

## **Some Important Introductory Concepts: Scientific notation; how to get used to units; distances, angles,**

These preliminaries are an important part of the course because if you don't become *comfortable* with them, you may have difficulty reading the textbook and understanding the lecture material.

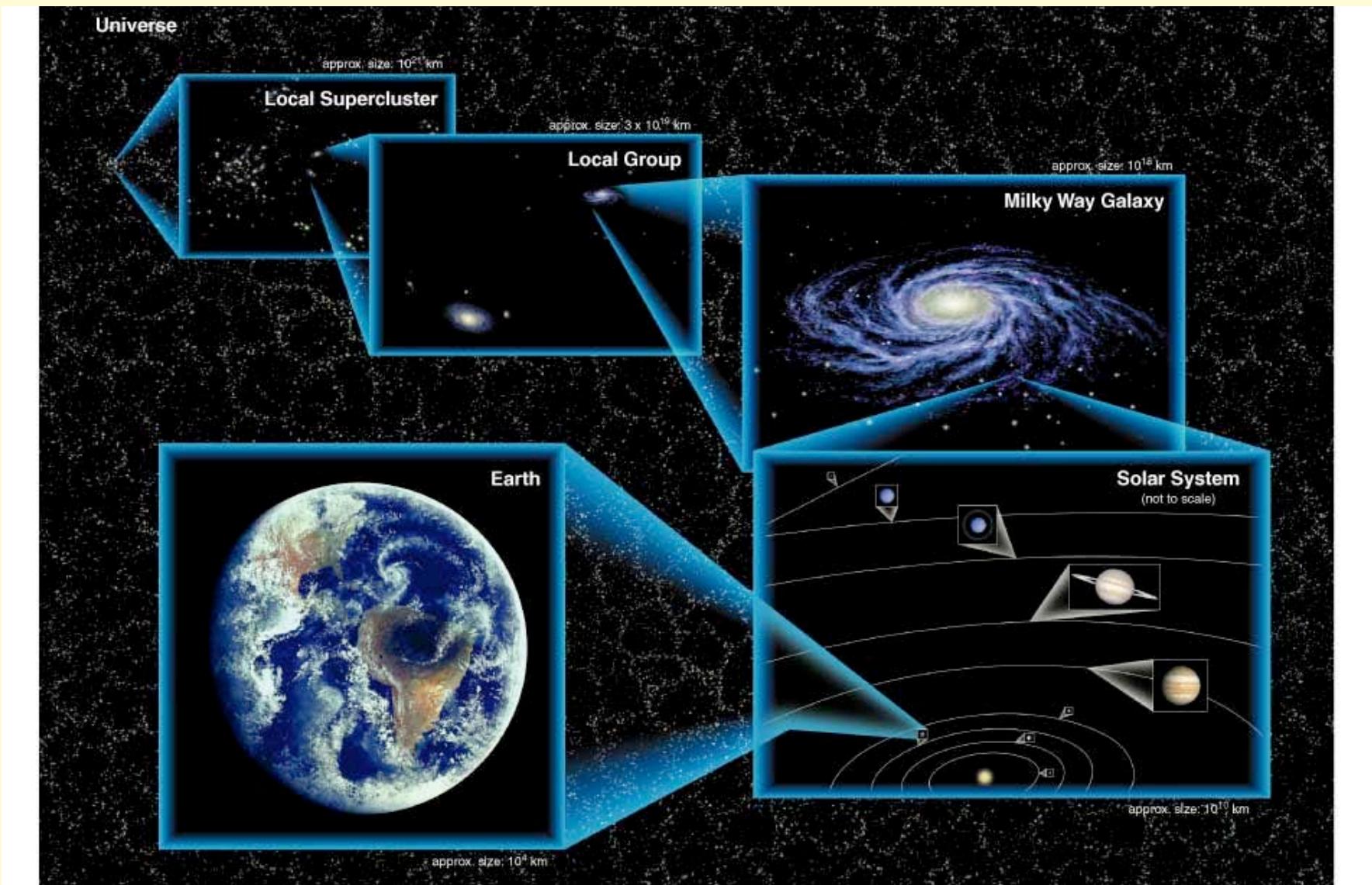
There is also more here than meets the eye--notice the huge range of scales that you will encounter for everything, from atoms to planets to galaxies. Now is a good time to see if you can give a typical value for the size of these various objects.

FIRST: → **Scientific notation** for very large and small numbers  
**(read Appendix 1 in text)**

Example:  $3 \times 10^6$  = 3 million,  $4 \times 10^{-3}$  = 0.004.

You will continuously encounter this notation in the textbook, so become comfortable with it now (even though I will not ask you to manipulate such numbers on exams). Just get used to it—try writing down a few yourself—e.g. two million, 3 one-thousandths, ...

