something they want subsequent interviewers to drill into.

Towards the end of the day, your interviewers will compare notes. If everyone still feels you're a viable candidate, you will have an interview with the director and the VP of the organization to which you're applying. While this decision is rather informal, it's a very good sign if you make it. This decision also happens behind the scenes, and if you don't pass, you'll simply be escorted out of the building without ever having been the wiser (until now).

If you made it to the director and VP interviews, all of your interviewers will gather in a conference room to give an official thumbs up or thumbs down. The VP typically won't be present but can still veto the hire if they weren't impressed. Your recruiter will usually follow up a few days later, but feel free to ping him or her for updates.

### **Definitely Prepare:**

If you know what team you're interviewing with, make sure you read up on that product. What do you like about it? What would you improve? Offering specific recommendations can show your passion for the job.

### **What's Unique:**

Apple does two-on-one interviews often, but don't get stressed out about them—it's the same as a one-on-one interview!

Also, Apple employees are huge Apple fans. You should show this same passion in your interview.

## ► The Facebook Interview

Once selected for an interview, candidates will generally do one or two phone screens. Phone screens will be technical and will involve coding, usually an online document editor.

After the phone interview(s), you might be asked to do a homework assignment that will include a mix of coding and algorithms. Pay attention to your coding style here. If you've never worked in an environment which had thorough code reviews, it may be a good idea to get someone who has to review your code.

During your on-site interview, you will interview primarily with other software engineers, but hiring managers are also involved whenever they are available. All interviewers have gone through comprehensive interview training, and who you interview with has no bearing on your odds of getting an offer.

Each interviewer is given a "role" during the on-site interviews, which helps ensure that there are no repetitive questions and that they get a holistic picture of a candidate. These roles are:

- **Behavioral ("Jedi"):** This interview assesses your ability to be successful in Facebook's environment. Would you fit well with the culture and values? What are you excited about? How do you tackle challenges? Be prepared to talk about your interest in Facebook as well. Facebook wants passionate people. You might also be asked some coding questions in this interview.
- **Coding and Algorithms ("Ninja"):** These are your standard coding and algorithms questions, much like what you'll find in this book. These questions are designed to be challenging. You can use any programming language you want.

- Design/Architecture ("Pirate"): For a backend software engineer, you might be asked system design questions. Front-end or other specialties will be asked design questions related to that discipline. You should openly discuss different solutions and their tradeoffs.

You can typically expect two "ninja" interviews and one "jedi" interview. Experienced candidates will also usually get a "pirate" interview.

After your interview, interviewers submit written feedback, prior to discussing your performance with each other. This ensures that your performance in one interview will not bias another interviewer's feedback.

Once everyone's feedback is submitted, your interviewing team and a hiring manager get together to collaborate on a final decision. They come to a consensus decision and submit a final hire recommendation to the hiring committee.

#### **Definitely Prepare:**

The youngest of the "elite" tech companies, Facebook wants developers with an entrepreneurial spirit. In your interviews, you should show that you love to build stuff fast.

They want to know you can hack together an elegant and scalable solution using any language of choice. Knowing PHP is not especially important, particularly given that Facebook also does a lot of backend work in C++, Python, Erlang, and other languages.

#### **What's Unique:**

Facebook interviews developers for the company "in general," not for a specific team. If you are hired, you will go through a six-week "bootcamp" which will help ramp you up in the massive code base. You'll get mentorship from senior devs, learn best practices, and, ultimately, get a greater flexibility in choosing a project than if you were assigned to a project in your interview.

### **► The Palantir Interview**

Unlike some companies which do "pooled" interviews (where you interview with the company as a whole, not with a specific team), Palantir interviews for a specific team. Occasionally, your application might be re-routed to another team where there is a better fit.

The Palantir interview process typically starts with two phone interviews. These interviews are about 30 to 45 minutes and will be primarily technical. Expect to cover a bit about your prior experience, with a heavy focus on algorithm questions.

You might also be sent a HackerRank coding assessment, which will evaluate your ability to write optimal algorithms and correct code. Less experienced candidates, such as those in college, are particularly likely to get such a test.

After this, successful candidates are invited to campus and will interview with up to five people. Onsite interviews cover your prior experience, relevant domain knowledge, data structures and algorithms, and design.

You may also likely get a demo of Palantir's products. Ask good questions and demonstrate your passion for the company.

After the interview, the interviewers meet to discuss your feedback with the hiring manager.

### Definitely Prepare:

Palantir values hiring brilliant engineers. Many candidates report that Palantir's questions were harder than those they saw at Google and other top companies. This doesn't necessarily mean it's harder to get an offer (although it certainly can); it just means interviewers prefer more challenging questions. If you're interviewing with Palantir, you should learn your core data structures and algorithms inside and out. Then, focus on preparing with the hardest algorithm questions.

Brush up on system design too if you're interviewing for a backend role. This is an important part of the process.

### What's Unique:

A coding challenge is a common part of Palantir's process. Although you'll be at your computer and can look up material as needed, don't walk into this unprepared. The questions can be extremely challenging and the efficiency of your algorithm will be evaluated. Thorough interview preparation will help you here. You can also practice coding challenges online at [HackerRank.com](https://www.hackerrank.com).



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## Special Situations

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There are many paths that lead someone to this book. Perhaps you have more experience but have never done this sort of interview. Perhaps you're a tester or a PM. Or perhaps you're actually using this book to teach yourself how to interview better. Here's a little something for all these "special situations."

### ► Experienced Candidates

Some people assume that the algorithm-style questions you see in this book are only for recent grads. That's not entirely true.

More experienced engineers might see slightly less focus on algorithm questions—but only slightly.

If a company asks algorithm questions to inexperienced candidates, they tend to ask them to experienced candidates too. Rightly or wrongly, they feel that the skills demonstrated in these questions are important for all developers.

Some interviewers might hold experience candidates to a somewhat lower standard. After all, it's been years since these candidates took an algorithms class. They're out of practice.

Others though hold experienced candidates to a higher standard, reasoning that the more years of experience allow a candidate to have seen many more types of problems.

On average, it balances out.

The exception to this rule is system design and architecture questions, as well as questions about your resume. Typically, students don't study much system architecture, so experience with such challenges would only come professionally. Your performance in such interview questions would be evaluated with respect to your experience level. However, students and recent graduates are still asked these questions and should be prepared to solve them as well as they can.

Additionally, experienced candidates will be expected to give a more in-depth, impressive response to questions like, "What was the hardest bug you've faced?" You have more experience, and your response to these questions should show it.

### ► Testers and SDETs

SDETs (software design engineers in test) write code, but to test features instead of build features. As such, they have to be great coders and great testers. Double the prep work!

If you're applying for an SDET role, take the following approach:

- *Prepare the Core Testing Problems:* For example, how would you test a light bulb? A pen? A cash register? Microsoft Word? The Testing chapter will give you more background on these problems.
- *Practice the Coding Questions:* The number one thing that SDETs get rejected for is coding skills. Although coding standards are typically lower for an SDET than for a traditional developer, SDETs are still expected to be very strong in coding and algorithms. Make sure that you practice solving all the same coding and algorithm questions that a regular developer would get.
- *Practice Testing the Coding Questions:* A very popular format for SDET questions is “Write code to do X,” followed up by, “Okay, now test it.” Even when the question doesn’t specifically require this, you should ask yourself, “How would I test this?” Remember: any problem can be an SDET problem!

Strong communication skills can also be very important for testers, since your job requires you to work with so many different people. Do not neglect the Behavioral Questions section.

#### Career Advice

Finally, a word of career advice: If, like many candidates, you are hoping to apply to an SDET position as the “easy” way into a company, be aware that many candidates find it very difficult to move from an SDET position to a dev position. Make sure to keep your coding and algorithms skills very sharp if you hope to make this move, and try to switch within one to two years. Otherwise, you might find it very difficult to be taken seriously in a dev interview.

Never let your coding skills atrophy.

## ► Product (and Program) Management

These “PM” roles vary wildly across companies and even within a company. At Microsoft, for instance, some PMs may be essentially customer evangelists, working in a customer-facing role that borders on marketing. Across campus though, other PMs may spend much of their day coding. The latter type of PMs would likely be tested on coding, since this is an important part of their job function.

Generally speaking, interviewers for PM positions are looking for candidates to demonstrate skills in the following areas:

- *Handling Ambiguity:* This is typically not the most critical area for an interview, but you should be aware that interviewers do look for skill here. Interviewers want to see that, when faced with an ambiguous situation, you don’t get overwhelmed and stall. They want to see you tackle the problem head on: seeking new information, prioritizing the most important parts, and solving the problem in a structured way. This typically will not be tested directly (though it can be), but it may be one of many things the interviewer is looking for in a problem.
- *Customer Focus (Attitude):* Interviewers want to see that your attitude is customer-focused. Do you assume that everyone will use the product just like you do? Or are you the type of person who puts himself in the customer’s shoes and tries to understand how they want to use the product? Questions like “Design an alarm clock for the blind” are ripe for examining this aspect. When you hear a question like this, be sure to ask a lot of questions to understand *who* the customer is and *how* they are using the product. The skills covered in the Testing section are closely related to this.
- *Customer Focus (Technical Skills):* Some teams with more complex products need to ensure that their PMs walk in with a strong understanding of the product, as it would be difficult to acquire this knowledge on the job. Deep technical knowledge of mobile phones is probably not necessary to work on the Android or Windows Phone teams (although it might still be nice to have), whereas an understanding of security might be necessary to work on Windows Security. Hopefully, you wouldn’t interview with a team that

required specific technical skills unless you at least claim to possess the requisite skills.

- *Multi-Level Communication:* PMs need to be able to communicate with people at all levels in the company, across many positions and ranges of technical skills. Your interviewer will want to see that you possess this flexibility in your communication. This is often examined directly, through a question such as, "Explain TCP/IP to your grandmother." Your communication skills may also be assessed by how you discuss your prior projects.
- *Passion for Technology:* Happy employees are productive employees, so a company wants to make sure that you'll enjoy the job and be excited about your work. A passion for technology—and, ideally, the company or team—should come across in your answers. You may be asked a question directly like, "Why are you interested in Microsoft?" Additionally, your interviewers will look for enthusiasm in how you discuss your prior experience and how you discuss the team's challenges. They want to see that you will be eager to face the job's challenges.
- *Teamwork / Leadership:* This may be the most important aspect of the interview, and—not surprisingly—the job itself. All interviewers will be looking for your ability to work well with other people. Most commonly, this is assessed with questions like, "Tell me about a time when a teammate wasn't pulling his / her own weight." Your interviewer is looking to see that you handle conflicts well, that you take initiative, that you understand people, and that people like working with you. Your work preparing for behavioral questions will be extremely important here.

All of the above areas are important skills for PMs to master and are therefore key focus areas of the interview. The weighting of each of these areas will roughly match the importance that the area holds in the actual job.

## ► Dev Lead and Managers

Strong coding skills are almost always required for dev lead positions and often for management positions as well. If you'll be coding on the job, make sure to be very strong with coding and algorithms—just like a dev would be. Google, in particular, holds managers to high standards when it comes to coding.

In addition, prepare to be examined for skills in the following areas:

- *Teamwork / Leadership:* Anyone in a management-like role needs to be able to both lead and work with people. You will be examined implicitly and explicitly in these areas. Explicit evaluation will come in the form of asking you how you handled prior situations, such as when you disagreed with a manager. The implicit evaluation comes in the form of your interviewers watching how you interact with them. If you come off as too arrogant or too passive, your interviewer may feel you aren't great as a manager.
- *Prioritization:* Managers are often faced with tricky issues, such as how to make sure a team meets a tough deadline. Your interviewers will want to see that you can prioritize a project appropriately, cutting the less important aspects. Prioritization means asking the right questions to understand what is critical and what you can reasonably expect to accomplish.
- *Communication:* Managers need to communicate with people both above and below them, and potentially with customers and other much less technical people. Interviewers will look to see that you can communicate at many levels and that you can do so in a way that is friendly and engaging. This is, in some ways, an evaluation of your personality.
- *"Getting Things Done":* Perhaps the most important thing that a manager can do is be a person who "gets things done." This means striking the right balance between preparing for a project and actually implementing it. You need to understand how to structure a project and how to motivate people so you can accomplish the team's goals.

Ultimately, most of these areas come back to your prior experience and your personality. Be sure to prepare very, very thoroughly using the interview preparation grid.

#### ► Startups

The application and interview process for startups is highly variable. We can't go through every startup, but we can offer some general pointers. Understand, however, that the process at a specific startup might deviate from this.

#### The Application Process

Many startups might post job listings, but for the hottest startups, often the best way in is through a personal referral. This reference doesn't necessarily need to be a close friend or a coworker. Often just by reaching out and expressing your interest, you can get someone to pick up your resume to see if you're a good fit.

#### Visas and Work Authorization

Unfortunately, many smaller startups in the U.S. are not able to sponsor work visas. They hate the system as much you do, but you won't be able to convince them to hire you anyway. If you require a visa and wish to work at a startup, your best bet is to reach out to a professional recruiter who works with many startups (and may have a better idea of which startups will work with visa issues), or to focus your search on bigger startups.

#### Resume Selection Factors

Startups tend to want engineers who are not only smart and who can code, but also people who would work well in an entrepreneurial environment. Your resume should ideally show initiative. What sort of projects have you started?

Being able to "hit the ground running" is also very important; they want people who already know the language of the company.

#### The Interview Process

In contrast to big companies, which tend to look mostly at your general aptitude with respect to software development, startups often look closely at your personality fit, skill set, and prior experience.

- *Personality Fit:* Personality fit is typically assessed by how you interact with your interviewer. Establishing a friendly, engaging conversation with your interviewers is your ticket to many job offers.
- *Skill Set:* Because startups need people who can hit the ground running, they are likely to assess your skills with specific programming languages. If you know a language that the startup works with, make sure to brush up on the details.
- *Experience:* Startups are likely to ask you a lot of questions about your experience. Pay special attention to the Behavioral Questions section.

In addition to the above areas, the coding and algorithms questions that you see in this book are also very common.

## ► Acquisitions and Acquihires

During the technical due diligence process for many acquisitions, the acquirer will often interview most or all of a startup's employees. Google, Yahoo, Facebook, and many other companies have this as a standard part of many acquisitions.

### Which startups go through this? And why?

Part of the reasoning for this is that their employees had to go through this process to get hired. They don't want acquisitions to be an "easy way" into the company. And, since the team is a core motivator for the acquisition, they figure it makes sense to assess the skills of the team.

Not all acquisitions are like this, of course. The famous multi-billion dollar acquisitions generally did not have to go through this process. Those acquisitions, after all, are usually about the user base and community, less so about the employees or even the technology. Assessing the team's skills is less essential.

However, it is not as simple as "acquihiires get interviewed, traditional acquisitions do not." There is a big gray area between acquihiires (i.e., talent acquisitions) and product acquisitions. Many startups are acquired for the team and ideas behind the technology. The acquirer might discontinue the product, but have the team work on something very similar.

If your startup is going through this process, you can typically expect your team to have interviews very similar to what a normal candidate would experience (and, therefore, very similar to what you'll see in this book).

### How important are these interviews?

These interviews can carry enormous importance. They have three different roles:

- They can make or break acquisitions. They are often the reason a company does not get acquired.
- They determine which employees receive offers to join the acquirer.
- They can affect the acquisition price (in part as a consequence of the number of employees who join).

These interviews are much more than a mere "screen."

### Which employees go through the interviews?

For tech startups, usually all of the engineers go through the interview process, as they are one of the core motivators for the acquisition.

In addition, sales, customer support, product managers, and essentially any other role might have to go through it.

The CEO is often slotted into a product manager interview or a dev manager interview, as this is often the closest match for the CEO's current responsibilities. This is not an absolute rule, though. It depends on what the CEO's role presently is and what the CEO is interested in. With some of my clients, the CEO has even opted to not interview and to leave the company upon the acquisition.

### What happens to employees who don't perform well in the interview?

Employees who underperform will often not receive offers to join the acquirer. (If many employees don't perform well, then the acquisition will likely not go through.)

In some cases, employees who performed poorly in interviews will get contract positions for the purpose of “knowledge transfer.” These are temporary positions with the expectation that the employee leaves at the termination of the contract (often six months), although sometimes the employee ends up being retained.

In other cases, the poor performance was a result of the employee being mis-slotted. This occurs in two common situations:

- Sometimes a startup labels someone who is not a “traditional” software engineer as a software engineer. This often happens with data scientists or database engineers. These people may underperform during the software engineer interviews, as their actual role involves other skills.
- In other cases, a CEO “sells” a junior software engineer as more senior than he actually is. He underperforms for the senior bar because he’s being held to an unfairly high standard.

In either case, sometimes the employee will be re-interviewed for a more appropriate position. (Other times though, the employee is just out of luck.)

In rare cases, a CEO is able to override the decision for a particularly strong employee whose interview performance didn’t reflect this.

#### **Your “best” (and worst) employees might surprise you.**

The problem-solving/algorithm interviews conducted at the top tech companies evaluate particular skills, which might not perfectly match what their manager evaluates in their employees.

I’ve worked with many companies that are surprised at who their strongest and weakest performers are in interviews. That junior engineer who still has a lot to learn about professional development might turn out to be a great problem-solver in these interviews.

Don’t count anyone out—or in—until you’ve evaluated them the same way their interviewers will.

#### **Are employees held to the same standards as typical candidates?**

Essentially yes, although there is a bit more leeway.

The big companies tend to take a risk-averse approach to hiring. If someone is on the fence, they often lean towards a no-hire.

In the case of an acquisition, the “on the fence” employees can be pulled through by strong performance from the rest of the team.

#### **How do employees tend to react to the news of an acquisition/acquisition?**

This is a big concern for many startup CEOs and founders. Will the employees be upset about this process? Or, what if we get their hopes up but it doesn’t happen?

What I’ve seen with my clients is that the leadership is worried about this more than is necessary.

Certainly, some employees are upset about the process. They might not be excited about joining one of the big companies for any number of reasons.

Most employees, though, are cautiously optimistic about the process. They hope it goes through, but they know that the existence of these interviews means that it might not.

### What happens to the team after an acquisition?

Every situation is different. However, most of my clients have been kept together as a team, or possibly integrated into an existing team.

### How should you prepare your team for acquisition interviews?

Interview prep for acquisition interviews is fairly similar to typical interviews at the acquirer. The difference is that your company is doing this as a team and that each employee wasn't individually selected for the interview on their own merits.

*You're all in this together.*

Some startups I've worked with put their "real" work on hold and have their teams spend the next two or three weeks on interview prep.

Obviously, that's not a choice all companies can make, but—from the perspective of wanting the acquisition to go through—that does increase your results substantially.

Your team should study individually, in teams of two or three, or by doing mock interviews with each other. If possible, use all three of these approaches.

*Some people may be less prepared than others.*

Many developers at startups might have only vaguely heard of big O time, binary search tree, breadth-first search, and other important concepts. They'll need some extra time to prepare.

People without computer science degrees (or who earned their degrees a long time ago) should focus first on learning the core concepts discussed in this book, especially big O time (which is one of the most important). A good first exercise is to implement all the core data structures and algorithms from scratch.

If the acquisition is important to your company, give these people the time they need to prepare. They'll need it.

*Don't wait until the last minute.*

As a startup, you might be used to taking things as they come without a ton of planning. Startups that do this with acquisition interviews tend not to fare well.

Acquisition interviews often come up very suddenly. A company's CEO is chatting with an acquirer (or several acquirers) and conversations get increasingly serious. The acquirer mentions the possibility of interviews at some point in the future. Then, all of a sudden, there's a "come in at the end of this week" message.

If you wait until there's a firm date set for the interviews, you probably won't get much more than a couple of days to prepare. That might not be enough time for your engineers to learn core computer science concepts and practice interview questions.

## ► For Interviewers

Since writing the last edition, I've learned that a lot of interviewers are using *Cracking the Coding Interview* to learn how to interview. That wasn't really the book's intention, but I might as well offer some guidance for interviews.

#### **Don't actually ask the exact questions in here.**

First, these questions were selected because they're good for interview preparation. Some questions that are good for interview preparation are not always good for interviewing. For example, there are some brainteasers in this book because sometimes interviewers ask these sorts of questions. It's worthwhile for candidates to practice those if they're interviewing at a company that likes them, even though I personally find them to be bad questions.

Second, your candidates are reading this book, too. You don't want to ask questions that your candidates have already solved.

You can ask questions *similar* to these, but don't just pluck questions out of here. Your goal is to test their problem-solving skills, not their memorization skills.

#### **Ask Medium and Hard Problems**

The goal of these questions is to evaluate someone's problem-solving skills. When you ask questions that are too easy, performance gets clustered together. Minor issues can substantially drop someone's performance. It's not a reliable indicator.

#### **Look for questions with multiple hurdles.**

Some questions have "Aha!" moments. They rest on a particular insight. If the candidate doesn't get that one bit, then they do poorly. If they get it, then suddenly they've outperformed many candidates.

Even if that insight is an indicator of skills, it's still only one indicator. Ideally, you want a question that has a series of hurdles, insights, or optimizations. Multiple data points beat a single data point.

Here's a test: if you can give a hint or piece of guidance that makes a substantial difference in a candidate's performance, then it's probably not a good interview question.

#### **Use hard questions, not hard knowledge.**

Some interviewers, in an attempt to make a question hard, inadvertently make the *knowledge* hard. Sure enough, fewer candidates do well so the statistics look right, but it's not for reasons that indicate much about the candidates' skills.

The knowledge you are expecting candidates to have should be fairly straightforward data structure and algorithm knowledge. It's reasonable to expect a computer science graduate to understand the basics of big O and trees. Most won't remember Dijkstra's algorithm or the specifics of how AVL trees works.

If your interview question expects obscure knowledge, ask yourself: is this truly an important skill? Is it so important that I would like to either reduce the number of candidates I hire or reduce the amount to which I focus on problem-solving or other skills?

Every new skill or attribute you evaluate shrinks the number of offers extended, unless you counter-balance this by relaxing the requirements for a different skill. Sure, all else being equal, you might prefer someone who could recite the finer points of a two-inch thick algorithms textbook. But all else isn't equal.

#### **Avoid "scary" questions.**

Some questions intimidate candidates because it seems like they involve some specialized knowledge, even if they really don't. This often includes questions that involve:

- Math or probability.

- Low-level knowledge (memory allocation, etc.).
- System design or scalability.
- Proprietary systems (Google Maps, etc.).

For example, one question I sometimes ask is to find all positive integer solutions under 1,000 to  $a^3 + b^3 = c^3 + d^3$  (page 68).

Many candidates will at first think they have to do some sort of fancy factorization of this or semi-advanced math. They don't. They need to understand the concept of exponents, sums, and equality, and that's it.

When I ask this question, I explicitly say, "I know this sounds like a math problem. Don't worry. It's not. It's an algorithm question." If they start going down the path of factorization, I stop them and remind them that it's not a math question.

Other questions might involve a bit of probability. It might be stuff that a candidate would surely know (e.g., to pick between five options, pick a random number between 1 and 5). But simply the fact that it involves probability will intimidate candidates.

Be careful asking questions that sound intimidating. Remember that this is already a really intimidating situation for candidates. Adding on a "scary" question might just fluster a candidate and cause him to underperform.

If you're going to ask a question that sounds "scary," make sure you really reassure candidates that it doesn't require the knowledge that they think it does.

### **Offer positive reinforcement.**

Some interviewers put so much focus on the "right" question that they forget to think about their own behavior.

Many candidates are intimidated by interviewing and try to read into the interviewer's every word. They can cling to each thing that might possibly sound positive or negative. They interpret that little comment of "good luck" to mean something, even though you say it to everyone regardless of performance.

You want candidates to feel good about the experience, about you, and about their performance. You want them to feel comfortable. A candidate who is nervous will perform poorly, and it doesn't mean that they aren't good. Moreover, a good candidate who has a negative reaction to you or to the company is less likely to accept an offer—and they might dissuade their friends from interviewing/accepting as well.

Try to be warm and friendly to candidates. This is easier for some people than others, but do your best.

Even if being warm and friendly doesn't come naturally to you, you can still make a concerted effort to sprinkle in positive remarks throughout the interview:

- "Right, exactly."
- "Great point."
- "Good work."
- "Okay, that's a really interesting approach."
- "Perfect."

No matter how poorly a candidate is doing, there is always something they got right. Find a way to infuse some positivity into the interview.

#### Probe deeper on behavioral questions.

Many candidates are poor at articulating their specific accomplishments.

You ask them a question about a challenging situation, and they tell you about a difficult situation their team faced. As far as you can tell, the candidate didn't really do much.

Not so fast, though. A candidate might not focus on themselves because they've been trained to celebrate their team's accomplishments and not boast about themselves. This is especially common for people in leadership roles and female candidates.

Don't assume that a candidate didn't do much in a situation just because you have trouble understanding what they did. Call out the situation (nicely!). Ask them specifically if they can tell you what their role was.

If it didn't really sound like resolving the situation was difficult, then, again, probe deeper. Ask them to go into more details about how they thought about the issue and the different steps they took. Ask them why they took certain actions. Not describing the details of the actions they took makes them a flawed *candidate*, but not necessarily a flawed employee.

Being a good interview candidate is its own skill (after all, that's part of why this book exists), and it's probably not one you want to evaluate.

#### Coach your candidates.

Read through the sections on how candidates can develop good algorithms. Many of these tips are ones you can offer to candidates who are struggling. You're not "teaching to the test" when you do this; you're separating interview skills from job skills.

- Many candidates don't use an example to solve an interview question (or they don't use a *good* example). This makes it substantially more difficult to develop a solution, but it doesn't necessarily mean that they're not very good problem solvers. If candidates don't write an example themselves, or if they inadvertently write a special case, guide them.
- Some candidates take a long time to find the bug because they use an enormous example. This doesn't make them a bad tester or developer. It just means that they didn't realize that it would be more efficient to analyze their code conceptually first, or that a small example would work nearly as well. Guide them.
- If they dive into code before they have an optimal solution, pull them back and focus them on the algorithm (if that's what you want to see). It's unfair to say that a candidate never found or implemented the optimal solution if they didn't really have the time to do so.
- If they get nervous and stuck and aren't sure where to go, suggest to them that they walk through the brute force solution and look for areas to optimize.
- If they haven't said anything and there is a fairly obvious brute force, remind them that they can start off with a brute force. Their first solution doesn't have to be perfect.

Even if you think that a candidate's ability in one of these areas is an important factor, it's not the only factor. You can always mark someone down for "failing" this hurdle while helping to guide them past it.

While this book is here to coach candidates through interviews, one of your goals as an interviewer is to remove the effect of not preparing. After all, some candidates have studied for interviews and some candidates haven't, and this probably doesn't reveal much about their skills as an engineer.

Guide candidates using the tips in this book (within reason, of course—you don't want to coach candidates through the problems so much that you're not evaluating their problem-solving skills anymore).

Be careful here, though. If you're someone who comes off as intimidating to candidates, this coaching could make things worse. It can come off as your telling candidates that they're constantly messing up by creating bad examples, not prioritizing testing the right way, and so on.

### If they want silence, give them silence.

One of the most common questions that candidates ask me is how to deal with an interviewer who insists on talking when they just need a moment to think in silence.

If your candidate needs this, give your candidate this time to think. Learn to distinguish between "I'm stuck and have no idea what to do," and "I'm thinking in silence."

It might help you to guide your candidate, and it might help many candidates, but it doesn't necessarily help *all* candidates. Some need a moment to think. Give them that time, and take into account when you're evaluating them that they got a bit less guidance than others.

### Know your mode: sanity check, quality, specialist, and proxy.

At a very, very high level, there are four modes of questions:

- **Sanity Check:** These are often easy problem-solving or design questions. They assess a minimum degree of competence in problem-solving. They won't tell distinguish between "okay" versus "great", so don't evaluate them as such. You can use them early in the process (to filter out the worst candidates), or when you only need a minimum degree of competency.
- **Quality Check:** These are the more challenging questions, often in problem-solving or design. They are designed to be rigorous and really make a candidate think. Use these when algorithmic/problem-solving skills are of high importance. The biggest mistake people make here is asking questions that are, in fact, bad problem-solving questions.
- **Specialist Questions:** These questions test knowledge of specific topics, such as Java or machine learning. They should be used when for skills a good engineer couldn't quickly learn on the job. These questions need to be appropriate for true specialists. Unfortunately, I've seen situations where a company asks a candidate who just completed a 10-week coding bootcamp detailed questions about Java. What does this show? If she has this knowledge, then she only learned it recently and, therefore, it's likely to be easily acquirable. If it's easily acquirable, then there's no reason to hire for it.
- **Proxy Knowledge:** This is knowledge that is not quite at the specialist level (in fact, you might not even need it), but that you would expect a candidate at their level to know. For example, it might not be very important to you if a candidate knows CSS or HTML. But if a candidate has worked in depth with these technologies and can't talk about why tables are or aren't good, that suggests an issue. They're not absorbing information core to their job.

When companies get into trouble is when they mix and match these:

- They ask specialist questions to people who aren't specialists.
- They hire for specialist roles when they don't need specialists.
- They need specialists but are only assessing pretty basic skills.
- They are asking sanity check (easy) questions, but think they're asking quality check questions. They therefore interpret a strong difference between "okay" and "great" performance, even though a very minor detail might have separated these.

In fact, having worked with a number of small and large tech companies on their hiring process, I have found that most companies are doing one of these things wrong.

# IV

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## Before the Interview

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Acing an interview starts well before the interview itself—years before, in fact. The following timeline outlines what you should be thinking about when.

If you’re starting late into this process, don’t worry. Do as much “catching up” as you can, and then focus on preparation. Good luck!

### ► Getting the Right Experience

Without a great resume, there’s no interview. And without great experience, there’s no great resume. Therefore, the first step in landing an interview is getting great experience. The further in advance you can think about this the better.

For current students, this may mean the following:

- *Take the Big Project Classes:* Seek out the classes with big coding projects. This is a great way to get somewhat practical experience before you have any formal work experience. The more relevant the project is to the real world, the better.
- *Get an Internship:* Do everything you can to land an internship early in school. It will pave the way for even better internships before you graduate. Many of the top tech companies have internship programs designed especially for freshman and sophomores. You can also look at startups, which might be more flexible.
- *Start Something:* Build a project on your own time, participate in hackathons, or contribute to an open source project. It doesn’t matter too much what it is. The important thing is that you’re coding. Not only will this develop your technical skills and practical experience, your initiative will impress companies.

Professionals, on the other hand, may already have the right experience to switch to their dream company. For instance, a Google dev probably already has sufficient experience to switch to Facebook. However, if you’re trying to move from a lesser-known company to one of the “biggies,” or from testing/IT into a dev role, the following advice will be useful:

- *Shift Work Responsibilities More Towards Coding:* Without revealing to your manager that you are thinking of leaving, you can discuss your eagerness to take on bigger coding challenges. As much as possible, try to ensure that these projects are “meaty,” use relevant technologies, and lend themselves well to a resume bullet or two. It is these coding projects that will, ideally, form the bulk of your resume.
- *Use Your Nights and Weekends:* If you have some free time, use it to build a mobile app, a web app, or a piece of desktop software. Doing such projects is also a great way to get experience with new technologies, making you more relevant to today’s companies. This project work should definitely be listed on your resume; few things are as impressive to an interviewer as a candidate who built something “just

for fun."

All of these boil down to the two big things that companies want to see: that you're smart and that you can code. If you can prove that, you can land your interview.

In addition, you should think in advance about where you want your career to go. If you want to move into management down the road, even though you're currently looking for a dev position, you should find ways now of developing leadership experience.

## ► Writing a Great Resume

Resume screeners look for the same things that interviewers do. They want to know that you're smart and that you can code.

That means you should prepare your resume to highlight those two things. Your love of tennis, traveling, or magic cards won't do much to show that. Think twice before cutting more technical lines in order to allow space for your non-technical hobbies.

### Appropriate Resume Length

In the US, it is strongly advised to keep a resume to one page if you have less than ten years of experience. More experienced candidates can often justify 1.5 - 2 pages otherwise.

Think twice about a long resume. Shorter resumes are often more impressive.

- Recruiters only spend a fixed amount of time (about 10 seconds) looking at your resume. If you limit the content to the most impressive items, the recruiter is sure to see them. Adding additional items just distracts the recruiter from what you'd really like them to see.
- Some people just flat-out refuse to read long resumes. Do you really want to risk having your resume tossed for this reason?

If you are thinking right now that you have too much experience and can't fit it all on one or two pages, trust me, *you can*. Long resumes are not a reflection of having tons of experience; they're a reflection of not understanding how to prioritize content.

### Employment History

Your resume does not—and should not—include a full history of every role you've ever had. Include only the relevant positions—the ones that make you a more impressive candidate.

#### *Writing Strong Bullets*

For each role, try to discuss your accomplishments with the following approach: "Accomplished X by implementing Y which led to Z." Here's an example:

- "Reduced object rendering time by 75% by implementing distributed caching, leading to a 10% reduction in log-in time."

Here's another example with an alternate wording:

- "Increased average match accuracy from 1.2 to 1.5 by implementing a new comparison algorithm based on windiff."

Not everything you did will fit into this approach, but the principle is the same: show what you did, how you did it, and what the results were. Ideally, you should try to make the results "measurable" somehow.

### Projects

Developing the projects section on your resume is often the best way to present yourself as more experienced. This is especially true for college students or recent grads.

The projects should include your 2 - 4 most significant projects. State what the project was and which languages or technologies it employed. You may also want to consider including details such as whether the project was an individual or a team project, and whether it was completed for a course or independently. These details are not required, so only include them if they make you look better. Independent projects are generally preferred over course projects, as it shows initiative.

Do not add too many projects. Many candidates make the mistake of adding all 13 of their prior projects, cluttering their resume with small, non-impressive projects.

So what should you build? Honestly, it doesn't matter that much. Some employers really like open source projects (it offers experience contributing to a large code base), while others prefer independent projects (it's easier to understand your personal contributions). You could build a mobile app, a web app, or almost anything. The most important thing is that you're building something.

### Programming Languages and Software

#### *Software*

Be conservative about what software you list, and understand what's appropriate for the company. Software like Microsoft Office can almost always be cut. Technical software like Visual Studio and Eclipse is somewhat more relevant, but many of the top tech companies won't even care about that. After all, is it really that hard to learn Visual Studio?

Of course, it won't hurt you to list all this software. It just takes up valuable space. You need to evaluate the trade-off of that.

#### *Languages*

Should you list everything you've ever worked with, or shorten the list to just the ones that you're most comfortable with?

Listing everything you've ever worked with is dangerous. Many interviewers consider anything on your resume to be "fair game" as far as the interview.

One alternative is to list most of the languages you've used, but add your experience level. This approach is shown below:

- Languages: Java (expert), C++ (proficient), JavaScript (prior experience).

Use whatever wording ("expert", "fluent", etc.) effectively communicates your skillset.

Some people list the number of years of experience they have with a particular language, but this can be really confusing. If you first learned Java 10 years ago, and have used it occasionally throughout that time, how many years of experience is this?

For this reason, the number of years of experience is a poor metric for resumes. It's better to just describe what you mean in plain English.

### Advice for Non-Native English Speakers and Internationals

Some companies will throw out your resume just because of a typo. Please get at least one native English speaker to proofread your resume.

Additionally, for US positions, do *not* include age, marital status, or nationality. This sort of personal information is not appreciated by companies, as it creates a legal liability for them.

### Beware of (Potential) Stigma

Certain languages have stigmas associated with them. Sometimes this is because of the language themselves, but often it's because of the places where this language is used. I'm not defending the stigma; I'm just letting you know of it.

A few stigmas you should be aware of:

- **Enterprise Languages:** Certain languages have a stigma associated with them, and those are often the ones that are used for enterprise development. Visual Basic is a good example of this. If you show yourself to be an expert with VB, it can cause people to assume that you're less skilled. Many of these same people will admit that, yes, VB.NET is actually perfectly capable of building sophisticated applications. But still, the kinds of applications that people tend to build with it are not very sophisticated. You would be unlikely to see a big name Silicon Valley using VB.

In fact, the same argument (although less strong) applies to the whole .NET platform. If your primary focus is .NET and you're not applying for .NET roles, you'll have to do more to show that you're strong technically than if you were coming in with a different background.

- **Being Too Language Focused:** When recruiters at some of the top tech companies see resumes that list every flavor of Java on their resume, they make negative assumptions about the caliber of candidate. There is a belief in many circles that the best software engineers don't define themselves around a particular language. Thus, when they see a candidate seems to flaunt which specific versions of a language they know, recruiters will often bucket the candidate as "not our kind of person."

Note that this does not mean that you should necessarily take this "language flaunting" off your resume. You need to understand what that company values. Some companies do value this.

- **Certifications:** Certifications for software engineers can be anything from a positive, to a neutral, to a negative. This goes hand-in-hand with being too language focused; the companies that are biased against candidates with a very lengthy list of technologies tend to also be biased against certifications. This means that in some cases, you should actually remove this sort of experience from your resume.

- **Knowing Only One or Two Languages:** The more time you've spent coding, the more things you've built, the more languages you will have tended to work with. The assumption then, when they see a resume with only one language, is that you haven't experienced very many problems. They also often worry that candidates with only one or two languages will have trouble learning new technologies (why hasn't the candidate learned more things?) or will just feel too tied with a specific technology (potentially not using the best language for the task).

This advice is here not just to help you work on your resume, but also to help you develop the right experience. If your expertise is in C#.NET, try developing some projects in Python and JavaScript. If you only know one or two languages, build some applications in a different language.

Where possible, try to truly diversify. The languages in the cluster of {Python, Ruby, and JavaScript} are somewhat similar to each other. It's better if you can learn languages that are more different, like Python, C++, and Java.

## ▶ Preparation Map

The following map should give you an idea of how to tackle the interview preparation process. One of the key takeaways here is that it's not just about interview questions. Do projects and write code, too!





# V

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## Behavioral Questions

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Behavioral questions are asked to get to know your personality, to understand your resume more deeply, and just to ease you into an interview. They are important questions and can be prepared for.

### ► Interview Preparation Grid

Go through each of the projects or components of your resume and ensure that you can talk about them in detail. Filling out a grid like this may help:

Common Questions	Project 1	Project 2	Project 3
Challenges			
Mistakes/Failures			
Enjoyed			
Leadership			
Conflicts			
What You'd Do Differently			

Along the top, as columns, you should list all the major aspects of your resume, including each project, job, or activity. Along the side, as rows, you should list the common behavioral questions.

Study this grid before your interview. Reducing each story to just a couple of keywords may make the grid easier to study and recall. You can also more easily have this grid in front of you during an interview without it being a distraction.

In addition, ensure that you have one to three projects that you can talk about in detail. You should be able to discuss the technical components in depth. These should be projects where you played a central role.

### What are your weaknesses?

When asked about your weaknesses, give a real weakness! Answers like "My greatest weakness is that I work too hard" tell your interviewer that you're arrogant and/or won't admit to your faults. A good answer conveys a real, legitimate weakness but emphasizes how you work to overcome it.

For example:

"Sometimes, I don't have a very good attention to detail. While that's good because it lets me execute quickly, it also means that I sometimes make careless mistakes. Because of that, I make sure to always have someone else double check my work."

## What questions should you ask the interviewer?

Most interviewers will give you a chance to ask them questions. The quality of your questions will be a factor, whether subconsciously or consciously, in their decisions. Walk into the interview with some questions in mind.

You can think about three general types of questions.

### *Genuine Questions*

These are the questions you actually want to know the answers to. Here are a few ideas of questions that are valuable to many candidates:

1. "What is the ratio of testers to developers to program managers? What is the interaction like? How does project planning happen on the team?"
2. "What brought you to this company? What has been most challenging for you?"

These questions will give you a good feel for what the day-to-day life is like at the company.

### *Insightful Questions*

These questions demonstrate your knowledge or understanding of technology.

1. "I noticed that you use technology X. How do you handle problem Y?"
2. "Why did the product choose to use the X protocol over the Y protocol? I know it has benefits like A, B, C, but many companies choose not to use it because of issue D."

Asking such questions will typically require advance research about the company.

### *Passion Questions*

These questions are designed to demonstrate your passion for technology. They show that you're interested in learning and will be a strong contributor to the company.

1. "I'm very interested in scalability, and I'd love to learn more about it. What opportunities are there at this company to learn about this?"
2. "I'm not familiar with technology X, but it sounds like a very interesting solution. Could you tell me a bit more about how it works?"

## ► Know Your Technical Projects

As part of your preparation, you should focus on two or three technical projects that you should deeply master. Select projects that ideally fit the following criteria:

- The project had challenging components (beyond just "learning a lot").
- You played a central role (ideally on the challenging components).
- You can talk at technical depth.

For those projects, and all your projects, be able to talk about the challenges, mistakes, technical decisions, choices of technologies (and tradeoffs of these), and the things you would do differently.

You can also think about follow-up questions, like how you would scale the application.

### ► Responding to Behavioral Questions

Behavioral questions allow your interviewer to get to know you and your prior experience better. Remember the following advice when responding to questions.

#### Be Specific, Not Arrogant

Arrogance is a red flag, but you still want to make yourself sound impressive. So how do you make yourself sound good without being arrogant? By being specific!

Specificity means giving just the facts and letting the interviewer derive an interpretation. For example, rather than saying that you “did all the hard parts,” you can instead describe the specific bits you did that were challenging.

#### Limit Details

When a candidate blabbers on about a problem, it’s hard for an interviewer who isn’t well versed in the subject or project to understand it.

Stay light on details and just state the key points. When possible, try to translate it or at least explain the impact. You can always offer the interviewer the opportunity to drill in further.

“By examining the most common user behavior and applying the Rabin-Karp algorithm, I designed a new algorithm to reduce search from  $O(n)$  to  $O(\log n)$  in 90% of cases. I can go into more details if you’d like.”

This demonstrates the key points while letting your interviewer ask for more details if he wants to.

#### Focus on Yourself, Not Your Team

Interviews are fundamentally an individual assessment. Unfortunately, when you listen to many candidates (especially those in leadership roles), their answers are about “we”, “us”, and “the team.” The interviewer walks away having little idea what the candidate’s actual impact was and might conclude that the candidate did little.

Pay attention to your answers. Listen for how much you say “we” versus “I.” Assume that every question is about your role, and speak to that.

#### Give Structured Answers

There are two common ways to think about structuring responses to a behavioral question: nugget first and S.A.R. These techniques can be used separately or together.

##### *Nugget First*

Nugget First means starting your response with a “nugget” that succinctly describes what your response will be about.

For example:

- Interviewer: “Tell me about a time you had to persuade a group of people to make a big change.”
- Candidate: “Sure, let me tell you about the time when I convinced my school to let undergraduates teach their own courses. Initially, my school had a rule where...”

This technique grabs your interviewer's attention and makes it very clear what your story will be about. It also helps you be more focused in your communication, since you've made it very clear to yourself what the gist of your response is.

#### S.A.R. (Situation, Action, Result)

The S.A.R. approach means that you start off outlining the situation, then explaining the actions you took, and lastly, describing the result.

