

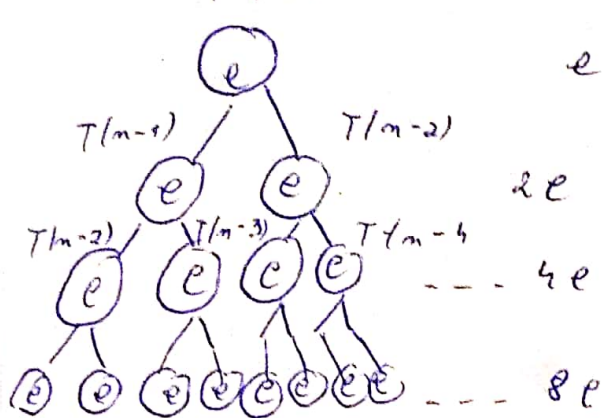
⑤ Pentru $n=0$: $T(0) = c$

$$n=1 : T(1) = d$$

$$n > 1 : T(n) = T(n-2) + T(n-1) + \Theta(1)$$

$$T(n) = T(n-2) + T(n-1) + e$$

$T(n)$



$$e = 2^0 \cdot e$$

$$2e = 2^1 \cdot e$$

$$4e = 2^2 \cdot e$$

$$8e = 2^3 \cdot e$$

$$= 2^{h-1} \cdot e$$

$$= e(2^0 + 2^1 + \dots + 2^{h-1}) = e \frac{2^{h+0} - 1}{2 - 1} =$$

$$= e(2^{h+0} - 1) = e \cdot (2^h - 1)$$

Dar
 $h_1 = n$

$$h_2 = \frac{n}{2}$$

$$\Rightarrow T_1 = e(2^{n-1}) \quad \text{și} \quad T_2 = e(2^{\frac{n}{2}-1})$$

$$(2^{\frac{n}{2}-1}e < T(n) < e(2^{n-1})) \Leftrightarrow$$

$$(\Rightarrow e\sqrt{2} \cdot 2^{\frac{n}{2}} - e < T(n) < e \cdot 2^{\frac{n}{2}} - e$$

$$\Theta(2^{\frac{n}{2}})$$

$$\Rightarrow T(n) \in \Theta(2^{\frac{n}{2}})$$