Range of size scales in the universe requires the use of a variety of **units of distance** -- kilometer (km), astronomical unit (AU), parsec (pc), kiloparsec (kpc), megaparsec (Mpc)



## **Units of length, size, mass, ... *Defined just for convenience***

→ First, realize that the units we use in measuring *anything* are usually just for convenience. You don't give the distance from Austin to New York in inches, or your age in seconds, or your height in miles.

Example: For distance or size, we could use "microns" for light waves or for dust particles, "centimeters" or "inches" for everyday objects, "light years" or "parsecs" for stars, "megaparsecs" for galaxies.

→ This is really nothing--you just have to get used to it! Keep thinking about it for a while and soon it will be second nature.

*It will help if you associate each new unit with some object--e.g. a "micron" is 0.0001 cm, but you don't need to know that, only that it is like the size of a microscopic dust grain.*

Appendix 2 in the textbook goes over some of this; just skim it now and use it for future reference if you become confused about units. But we will only be using a few units in this class, so it shouldn't cause any problem.

Another (important) example: it is convenient to state the masses of astronomical objects in units of the Sun's mass, e.g. "200 solar masses" or "200  $M_{\text{sun}}$ " instead of writing " $4 \times 10^{35}$  grams." The masses of many galaxies (including our own) are in the range  $10^9$  to  $10^{12}$  solar masses, so you can see there is no escaping scientific notation, even if we use a convenient unit. The range of properties of astronomical objects is just too large.

→ *What unit would you use to express the mass of the planets in our solar system?*

**Angular measure** – degree, arcminute, **arcsecond** (especially important).

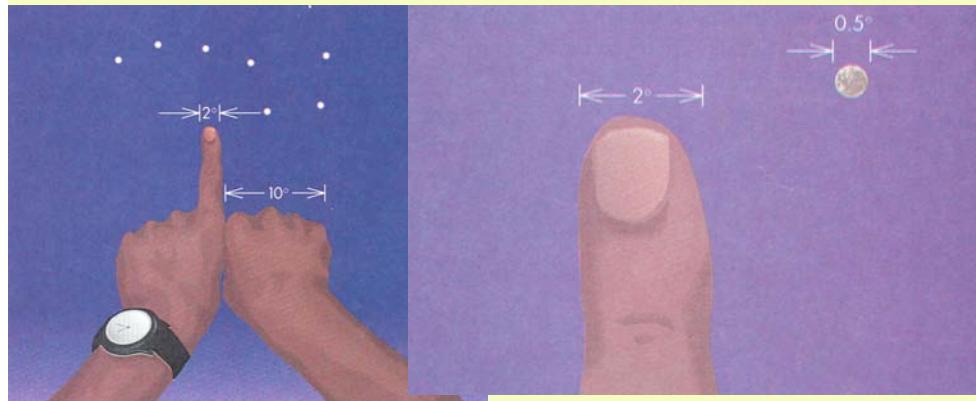
*This is usually the most difficult kind of unit for students to get used to. [See box p. 11]*

→ Angular measure using “**arcsecond**” terminology will occur in many places throughout the course (first in connection with “parallax”).

Most astronomy today commonly breaks the “arcsecond barrier” imposed by our own Earth’s atmosphere. (This effect, called “scintillation,” is due to the turbulence in the Earth’s atmosphere, which makes stars “twinkle.”)

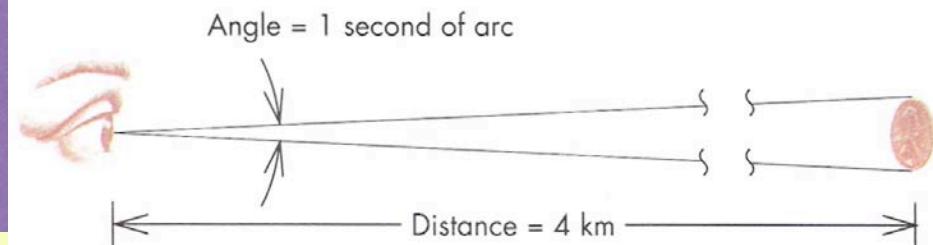
→ The term for the smallest angular size at which you can distinguish objects is called “**angular resolution**,” a phrase you will encounter frequently! Learn it now!

You can remember what resolution means by keeping in mind that poor resolution is like being very nearsighted—everything looks blurry → “you can’t resolve it”



#### One Second of Arc

A penny at a distance of 4 km (2.5 miles) has an angular diameter of 1 second of arc.



**Constellations:** These are just apparent groupings of stars in the sky; they are (usually) not physically associated, and could be at *very* different distances (see Orion example).