*Example: "Tell me about a challenging interaction with a teammate."*

- **Situation:** On my operating systems project, I was assigned to work with three other people. While two were great, the third team member didn't contribute much. He stayed quiet during meetings, rarely chimed in during email discussions, and struggled to complete his components. This was an issue not only because it shifted more work onto us, but also because we didn't know if we could count on him.
- **Action:** I didn't want to write him off completely yet, so I tried to resolve the situation. I did three things.

First, I wanted to understand why he was acting like this. Was it laziness? Was he busy with something else? I struck up a conversation with him and then asked him open-ended questions about how he felt it was going. Interestingly, basically out of nowhere, he said that he wanted to take on the writeup, which is one of the most time intensive parts. This showed me that it wasn't laziness; it was that he didn't feel like he was good enough to write code.

Second, now that I understand the cause, I tried to make it clear that he shouldn't fear messing up. I told him about some of the bigger mistakes that I made and admitted that I wasn't clear about a lot of parts of the project either.

Third and finally, I asked him to help me with breaking out some of the components of the project. We sat down together and designed a thorough spec for one of the big component, in much more detail than we had before. Once he could see all the pieces, it helped show him that the project wasn't as scary as he'd assumed.

- **Result:** With his confidence raised, he now offered to take on a bunch of the smaller coding work, and then eventually some of the biggest parts. He finished all his work on time, and he contributed more in discussions. We were happy to work with him on a future project.

The situation and the result should be succinct. Your interviewer generally does not need many details to understand what happened and, in fact, may be confused by them.

By using the S.A.R. model with clear situations, actions and results, the interviewer will be able to easily identify how you made an impact and why it mattered.

Consider putting your stories into the following grid:

	Nugget	Situation	Action(s)	Result	What It Says
Story 1			1. ... 2. ... 3. ...		
Story 2					

#### Explore the Action

In almost all cases, the "action" is the most important part of the story. Unfortunately, far too many people talk on and on about the situation, but then just breeze through the action.

Instead, dive into the action. Where possible, break down the action into multiple parts. For example: "I did three things. First, I..." This will encourage sufficient depth.

### Think About What It Says

Re-read the story on page 35. What personality attributes has the candidate demonstrated?

- **Initiative/Leadership:** The candidate tried to resolve the situation by addressing it head-on.
- **Empathy:** The candidate tried to understand what was happening to the person. The candidate also showed empathy in knowing what would resolve the teammate's insecurity.
- **Compassion:** Although the teammate was harming the team, the candidate wasn't angry at the teammate. His empathy led him to compassion.
- **Humility:** The candidate was able to admit to his own flaws (not only to the teammate, but also to the interviewer).
- **Teamwork/Helpfulness:** The candidate worked with the teammate to break down the project into manageable chunks.

You should think about your stories from this perspective. Analyze the actions you took and how you reacted. What personality attributes does your reaction demonstrate?

In many cases, the answer is "none." That usually means you need to rework how you communicate the story to make the attribute clearer. You don't want to explicitly say, "I did X because I have empathy," but you can go one step away from that. For example:

- **Less Clear Attribute:** "I called up the client and told him what happened."
- **More Clear Attribute (Empathy and Courage):** "I made sure to call the client myself, because I knew that he would appreciate hearing it directly from me."

If you still can't make the personality attributes clear, then you might need to come up with a new story entirely.

### ► So, tell me about yourself...

Many interviewers kick off the session by asking you to tell them a bit about yourself, or asking you to walk through your resume. This is essentially a "pitch". It's your interviewer's first impression of you, so you want to be sure to nail this.

#### Structure

A typical structure that works well for many people is essentially chronological, with the opening sentence describing their current job and the conclusion discussing their relevant and interesting hobbies outside of work (if any).

1. **Current Role [Headline Only]:** "I'm a software engineer at Microworks, where I've been leading the Android team for the last five years."
2. **College:** My background is in computer science. I did my undergrad at Berkeley and spent a few summers working at startups, including one where I attempted to launch my own business.
3. **Post College & Onwards:** After college, I wanted to get some exposure to larger corporations so I joined Amazon as a developer. It was a great experience. I learned a ton about large system design and I got to really drive the launch of a key part of AWS. That actually showed me that I really wanted to be in a more

entrepreneurial environment.

4. **Current Role [Details]:** One of my old managers from Amazon recruited me out to join her startup, which was what brought me to Microworks. Here, I did the initial system architecture, which has scaled pretty well with our rapid growth. I then took an opportunity to lead the Android team. I do manage a team of three, but my role is primarily with technical leadership: architecture, coding, etc.
5. **Outside of Work:** Outside of work, I've been participating in some hackathons—mostly doing iOS development there as a way to learn it more deeply. I'm also active as a moderator on online forums around Android development.
6. **Wrap Up:** I'm looking now for something new, and your company caught my eye. I've always loved the connection with the user, and I really want to get back to a smaller environment too.

This structure works well for about 95% of candidates. For candidate with more experience, you might condense part of it. Ten years from now, the candidate's initial statements might become just: "After my CS degree from Berkeley, I spent a few years at Amazon and then joined a startup where I led the Android team."

## Hobbies

Think carefully about your hobbies. You may or may not want to discuss them.

Often they're just fluff. If your hobby is just generic activities like skiing or playing with your dog, you can probably skip it.

Sometimes though, hobbies can be useful. This often happens when:

- The hobby is extremely unique (e.g., fire breathing). It may strike up a bit of a conversation and kick off the interview on a more amiable note.
- The hobby is technical. This not only boosts your actual skillset, but it also shows passion for technology.
- The hobby demonstrates a positive personality attribute. A hobby like "remodeling your house yourself" shows a drive to learn new things, take some risks, and get your hands dirty (literally and figuratively).

It would rarely hurt to mention hobbies, so when in doubt, you might as well.

Think about how to best frame your hobby though. Do you have any successes or specific work to show from it (e.g., landing a part in a play)? Is there a personality attribute this hobby demonstrates?

## Sprinkle in Shows of Successes

In the above pitch, the candidate has casually dropped in some highlights of his background.

- He specifically mentioned that he was recruited out of Microworks by his old manager, which shows that he was successful at Amazon.
- He also mentions wanting to be in a smaller environment, which shows some element of culture fit (assuming this is a startup he's applying for).
- He mentions some successes he's had, such as launching a key part of AWS and architecting a scalable system.
- He mentions his hobbies, both of which show a drive to learn.

When you think about your pitch, think about what different aspects of your background say about you. Can you drop in shows of successes (awards, promotions, being recruited out by someone you worked with, launches, etc.)? What do you want to communicate about yourself?

# VI

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## Big O

---

This is such an important concept that we are dedicating an entire (long!) chapter to it.

Big O time is the language and metric we use to describe the efficiency of algorithms. Not understanding it thoroughly can really hurt you in developing an algorithm. Not only might you be judged harshly for not really understanding big O, but you will also struggle to judge when your algorithm is getting faster or slower.

Master this concept.

### ► An Analogy

Imagine the following scenario: You've got a file on a hard drive and you need to send it to your friend who lives across the country. You need to get the file to your friend as fast as possible. How should you send it?

Most people's first thought would be email, FTP, or some other means of electronic transfer. That thought is reasonable, but only half correct.

If it's a small file, you're certainly right. It would take 5 - 10 hours to get to an airport, hop on a flight, and then deliver it to your friend.

But what if the file were really, really large? Is it possible that it's faster to physically deliver it via plane?

Yes, actually it is. A one-terabyte (1 TB) file could take more than a day to transfer electronically. It would be much faster to just fly it across the country. If your file is that urgent (and cost isn't an issue), you might just want to do that.

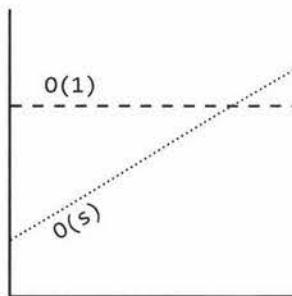
What if there were no flights, and instead you had to drive across the country? Even then, for a really huge file, it would be faster to drive.

### ► Time Complexity

This is what the concept of asymptotic runtime, or big O time, means. We could describe the data transfer "algorithm" runtime as:

- Electronic Transfer:  $O(s)$ , where  $s$  is the size of the file. This means that the time to transfer the file increases linearly with the size of the file. (Yes, this is a bit of a simplification, but that's okay for these purposes.)
- Airplane Transfer:  $O(1)$  with respect to the size of the file. As the size of the file increases, it won't take any longer to get the file to your friend. The time is constant.

No matter how big the constant is and how slow the linear increase is, linear will at some point surpass constant.



There are many more runtimes than this. Some of the most common ones are  $O(\log N)$ ,  $O(N \log N)$ ,  $O(N)$ ,  $O(N^2)$  and  $O(2^N)$ . There's no fixed list of possible runtimes, though.

You can also have multiple variables in your runtime. For example, the time to paint a fence that's  $w$  meters wide and  $h$  meters high could be described as  $O(wh)$ . If you needed  $p$  layers of paint, then you could say that the time is  $O(whp)$ .

### Big O, Big Theta, and Big Omega

If you've never covered big O in an academic setting, you can probably skip this subsection. It might confuse you more than it helps. This "FYI" is mostly here to clear up ambiguity in wording for people who have learned big O before, so that they don't say, "But I thought big O meant..."

Academics use big O, big  $\Theta$  (theta), and big  $\Omega$  (omega) to describe runtimes.

- **O (big O):** In academia, big O describes an upper bound on the time. An algorithm that prints all the values in an array could be described as  $O(N)$ , but it could also be described as  $O(N^2)$ ,  $O(N^3)$ , or  $O(2^N)$  (or many other big O times). The algorithm is at least as fast as each of these; therefore they are upper bounds on the runtime. This is similar to a less-than-or-equal-to relationship. If Bob is  $X$  years old (I'll assume no one lives past age 130), then you could say  $X \leq 130$ . It would also be correct to say that  $X \leq 1,000$  or  $X \leq 1,000,000$ . It's technically true (although not terribly useful). Likewise, a simple algorithm to print the values in an array is  $O(N)$  as well as  $O(N^3)$  or any runtime bigger than  $O(N)$ .
- **$\Omega$  (big omega):** In academia,  $\Omega$  is the equivalent concept but for lower bound. Printing the values in an array is  $\Omega(N)$  as well as  $\Omega(\log N)$  and  $\Omega(1)$ . After all, you know that it won't be *faster* than those runtimes.
- **$\Theta$  (big theta):** In academia,  $\Theta$  means both O and  $\Omega$ . That is, an algorithm is  $\Theta(N)$  if it is both  $O(N)$  and  $\Omega(N)$ .  $\Theta$  gives a tight bound on runtime.

In industry (and therefore in interviews), people seem to have merged  $\Theta$  and O together. Industry's meaning of big O is closer to what academics mean by  $\Theta$ , in that it would be seen as incorrect to describe printing an array as  $O(N^2)$ . Industry would just say this is  $O(N)$ .

For this book, we will use big O in the way that industry tends to use it: By always trying to offer the tightest description of the runtime.

### Best Case, Worst Case, and Expected Case

We can actually describe our runtime for an algorithm in three different ways.

Let's look at this from the perspective of quick sort. Quick sort picks a random element as a "pivot" and then swaps values in the array such that the elements less than pivot appear before elements greater than pivot. This gives a "partial sort." Then it recursively sorts the left and right sides using a similar process.

- **Best Case:** If all elements are equal, then quick sort will, on average, just traverse through the array once. This is  $O(N)$ . (This actually depends slightly on the implementation of quick sort. There are implementations, though, that will run very quickly on a sorted array.)
- **Worst Case:** What if we get really unlucky and the pivot is repeatedly the biggest element in the array? (Actually, this can easily happen. If the pivot is chosen to be the first element in the subarray and the array is sorted in reverse order, we'll have this situation.) In this case, our recursion doesn't divide the array in half and recurse on each half. It just shrinks the subarray by one element. This will degenerate to an  $O(N^2)$  runtime.
- **Expected Case:** Usually, though, these wonderful or terrible situations won't happen. Sure, sometimes the pivot will be very low or very high, but it won't happen over and over again. We can expect a runtime of  $O(N \log N)$ .

We rarely ever discuss best case time complexity, because it's not a very useful concept. After all, we could take essentially any algorithm, special case some input, and then get an  $O(1)$  time in the best case.

For many—probably most—algorithms, the worst case and the expected case are the same. Sometimes they're different, though, and we need to describe both of the runtimes.

*What is the relationship between best/worst/expected case and big O/theta/omega?*

It's easy for candidates to muddle these concepts (probably because both have some concepts of "higher", "lower" and "exactly right"), but there is no particular relationship between the concepts.

Best, worst, and expected cases describe the big O (or big theta) time for particular inputs or scenarios.

Big O, big omega, and big theta describe the upper, lower, and tight bounds for the runtime.

## ► Space Complexity

Time is not the only thing that matters in an algorithm. We might also care about the amount of memory—or space—required by an algorithm.

Space complexity is a parallel concept to time complexity. If we need to create an array of size  $n$ , this will require  $O(n)$  space. If we need a two-dimensional array of size  $n \times n$ , this will require  $O(n^2)$  space.

Stack space in recursive calls counts, too. For example, code like this would take  $O(n)$  time and  $O(n)$  space.

```
1 int sum(int n) { /* Ex 1.*/
2     if (n <= 0) {
3         return 0;
4     }
5     return n + sum(n-1);
6 }
```

Each call adds a level to the stack.

```
1 sum(4)
2   -> sum(3)
3     -> sum(2)
4       -> sum(1)
5         -> sum(0)
```

Each of these calls is added to the call stack and takes up actual memory.

However, just because you have  $n$  calls total doesn't mean it takes  $O(n)$  space. Consider the below function, which adds adjacent elements between 0 and  $n$ :

```

1 int pairSumSequence(int n) { /* Ex 2.*/
2     int sum = 0;
3     for (int i = 0; i < n; i++) {
4         sum += pairSum(i, i + 1);
5     }
6     return sum;
7 }
8
9 int pairSum(int a, int b) {
10    return a + b;
11 }
```

There will be roughly  $O(n)$  calls to `pairSum`. However, those calls do not exist simultaneously on the call stack, so you only need  $O(1)$  space.

## ► Drop the Constants

It is very possible for  $O(N)$  code to run faster than  $O(1)$  code for specific inputs. Big O just describes the rate of increase.

For this reason, we drop the constants in runtime. An algorithm that one might have described as  $O(2N)$  is actually  $O(N)$ .

Many people resist doing this. They will see code that has two (non-nested) for loops and continue this  $O(2N)$ . They think they're being more "precise." They're not.

Consider the below code:

### Min and Max 1

```

1 int min = Integer.MAX_VALUE;
2 int max = Integer.MIN_VALUE;
3 for (int x : array) {
4     if (x < min) min = x;
5     if (x > max) max = x;
6 }
```

### Min and Max 2

```

1 int min = Integer.MAX_VALUE;
2 int max = Integer.MIN_VALUE;
3 for (int x : array) {
4     if (x < min) min = x;
5 }
6 for (int x : array) {
7     if (x > max) max = x;
8 }
```

Which one is faster? The first one does one for loop and the other one does two for loops. But then, the first solution has two lines of code per for loop rather than one.

If you're going to count the number of instructions, then you'd have to go to the assembly level and take into account that multiplication requires more instructions than addition, how the compiler would optimize something, and all sorts of other details.

This would be horrendously complicated, so don't even start going down this road. Big O allows us to express how the runtime scales. We just need to accept that it doesn't mean that  $O(N)$  is always better than  $O(N^2)$ .

## ► Drop the Non-Dominant Terms

What do you do about an expression such as  $O(N^2 + N)$ ? That second  $N$  isn't exactly a constant. But it's not especially important.

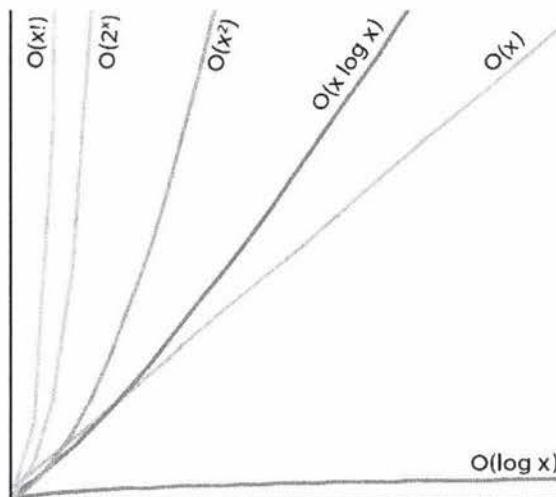
We already said that we drop constants. Therefore,  $O(N^2 + N^2)$  would be  $O(N^2)$ . If we don't care about that latter  $N^2$  term, why would we care about  $N$ ? We don't.

You should drop the non-dominant terms.

- $O(N^2 + N)$  becomes  $O(N^2)$ .
- $O(N + \log N)$  becomes  $O(N)$ .
- $O(5*2^N + 1000N^{100})$  becomes  $O(2^N)$ .

We might still have a sum in a runtime. For example, the expression  $O(B^2 + A)$  cannot be reduced (without some special knowledge of  $A$  and  $B$ ).

The following graph depicts the rate of increase for some of the common big O times.



As you can see,  $O(x^2)$  is much worse than  $O(x)$ , but it's not nearly as bad as  $O(2^x)$  or  $O(x!)$ . There are lots of runtimes worse than  $O(x!)$  too, such as  $O(x^x)$  or  $O(2^x * x!)$ .

## ► Multi-Part Algorithms: Add vs. Multiply

Suppose you have an algorithm that has two steps. When do you multiply the runtimes and when do you add them?

This is a common source of confusion for candidates.

**Add the Runtimes:  $O(A + B)$** 

```

1  for (int a : arrA) {
2      print(a);
3  }
4
5  for (int b : arrB) {
6      print(b);
7  }

```

**Multiply the Runtimes:  $O(A * B)$** 

```

1  for (int a : arrA) {
2      for (int b : arrB) {
3          print(a + "," + b);
4      }
5  }

```

In the example on the left, we do A chunks of work then B chunks of work. Therefore, the total amount of work is  $O(A + B)$ .

In the example on the right, we do B chunks of work for each element in A. Therefore, the total amount of work is  $O(A * B)$ .

In other words:

- If your algorithm is in the form “do this, then, when you’re all done, do that” then you add the runtimes.
- If your algorithm is in the form “do this for each time you do that” then you multiply the runtimes.

It’s very easy to mess this up in an interview, so be careful.

## ► Amortized Time

An `ArrayList`, or a dynamically resizing array, allows you to have the benefits of an array while offering flexibility in size. You won’t run out of space in the `ArrayList` since its capacity will grow as you insert elements.

An `ArrayList` is implemented with an array. When the array hits capacity, the `ArrayList` class will create a new array with double the capacity and copy all the elements over to the new array.

How do you describe the runtime of insertion? This is a tricky question.

The array could be full. If the array contains  $N$  elements, then inserting a new element will take  $O(N)$  time. You will have to create a new array of size  $2N$  and then copy  $N$  elements over. This insertion will take  $O(N)$  time.

However, we also know that this doesn’t happen very often. The vast majority of the time insertion will be in  $O(1)$  time.

We need a concept that takes both into account. This is what amortized time does. It allows us to describe that, yes, this worst case happens every once in a while. But once it happens, it won’t happen again for so long that the cost is “amortized.”

In this case, what is the amortized time?

As we insert elements, we double the capacity when the size of the array is a power of 2. So after  $X$  elements, we double the capacity at array sizes 1, 2, 4, 8, 16, ...,  $X$ . That doubling takes, respectively, 1, 2, 4, 8, 16, 32, 64, ...,  $X$  copies.

What is the sum of  $1 + 2 + 4 + 8 + 16 + \dots + X$ ? If you read this sum left to right, it starts with 1 and doubles until it gets to  $X$ . If you read right to left, it starts with  $X$  and halves until it gets to 1.

What then is the sum of  $X + \frac{X}{2} + \frac{X}{4} + \frac{X}{8} + \dots + 1$ ? This is roughly  $2X$ .

Therefore,  $X$  insertions take  $O(2X)$  time. The amortized time for each insertion is  $O(1)$ .

## ► Log N Runtimes

We commonly see  $O(\log N)$  in runtimes. Where does this come from?

Let's look at binary search as an example. In binary search, we are looking for an example  $x$  in an  $N$ -element sorted array. We first compare  $x$  to the midpoint of the array. If  $x == \text{middle}$ , then we return. If  $x < \text{middle}$ , then we search on the left side of the array. If  $x > \text{middle}$ , then we search on the right side of the array.

```
search 9 within {1, 5, 8, 9, 11, 13, 15, 19, 21}
    compare 9 to 11 -> smaller.
    search 9 within {1, 5, 8, 9, 11}
        compare 9 to 8 -> bigger
        search 9 within {9, 11}
            compare 9 to 9
            return
```

We start off with an  $N$ -element array to search. Then, after a single step, we're down to  $\frac{N}{2}$  elements. One more step, and we're down to  $\frac{N}{4}$  elements. We stop when we either find the value or we're down to just one element.

The total runtime is then a matter of how many steps (dividing  $N$  by 2 each time) we can take until  $N$  becomes 1.

```
N = 16
N = 8      /* divide by 2 */
N = 4      /* divide by 2 */
N = 2      /* divide by 2 */
N = 1      /* divide by 2 */
```

We could look at this in reverse (going from 1 to 16 instead of 16 to 1). How many times we can multiply 1 by 2 until we get  $N$ ?

```
N = 1
N = 2      /* multiply by 2 */
N = 4      /* multiply by 2 */
N = 8      /* multiply by 2 */
N = 16     /* multiply by 2 */
```

What is  $k$  in the expression  $2^k = N$ ? This is exactly what  $\log$  expresses.

$$\begin{aligned} 2^4 &= 16 \rightarrow \log_2 16 = 4 \\ \log_2 N &= k \rightarrow 2^k = N \end{aligned}$$

This is a good takeaway for you to have. When you see a problem where the number of elements in the problem space gets halved each time, that will likely be a  $O(\log N)$  runtime.

This is the same reason why finding an element in a balanced binary search tree is  $O(\log N)$ . With each comparison, we go either left or right. Half the nodes are on each side, so we cut the problem space in half each time.

What's the base of the log? That's an excellent question! The short answer is that it doesn't matter for the purposes of big O. The longer explanation can be found at "Bases of Logs" on page 630.

## ► Recursive Runtimes

Here's a tricky one. What's the runtime of this code?

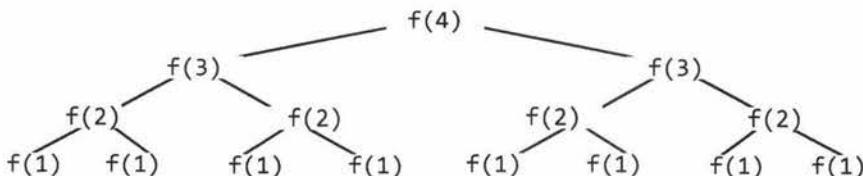
```
1 int f(int n) {
```

```

2   if (n <= 1) {
3       return 1;
4   }
5   return f(n - 1) + f(n - 1);
6 }
```

A lot of people will, for some reason, see the two calls to  $f$  and jump to  $O(N^2)$ . This is completely incorrect.

Rather than making assumptions, let's derive the runtime by walking through the code. Suppose we call  $f(4)$ . This calls  $f(3)$  twice. Each of those calls to  $f(3)$  calls  $f(2)$ , until we get down to  $f(1)$ .



How many calls are in this tree? (Don't count!)

The tree will have depth  $N$ . Each node (i.e., function call) has two children. Therefore, each level will have twice as many calls as the one above it. The number of nodes on each level is:

Level	# Nodes	Also expressed as...	Or...
0	1		$2^0$
1	2	$2 * \text{previous level} = 2$	$2^1$
2	4	$2 * \text{previous level} = 2 * 2^1 = 2^2$	$2^2$
3	8	$2 * \text{previous level} = 2 * 2^2 = 2^3$	$2^3$
4	16	$2 * \text{previous level} = 2 * 2^3 = 2^4$	$2^4$

Therefore, there will be  $2^0 + 2^1 + 2^2 + 2^3 + 2^4 + \dots + 2^N$  (which is  $2^{N+1} - 1$ ) nodes. (See "Sum of Powers of 2" on page 630.)

Try to remember this pattern. When you have a recursive function that makes multiple calls, the runtime will often (but not always) look like  $O(\text{branches}^{\text{depth}})$ , where branches is the number of times each recursive call branches. In this case, this gives us  $O(2^N)$ .

As you may recall, the base of a log doesn't matter for big O since logs of different bases are only different by a constant factor. However, this does not apply to exponents. The base of an exponent does matter. Compare  $2^n$  and  $8^n$ . If you expand  $8^n$ , you get  $(2^3)^n$ , which equals  $2^{3n}$ , which equals  $2^{2n} * 2^n$ . As you can see,  $8^n$  and  $2^n$  are different by a factor of  $2^{2n}$ . That is very much not a constant factor!

The space complexity of this algorithm will be  $O(N)$ . Although we have  $O(2^N)$  nodes in the tree total, only  $O(N)$  exist at any given time. Therefore, we would only need to have  $O(N)$  memory available.

## ► Examples and Exercises

Big O time is a difficult concept at first. However, once it "clicks," it gets fairly easy. The same patterns come up again and again, and the rest you can derive.

We'll start off easy and get progressively more difficult.

**Example 1**

What is the runtime of the below code?

```
1 void foo(int[] array) {  
2     int sum = 0;  
3     int product = 1;  
4     for (int i = 0; i < array.length; i++) {  
5         sum += array[i];  
6     }  
7     for (int i = 0; i < array.length; i++) {  
8         product *= array[i];  
9     }  
10    System.out.println(sum + ", " + product);  
11 }
```

This will take  $O(N)$  time. The fact that we iterate through the array twice doesn't matter.

**Example 2**

What is the runtime of the below code?

```
1 void printPairs(int[] array) {  
2     for (int i = 0; i < array.length; i++) {  
3         for (int j = 0; j < array.length; j++) {  
4             System.out.println(array[i] + "," + array[j]);  
5         }  
6     }  
7 }
```

The inner for loop has  $O(N)$  iterations and it is called  $N$  times. Therefore, the runtime is  $O(N^2)$ .

Another way we can see this is by inspecting what the “meaning” of the code is. It is printing all pairs (two-element sequences). There are  $O(N^2)$  pairs; therefore, the runtime is  $O(N^2)$ .

**Example 3**

This is very similar code to the above example, but now the inner for loop starts at  $i + 1$ .

```
1 void printUnorderedPairs(int[] array) {  
2     for (int i = 0; i < array.length; i++) {  
3         for (int j = i + 1; j < array.length; j++) {  
4             System.out.println(array[i] + "," + array[j]);  
5         }  
6     }  
7 }
```

We can derive the runtime several ways.

This pattern of for loop is very common. It's important that you know the runtime and that you deeply understand it. You can't rely on just memorizing common runtimes. Deep comprehension is important.

#### *Counting the Iterations*

The first time through  $j$  runs for  $N-1$  steps. The second time, it's  $N-2$  steps. Then  $N-3$  steps. And so on.

Therefore, the number of steps total is:

$$(N-1) + (N-2) + (N-3) + \dots + 2 + 1$$

= 1 + 2 + 3 + ... + N-1  
= sum of 1 through N-1

The sum of 1 through N-1 is  $\frac{N(N-1)}{2}$  (see "Sum of Integers 1 through N" on page 630), so the runtime will be  $O(N^2)$ .

### What It Means

Alternatively, we can figure out the runtime by thinking about what the code "means." It iterates through each pair of values for  $(i, j)$  where  $j$  is bigger than  $i$ .

There are  $N^2$  total pairs. Roughly half of those will have  $i < j$  and the remaining half will have  $i > j$ . This code goes through roughly  $\frac{N^2}{2}$  pairs so it does  $O(N^2)$  work.

### Visualizing What It Does

The code iterates through the following  $(i, j)$  pairs when  $N = 8$ :

```
(0, 1) (0, 2) (0, 3) (0, 4) (0, 5) (0, 6) (0, 7)
      (1, 2) (1, 3) (1, 4) (1, 5) (1, 6) (1, 7)
      (2, 3) (2, 4) (2, 5) (2, 6) (2, 7)
      (3, 4) (3, 5) (3, 6) (3, 7)
      (4, 5) (4, 6) (4, 7)
      (5, 6) (5, 7)
      (6, 7)
```

This looks like half of an  $N \times N$  matrix, which has size (roughly)  $\frac{N^2}{2}$ . Therefore, it takes  $O(N^2)$  time.

### Average Work

We know that the outer loop runs  $N$  times. How much work does the inner loop do? It varies across iterations, but we can think about the average iteration.

What is the average value of 1, 2, 3, 4, 5, 6, 7, 8, 9, 10? The average value will be in the middle, so it will be *roughly* 5. (We could give a more precise answer, of course, but we don't need to for big O.)

What about for 1, 2, 3, ...,  $N$ ? The average value in this sequence is  $N/2$ .

Therefore, since the inner loop does  $\frac{N}{2}$  work on average and it is run  $N$  times, the total work is  $\frac{N^2}{2}$  which is  $O(N^2)$ .

### Example 4

This is similar to the above, but now we have two different arrays.

```
1 void printUnorderedPairs(int[] arrayA, int[] arrayB) {
2     for (int i = 0; i < arrayA.length; i++) {
3         for (int j = 0; j < arrayB.length; j++) {
4             if (arrayA[i] < arrayB[j]) {
5                 System.out.println(arrayA[i] + "," + arrayB[j]);
6             }
7         }
8     }
9 }
```

We can break up this analysis. The if-statement within  $j$ 's for loop is  $O(1)$  time since it's just a sequence of constant-time statements.

We now have this:

```
1 void printUnorderedPairs(int[] arrayA, int[] arrayB) {
```

```

2   for (int i = 0; i < arrayA.length; i++) {
3       for (int j = 0; j < arrayB.length; j++) {
4           /* O(1) work */
5       }
6   }
7 }
```

For each element of arrayA, the inner for loop goes through b iterations, where  $b = \text{arrayB.length}$ . If  $a = \text{arrayA.length}$ , then the runtime is  $O(ab)$ .

If you said  $O(N^2)$ , then remember your mistake for the future. It's not  $O(N^2)$  because there are two different inputs. Both matter. This is an extremely common mistake.

### Example 5

What about this strange bit of code?

```

1 void printUnorderedPairs(int[] arrayA, int[] arrayB) {
2     for (int i = 0; i < arrayA.length; i++) {
3         for (int j = 0; j < arrayB.length; j++) {
4             for (int k = 0; k < 100000; k++) {
5                 System.out.println(arrayA[i] + "," + arrayB[j]);
6             }
7         }
8     }
9 }
```

Nothing has really changed here. 100,000 units of work is still constant, so the runtime is  $O(ab)$ .

### Example 6

The following code reverses an array. What is its runtime?

```

1 void reverse(int[] array) {
2     for (int i = 0; i < array.length / 2; i++) {
3         int other = array.length - i - 1;
4         int temp = array[i];
5         array[i] = array[other];
6         array[other] = temp;
7     }
8 }
```

This algorithm runs in  $O(N)$  time. The fact that it only goes through half of the array (in terms of iterations) does not impact the big O time.

### Example 7

Which of the following are equivalent to  $O(N)$ ? Why?

- $O(N + P)$ , where  $P < \frac{N}{2}$
- $O(2N)$
- $O(N + \log N)$
- $O(N + M)$

Let's go through these.

- If  $P < \frac{N}{2}$ , then we know that  $N$  is the dominant term so we can drop the  $O(P)$ .
- $O(2N)$  is  $O(N)$  since we drop constants.

- $O(N)$  dominates  $O(\log N)$ , so we can drop the  $O(\log N)$ .
- There is no established relationship between  $N$  and  $M$ , so we have to keep both variables in there.

Therefore, all but the last one are equivalent to  $O(N)$ .

### Example 8

Suppose we had an algorithm that took in an array of strings, sorted each string, and then sorted the full array. What would the runtime be?

Many candidates will reason the following: sorting each string is  $O(N \log N)$  and we have to do this for each string, so that's  $O(N^2 \log N)$ . We also have to sort this array, so that's an additional  $O(N \log N)$  work. Therefore, the total runtime is  $O(N^2 \log N + N \log N)$ , which is just  $O(N^2 \log N)$ .

This is completely incorrect. Did you catch the error?

The problem is that we used  $N$  in two different ways. In one case, it's the length of the string (which string?). And in another case, it's the length of the array.

In your interviews, you can prevent this error by either not using the variable "N" at all, or by only using it when there is no ambiguity as to what  $N$  could represent.

In fact, I wouldn't even use  $a$  and  $b$  here, or  $m$  and  $n$ . It's too easy to forget which is which and mix them up. An  $O(a^2)$  runtime is completely different from an  $O(a*b)$  runtime.

Let's define new terms—and use names that are logical.

- Let  $s$  be the length of the longest string.
- Let  $a$  be the length of the array.

Now we can work through this in parts:

- Sorting each string is  $O(s \log s)$ .
- We have to do this for every string (and there are  $a$  strings), so that's  $O(a*s \log s)$ .
- Now we have to sort all the strings. There are  $a$  strings, so you'll may be inclined to say that this takes  $O(a \log a)$  time. This is what most candidates would say. You should also take into account that you need to compare the strings. Each string comparison takes  $O(s)$  time. There are  $O(a \log a)$  comparisons, therefore this will take  $O(a*s \log a)$  time.

If you add up these two parts, you get  $O(a*s(\log a + \log s))$ .

This is it. There is no way to reduce it further.

### Example 9

The following simple code sums the values of all the nodes in a balanced binary search tree. What is its runtime?

```
1 int sum(Node node) {
2     if (node == null) {
3         return 0;
4     }
5     return sum(node.left) + node.value + sum(node.right);
6 }
```

Just because it's a binary search tree doesn't mean that there is a log in it!

We can look at this two ways.

### What It Means

The most straightforward way is to think about what this means. This code touches each node in the tree once and does a constant time amount of work with each “touch” (excluding the recursive calls).

Therefore, the runtime will be linear in terms of the number of nodes. If there are  $N$  nodes, then the runtime is  $O(N)$ .

### Recursive Pattern

On page 44, we discussed a pattern for the runtime of recursive functions that have multiple branches. Let’s try that approach here.

We said that the runtime of a recursive function with multiple branches is typically  $O(\text{branches}^{\text{depth}})$ . There are two branches at each call, so we’re looking at  $O(2^{\text{depth}})$ .

At this point many people might assume that something went wrong since we have an exponential algorithm—that something in our logic is flawed or that we’ve inadvertently created an exponential time algorithm (yikes!).

The second statement is correct. We do have an exponential time algorithm, but it’s not as bad as one might think. Consider what variable it’s exponential with respect to.

What is depth? The tree is a balanced binary search tree. Therefore, if there are  $N$  total nodes, then depth is roughly  $\log N$ .

By the equation above, we get  $O(2^{\log N})$ .

Recall what  $\log_2$  means:

$$2^P = Q \rightarrow \log_2 Q = P$$

What is  $2^{\log N}$ ? There is a relationship between 2 and log, so we should be able to simplify this.

Let  $P = 2^{\log N}$ . By the definition of  $\log_2$ , we can write this as  $\log_2 P = \log_2 N$ . This means that  $P = N$ .

$$\text{Let } P = 2^{\log N}$$

$$\rightarrow \log_2 P = \log_2 N$$

$$\rightarrow P = N$$

$$\rightarrow 2^{\log N} = N$$

Therefore, the runtime of this code is  $O(N)$ , where  $N$  is the number of nodes.

### Example 10

The following method checks if a number is prime by checking for divisibility on numbers less than it. It only needs to go up to the square root of  $n$  because if  $n$  is divisible by a number greater than its square root then it’s divisible by something smaller than it.

For example, while 33 is divisible by 11 (which is greater than the square root of 33), the “counterpart” to 11 is 3 ( $3 * 11 = 33$ ). 33 will have already been eliminated as a prime number by 3.

What is the time complexity of this function?

```
1 boolean isPrime(int n) {  
2     for (int x = 2; x * x <= n; x++) {  
3         if (n % x == 0) {  
4             return false;  
5         }  
6     }  
7     return true;
```

---

```
8 }
```

Many people get this question wrong. If you're careful about your logic, it's fairly easy.

The work inside the for loop is constant. Therefore, we just need to know how many iterations the for loop goes through in the worst case.

The for loop will start when  $x = 2$  and end when  $x \cdot x = n$ . Or, in other words, it stops when  $x = \sqrt{n}$  (when  $x$  equals the square root of  $n$ ).

This for loop is really something like this:

```
1 boolean isPrime(int n) {
2     for (int x = 2; x <= sqrt(n); x++) {
3         if (n % x == 0) {
4             return false;
5         }
6     }
7     return true;
8 }
```

This runs in  $O(\sqrt{n})$  time.

### Example 11

The following code computes  $n!$  ( $n$  factorial). What is its time complexity?

```
1 int factorial(int n) {
2     if (n < 0) {
3         return -1;
4     } else if (n == 0) {
5         return 1;
6     } else {
7         return n * factorial(n - 1);
8     }
9 }
```

This is just a straight recursion from  $n$  to  $n-1$  to  $n-2$  down to 1. It will take  $O(n)$  time.

### Example 12

This code counts all permutations of a string.

```
1 void permutation(String str) {
2     permutation(str, "");
3 }
4
5 void permutation(String str, String prefix) {
6     if (str.length() == 0) {
7         System.out.println(prefix);
8     } else {
9         for (int i = 0; i < str.length(); i++) {
10            String rem = str.substring(0, i) + str.substring(i + 1);
11            permutation(rem, prefix + str.charAt(i));
12        }
13    }
14 }
```

This is a (very!) tricky one. We can think about this by looking at how many times `permutation` gets called and how long each call takes. We'll aim for getting as tight of an upper bound as possible.

*How many times does permutation get called in its base case?*

If we were to generate a permutation, then we would need to pick characters for each “slot.” Suppose we had 7 characters in the string. In the first slot, we have 7 choices. Once we pick the letter there, we have 6 choices for the next slot. (Note that this is 6 choices *for each* of the 7 choices earlier.) Then 5 choices for the next slot, and so on.

Therefore, the total number of options is  $7 * 6 * 5 * 4 * 3 * 2 * 1$ , which is also expressed as  $7!$  (7 factorial).

This tells us that there are  $n!$  permutations. Therefore, permutation is called  $n!$  times in its base case (when prefix is the full permutation).

*How many times does permutation get called before its base case?*

But, of course, we also need to consider how many times lines 9 through 12 are hit. Picture a large call tree representing all the calls. There are  $n!$  leaves, as shown above. Each leaf is attached to a path of length  $n$ . Therefore, we know there will be no more than  $n * n!$  nodes (function calls) in this tree.

*How long does each function call take?*

Executing line 7 takes  $O(n)$  time since each character needs to be printed.

Line 10 and line 11 will also take  $O(n)$  time combined, due to the string concatenation. Observe that the sum of the lengths of rem, prefix, and str.charAt(i) will always be  $n$ .

Each node in our call tree therefore corresponds to  $O(n)$  work.

*What is the total runtime?*

Since we are calling permutation  $O(n * n!)$  times (as an upper bound), and each one takes  $O(n)$  time, the total runtime will not exceed  $O(n^2 * n!)$ .

Through more complex mathematics, we can derive a tighter runtime equation (though not necessarily a nice closed-form expression). This would almost certainly be beyond the scope of any normal interview.

### Example 13

The following code computes the Nth Fibonacci number.

```
1 int fib(int n) {  
2     if (n <= 0) return 0;  
3     else if (n == 1) return 1;  
4     return fib(n - 1) + fib(n - 2);  
5 }
```

We can use the earlier pattern we'd established for recursive calls:  $O(\text{branches}^{\text{depth}})$ .

There are 2 branches per call, and we go as deep as  $N$ , therefore the runtime is  $O(2^N)$ .

Through some very complicated math, we can actually get a tighter runtime. The time is indeed exponential, but it's actually closer to  $O(1.6^N)$ . The reason that it's not exactly  $O(2^N)$  is that, at the bottom of the call stack, there is sometimes only one call. It turns out that a lot of the nodes are at the bottom (as is true in most trees), so this single versus double call actually makes a big difference. Saying  $O(2^N)$  would suffice for the scope of an interview, though (and is still technically correct, if you read the note about big theta on page 39). You might get “bonus points” if you can recognize that it'll actually be less than that.

Generally speaking, when you see an algorithm with multiple recursive calls, you're looking at exponential runtime.

### Example 14

The following code prints all Fibonacci numbers from 0 to n. What is its time complexity?

```

1 void allFib(int n) {
2     for (int i = 0; i < n; i++) {
3         System.out.println(i + ":" + fib(i));
4     }
5 }
6
7 int fib(int n) {
8     if (n <= 0) return 0;
9     else if (n == 1) return 1;
10    return fib(n - 1) + fib(n - 2);
11 }
```

Many people will rush to concluding that since `fib(n)` takes  $O(2^n)$  time and it's called n times, then it's  $O(n2^n)$ .

Not so fast. Can you find the error in the logic?

The error is that the n is changing. Yes, `fib(n)` takes  $O(2^n)$  time, but it matters what that value of n is.

Instead, let's walk through each call.

```

fib(1) -> 21 steps
fib(2) -> 22 steps
fib(3) -> 23 steps
fib(4) -> 24 steps
...
fib(n) -> 2n steps
```

Therefore, the total amount of work is:

$$2^1 + 2^2 + 2^3 + 2^4 + \dots + 2^n$$

As we showed on page 44, this is  $2^{n+1}$ . Therefore, the runtime to compute the first n Fibonacci numbers (using this terrible algorithm) is still  $O(2^n)$ .

### Example 15

The following code prints all Fibonacci numbers from 0 to n. However, this time, it stores (i.e., caches) previously computed values in an integer array. If it has already been computed, it just returns the cache. What is its runtime?

```

1 void allFib(int n) {
2     int[] memo = new int[n + 1];
3     for (int i = 0; i < n; i++) {
4         System.out.println(i + ":" + fib(i, memo));
5     }
6 }
7
8 int fib(int n, int[] memo) {
9     if (n <= 0) return 0;
10    else if (n == 1) return 1;
11    else if (memo[n] > 0) return memo[n];
12
13    memo[n] = fib(n - 1, memo) + fib(n - 2, memo);
```

```
14     return memo[n];
15 }
```

Let's walk through what this algorithm does.

```
fib(1) -> return 1
fib(2)
    fib(1) -> return 1
    fib(0) -> return 0
    store 1 at memo[2]
fib(3)
    fib(2) -> lookup memo[2] -> return 1
    fib(1) -> return 1
    store 2 at memo[3]
fib(4)
    fib(3) -> lookup memo[3] -> return 2
    fib(2) -> lookup memo[2] -> return 1
    store 3 at memo[4]
fib(5)
    fib(4) -> lookup memo[4] -> return 3
    fib(3) -> lookup memo[3] -> return 2
    store 5 at memo[5]
...

```

At each call to `fib(i)`, we have already computed and stored the values for `fib(i-1)` and `fib(i-2)`. We just look up those values, sum them, store the new result, and return. This takes a constant amount of time.

We're doing a constant amount of work N times, so this is  $O(n)$  time.

This technique, called memoization, is a very common one to optimize exponential time recursive algorithms.

### Example 16

The following function prints the powers of 2 from 1 through n (inclusive). For example, if n is 4, it would print 1, 2, and 4. What is its runtime?

```
1 int powersOf2(int n) {
2     if (n < 1) {
3         return 0;
4     } else if (n == 1) {
5         System.out.println(1);
6         return 1;
7     } else {
8         int prev = powersOf2(n / 2);
9         int curr = prev * 2;
10        System.out.println(curr);
11        return curr;
12    }
13 }
```

There are several ways we could compute this runtime.

#### *What It Does*

Let's walk through a call like `powersOf2(50)`.

```
powersOf2(50)
-> powersOf2(25)
```

```

-> powersOf2(12)
-> powersOf2(6)
-> powersOf2(3)
-> powersOf2(1)
-> print & return 1
print & return 2
print & return 4
print & return 8
print & return 16
print & return 32

```

The runtime, then, is the number of times we can divide 50 (or n) by 2 until we get down to the base case (1). As we discussed on page 44, the number of times we can halve n until we get 1 is  $O(\log n)$ .

### *What It Means*

We can also approach the runtime by thinking about what the code is supposed to be doing. It's supposed to be computing the powers of 2 from 1 through n.

Each call to `powersOf2` results in exactly one number being printed and returned (excluding what happens in the recursive calls). So if the algorithm prints 13 values at the end, then `powersOf2` was called 13 times.

In this case, we are told that it prints all the powers of 2 between 1 and n. Therefore, the number of times the function is called (which will be its runtime) must equal the number of powers of 2 between 1 and n.

There are  $\log N$  powers of 2 between 1 and n. Therefore, the runtime is  $O(\log n)$ .

### *Rate of Increase*

A final way to approach the runtime is to think about how the runtime changes as n gets bigger. After all, this is exactly what big O time means.

If N goes from P to P+1, the number of calls to `powersOfTwo` might not change at all. When will the number of calls to `powersOfTwo` increase? It will increase by 1 each time n doubles in size.

So, each time n doubles, the number of calls to `powersOfTwo` increases by 1. Therefore, the number of calls to `powersOfTwo` is the number of times you can double 1 until you get n. It is x in the equation  $2^x = n$ .

What is x? The value of x is  $\log n$ . This is exactly what meant by  $x = \log n$ .

Therefore, the runtime is  $O(\log n)$ .

---

## Additional Problems

---

### VI.1 The following code computes the product of a and b. What is its runtime?

```

int product(int a, int b) {
    int sum = 0;
    for (int i = 0; i < b; i++) {
        sum += a;
    }
    return sum;
}

```

### VI.2 The following code computes $a^b$ . What is its runtime?

```

int power(int a, int b) {
    if (b < 0) {

```

```
        return 0; // error
    } else if (b == 0) {
        return 1;
    } else {
        return a * power(a, b - 1);
    }
}
```

- VI.3 The following code computes  $a \% b$ . What is its runtime?

```
int mod(int a, int b) {
    if (b <= 0) {
        return -1;
    }
    int div = a / b;
    return a - div * b;
}
```

- VI.4 The following code performs integer division. What is its runtime (assume  $a$  and  $b$  are both positive)?

```
int div(int a, int b) {
    int count = 0;
    int sum = b;
    while (sum <= a) {
        sum += b;
        count++;
    }
    return count;
}
```

- VI.5 The following code computes the [integer] square root of a number. If the number is not a perfect square (there is no integer square root), then it returns -1. It does this by successive guessing. If  $n$  is 100, it first guesses 50. Too high? Try something lower – halfway between 1 and 50. What is its runtime?

```
int sqrt(int n) {
    return sqrt_helper(n, 1, n);
}

int sqrt_helper(int n, int min, int max) {
    if (max < min) return -1; // no square root

    int guess = (min + max) / 2;
    if (guess * guess == n) { // found it!
        return guess;
    } else if (guess * guess < n) { // too low
        return sqrt_helper(n, guess + 1, max); // try higher
    } else { // too high
        return sqrt_helper(n, min, guess - 1); // try lower
    }
}
```

- VI.6 The following code computes the [integer] square root of a number. If the number is not a perfect square (there is no integer square root), then it returns -1. It does this by trying increasingly large numbers until it finds the right value (or is too high). What is its runtime?

```
int sqrt(int n) {
    for (int guess = 1; guess * guess <= n; guess++) {
        if (guess * guess == n) {
            return guess;
        }
    }
}
```

```

        }
    }
    return -1;
}

```

**VI.7** If a binary search tree is not balanced, how long might it take (worst case) to find an element in it?

**VI.8** You are looking for a specific value in a binary tree, but the tree is not a binary search tree. What is the time complexity of this?

**VI.9** The appendToNew method appends a value to an array by creating a new, longer array and returning this longer array. You've used the appendToNew method to create a copyArray function that repeatedly calls appendToNew. How long does copying an array take?

```

int[] copyArray(int[] array) {
    int[] copy = new int[0];
    for (int value : array) {
        copy = appendToNew(copy, value);
    }
    return copy;
}

int[] appendToNew(int[] array, int value) {
    // copy all elements over to new array
    int[] bigger = new int[array.length + 1];
    for (int i = 0; i < array.length; i++) {
        bigger[i] = array[i];
    }

    // add new element
    bigger[bigger.length - 1] = value;
    return bigger;
}

```

**VI.10** The following code sums the digits in a number. What is its big O time?

```

int sumDigits(int n) {
    int sum = 0;
    while (n > 0) {
        sum += n % 10;
        n /= 10;
    }
    return sum;
}

```

**VI.11** The following code prints all strings of length k where the characters are in sorted order. It does this by generating all strings of length k and then checking if each is sorted. What is its runtime?

```

int numChars = 26;

void printSortedStrings(int remaining) {
    printSortedStrings(remaining, "");
}

void printSortedStrings(int remaining, String prefix) {
    if (remaining == 0) {
        if (isInOrder(prefix)) {
            System.out.println(prefix);
        }
    }
}

```

```
        } else {
            for (int i = 0; i < numChars; i++) {
                char c = ithLetter(i);
                printSortedStrings(remaining - 1, prefix + c);
            }
        }
    }

boolean isInOrder(String s) {
    for (int i = 1; i < s.length(); i++) {
        int prev = ithLetter(s.charAt(i - 1));
        int curr = ithLetter(s.charAt(i));
        if (prev > curr) {
            return false;
        }
    }
    return true;
}

char ithLetter(int i) {
    return (char) (((int) 'a') + i);
}
```

- VI.12 The following code computes the intersection (the number of elements in common) of two arrays. It assumes that neither array has duplicates. It computes the intersection by sorting one array (array b) and then iterating through array a checking (via binary search) if each value is in b. What is its runtime?

```
int intersection(int[] a, int[] b) {
    mergesort(b);
    int intersect = 0;

    for (int x : a) {
        if (binarySearch(b, x) >= 0) {
            intersect++;
        }
    }

    return intersect;
}
```

---

## Solutions

---

1.  $O(b)$ . The for loop just iterates through b.
2.  $O(b)$ . The recursive code iterates through b calls, since it subtracts one at each level.
3.  $O(1)$ . It does a constant amount of work.
4.  $O(\frac{n}{b})$ . The variable count will eventually equal  $\frac{n}{b}$ . The while loop iterates count times. Therefore, it iterates  $\frac{n}{b}$  times.
5.  $O(\log n)$ . This algorithm is essentially doing a binary search to find the square root. Therefore, the runtime is  $O(\log n)$ .
6.  $O(\sqrt{n})$ . This is just a straightforward loop that stops when  $guess * guess > n$  (or, in other words, when  $guess > \sqrt{n}$ ).

7.  $O(n)$ , where  $n$  is the number of nodes in the tree. The max time to find an element is the depth tree. The tree could be a straight list downwards and have depth  $n$ .
  8.  $O(n)$ . Without any ordering property on the nodes, we might have to search through all the nodes.
  9.  $O(n^2)$ , where  $n$  is the number of elements in the array. The first call to `appendToNew` takes 1 copy. The second call takes 2 copies. The third call takes 3 copies. And so on. The total time will be the sum of 1 through  $n$ , which is  $O(n^2)$ .
10.  $O(\log n)$ . The runtime will be the number of digits in the number. A number with  $d$  digits can have a value up to  $10^d$ . If  $n = 10^d$ , then  $d = \log n$ . Therefore, the runtime is  $O(\log n)$ .
11.  $O(kc^k)$ , where  $k$  is the length of the string and  $c$  is the number of characters in the alphabet. It takes  $O(c^k)$  time to generate each string. Then, we need to check that each of these is sorted, which takes  $O(k)$  time.
12.  $O(b \log b + a \log b)$ . First, we have to sort array  $b$ , which takes  $O(b \log b)$  time. Then, for each element in  $a$ , we do binary search in  $O(\log b)$  time. The second part takes  $O(a \log b)$  time.

# VII

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## Technical Questions

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Technical questions form the basis for how many of the top tech companies interview. Many candidates are intimidated by the difficulty of these questions, but there are logical ways to approach them.

### ► How to Prepare

Many candidates just read through problems and solutions. That's like trying to learn calculus by reading a problem and its answer. You need to practice solving problems. Memorizing solutions won't help you much.

For each problem in this book (and any other problem you might encounter), do the following:

1. *Try to solve the problem on your own.* Hints are provided at the back of this book, but push yourself to develop a solution with as little help as possible. Many questions are designed to be tough—that's okay! When you're solving a problem, make sure to think about the space and time efficiency.
2. *Write the code on paper.* Coding on a computer offers luxuries such as syntax highlighting, code completion, and quick debugging. Coding on paper does not. Get used to this—and to how slow it is to write and edit code—by coding on paper.
3. *Test your code—on paper.* This means testing the general cases, base cases, error cases, and so on. You'll need to do this during your interview, so it's best to practice this in advance.
4. *Type your paper code as-is into a computer.* You will probably make a bunch of mistakes. Start a list of all the errors you make so that you can keep these in mind during the actual interview.

In addition, try to do as many mock interviews as possible. You and a friend can take turns giving each other mock interviews. Though your friend may not be an expert interviewer, he or she may still be able to walk you through a coding or algorithm problem. You'll also learn a lot by experiencing what it's like to be an interviewer.

### ► What You Need To Know

The sorts of data structure and algorithm questions that many companies focus on are not knowledge tests. However, they do assume a baseline of knowledge.

#### **Core Data Structures, Algorithms, and Concepts**

Most interviewers won't ask about specific algorithms for binary tree balancing or other complex algorithms. Frankly, being several years out of school, they probably don't remember these algorithms either.

You're usually only expected to know the basics. Here's a list of the absolute, must-have knowledge:

Data Structures	Algorithms	Concepts
Linked Lists	Breadth-First Search	Bit Manipulation
Trees, Tries, & Graphs	Depth-First Search	Memory (Stack vs. Heap)
Stacks & Queues	Binary Search	Recursion
Heaps	Merge Sort	Dynamic Programming
Vectors / ArrayLists	Quick Sort	Big O Time & Space
Hash Tables		

For each of these topics, make sure you understand how to use and implement them and, where applicable, the space and time complexity.

Practicing implementing the data structures and algorithm (on paper, and then on a computer) is also a great exercise. It will help you learn how the internals of the data structures work, which is important for many interviews.

Did you miss that paragraph above? It's important. If you don't feel very, very comfortable with each of the data structures and algorithms listed, practice implementing them from scratch.

In particular, hash tables are an extremely important topic. Make sure you are very comfortable with this data structure.

### Powers of 2 Table

The table below is useful for many questions involving scalability or any sort of memory limitation. Memorizing this table isn't strictly required, but it can be useful. You should at least be comfortable deriving it.

Power of 2	Exact Value (X)	Approx. Value	X Bytes into MB, GB, etc.
7	128		
8	256		
10	1024	1 thousand	1 KB
16	65,536		64 KB
20	1,048,576	1 million	1 MB
30	1,073,741,824	1 billion	1 GB
32	4,294,967,296		4 GB
40	1,099,511,627,776	1 trillion	1 TB

For example, you could use this table to quickly compute that a bit vector mapping every 32-bit integer to a boolean value could fit in memory on a typical machine. There are  $2^{32}$  such integers. Because each integer takes one bit in this bit vector, we need  $2^{32}$  bits (or  $2^{29}$  bytes) to store this mapping. That's about half a gigabyte of memory, which can be easily held in memory on a typical machine.

If you are doing a phone screen with a web-based company, it may be useful to have this table in front of you.

## ► Walking Through a Problem

The below map/flowchart walks you through how to solve a problem. Use this in your practice. You can download this handout and more at [CrackingTheCodingInterview.com](http://CrackingTheCodingInterview.com).

### *A Problem-Solving Flowchart*



We'll go through this flowchart in more detail.

### What to Expect

Interviews are supposed to be difficult. If you don't get every—or any—answer immediately, that's okay! That's the normal experience, and it's not bad.

Listen for guidance from the interviewer. The interviewer might take a more active or less active role in your problem solving. The level of interviewer participation depends on your performance, the difficulty of the question, what the interviewer is looking for, and the interviewer's own personality.

When you're given a problem (or when you're practicing), work your way through it using the approach below.

#### 1. Listen Carefully

You've likely heard this advice before, but I'm saying something a bit more than the standard "make sure you hear the problem correctly" advice.

Yes, you do want to listen to the problem and make sure you heard it correctly. You do want to ask questions about anything you're unsure about.

But I'm saying something more than that.

Listen carefully to the problem, and be sure that you've mentally recorded any *unique* information in the problem.

For example, suppose a question starts with one of the following lines. It's reasonable to assume that the information is there for a reason.

- "Given two arrays that are sorted, find ..."

You probably need to know that the data is sorted. The optimal algorithm for the sorted situation is probably different than the optimal algorithm for the unsorted situation.

- "Design an algorithm to be run repeatedly on a server that ..."

The server/to-be-run-repeatedly situation is different from the run-once situation. Perhaps this means that you cache data? Or perhaps it justifies some reasonable precomputation on the initial dataset?

It's unlikely (although not impossible) that your interviewer would give you this information if it didn't affect the algorithm.

Many candidates will hear the problem correctly. But ten minutes into developing an algorithm, some of the key details of the problem have been forgotten. Now they are in a situation where they actually can't solve the problem optimally.

Your first algorithm doesn't need to use the information. But if you find yourself stuck, or you're still working to develop something more optimal, ask yourself if you've used all the information in the problem.

You might even find it useful to write the pertinent information on the whiteboard.

#### 2. Draw an Example

An example can dramatically improve your ability to solve an interview question, and yet so many candidates just try to solve the question in their heads.

When you hear a question, get out of your chair, go to the whiteboard, and draw an example.

There's an art to drawing an example though. You want a good example.

Very typically, a candidate might draw something like this for an example of a binary search tree:



This is a bad example for several reasons. First, it's too small. You will have trouble finding a pattern in such a small example. Second, it's not specific. A binary search tree has values. What if the numbers tell you something about how to approach the problem? Third, it's actually a special case. It's not just a balanced tree, but it's also a beautiful, perfect tree where every node other than the leaves has two children. Special cases can be very deceiving.

Instead, you want to create an example that is:

- Specific. It should use real numbers or strings (if applicable to the problem).
- Sufficiently large. Most examples are too small, by about 50%.
- Not a special case. Be careful. It's very easy to inadvertently draw a special case. If there's any way your example is a special case (even if you think it probably won't be a big deal), you should fix it.

Try to make the best example you can. If it later turns out your example isn't quite right, you can and should fix it.

### 3. State a Brute Force

Once you have an example done (actually, you can switch the order of steps 2 and 3 in some problems), state a brute force. It's okay and expected that your initial algorithm won't be very optimal.

Some candidates don't state the brute force because they think it's both obvious and terrible. But here's the thing: Even if it's obvious for you, it's not necessarily obvious for all candidates. You don't want your interviewer to think that you're struggling to see even the easy solution.

It's okay that this initial solution is terrible. Explain what the space and time complexity is, and then dive into improvements.

Despite being possibly slow, a brute force algorithm is valuable to discuss. It's a starting point for optimizations, and it helps you wrap your head around the problem.

### 4. Optimize

Once you have a brute force algorithm, you should work on optimizing it. A few techniques that work well are:

1. Look for any unused information. Did your interviewer tell you that the array was sorted? How can you leverage that information?
2. Use a fresh example. Sometimes, just seeing a different example will unclog your mind or help you see a pattern in the problem.
3. Solve it "incorrectly." Just like having an inefficient solution can help you find an efficient solution, having an incorrect solution might help you find a correct solution. For example, if you're asked to generate a

random value from a set such that all values are equally likely, an incorrect solution might be one that returns a semi-random value: Any value could be returned, but some are more likely than others. You can then think about why that solution isn't perfectly random. Can you rebalance the probabilities?

4. Make time vs. space tradeoff. Sometimes storing extra state about the problem can help you optimize the runtime.
5. Precompute information. Is there a way that you can reorganize the data (sorting, etc.) or compute some values upfront that will help save time in the long run?
6. Use a hash table. Hash tables are widely used in interview questions and should be at the top of your mind.
7. Think about the best conceivable runtime (discussed on page 72).

Walk through the brute force with these ideas in mind and look for BUD (page 67).

## 5. Walk Through

After you've nailed down an optimal algorithm, don't just dive into coding. Take a moment to solidify your understanding of the algorithm.

Whiteboard coding is slow—very slow. So is testing your code and fixing it. As a result, you need to make sure that you get it as close to "perfect" in the beginning as possible.

Walk through your algorithm and get a feel for the structure of the code. Know what the variables are and when they change.

What about pseudocode? You can write pseudocode if you'd like. Be careful about what you write. Basic steps ("(1) Search array. (2) Find biggest. (3) Insert in heap.") or brief logic ("if  $p < q$ , move  $p$ . else move  $q$ ") can be valuable. But when your pseudocode starts having for loops that are written in plain English, then you're essentially just writing sloppy code. It'd probably be faster to just write the code.

If you don't understand exactly what you're about to write, you'll struggle to code it. It will take you longer to finish the code, and you're more likely to make major errors.

## 6. Implement

Now that you have an optimal algorithm and you know exactly what you're going to write, go ahead and implement it.

Start coding in the far top left corner of the whiteboard (you'll need the space). Avoid "line creep" (where each line of code is written an awkward slant). It makes your code look messy and can be very confusing when working in a whitespace-sensitive language, like Python.

Remember that you only have a short amount of code to demonstrate that you're a great developer. Everything counts. Write beautiful code.

Beautiful code means:

- Modularized code. This shows good coding style. It also makes things easier for you. If your algorithm uses a matrix initialized to `{ {1, 2, 3}, {4, 5, 6}, ... }`, don't waste your time writing this initialization code. Just pretend you have a function `initIncrementalMatrix(int size)`. Fill in the details later if you need to.

- Error checks. Some interviewers care a lot about this, while others don't. A good compromise here is to add a `todo` and then just explain out loud what you'd like to test.
- Use other classes/structs where appropriate. If you need to return a list of start and end points from a function, you could do this as a two-dimensional array. It's better though to do this as a list of `StartEndPair` (or possibly `Range`) objects. You don't necessarily have to fill in the details for the class. Just pretend it exists and deal with the details later if you have time.
- Good variable names. Code that uses single-letter variables everywhere is difficult to read. That's not to say that there's anything wrong with using `i` and `j`, where appropriate (such as in a basic for-loop iterating through an array). However, be careful about where you do this. If you write something like `int i = startOfChild(array)`, there might be a better name for this variable, such as `startChild`.

Long variable names can also be slow to write though. A good compromise that most interviewers will be okay with is to abbreviate it after the first usage. You can use `startChild` the first time, and then explain to your interviewer that you will abbreviate this as `sc` after this.

The specifics of what makes good code vary between interviewers and candidates, and the problem itself. Focus on writing beautiful code, whatever that means to you.

If you see something you can refactor later on, then explain this to your interviewer and decide whether or not it's worth the time to do so. Usually it is, but not always.

If you get confused (which is common), go back to your example and walk through it again.

### 7. Test

You wouldn't check in code in the real world without testing it, and you shouldn't "submit" code in an interview without testing it either.

There are smart and not-so-smart ways to test your code though.

What many candidates do is take their earlier example and test it against their code. That might discover bugs, but it'll take a really long time to do so. Hand testing is very slow. If you really did use a nice, big example to develop your algorithm, then it'll take you a very long time to find that little off-by-one error at the end of your code.

Instead, try this approach:

1. Start with a "conceptual" test. A conceptual test means just reading and analyzing what each line of code does. Think about it like you're explaining the lines of code for a code reviewer. Does the code do what you think it should do?
2. Weird looking code. Double check that line of code that says `x = length - 2`. Investigate that for loop that starts at `i = 1`. While you undoubtedly did this for a reason, it's really easy to get it just slightly wrong.
3. Hot spots. You've coded long enough to know what things are likely to cause problems. Base cases in recursive code. Integer division. Null nodes in binary trees. The start and end of iteration through a linked list. Double check that stuff.
4. Small test cases. This is the first time we use an actual, specific test case to test the code. Don't use that nice, big 8-element array from the algorithm part. Instead, use a 3 or 4 element array. It'll likely discover the same bugs, but it will be much faster to do so.
5. Special cases. Test your code against null or single element values, the extreme cases, and other special cases.

When you find bugs (and you probably will), you should of course fix them. But don't just make the first correction you think of. Instead, carefully analyze why the bug occurred and ensure that your fix is the best one.

## ► Optimize & Solve Technique #1: Look for BUD

This is perhaps the most useful approach I've found for optimizing problems. "BUD" is a silly acronym for:

- Bottlenecks
- Unnecessary work
- Duplicated work

These are three of the most common things that an algorithm can "waste" time doing. You can walk through your brute force looking for these things. When you find one of them, you can then focus on getting rid of it.

If it's still not optimal, you can repeat this approach on your current best algorithm.

### Bottlenecks

A bottleneck is a part of your algorithm that slows down the overall runtime. There are two common ways this occurs:

- You have one-time work that slows down your algorithm. For example, suppose you have a two-step algorithm where you first sort the array and then you find elements with a particular property. The first step is  $O(N \log N)$  and the second step is  $O(N)$ . Perhaps you could reduce the second step to  $O(\log N)$  or  $O(1)$ , but would it matter? Not too much. It's certainly not a priority, as the  $O(N \log N)$  is the bottleneck. Until you optimize the first step, your overall algorithm will be  $O(N \log N)$ .
- You have a chunk of work that's done repeatedly, like searching. Perhaps you can reduce that from  $O(N)$  to  $O(\log N)$  or even  $O(1)$ . That will greatly speed up your overall runtime.

Optimizing a bottleneck can make a big difference in your overall runtime.

**Example:** Given an array of distinct integer values, count the number of pairs of integers that have difference  $k$ . For example, given the array  $\{1, 7, 5, 9, 2, 12, 3\}$  and the difference  $k = 2$ , there are four pairs with difference 2:  $(1, 3)$ ,  $(3, 5)$ ,  $(5, 7)$ ,  $(7, 9)$ .

A brute force algorithm is to go through the array, starting from the first element, and then search through the remaining elements (which will form the other side of the pair). For each pair, compute the difference. If the difference equals  $k$ , increment a counter of the difference.

The bottleneck here is the repeated search for the "other side" of the pair. It's therefore the main thing to focus on optimizing.

How can we more quickly find the right "other side"? Well, we actually know the other side of  $(x, ?)$ . It's  $x + k$  or  $x - k$ . If we sorted the array, we could find the other side for each of the  $N$  elements in  $O(\log N)$  time by doing a binary search.

We now have a two-step algorithm, where both steps take  $O(N \log N)$  time. Now, sorting is the new bottleneck. Optimizing the second step won't help because the first step is slowing us down anyway.

We just have to get rid of the first step entirely and operate on an unsorted array. How can we find things quickly in an unsorted array? With a hash table.

Throw everything in the array into the hash table. Then, to look up if  $x + k$  or  $x - k$  exist in the array, we just look it up in the hash table. We can do this in  $O(N)$  time.

### Unnecessary Work

Example: Print all positive integer solutions to the equation  $a^3 + b^3 = c^3 + d^3$  where  $a, b, c,$  and  $d$  are integers between 1 and 1000.

A brute force solution will just have four nested for loops. Something like:

```
1 n = 1000
2 for a from 1 to n
3   for b from 1 to n
4     for c from 1 to n
5       for d from 1 to n
6         if a3 + b3 == c3 + d3
7           print a, b, c, d
```

This algorithm iterates through all possible values of  $a, b, c,$  and  $d$  and checks if that combination happens to work.

It's unnecessary to continue checking for other possible values of  $d$ . Only one could work. We should at least break after we find a valid solution.

```
1 n = 1000
2 for a from 1 to n
3   for b from 1 to n
4     for c from 1 to n
5       for d from 1 to n
6         if a3 + b3 == c3 + d3
7           print a, b, c, d
8           break // break out of d's loop
```

This won't make a meaningful change to the runtime—our algorithm is still  $O(N^4)$ —but it's still a good, quick fix to make.

Is there anything else that is unnecessary? Yes. If there's only one valid  $d$  value for each  $(a, b, c),$  then we can just compute it. This is just simple math:  $d = \sqrt[3]{a^3 + b^3 - c^3}$ .

```
1 n = 1000
2 for a from 1 to n
3   for b from 1 to n
4     for c from 1 to n
5       d = pow(a3 + b3 - c3, 1/3) // Will round to int
6       if a3 + b3 == c3 + d3 // Validate that the value works
7       print a, b, c, d
```

The `if` statement on line 6 is important. Line 5 will always find a value for  $d,$  but we need to check that it's the right integer value.

This will reduce our runtime from  $O(N^4)$  to  $O(N^3)$ .

### Duplicated Work

Using the same problem and brute force algorithm as above, let's look for duplicated work this time.

The algorithm operates by essentially iterating through all  $(a, b)$  pairs and then searching all  $(c, d)$  pairs to find if there are any matches to that  $(a, b)$  pair.

Why do we keep on computing all ( $c$ ,  $d$ ) pairs for each ( $a$ ,  $b$ ) pair? We should just create the list of ( $c$ ,  $d$ ) pairs once. Then, when we have an ( $a$ ,  $b$ ) pair, find the matches within the ( $c$ ,  $d$ ) list. We can quickly locate the matches by inserting each ( $c$ ,  $d$ ) pair into a hash table that maps from the sum to the pair (or, rather, the list of pairs that have that sum).

```

1 n = 1000
2 for c from 1 to n
3   for d from 1 to n
4     result = c3 + d3
5     append (c, d) to list at value map[result]
6 for a from 1 to n
7   for b from 1 to n
8     result = a3 + b3
9     list = map.get(result)
10    for each pair in list
11      print a, b, pair

```

Actually, once we have the map of all the ( $c$ ,  $d$ ) pairs, we can just use that directly. We don't need to generate the ( $a$ ,  $b$ ) pairs. Each ( $a$ ,  $b$ ) will already be in the map.

```

1 n = 1000
2 for c from 1 to n
3   for d from 1 to n
4     result = c3 + d3
5     append (c, d) to list at value map[result]
6
7 for each result, list in map
8   for each pair1 in list
9     for each pair2 in list
10    print pair1, pair2

```

This will take our runtime to  $O(N^2)$ .

## ► Optimize & Solve Technique #2: DIY (Do It Yourself)

The first time you heard about how to find an element in a sorted array (before being taught binary search), you probably didn't jump to, "Ah ha! We'll compare the target element to the midpoint and then recurse on the appropriate half."

And yet, you could give someone who has no knowledge of computer science an alphabetized pile of student papers and they'll likely implement something like binary search to locate a student's paper. They'll probably say, "Gosh, Peter Smith? He'll be somewhere in the bottom of the stack." They'll pick a random paper in the middle(ish), compare the name to "Peter Smith", and then continue this process on the remainder of the papers. Although they have no knowledge of binary search, they intuitively "get it."

Our brains are funny like this. Throw the phrase "Design an algorithm" in there and people often get all jumbled up. But give people an actual example—whether just of the data (e.g., an array) or of the real-life parallel (e.g., a pile of papers)—and their intuition gives them a very nice algorithm.

I've seen this come up countless times with candidates. Their computer algorithm is extraordinarily slow, but when asked to solve the same problem manually, they immediately do something quite fast. (And it's not too surprisingly, in some sense. Things that are slow for a computer are often slow by hand. Why would you put yourself through extra work?)

Therefore, when you get a question, try just working it through intuitively on a real example. Often a bigger example will be easier.

Example: Given a smaller string  $s$  and a bigger string  $b$ , design an algorithm to find all permutations of the shorter string within the longer one. Print the location of each permutation.

Think for a moment about how you'd solve this problem. Note permutations are rearrangements of the string, so the characters in  $s$  can appear in any order in  $b$ . They must be contiguous though (not split by other characters).

If you're like most candidates, you probably thought of something like: Generate all permutations of  $s$  and then look for each in  $b$ . Since there are  $S!$  permutations, this will take  $O(S! * B)$  time, where  $S$  is the length of  $s$  and  $B$  is the length of  $b$ .

This works, but it's an extraordinarily slow algorithm. It's actually worse than an exponential algorithm. If  $s$  has 14 characters, that's over 87 billion permutations. Add one more character into  $s$  and we have 15 times more permutations. Ouch!

Approached a different way, you could develop a decent algorithm fairly easily. Give yourself a big example, like this one:

$s$ : abbc  
 $b$ : cbabadcbbabbcbabaabccbabc

Where are the permutations of  $s$  within  $b$ ? Don't worry about how you're doing it. Just find them. Even a 12 year old could do this!

(No, really, go find them. I'll wait!)

I've underlined below each permutation.

$s$ : abbc  
 $b$ : cbabadcbbabbcbabaabccbabc

— — — —

Did you find these? How?

Few people—even those who earlier came up with the  $O(S! * B)$  algorithm—actually generate all the permutations of  $abbc$  to locate those permutations in  $b$ . Almost everyone takes one of two (very similar) approaches:

1. Walk through  $b$  and look at sliding windows of 4 characters (since  $s$  has length 4). Check if each window is a permutation of  $s$ .
2. Walk through  $b$ . Every time you see a character in  $s$ , check if the next four (the length of  $s$ ) characters are a permutation of  $s$ .

Depending on the exact implementation of the “is this a permutation” part, you’ll probably get a runtime of either  $O(B * S)$ ,  $O(B * S \log S)$ , or  $O(B * S^2)$ . None of these are the most optimal algorithm (there is an  $O(B)$  algorithm), but it’s a lot better than what we had before.

Try this approach when you’re solving questions. Use a nice, big example and intuitively—manually, that is—solve it for the specific example. Then, afterwards, think hard about how you solved it. Reverse engineer your own approach.

Be particularly aware of any “optimizations” you intuitively or automatically made. For example, when you were doing this problem, you might have just skipped right over the sliding window with “d” in it, since “d” isn’t in  $abbc$ . That’s an optimization your brain made, and it’s something you should at least be aware of in your algorithm.

## ► Optimize & Solve Technique #3: Simplify and Generalize

With Simplify and Generalize, we implement a multi-step approach. First, we simplify or tweak some constraint, such as the data type. Then, we solve this new simplified version of the problem. Finally, once we have an algorithm for the simplified problem, we try to adapt it for the more complex version.

Example: A ransom note can be formed by cutting words out of a magazine to form a new sentence. How would you figure out if a ransom note (represented as a string) can be formed from a given magazine (string)?

To simplify the problem, we can modify it so that we are cutting *characters* out of a magazine instead of whole words.

We can solve the simplified ransom note problem with characters by simply creating an array and counting the characters. Each spot in the array corresponds to one letter. First, we count the number of times each character in the ransom note appears, and then we go through the magazine to see if we have all of those characters.

When we generalize the algorithm, we do a very similar thing. This time, rather than creating an array with character counts, we create a hash table that maps from a word to its frequency.

## ► Optimize & Solve Technique #4: Base Case and Build

With Base Case and Build, we solve the problem first for a base case (e.g.,  $n = 1$ ) and then try to build up from there. When we get to more complex/interesting cases (often  $n = 3$  or  $n = 4$ ), we try to build those using the prior solutions.

Example: Design an algorithm to print all permutations of a string. For simplicity, assume all characters are unique.

Consider a test string abcdefg.

```
Case "a" --> {"a"}  
Case "ab" --> {"ab", "ba"}  
Case "abc" --> ?
```

This is the first "interesting" case. If we had the answer to  $P("ab")$ , how could we generate  $P("abc")$ ? Well, the additional letter is "c," so we can just stick c in at every possible point. That is:

```
 $P("abc") = \text{insert } "c" \text{ into all locations of all strings in } P("ab")$   
 $P("abc") = \text{insert } "c" \text{ into all locations of all strings in } \{"ab", "ba"\}$   
 $P("abc") = \text{merge}(\{"cab", "acb", "abc\}, \{"cba", "bca", "bac"\})$   
 $P("abc") = \{"cab", "acb", "abc", "cba", "bca", "bac"\}$ 
```

Now that we understand the pattern, we can develop a general recursive algorithm. We generate all permutations of a string  $s_1 \dots s_n$  by "chopping off" the last character and generating all permutations of  $s_1 \dots s_{n-1}$ . Once we have the list of all permutations of  $s_1 \dots s_{n-1}$ , we iterate through this list. For each string in it, we insert  $s_n$  into every location of the string.

Base Case and Build algorithms often lead to natural recursive algorithms.

### ► Optimize & Solve Technique #5: Data Structure Brainstorm

This approach is certainly hacky, but it often works. We can simply run through a list of data structures and try to apply each one. This approach is useful because solving a problem may be trivial once it occurs to us to use, say, a tree.

Example: Numbers are randomly generated and stored into an (expanding) array. How would you keep track of the median?

Our data structure brainstorm might look like the following:

- Linked list? Probably not. Linked lists tend not to do very well with accessing and sorting numbers.
- Array? Maybe, but you already have an array. Could you somehow keep the elements sorted? That's probably expensive. Let's hold off on this and return to it if it's needed.
- Binary tree? This is possible, since binary trees do fairly well with ordering. In fact, if the binary search tree is perfectly balanced, the top might be the median. But, be careful—if there's an even number of elements, the median is actually the average of the middle two elements. The middle two elements can't both be at the top. This is probably a workable algorithm, but let's come back to it.
- Heap? A heap is really good at basic ordering and keeping track of max and mins. This is actually interesting—if you had two heaps, you could keep track of the bigger half and the smaller half of the elements. The bigger half is kept in a min heap, such that the smallest element in the bigger half is at the root. The smaller half is kept in a max heap, such that the biggest element of the smaller half is at the root. Now, with these data structures, you have the potential median elements at the roots. If the heaps are no longer the same size, you can quickly "rebalance" the heaps by popping an element off the one heap and pushing it onto the other.

Note that the more problems you do, the more developed your instinct on which data structure to apply will be. You will also develop a more finely tuned instinct as to which of these approaches is the most useful.

### ► Best Conceivable Runtime (BCR)

Considering the best conceivable runtime can offer a useful hint for some problem.

The best conceivable runtime is, literally, the *best* runtime you could conceive of a solution to a problem having. You can easily prove that there is no way you could beat the BCR.

For example, suppose you want to compute the number of elements that two arrays (of length A and B) have in common. You immediately know that you can't do that in better than  $O(A + B)$  time because you have to "touch" each element in each array.  $O(A + B)$  is the BCR.

Or, suppose you want to print all pairs of values within an array. You know you can't do that in better than  $O(N^2)$  time because there are  $N^2$  pairs to print.

Be careful though! Suppose your interviewer asks you to find all pairs with sum k within an array (assuming all distinct elements). Some candidates who have not fully mastered the concept of BCR will say that the BCR is  $O(N^2)$  because you have to look at  $N^2$  pairs.

That's not true. Just because you want all pairs with a particular sum doesn't mean you have to look at *all* pairs. In fact, you don't.

What's the relationship between the Best Conceivable Runtime and Best Case Runtime? Nothing at all! The Best Conceivable Runtime is for a *problem* and is largely a function of the inputs and outputs. It has no particular connection to a specific algorithm. In fact, if you compute the Best Conceivable Runtime by thinking about what *your* algorithm does, you're probably doing something wrong. The Best Case Runtime is for a specific algorithm (and is a mostly useless value).

Note that the best conceivable runtime is not necessarily achievable. It says only that you can't do *better* than it.

### An Example of How to Use BCR

Question: Given two sorted arrays, find the number of elements in common. The arrays are the same length and each has all distinct elements.

Let's start with a good example. We'll underline the elements in common.

A:	13	27	<u>35</u>	<u>40</u>	49	<u>55</u>	59
B:	17	<u>35</u>	39	<u>40</u>	<u>55</u>	58	60

A brute force algorithm for this problem is to start with each element in A and search for it in B. This takes  $O(N^2)$  time since for each of N elements in A, we need to do an  $O(N)$  search in B.

The BCR is  $O(N)$ , because we know we will have to look at each element at least once and there are  $2N$  total elements. (If we skipped an element, then the value of that element could change the result. For example, if we never looked at the last value in B, then that 60 could be a 59.)

Let's think about where we are right now. We have an  $O(N^2)$  algorithm and we want to do better than that—potentially, but not necessarily, as fast as  $O(N)$ .

Brute Force:	$O(N^2)$
Optimal Algorithm:	?
BCR:	$O(N)$

What is between  $O(N^2)$  and  $O(N)$ ? Lots of things. Infinite things actually. We could theoretically have an algorithm that's  $O(N \log(\log(\log(\log(N))))$ ). However, both in interviews and in real life, that runtime doesn't come up a whole lot.

Try to remember this for your interview because it throws a lot of people off. Runtime is not a multiple choice question. Yes, it's very common to have a runtime that's  $O(\log N)$ ,  $O(N)$ ,  $O(N \log N)$ ,  $O(N^2)$  or  $O(2^N)$ . But you shouldn't assume that something has a particular runtime by sheer process of elimination. In fact, those times when you're confused about the runtime and so you want to take a guess—those are the times when you're most likely to have a non-obvious and less common runtime. Maybe the runtime is  $O(N^K)$ , where N is the size of the array and K is the number of pairs. Derive, don't guess.

Most likely, we're driving towards an  $O(N)$  algorithm or an  $O(N \log N)$  algorithm. What does that tell us?

If we imagine our current algorithm's runtime as  $O(N \times N)$ , then getting to  $O(N)$  or  $O(N \times \log N)$  might mean reducing that second  $O(N)$  in the equation to  $O(1)$  or  $O(\log N)$ .

This is one way that BCR can be useful. We can use the runtimes to get a "hint" for what we need to reduce.

That second  $O(N)$  comes from searching. The array is sorted. Can we search in a sorted array in faster than  $O(N)$  time?

Why, yes. We can use binary search to find an element in a sorted array in  $O(\log N)$  time.

We now have an improved algorithm:  $O(N \log N)$ .

Brute Force:	$O(N^2)$
Improved Algorithm:	$O(N \log N)$
Optimal Algorithm:	?
BCR:	$O(N)$

Can we do even better? Doing better likely means reducing that  $O(\log N)$  to  $O(1)$ .

In general, we cannot search an array—even a sorted array—in better than  $O(\log N)$  time. This is *not* the general case though. We're doing this search over and over again.

The BCR is telling us that we will never, ever have an algorithm that's faster than  $O(N)$ . Therefore, any work we do in  $O(N)$  time is a "freebie"—it won't impact our runtime.

Re-read the list of optimization tips on page 64. Is there anything that can help us?

One of the tips there suggests precomputing or doing upfront work. Any upfront work we do in  $O(N)$  time is a freebie. It won't impact our runtime.

This is another place where BCR can be useful. Any work you do that's less than or equal to the BCR is "free," in the sense that it won't impact your runtime. You might want to eliminate it eventually, but it's not a top priority just yet.

Our focus is still on reducing search from  $O(\log N)$  to  $O(1)$ . Any precomputation that's  $O(N)$  or less is "free."

In this case, we can just throw everything in B into a hash table. This will take  $O(N)$  time. Then, we just go through A and look up each element in the hash table. This look up (or search) is  $O(1)$ , so our runtime is  $O(N)$ .

Suppose our interviewer hits us with a question that makes us cringe: Can we do better?

No, not in terms of runtime. We have achieved the fastest possible runtime, therefore we cannot optimize the big O time. We could potentially optimize the space complexity.

This is another place where BCR is useful. It tells us that we're "done" in terms of optimizing the runtime, and we should therefore turn our efforts to the space complexity.

In fact, even without the interviewer prompting us, we should have a question mark with respect to our algorithm. We would have achieved the exact same runtime if the data wasn't sorted. So why did the interviewer give us sorted arrays? That's not unheard of, but it is a bit strange.

Let's turn back to our example.

A: 13 27 35 40 49 55 59  
B: 17 35 39 40 55 58 60

We're now looking for an algorithm that:

- Operates in  $O(1)$  space (probably). We already have an  $O(N)$  space algorithm with optimal runtime. If we want to use less additional space, that probably means no additional space. Therefore, we need to drop the hash table.

- Operates in  $O(N)$  time (probably). We'll probably want to at least match the current best runtime, and we know we can't beat it.
- Uses the fact that the arrays are sorted.

Our best algorithm that doesn't use extra space was the binary search one. Let's think about optimizing that. We can try walking through the algorithm.

1. Do a binary search in B for A[0] = 13. Not found.
2. Do a binary search in B for A[1] = 27. Not found.
3. Do a binary search in B for A[2] = 35. Found at B[1].
4. Do a binary search in B for A[3] = 40. Found at B[5].
5. Do a binary search in B for A[4] = 49. Not found.
6. ...

Think about BUD. The bottleneck is the searching. Is there anything unnecessary or duplicated?

It's unnecessary that A[3] = 40 searched over all of B. We know that we just found 35 at B[1], so 40 certainly won't be before 35.

Each binary search should start where the last one left off.

In fact, we don't need to do a binary search at all now. We can just do a linear search. As long as the linear search in B is just picking up where the last one left off, we know that we're going to be operating in linear time.

1. Do a linear search in B for A[0] = 13. Start at B[0] = 17. Stop at B[0] = 17. Not found.
2. Do a linear search in B for A[1] = 27. Start at B[0] = 17. Stop at B[1] = 35. Not found.
3. Do a linear search in B for A[2] = 35. Start at B[1] = 35. Stop at B[1] = 35. Found.
4. Do a linear search in B for A[3] = 40. Start at B[2] = 39. Stop at B[3] = 40. Found.
5. Do a linear search in B for A[4] = 49. Start at B[3] = 40. Stop at B[4] = 55. Found.
6. ...

This algorithm is very similar to merging two sorted arrays. It operates in  $O(N)$  time and  $O(1)$  space.

We have now reached the BCR and have minimal space. We know that we cannot do better.

**|| This is another way we can use BCR. If you ever reach the BCR and have  $O(1)$  additional space, then you know that you can't optimize the big O time or space.**

Best Conceivable Runtime is not a "real" algorithm concept, in that you won't find it in algorithm textbooks. But I have found it personally very useful, when solving problems myself, as well as while coaching people through problems.

If you're struggling to grasp it, make sure you understand big O time first (page 38). You need to master it. Once you do, figuring out the BCR of a problem should take literally seconds.

### ► Handling Incorrect Answers

One of the most pervasive—and dangerous—rumors is that candidates need to get every question right. That's not quite true.

First, responses to interview questions shouldn't be thought of as "correct" or "incorrect." When I evaluate how someone performed in an interview, I never think, "How many questions did they get right?" It's not a binary evaluation. Rather, it's about how optimal their final solution was, how long it took them to get there, how much help they needed, and how clean was their code. There is a range of factors.

Second, your performance is evaluated *in comparison to other candidates*. For example, if you solve a question optimally in 15 minutes, and someone else solves an easier question in five minutes, did that person do better than you? Maybe, but maybe not. If you are asked really easy questions, then you might be expected to get optimal solutions really quickly. But if the questions are hard, then a number of mistakes are expected.

Third, many—possibly most—questions are too difficult to expect even a strong candidate to immediately spit out the optimal algorithm. The questions I tend to ask would take strong candidates typically 20 to 30 minutes to solve.

In evaluating thousands of hiring packets at Google, I have only once seen a candidate have a "flawless" set of interviews. Everyone else, including the hundreds who got offers, made mistakes.

### ► When You've Heard a Question Before

If you've heard a question before, admit this to your interviewer. Your interviewer is asking you these questions in order to evaluate your problem-solving skills. If you already know the question, then you aren't giving them the opportunity to evaluate you.

Additionally, your interviewer may find it highly dishonest if you don't reveal that you know the question. (And, conversely, you'll get big honesty points if you do reveal this.)

### ► The "Perfect" Language for Interviews

At many of the top companies, interviewers aren't picky about languages. They're more interested in how well you solve the problems than whether you know a specific language.

Other companies though are more tied to a language and are interested in seeing how well you can code in a particular language.

If you're given a choice of languages, then you should probably pick whatever language you're most comfortable with.

That said, if you have several good languages, you should keep in mind the following.

#### **Prevalence**

It's not required, but it is ideal for your interviewer to know the language you're coding in. A more widely known language can be better for this reason.

#### **Language Readability**

Even if your interviewer doesn't know your programming language, they should hopefully be able to basically understand it. Some languages are more naturally readable than others, due to their similarity to other languages.

For example, Java is fairly easy for people to understand, even if they haven't worked in it. Most people have worked in something with Java-like syntax, such as C and C++.

However, languages such as Scala or Objective C have fairly different syntax.

### Potential Problems

Some languages just open you up to potential issues. For example, using C++ means that, in addition to all the usual bugs you can have in your code, you can have memory management and pointer issues.

### Verbosity

Some languages are more verbose than others. Java for example is a fairly verbose language as compared with Python. Just compare the following code snippets.

Python:

```
1 dict = {"left": 1, "right": 2, "top": 3, "bottom": 4};
```

Java:

```
1 HashMap<String, Integer> dict = new HashMap<String, Integer>().  
2 dict.put("left", 1);  
3 dict.put("right", 2);  
4 dict.put("top", 3);  
5 dict.put("bottom", 4);
```

However, some of the verbosity of Java can be reduced by abbreviating code. I could imagine a candidate on a whiteboard writing something like this:

```
1 HM<S, I> dict = new HM<S, I>().  
2 dict.put("left", 1);  
3 ...     "right", 2  
4 ...     "top", 3  
5 ...     "bottom", 4
```

The candidate would need to explain the abbreviations, but most interviewers wouldn't mind.

### Ease of Use

Some operations are easier in some languages than others. For example, in Python, you can very easily return multiple values from a function. In Java, the same action would require a new class. This can be handy for certain problems.

Similar to the above though, this can be mitigated by just abbreviating code or presuming methods that you don't actually have. For example, if one language provides a function to transpose a matrix and another language doesn't, this doesn't necessarily make the first language much better to code in (for a problem that needs such a function). You could just assume that the other language has a similar method.

## ► What Good Coding Looks Like

You probably know by now that employers want to see that you write "good, clean" code. But what does this really mean, and how is this demonstrated in an interview?

Broadly speaking, good code has the following properties:

- **Correct:** The code should operate correctly on all expected and unexpected inputs.
- **Efficient:** The code should operate as efficiently as possible in terms of both time and space. This "efficiency" includes both the asymptotic (big O) efficiency and the practical, real-life efficiency. That is, a

constant factor might get dropped when you compute the big O time, but in real life, it can very much matter.

- **Simple:** If you can do something in 10 lines instead of 100, you should. Code should be as quick as possible for a developer to write.
- **Readable:** A different developer should be able to read your code and understand what it does and how it does it. Readable code has comments where necessary, but it implements things in an easily understandable way. That means that your fancy code that does a bunch of complex bit shifting is not necessarily *good* code.
- **Maintainable:** Code should be reasonably adaptable to changes during the life cycle of a product and should be easy to maintain by other developers, as well as the initial developer.

Striving for these aspects requires a balancing act. For example, it's often advisable to sacrifice some degree of efficiency to make code more maintainable, and vice versa.

You should think about these elements as you code during an interview. The following aspects of code are more specific ways to demonstrate the earlier list.

### Use Data Structures Generously

Suppose you were asked to write a function to add two simple mathematical expressions which are of the form  $Ax^a + Bx^b + \dots$  (where the coefficients and exponents can be any positive or negative real number). That is, the expression is a sequence of terms, where each term is simply a constant times an exponent. The interviewer also adds that she doesn't want you to have to do string parsing, so you can use whatever data structure you'd like to hold the expressions.

There are a number of different ways you can implement this.

#### *Bad Implementation*

A bad implementation would be to store the expression as a single array of doubles, where the  $k$ th element corresponds to the coefficient of the  $x^k$  term in the expression. This structure is problematic because it could not support expressions with negative or non-integer exponents. It would also require an array of 1000 elements to store just the expression  $x^{100}$ .

```
1 int[] sum(double[] expr1, double[] expr2) {  
2     ...  
3 }
```

#### *Less Bad Implementation*

A slightly less bad implementation would be to store the expression as a set of two arrays, `coefficients` and `exponents`. Under this approach, the terms of the expression are stored in any order, but "matched" such that the  $i$ th term of the expression is represented by `coefficients[i] * xexponents[i]`.

Under this implementation, if `coefficients[p] = k` and `exponents[p] = m`, then the  $p$ th term is  $kx^m$ . Although this doesn't have the same limitations as the earlier solution, it's still very messy. You need to keep track of two arrays for just one expression. Expressions could have "undefined" values if the arrays were of different lengths. And returning an expression is annoying because you need to return two arrays.

```
1 ??? sum(double[] coeffs1, double[] expon1, double[] coeffs2, double[] expon2) {  
2     ...  
3 }
```

### *Good Implementation*

A good implementation for this problem is to design your own data structure for the expression.

```

1  class ExprTerm {
2      double coefficient;
3      double exponent;
4  }
5
6  ExprTerm[] sum(ExprTerm[] expr1, ExprTerm[] expr2) {
7      ...
8 }
```

Some might (and have) argued that this is “over-optimizing.” Perhaps so, perhaps not. Regardless of whether you think it’s over-optimizing, the above code demonstrates that you think about how to design your code and don’t just slop something together in the fastest way possible.

### **Appropriate Code Reuse**

Suppose you were asked to write a function to check if the value of a binary number (passed as a string) equals the hexadecimal representation of a string.

An elegant implementation of this problem leverages code reuse.

```

1  boolean compareBinToHex(String binary, String hex) {
2      int n1 = convertFromBase(binary, 2);
3      int n2 = convertFromBase(hex, 16);
4      if (n1 < 0 || n2 < 0) {
5          return false;
6      }
7      return n1 == n2;
8  }
9
10 int convertFromBase(String number, int base) {
11     if (base < 2 || (base > 10 && base != 16)) return -1;
12     int value = 0;
13     for (int i = number.length() - 1; i >= 0; i--) {
14         int digit = digitToValue(number.charAt(i));
15         if (digit < 0 || digit >= base) {
16             return -1;
17         }
18         int exp = number.length() - 1 - i;
19         value += digit * Math.pow(base, exp);
20     }
21     return value;
22 }
23
24 int digitToValue(char c) { ... }
```

We could have implemented separate code to convert a binary number and a hexadecimal code, but this just makes our code harder to write and harder to maintain. Instead, we reuse code by writing one `convertFromBase` method and one `digitToValue` method.

### **Modular**

Writing modular code means separating isolated chunks of code out into their own methods. This helps keep the code more maintainable, readable, and testable.

Imagine you are writing code to swap the minimum and maximum element in an integer array. You could implement it all in one method like this:

```
1 void swapMinMax(int[] array) {  
2     int minIndex = 0;  
3     for (int i = 1; i < array.length; i++) {  
4         if (array[i] < array[minIndex]) {  
5             minIndex = i;  
6         }  
7     }  
8  
9     int maxIndex = 0;  
10    for (int i = 1; i < array.length; i++) {  
11        if (array[i] > array[maxIndex]) {  
12            maxIndex = i;  
13        }  
14    }  
15  
16    int temp = array[minIndex];  
17    array[minIndex] = array[maxIndex];  
18    array[maxIndex] = temp;  
19 }
```

Or, you could implement in a more modular way by separating the relatively isolated chunks of code into their own methods.

```
1 void swapMinMaxBetter(int[] array) {  
2     int minIndex = getMinIndex(array);  
3     int maxIndex = getMaxIndex(array);  
4     swap(array, minIndex, maxIndex);  
5 }  
6  
7 int getMinIndex(int[] array) { ... }  
8 int getMaxIndex(int[] array) { ... }  
9 void swap(int[] array, int m, int n) { ... }
```

While the non-modular code isn't particularly awful, the nice thing about the modular code is that it's easily testable because each component can be verified separately. As code gets more complex, it becomes increasingly important to write it in a modular way. This will make it easier to read and maintain. Your interviewer wants to see you demonstrate these skills in your interview.

### Flexible and Robust

Just because your interviewer only asks you to write code to check if a normal tic-tac-toe board has a winner, doesn't mean you *must* assume that it's a 3x3 board. Why not write the code in a more general way that implements it for an NxN board?

Writing flexible, general-purpose code may also mean using variables instead of hard-coded values or using templates / generics to solve a problem. If we can write our code to solve a more general problem, we should.

Of course, there is a limit. If the solution is much more complex for the general case, and it seems unnecessary at this point in time, it may be better just to implement the simple, expected case.

### Error Checking

One sign of a careful coder is that she doesn't make assumptions about the input. Instead, she validates that the input is what it should be, either through ASSERT statements or if-statements.

For example, recall the earlier code to convert a number from its base  $i$  (e.g., base 2 or base 16) representation to an `int`.

```
1 int convertToBase(String number, int base) {  
2     if (base < 2 || (base > 10 && base != 16)) return -1;  
3     int value = 0;  
4     for (int i = number.length() - 1; i >= 0; i--) {  
5         int digit = digitToValue(number.charAt(i));  
6         if (digit < 0 || digit >= base) {  
7             return -1;  
8         }  
9         int exp = number.length() - 1 - i;  
10        value += digit * Math.pow(base, exp);  
11    }  
12    return value;  
13 }
```

In line 2, we check to see that `base` is valid (we assume that bases greater than 10, other than base 16, have no standard representation in string form). In line 6, we do another error check: making sure that each digit falls within the allowable range.

Checks like these are critical in production code and, therefore, in interview code as well.

Of course, writing these error checks can be tedious and can waste precious time in an interview. The important thing is to point out that you *would* write the checks. If the error checks are much more than a quick if-statement, it may be best to leave some space where the error checks would go and indicate to your interviewer that you'll fill them in when you're finished with the rest of the code.

## ► Don't Give Up!

I know interview questions can be overwhelming, but that's part of what the interviewer is testing. Do you rise to a challenge, or do you shrink back in fear? It's important that you step up and eagerly meet a tricky problem head-on. After all, remember that interviews are supposed to be hard. It shouldn't be a surprise when you get a really tough problem.

For extra "points," show excitement about solving hard problems.

# VIII

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## The Offer and Beyond

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Just when you thought you could sit back and relax after your interviews, now you're faced with the post-interview stress: Should you accept the offer? Is it the right one? How do you decline an offer? What about deadlines? We'll handle a few of these issues here and go into more details about how to evaluate an offer, and how to negotiate it.

### ► Handling Offers and Rejection

Whether you're accepting an offer, declining an offer, or responding to a rejection, it matters what you do.

#### Offer Deadlines and Extensions

When companies extend an offer, there's almost always a deadline attached to it. Usually these deadlines are one to four weeks out. If you're still waiting to hear back from other companies, you can ask for an extension. Companies will usually try to accommodate this, if possible.

#### Declining an Offer

Even if you aren't interested in working for this company right now, you might be interested in working for it in a few years. (Or, your contacts might one day move to a more exciting company.) It's in your best interest to decline the offer on good terms and keep a line of communication open.

When you decline an offer, provide a reason that is non-offensive and inarguable. For example, if you were declining a big company for a startup, you could explain that you feel a startup is the right choice for you at this time. The big company can't suddenly "become" a startup, so they can't argue about your reasoning.

#### Handling Rejection

Getting rejected is unfortunate, but it doesn't mean that you're not a great engineer. Lots of great engineers do poorly, either because they don't "test well" on these sort of interviewers, or they just had an "off" day.

Fortunately, most companies understand that these interviews aren't perfect and many good engineers get rejected. For this reason, companies are often eager to re-interview previously rejected candidate. Some companies will even reach out to old candidates or expedite their application *because* of their prior performance.

When you do get the unfortunate call, use this as an opportunity to build a bridge to re-apply. Thank your recruiter for his time, explain that you're disappointed but that you understand their position, and ask when you can reapply to the company.

You can also ask for feedback from the recruiter. In most cases, the big tech companies won't offer feedback, but there are some companies that will. It doesn't hurt to ask a question like, "Is there anything you'd suggest I work on for next time?"

## ► Evaluating the Offer

Congratulations! You got an offer! And—if you're lucky—you may have even gotten multiple offers. Your recruiter's job is now to do everything he can to encourage you to accept it. How do you know if the company is the right fit for you? We'll go through a few things you should consider in evaluating an offer.

### The Financial Package

Perhaps the biggest mistake that candidates make in evaluating an offer is looking too much at their salary. Candidates often look so much at this one number that they wind up accepting the offer that is *worse* financially. Salary is just one part of your financial compensation. You should also look at:

- *Signing Bonus, Relocation, and Other One Time Perks:* Many companies offer a signing bonus and/or relocation. When comparing offers, it's wise to amortize this cash over three years (or however long you expect to stay).
- *Cost of Living Difference:* Taxes and other cost of living differences can make a big difference in your take-home pay. Silicon Valley, for example, is 30+% more expensive than Seattle.
- *Annual Bonus:* Annual bonuses at tech companies can range from anywhere from 3% to 30%. Your recruiter might reveal the average annual bonus, but if not, check with friends at the company.
- *Stock Options and Grants:* Equity compensation can form another big part of your annual compensation. Like signing bonuses, stock compensation between companies can be compared by amortizing it over three years and then lumping that value into salary.

Remember, though, that what you learn and how a company advances your career often makes far more of a difference to your long term finances than the salary. Think very carefully about how much emphasis you really want to put on money right now.

### Career Development

As thrilled as you may be to receive this offer, odds are, in a few years, you'll start thinking about interviewing again. Therefore, it's important that you think right now about how this offer would impact your career path. This means considering the following questions:

- How good does the company's name look on my resume?
- How much will I learn? Will I learn relevant things?
- What is the promotion plan? How do the careers of developers progress?
- If I want to move into management, does this company offer a realistic plan?
- Is the company or team growing?
- If I do want to leave the company, is it situated near other companies I'm interested in, or will I need to move?

The final point is extremely important and usually overlooked. If you only have a few other companies to pick from in your city, your career options will be more restricted. Fewer options means that you're less likely to discover really great opportunities.

### Company Stability

All else being equal, of course stability is a good thing. No one wants to be fired or laid off.

However, all else isn't actually equal. The more stable companies are also often growing more slowly.

How much emphasis you should put on company stability really depends on you and your values. For some candidates, stability should not be a large factor. Can you fairly quickly find a new job? If so, it might be better to take the rapidly growing company, even if it's unstable? If you have work visa restrictions or just aren't confident in your ability to find something new, stability might be more important.

### The Happiness Factor

Last but not least, you should of course consider how happy you will be. Any of the following factors may impact that:

- *The Product:* Many people look heavily at what product they are building, and of course this matters a bit. However, for most engineers, there are more important factors, such as who you work with.
- *Manager and Teammates:* When people say that they love, or hate, their job, it's often because of their teammates and their manager. Have you met them? Did you enjoy talking with them?
- *Company Culture:* Culture is tied to everything from how decisions get made, to the social atmosphere, to how the company is organized. Ask your future teammates how they would describe the culture.
- *Hours:* Ask future teammates about how long they typically work, and figure out if that meshes with your lifestyle. Remember, though, that hours before major deadlines are typically much longer.

Additionally, note that if you are given the opportunity to switch teams easily (like you are at Google and Facebook), you'll have an opportunity to find a team and product that matches you well.

## ► Negotiation

Years ago, I signed up for a negotiations class. On the first day, the instructor asked us to imagine a scenario where we wanted to buy a car. Dealership A sells the car for a fixed \$20,000—no negotiating. Dealership B allows us to negotiate. How much would the car have to be (after negotiating) for us to go to Dealership B? (Quick! Answer this for yourself!)

On average, the class said that the car would have to be \$750 cheaper. In other words, students were willing to pay \$750 just to avoid having to negotiate for an hour or so. Not surprisingly, in a class poll, most of these students also said they didn't negotiate their job offer. They just accepted whatever the company gave them.

Many of us can probably sympathize with this position. Negotiation isn't fun for most of us. But still, the financial benefits of negotiation are usually worth it.

Do yourself a favor. Negotiate. Here are some tips to get you started.

1. *Just Do It.* Yes, I know it's scary; (almost) no one likes negotiating. But it's so, so worth it. Recruiters will not revoke an offer because you negotiated, so you have little to lose. This is especially true if the offer is from a larger company. You probably won't be negotiating with your future teammates.
2. *Have a Viable Alternative.* Fundamentally, recruiters negotiate with you because they're concerned you may not join the company otherwise. If you have alternative options, that will make their concern much more real.
3. *Have a Specific "Ask":* It's more effective to ask for an additional \$7000 in salary than to just ask for "more."

After all, if you just ask for more, the recruiter could throw in another \$1000 and technically have satisfied your wishes.

4. **Overshoot:** In negotiations, people usually don't agree to whatever you demand. It's a back and forth conversation. Ask for a bit more than you're really hoping to get, since the company will probably meet you in the middle.
5. **Think Beyond Salary:** Companies are often more willing to negotiate on non-salary components, since boosting your salary too much could mean that they're paying you more than your peers. Consider asking for more equity or a bigger signing bonus. Alternatively, you may be able to ask for your relocation benefits in cash, instead of having the company pay directly for the moving fees. This is a great avenue for many college students, whose actual moving expenses are fairly cheap.
6. **Use Your Best Medium:** Many people will advise you to only negotiate over the phone. To a certain extent, they're right; it is better to negotiate over the phone. However, if you don't feel comfortable on a phone negotiation, do it via email. It's more important that you attempt to negotiate than that you do it via a specific medium.

Additionally, if you're negotiating with a big company, you should know that they often have "levels" for employees, where all employees at a particular level are paid around the same amount. Microsoft has a particularly well-defined system for this. You can negotiate within the salary range for your level, but going beyond that requires bumping up a level. If you're looking for a big bump, you'll need to convince the recruiter and your future team that your experience matches this higher level—a difficult, but feasible, thing to do.

## ► On the Job

Navigating your career path doesn't end at the interview. In fact, it's just getting started. Once you actually join a company, you need to start thinking about your career path. Where will you go from here, and how will you get there?

### Set a Timeline

It's a common story: you join a company, and you're psyched. Everything is great. Five years later, you're still there. And it's then that you realize that these last three years didn't add much to your skill set or to your resume. Why didn't you just leave after two years?

When you're enjoying your job, it's very easy to get wrapped up in it and not realize that your career is not advancing. This is why you should outline your career path before starting a new job. Where do you want to be in ten years? And what are the steps necessary to get there? In addition, each year, think about what the next year of experience will bring you and how your career or your skill set advanced in the last year.

By outlining your path in advance and checking in on it regularly, you can avoid falling into this complacency trap.

### Build Strong Relationships

When you want to move on to something new, your network will be critical. After all, applying online is tricky; a personal referral is much better, and your ability to do so hinges on your network.

At work, establish strong relationships with your manager and teammates. When employees leave, keep in touch with them. Just a friendly note a few weeks after their departure will help to bridge that connection from a work acquaintance to a personal acquaintance.

This same approach applies to your personal life. Your friends, and your friends of friends, are valuable connections. Be open to helping others, and they'll be more likely to help you.

### **Ask for What You Want**

While some managers may really try to grow your career, others will take a more hands-off approach. It's up to you to pursue the challenges that are right for your career.

Be (reasonably) frank about your goals with your manager. If you want to take on more back-end coding projects, say so. If you'd like to explore more leadership opportunities, discuss how you might be able to do so.

You need to be your best advocate, so that you can achieve goals according to your timeline.

### **Keep Interviewing**

Set a goal of interviewing at least once a year, even if you aren't actively looking for a new job. This will keep your interview skills fresh, and also keep you in tune with what sorts of opportunities (and salaries) are out there.

If you get an offer, you don't have to take it. It will still build a connection with that company in case you want to join at a later date.

# Interview Questions

**IX**

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# 1

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## Arrays and Strings

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**H**opefully, all readers of this book are familiar with arrays and strings, so we won't bore you with such details. Instead, we'll focus on some of the more common techniques and issues with these data structures.

Please note that array questions and string questions are often interchangeable. That is, a question that this book states using an array may be asked instead as a string question, and vice versa.

### ► Hash Tables

A hash table is a data structure that maps keys to values for highly efficient lookup. There are a number of ways of implementing this. Here, we will describe a simple but common implementation.

In this simple implementation, we use an array of linked lists and a hash code function. To insert a key (which might be a string or essentially any other data type) and value, we do the following:

1. First, compute the key's hash code, which will usually be an `int` or `long`. Note that two different keys could have the same hash code, as there may be an infinite number of keys and a finite number of ints.
2. Then, map the hash code to an index in the array. This could be done with something like `hash(key) % array_length`. Two different hash codes could, of course, map to the same index.
3. At this index, there is a linked list of keys and values. Store the key and value in this index. We must use a linked list because of collisions: you could have two different keys with the same hash code, or two different hash codes that map to the same index.

To retrieve the value pair by its key, you repeat this process. Compute the hash code from the key, and then compute the index from the hash code. Then, search through the linked list for the value with this key.

If the number of collisions is very high, the worst case runtime is  $O(N)$ , where  $N$  is the number of keys. However, we generally assume a good implementation that keeps collisions to a minimum, in which case the lookup time is  $O(1)$ .



Alternatively, we can implement the hash table with a balanced binary search tree. This gives us an  $O(\log N)$  lookup time. The advantage of this is potentially using less space, since we no longer allocate a large array. We can also iterate through the keys in order, which can be useful sometimes.

## ► ArrayList & Resizable Arrays

In some languages, arrays (often called lists in this case) are automatically resizable. The array or list will grow as you append items. In other languages, like Java, arrays are fixed length. The size is defined when you create the array.

When you need an array-like data structure that offers dynamic resizing, you would usually use an `ArrayList`. An `ArrayList` is an array that resizes itself as needed while still providing  $O(1)$  access. A typical implementation is that when the array is full, the array doubles in size. Each doubling takes  $O(n)$  time, but happens so rarely that its amortized insertion time is still  $O(1)$ .

```
1  ArrayList<String> merge(String[] words, String[] more) {
2      ArrayList<String> sentence = new ArrayList<String>();
3      for (String w : words) sentence.add(w);
4      for (String w : more) sentence.add(w);
5      return sentence;
6  }
```

This is an essential data structure for interviews. Be sure you are comfortable with dynamically resizable arrays/lists in whatever language you will be working with. Note that the name of the data structure as well as the “resizing factor” (which is 2 in Java) can vary.

*Why is the amortized insertion runtime  $O(1)$ ?*

Suppose you have an array of size  $N$ . We can work backwards to compute how many elements we copied at each capacity increase. Observe that when we increase the array to  $K$  elements, the array was previously half that size. Therefore, we needed to copy  $\frac{K}{2}$  elements.

```
final capacity increase    : n/2 elements to copy
previous capacity increase: n/4 elements to copy
previous capacity increase: n/8 elements to copy
previous capacity increase: n/16 elements to copy
...
second capacity increase  : 2 elements to copy
first capacity increase   : 1 element to copy
```

Therefore, the total number of copies to insert  $N$  elements is roughly  $\frac{N}{2} + \frac{N}{4} + \frac{N}{8} + \dots + 2 + 1$ , which is just less than  $N$ .

If the sum of this series isn't obvious to you, imagine this: Suppose you have a kilometer-long walk to the store. You walk 0.5 kilometers, and then 0.25 kilometers, and then 0.125 kilometers, and so on. You will never exceed one kilometer (although you'll get very close to it).

Therefore, inserting  $N$  elements takes  $O(N)$  work total. Each insertion is  $O(1)$  on average, even though some insertions take  $O(N)$  time in the worst case.

## ► StringBuilder

Imagine you were concatenating a list of strings, as shown below. What would the running time of this code be? For simplicity, assume that the strings are all the same length (call this  $x$ ) and that there are  $n$  strings.

```
1 String joinWords(String[] words) {  
2     String sentence = "";  
3     for (String w : words) {  
4         sentence = sentence + w;  
5     }  
6     return sentence;  
7 }
```

On each concatenation, a new copy of the string is created, and the two strings are copied over, character by character. The first iteration requires us to copy  $x$  characters. The second iteration requires copying  $2x$  characters. The third iteration requires  $3x$ , and so on. The total time therefore is  $O(x + 2x + \dots + nx)$ . This reduces to  $O(xn^2)$ .

Why is it  $O(xn^2)$ ? Because  $1 + 2 + \dots + n$  equals  $n(n+1)/2$ , or  $O(n^2)$ .

`StringBuilder` can help you avoid this problem. `StringBuilder` simply creates a resizable array of all the strings, copying them back to a string only when necessary.

```
1 String joinWords(String[] words) {  
2     StringBuilder sentence = new StringBuilder();  
3     for (String w : words) {  
4         sentence.append(w);  
5     }  
6     return sentence.toString();  
7 }
```

A good exercise to practice strings, arrays, and general data structures is to implement your own version of `StringBuilder`, `HashTable` and `ArrayList`.

**Additional Reading:** Hash Table Collision Resolution (pg 636), Rabin-Karp Substring Search (pg 636).

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### Interview Questions

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- 1.1 Is Unique:** Implement an algorithm to determine if a string has all unique characters. What if you cannot use additional data structures?

Hints: #44, #117, #132

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- 1.2 Check Permutation:** Given two strings, write a method to decide if one is a permutation of the other.

Hints: #1, #84, #122, #131

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- 1.3 URLify:** Write a method to replace all spaces in a string with '%20'. You may assume that the string has sufficient space at the end to hold the additional characters, and that you are given the "true" length of the string. (Note: If implementing in Java, please use a character array so that you can perform this operation in place.)

EXAMPLE

Input: "Mr John Smith ", 13

Output: "Mr%20John%20Smith"

Hints: #53, #118

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- 1.4 Palindrome Permutation:** Given a string, write a function to check if it is a permutation of a palindrome. A palindrome is a word or phrase that is the same forwards and backwards. A permutation is a rearrangement of letters. The palindrome does not need to be limited to just dictionary words.

EXAMPLE

Input: Tact Coa

Output: True (permutations: "taco cat", "atco cta", etc.)

Hints: #106, #121, #134, #136

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- 1.5 One Away:** There are three types of edits that can be performed on strings: insert a character, remove a character, or replace a character. Given two strings, write a function to check if they are one edit (or zero edits) away.

EXAMPLE

pale, ple -> true

pales, pale -> true

pale, bale -> true

pale, bake -> false

Hints: #23, #97, #130

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- 1.6 String Compression:** Implement a method to perform basic string compression using the counts of repeated characters. For example, the string abccccccaa would become a2b1c5a3. If the "compressed" string would not become smaller than the original string, your method should return the original string. You can assume the string has only uppercase and lowercase letters (a - z).

Hints: #92, #110

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- 1.7 Rotate Matrix:** Given an image represented by an NxN matrix, where each pixel in the image is 4 bytes, write a method to rotate the image by 90 degrees. Can you do this in place?

Hints: #51, #100

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- 1.8 Zero Matrix:** Write an algorithm such that if an element in an MxN matrix is 0, its entire row and column are set to 0.

Hints: #17, #74, #102

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- 1.9 String Rotation:** Assume you have a method `isSubstring` which checks if one word is a substring of another. Given two strings, `s1` and `s2`, write code to check if `s2` is a rotation of `s1` using only one call to `isSubstring` (e.g., "waterbottle" is a rotation of "erbottlewat").

Hints: #34, #88, #104

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Additional Questions: Object-Oriented Design (#7.12), Recursion (#8.3), Sorting and Searching (#10.9), C++ (#12.11), Moderate Problems (#16.8, #16.17, #16.22), Hard Problems (#17.4, #17.7, #17.13, #17.22, #17.26).

Hints start on page 653.

# 2

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## Linked Lists

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A linked list is a data structure that represents a sequence of nodes. In a singly linked list, each node points to the next node in the linked list. A doubly linked list gives each node pointers to both the next node and the previous node.

The following diagram depicts a doubly linked list:



Unlike an array, a linked list does not provide constant time access to a particular “index” within the list. This means that if you’d like to find the Kth element in the list, you will need to iterate through K elements.

The benefit of a linked list is that you can add and remove items from the beginning of the list in constant time. For specific applications, this can be useful.

### ► Creating a Linked List

The code below implements a very basic singly linked list.

```
1  class Node {  
2      Node next = null;  
3      int data;  
4  
5      public Node(int d) {  
6          data = d;  
7      }  
8  
9      void appendToTail(int d) {  
10         Node end = new Node(d);  
11         Node n = this;  
12         while (n.next != null) {  
13             n = n.next;  
14         }  
15         n.next = end;  
16     }  
17 }
```

In this implementation, we don’t have a `LinkedList` data structure. We access the linked list through a reference to the head `Node` of the linked list. When you implement the linked list this way, you need to be a bit careful. What if multiple objects need a reference to the linked list, and then the head of the linked list changes? Some objects might still be pointing to the old head.

We could, if we chose, implement a `LinkedList` class that wraps the `Node` class. This would essentially just have a single member variable: the head `Node`. This would largely resolve the earlier issue.

Remember that when you're discussing a linked list in an interview, you must understand whether it is a singly linked list or a doubly linked list.

### ► Deleting a Node from a Singly Linked List

Deleting a node from a linked list is fairly straightforward. Given a node `n`, we find the previous node `prev` and set `prev.next` equal to `n.next`. If the list is doubly linked, we must also update `n.next` to set `n.next.prev` equal to `n.prev`. The important things to remember are (1) to check for the null pointer and (2) to update the head or tail pointer as necessary.

Additionally, if you implement this code in C, C++ or another language that requires the developer to do memory management, you should consider if the removed node should be deallocated.

```
1  Node deleteNode(Node head, int d) {  
2      Node n = head;  
3  
4      if (n.data == d) {  
5          return head.next; /* moved head */  
6      }  
7  
8      while (n.next != null) {  
9          if (n.next.data == d) {  
10              n.next = n.next.next;  
11              return head; /* head didn't change */  
12          }  
13          n = n.next;  
14      }  
15      return head;  
16 }
```

### ► The “Runner” Technique

The “runner” (or second pointer) technique is used in many linked list problems. The runner technique means that you iterate through the linked list with two pointers simultaneously, with one ahead of the other. The “fast” node might be ahead by a fixed amount, or it might be hopping multiple nodes for each one node that the “slow” node iterates through.

For example, suppose you had a linked list  $a_1 \rightarrow a_2 \rightarrow \dots \rightarrow a_n \rightarrow b_1 \rightarrow b_2 \rightarrow \dots \rightarrow b_n$  and you wanted to rearrange it into  $a_1 \rightarrow b_1 \rightarrow a_2 \rightarrow b_2 \rightarrow \dots \rightarrow a_n \rightarrow b_n$ . You do not know the length of the linked list (but you do know that the length is an even number).

You could have one pointer `p1` (the fast pointer) move every two elements for every one move that `p2` makes. When `p1` hits the end of the linked list, `p2` will be at the midpoint. Then, move `p1` back to the front and begin “weaving” the elements. On each iteration, `p2` selects an element and inserts it after `p1`.

### ► Recursive Problems

A number of linked list problems rely on recursion. If you're having trouble solving a linked list problem, you should explore if a recursive approach will work. We won't go into depth on recursion here, since a later chapter is devoted to it.

However, you should remember that recursive algorithms take at least  $O(n)$  space, where  $n$  is the depth of the recursive call. All recursive algorithms *can* be implemented iteratively, although they may be much more complex.

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### Interview Questions

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- 2.1 Remove Dups:** Write code to remove duplicates from an unsorted linked list.

FOLLOW UP

How would you solve this problem if a temporary buffer is not allowed?

Hints: #9, #40

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- 2.2 Return Kth to Last:** Implement an algorithm to find the  $k$ th to last element of a singly linked list.

Hints: #8, #25, #41, #67, #126

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- 2.3 Delete Middle Node:** Implement an algorithm to delete a node in the middle (i.e., any node but the first and last node, not necessarily the exact middle) of a singly linked list, given only access to that node.

EXAMPLE

Input: the node  $c$  from the linked list  $a \rightarrow b \rightarrow c \rightarrow d \rightarrow e \rightarrow f$

Result: nothing is returned, but the new linked list looks like  $a \rightarrow b \rightarrow d \rightarrow e \rightarrow f$

Hints: #72

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- 2.4 Partition:** Write code to partition a linked list around a value  $x$ , such that all nodes less than  $x$  come before all nodes greater than or equal to  $x$ . If  $x$  is contained within the list, the values of  $x$  only need to be after the elements less than  $x$  (see below). The partition element  $x$  can appear anywhere in the “right partition”; it does not need to appear between the left and right partitions.

EXAMPLE

Input:     $3 \rightarrow 5 \rightarrow 8 \rightarrow 5 \rightarrow 10 \rightarrow 2 \rightarrow 1$  [partition = 5]

Output:    $3 \rightarrow 1 \rightarrow 2 \rightarrow 10 \rightarrow 5 \rightarrow 5 \rightarrow 8$

Hints: #3, #24

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- 2.5 Sum Lists:** You have two numbers represented by a linked list, where each node contains a single digit. The digits are stored in *reverse* order, such that the 1's digit is at the head of the list. Write a function that adds the two numbers and returns the sum as a linked list.

EXAMPLE

Input:  $(7 \rightarrow 1 \rightarrow 6) + (5 \rightarrow 9 \rightarrow 2)$ . That is, 617 + 295.

Output:  $2 \rightarrow 1 \rightarrow 9$ . That is, 912.

FOLLOW UP

Suppose the digits are stored in forward order. Repeat the above problem.

EXAMPLE

Input:  $(6 \rightarrow 1 \rightarrow 7) + (2 \rightarrow 9 \rightarrow 5)$ . That is, 617 + 295.

Output:  $9 \rightarrow 1 \rightarrow 2$ . That is, 912.

Hints: #7, #30, #71, #95, #109

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- 2.6 Palindrome:** Implement a function to check if a linked list is a palindrome.

Hints: #5, #13, #29, #61, #101

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- 2.7 Intersection:** Given two (singly) linked lists, determine if the two lists intersect. Return the intersecting node. Note that the intersection is defined based on reference, not value. That is, if the  $k$ th node of the first linked list is the exact same node (by reference) as the  $j$ th node of the second linked list, then they are intersecting.

Hints: #20, #45, #55, #65, #76, #93, #111, #120, #129

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- 2.8 Loop Detection:** Given a circular linked list, implement an algorithm that returns the node at the beginning of the loop.

DEFINITION

Circular linked list: A (corrupt) linked list in which a node's next pointer points to an earlier node, so as to make a loop in the linked list.

EXAMPLE

Input: A  $\rightarrow$  B  $\rightarrow$  C  $\rightarrow$  D  $\rightarrow$  E  $\rightarrow$  C [the same C as earlier]

Output: C

Hints: #50, #69, #83, #90

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Additional Questions: Trees and Graphs (#4.3), Object-Oriented Design (#7.12), System Design and Scalability (#9.5), Moderate Problems (#16.25), Hard Problems (#17.12).

Hints start on page 653.

# 3

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## Stacks and Queues

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Questions on stacks and queues will be much easier to handle if you are comfortable with the ins and outs of the data structure. The problems can be quite tricky, though. While some problems may be slight modifications on the original data structure, others have much more complex challenges.

### ► Implementing a Stack

The stack data structure is precisely what it sounds like: a stack of data. In certain types of problems, it can be favorable to store data in a stack rather than in an array.

A stack uses LIFO (last-in first-out) ordering. That is, as in a stack of dinner plates, the most recent item added to the stack is the first item to be removed.

It uses the following operations:

- `pop()`: Remove the top item from the stack.
- `push(item)`: Add an item to the top of the stack.
- `peek()`: Return the top of the stack.
- `isEmpty()`: Return true if and only if the stack is empty.

Unlike an array, a stack does not offer constant-time access to the  $i$ th item. However, it does allow constant-time adds and removes, as it doesn't require shifting elements around.

We have provided simple sample code to implement a stack. Note that a stack can also be implemented using a linked list, if items were added and removed from the same side.

```
1  public class MyStack<T> {  
2      private static class StackNode<T> {  
3          private T data;  
4          private StackNode<T> next;  
5  
6          public StackNode(T data) {  
7              this.data = data;  
8          }  
9      }  
10     private StackNode<T> top;  
11  
12     public T pop() {  
13         if (top == null) throw new EmptyStackException();  
14         T item = top.data;  
15     }
```

```

16     top = top.next;
17     return item;
18 }
19
20 public void push(T item) {
21     StackNode<T> t = new StackNode<T>(item);
22     t.next = top;
23     top = t;
24 }
25
26 public T peek() {
27     if (top == null) throw new EmptyStackException();
28     return top.data;
29 }
30
31 public boolean isEmpty() {
32     return top == null;
33 }
34 }

```

One case where stacks are often useful is in certain recursive algorithms. Sometimes you need to push temporary data onto a stack as you recurse, but then remove them as you backtrack (for example, because the recursive check failed). A stack offers an intuitive way to do this.

A stack can also be used to implement a recursive algorithm iteratively. (This is a good exercise! Take a simple recursive algorithm and implement it iteratively.)

## ► Implementing a Queue

A queue implements FIFO (first-in first-out) ordering. As in a line or queue at a ticket stand, items are removed from the data structure in the same order that they are added.

It uses the operations:

- `add(item)`: Add an item to the end of the list.
- `remove()`: Remove the first item in the list.
- `peek()`: Return the top of the queue.
- `isEmpty()`: Return true if and only if the queue is empty.

A queue can also be implemented with a linked list. In fact, they are essentially the same thing, as long as items are added and removed from opposite sides.

```

1  public class MyQueue<T> {
2      private static class QueueNode<T> {
3          private T data;
4          private QueueNode<T> next;
5
6          public QueueNode(T data) {
7              this.data = data;
8          }
9      }
10
11     private QueueNode<T> first;
12     private QueueNode<T> last;
13
14     public void add(T item) {

```

```
15     QueueNode<T> t = new QueueNode<T>(item);
16     if (last != null) {
17         last.next = t;
18     }
19     last = t;
20     if (first == null) {
21         first = last;
22     }
23 }
24
25 public T remove() {
26     if (first == null) throw new NoSuchElementException();
27     T data = first.data;
28     first = first.next;
29     if (first == null) {
30         last = null;
31     }
32     return data;
33 }
34
35 public T peek() {
36     if (first == null) throw new NoSuchElementException();
37     return first.data;
38 }
39
40 public boolean isEmpty() {
41     return first == null;
42 }
43 }
```

It is especially easy to mess up the updating of the first and last nodes in a queue. Be sure to double check this.

One place where queues are often used is in breadth-first search or in implementing a cache.

In breadth-first search, for example, we used a queue to store a list of the nodes that we need to process. Each time we process a node, we add its adjacent nodes to the back of the queue. This allows us to process nodes in the order in which they are viewed.

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### Interview Questions

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- 3.1 Three in One:** Describe how you could use a single array to implement three stacks.

Hints: #2, #12, #38, #58

pg 227

- 3.2 Stack Min:** How would you design a stack which, in addition to push and pop, has a function `min` which returns the minimum element? Push, pop and `min` should all operate in  $O(1)$  time.

Hints: #27, #59, #78

pg 232

- 3.3 Stack of Plates:** Imagine a (literal) stack of plates. If the stack gets too high, it might topple. Therefore, in real life, we would likely start a new stack when the previous stack exceeds some threshold. Implement a data structure `SetOfStacks` that mimics this. `SetOfStacks` should be composed of several stacks and should create a new stack once the previous one exceeds capacity. `SetOfStacks.push()` and `SetOfStacks.pop()` should behave identically to a single stack (that is, `pop()` should return the same values as it would if there were just a single stack).

**FOLLOW UP**

Implement a function `popAt(int index)` which performs a pop operation on a specific sub-stack.

Hints: #64, #81

pg 233

- 3.4 Queue via Stacks:** Implement a `MyQueue` class which implements a queue using two stacks.

Hints: #98, #114

pg 236

- 3.5 Sort Stack:** Write a program to sort a stack such that the smallest items are on the top. You can use an additional temporary stack, but you may not copy the elements into any other data structure (such as an array). The stack supports the following operations: `push`, `pop`, `peek`, and `isEmpty`.

Hints: #15, #32, #43

pg 237

- 3.6 Animal Shelter:** An animal shelter, which holds only dogs and cats, operates on a strictly "first in, first out" basis. People must adopt either the "oldest" (based on arrival time) of all animals at the shelter, or they can select whether they would prefer a dog or a cat (and will receive the oldest animal of that type). They cannot select which specific animal they would like. Create the data structures to maintain this system and implement operations such as `enqueue`, `dequeueAny`, `dequeueDog`, and `dequeueCat`. You may use the built-in `LinkedList` data structure.

Hints: #22, #56, #63

pg 239

Additional Questions: Linked Lists (#2.6), Moderate Problems (#16.26), Hard Problems (#17.9).

Hints start on page 653.

# 4

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## Trees and Graphs

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Many interviewees find tree and graph problems to be some of the trickiest. Searching a tree is more complicated than searching in a linearly organized data structure such as an array or linked list. Additionally, the worst case and average case time may vary wildly, and we must evaluate both aspects of any algorithm. Fluency in implementing a tree or graph from scratch will prove essential.

Because most people are more familiar with trees than graphs (and they're a bit simpler), we'll discuss trees first. This is a bit out of order though, as a tree is actually a type of graph.

Note: Some of the terms in this chapter can vary slightly across different textbooks and other sources. If you're used to a different definition, that's fine. Make sure to clear up any ambiguity with your interviewer.

### ► Types of Trees

A nice way to understand a tree is with a recursive explanation. A tree is a data structure composed of nodes.

- Each tree has a root node. (Actually, this isn't strictly necessary in graph theory, but it's usually how we use trees in programming, and especially programming interviews.)
- The root node has zero or more child nodes.
- Each child node has zero or more child nodes, and so on.

The tree cannot contain cycles. The nodes may or may not be in a particular order, they could have any data type as values, and they may or may not have links back to their parent nodes.

A very simple class definition for Node is:

```
1  class Node {  
2      public String name;  
3      public Node[] children;  
4  }
```

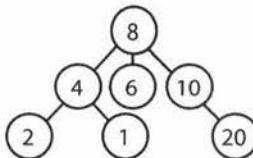
You might also have a Tree class to wrap this node. For the purposes of interview questions, we typically do not use a Tree class. You can if you feel it makes your code simpler or better, but it rarely does.

```
1  class Tree {  
2      public Node root;  
3  }
```

Tree and graph questions are rife with ambiguous details and incorrect assumptions. Be sure to watch out for the following issues and seek clarification when necessary.

### Trees vs. Binary Trees

A binary tree is a tree in which each node has up to two children. Not all trees are binary trees. For example, this tree is not a binary tree. You could call it a ternary tree.



There are occasions when you might have a tree that is not a binary tree. For example, suppose you were using a tree to represent a bunch of phone numbers. In this case, you might use a 10-ary tree, with each node having up to 10 children (one for each digit).

A node is called a “leaf” node if it has no children.

### Binary Tree vs. Binary Search Tree

A binary search tree is a binary tree in which every node fits a specific ordering property: all left descendants  $\leq n <$  all right descendants. This must be true for each node  $n$ .

The definition of a binary search tree can vary slightly with respect to equality. Under some definitions, the tree cannot have duplicate values. In others, the duplicate values will be on the right or can be on either side. All are valid definitions, but you should clarify this with your interviewer.

Note that this inequality must be true for all of a node’s descendants, not just its immediate children. The following tree on the left below is a binary search tree. The tree on the right is not, since 12 is to the left of 8.

A binary search tree.



Not a binary search tree.



When given a tree question, many candidates assume the interviewer means a binary *search* tree. Be sure to ask. A binary search tree imposes the condition that, for each node, its left descendants are less than or equal to the current node, which is less than the right descendants.

### Balanced vs. Unbalanced

While many trees are balanced, not all are. Ask your interviewer for clarification here. Note that balancing a tree does not mean the left and right subtrees are exactly the same size (like you see under “perfect binary trees” in the following diagram).

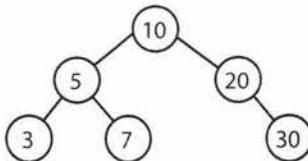
One way to think about it is that a “balanced” tree really means something more like “not terribly imbalanced.” It’s balanced enough to ensure  $O(\log n)$  times for `insert` and `find`, but it’s not necessarily as balanced as it could be.

Two common types of balanced trees are red-black trees (pg 639) and AVL trees (pg 637). These are discussed in more detail in the Advanced Topics section.

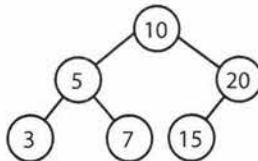
### Complete Binary Trees

A complete binary tree is a binary tree in which every level of the tree is fully filled, except for perhaps the last level. To the extent that the last level is filled, it is filled left to right.

not a complete binary tree



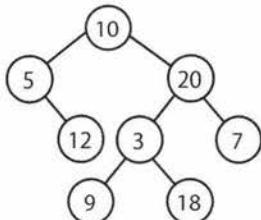
a complete binary tree



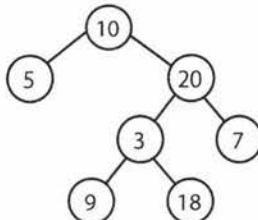
### Full Binary Trees

A full binary tree is a binary tree in which every node has either zero or two children. That is, no nodes have only one child.

not a full binary tree

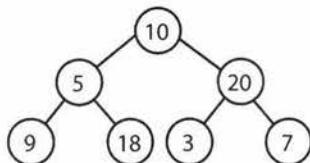


a full binary tree



### Perfect Binary Trees

A perfect binary tree is one that is both full and complete. All leaf nodes will be at the same level, and this level has the maximum number of nodes.



Note that perfect trees are rare in interviews and in real life, as a perfect tree must have exactly  $2^k - 1$  nodes (where  $k$  is the number of levels). In an interview, do not assume a binary tree is perfect.

## ► Binary Tree Traversal

Prior to your interview, you should be comfortable implementing in-order, post-order, and pre-order traversal. The most common of these is in-order traversal.

### In-Order Traversal

In-order traversal means to “visit” (often, print) the left branch, then the current node, and finally, the right branch.

```
1 void inOrderTraversal(TreeNode node) {  
2     if (node != null) {  
3         inOrderTraversal(node.left);  
4         visit(node);  
5         inOrderTraversal(node.right);  
6     }  
7 }
```

When performed on a binary search tree, it visits the nodes in ascending order (hence the name “in-order”).

### Pre-Order Traversal

Pre-order traversal visits the current node before its child nodes (hence the name “pre-order”).

```
1 void preOrderTraversal(TreeNode node) {  
2     if (node != null) {  
3         visit(node);  
4         preOrderTraversal(node.left);  
5         preOrderTraversal(node.right);  
6     }  
7 }
```

In a pre-order traversal, the root is always the first node visited.

### Post-Order Traversal

Post-order traversal visits the current node after its child nodes (hence the name “post-order”).

```
1 void postOrderTraversal(TreeNode node) {  
2     if (node != null) {  
3         postOrderTraversal(node.left);  
4         postOrderTraversal(node.right);  
5         visit(node);  
6     }  
7 }
```

In a post-order traversal, the root is always the last node visited.

## ► Binary Heaps (Min-Heaps and Max-Heaps)

We'll just discuss min-heaps here. Max-heaps are essentially equivalent, but the elements are in descending order rather than ascending order.

A min-heap is a *complete* binary tree (that is, totally filled other than the rightmost elements on the last level) where each node is smaller than its children. The root, therefore, is the minimum element in the tree.

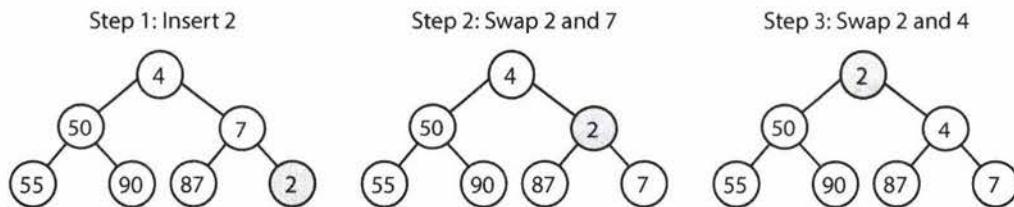


We have two key operations on a min-heap: `insert` and `extract_min`.

#### *Insert*

When we insert into a min-heap, we always start by inserting the element at the bottom. We insert at the rightmost spot so as to maintain the complete tree property.

Then, we “fix” the tree by swapping the new element with its parent, until we find an appropriate spot for the element. We essentially bubble up the minimum element.



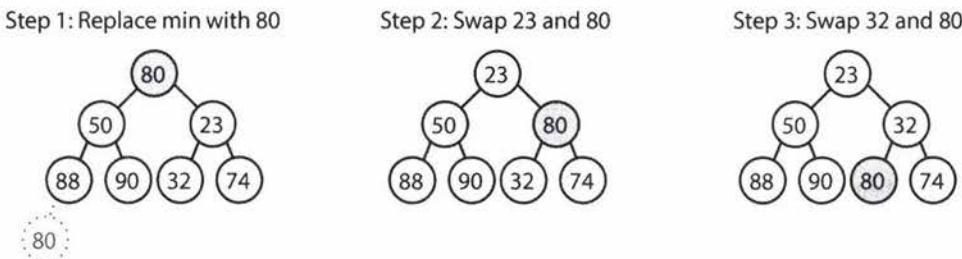
This takes  $O(\log n)$  time, where  $n$  is the number of nodes in the heap.

#### *Extract Minimum Element*

Finding the minimum element of a min-heap is easy: it's always at the top. The trickier part is how to remove it. (In fact, this isn't that tricky.)

First, we remove the minimum element and swap it with the last element in the heap (the bottommost, rightmost element). Then, we bubble down this element, swapping it with one of its children until the min-heap property is restored.

Do we swap it with the left child or the right child? That depends on their values. There's no inherent ordering between the left and right element, but you'll need to take the smaller one in order to maintain the min-heap ordering.



This algorithm will also take  $O(\log n)$  time.

## ▶ Tries (Prefix Trees)

A trie (sometimes called a prefix tree) is a funny data structure. It comes up a lot in interview questions, but algorithm textbooks don't spend much time on this data structure.

A trie is a variant of an n-ary tree in which characters are stored at each node. Each path down the tree may represent a word.

The \* nodes (sometimes called "null nodes") are often used to indicate complete words. For example, the fact that there is a \* node under MANY indicates that MANY is a complete word. The existence of the MA path indicates there are words that start with MA.

The actual implementation of these \* nodes might be a special type of child (such as a `TerminatingTrieNode`, which inherits from `TrieNode`). Or, we could use just a boolean flag terminates within the "parent" node.

A node in a trie could have anywhere from 1 through `ALPHABET_SIZE + 1` children (or, 0 through `ALPHABET_SIZE` if a boolean flag is used instead of a \* node).



Very commonly, a trie is used to store the entire (English) language for quick prefix lookups. While a hash table can quickly look up whether a string is a valid word, it cannot tell us if a string is a prefix of any valid words. A trie can do this very quickly.

How quickly? A trie can check if a string is a valid prefix in  $O(K)$  time, where  $K$  is the length of the string. This is actually the same runtime as a hash table will take. Although we often refer to hash table lookups as being  $O(1)$  time, this isn't entirely true. A hash table must read through all the characters in the input, which takes  $O(K)$  time in the case of a word lookup.

Many problems involving lists of valid words leverage a trie as an optimization. In situations when we search through the tree on related prefixes repeatedly (e.g., looking up M, then MA, then MAN, then MANY), we might pass around a reference to the current node in the tree. This will allow us to just check if Y is a child of MAN, rather than starting from the root each time.

## ▶ Graphs

A tree is actually a type of graph, but not all graphs are trees. Simply put, a tree is a connected graph without cycles.

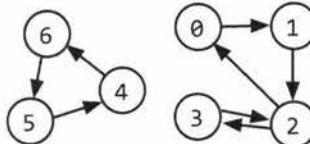
A graph is simply a collection of nodes with edges between (some of) them.

- Graphs can be either directed (like the following graph) or undirected. While directed edges are like a

one-way street, undirected edges are like a two-way street.

- The graph might consist of multiple isolated subgraphs. If there is a path between every pair of vertices, it is called a “connected graph.”
- The graph can also have cycles (or not). An “acyclic graph” is one without cycles.

Visually, you could draw a graph like this:



In terms of programming, there are two common ways to represent a graph.

### Adjacency List

This is the most common way to represent a graph. Every vertex (or node) stores a list of adjacent vertices. In an undirected graph, an edge like  $(a, b)$  would be stored twice: once in  $a$ 's adjacent vertices and once in  $b$ 's adjacent vertices.

A simple class definition for a graph node could look essentially the same as a tree node.

```
1 class Graph {  
2     public Node[] nodes;  
3 }  
4  
5 class Node {  
6     public String name;  
7     public Node[] children;  
8 }
```

The Graph class is used because, unlike in a tree, you can't necessarily reach all the nodes from a single node.

You don't necessarily need any additional classes to represent a graph. An array (or a hash table) of lists (arrays, arraylists, linked lists, etc.) can store the adjacency list. The graph above could be represented as:

```
0: 1  
1: 2  
2: 0, 3  
3: 2  
4: 6  
5: 4  
6: 5
```

This is a bit more compact, but it isn't quite as clean. We tend to use node classes unless there's a compelling reason not to.

### Adjacency Matrices

An adjacency matrix is an  $N \times N$  boolean matrix (where  $N$  is the number of nodes), where a true value at  $\text{matrix}[i][j]$  indicates an edge from node  $i$  to node  $j$ . (You can also use an integer matrix with 0s and 1s.)

In an undirected graph, an adjacency matrix will be symmetric. In a directed graph, it will not (necessarily) be.



	0	1	2	3
0	0	1	0	0
1	0	0	1	0
2	1	0	0	0
3	0	0	1	0

The same graph algorithms that are used on adjacency lists (breadth-first search, etc.) can be performed with adjacency matrices, but they may be somewhat less efficient. In the adjacency list representation, you can easily iterate through the neighbors of a node. In the adjacency matrix representation, you will need to iterate through all the nodes to identify a node's neighbors.

## ► Graph Search

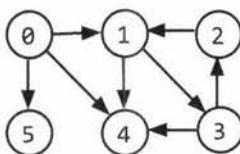
The two most common ways to search a graph are depth-first search and breadth-first search.

In depth-first search (DFS), we start at the root (or another arbitrarily selected node) and explore each branch completely before moving on to the next branch. That is, we go deep first (hence the name *depth-first search*) before we go wide.

In breadth-first search (BFS), we start at the root (or another arbitrarily selected node) and explore each neighbor before going on to any of their children. That is, we go wide (hence *breadth-first search*) before we go deep.

See the below depiction of a graph and its depth-first and breadth-first search (assuming neighbors are iterated in numerical order).

**Graph**



**Depth-First Search**

- 1 Node 0
- 2 Node 1
- 3 Node 3
- 4 Node 2
- 5 Node 4
- 6 Node 5

**Breadth-First Search**

- 1 Node 0
- 2 Node 1
- 3 Node 4
- 4 Node 5
- 5 Node 3
- 6 Node 2

Breadth-first search and depth-first search tend to be used in different scenarios. DFS is often preferred if we want to visit every node in the graph. Both will work just fine, but depth-first search is a bit simpler.

However, if we want to find the shortest path (or just any path) between two nodes, BFS is generally better. Consider representing all the friendships in the entire world in a graph and trying to find a path of friendships between Ash and Vanessa.

In depth-first search, we could take a path like Ash → Brian → Carleton → Davis → Eric → Farah → Gayle → Harry → Isabella → John → Kari... and then find ourselves very far away. We could go through most of the world without realizing that, in fact, Vanessa is Ash's friend. We will still eventually find the path, but it may take a long time. It also won't find us the shortest path.

In breadth-first search, we would stay close to Ash for as long as possible. We might iterate through many of Ash's friends, but we wouldn't go to his more distant connections until absolutely necessary. If Vanessa is Ash's friend, or his friend-of-a-friend, we'll find this out relatively quickly.

### Depth-First Search (DFS)

In DFS, we visit a node  $a$  and then iterate through each of  $a$ 's neighbors. When visiting a node  $b$  that is a neighbor of  $a$ , we visit all of  $b$ 's neighbors before going on to  $a$ 's other neighbors. That is, a exhaustively searches  $b$ 's branch before any of its other neighbors.

Note that pre-order and other forms of tree traversal are a form of DFS. The key difference is that when implementing this algorithm for a graph, we must check if the node has been visited. If we don't, we risk getting stuck in an infinite loop.

The pseudocode below implements DFS.

```
1 void search(Node root) {  
2     if (root == null) return;  
3     visit(root);  
4     root.visited = true;  
5     for each (Node n in root.adjacent) {  
6         if (n.visited == false) {  
7             search(n);  
8         }  
9     }  
10 }
```

### Breadth-First Search (BFS)

BFS is a bit less intuitive, and many interviewees struggle with the implementation unless they are already familiar with it. The main tripping point is the (false) assumption that BFS is recursive. It's not. Instead, it uses a queue.

In BFS, node  $a$  visits each of  $a$ 's neighbors before visiting any of *their* neighbors. You can think of this as searching level by level out from  $a$ . An iterative solution involving a queue usually works best.

```
1 void search(Node root) {  
2     Queue queue = new Queue();  
3     root.marked = true;  
4     queue.enqueue(root); // Add to the end of queue  
5  
6     while (!queue.isEmpty()) {  
7         Node r = queue.dequeue(); // Remove from the front of the queue  
8         visit(r);  
9         foreach (Node n in r.adjacent) {  
10             if (n.marked == false) {  
11                 n.marked = true;  
12                 queue.enqueue(n);  
13             }  
14         }  
15     }  
16 }
```

If you are asked to implement BFS, the key thing to remember is the use of the queue. The rest of the algorithm flows from this fact.

### Bidirectional Search

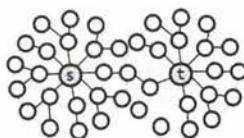
Bidirectional search is used to find the shortest path between a source and destination node. It operates by essentially running two simultaneous breadth-first searches, one from each node. When their searches collide, we have found a path.

**Breadth-First Search**

Single search from  $s$  to  $t$  that collides after four levels.

**Bidirectional Search**

Two searches (one from  $s$  and one from  $t$ ) that collide after four levels total (two levels each).



To see why this is faster, consider a graph where every node has at most  $k$  adjacent nodes and the shortest path from node  $s$  to node  $t$  has length  $d$ .

- In traditional breadth-first search, we would search up to  $k$  nodes in the first “level” of the search. In the second level, we would search up to  $k$  nodes for each of those first  $k$  nodes, so  $k^2$  nodes total (thus far). We would do this  $d$  times, so that’s  $O(k^d)$  nodes.
- In bidirectional search, we have two searches that collide after approximately  $\frac{d}{2}$  levels (the midpoint of the path). The search from  $s$  visits approximately  $k^{d/2}$ , as does the search from  $t$ . That’s approximately  $2 k^{d/2}$ , or  $O(k^{d/2})$ , nodes total.

This might seem like a minor difference, but it’s not. It’s huge. Recall that  $(k^{d/2}) * (k^{d/2}) = k^d$ . The bidirectional search is actually faster by a factor of  $k^{d/2}$ .

Put another way: if our system could only support searching “friend of friend” paths in breadth-first search, it could now likely support “friend of friend of friend of friend” paths. We can support paths that are twice as long.

**Additional Reading:** Topological Sort (pg 632), Dijkstra’s Algorithm (pg 633), AVL Trees (pg 637), Red-Black Trees (pg 639).

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## Interview Questions

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- 4.1 Route Between Nodes:** Given a directed graph, design an algorithm to find out whether there is a route between two nodes.

Hints: #127

pg 241

- 4.2 Minimal Tree:** Given a sorted (increasing order) array with unique integer elements, write an algorithm to create a binary search tree with minimal height.

Hints: #19, #73, #116

pg 242

- 4.3 List of Depths:** Given a binary tree, design an algorithm which creates a linked list of all the nodes at each depth (e.g., if you have a tree with depth  $D$ , you’ll have  $D$  linked lists).

Hints: #107, #123, #135

pg 243

- 4.4 Check Balanced:** Implement a function to check if a binary tree is balanced. For the purposes of this question, a balanced tree is defined to be a tree such that the heights of the two subtrees of any node never differ by more than one.

Hints: #21, #33, #49, #105, #124

pg 244

- 4.5 Validate BST:** Implement a function to check if a binary tree is a binary search tree.

Hints: #35, #57, #86, #113, #128

pg 245

- 4.6 Successor:** Write an algorithm to find the “next” node (i.e., in-order successor) of a given node in a binary search tree. You may assume that each node has a link to its parent.

Hints: #79, #91

pg 248

- 4.7 Build Order:** You are given a list of projects and a list of dependencies (which is a list of pairs of projects, where the second project is dependent on the first project). All of a project’s dependencies must be built before the project is. Find a build order that will allow the projects to be built. If there is no valid build order, return an error.

EXAMPLE

Input:

projects: a, b, c, d, e, f

dependencies: (a, d), (f, b), (b, d), (f, a), (d, c)

Output: f, e, a, b, d, c

Hints: #26, #47, #60, #85, #125, #133

pg 250

- 4.8 First Common Ancestor:** Design an algorithm and write code to find the first common ancestor of two nodes in a binary tree. Avoid storing additional nodes in a data structure. NOTE: This is not necessarily a binary search tree.

Hints: #10, #16, #28, #36, #46, #70, #80, #96

pg 257

- 4.9 BST Sequences:** A binary search tree was created by traversing through an array from left to right and inserting each element. Given a binary search tree with distinct elements, print all possible arrays that could have led to this tree.

EXAMPLE

Input:



Output: {2, 1, 3}, {2, 3, 1}

Hints: #39, #48, #66, #82

pg 262

- 4.10 Check Subtree:** T1 and T2 are two very large binary trees, with T1 much bigger than T2. Create an algorithm to determine if T2 is a subtree of T1.

A tree T2 is a subtree of T1 if there exists a node n in T1 such that the subtree of n is identical to T2. That is, if you cut off the tree at node n, the two trees would be identical.

Hints: #4, #11, #18, #31, #37

pg 265

- 4.11 Random Node:** You are implementing a binary tree class from scratch which, in addition to insert, find, and delete, has a method `getRandomNode()` which returns a random node from the tree. All nodes should be equally likely to be chosen. Design and implement an algorithm for `getRandomNode`, and explain how you would implement the rest of the methods.

Hints: #42, #54, #62, #75, #89, #99, #112, #119

pg 268

- 4.12 Paths with Sum:** You are given a binary tree in which each node contains an integer value (which might be positive or negative). Design an algorithm to count the number of paths that sum to a given value. The path does not need to start or end at the root or a leaf, but it must go downwards (traveling only from parent nodes to child nodes).

Hints: #6, #14, #52, #68, #77, #87, #94, #103, #108, #115

pg 272

Additional Questions: Recursion (#8.10), System Design and Scalability (#9.2, #9.3), Sorting and Searching (#10.10), Hard Problems (#17.7, #17.12, #17.13, #17.14, #17.17, #17.20, #17.22, #17.25).

Hints start on page 653.

# 5

## Bit Manipulation

**B**it manipulation is used in a variety of problems. Sometimes, the question explicitly calls for bit manipulation. Other times, it's simply a useful technique to optimize your code. You should be comfortable doing bit manipulation by hand, as well as with code. Be careful; it's easy to make little mistakes.

### ► Bit Manipulation By Hand

If you're rusty on bit manipulation, try the following exercises by hand. The items in the third column can be solved manually or with "tricks" (described below). For simplicity, assume that these are four-bit numbers.

If you get confused, work them through as a base 10 number. You can then apply the same process to a binary number. Remember that  $\wedge$  indicates an XOR, and  $\sim$  is a NOT (negation).

0110 + 0010	0011 * 0101	0110 + 0110
0011 + 0010	0011 * 0011	0100 * 0011
0110 - 0011	1101 >> 2	1101 $\wedge$ ( $\sim$ 1101)
1000 - 0110	1101 $\wedge$ 0101	1011 & ( $\sim$ 0 << 2)

Solutions: line 1 (1000, 1111, 1100); line 2 (0101, 1001, 1100); line 3 (0011, 0011, 1111); line 4 (0010, 1000, 1000).

The tricks in Column 3 are as follows:

1.  $0110 + 0110$  is equivalent to  $0110 * 2$ , which is equivalent to shifting  $0110$  left by 1.
2.  $0100$  equals 4, and multiplying by 4 is just left shifting by 2. So we shift  $0011$  left by 2 to get  $1100$ .
3. Think about this operation bit by bit. If you XOR a bit with its own negated value, you will always get 1. Therefore, the solution to  $a \wedge (\sim a)$  will be a sequence of 1s.
4.  $\sim 0$  is a sequence of 1s, so  $\sim 0 << 2$  is 1s followed by two 0s. ANDing that with another value will clear the last two bits of the value.

If you didn't see these tricks immediately, think about them logically.

### ► Bit Facts and Tricks

The following expressions are useful in bit manipulation. Don't just memorize them, though; think deeply about why each of these is true. We use "1s" and "0s" to indicate a sequence of 1s or 0s, respectively.

$$\begin{array}{lll} x \wedge 0s = x & x \wedge 1s = \sim x & x \mid 0s = x \\ x \wedge 1s = \sim x & x \wedge 1s = x & x \mid 1s = 1s \\ x \wedge x = 0 & x \wedge x = x & x \mid x = x \end{array}$$

To understand these expressions, recall that these operations occur bit-by-bit, with what's happening on one bit never impacting the other bits. This means that if one of the above statements is true for a single bit, then it's true for a sequence of bits.

## ► Two's Complement and Negative Numbers

Computers typically store integers in two's complement representation. A positive number is represented as itself while a negative number is represented as the two's complement of its absolute value (with a 1 in its sign bit to indicate that a negative value). The two's complement of an N-bit number (where N is the number of bits used for the number, *excluding* the sign bit) is the complement of the number with respect to  $2^N$ .

Let's look at the 4-bit integer -3 as an example. If it's a 4-bit number, we have one bit for the sign and three bits for the value. We want the complement with respect to  $2^3$ , which is 8. The complement of 3 (the absolute value of -3) with respect to 8 is 5. 5 in binary is 101. Therefore, -3 in binary as a 4-bit number is 1101, with the first bit being the sign bit.

In other words, the binary representation of -K (negative K) as a N-bit number is concat(1,  $2^{N-1} - K$ ).

Another way to look at this is that we invert the bits in the positive representation and then add 1. 3 is 011 in binary. Flip the bits to get 100, add 1 to get 101, then prepend the sign bit (1) to get 1101.

In a four-bit integer, this would look like the following.

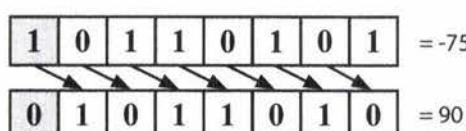
Positive Values		Negative Values	
7	<u>0</u> 111	-1	<u>1</u> 111
6	<u>0</u> 110	-2	<u>1</u> 110
5	<u>0</u> 101	-3	<u>1</u> 101
4	<u>0</u> 100	-4	<u>1</u> 100
3	<u>0</u> 011	-5	<u>1</u> 011
2	<u>0</u> 010	-6	<u>1</u> 010
1	<u>0</u> 001	-7	<u>1</u> 001
0	<u>0</u> 000		

Observe that the absolute values of the integers on the left and right always sum to  $2^3$ , and that the binary values on the left and right sides are identical, other than the sign bit. Why is that?

## ► Arithmetic vs. Logical Right Shift

There are two types of right shift operators. The arithmetic right shift essentially divides by two. The logical right shift does what we would visually see as shifting the bits. This is best seen on a negative number.

In a logical right shift, we shift the bits and put a 0 in the most significant bit. It is indicated with a `>>` operator. On an 8-bit integer (where the sign bit is the most significant bit), this would look like the image below. The sign bit is indicated with a gray background.



In an arithmetic right shift, we shift values to the right but fill in the new bits with the value of the sign bit. This has the effect of (roughly) dividing by two. It is indicated by a `>>` operator.



What do you think these functions would do on parameters `x = -93242` and `count = 40`?

```
1 int repeatedArithmeticShift(int x, int count) {
2     for (int i = 0; i < count; i++) {
3         x >>= 1; // Arithmetic shift by 1
4     }
5     return x;
6 }
7
8 int repeatedLogicalShift(int x, int count) {
9     for (int i = 0; i < count; i++) {
10         x >>>= 1; // Logical shift by 1
11     }
12     return x;
13 }
```

With the logical shift, we would get 0 because we are shifting a zero into the most significant bit repeatedly.

With the arithmetic shift, we would get -1 because we are shifting a one into the most significant bit repeatedly. A sequence of all 1s in a (signed) integer represents -1.

## ▶ Common Bit Tasks: Getting and Setting

The following operations are very important to know, but do not simply memorize them. Memorizing leads to mistakes that are impossible to recover from. Rather, understand *how* to implement these methods, so that you can implement these, and other, bit problems.

## Get Bit

This method shifts 1 over by  $i$  bits, creating a value that looks like 00010000. By performing an AND with  $num$ , we clear all bits other than the bit at bit  $i$ . Finally, we compare that to 0. If that new value is not zero, then bit  $i$  must have a 1. Otherwise, bit  $i$  is a 0.

```
1 boolean getBit(int num, int i) {  
2     return ((num & (1 << i)) != 0);  
3 }
```

### **Set Bit**

`SetBit` shifts 1 over by  $i$  bits, creating a value like `00010000`. By performing an OR with `num`, only the value at bit  $i$  will change. All other bits of the mask are zero and will not affect `num`.

```
1 int setBit(int num, int i) {  
2     return num | (1 << i);  
3 }
```

### Clear Bit

This method operates in almost the reverse of `setBit`. First, we create a number like 11101111 by creating the reverse of it (00010000) and negating it. Then, we perform an AND with num. This will clear the  $i$ th bit and leave the remainder unchanged.

```
1 int clearBit(int num, int i) {
2     int mask = ~(1 << i);
3     return num & mask;
4 }
```

To clear all bits from the most significant bit through  $i$  (inclusive), we create a mask with a 1 at the  $i$ th bit ( $1 << i$ ). Then, we subtract 1 from it, giving us a sequence of 0s followed by  $i$  1s. We then AND our number with this mask to leave just the last  $i$  bits.

```
1 int clearBitsMSBthroughI(int num, int i) {
2     int mask = (1 << i) - 1;
3     return num & mask;
4 }
```

To clear all bits from  $i$  through 0 (inclusive), we take a sequence of all 1s (which is -1) and shift it left by  $i + 1$  bits. This gives us a sequence of 1s (in the most significant bits) followed by  $i + 1$  0 bits.

```
1 int clearBitsIthrough0(int num, int i) {
2     int mask = (-1 << (i + 1));
3     return num & mask;
4 }
```

### Update Bit

To set the  $i$ th bit to a value  $v$ , we first clear the bit at position  $i$  by using a mask that looks like 11101111. Then, we shift the intended value,  $v$ , left by  $i$  bits. This will create a number with bit  $i$  equal to  $v$  and all other bits equal to 0. Finally, we OR these two numbers, updating the  $i$ th bit if  $v$  is 1 and leaving it as 0 otherwise.

```
1 int updateBit(int num, int i, boolean bitIs1) {
2     int value = bitIs1 ? 1 : 0;
3     int mask = ~(1 << i);
4     return (num & mask) | (value << i);
5 }
```

---

### Interview Questions

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- 5.1 Insertion:** You are given two 32-bit numbers,  $N$  and  $M$ , and two bit positions,  $i$  and  $j$ . Write a method to insert  $M$  into  $N$  such that  $M$  starts at bit  $j$  and ends at bit  $i$ . You can assume that the bits  $j$  through  $i$  have enough space to fit all of  $M$ . That is, if  $M = 10011$ , you can assume that there are at least 5 bits between  $j$  and  $i$ . You would not, for example, have  $j = 3$  and  $i = 2$ , because  $M$  could not fully fit between bit 3 and bit 2.

EXAMPLE

Input:  $N = 100000000000$ ,  $M = 10011$ ,  $i = 2$ ,  $j = 6$

Output:  $N = 10001001100$

Hints: #137, #169, #215

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- 5.2 Binary to String:** Given a real number between 0 and 1 (e.g., 0.72) that is passed in as a double, print the binary representation. If the number cannot be represented accurately in binary with at most 32 characters, print "ERROR."

Hints: #143, #167, #173, #269, #297

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- 5.3 Flip Bit to Win:** You have an integer and you can flip exactly one bit from a 0 to a 1. Write code to find the length of the longest sequence of 1s you could create.

EXAMPLE

Input: 1775 (or: 11011101111)

Output: 8

Hints: #159, #226, #314, #352

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- 5.4 Next Number:** Given a positive integer, print the next smallest and the next largest number that have the same number of 1 bits in their binary representation.

Hints: #147, #175, #242, #312, #339, #358, #375, #390

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- 5.5 Debugger:** Explain what the following code does: `((n & (n-1)) == 0)`.

Hints: #151, #202, #261, #302, #346, #372, #383, #398

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- 5.6 Conversion:** Write a function to determine the number of bits you would need to flip to convert integer A to integer B.

EXAMPLE

Input: 29 (or: 11101), 15 (or: 01111)

Output: 2

Hints: #336, #369

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- 5.7 Pairwise Swap:** Write a program to swap odd and even bits in an integer with as few instructions as possible (e.g., bit 0 and bit 1 are swapped, bit 2 and bit 3 are swapped, and so on).

Hints: #145, #248, #328, #355

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- 5.8 Draw Line:** A monochrome screen is stored as a single array of bytes, allowing eight consecutive pixels to be stored in one byte. The screen has width w, where w is divisible by 8 (that is, no byte will be split across rows). The height of the screen, of course, can be derived from the length of the array and the width. Implement a function that draws a horizontal line from (x1, y) to (x2, y).

The method signature should look something like:

`drawLine(byte[] screen, int width, int x1, int x2, int y)`

Hints: #366, #381, #384, #391

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Additional Questions: Arrays and Strings (#1.1, #1.4, #1.8), Math and Logic Puzzles (#6.10), Recursion (#8.4, #8.14), Sorting and Searching (#10.7, #10.8), C++ (#12.10), Moderate Problems (#16.1, #16.7), Hard Problems (#17.1).

Hints start on page 662.

# 6

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## Math and Logic Puzzles

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**S**o-called “puzzles” (or brain teasers) are some of the most hotly debated questions, and many companies have policies banning them. Unfortunately, even when these questions are banned, you still may find yourself being asked one of them. Why? Because no one can agree on a definition of what a brainteaser is.

The good news is that if you are asked a puzzle or brainteaser, it’s likely to be a reasonably fair one. It probably won’t rely on a trick of wording, and it can almost always be logically deduced. Many have their foundations in mathematics or computer science, and almost all have solutions that can be logically deduced.

We’ll go through some common approaches for tackling these questions, as well as some of the essential knowledge.

### ► Prime Numbers

As you probably know, every positive integer can be decomposed into a product of primes. For example:

$$84 = 2^2 * 3^1 * 5^0 * 7^1 * 11^0 * 13^0 * 17^0 * \dots$$

Note that many of these primes have an exponent of zero.

### Divisibility

The prime number law stated above means that, in order for a number  $x$  to divide a number  $y$  (written  $x \mid y$ , or  $\text{mod}(y, x) = 0$ ), all primes in  $x$ ’s prime factorization must be in  $y$ ’s prime factorization. Or, more specifically:

$$\text{Let } x = 2^{j_0} * 3^{j_1} * 5^{j_2} * 7^{j_3} * 11^{j_4} * \dots$$

$$\text{Let } y = 2^{k_0} * 3^{k_1} * 5^{k_2} * 7^{k_3} * 11^{k_4} * \dots$$

If  $x \mid y$ , then for all  $i$ ,  $j_i \leq k_i$ .

In fact, the greatest common divisor of  $x$  and  $y$  will be:

$$\text{gcd}(x, y) = 2^{\min(j_0, k_0)} * 3^{\min(j_1, k_1)} * 5^{\min(j_2, k_2)} * \dots$$

The least common multiple of  $x$  and  $y$  will be:

$$\text{lcm}(x, y) = 2^{\max(j_0, k_0)} * 3^{\max(j_1, k_1)} * 5^{\max(j_2, k_2)} * \dots$$

As a fun exercise, stop for a moment and think what would happen if you did  $\text{gcd} * \text{lcm}$ :

$$\begin{aligned}\text{gcd} * \text{lcm} &= 2^{\min(j_0, k_0)} * 2^{\max(j_0, k_0)} * 3^{\min(j_1, k_1)} * 3^{\max(j_1, k_1)} * \dots \\ &= 2^{\min(j_0, k_0) + \max(j_0, k_0)} * 3^{\min(j_1, k_1) + \max(j_1, k_1)} * \dots \\ &= 2^{j_0 + k_0} * 3^{j_1 + k_1} * \dots \\ &= 2^{j_0} * 2^{k_0} * 3^{j_1} * 3^{k_1} * \dots\end{aligned}$$

= xy

### Checking for Primality

This question is so common that we feel the need to specifically cover it. The naive way is to simply iterate from 2 through  $n-1$ , checking for divisibility on each iteration.

```
1 boolean primeNaive(int n) {  
2     if (n < 2) {  
3         return false;  
4     }  
5     for (int i = 2; i < n; i++) {  
6         if (n % i == 0) {  
7             return false;  
8         }  
9     }  
10    return true;  
11 }
```

A small but important improvement is to iterate only up through the square root of  $n$ .

```
1 boolean primeSlightlyBetter(int n) {  
2     if (n < 2) {  
3         return false;  
4     }  
5     int sqrt = (int) Math.sqrt(n);  
6     for (int i = 2; i <= sqrt; i++) {  
7         if (n % i == 0) return false;  
8     }  
9     return true;  
10 }
```

The  $\sqrt{n}$  is sufficient because, for every number  $a$  which divides  $n$  evenly, there is a complement  $b$ , where  $a * b = n$ . If  $a > \sqrt{n}$ , then  $b < \sqrt{n}$  (since  $(\sqrt{n})^2 = n$ ). We therefore don't need  $a$  to check  $n$ 's primality, since we would have already checked with  $b$ .

Of course, in reality, all we *really* need to do is to check if  $n$  is divisible by a prime number. This is where the Sieve of Eratosthenes comes in.

### Generating a List of Primes: The Sieve of Eratosthenes

The Sieve of Eratosthenes is a highly efficient way to generate a list of primes. It works by recognizing that all non-prime numbers are divisible by a prime number.

We start with a list of all the numbers up through some value  $max$ . First, we cross off all numbers divisible by 2. Then, we look for the next prime (the next non-crossed off number) and cross off all numbers divisible by it. By crossing off all numbers divisible by 2, 3, 5, 7, 11, and so on, we wind up with a list of prime numbers from 2 through  $max$ .

The code below implements the Sieve of Eratosthenes.

```
1 boolean[] sieveOfEratosthenes(int max) {  
2     boolean[] flags = new boolean[max + 1];  
3     int count = 0;  
4  
5     init(flags); // Set all flags to true other than 0 and 1  
6     int prime = 2;  
7  
8     while (prime <= Math.sqrt(max)) {
```

```

9     /* Cross off remaining multiples of prime */
10    crossOff(flags, prime);
11
12    /* Find next value which is true */
13    prime = getNextPrime(flags, prime);
14 }
15
16 return flags;
17 }
18
19 void crossOff(boolean[] flags, int prime) {
20     /* Cross off remaining multiples of prime. We can start with (prime*prime),
21      * because if we have a k * prime, where k < prime, this value would have
22      * already been crossed off in a prior iteration. */
23     for (int i = prime * prime; i < flags.length; i += prime) {
24         flags[i] = false;
25     }
26 }
27
28 int getNextPrime(boolean[] flags, int prime) {
29     int next = prime + 1;
30     while (next < flags.length && !flags[next]) {
31         next++;
32     }
33     return next;
34 }
```

Of course, there are a number of optimizations that can be made to this. One simple one is to only use odd numbers in the array, which would allow us to reduce our space usage by half.

## ► Probability

Probability can be a complex topic, but it's based in a few basic laws that can be logically derived.

Let's look at a Venn diagram to visualize two events A and B. The areas of the two circles represent their relative probability, and the overlapping area is the event {A and B}.



### Probability of A and B

Imagine you were throwing a dart at this Venn diagram. What is the probability that you would land in the intersection between A and B? If you knew the odds of landing in A, and you also knew the percent of A that's also in B (that is, the odds of being in B given that you were in A), then you could express the probability as:

$$P(A \text{ and } B) = P(B \text{ given } A) \cdot P(A)$$

For example, imagine we were picking a number between 1 and 10 (inclusive). What's the probability of picking an even number *and* a number between 1 and 5? The odds of picking a number between 1 and 5 is 50%, and the odds of a number between 1 and 5 being even is 40%. So, the odds of doing both are:

$$P(x \text{ is even and } x \leq 5)$$

$$\begin{aligned} &= P(x \text{ is even given } x \leq 5) P(x \leq 5) \\ &= (2/5) * (1/2) \\ &= 1/5 \end{aligned}$$

Observe that since  $P(A \text{ and } B) = P(B \text{ given } A) P(A) = P(A \text{ given } B) P(B)$ , you can express the probability of A given B in terms of the reverse:

$$P(A \text{ given } B) = P(B \text{ given } A) P(A) / P(B)$$

The above equation is called Bayes' Theorem.

### Probability of A or B

Now, imagine you wanted to know what the probability of landing in A or B is. If you knew the odds of landing in each individually, and you also knew the odds of landing in their intersection, then you could express the probability as:

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

Logically, this makes sense. If we simply added their sizes, we would have double-counted their intersection. We need to subtract this out. We can again visualize this through a Venn diagram:



For example, imagine we were picking a number between 1 and 10 (inclusive). What's the probability of picking an even number or a number between 1 and 5? We have a 50% probability of picking an even number and a 50% probability of picking a number between 1 and 5. The odds of doing both are 20%. So the odds are:

$$\begin{aligned} &P(x \text{ is even or } x \leq 5) \\ &= P(x \text{ is even}) + P(x \leq 5) - P(x \text{ is even and } x \leq 5) \\ &= \frac{1}{2} + \frac{1}{2} - \frac{1}{5} \\ &= \frac{4}{5} \end{aligned}$$

From here, getting the special case rules for independent events and for mutually exclusive events is easy.

### Independence

If A and B are independent (that is, one happening tells you nothing about the other happening), then  $P(A \text{ and } B) = P(A) P(B)$ . This rule simply comes from recognizing that  $P(B \text{ given } A) = P(B)$ , since A indicates nothing about B.

### Mutual Exclusivity

If A and B are mutually exclusive (that is, if one happens, then the other cannot happen), then  $P(A \text{ or } B) = P(A) + P(B)$ . This is because  $P(A \text{ and } B) = 0$ , so this term is removed from the earlier  $P(A \text{ or } B)$  equation.

Many people, strangely, mix up the concepts of independence and mutual exclusivity. They are *entirely* different. In fact, two events cannot be both independent and mutually exclusive (provided both have probabilities greater than 0). Why? Because mutual exclusivity means that if one happens then the other cannot. Independence, however, says that one event happening means absolutely *nothing* about the other event. Thus, as long as two events have non-zero probabilities, they will never be both mutually exclusive and independent.

If one or both events have a probability of zero (that is, it is impossible), then the events are both independent and mutually exclusive. This is provable through a simple application of the definitions (that is, the formulas) of independence and mutual exclusivity.

### ► Start Talking

Don't panic when you get a brainteaser. Like algorithm questions, interviewers want to see how you tackle a problem; they don't expect you to immediately know the answer. Start talking, and show the interviewer how you approach a problem.

### ► Develop Rules and Patterns

In many cases, you will find it useful to write down "rules" or patterns that you discover while solving the problem. And yes, you really should write these down—it will help you remember them as you solve the problem. Let's demonstrate this approach with an example.

You have two ropes, and each takes exactly one hour to burn. How would you use them to time exactly 15 minutes? Note that the ropes are of uneven densities, so half the rope length-wise does not necessarily take half an hour to burn.

*Tip: Stop here and spend some time trying to solve this problem on your own. If you absolutely must, read through this section for hints—but do so slowly. Every paragraph will get you a bit closer to the solution.*

From the statement of the problem, we immediately know that we can time one hour. We can also time two hours, by lighting one rope, waiting until it is burnt, and then lighting the second. We can generalize this into a rule.

*Rule 1:* Given a rope that takes  $x$  minutes to burn and another that takes  $y$  minutes, we can time  $x+y$  minutes.

What else can we do with the rope? We can probably assume that lighting a rope in the middle (or anywhere other than the ends) won't do us much good. The flames would expand in both directions, and we have no idea how long it would take to burn.

However, we can light a rope at both ends. The two flames would meet after 30 minutes.

*Rule 2:* Given a rope that takes  $x$  minutes to burn, we can time  $\frac{x}{2}$  minutes.

We now know that we can time 30 minutes using a single rope. This also means that we can remove 30 minutes of burning time from the second rope, by lighting rope 1 on both ends and rope 2 on just one end.

*Rule 3:* If rope 1 takes  $x$  minutes to burn and rope 2 takes  $y$  minutes, we can turn rope 2 into a rope that takes  $(y-x)$  minutes or  $(y - \frac{x}{2})$  minutes.

Now, let's piece all of these together. We can turn rope 2 into a rope with 30 minutes of burn time. If we then light rope 2 on the other end (see rule 2), rope 2 will be done after 15 minutes.

From start to end, our approach is as follows:

1. Light rope 1 at both ends and rope 2 at one end.
2. When the two flames on Rope 1 meet, 30 minutes will have passed. Rope 2 has 30 minutes left of burn-time.

3. At that point, light Rope 2 at the other end.
4. In exactly fifteen minutes, Rope 2 will be completely burnt.

Note how solving this problem is made easier by listing out what you've learned and what "rules" you've discovered.

### ► Worst Case Shifting

Many brainteasers are worst-case minimization problems, worded either in terms of *minimizing* an action or in doing something at most a specific number of times. A useful technique is to try to "balance" the worst case. That is, if an early decision results in a skewing of the worst case, we can sometimes change the decision to balance out the worst case. This will be clearest when explained with an example.

The "nine balls" question is a classic interview question. You have nine balls. Eight are of the same weight, and one is heavier. You are given a balance which tells you only whether the left side or the right side is heavier. Find the heavy ball in just two uses of the scale.

A first approach is to divide the balls in sets of four, with the ninth ball sitting off to the side. The heavy ball is in the heavier set. If they are the same weight, then we know that the ninth ball is the heavy one. Replicating this approach for the remaining sets would result in a worst case of three weighings—one too many!

This is an imbalance in the worst case: the ninth ball takes just one weighing to discover if it's heavy, whereas others take three. If we *penalize* the ninth ball by putting more balls off to the side, we can lighten the load on the others. This is an example of "worst case balancing."

If we divide the balls into sets of three items each, we will know after just one weighing which set has the heavy one. We can even formalize this into a *rule*: given N balls, where N is divisible by 3, one use of the scale will point us to a set of  $\frac{N}{3}$  balls with the heavy ball.

For the final set of three balls, we simply repeat this: put one ball off to the side and weigh two. Pick the heavier of the two. Or, if the balls are the same weight, pick the third one.

### ► Algorithm Approaches

If you're stuck, consider applying one of the approaches for solving algorithm questions (starting on page 67). Brainteasers are often nothing more than algorithm questions with the technical aspects removed. Base Case and Build and Do It Yourself (DIY) can be especially useful.

**Additional Reading:** Useful Math (pg 629).

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## Interview Questions

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- 6.1 The Heavy Pill:** You have 20 bottles of pills. 19 bottles have 1.0 gram pills, but one has pills of weight 1.1 grams. Given a scale that provides an exact measurement, how would you find the heavy bottle? You can only use the scale once.

Hints: #186, #252, #319, #387

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- 6.2 Basketball:** You have a basketball hoop and someone says that you can play one of two games.

Game 1: You get one shot to make the hoop.

Game 2: You get three shots and you have to make two of three shots.

If  $p$  is the probability of making a particular shot, for which values of  $p$  should you pick one game or the other?

Hints: #181, #239, #284, #323

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- 6.3 Dominos:** There is an 8x8 chessboard in which two diagonally opposite corners have been cut off. You are given 31 dominos, and a single domino can cover exactly two squares. Can you use the 31 dominos to cover the entire board? Prove your answer (by providing an example or showing why it's impossible).

Hints: #367, #397

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- 6.4 Ants on a Triangle:** There are three ants on different vertices of a triangle. What is the probability of collision (between any two or all of them) if they start walking on the sides of the triangle? Assume that each ant randomly picks a direction, with either direction being equally likely to be chosen, and that they walk at the same speed.

Similarly, find the probability of collision with  $n$  ants on an  $n$ -vertex polygon.

Hints: #157, #195, #296

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- 6.5 Jugs of Water:** You have a five-quart jug, a three-quart jug, and an unlimited supply of water (but no measuring cups). How would you come up with exactly four quarts of water? Note that the jugs are oddly shaped, such that filling up exactly "half" of the jug would be impossible.

Hints: #149, #379, #400

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- 6.6 Blue-Eyed Island:** A bunch of people are living on an island, when a visitor comes with a strange order: all blue-eyed people must leave the island as soon as possible. There will be a flight out at 8:00 pm every evening. Each person can see everyone else's eye color, but they do not know their own (nor is anyone allowed to tell them). Additionally, they do not know how many people have blue eyes, although they do know that at least one person does. How many days will it take the blue-eyed people to leave?

Hints: #218, #282, #341, #370

pg 293

- 6.7 The Apocalypse:** In the new post-apocalyptic world, the world queen is desperately concerned about the birth rate. Therefore, she decrees that all families should ensure that they have one girl or else they face massive fines. If all families abide by this policy—that is, they have continue to have children until they have one girl, at which point they immediately stop—what will the gender ratio of the new generation be? (Assume that the odds of someone having a boy or a girl on any given pregnancy is equal.) Solve this out logically and then write a computer simulation of it.

Hints: #154, #160, #171, #188, #201

pg 293

- 6.8 The Egg Drop Problem:** There is a building of 100 floors. If an egg drops from the Nth floor or above, it will break. If it's dropped from any floor below, it will not break. You're given two eggs. Find N, while minimizing the number of drops for the worst case.

Hints: #156, #233, #294, #333, #357, #374, #395

pg 296

- 6.9 100 Lockers:** There are 100 closed lockers in a hallway. A man begins by opening all 100 lockers. Next, he closes every second locker. Then, on his third pass, he toggles every third locker (closes it if it is open or opens it if it is closed). This process continues for 100 passes, such that on each pass i, the man toggles every  $i$ th locker. After his 100th pass in the hallway, in which he toggles only locker #100, how many lockers are open?

Hints: #139, #172, #264, #306

pg 297

- 6.10 Poison:** You have 1000 bottles of soda, and exactly one is poisoned. You have 10 test strips which can be used to detect poison. A single drop of poison will turn the test strip positive permanently. You can put any number of drops on a test strip at once and you can reuse a test strip as many times as you'd like (as long as the results are negative). However, you can only run tests once per day and it takes seven days to return a result. How would you figure out the poisoned bottle in as few days as possible?

FOLLOW UP

Write code to simulate your approach.

Hints: #146, #163, #183, #191, #205, #221, #230, #241, #249

pg 298

Additional Problems: Moderate Problems (#16.5), Hard Problems (#17.19)

Hints start on page 662.

# 7

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## Object-Oriented Design

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**O**bject-oriented design questions require a candidate to sketch out the classes and methods to implement technical problems or real-life objects. These problems give—or at least are believed to give—an interviewer insight into your coding style.

These questions are not so much about regurgitating design patterns as they are about demonstrating that you understand how to create elegant, maintainable object-oriented code. Poor performance on this type of question may raise serious red flags.

### ► How to Approach

Regardless of whether the object is a physical item or a technical task, object-oriented design questions can be tackled in similar ways. The following approach will work well for many problems.

#### Step 1: Handle Ambiguity

Object-oriented design (OOD) questions are often intentionally vague in order to test whether you'll make assumptions or if you'll ask clarifying questions. After all, a developer who just codes something without understanding what she is expected to create wastes the company's time and money, and may create much more serious issues.

When being asked an object-oriented design question, you should inquire *who* is going to use it and *how* they are going to use it. Depending on the question, you may even want to go through the "six Ws": who, what, where, when, how, why.

For example, suppose you were asked to describe the object-oriented design for a coffee maker. This seems straightforward enough, right? Not quite.

Your coffee maker might be an industrial machine designed to be used in a massive restaurant servicing hundreds of customers per hour and making ten different kinds of coffee products. Or it might be a very simple machine, designed to be used by the elderly for just simple black coffee. These use cases will significantly impact your design.

#### Step 2: Define the Core Objects

Now that we understand what we're designing, we should consider what the "core objects" in a system are. For example, suppose we are asked to do the object-oriented design for a restaurant. Our core objects might be things like **Table**, **Guest**, **Party**, **Order**, **Meal**, **Employee**, **Server**, and **Host**.

### Step 3: Analyze Relationships

Having more or less decided on our core objects, we now want to analyze the relationships between the objects. Which objects are members of which other objects? Do any objects inherit from any others? Are relationships many-to-many or one-to-many?

For example, in the restaurant question, we may come up with the following design:

- Party should have an array of Guests .
- Server and Host inherit from Employee .
- Each Table has one Party , but each Party may have multiple Tables .
- There is one Host for the Restaurant .

Be very careful here—you can often make incorrect assumptions. For example, a single Table may have multiple Parties (as is common in the trendy “communal tables” at some restaurants). You should talk to your interviewer about how general purpose your design should be.

### Step 4: Investigate Actions

At this point, you should have the basic outline of your object-oriented design. What remains is to consider the key actions that the objects will take and how they relate to each other. You may find that you have forgotten some objects, and you will need to update your design.

For example, a Party walks into the Restaurant , and a Guest requests a Table from the Host . The Host looks up the Reservation and, if it exists, assigns the Party to a Table . Otherwise, the Party is added to the end of the list . When a Party leaves, the Table is freed and assigned to a new Party in the list .

## ► Design Patterns

Because interviewers are trying to test your capabilities and not your knowledge, design patterns are mostly beyond the scope of an interview. However, the Singleton and Factory Method design patterns are widely used in interviews, so we will cover them here.

There are far more design patterns than this book could possibly discuss. A great way to improve your software engineering skills is to pick up a book that focuses on this area specifically.

Be careful you don’t fall into a trap of constantly trying to find the “right” design pattern for a particular problem. You should create the design that works for that problem. In some cases it might be an established pattern, but in many other cases it is not.

### Singleton Class

The Singleton pattern ensures that a class has only one instance and ensures access to the instance through the application. It can be useful in cases where you have a “global” object with exactly one instance. For example, we may want to implement Restaurant such that it has exactly one instance of Restaurant .

```
1  public class Restaurant {  
2      private static Restaurant _instance = null;  
3      protected Restaurant() { ... }  
4      public static Restaurant getInstance() {  
5          if (_instance == null) {  
6              _instance = new Restaurant();  
7          }  
8      }  
9  }
```

```

8     return _instance;
9 }
10 }
```

It should be noted that many people dislike the Singleton design pattern, even calling it an “anti-pattern.” One reason for this is that it can interfere with unit testing.

### Factory Method

The Factory Method offers an interface for creating an instance of a class, with its subclasses deciding which class to instantiate. You might want to implement this with the creator class being abstract and not providing an implementation for the Factory method. Or, you could have the Creator class be a concrete class that provides an implementation for the Factory method. In this case, the Factory method would take a parameter representing which class to instantiate.

```

1 public class CardGame {
2     public static CardGame createCardGame(GameType type) {
3         if (type == GameType.Poker) {
4             return new PokerGame();
5         } else if (type == GameType.BlackJack) {
6             return new BlackJackGame();
7         }
8     return null;
9 }
10 }
```

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### Interview Questions

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- 7.1 Deck of Cards:** Design the data structures for a generic deck of cards. Explain how you would subclass the data structures to implement blackjack.

Hints: #153, #275

pg 305

- 7.2 Call Center:** Imagine you have a call center with three levels of employees: respondent, manager, and director. An incoming telephone call must be first allocated to a respondent who is free. If the respondent can't handle the call, he or she must escalate the call to a manager. If the manager is not free or not able to handle it, then the call should be escalated to a director. Design the classes and data structures for this problem. Implement a method `dispatchCall()` which assigns a call to the first available employee.

Hints: #363

pg 307

- 7.3 Jukebox:** Design a musical jukebox using object-oriented principles.

Hints: #198

pg 310

- 7.4 Parking Lot:** Design a parking lot using object-oriented principles.

Hints: #258

pg 312

- 7.5 Online Book Reader:** Design the data structures for an online book reader system.

Hints: #344

pg 318

- 7.6 Jigsaw:** Implement an NxN jigsaw puzzle. Design the data structures and explain an algorithm to solve the puzzle. You can assume that you have a `fitsWith` method which, when passed two puzzle edges, returns true if the two edges belong together.

Hints: #192, #238, #283

pg 318

- 7.7 Chat Server:** Explain how you would design a chat server. In particular, provide details about the various backend components, classes, and methods. What would be the hardest problems to solve?

Hints: #213, #245, #271

pg 326

- 7.8 Othello:** Othello is played as follows: Each Othello piece is white on one side and black on the other. When a piece is surrounded by its opponents on both the left and right sides, or both the top and bottom, it is said to be captured and its color is flipped. On your turn, you must capture at least one of your opponent's pieces. The game ends when either user has no more valid moves. The win is assigned to the person with the most pieces. Implement the object-oriented design for Othello.

Hints: #179, #228

pg 326

- 7.9 Circular Array:** Implement a `CircularArray` class that supports an array-like data structure which can be efficiently rotated. If possible, the class should use a generic type (also called a template), and should support iteration via the standard for `(Obj o : circularArray)` notation.

Hints: #389

pg 329

- 7.10 Minesweeper:** Design and implement a text-based Minesweeper game. Minesweeper is the classic single-player computer game where an  $N \times N$  grid has 8 mines (or bombs) hidden across the grid. The remaining cells are either blank or have a number behind them. The numbers reflect the number of bombs in the surrounding eight cells. The user then uncovers a cell. If it is a bomb, the player loses. If it is a number, the number is exposed. If it is a blank cell, this cell and all adjacent blank cells (up to and including the surrounding numeric cells) are exposed. The player wins when all non-bomb cells are exposed. The player can also flag certain places as potential bombs. This doesn't affect game play, other than to block the user from accidentally clicking a cell that is thought to have a bomb. (Tip for the reader: if you're not familiar with this game, please play a few rounds online first.)

This is a fully exposed board with 3 bombs. This is not shown to the user.

1	1	1				
1	*	1				
2	2	2				
1	*	1				
1	1	1				
			1	1	1	
			1	*	1	

The player initially sees a board with nothing exposed.

?	?	?	?	?	?	?
?	?	?	?	?	?	?
?	?	?	?	?	?	?
?	?	?	?	?	?	?
?	?	?	?	?	?	?
?	?	?	?	?	?	?
?	?	?	?	?	?	?

Clicking on cell (row = 1, col = 0) would expose this:

1	?	?	?	?	?	?
1	?	?	?	?	?	?
2	?	?	?	?	?	?
1	?	?	?	?	?	?
1	1	1	?	?	?	?
			1	?	?	?
			1	?	?	?

The user wins when everything other than bombs has been exposed.

1	1	1				
1	?	1				
2	2	2				
1	?	1				
1	1	1				
			1	1	1	
			1	?	1	

Hints: #351, #361, #377, #386, #399

pg 332

- 7.11 File System:** Explain the data structures and algorithms that you would use to design an in-memory file system. Illustrate with an example in code where possible.

Hints: #141, #216

pg 337

- 7.12 Hash Table:** Design and implement a hash table which uses chaining (linked lists) to handle collisions.

Hints: #287, #307

pg 339

Additional Questions: Threads and Locks (#16.3)

Hints start on page 662.

# 8

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## Recursion and Dynamic Programming

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**W**hile there are a large number of recursive problems, many follow similar patterns. A good hint that a problem is recursive is that it can be built off of subproblems.

When you hear a problem beginning with the following statements, it's often (though not always) a good candidate for recursion: "Design an algorithm to compute the nth ...," "Write code to list the first n...," "Implement a method to compute all...", and so on.

**Tip:** In my experience coaching candidates, people typically have about 50% accuracy in their "this sounds like a recursive problem" instinct. Use that instinct, since that 50% is valuable. But don't be afraid to look at the problem in a different way, even if you initially thought it seemed recursive. There's also a 50% chance that you were wrong.

Practice makes perfect! The more problems you do, the easier it will be to recognize recursive problems.

### ► How to Approach

Recursive solutions, by definition, are built off of solutions to subproblems. Many times, this will mean simply to compute  $f(n)$  by adding something, removing something, or otherwise changing the solution for  $f(n-1)$ . In other cases, you might solve the problem for the first half of the data set, then the second half, and then merge those results.

There are many ways you might divide a problem into subproblems. Three of the most common approaches to develop an algorithm are bottom-up, top-down, and half-and-half.

#### Bottom-Up Approach

The bottom-up approach is often the most intuitive. We start with knowing how to solve the problem for a simple case, like a list with only one element. Then we figure out how to solve the problem for two elements, then for three elements, and so on. The key here is to think about how you can *build* the solution for one case off of the previous case (or multiple previous cases).

#### Top-Down Approach

The top-down approach can be more complex since it's less concrete. But sometimes, it's the best way to think about the problem.

In these problems, we think about how we can divide the problem for case N into subproblems.

Be careful of overlap between the cases.

## Half-and-Half Approach

In addition to top-down and bottom-up approaches, it's often effective to divide the data set in half.

For example, binary search works with a "half-and-half" approach. When we look for an element in a sorted array, we first figure out which half of the array contains the value. Then we recurse and search for it in that half.

Merge sort is also a "half-and-half" approach. We sort each half of the array and then merge together the sorted halves.

## ► Recursive vs. Iterative Solutions

Recursive algorithms can be very space inefficient. Each recursive call adds a new layer to the stack, which means that if your algorithm recurses to a depth of  $n$ , it uses at least  $O(n)$  memory.

For this reason, it's often better to implement a recursive algorithm iteratively. *All* recursive algorithms can be implemented iteratively, although sometimes the code to do so is much more complex. Before diving into recursive code, ask yourself how hard it would be to implement it iteratively, and discuss the tradeoffs with your interviewer.

## ► Dynamic Programming & Memoization

Although people make a big deal about how scary dynamic programming problems are, there's really no need to be afraid of them. In fact, once you get the hang of them, these can actually be very easy problems.

Dynamic programming is mostly just a matter of taking a recursive algorithm and finding the overlapping subproblems (that is, the repeated calls). You then cache those results for future recursive calls.

Alternatively, you can study the pattern of the recursive calls and implement something iterative. You still "cache" previous work.

A note on terminology: Some people call top-down dynamic programming "memoization" and only use "dynamic programming" to refer to bottom-up work. We do not make such a distinction here. We call both dynamic programming.

One of the simplest examples of dynamic programming is computing the  $n$ th Fibonacci number. A good way to approach such a problem is often to implement it as a normal recursive solution, and then add the caching part.

### Fibonacci Numbers

Let's walk through an approach to compute the  $n$ th Fibonacci number.

#### Recursive

We will start with a recursive implementation. Sounds simple, right?

```
1 int fibonacci(int i) {
2     if (i == 0) return 0;
3     if (i == 1) return 1;
4     return fibonacci(i - 1) + fibonacci(i - 2);
5 }
```

What is the runtime of this function? Think for a second before you answer.

If you said  $O(n)$  or  $O(n^2)$  (as many people do), think again. Study the code path that the code takes. Drawing the code paths as a tree (that is, the recursion tree) is useful on this and many recursive problems.



Observe that the leaves on the tree are all `fib(1)` and `fib(0)`. Those signify the base cases.

The total number of nodes in the tree will represent the runtime, since each call only does  $O(1)$  work outside of its recursive calls. Therefore, the number of calls is the runtime.

**Tip:** Remember this for future problems. Drawing the recursive calls as a tree is a great way to figure out the runtime of a recursive algorithm.

How many nodes are in the tree? Until we get down to the base cases (leaves), each node has two children. Each node branches out twice.

The root node has two children. Each of those children has two children (so four children total in the “grandchildren” level). Each of those grandchildren has two children, and so on. If we do this  $n$  times, we’ll have roughly  $O(2^n)$  nodes. This gives us a runtime of roughly  $O(2^n)$ .

Actually, it’s slightly better than  $O(2^n)$ . If you look at the subtree, you might notice that (excluding the leaf nodes and those immediately above it) the right subtree of any node is always smaller than the left subtree. If they were the same size, we’d have an  $O(2^n)$  runtime. But since the right and left subtrees are not the same size, the true runtime is closer to  $O(1 \cdot 6^n)$ . Saying  $O(2^n)$  is still technically correct though as it describes an upper bound on the runtime (see “Big O, Big Theta, and Big Omega” on page 39). Either way, we still have an exponential runtime.

Indeed, if we implemented this on a computer, we’d see the number of seconds increase exponentially.



We should look for a way to optimize this.

*Top-Down Dynamic Programming (or Memoization)*

Study the recursion tree. Where do you see identical nodes?

There are lots of identical nodes. For example, `fib(3)` appears twice and `fib(2)` appears three times. Why should we recompute these from scratch each time?

In fact, when we call `fib(n)`, we shouldn't have to do much more than  $O(n)$  calls, since there's only  $O(n)$  possible values we can throw at `fib`. Each time we compute `fib(i)`, we should just cache this result and use it later.

This is exactly what memoization is.

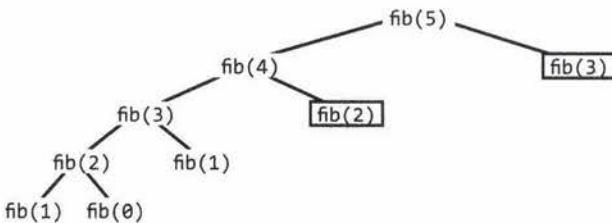
With just a small modification, we can tweak this function to run in  $O(n)$  time. We simply cache the results of `fibonacci(i)` between calls.

```

1 int fibonacci(int n) {
2     return fibonacci(n, new int[n + 1]);
3 }
4
5 int fibonacci(int i, int[] memo) {
6     if (i == 0 || i == 1) return i;
7
8     if (memo[i] == 0) {
9         memo[i] = fibonacci(i - 1, memo) + fibonacci(i - 2, memo);
10    }
11    return memo[i];
12 }
```

While the first recursive function may take over a minute to generate the 50th Fibonacci number on a typical computer, the dynamic programming method can generate the 10,000th Fibonacci number in just fractions of a millisecond. (Of course, with this exact code, the `int` would have overflowed very early on.)

Now, if we draw the recursion tree, it looks something like this (the black boxes represent cached calls that returned immediately):



How many nodes are in this tree now? We might notice that the tree now just shoots straight down, to a depth of roughly  $n$ . Each node of those nodes has one other child, resulting in roughly  $2n$  children in the tree. This gives us a runtime of  $O(n)$ .

Often it can be useful to picture the recursion tree as something like this:



This is *not* actually how the recursion occurred. However, by expanding the further up nodes rather than the

lower nodes, you have a tree that grows wide before it grows deep. (It's like doing this breadth-first rather than depth-first.) Sometimes this makes it easier to compute the number of nodes in the tree. All you're really doing is changing which nodes you expand and which ones return cached values. Try this if you're stuck on computing the runtime of a dynamic programming problem.

### *Bottom-Up Dynamic Programming*

We can also take this approach and implement it with bottom-up dynamic programming. Think about doing the same things as the recursive memoized approach, but in reverse.

First, we compute `fib(1)` and `fib(0)`, which are already known from the base cases. Then we use those to compute `fib(2)`. Then we use the prior answers to compute `fib(3)`, then `fib(4)`, and so on.

```
1 int fibonacci(int n) {  
2     if (n == 0) return 0;  
3     else if (n == 1) return 1;  
4  
5     int[] memo = new int[n];  
6     memo[0] = 0;  
7     memo[1] = 1;  
8     for (int i = 2; i < n; i++) {  
9         memo[i] = memo[i - 1] + memo[i - 2];  
10    }  
11    return memo[n - 1] + memo[n - 2];  
12 }
```

If you really think about how this works, you only use `memo[i]` for `memo[i+1]` and `memo[i+2]`. You don't need it after that. Therefore, we can get rid of the memo table and just store a few variables.

```
1 int fibonacci(int n) {  
2     if (n == 0) return 0;  
3     int a = 0;  
4     int b = 1;  
5     for (int i = 2; i < n; i++) {  
6         int c = a + b;  
7         a = b;  
8         b = c;  
9     }  
10    return a + b;  
11 }
```

This is basically storing the results from the last two Fibonacci values into `a` and `b`. At each iteration, we compute the next value (`c = a + b`) and then move (`b, c = a + b`) into (`a, b`).

This explanation might seem like overkill for such a simple problem, but truly understanding this process will make more difficult problems much easier. Going through the problems in this chapter, many of which use dynamic programming, will help solidify your understanding.

**Additional Reading:** Proof by Induction (pg 631).

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### Interview Questions

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- 8.1 Triple Step:** A child is running up a staircase with  $n$  steps and can hop either 1 step, 2 steps, or 3 steps at a time. Implement a method to count how many possible ways the child can run up the stairs.

Hints: #152, #178, #217, #237, #262, #359

pg 342

- 8.2 Robot in a Grid:** Imagine a robot sitting on the upper left corner of grid with  $r$  rows and  $c$  columns. The robot can only move in two directions, right and down, but certain cells are “off limits” such that the robot cannot step on them. Design an algorithm to find a path for the robot from the top left to the bottom right.

Hints: #331, #360, #388

pg 344

- 8.3 Magic Index:** A magic index in an array  $A[0 \dots n-1]$  is defined to be an index such that  $A[i] = i$ . Given a sorted array of distinct integers, write a method to find a magic index, if one exists, in array  $A$ .

FOLLOW UP

What if the values are not distinct?

Hints: #170, #204, #240, #286, #340

pg 346

- 8.4 Power Set:** Write a method to return all subsets of a set.

Hints: #273, #290, #338, #354, #373

pg 348

- 8.5 Recursive Multiply:** Write a recursive function to multiply two positive integers without using the `*` operator. You can use addition, subtraction, and bit shifting, but you should minimize the number of those operations.

Hints: #166, #203, #227, #234, #246, #280

pg 350

- 8.6 Towers of Hanoi:** In the classic problem of the Towers of Hanoi, you have 3 towers and  $N$  disks of different sizes which can slide onto any tower. The puzzle starts with disks sorted in ascending order of size from top to bottom (i.e., each disk sits on top of an even larger one). You have the following constraints:

- (1) Only one disk can be moved at a time.
- (2) A disk is slid off the top of one tower onto another tower.
- (3) A disk cannot be placed on top of a smaller disk.

Write a program to move the disks from the first tower to the last using stacks.

Hints: #144, #224, #250, #272, #318

pg 353

- 8.7 Permutations without Dups:** Write a method to compute all permutations of a string of unique characters.

Hints: #150, #185, #200, #267, #278, #309, #335, #356

pg 355

- 8.8 Permutations with Dups:** Write a method to compute all permutations of a string whose characters are not necessarily unique. The list of permutations should not have duplicates.

Hints: #161, #190, #222, #255

pg 357

- 8.9 Paren:** Implement an algorithm to print all valid (e.g., properly opened and closed) combinations of  $n$  pairs of parentheses.

EXAMPLE

Input: 3

Output: ((())), ((())(), (())()), ()((())), ()()()

Hints: #138, #174, #187, #209, #243, #265, #295

pg 359

- 8.10 Paint Fill:** Implement the “paint fill” function that one might see on many image editing programs. That is, given a screen (represented by a two-dimensional array of colors), a point, and a new color, fill in the surrounding area until the color changes from the original color.

Hints: #364, #382

pg 361

- 8.11 Coins:** Given an infinite number of quarters (25 cents), dimes (10 cents), nickels (5 cents), and pennies (1 cent), write code to calculate the number of ways of representing  $n$  cents.

Hints: #300, #324, #343, #380, #394

pg 362

- 8.12 Eight Queens:** Write an algorithm to print all ways of arranging eight queens on an 8x8 chess board so that none of them share the same row, column, or diagonal. In this case, “diagonal” means all diagonals, not just the two that bisect the board.

Hints: #308, #350, #371

pg 364

- 8.13 Stack of Boxes:** You have a stack of  $n$  boxes, with widths  $w_i$ , heights  $h_i$ , and depths  $d_i$ . The boxes cannot be rotated and can only be stacked on top of one another if each box in the stack is strictly larger than the box above it in width, height, and depth. Implement a method to compute the height of the tallest possible stack. The height of a stack is the sum of the heights of each box.

Hints: #155, #194, #214, #260, #322, #368, #378

pg 366

- 8.14 Boolean Evaluation:** Given a boolean expression consisting of the symbols 0 (false), 1 (true), & (AND), | (OR), and ^ (XOR), and a desired boolean result value  $result$ , implement a function to count the number of ways of parenthesizing the expression such that it evaluates to  $result$ .

EXAMPLE

```
countEval("1^0|0|1", false) -> 2  
countEval("0&0&0&1^1|0", true) -> 10
```

Hints: #148, #168, #197, #305, #327

pg 368

Additional Questions: Linked Lists (#2.2, #2.5, #2.6), Stacks and Queues (#3.3), Trees and Graphs (#4.2, #4.3, #4.4, #4.5, #4.8, #4.10, #4.11, #4.12), Math and Logic Puzzles (#6.6), Sorting and Searching (#10.5, #10.9, #10.10), C++ (#12.8), Moderate Problems (#16.11), Hard Problems (#17.4, #17.6, #17.8, #17.12, #17.13, #17.15, #17.16, #17.24, #17.25).

Hints start on page 662.

# 9

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## System Design and Scalability

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**D**espite how intimidating they seem, scalability questions can be among the easiest questions. There are no “gotchas,” no tricks, and no fancy algorithms—at least not usually. What trips up many people is that they believe there’s something “magic” to these problems—some hidden bit of knowledge.

It’s not like that. These questions are simply designed to see how you would perform in the real world. If you were asked by your manager to design some system, what would you do?

That’s why you should approach it just like this. Tackle the problem by doing it just like you would at work. Ask questions. Engage the interviewer. Discuss the tradeoffs.

We will touch on some key concepts in this chapter, but recognize it’s not really about memorizing these concepts. Yes, understanding some big components of system design can be useful, but it’s much more about the process you take. There are good solutions and bad solutions. There is no perfect solution.

### ► Handling the Questions

- **Communicate:** A key goal of system design questions is to evaluate your ability to communicate. Stay engaged with the interviewer. Ask them questions. Be open about the issues of your system.
- **Go broad first:** Don’t dive straight into the algorithm part or get excessively focused on one part.
- **Use the whiteboard:** Using a whiteboard helps your interviewer follow your proposed design. Get up to the whiteboard in the very beginning and use it to draw a picture of what you’re proposing.
- **Acknowledge interviewer concerns:** Your interviewer will likely jump in with concerns. Don’t brush them off; validate them. Acknowledge the issues your interviewer points out and make changes accordingly.
- **Be careful about assumptions:** An incorrect assumption can dramatically change the problem. For example, if your system produces analytics / statistics for a dataset, it matters whether those analytics must be totally up to date.
- **State your assumptions explicitly:** When you do make assumptions, state them. This allows your interviewer to correct you if you’re mistaken, and shows that you at least know what assumptions you’re making.
- **Estimate when necessary:** In many cases, you might not have the data you need. For example, if you’re designing a web crawler, you might need to estimate how much space it will take to store all the URLs. You can estimate this with other data you know.
- **Drive:** As the candidate, you should stay in the driver’s seat. This doesn’t mean you don’t talk to your interviewer; in fact, you *must* talk to your interviewer. However, you should be driving through the ques-

tion. Ask questions. Be open about tradeoffs. Continue to go deeper. Continue to make improvements. These questions are largely about the process rather than the ultimate design.

### ► Design: Step-By-Step

If your manager asked you to design a system such as TinyURL, you probably wouldn't just say, "Okay", then lock yourself in your office to design it by yourself. You would probably have a lot more questions before you do it. This is the way you should handle it in an interview.

#### **Step 1: Scope the Problem**

You can't design a system if you don't know what you're designing. Scoping the problem is important because you want to ensure that you're building what the interviewer wants and because this might be something that interviewer is specifically evaluating.

If you're asked something such as "Design TinyURL", you'll want to understand what exactly you need to implement. Will people be able to specify their own short URLs? Or will it all be auto-generated? Will you need to keep track of any stats on the clicks? Should the URLs stay alive forever, or do they have a timeout?

These are questions that must be answered before going further.

Make a list here as well of the major features or use cases. For example, for TinyURL, it might be:

- Shortening a URL to a TinyURL.
- Analytics for a URL.
- Retrieving the URL associated with a TinyURL.
- User accounts and link management.

#### **Step 2: Make Reasonable Assumptions**

It's okay to make some assumptions (when necessary), but they should be reasonable. For example, it would not be reasonable to assume that your system only needs to process 100 users per day, or to assume that you have infinite memory available.

However, it might be reasonable to design for a max of one million new URLs per day. Making this assumption can help you calculate how much data your system might need to store.

Some assumptions might take some "product sense" (which is not a bad thing). For example, is it okay for the data to be stale by a max of ten minutes? That all depends. If it takes 10 minutes for a just-entered URL to work, that's a deal-breaking issue. People usually want these URLs to be active immediately. However, if the statistics are ten minutes out of date, that might be okay. Talk to your interviewer about these sorts of assumptions.

#### **Step 3: Draw the Major Components**

Get up out of that chair and go to the whiteboard. Draw a diagram of the major components. You might have something like a frontend server (or set of servers) that pull data from the backend's data store. You might have another set of servers that crawl the internet for some data, and another set that process analytics. Draw a picture of what this system might look like.

Walk through your system from end-to-end to provide a flow. A user enters a new URL. Then what?

It may help here to ignore major scalability challenges and just pretend that the simple, obvious approaches will be okay. You'll handle the big issues in Step 4.

### Step 4: Identify the Key Issues

Once you have a basic design in mind, focus on the key issues. What will be the bottlenecks or major challenges in the system?

For example, if you were designing TinyURL, one situation you might consider is that while some URLs will be infrequently accessed, others can suddenly peak. This might happen if a URL is posted on Reddit or another popular forum. You don't necessarily want to constantly hit the database.

Your interviewer might provide some guidance here. If so, take this guidance and use it.

### Step 5: Redesign for the Key Issues

Once you have identified the key issues, it's time to adjust your design for it. You might find that it involves a major redesign or just some minor tweaking (like using a cache).

Stay up at the whiteboard here and update your diagram as your design changes.

Be open about any limitations in your design. Your interviewer will likely be aware of them, so it's important to communicate that you're aware of them, too.

## ► Algorithms that Scale: Step-By-Step

In some cases, you're not being asked to design an entire system. You're just being asked to design a single feature or algorithm, but you have to do it in a scalable way. Or, there might be one algorithm part that is the "real" focus of a broader design question.

In these cases, try the following approach.

### Step 1: Ask Questions

As in the earlier approach, ask questions to make sure you really understand the question. There might be details the interviewer left out (intentionally or unintentionally). You can't solve a problem if you don't understand exactly what the problem is.

### Step 2: Make Believe

Pretend that the data can all fit on one machine and there are no memory limitations. How would you solve the problem? The answer to this question will provide the general outline for your solution.

### Step 3: Get Real

Now go back to the original problem. How much data can you fit on one machine, and what problems will occur when you split up the data? Common problems include figuring out how to logically divide the data up, and how one machine would identify where to look up a different piece of data.

### Step 4: Solve Problems

Finally, think about how to solve the issues you identified in Step 2. Remember that the solution for each issue might be to actually remove the issue entirely, or it might be to simply mitigate the issue. Usually, you

can continue using (with modifications) the approach you outlined in Step 1, but occasionally you will need to fundamentally alter the approach.

Note that an iterative approach is typically useful. That is, once you have solved the problems from Step 3, new problems may have emerged, and you must tackle those as well.

Your goal is not to re-architect a complex system that companies have spent millions of dollars building, but rather to demonstrate that you can analyze and solve problems. Poking holes in your own solution is a fantastic way to demonstrate this.

### ► Key Concepts

While system design questions aren't really tests of what you know, certain concepts can make things a lot easier. We will give a brief overview here. All of these are deep, complex topics, so we encourage you to use online resources for more research.

#### Horizontal vs. Vertical Scaling

A system can be scaled one of two ways.

- Vertical scaling means increasing the resources of a specific node. For example, you might add additional memory to a server to improve its ability to handle load changes.
- Horizontal scaling means increasing the number of nodes. For example, you might add additional servers, thus decreasing the load on any one server.

Vertical scaling is generally easier than horizontal scaling, but it's limited. You can only add so much memory or disk space.

#### Load Balancer

Typically, some frontend parts of a scalable website will be thrown behind a load balancer. This allows a system to distribute the load evenly so that one server doesn't crash and take down the whole system. To do so, of course, you have to build out a network of cloned servers that all have essentially the same code and access to the same data.

#### Database Denormalization and NoSQL

Joins in a relational database such as SQL can get very slow as the system grows bigger. For this reason, you would generally avoid them.

Denormalization is one part of this. Denormalization means adding redundant information into a database to speed up reads. For example, imagine a database describing projects and tasks (where a project can have multiple tasks). You might need to get the project name and the task information. Rather than doing a join across these tables, you can store the project name within the task table (in addition to the project table).

Or, you can go with a NoSQL database. A NoSQL database does not support joins and might structure data in a different way. It is designed to scale better.

#### Database Partitioning (Sharding)

Sharding means splitting the data across multiple machines while ensuring you have a way of figuring out which data is on which machine.

A few common ways of partitioning include:

- **Vertical Partitioning:** This is basically partitioning by feature. For example, if you were building a social network, you might have one partition for tables relating to profiles, another one for messages, and so on. One drawback of this is that if one of these tables gets very large, you might need to repartition that database (possibly using a different partitioning scheme).
- **Key-Based (or Hash-Based) Partitioning:** This uses some part of the data (for example an ID) to partition it. A very simple way to do this is to allocate  $N$  servers and put the data on  $\text{mod}(\text{key}, N)$ . One issue with this is that the number of servers you have is effectively fixed. Adding additional servers means reallocating all the data—a very expensive task.
- **Directory-Based Partitioning:** In this scheme, you maintain a lookup table for where the data can be found. This makes it relatively easy to add additional servers, but it comes with two major drawbacks. First, the lookup table can be a single point of failure. Second, constantly accessing this table impacts performance.

Many architectures actually end up using multiple partitioning schemes.

### Caching

An in-memory cache can deliver very rapid results. It is a simple key-value pairing and typically sits between your application layer and your data store.

When an application requests a piece of information, it first tries the cache. If the cache does not contain the key, it will then look up the data in the data store. (At this point, the data might—or might not—be stored in the data store.)

When you cache, you might cache a query and its results directly. Or, alternatively, you can cache the specific object (for example, a rendered version of a part of the website, or a list of the most recent blog posts).

### Asynchronous Processing & Queues

Slow operations should ideally be done asynchronously. Otherwise, a user might get stuck waiting and waiting for a process to complete.

In some cases, we can do this in advance (i.e., we can pre-process). For example, we might have a queue of jobs to be done that update some part of the website. If we were running a forum, one of these jobs might be to re-render a page that lists the most popular posts and the number of comments. That list might end up being slightly out of date, but that's perhaps okay. It's better than a user stuck waiting on the website to load simply because someone added a new comment and invalidated the cached version of this page.

In other cases, we might tell the user to wait and notify them when the process is done. You've probably seen this on websites before. Perhaps you enabled some new part of a website and it says it needs a few minutes to import your data, but you'll get a notification when it's done.

### Networking Metrics

Some of the most important metrics around networking include:

- **Bandwidth:** This is the maximum amount of data that can be transferred in a unit of time. It is typically expressed in bits per second (or some similar ways, such as gigabytes per second).
- **Throughput:** Whereas bandwidth is the maximum data that can be transferred in a unit of time, throughput is the actual amount of data that is transferred.
- **Latency:** This is how long it takes data to go from one end to the other. That is, it is the delay between the sender sending information (even a very small chunk of data) and the receiver receiving it.

Imagine you have a conveyor belt that transfers items across a factory. Latency is the time it takes an item to go from one side to another. Throughput is the number of items that roll off the conveyor belt per second.

- Building a fatter conveyor belt will not change latency. It will, however, change throughput and bandwidth. You can get more items on the belt, thus transferring more in a given unit of time.
- Shortening the belt will decrease latency, since items spend less time in transit. It won't change the throughput or bandwidth. The same number of items will roll off the belt per unit of time.
- Making a faster conveyor belt will change all three. The time it takes an item to travel across the factory decreases. More items will also roll off the conveyor belt per unit of time.
- Bandwidth is the number of items that can be transferred per unit of time, in the best possible conditions. Throughput is the time it really takes, when the machines perhaps aren't operating smoothly.

Latency can be easy to disregard, but it can be very important in particular situations. For example, if you're playing certain online games, latency can be a very big deal. How can you play a typical online sports game (like a two-player football game) if you aren't notified very quickly of your opponent's movement? Additionally, unlike throughput where at least you have the option of speeding things up through data compression, there is often little you can do about latency.

### MapReduce

MapReduce is often associated with Google, but it's used much more broadly than that. A MapReduce program is typically used to process large amounts of data.

As its name suggests, a MapReduce program requires you to write a Map step and a Reduce step. The rest is handled by the system.

- Map takes in some data and emits a `<key, value>` pair.
- Reduce takes a key and a set of associated values and "reduces" them in some way, emitting a new key and value. The results of this might be fed back into the Reduce program for more reducing.

MapReduce allows us to do a lot of processing in parallel, which makes processing huge amounts of data more scalable.

For more information, see "MapReduce" on page 642.

### ► Considerations

In addition to the earlier concepts to learn, you should consider the following issues when designing a system.

- **Failures:** Essentially any part of a system can fail. You'll need to plan for many or all of these failures.
- **Availability and Reliability:** Availability is a function of the percentage of time the system is operational. Reliability is a function of the probability that the system is operational for a certain unit of time.
- **Read-heavy vs. Write-heavy:** Whether an application will do a lot of reads or a lot of writes impacts the design. If it's write-heavy, you could consider queuing up the writes (but think about potential failure here!). If it's read-heavy, you might want to cache. Other design decisions could change as well.
- **Security:** Security threats can, of course, be devastating for a system. Think about the types of issues a system might face and design around those.

This is just to get you started with the potential issues for a system. Remember to be open in your interview about the tradeoffs.

## ► There is no “perfect” system.

There is no single design for TinyURL or Google Maps or any other system that works perfectly (although there are a great number that would work terribly). There are always tradeoffs. Two people could have substantially different designs for a system, with both being excellent given different assumptions.

Your goal in these problems is to be able to understand use cases, scope a problem, make reasonable assumptions, create a solid design based on those assumptions, and be open about the weaknesses of your design. Do not expect something perfect.

## ► Example Problem

*Given a list of millions of documents, how would you find all documents that contain a list of words? The words can appear in any order, but they must be complete words. That is, “book” does not match “bookkeeper.”*

Before we start solving the problem, we need to understand whether this is a one time only operation, or if this `findWords` procedure will be called repeatedly. Let's assume that we will be calling `findWords` many times for the same set of documents, and, therefore, we can accept the burden of pre-processing.

### Step 1

The first step is to pretend we just have a few dozen documents. How would we implement `findWords` in this case? (Tip: stop here and try to solve this yourself before reading on.)

One way to do this is to pre-process each document and create a hash table index. This hash table would map from a word to a list of the documents that contain that word.

```
“books” -> {doc2, doc3, doc6, doc8}  
“many” -> {doc1, doc3, doc7, doc8, doc9}
```

To search for “many books,” we would simply do an intersection on the values for “books” and “many”, and return {doc3, doc8} as the result.

### Step 2

Now go back to the original problem. What problems are introduced with millions of documents? For starters, we probably need to divide up the documents across many machines. Also, depending on a variety of factors, such as the number of possible words and the repetition of words in a document, we may not be able to fit the full hash table on one machine. Let's assume that this is the case.

This division introduces the following key concerns:

1. How will we divide up our hash table? We could divide it up by keyword, such that a given machine contains the full document list for a given word. Or, we could divide by document, such that a machine contains the keyword mapping for only a subset of the documents.
2. Once we decide how to divide up the data, we may need to process a document on one machine and push the results off to other machines. What does this process look like? (Note: if we divide the hash table by document, this step may not be necessary.)
3. We will need a way of knowing which machine holds a piece of data. What does this lookup table look like, and where is it stored?

These are just three concerns. There may be many others.

### Step 3

In Step 3, we find solutions to each of these issues. One solution is to divide up the words alphabetically by keyword, such that each machine controls a range of words (e.g., “after” through “apple”).

We can implement a simple algorithm in which we iterate through the keywords alphabetically, storing as much data as possible on one machine. When that machine is full, we can move to the next machine.

The advantage of this approach is that the lookup table is small and simple (since it must only specify a range of values), and each machine can store a copy of the lookup table. However, the disadvantage is that if new documents or words are added, we may need to perform an expensive shift of keywords.

To find all the documents that match a list of strings, we would first sort the list and then send each machine a lookup request for the strings that the machine owns. For example, if our string is “after builds boat amaze banana”, machine 1 would get a lookup request for {“after”, “amaze”}.

Machine 1 looks up the documents containing “after” and “amaze,” and performs an intersection on these document lists. Machine 3 does the same for {“banana”, “boat”, “builds”}, and intersects their lists.

In the final step, the initial machine would do an intersection on the results from Machine 1 and Machine 3.

The following diagram explains this process.



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### Interview Questions

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These questions are designed to mirror a real interview, so they will not always be well defined. Think about what questions you would ask your interviewer and then make reasonable assumptions. You may make different assumptions than us, and that will lead you to a very different design. That's okay!

- 9.1 Stock Data:** Imagine you are building some sort of service that will be called by up to 1,000 client applications to get simple end-of-day stock price information (open, close, high, low). You may assume that you already have the data, and you can store it in any format you wish. How would you design the client-facing service that provides the information to client applications? You are responsible for the development, rollout, and ongoing monitoring and maintenance of the feed. Describe the different methods you considered and why you would recommend your approach. Your service can use any technologies you wish, and can distribute the information to the client applications in any mechanism you choose.

Hints: #385, #396

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- 9.2 Social Network:** How would you design the data structures for a very large social network like Facebook or LinkedIn? Describe how you would design an algorithm to show the shortest path between two people (e.g., Me -> Bob -> Susan -> Jason -> You).

Hints: #270, #285, #304, #321

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- 9.3 Web Crawler:** If you were designing a web crawler, how would you avoid getting into infinite loops?

Hints: #334, #353, #365

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- 9.4 Duplicate URLs:** You have 10 billion URLs. How do you detect the duplicate documents? In this case, assume "duplicate" means that the URLs are identical.

Hints: #326, #347

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- 9.5 Cache:** Imagine a web server for a simplified search engine. This system has 100 machines to respond to search queries, which may then call out using processSearch(string query) to another cluster of machines to actually get the result. The machine which responds to a given query is chosen at random, so you cannot guarantee that the same machine will always respond to the same request. The method processSearch is very expensive. Design a caching mechanism for the most recent queries. Be sure to explain how you would update the cache when data changes.

Hints: #259, #274, #293, #311

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- 9.6 Sales Rank:** A large eCommerce company wishes to list the best-selling products, overall and by category. For example, one product might be the #1056th best-selling product overall but the #13th best-selling product under "Sports Equipment" and the #24th best-selling product under "Safety." Describe how you would design this system.

Hints: #142, #158, #176, #189, #208, #223, #236, #244

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- 9.7 Personal Financial Manager:** Explain how you would design a personal financial manager (like Mint.com). This system would connect to your bank accounts, analyze your spending habits, and make recommendations.

Hints: #162, #180, #199, #212, #247, #276

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- 9.8 Pastebin:** Design a system like Pastebin, where a user can enter a piece of text and get a randomly generated URL to access it.

Hints: #165, #184, #206, #232

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Additional Questions: Object-Oriented Design (#7.7)

Hints start on page 662.

# 10

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## Sorting and Searching

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**U**nderstanding the common sorting and searching algorithms is incredibly valuable, as many sorting and searching problems are tweaks of the well-known algorithms. A good approach is therefore to run through the different sorting algorithms and see if one applies particularly well.

For example, suppose you are asked the following question: Given a very large array of Person objects, sort the people in increasing order of age.

We're given two interesting bits of knowledge here:

1. It's a large array, so efficiency is very important.
2. We are sorting based on ages, so we know the values are in a small range.

By scanning through the various sorting algorithms, we might notice that bucket sort (or radix sort) would be a perfect candidate for this algorithm. In fact, we can make the buckets small (just 1 year each) and get  $O(n)$  running time.

### ► Common Sorting Algorithms

Learning (or re-learning) the common sorting algorithms is a great way to boost your performance. Of the five algorithms explained below, Merge Sort, Quick Sort and Bucket Sort are the most commonly used in interviews.

**Bubble Sort | Runtime:  $O(n^2)$  average and worst case. Memory:  $O(1)$ .**

In bubble sort, we start at the beginning of the array and swap the first two elements if the first is greater than the second. Then, we go to the next pair, and so on, continuously making sweeps of the array until it is sorted. In doing so, the smaller items slowly “bubble” up to the beginning of the list.

**Selection Sort | Runtime:  $O(n^2)$  average and worst case. Memory:  $O(1)$ .**

Selection sort is the child's algorithm: simple, but inefficient. Find the smallest element using a linear scan and move it to the front (swapping it with the front element). Then, find the second smallest and move it, again doing a linear scan. Continue doing this until all the elements are in place.

**Merge Sort | Runtime:  $O(n \log(n))$  average and worst case. Memory: Depends.**

Merge sort divides the array in half, sorts each of those halves, and then merges them back together. Each of those halves has the same sorting algorithm applied to it. Eventually, you are merging just two single-element arrays. It is the “merge” part that does all the heavy lifting.

The merge method operates by copying all the elements from the target array segment into a helper array, keeping track of where the start of the left and right halves should be (`helperLeft` and `helperRight`). We then iterate through helper, copying the smaller element from each half into the array. At the end, we copy any remaining elements into the target array.

```

1 void mergesort(int[] array) {
2     int[] helper = new int[array.length];
3     mergesort(array, helper, 0, array.length - 1);
4 }
5
6 void mergesort(int[] array, int[] helper, int low, int high) {
7     if (low < high) {
8         int middle = (low + high) / 2;
9         mergesort(array, helper, low, middle); // Sort left half
10        mergesort(array, helper, middle+1, high); // Sort right half
11        merge(array, helper, low, middle, high); // Merge them
12    }
13 }
14
15 void merge(int[] array, int[] helper, int low, int middle, int high) {
16     /* Copy both halves into a helper array */
17     for (int i = low; i <= high; i++) {
18         helper[i] = array[i];
19     }
20
21     int helperLeft = low;
22     int helperRight = middle + 1;
23     int current = low;
24
25     /* Iterate through helper array. Compare the left and right half, copying back
26      * the smaller element from the two halves into the original array. */
27     while (helperLeft <= middle && helperRight <= high) {
28         if (helper[helperLeft] <= helper[helperRight]) {
29             array[current] = helper[helperLeft];
30             helperLeft++;
31         } else { // If right element is smaller than left element
32             array[current] = helper[helperRight];
33             helperRight++;
34         }
35         current++;
36     }
37
38     /* Copy the rest of the left side of the array into the target array */
39     int remaining = middle - helperLeft;
40     for (int i = 0; i <= remaining; i++) {
41         array[current + i] = helper[helperLeft + i];
42     }
43 }
```

You may notice that only the remaining elements from the left half of the helper array are copied into the target array. Why not the right half? The right half doesn't need to be copied because it's *already* there.

Consider, for example, an array like [1, 4, 5 || 2, 8, 9] (the "||" indicates the partition point). Prior to merging the two halves, both the helper array and the target array segment will end with [8, 9]. Once we copy over four elements (1, 4, 5, and 2) into the target array, the [8, 9] will still be in place in both arrays. There's no need to copy them over.

The space complexity of merge sort is  $O(n)$  due to the auxiliary space used to merge parts of the array.

**Quick Sort | Runtime:**  $O(n \log(n))$  **average,**  $O(n^2)$  **worst case.** **Memory:**  $O(\log(n))$ .

In quick sort, we pick a random element and partition the array, such that all numbers that are less than the partitioning element come before all elements that are greater than it. The partitioning can be performed efficiently through a series of swaps (see below).

If we repeatedly partition the array (and its sub-arrays) around an element, the array will eventually become sorted. However, as the partitioned element is not guaranteed to be the median (or anywhere near the median), our sorting could be very slow. This is the reason for the  $O(n^2)$  worst case runtime.

```
1 void quickSort(int[] arr, int left, int right) {
2     int index = partition(arr, left, right);
3     if (left < index - 1) { // Sort left half
4         quickSort(arr, left, index - 1);
5     }
6     if (index < right) { // Sort right half
7         quickSort(arr, index, right);
8     }
9 }
10
11 int partition(int[] arr, int left, int right) {
12     int pivot = arr[(left + right) / 2]; // Pick pivot point
13     while (left <= right) {
14         // Find element on left that should be on right
15         while (arr[left] < pivot) left++;
16
17         // Find element on right that should be on left
18         while (arr[right] > pivot) right--;
19
20         // Swap elements, and move left and right indices
21         if (left <= right) {
22             swap(arr, left, right); // swaps elements
23             left++;
24             right--;
25         }
26     }
27     return left;
28 }
```

**Radix Sort | Runtime:**  $O(kn)$  (see below)

Radix sort is a sorting algorithm for integers (and some other data types) that takes advantage of the fact that integers have a finite number of bits. In radix sort, we iterate through each digit of the number, grouping numbers by each digit. For example, if we have an array of integers, we might first sort by the first digit, so that the 0s are grouped together. Then, we sort each of these groupings by the next digit. We repeat this process sorting by each subsequent digit, until finally the whole array is sorted.

Unlike comparison sorting algorithms, which cannot perform better than  $O(n \log(n))$  in the average case, radix sort has a runtime of  $O(kn)$ , where  $n$  is the number of elements and  $k$  is the number of passes of the sorting algorithm.

## ▶ Searching Algorithms

When we think of searching algorithms, we generally think of binary search. Indeed, this is a very useful algorithm to study.

In binary search, we look for an element  $x$  in a sorted array by first comparing  $x$  to the midpoint of the array. If  $x$  is less than the midpoint, then we search the left half of the array. If  $x$  is greater than the midpoint, then we search the right half of the array. We then repeat this process, treating the left and right halves as subarrays. Again, we compare  $x$  to the midpoint of this subarray and then search either its left or right side. We repeat this process until we either find  $x$  or the subarray has size 0.

Note that although the concept is fairly simple, getting all the details right is far more difficult than you might think. As you study the code below, pay attention to the plus ones and minus ones.

```

1 int binarySearch(int[] a, int x) {
2     int low = 0;
3     int high = a.length - 1;
4     int mid;
5
6     while (low <= high) {
7         mid = (low + high) / 2;
8         if (a[mid] < x) {
9             low = mid + 1;
10        } else if (a[mid] > x) {
11            high = mid - 1;
12        } else {
13            return mid;
14        }
15    }
16    return -1; // Error
17 }
18
19 int binarySearchRecursive(int[] a, int x, int low, int high) {
20     if (low > high) return -1; // Error
21
22     int mid = (low + high) / 2;
23     if (a[mid] < x) {
24         return binarySearchRecursive(a, x, mid + 1, high);
25     } else if (a[mid] > x) {
26         return binarySearchRecursive(a, x, low, mid - 1);
27     } else {
28         return mid;
29     }
30 }
```

Potential ways to search a data structure extend beyond binary search, and you would do best not to limit yourself to just this option. You might, for example, search for a node by leveraging a binary tree, or by using a hash table. Think beyond binary search!

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## Interview Questions

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- 10.1 Sorted Merge:** You are given two sorted arrays, A and B, where A has a large enough buffer at the end to hold B. Write a method to merge B into A in sorted order.

Hints: #332

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- 10.2 Group Anagrams:** Write a method to sort an array of strings so that all the anagrams are next to each other.

Hints: #177, #182, #263, #342

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- 10.3 Search in Rotated Array:** Given a sorted array of  $n$  integers that has been rotated an unknown number of times, write code to find an element in the array. You may assume that the array was originally sorted in increasing order.

EXAMPLE

Input: find 5 in {15, 16, 19, 20, 25, 1, 3, 4, 5, 7, 10, 14}

Output: 8 (the index of 5 in the array)

Hints: #298, #310

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- 10.4 Sorted Search, No Size:** You are given an array-like data structure `Listy` which lacks a size method. It does, however, have an `elementAt(i)` method that returns the element at index  $i$  in  $O(1)$  time. If  $i$  is beyond the bounds of the data structure, it returns -1. (For this reason, the data structure only supports positive integers.) Given a `Listy` which contains sorted, positive integers, find the index at which an element  $x$  occurs. If  $x$  occurs multiple times, you may return any index.

Hints: #320, #337, #348

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- 10.5 Sparse Search:** Given a sorted array of strings that is interspersed with empty strings, write a method to find the location of a given string.

EXAMPLE

Input: ball, {"at", "", "", "", "ball", "", "", "car", "", "", "dad", "", ""}

Output: 4

Hints: #256

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- 10.6 Sort Big File:** Imagine you have a 20 GB file with one string per line. Explain how you would sort the file.

Hints: #207

pg 402

- 10.7 Missing Int:** Given an input file with four billion non-negative integers, provide an algorithm to generate an integer that is not contained in the file. Assume you have 1 GB of memory available for this task.

FOLLOW UP

What if you have only 10 MB of memory? Assume that all the values are distinct and we now have no more than one billion non-negative integers.

Hints: #235, #254, #281

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- 10.8 Find Duplicates:** You have an array with all the numbers from 1 to N, where N is at most 32,000. The array may have duplicate entries and you do not know what N is. With only 4 kilobytes of memory available, how would you print all duplicate elements in the array?

Hints: #289, #315

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- 10.9 Sorted Matrix Search:** Given an M x N matrix in which each row and each column is sorted in ascending order, write a method to find an element.

Hints: #193, #211, #229, #251, #266, #279, #288, #291, #303, #317, #330

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- 10.10 Rank from Stream:** Imagine you are reading in a stream of integers. Periodically, you wish to be able to look up the rank of a number x (the number of values less than or equal to x). Implement the data structures and algorithms to support these operations. That is, implement the method `track(int x)`, which is called when each number is generated, and the method `getRankOfNumber(int x)`, which returns the number of values less than or equal to x (not including x itself).

EXAMPLE

Stream (in order of appearance): 5, 1, 4, 4, 5, 9, 7, 13, 3

`getRankOfNumber(1) = 0`  
`getRankOfNumber(3) = 1`  
`getRankOfNumber(4) = 3`

Hints: #301, #376, #392

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- 10.11 Peaks and Valleys:** In an array of integers, a “peak” is an element which is greater than or equal to the adjacent integers and a “valley” is an element which is less than or equal to the adjacent integers. For example, in the array {5, 8, 6, 2, 3, 4, 6}, {8, 6} are peaks and {5, 2} are valleys. Given an array of integers, sort the array into an alternating sequence of peaks and valleys.

EXAMPLE

Input: {5, 3, 1, 2, 3}

Output: {5, 1, 3, 2, 3}

Hints: #196, #219, #231, #253, #277, #292, #316

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Additional Questions: Arrays and Strings (#1.2), Recursion (#8.3), Moderate (#16.10, #16.16, #16.21, #16.24), Hard (#17.11, #17.26).

Hints start on page 662.

# 11

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## Testing

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**B**efore you flip past this chapter saying, “but I’m not a tester” stop and think. Testing is an important task for a software engineer, and for this reason, testing questions may come up during your interview. Of course, if you are applying for Testing roles (or Software Engineer in Test), then that’s all the more reason why you need to pay attention.

Testing problems usually fall under one of four categories: (1) Test a real world object (like a pen); (2) Test a piece of software; (3) Write test code for a function; (4) Troubleshoot an existing issue. We’ll cover approaches for each of these four types.

Remember that all four types require you to not make an assumption that the input or the user will play nice. Expect abuse and plan for it.

### ► What the Interviewer Is Looking For

At their surface, testing questions seem like they’re just about coming up with an extensive list of test cases. And to some extent, that’s right. You do need to come up with a reasonable list of test cases.

But in addition, interviewers want to test the following:

- *Big Picture Understanding:* Are you a person who understands what the software is really about? Can you prioritize test cases properly? For example, suppose you’re asked to test an e-commerce system like Amazon. It’s great to make sure that the product images appear in the right place, but it’s even more important that payments work reliably, products are added to the shipment queue, and customers are never double charged.
- *Knowing How the Pieces Fit Together:* Do you understand how software works, and how it might fit into a greater ecosystem? Suppose you’re asked to test Google Spreadsheets. It’s important that you test opening, saving, and editing documents. But, Google Spreadsheets is part of a larger ecosystem. You need to test integration with Gmail, with plug-ins, and with other components.
- *Organization:* Do you approach the problem in a structured manner, or do you just spout off anything that comes to your head? Some candidates, when asked to come up with test cases for a camera, will just state anything and everything that comes to their head. A good candidate will break down the parts into categories like Taking Photos, Image Management, Settings, and so on. This structured approach will also help you to do a more thorough job creating the test cases.
- *Practicality:* Can you actually create reasonable testing plans? For example, if a user reports that the software crashes when they open a specific image, and you just tell them to reinstall the software, that’s typically not very practical. Your testing plans need to be feasible and realistic for a company to implement.

Demonstrating these aspects will show that you will be a valuable member of the testing team.

## ► Testing a Real World Object

Some candidates are surprised to be asked questions like how to test a pen. After all, you should be testing software, right? Maybe, but these “real world” questions are still very common. Let’s walk through this with an example.

Question: How would you test a paperclip?

### **Step 1: Who will use it? And why?**

You need to discuss with your interviewer who is using the product and for what purpose. The answer may not be what you think. The answer could be “by teachers, to hold papers together,” or it could be “by artists, to bend into the shape of animal.” Or, it could be both. The answer to this question will shape how you handle the remaining questions.

### **Step 2: What are the use cases?**

It will be useful for you to make a list of the use cases. In this case, the use case might be simply fastening paper together in a non-damaging (to the paper) way.

For other questions, there might be multiple use cases. It might be, for example, that the product needs to be able to send and receive content, or write and erase, and so on.

### **Step 3: What are the bounds of use?**

The bounds of use might mean holding up to thirty sheets of paper in a single usage without permanent damage (e.g., bending), and thirty to fifty sheets with minimal permanent bending.

The bounds also extend to environmental factors as well. For example, should the paperclip work during very warm temperatures (90 - 110 degrees Fahrenheit)? What about extreme cold?

### **Step 4: What are the stress / failure conditions?**

No product is fail-proof, so analyzing failure conditions needs to be part of your testing. A good discussion to have with your interviewer is about when it’s acceptable (or even necessary) for the product to fail, and what failure should mean.

For example, if you were testing a laundry machine, you might decide that the machine should be able to handle at least 30 shirts or pants. Loading 30 - 45 pieces of clothing may result in minor failure, such as the clothing being inadequately cleaned. At more than 45 pieces of clothing, extreme failure might be acceptable. However, extreme failure in this case should probably mean the machine never turning on the water. It should certainly *not* mean a flood or a fire.

### **Step 5: How would you perform the testing?**

In some cases, it might also be relevant to discuss the details of performing the testing. For example, if you need to make sure a chair can withstand normal usage for five years, you probably can’t actually place it in a home and wait five years. Instead, you’d need to define what “normal” usage is (How many “sits” per year on the seat? What about the armrest?). Then, in addition to doing some manual testing, you would likely want a machine to automate some of the usage.

### ▶ Testing a Piece of Software

Testing a piece of software is actually very similar to testing a real world object. The major difference is that software testing generally places a greater emphasis on the details of performing testing.

Note that software testing has two core aspects to it:

- *Manual vs. Automated Testing:* In an ideal world, we might love to automate everything, but that's rarely feasible. Some things are simply much better with manual testing because some features are too qualitative for a computer to effectively examine (such as if content represents pornography). Additionally, whereas a computer can generally recognize only issues that it's been told to look for, human observation may reveal new issues that haven't been specifically examined. Both humans and computers form an essential part of the testing process.
- *Black Box Testing vs. White Box Testing:* This distinction refers to the degree of access we have into the software. In black box testing, we're just given the software as-is and need to test it. With white box testing, we have additional programmatic access to test individual functions. We can also automate some black box testing, although it's certainly much harder.

Let's walk through an approach from start to end.

#### **Step 1: Are we doing Black Box Testing or White Box Testing?**

Though this question can often be delayed to a later step, I like to get it out of the way early on. Check with your interviewer as to whether you're doing black box testing or white box testing—or both.

#### **Step 2: Who will use it? And why?**

Software typically has one or more target users, and the features are designed with this in mind. For example, if you're asked to test software for parental controls on a web browser, your target users include both parents (who are implementing the blocking) and children (who are the recipients of blocking). You may also have "guests" (people who should neither be implementing nor receiving blocking).

#### **Step 3: What are the use cases?**

In the software blocking scenario, the use cases of the parents include installing the software, updating controls, removing controls, and of course their own personal internet usage. For the children, the use cases include accessing legal content as well as "illegal" content.

Remember that it's not up to you to just magically decide the use cases. This is a conversation to have with your interviewer.

#### **Step 4: What are the bounds of use?**

Now that we have the vague use cases defined, we need to figure out what exactly this means. What does it mean for a website to be blocked? Should just the "illegal" page be blocked, or the entire website? Is the application supposed to "learn" what is bad content, or is it based on a white list or black list? If it's supposed to learn what inappropriate content is, what degree of false positives or false negatives is acceptable?

#### **Step 5: What are the stress conditions / failure conditions?**

When the software fails—which it inevitably will—what should the failure look like? Clearly, the software failure shouldn't crash the computer. Instead, it's likely that the software should just permit a blocked site,

or ban an allowable site. In the latter case, you might want to discuss the possibility of a selective override with a password from the parents.

#### Step 6: What are the test cases? How would you perform the testing?

Here is where the distinctions between manual and automated testing, and between black box and white box testing, really come into play.

Steps 3 and 4 should have roughly defined the use cases. In step 6, we further define them and discuss how to perform the testing. What exact situations are you testing? Which of these steps can be automated? Which require human intervention?

Remember that while automation allows you to do some very powerful testing, it also has some significant drawbacks. Manual testing should usually be part of your test procedures.

When you go through this list, don't just rattle off every scenario you can think of. It's disorganized, and you're sure to miss major categories. Instead, approach this in a structured manner. Break down your testing into the main components, and go from there. Not only will you give a more complete list of test cases, but you'll also show that you're a structured, methodical person.

### ► Testing a Function

In many ways, testing a function is the easiest type of testing. The conversation is typically briefer and less vague, as the testing is usually limited to validating input and output.

However, don't overlook the value of some conversation with your interviewer. You should discuss any assumptions with your interviewer, particularly with respect to how to handle specific situations.

Suppose you were asked to write code to test `sort(int[] array)`, which sorts an array of integers. You might proceed as follows.

#### Step 1: Define the test cases

In general, you should think about the following types of test cases:

- *The normal case:* Does it generate the correct output for typical inputs? Remember to think about potential issues here. For example, because sorting often requires some sort of partitioning, it's reasonable to think that the algorithm might fail on arrays with an odd number of elements, since they can't be evenly partitioned. Your test case should list both examples.
- *The extremes:* What happens when you pass in an empty array? Or a very small (one element) array? What if you pass in a very large one?
- *Nulls and "illegal" input:* It is worthwhile to think about how the code should behave when given illegal input. For example, if you're testing a function to generate the nth Fibonacci number, your test cases should probably include the situation where n is negative.
- *Strange input:* A fourth kind of input sometimes comes up: strange input. What happens when you pass in an already sorted array? Or an array that's sorted in reverse order?

Generating these tests does require knowledge of the function you are writing. If you are unclear as to the constraints, you will need to ask your interviewer about this first.

### Step 2: Define the expected result

Often, the expected result is obvious: the right output. However, in some cases, you might want to validate additional aspects. For instance, if the `sort` method returns a new sorted copy of the array, you should probably validate that the original array has not been touched.

### Step 3: Write test code

Once you have the test cases and results defined, writing the code to implement the test cases should be fairly straightforward. Your code might look something like:

```
1 void testAddThreeSorted() {  
2     MyList list = new MyList();  
3     list.addThreeSorted(3, 1, 2); // Adds 3 items in sorted order  
4     assertEquals(list.getElement(0), 1);  
5     assertEquals(list.getElement(1), 2);  
6     assertEquals(list.getElement(2), 3);  
7 }
```

## ► Troubleshooting Questions

A final type of question is explaining how you would debug or troubleshoot an existing issue. Many candidates balk at a question like this, giving unrealistic answers like “reinstall the software.” You can approach these questions in a structured manner, like anything else.

Let’s walk through this problem with an example: You’re working on the Google Chrome team when you receive a bug report: Chrome crashes on launch. What would you do?

Reinstalling the browser might solve this user’s problem, but it wouldn’t help the other users who might be experiencing the same issue. Your goal is to understand what’s *really* happening, so that the developers can fix it.

### Step 1: Understand the Scenario

The first thing you should do is ask questions to understand as much about the situation as possible.

- How long has the user been experiencing this issue?
- What version of the browser is it? What operating system?
- Does the issue happen consistently, or how often does it happen? When does it happen?
- Is there an error report that launches?

### Step 2: Break Down the Problem

Now that you understand the details of the scenario, you want to break down the problem into testable units. In this case, you can imagine the flow of the situation as follows:

1. Go to Windows Start menu.
2. Click on Chrome icon.
3. Browser instance starts.
4. Browser loads settings.
5. Browser issues HTTP request for homepage.

6. Browser gets HTTP response.
7. Browser parses webpage.
8. Browser displays content.

At some point in this process, something fails and it causes the browser to crash. A strong tester would iterate through the elements of this scenario to diagnose the problem.

### Step 3: Create Specific, Manageable Tests

Each of the above components should have realistic instructions—things that you can ask the user to do, or things that you can do yourself (such as replicating steps on your own machine). In the real world, you will be dealing with customers, and you can't give them instructions that they can't or won't do.

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## Interview Questions

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- 11.1 Mistake:** Find the mistake(s) in the following code:

```
unsigned int i;
for (i = 100; i >= 0; --i)
    printf("%d\n", i);
```

Hints: #257, #299, #362

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- 11.2 Random Crashes:** You are given the source to an application which crashes when it is run. After running it ten times in a debugger, you find it never crashes in the same place. The application is single threaded, and uses only the C standard library. What programming errors could be causing this crash? How would you test each one?

Hints: #325

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- 11.3 Chess Test:** We have the following method used in a chess game: boolean `canMoveTo(int x, int y)`. This method is part of the `Piece` class and returns whether or not the piece can move to position `(x, y)`. Explain how you would test this method.

Hints: #329, #401

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- 11.4 No Test Tools:** How would you load test a webpage without using any test tools?

Hints: #313, #345

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- 11.5 Test a Pen:** How would you test a pen?

Hints: #140, #164, #220

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- 11.6 Test an ATM:** How would you test an ATM in a distributed banking system?

Hints: #210, #225, #268, #349, #393

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Hints start on page 662.

# 12

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## C and C++

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A good interviewer won't demand that you code in a language you don't profess to know. Hopefully, if you're asked to code in C++, it's listed on your resume. If you don't remember all the APIs, don't worry—most interviewers (though not all) don't care that much. We do recommend, however, studying up on basic C++ syntax so that you can approach these questions with ease.

### ► Classes and Inheritance

Though C++ classes have similar characteristics to those of other languages, we'll review some of the syntax below.

The code below demonstrates the implementation of a basic class with inheritance.

```
1 #include <iostream>
2 using namespace std;
3
4 #define NAME_SIZE 50 // Defines a macro
5
6 class Person {
7     int id; // all members are private by default
8     char name[NAME_SIZE];
9
10 public:
11     void aboutMe() {
12         cout << "I am a person.";
13     }
14 };
15
16 class Student : public Person {
17 public:
18     void aboutMe() {
19         cout << "I am a student.";
20     }
21 };
22
23 int main() {
24     Student * p = new Student();
25     p->aboutMe(); // prints "I am a student."
26     delete p; // Important! Make sure to delete allocated memory.
27     return 0;
28 }
```

All data members and methods are private by default in C++. One can modify this by introducing the keyword `public`.

## ► Constructors and Destructors

The constructor of a class is automatically called upon an object's creation. If no constructor is defined, the compiler automatically generates one called the Default Constructor. Alternatively, we can define our own constructor.

If you just need to initialize primitive types, a simple way to do it is this:

```
1 Person(int a) {
2     id = a;
3 }
```

This works for primitive types, but you might instead want to do this:

```
1 Person(int a) : id(a) {
2     ...
3 }
```

The data member `id` is assigned before the actual object is created and before the remainder of the constructor code is called. This approach is necessary when the fields are constant or class types.

The destructor cleans up upon object deletion and is automatically called when an object is destroyed. It cannot take an argument as we don't explicitly call a destructor.

```
1 ~Person() {
2     delete obj; // free any memory allocated within class
3 }
```

## ► Virtual Functions

In an earlier example, we defined `p` to be of type `Student`:

```
1 Student * p = new Student();
2 p->aboutMe();
```

What would happen if we defined `p` to be a `Person*`, like so?

```
1 Person * p = new Student();
2 p->aboutMe();
```

In this case, "I am a person" would be printed instead. This is because the function `aboutMe` is resolved at compile-time, in a mechanism known as *static binding*.

If we want to ensure that the `Student`'s implementation of `aboutMe` is called, we can define `aboutMe` in the `Person` class to be `virtual`.

```
1 class Person {
2     ...
3     virtual void aboutMe() {
4         cout << "I am a person.";
5     }
6 };
7
8 class Student : public Person {
9 public:
10    void aboutMe() {
11        cout << "I am a student.";
12    }
13 }
```

```
13 };
```

Another usage for virtual functions is when we can't (or don't want to) implement a method for the parent class. Imagine, for example, that we want `Student` and `Teacher` to inherit from `Person` so that we can implement a common method such as `addCourse(string s)`. Calling `addCourse` on `Person`, however, wouldn't make much sense since the implementation depends on whether the object is actually a `Student` or `Teacher`.

In this case, we might want `addCourse` to be a virtual function defined within `Person`, with the implementation being left to the subclass.

```
1 class Person {
2     int id; // all members are private by default
3     char name[NAME_SIZE];
4 public:
5     virtual void aboutMe() {
6         cout << "I am a person." << endl;
7     }
8     virtual bool addCourse(string s) = 0;
9 };
10
11 class Student : public Person {
12 public:
13     void aboutMe() {
14         cout << "I am a student." << endl;
15     }
16
17     bool addCourse(string s) {
18         cout << "Added course " << s << " to student." << endl;
19         return true;
20     }
21 };
22
23 int main() {
24     Person * p = new Student();
25     p->aboutMe(); // prints "I am a student."
26     p->addCourse("History");
27     delete p;
28 }
```

Note that by defining `addCourse` to be a "pure virtual function," `Person` is now an abstract class and we cannot instantiate it.

### ► Virtual Destructor

The virtual function naturally introduces the concept of a "virtual destructor." Suppose we wanted to implement a destructor method for `Person` and `Student`. A naive solution might look like this:

```
1 class Person {
2 public:
3     ~Person() {
4         cout << "Deleting a person." << endl;
5     }
6 };
7
8 class Student : public Person {
9 public:
```

```

10 ~Student() {
11     cout << "Deleting a student." << endl;
12 }
13 };
14
15 int main() {
16     Person * p = new Student();
17     delete p; // prints "Deleting a person."
18 }
```

As in the earlier example, since `p` is a `Person`, the destructor for the `Person` class is called. This is problematic because the memory for `Student` may not be cleaned up.

To fix this, we simply define the destructor for `Person` to be virtual.

```

1 class Person {
2 public:
3     virtual ~Person() {
4         cout << "Deleting a person." << endl;
5     }
6 };
7
8 class Student : public Person {
9 public:
10    ~Student() {
11        cout << "Deleting a student." << endl;
12    }
13 };
14
15 int main() {
16     Person * p = new Student();
17     delete p;
18 }
```

This will output the following:

```

Deleting a student.
Deleting a person.
```

## ► Default Values

Functions can specify default values, as shown below. Note that all default parameters must be on the right side of the function declaration, as there would be no other way to specify how the parameters line up.

```

1 int func(int a, int b = 3) {
2     x = a;
3     y = b;
4     return a + b;
5 }
6
7 w = func(4);
8 z = func(4, 5);
```

## ► Operator Overloading

Operator overloading enables us to apply operators like `+` to objects that would otherwise not support these operations. For example, if we wanted to merge two `BookShelves` into one, we could overload the `+` operator as follows.

```
1 BookShelf BookShelf::operator+(BookShelf &other) { ... }
```

### ▶ Pointers and References

A pointer holds the address of a variable and can be used to perform any operation that could be directly done on the variable, such as accessing and modifying it.

Two pointers can equal each other, such that changing one's value also changes the other's value (since they, in fact, point to the same address).

```
1 int * p = new int;
2 *p = 7;
3 int * q = p;
4 *p = 8;
5 cout << *q; // prints 8
```

Note that the size of a pointer varies depending on the architecture: 32 bits on a 32-bit machine and 64 bits on a 64-bit machine. Pay attention to this difference, as it's common for interviewers to ask exactly how much space a data structure takes up.

### References

A reference is another name (an alias) for a pre-existing object and it does not have memory of its own. For example:

```
1 int a = 5;
2 int & b = a;
3 b = 7;
4 cout << a; // prints 7
```

In line 2 above, `b` is a reference to `a`; modifying `b` will also modify `a`.

You cannot create a reference without specifying where in memory it refers to. However, you can create a free-standing reference as shown below:

```
1 /* allocates memory to store 12 and makes b a reference to this
2  * piece of memory. */
3 const int & b = 12;
```

Unlike pointers, references cannot be null and cannot be reassigned to another piece of memory.

### Pointer Arithmetic

One will often see programmers perform addition on a pointer, such as what you see below:

```
1 int * p = new int[2];
2 p[0] = 0;
3 p[1] = 1;
4 p++;
5 cout << *p; // Outputs 1
```

Performing `p++` will skip ahead by `sizeof(int)` bytes, such that the code outputs 1. Had `p` been of different type, it would skip ahead as many bytes as the size of the data structure.

## ► Templates

Templates are a way of reusing code to apply the same class to different data types. For example, we might have a list-like data structure which we would like to use for lists of various types. The code below implements this with the `ShiftedList` class.

```

1  template <class T> class ShiftedList {
2      T* array;
3      int offset, size;
4  public:
5      ShiftedList(int sz) : offset(0), size(sz) {
6          array = new T[size];
7      }
8
9      ~ShiftedList() {
10         delete [] array;
11     }
12
13     void shiftBy(int n) {
14         offset = (offset + n) % size;
15     }
16
17     T getAt(int i) {
18         return array[convertIndex(i)];
19     }
20
21     void setAt(T item, int i) {
22         array[convertIndex(i)] = item;
23     }
24
25 private:
26     int convertIndex(int i) {
27         int index = (i - offset) % size;
28         while (index < 0) index += size;
29         return index;
30     }
31 };

```

---

## Interview Questions

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- 12.1 Last K Lines:** Write a method to print the last K lines of an input file using C++.

Hints: #449, #459

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- 12.2 Reverse String:** Implement a function `void reverse(char* str)` in C or C++ which reverses a null-terminated string.

Hints: #410, #452

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- 12.3 Hash Table vs. STL Map:** Compare and contrast a hash table and an STL map. How is a hash table implemented? If the number of inputs is small, which data structure options can be used instead of a hash table?

Hints: #423

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**12.4 Virtual Functions:** How do virtual functions work in C++?

Hints: #463

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**12.5 Shallow vs. Deep Copy:** What is the difference between deep copy and shallow copy? Explain how you would use each.

Hints: #445

pg 425

**12.6 Volatile:** What is the significance of the keyword “volatile” in C?

Hints: #456

pg 426

**12.7 Virtual Base Class:** Why does a destructor in base class need to be declared virtual?

Hints: #421, #460

pg 427

**12.8 Copy Node:** Write a method that takes a pointer to a Node structure as a parameter and returns a complete copy of the passed in data structure. The Node data structure contains two pointers to other Nodes.

Hints: #427, #462

pg 427

**12.9 Smart Pointer:** Write a smart pointer class. A smart pointer is a data type, usually implemented with templates, that simulates a pointer while also providing automatic garbage collection. It automatically counts the number of references to a `SmartPointer<T*>` object and frees the object of type T when the reference count hits zero.

Hints: #402, #438, #453

pg 428

**12.10 Malloc:** Write an aligned malloc and free function that supports allocating memory such that the memory address returned is divisible by a specific power of two.

EXAMPLE

`align_malloc(1000, 128)` will return a memory address that is a multiple of 128 and that points to memory of size 1000 bytes.

`aligned_free()` will free memory allocated by `align_malloc`.

Hints: #413, #432, #440

pg 430

**12.11 2D Alloc:** Write a function in C called `my2DAalloc` which allocates a two-dimensional array. Minimize the number of calls to `malloc` and make sure that the memory is accessible by the notation `arr[i][j]`.

Hints: #406, #418, #426

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Additional Questions: Linked Lists (#2.6), Testing (#11.1), Java (#13.4), Threads and Locks (#15.3).

Hints start on page 676.

# 13

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## Java

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**W**hile Java-related questions are found throughout this book, this chapter deals with questions about the language and syntax. Such questions are more unusual at bigger companies, which believe more in testing a candidate's aptitude than a candidate's knowledge (and which have the time and resources to train a candidate in a particular language). However, at other companies, these pesky questions can be quite common.

### ► How to Approach

As these questions focus so much on knowledge, it may seem silly to talk about an approach to these problems. After all, isn't it just about knowing the right answer?

Yes and no. Of course, the best thing you can do to master these questions is to learn Java inside and out. But, if you do get stumped, you can try to tackle it with the following approach:

1. Create an example of the scenario, and ask yourself how things should play out.
2. Ask yourself how other languages would handle this scenario.
3. Consider how you would design this situation if you were the language designer. What would the implications of each choice be?

Your interviewer may be equally—or more—impressed if you can derive the answer than if you automatically knew it. Don't try to bluff though. Tell the interviewer, "I'm not sure I can recall the answer, but let me see if I can figure it out. Suppose we have this code..."

### ► Overloading vs. Overriding

Overloading is a term used to describe when two methods have the same name but differ in the type or number of arguments.

```
1 public double computeArea(Circle c) { ... }  
2 public double computeArea(Square s) { ... }
```

Overriding, however, occurs when a method shares the same name and function signature as another method in its super class.

```
1 public abstract class Shape {  
2     public void printMe() {  
3         System.out.println("I am a shape.");  
4     }  
5     public abstract double computeArea();  
6 }
```

```
7
8  public class Circle extends Shape {
9      private double rad = 5;
10     public void printMe() {
11         System.out.println("I am a circle.");
12     }
13
14     public double computeArea() {
15         return rad * rad * 3.15;
16     }
17 }
18
19 public class Ambiguous extends Shape {
20     private double area = 10;
21     public double computeArea() {
22         return area;
23     }
24 }
25
26 public class IntroductionOverriding {
27     public static void main(String[] args) {
28         Shape[] shapes = new Shape[2];
29         Circle circle = new Circle();
30         Ambiguous ambiguous = new Ambiguous();
31
32         shapes[0] = circle;
33         shapes[1] = ambiguous;
34
35         for (Shape s : shapes) {
36             s.printMe();
37             System.out.println(s.computeArea());
38         }
39     }
40 }
```

The above code will print:

```
1 I am a circle.
2 78.75
3 I am a shape.
4 10.0
```

Observe that `Circle` overrode `printMe()`, whereas `Ambiguous` just left this method as-is.

## ► Collection Framework

Java's collection framework is incredibly useful, and you will see it used throughout this book. Here are some of the most useful items:

**ArrayList:** An `ArrayList` is a dynamically resizing array, which grows as you insert elements.

```
1 ArrayList<String> myArr = new ArrayList<String>();
2 myArr.add("one");
3 myArr.add("two");
4 System.out.println(myArr.get(0)); /* prints <one> */
```

**Vector:** A vector is very similar to an `ArrayList`, except that it is synchronized. Its syntax is almost identical as well.

```

1 Vector<String> myVect = new Vector<String>();
2 myVect.add("one");
3 myVect.add("two");
4 System.out.println(myVect.get(0));

```

**LinkedList:** `LinkedList` is, of course, Java's built-in `LinkedList` class. Though it rarely comes up in an interview, it's useful to study because it demonstrates some of the syntax for an iterator.

```

1 LinkedList<String> myLinkedList = new LinkedList<String>();
2 myLinkedList.add("two");
3 myLinkedList.addFirst("one");
4 Iterator<String> iter = myLinkedList.iterator();
5 while (iter.hasNext()) {
6     System.out.println(iter.next());
7 }

```

**HashMap:** The `HashMap` collection is widely used, both in interviews and in the real world. We've provided a snippet of the syntax below.

```

1 HashMap<String, String> map = new HashMap<String, String>();
2 map.put("one", "uno");
3 map.put("two", "dos");
4 System.out.println(map.get("one"));

```

Before your interview, make sure you're very comfortable with the above syntax. You'll need it.

## Interview Questions

---

Please note that because virtually all the solutions in this book are implemented with Java, we have selected only a small number of questions for this chapter. Moreover, most of these questions deal with the "trivia" of the languages, since the rest of the book is filled with Java programming questions.

- 13.1 Private Constructor:** In terms of inheritance, what is the effect of keeping a constructor private?

Hints: #404

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- 13.2 Return from Finally:** In Java, does the `finally` block get executed if we insert a `return` statement inside the `try` block of a `try-catch-finally`?

Hints: #409

pg 433

- 13.3 Final, etc.:** What is the difference between `final`, `finally`, and `finalize`?

Hints: #412

pg 433

- 13.4 Generics vs. Templates:** Explain the difference between templates in C++ and generics in Java.

Hints: #416, #425

pg 435

- 13.5 TreeMap, HashMap, LinkedHashMap:** Explain the differences between `TreeMap`, `HashMap`, and `LinkedHashMap`. Provide an example of when each one would be best.

Hints: #420, #424, #430, #454

pg 436

- 13.6 Object Reflection:** Explain what object reflection is in Java and why it is useful.

Hints: #435

pg 437

- 13.7 Lambda Expressions:** There is a class `Country` that has methods `getContinent()` and `getPopulation()`. Write a function `int getPopulation(List<Country> countries, String continent)` that computes the total population of a given continent, given a list of all countries and the name of a continent.

Hints: #448, #461, #464

pg 438

- 13.8 Lambda Random:** Using Lambda expressions, write a function `List<Integer> getRandomSubset(List<Integer> list)` that returns a random subset of arbitrary size. All subsets (including the empty set) should be equally likely to be chosen.

Hints: #443, #450, #457

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Additional Questions: Arrays and Strings (#1.3), Object-Oriented Design (#7.12), Threads and Locks (#15.3)

Hints start on page 676.

# 14

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## Databases

---

If you profess knowledge of databases, you might be asked some questions on it. We'll review some of the key concepts and offer an overview of how to approach these problems. As you read these queries, don't be surprised by minor variations in syntax. There are a variety of flavors of SQL, and you might have worked with a slightly different one. The examples in this book have been tested against Microsoft SQL Server.

### ► SQL Syntax and Variations

Implicit and explicit joins are shown below. These two statements are equivalent, and it's a matter of personal preference which one you choose. For consistency, we will stick to the explicit join.

#### Explicit Join

```
1 SELECT CourseName, TeacherName  
2 FROM Courses INNER JOIN Teachers  
3 ON Courses.TeacherID = Teachers.TeacherID
```

#### Implicit Join

```
1 SELECT CourseName, TeacherName  
2 FROM Courses, Teachers  
3 WHERE Courses.TeacherID =  
4 Teachers.TeacherID
```

### ► Denormalized vs. Normalized Databases

Normalized databases are designed to minimize redundancy, while denormalized databases are designed to optimize read time.

In a traditional normalized database with data like Courses and Teachers, Courses might contain a column called TeacherID, which is a foreign key to Teacher. One benefit of this is that information about the teacher (name, address, etc.) is only stored once in the database. The drawback is that many common queries will require expensive joins.

Instead, we can denormalize the database by storing redundant data. For example, if we knew that we would have to repeat this query often, we might store the teacher's name in the Courses table. Denormalization is commonly used to create highly scalable systems.

### ► SQL Statements

Let's walk through a review of basic SQL syntax, using as an example the database that was mentioned earlier. This database has the following simple structure (\* indicates a primary key):

Courses: CourseID\*, CourseName, TeacherID

Teachers: TeacherID\*, TeacherName

Students: StudentID\*, StudentName

StudentCourses: CourseID\*, StudentID\*

Using the above table, implement the following queries.

### Query 1: Student Enrollment

Implement a query to get a list of all students and how many courses each student is enrolled in.

At first, we might try something like this:

```
1 /* Incorrect Code */
2 SELECT Students.StudentName, count(*)
3 FROM Students INNER JOIN StudentCourses
4 ON Students.StudentID = StudentCourses.StudentID
5 GROUP BY Students.StudentID
```

This has three problems:

1. We have excluded students who are not enrolled in any courses, since `StudentCourses` only includes enrolled students. We need to change this to a `LEFT JOIN`.
2. Even if we changed it to a `LEFT JOIN`, the query is still not quite right. Doing `count(*)` would return how many items there are in a given group of `StudentID`s. Students enrolled in zero courses would still have one item in their group. We need to change this to count the number of `CourseID`s in each group: `count(StudentCourses.CourseID)`.
3. We've grouped by `Students.StudentID`, but there are still multiple `StudentNames` in each group. How will the database know which `StudentName` to return? Sure, they may all have the same value, but the database doesn't understand that. We need to apply an *aggregate* function to this, such as `first(Students.StudentName)`.

Fixing these issues gets us to this query:

```
1 /* Solution 1: Wrap with another query */
2 SELECT StudentName, Students.StudentID, Cnt
3 FROM (
4     SELECT Students.StudentID, count(StudentCourses.CourseID) as [Cnt]
5     FROM Students LEFT JOIN StudentCourses
6     ON Students.StudentID = StudentCourses.StudentID
7     GROUP BY Students.StudentID
8 ) T INNER JOIN Students on T.studentID = Students.StudentID
```

Looking at this code, one might ask why we don't just select the student name on line 3 to avoid having to wrap lines 3 through 6 with another query. This (incorrect) solution is shown below.

```
1 /* Incorrect Code */
2 SELECT StudentName, Students.StudentID, count(StudentCourses.CourseID) as [Cnt]
3 FROM Students LEFT JOIN StudentCourses
4 ON Students.StudentID = StudentCourses.StudentID
5 GROUP BY Students.StudentID
```

The answer is that we *can't* do that - at least not exactly as shown. We can only select values that are in an aggregate function or in the `GROUP BY` clause.

Alternatively, we could resolve the above issues with either of the following statements:

```
1 /* Solution 2: Add StudentName to GROUP BY clause. */
2 SELECT StudentName, Students.StudentID, count(StudentCourses.CourseID) as [Cnt]
3 FROM Students LEFT JOIN StudentCourses
4 ON Students.StudentID = StudentCourses.StudentID
5 GROUP BY Students.StudentID, Students.StudentName
```

OR

```

1  /* Solution 3: Wrap with aggregate function. */
2  SELECT max(StudentName) as [StudentName], Students.StudentID,
3         count(StudentCourses.CourseID) as [Count]
4  FROM Students LEFT JOIN StudentCourses
5  ON Students.StudentID = StudentCourses.StudentID
6  GROUP BY Students.StudentID

```

#### *Query 2: Teacher Class Size*

Implement a query to get a list of all teachers and how many students they each teach. If a teacher teaches the same student in two courses, you should double count the student. Sort the list in descending order of the number of students a teacher teaches.

We can construct this query step by step. First, let's get a list of TeacherIDs and how many students are associated with each TeacherID. This is very similar to the earlier query.

```

1  SELECT TeacherID, count(StudentCourses.CourseID) AS [Number]
2  FROM Courses INNER JOIN StudentCourses
3  ON Courses.CourseID = StudentCourses.CourseID
4  GROUP BY Courses.TeacherID

```

Note that this INNER JOIN will not select teachers who aren't teaching classes. We'll handle that in the below query when we join it with the list of all teachers.

```

1  SELECT TeacherName, isnull(StudentSize.Number, 0)
2  FROM Teachers LEFT JOIN
3      (SELECT TeacherID, count(StudentCourses.CourseID) AS [Number]
4       FROM Courses INNER JOIN StudentCourses
5       ON Courses.CourseID = StudentCourses.CourseID
6       GROUP BY Courses.TeacherID) StudentSize
7  ON Teachers.TeacherID = StudentSize.TeacherID
8  ORDER BY StudentSize.Number DESC

```

Note how we handled the NULL values in the SELECT statement to convert the NULL values to zeros.

## ► Small Database Design

Additionally, you might be asked to design your own database. We'll walk you through an approach for this. You might notice the similarities between this approach and the approach for object-oriented design.

### Step 1: Handle Ambiguity

Database questions often have some ambiguity, intentionally or unintentionally. Before you proceed with your design, you must understand exactly what you need to design.

Imagine you are asked to design a system to represent an apartment rental agency. You will need to know whether this agency has multiple locations or just one. You should also discuss with your interviewer how general you should be. For example, it would be extremely rare for a person to rent two apartments in the same building. But does that mean you shouldn't be able to handle that? Maybe, maybe not. Some very rare conditions might be best handled through a work around (like duplicating the person's contact information in the database).

#### *Step 2: Define the Core Objects*

Next, we should look at the core objects of our system. Each of these core objects typically translates into a table. In this case, our core objects might be *Property*, *Building*, *Apartment*, *Tenant* and *Manager*.

### Step 3: Analyze Relationships

Outlining the core objects should give us a good sense of what the tables should be. How do these tables relate to each other? Are they many-to-many? One-to-many?

If Buildings has a one-to-many relationship with Apartments (one Building has many Apartments), then we might represent this as follows:

Apartments	
ApartmentID	int
ApartmentAddress	varchar(100)
BuildingID	int

Buildings	
BuildingID	int
BuildingName	varchar(100)
BuildingAddress	varchar(500)

Note that the Apartments table links back to Buildings with a BuildingID column.

If we want to allow for the possibility that one person rents more than one apartment, we might want to implement a many-to-many relationship as follows:

TenantApartments	
TenantID	int
ApartmentID	int

Apartments	
ApartmentID	int
ApartmentAddress	varchar(500)
BuildingID	int

Tenants	
TenantID	int
TenantName	varchar(100)
TenantAddress	varchar(500)

The TenantApartments table stores a relationship between Tenants and Apartments.

### Step 4: Investigate Actions

Finally, we fill in the details. Walk through the common actions that will be taken and understand how to store and retrieve the relevant data. We'll need to handle lease terms, moving out, rent payments, etc. Each of these actions requires new tables and columns.

## ► Large Database Design

When designing a large, scalable database, joins (which are required in the above examples) are generally very slow. Thus, you must *denormalize* your data. Think carefully about how data will be used—you'll probably need to duplicate the data in multiple tables.

## Interview Questions

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Questions 1 through 3 refer to the database schema at the end of the chapter. Each apartment can have multiple tenants, and each tenant can have multiple apartments. Each apartment belongs to one building, and each building belongs to one complex.

**14.1 Multiple Apartments:** Write a SQL query to get a list of tenants who are renting more than one apartment.

Hints: #408

33 44 |

- 14.2 Open Requests:** Write a SQL query to get a list of all buildings and the number of open requests (Requests in which status equals ‘Open’).

Hints: #411

pg 442

- 14.3 Close All Requests:** Building #11 is undergoing a major renovation. Implement a query to close all requests from apartments in this building.

Hints: #431

pg 442

- 14.4 Joins:** What are the different types of joins? Please explain how they differ and why certain types are better in certain situations.

Hints: #451

pg 442

- 14.5 Denormalization:** What is denormalization? Explain the pros and cons.

Hints: #444, #455

pg 443

- 14.6 Entity-Relationship Diagram:** Draw an entity-relationship diagram for a database with companies, people, and professionals (people who work for companies).

Hints: #436

pg 444

- 14.7 Design Grade Database:** Imagine a simple database storing information for students’ grades. Design what this database might look like and provide a SQL query to return a list of the honor roll students (top 10%), sorted by their grade point average.

Hints: #428, #442

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Additional Questions: Object-Oriented Design (#7.7), System Design and Scalability (#9.6)

Hints start on page 676.

Apartments	
AptID	int
UnitNumber	varchar(10)
BuildingID	int

Buildings	
BuildingID	int
ComplexID	int
BuildingName	varchar(100)
Address	varchar(500)

Requests	
RequestID	int
Status	varchar(100)
AptID	int
Description	varchar(500)

Complexes	
ComplexID	int
ComplexName	varchar(100)

AptTenants	
TenantID	int
AptID	int

Tenants	
TenantID	int
TenantName	varchar(100)

# 15

---

## Threads and Locks

---

In a Microsoft, Google or Amazon interview, it's not terribly common to be asked to implement an algorithm with threads (unless you're working in a team for which this is a particularly important skill). It is, however, relatively common for interviewers at any company to assess your general understanding of threads, particularly your understanding of deadlocks.

This chapter will provide an introduction to this topic.

### ► Threads in Java

Every thread in Java is created and controlled by a unique object of the `java.lang.Thread` class. When a standalone application is run, a user thread is automatically created to execute the `main()` method. This thread is called the main thread.

In Java, we can implement threads in one of two ways:

- By implementing the `java.lang.Runnable` interface
- By extending the `java.lang.Thread` class

We will cover both of these below.

#### Implementing the Runnable Interface

The `Runnable` interface has the following very simple structure.

```
1 public interface Runnable {  
2     void run();  
3 }
```

To create and use a thread using this interface, we do the following:

1. Create a class which implements the `Runnable` interface. An object of this class is a `Runnable` object.
2. Create an object of type `Thread` by passing a `Runnable` object as argument to the `Thread` constructor. The `Thread` object now has a `Runnable` object that implements the `run()` method.
3. The `start()` method is invoked on the `Thread` object created in the previous step.

For example:

```
1 public class RunnableThreadExample implements Runnable {  
2     public int count = 0;  
3  
4     public void run() {  
5         System.out.println("RunnableThread starting.");  
6     }  
7 }
```

```

6     try {
7         while (count < 5) {
8             Thread.sleep(500);
9             count++;
10        }
11    } catch (InterruptedException exc) {
12        System.out.println("RunnableThread interrupted.");
13    }
14    System.out.println("RunnableThread terminating.");
15 }
16 }
17
18 public static void main(String[] args) {
19     RunnableThreadExample instance = new RunnableThreadExample();
20     Thread thread = new Thread(instance);
21     thread.start();
22
23     /* waits until above thread counts to 5 (slowly) */
24     while (instance.count != 5) {
25         try {
26             Thread.sleep(250);
27         } catch (InterruptedException exc) {
28             exc.printStackTrace();
29         }
30     }
31 }
```

In the above code, observe that all we really needed to do is have our class implement the `run()` method (line 4). Another method can then pass an instance of the class to new `Thread(obj)` (lines 19 - 20) and call `start()` on the thread (line 21).

### Extending the Thread Class

Alternatively, we can create a thread by extending the `Thread` class. This will almost always mean that we override the `run()` method, and the subclass may also call the thread constructor explicitly in its constructor.

The below code provides an example of this.

```

1  public class ThreadExample extends Thread {
2      int count = 0;
3
4      public void run() {
5          System.out.println("Thread starting.");
6          try {
7              while (count < 5) {
8                  Thread.sleep(500);
9                  System.out.println("In Thread, count is " + count);
10                 count++;
11             }
12         } catch (InterruptedException exc) {
13             System.out.println("Thread interrupted.");
14         }
15         System.out.println("Thread terminating.");
16     }
17 }
```

```
19 public class ExampleB {  
20     public static void main(String args[]) {  
21         ThreadExample instance = new ThreadExample();  
22         instance.start();  
23  
24         while (instance.count != 5) {  
25             try {  
26                 Thread.sleep(250);  
27             } catch (InterruptedException exc) {  
28                 exc.printStackTrace();  
29             }  
30         }  
31     }  
32 }
```

This code is very similar to the first approach. The difference is that since we are extending the `Thread` class, rather than just implementing an interface, we can call `start()` on the instance of the class itself.

### Extending the Thread Class vs. Implementing the Runnable Interface

When creating threads, there are two reasons why implementing the `Runnable` interface may be preferable to extending the `Thread` class:

- Java does not support multiple inheritance. Therefore, extending the `Thread` class means that the subclass cannot extend any other class. A class implementing the `Runnable` interface will be able to extend another class.
- A class might only be interested in being runnable, and therefore, inheriting the full overhead of the `Thread` class would be excessive.

## ► Synchronization and Locks

Threads within a given process share the same memory space, which is both a positive and a negative. It enables threads to share data, which can be valuable. However, it also creates the opportunity for issues when two threads modify a resource at the same time. Java provides synchronization in order to control access to shared resources.

The keyword `synchronized` and the `lock` form the basis for implementing synchronized execution of code.

### Synchronized Methods

Most commonly, we restrict access to shared resources through the use of the `synchronized` keyword. It can be applied to methods and code blocks, and restricts multiple threads from executing the code simultaneously *on the same object*.

To clarify the last point, consider the following code:

```
1 public class MyClass extends Thread {  
2     private String name;  
3     private MyObject myObj;  
4  
5     public MyClass(MyObject obj, String n) {  
6         name = n;  
7         myObj = obj;  
8     }
```

```

9
10    public void run() {
11        myObj.foo(name);
12    }
13 }
14
15 public class MyObject {
16     public synchronized void foo(String name) {
17         try {
18             System.out.println("Thread " + name + ".foo(): starting");
19             Thread.sleep(3000);
20             System.out.println("Thread " + name + ".foo(): ending");
21         } catch (InterruptedException exc) {
22             System.out.println("Thread " + name + ": interrupted.");
23         }
24     }
25 }

```

Can two instances of MyClass call foo at the same time? It depends. If they have the same instance of MyObject, then no. But, if they hold different references, then the answer is yes.

```

1 /* Difference references - both threads can call MyObject.foo() */
2 MyObject obj1 = new MyObject();
3 MyObject obj2 = new MyObject();
4 MyClass thread1 = new MyClass(obj1, "1");
5 MyClass thread2 = new MyClass(obj2, "2");
6 thread1.start();
7 thread2.start()
8
9 /* Same reference to obj. Only one will be allowed to call foo,
10 * and the other will be forced to wait. */
11 MyObject obj = new MyObject();
12 MyClass thread1 = new MyClass(obj, "1");
13 MyClass thread2 = new MyClass(obj, "2");
14 thread1.start()
15 thread2.start()

```

Static methods synchronize on the *class lock*. The two threads above could not simultaneously execute synchronized static methods on the same class, even if one is calling foo and the other is calling bar.

```

1 public class MyClass extends Thread {
2     ...
3     public void run() {
4         if (name.equals("1")) MyObject.foo(name);
5         else if (name.equals("2")) MyObject.bar(name);
6     }
7 }
8
9 public class MyObject {
10     public static synchronized void foo(String name) { /* same as before */ }
11     public static synchronized void bar(String name) { /* same as foo */ }
12 }

```

If you run this code, you will see the following printed:

```

Thread 1.foo(): starting
Thread 1.foo(): ending
Thread 2.bar(): starting
Thread 2.bar(): ending

```

### Synchronized Blocks

Similarly, a block of code can be synchronized. This operates very similarly to synchronizing a method.

```
1 public class MyClass extends Thread {  
2     ...  
3     public void run() {  
4         myObj.foo(name);  
5     }  
6 }  
7 public class MyObject {  
8     public void foo(String name) {  
9         synchronized(this) {  
10             ...  
11         }  
12     }  
13 }
```

Like synchronizing a method, only one thread per instance of `MyObject` can execute the code within the `synchronized` block. That means that, if `thread1` and `thread2` have the same instance of `MyObject`, only one will be allowed to execute the code block at a time.

### Locks

For more granular control, we can utilize a lock. A lock (or monitor) is used to synchronize access to a shared resource by associating the resource with the lock. A thread gets access to a shared resource by first acquiring the lock associated with the resource. At any given time, at most one thread can hold the lock and, therefore, only one thread can access the shared resource.

A common use case for locks is when a resource is accessed from multiple places, but should be only accessed by one thread *at a time*. This case is demonstrated in the code below.

```
1 public class LockedATM {  
2     private Lock lock;  
3     private int balance = 100;  
4  
5     public LockedATM() {  
6         lock = new ReentrantLock();  
7     }  
8  
9     public int withdraw(int value) {  
10        lock.lock();  
11        int temp = balance;  
12        try {  
13            Thread.sleep(100);  
14            temp = temp - value;  
15            Thread.sleep(100);  
16            balance = temp;  
17        } catch (InterruptedException e) {}  
18        lock.unlock();  
19        return temp;  
20    }  
21  
22    public int deposit(int value) {  
23        lock.lock();  
24        int temp = balance;  
25        try {  
26            Thread.sleep(100);  
27        } catch (InterruptedException e) {}  
28        balance = temp + value;  
29        lock.unlock();  
30        return balance;  
31    }  
32}
```

```

27     temp = temp + value;
28     Thread.sleep(300);
29     balance = temp;
30 } catch (InterruptedException e) {      }
31 lock.unlock();
32 return temp;
33 }
34 }
```

Of course, we've added code to intentionally slow down the execution of `withdraw` and `deposit`, as it helps to illustrate the potential problems that can occur. You may not write code exactly like this, but the situation it mirrors is very, very real. Using a lock will help protect a shared resource from being modified in unexpected ways.

## ► Deadlocks and Deadlock Prevention

A deadlock is a situation where a thread is waiting for an object lock that another thread holds, and this second thread is waiting for an object lock that the first thread holds (or an equivalent situation with several threads). Since each thread is waiting for the other thread to relinquish a lock, they both remain waiting forever. The threads are said to be deadlocked.

In order for a deadlock to occur, you must have all four of the following conditions met:

- Mutual Exclusion:* Only one process can access a resource at a given time. (Or, more accurately, there is limited access to a resource. A deadlock could also occur if a resource has limited quantity.)
- Hold and Wait:* Processes already holding a resource can request additional resources, without relinquishing their current resources.
- No Preemption:* One process cannot forcibly remove another process' resource.
- Circular Wait:* Two or more processes form a circular chain where each process is waiting on another resource in the chain.

Deadlock prevention entails removing any of the above conditions, but it gets tricky because many of these conditions are difficult to satisfy. For instance, removing #1 is difficult because many resources can only be used by one process at a time (e.g., printers). Most deadlock prevention algorithms focus on avoiding condition #4: circular wait.

## Interview Questions

- 15.1 Thread vs. Process:** What's the difference between a thread and a process?

Hints: #405

pg 447

- 15.2 Context Switch:** How would you measure the time spent in a context switch?

Hints: #403, #407, #415, #441

pg 447

- 15.3 Dining Philosophers:** In the famous dining philosophers problem, a bunch of philosophers are sitting around a circular table with one chopstick between each of them. A philosopher needs both chopsticks to eat, and always picks up the left chopstick before the right one. A deadlock could potentially occur if all the philosophers reached for the left chopstick at the same time. Using threads and locks, implement a simulation of the dining philosophers problem that prevents deadlocks.

Hints: #419, #437

pg 449

- 15.4 Deadlock-Free Class:** Design a class which provides a lock only if there are no possible deadlocks.

Hints: #422, #434

pg 452

- 15.5 Call In Order:** Suppose we have the following code:

```
public class Foo {  
    public Foo() { ... }  
    public void first() { ... }  
    public void second() { ... }  
    public void third() { ... }  
}
```

The same instance of Foo will be passed to three different threads. ThreadA will call first, threadB will call second, and threadC will call third. Design a mechanism to ensure that first is called before second and second is called before third.

Hints: #417, #433, #446

pg 456

- 15.6 Synchronized Methods:** You are given a class with synchronized method A and a normal method B. If you have two threads in one instance of a program, can they both execute A at the same time? Can they execute A and B at the same time?

Hints: #429

pg 458

- 15.7 FizzBuzz:** In the classic problem FizzBuzz, you are told to print the numbers from 1 to n. However, when the number is divisible by 3, print "Fizz". When it is divisible by 5, print "Buzz". When it is divisible by 3 and 5, print "FizzBuzz". In this problem, you are asked to do this in a multithreaded way. Implement a multithreaded version of FizzBuzz with four threads. One thread checks for divisibility of 3 and prints "Fizz". Another thread is responsible for divisibility of 5 and prints "Buzz". A third thread is responsible for divisibility of 3 and 5 and prints "FizzBuzz". A fourth thread does the numbers.

Hints: #414, #439, #447, #458

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Hints start on page 676.

# 16

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## Moderate

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- 16.1 Number Swapper:** Write a function to swap a number in place (that is, without temporary variables).

Hints: #492, #716, #737

pg 462

- 16.2 Word Frequencies:** Design a method to find the frequency of occurrences of any given word in a book. What if we were running this algorithm multiple times?

Hints: #489, #536

pg 463

- 16.3 Intersection:** Given two straight line segments (represented as a start point and an end point), compute the point of intersection, if any.

Hints: #465, #472, #497, #517, #527

pg 464

- 16.4 Tic Tac Win:** Design an algorithm to figure out if someone has won a game of tic-tac-toe.

Hints: #710, #732

pg 466

- 16.5 Factorial Zeros:** Write an algorithm which computes the number of trailing zeros in n factorial.

Hints: #585, #711, #729, #733, #745

pg 473

- 16.6 Smallest Difference:** Given two arrays of integers, compute the pair of values (one value in each array) with the smallest (non-negative) difference. Return the difference.

EXAMPLE

Input: {1, 3, 15, 11, 2}, {23, 127, 235, 19, 8}

Output: 3. That is, the pair (11, 8).

Hints: #632, #670, #679

pg 474

- 16.7 Number Max:** Write a method that finds the maximum of two numbers. You should not use if-else or any other comparison operator.

Hints: #473, #513, #707, #728

pg 475

- 16.8 English Int:** Given any integer, print an English phrase that describes the integer (e.g., "One Thousand, Two Hundred Thirty Four").

Hints: #502, #588, #688

pg 477

- 16.9 Operations:** Write methods to implement the multiply, subtract, and divide operations for integers. The results of all of these are integers. Use only the add operator.

Hints: #572, #600, #613, #648

pg 478

- 16.10 Living People:** Given a list of people with their birth and death years, implement a method to compute the year with the most number of people alive. You may assume that all people were born between 1900 and 2000 (inclusive). If a person was alive during any portion of that year, they should be included in that year's count. For example, Person (birth = 1908, death = 1909) is included in the counts for both 1908 and 1909.

Hints: #476, #490, #507, #514, #523, #532, #541, #549, #576

pg 482

- 16.11 Diving Board:** You are building a diving board by placing a bunch of planks of wood end-to-end. There are two types of planks, one of length shorter and one of length longer. You must use exactly K planks of wood. Write a method to generate all possible lengths for the diving board.

Hints: #690, #700, #715, #722, #740, #747

pg 486

- 16.12 XML Encoding:** Since XML is very verbose, you are given a way of encoding it where each tag gets mapped to a pre-defined integer value. The language/grammar is as follows:

Element --> Tag Attributes END Children END  
Attribute --> Tag Value  
END --> 0  
Tag --> some predefined mapping to int  
Value --> string value

For example, the following XML might be converted into the compressed string below (assuming a mapping of family -> 1, person -> 2, firstName -> 3, lastName -> 4, state -> 5).

```
<family lastName="McDowell" state="CA">  
    <person firstName="Gayle">Some Message</person>  
</family>
```

Becomes:

```
1 4 McDowell 5 CA 0 2 3 Gayle 0 Some Message 0 0
```

Write code to print the encoded version of an XML element (passed in Element and Attribute objects).

Hints: #466

pg 489

- 16.13 Bisect Squares:** Given two squares on a two-dimensional plane, find a line that would cut these two squares in half. Assume that the top and the bottom sides of the square run parallel to the x-axis.

Hints: #468, #479, #528, #560

pg 490

- 16.14 Best Line:** Given a two-dimensional graph with points on it, find a line which passes the most number of points.

Hints: #491, #520, #529, #563

pg 492

- 16.15 Master Mind:** The Game of Master Mind is played as follows:

The computer has four slots, and each slot will contain a ball that is red (R), yellow (Y), green (G) or blue (B). For example, the computer might have RGGB (Slot #1 is red, Slots #2 and #3 are green, Slot #4 is blue).

You, the user, are trying to guess the solution. You might, for example, guess YRGB.

When you guess the correct color for the correct slot, you get a "hit." If you guess a color that exists but is in the wrong slot, you get a "pseudo-hit." Note that a slot that is a hit can never count as a pseudo-hit.

For example, if the actual solution is RGBY and you guess GGRR, you have one hit and one pseudo-hit.

Write a method that, given a guess and a solution, returns the number of hits and pseudo-hits.

Hints: #639, #730

pg 493

- 16.16 Sub Sort:** Given an array of integers, write a method to find indices  $m$  and  $n$  such that if you sorted elements  $m$  through  $n$ , the entire array would be sorted. Minimize  $n - m$  (that is, find the smallest such sequence).

EXAMPLE

Input: 1, 2, 4, 7, 10, 11, 7, 12, 6, 7, 16, 18, 19

Output: (3, 9)

Hints: #482, #553, #667, #708, #735, #746

pg 494

- 16.17 Contiguous Sequence:** You are given an array of integers (both positive and negative). Find the contiguous sequence with the largest sum. Return the sum.

EXAMPLE

Input: 2, -8, 3, -2, 4, -10

Output: 5 (i.e., {3, -2, 4})

Hints: #531, #551, #567, #594, #614

pg 495

- 16.18 Pattern Matching:** You are given two strings, pattern and value. The pattern string consists of just the letters a and b, describing a pattern within a string. For example, the string catcatgocatgo matches the pattern aabab (where cat is a and go is b). It also matches patterns like a, ab, and b. Write a method to determine if value matches pattern.

Hints: #631, #643, #653, #663, #685, #718, #727

pg 496

**16.19 Pond Sizes:** You have an integer matrix representing a plot of land, where the value at that location represents the height above sea level. A value of zero indicates water. A pond is a region of water connected vertically, horizontally, or diagonally. The size of the pond is the total number of connected water cells. Write a method to compute the sizes of all ponds in the matrix.

EXAMPLE

Input:

```
0 2 1 0
0 1 0 1
1 1 0 1
0 1 0 1
```

Output: 2, 4, 1 (in any order)

Hints: #674, #687, #706, #723

pg 503

**16.20 T9:** On old cell phones, users typed on a numeric keypad and the phone would provide a list of words that matched these numbers. Each digit mapped to a set of 0 - 4 letters. Implement an algorithm to return a list of matching words, given a sequence of digits. You are provided a list of valid words (provided in whatever data structure you'd like). The mapping is shown in the diagram below:

1	2 abc	3 def
4 ghi	5 jkl	6 mno
7 pqrs	8 tuv	9 wxyz
	0	

EXAMPLE

Input: 8733

Output: tree, used

Hints: #471, #487, #654, #703, #726, #744

pg 505

**16.21 Sum Swap:** Given two arrays of integers, find a pair of values (one value from each array) that you can swap to give the two arrays the same sum.

EXAMPLE

Input: {4, 1, 2, 1, 1, 2} and {3, 6, 3, 3}

Output: {1, 3}

Hints: #545, #557, #564, #571, #583, #592, #602, #606, #635

pg 509

**16.22 Langton's Ant:** An ant is sitting on an infinite grid of white and black squares. It initially faces right. At each step, it does the following:

- (1) At a white square, flip the color of the square, turn 90 degrees right (clockwise), and move forward one unit.
- (2) At a black square, flip the color of the square, turn 90 degrees left (counter-clockwise), and move forward one unit.

Write a program to simulate the first K moves that the ant makes and print the final board as a grid. Note that you are not provided with the data structure to represent the grid. This is something you must design yourself. The only input to your method is K. You should print the final grid and return nothing. The method signature might be something like `void printKMoves(int K)`.

Hints: #474, #481, #533, #540, #559, #570, #599, #616, #627

pg 512

**16.23 Rand7 from Rand5:** Implement a method `rand7()` given `rand5()`. That is, given a method that generates a random number between 0 and 4 (inclusive), write a method that generates a random number between 0 and 6 (inclusive).

Hints: #505, #574, #637, #668, #697, #720

pg 518

**16.24 Pairs with Sum:** Design an algorithm to find all pairs of integers within an array which sum to a specified value.

Hints: #548, #597, #644, #673

pg 520

**16.25 LRU Cache:** Design and build a “least recently used” cache, which evicts the least recently used item. The cache should map from keys to values (allowing you to insert and retrieve a value associated with a particular key) and be initialized with a max size. When it is full, it should evict the least recently used item.

Hints: #524, #630, #694

pg 521

**16.26 Calculator:** Given an arithmetic equation consisting of positive integers, +, -, \* and / (no parentheses), compute the result.

EXAMPLE

Input: 2\*3+5/6\*3+15

Output: 23.5

Hints: #521, #624, #665, #698

pg 524

# 17

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## Hard

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- 17.1 Add Without Plus:** Write a function that adds two numbers. You should not use + or any arithmetic operators.

Hints: #467, #544, #601, #628, #642, #664, #692, #712, #724

pg 530

- 17.2 Shuffle:** Write a method to shuffle a deck of cards. It must be a perfect shuffle—in other words, each of the  $52!$  permutations of the deck has to be equally likely. Assume that you are given a random number generator which is perfect.

Hints: #483, #579, #634

pg 531

- 17.3 Random Set:** Write a method to randomly generate a set of  $m$  integers from an array of size  $n$ . Each element must have equal probability of being chosen.

Hints: #494, #596

pg 532

- 17.4 Missing Number:** An array  $A$  contains all the integers from 0 to  $n$ , except for one number which is missing. In this problem, we cannot access an entire integer in  $A$  with a single operation. The elements of  $A$  are represented in binary, and the only operation we can use to access them is “fetch the  $j$ th bit of  $A[i]$ ,” which takes constant time. Write code to find the missing integer. Can you do it in  $O(n)$  time?

Hints: #610, #659, #683

pg 533

- 17.5 Letters and Numbers:** Given an array filled with letters and numbers, find the longest subarray with an equal number of letters and numbers.

Hints: #485, #515, #619, #671, #713

pg 536

- 17.6 Count of 2s:** Write a method to count the number of 2s that appear in all the numbers between 0 and  $n$  (inclusive).

EXAMPLE

Input: 25

Output: 9 (2, 12, 20, 21, 22, 23, 24 and 25. Note that 22 counts for two 2s.)

Hints: #573, #612, #641

pg 538

- 17.7 Baby Names:** Each year, the government releases a list of the 10000 most common baby names and their frequencies (the number of babies with that name). The only problem with this is that some names have multiple spellings. For example, "John" and "Jon" are essentially the same name but would be listed separately in the list. Given two lists, one of names/frequencies and the other of pairs of equivalent names, write an algorithm to print a new list of the true frequency of each name. Note that if John and Jon are synonyms, and Jon and Johnny are synonyms, then John and Johnny are synonyms. (It is both transitive and symmetric.) In the final list, any name can be used as the "real" name.

EXAMPLE

Input:

Names: John (15), Jon (12), Chris (13), Kris (4), Christopher (19)

Synonyms: (Jon, John), (John, Johnny), (Chris, Kris), (Chris, Christopher)

Output: John (27), Kris (36)

Hints: #478, #493, #512, #537, #586, #605, #655, #675, #704

pg 541

- 17.8 Circus Tower:** A circus is designing a tower routine consisting of people standing atop one another's shoulders. For practical and aesthetic reasons, each person must be both shorter and lighter than the person below him or her. Given the heights and weights of each person in the circus, write a method to compute the largest possible number of people in such a tower.

EXAMPLE

Input (ht, wt): (65, 100) (70, 150) (56, 90) (75, 190) (60, 95) (68, 110)

Output: The longest tower is length 6 and includes from top to bottom:

(56, 90) (60, 95) (65, 100) (68, 110) (70, 150) (75, 190)

Hints: #638, #657, #666, #682, #699

pg 546

- 17.9 Kth Multiple:** Design an algorithm to find the kth number such that the only prime factors are 3, 5, and 7. Note that 3, 5, and 7 do not have to be factors, but it should not have any other prime factors. For example, the first several multiples would be (in order) 1, 3, 5, 7, 9, 15, 21.

Hints: #488, #508, #550, #591, #622, #660, #686

pg 549

- 17.10 Majority Element:** A majority element is an element that makes up more than half of the items in an array. Given a positive integers array, find the majority element. If there is no majority element, return -1. Do this in O(N) time and O(1) space.

EXAMPLE

Input: 1 2 5 9 5 9 5 5 5

Output: 5

Hints: #522, #566, #604, #620, #650

pg 554

- 17.11 Word Distance:** You have a large text file containing words. Given any two words, find the shortest distance (in terms of number of words) between them in the file. If the operation will be repeated many times for the same file (but different pairs of words), can you optimize your solution?

Hints: #486, #501, #538, #558, #633

pg 557

- 17.12 BiNode:** Consider a simple data structure called BiNode, which has pointers to two other nodes.

```
public class BiNode {  
    public BiNode node1, node2;  
    public int data;  
}
```

The data structure BiNode could be used to represent both a binary tree (where node1 is the left node and node2 is the right node) or a doubly linked list (where node1 is the previous node and node2 is the next node). Implement a method to convert a binary search tree (implemented with BiNode) into a doubly linked list. The values should be kept in order and the operation should be performed in place (that is, on the original data structure).

Hints: #509, #608, #646, #680, #701, #719

pg 560

- 17.13 Re-Space:** Oh, no! You have accidentally removed all spaces, punctuation, and capitalization in a lengthy document. A sentence like "I reset the computer. It still didn't boot!" became "iresetthecomputeritstilldidntboot". You'll deal with the punctuation and capitalization later; right now you need to re-insert the spaces. Most of the words are in a dictionary but a few are not. Given a dictionary (a list of strings) and the document (a string), design an algorithm to unconcatenate the document in a way that minimizes the number of unrecognized characters.

EXAMPLE:

Input: jesslookedjustliketimherbrother

Output: jess looked just like tim her brother (7 unrecognized characters)

Hints: #496, #623, #656, #677, #739, #749

pg 561

- 17.14 Smallest K:** Design an algorithm to find the smallest K numbers in an array.

Hints: #470, #530, #552, #593, #625, #647, #661, #678

pg 567

- 17.15 Longest Word:** Given a list of words, write a program to find the longest word made of other words in the list.

EXAMPLE

Input: cat, banana, dog, nana, walk, walker, dogwalker

Output: dogwalker

Hints: #475, #499, #543, #589

pg 572

- 17.16 The Masseuse:** A popular masseuse receives a sequence of back-to-back appointment requests and is debating which ones to accept. She needs a 15-minute break between appointments and therefore she cannot accept any adjacent requests. Given a sequence of back-to-back appointment requests (all multiples of 15 minutes, none overlap, and none can be moved), find the optimal (highest total booked minutes) set the masseuse can honor. Return the number of minutes.

EXAMPLE

Input: {30, 15, 60, 75, 45, 15, 15, 45}

Output: 180 minutes ({30, 60, 45, 45}).

Hints: #495, #504, #516, #526, #542, #554, #562, #568, #578, #587, #607

pg 574

- 17.17 Multi Search:** Given a string b and an array of smaller strings T, design a method to search b for each small string in T.

Hints: #480, #582, #617, #743

pg 578

- 17.18 Shortest Supersequence:** You are given two arrays, one shorter (with all distinct elements) and one longer. Find the shortest subarray in the longer array that contains all the elements in the shorter array. The items can appear in any order.

EXAMPLE

Input: {1, 5, 9} | {7, 5, 9, 0, 2, 1, 3, 5, 7, 9, 1, 1, 5, 8, 8, 9, 7}

Output: [7, 10] (the underlined portion above)

Hints: #645, #652, #669, #681, #691, #725, #731, #741

pg 584

- 17.19 Missing Two:** You are given an array with all the numbers from 1 to N appearing exactly once, except for one number that is missing. How can you find the missing number in O(N) time and O(1) space? What if there were two numbers missing?

Hints: #503, #590, #609, #626, #649, #672, #689, #696, #702, #717

pg 591

- 17.20 Continuous Median:** Numbers are randomly generated and passed to a method. Write a program to find and maintain the median value as new values are generated.

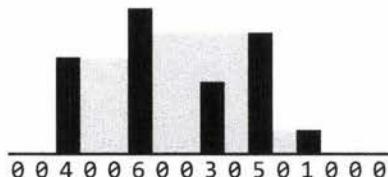
Hints: #519, #546, #575, #709

pg 595

- 17.21 Volume of Histogram:** Imagine a histogram (bar graph). Design an algorithm to compute the volume of water it could hold if someone poured water across the top. You can assume that each histogram bar has width 1.

EXAMPLE (Black bars are the histogram. Gray is water.)

Input: {0, 0, 4, 0, 0, 6, 0, 0, 3, 0, 5, 0, 1, 0, 0, 0}



Output: 26

Hints: #629, #640, #651, #658, #662, #676, #693, #734, #742

pg 596

- 17.22 Word Transformer:** Given two words of equal length that are in a dictionary, write a method to transform one word into another word by changing only one letter at a time. The new word you get in each step must be in the dictionary.

EXAMPLE

Input: DAMP, LIKE

Output: DAMP -> LAMP -> LIMP -> LIME -> LIKE

Hints: #506, #535, #556, #580, #598, #618, #738

pg 602

- 17.23 Max Black Square:** Imagine you have a square matrix, where each cell (pixel) is either black or white. Design an algorithm to find the maximum subsquare such that all four borders are filled with black pixels.

Hints: #684, #695, #705, #714, #721, #736

pg 608

- 17.24 Max Submatrix:** Given an NxN matrix of positive and negative integers, write code to find the submatrix with the largest possible sum.

Hints: #469, #511, #525, #539, #565, #581, #595, #615, #621

pg 611

- 17.25 Word Rectangle:** Given a list of millions of words, design an algorithm to create the largest possible rectangle of letters such that every row forms a word (reading left to right) and every column forms a word (reading top to bottom). The words need not be chosen consecutively from the list, but all rows must be the same length and all columns must be the same height.

Hints: #477, #500, #748

pg 615

- 17.26 Sparse Similarity:** The similarity of two documents (each with distinct words) is defined to be the size of the intersection divided by the size of the union. For example, if the documents consist of integers, the similarity of {1, 5, 3} and {1, 7, 2, 3} is 0.4, because the intersection has size 2 and the union has size 5.

We have a long list of documents (with distinct values and each with an associated ID) where the similarity is believed to be "sparse." That is, any two arbitrarily selected documents are very likely to have similarity 0. Design an algorithm that returns a list of pairs of document IDs and the associated similarity.

Print only the pairs with similarity greater than 0. Empty documents should not be printed at all. For simplicity, you may assume each document is represented as an array of distinct integers.

#### EXAMPLE

Input:

```
13: {14, 15, 100, 9, 3}  
16: {32, 1, 9, 3, 5}  
19: {15, 29, 2, 6, 8, 7}  
24: {7, 10}
```

Output:

```
ID1, ID2 : SIMILARITY  
13, 19   : 0.1  
13, 16   : 0.25  
19, 24   : 0.14285714285714285
```

Hints: #484, #498, #510, #518, #534, #547, #555, #561, #569, #577, #584, #603, #611, #636

pg 620

# Solutions

X

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