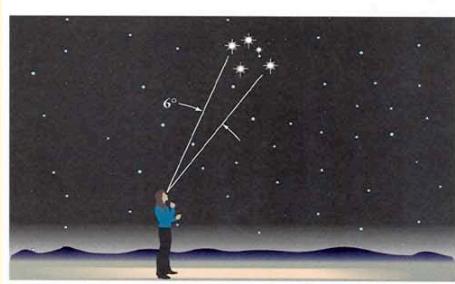
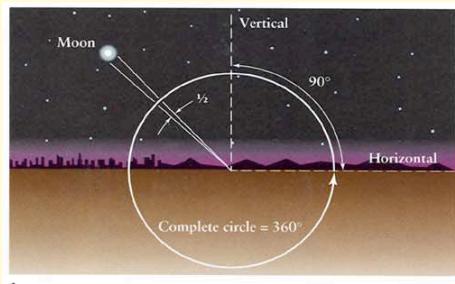
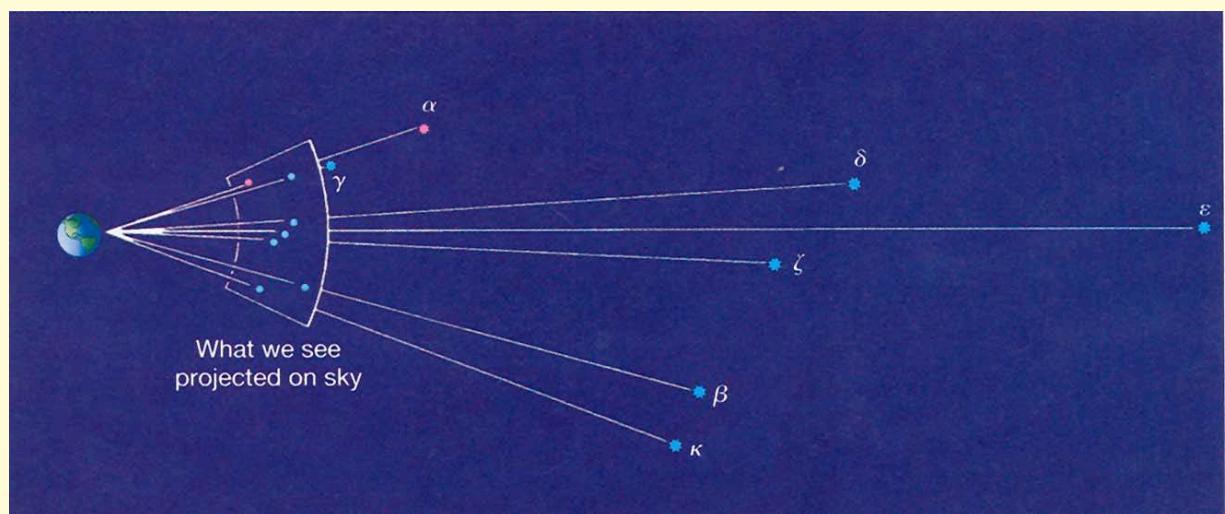
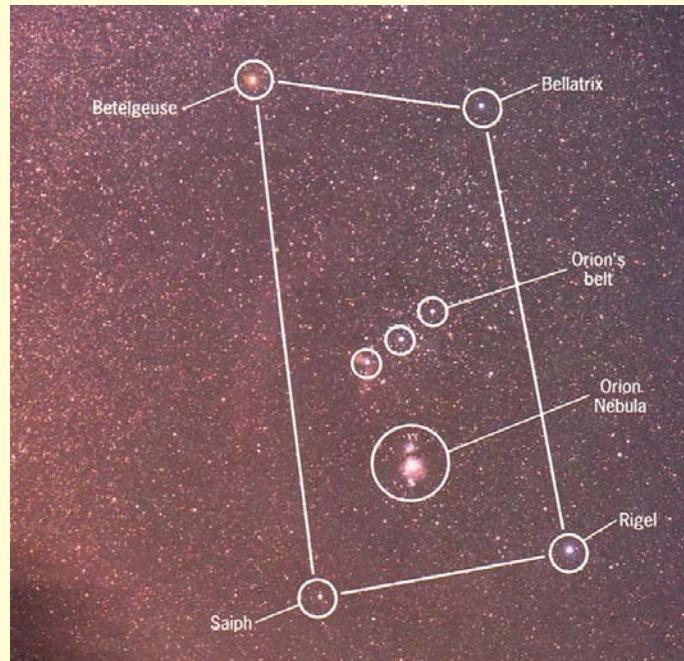
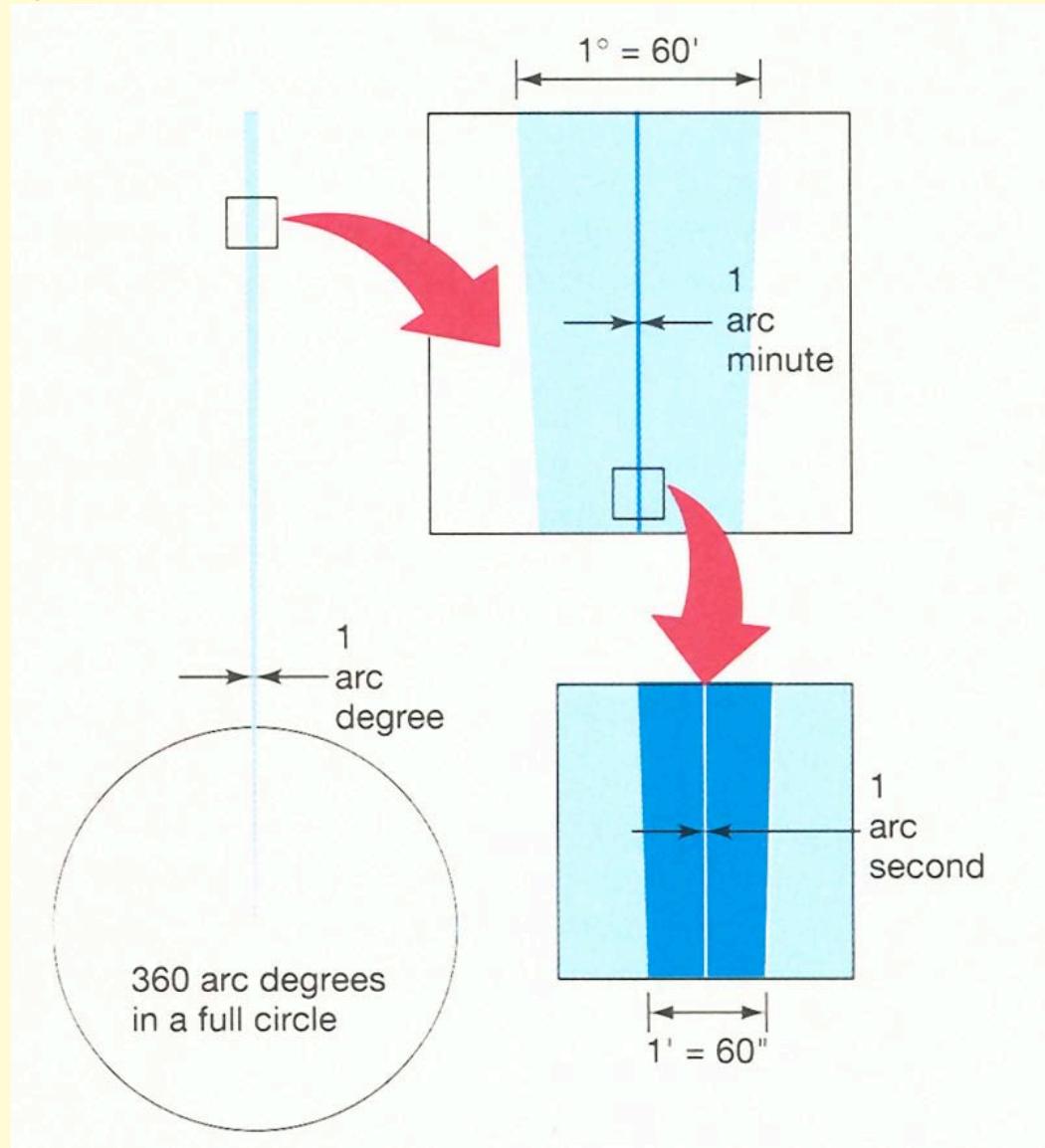


Figure 1-9

**Angles and Angular Measure** (a) Angles are measured in degrees ( $^{\circ}$ ). There are  $360^{\circ}$  in a complete circle and  $90^{\circ}$  in a right angle. For example, the angle between the vertical direction (directly above you) and the horizontal direction (toward the horizon) is  $90^{\circ}$ . The angular diameter of the full moon in the sky is about  $\frac{1}{2}^{\circ}$ . (b) The Big Dipper is an easily recognized grouping of seven bright stars, visible from anywhere in the northern hemisphere. The angular distance between the two pointer stars at the front of the Big Dipper is about  $5^{\circ}$ , roughly ten times the angular diameter of the Moon. (c) The four bright stars that make up the Southern Cross can be seen from anywhere in the southern hemisphere. The angular distance between the stars at the top and bottom of the cross is about  $6^{\circ}$ .



Angular measure--illustration from your textbook.

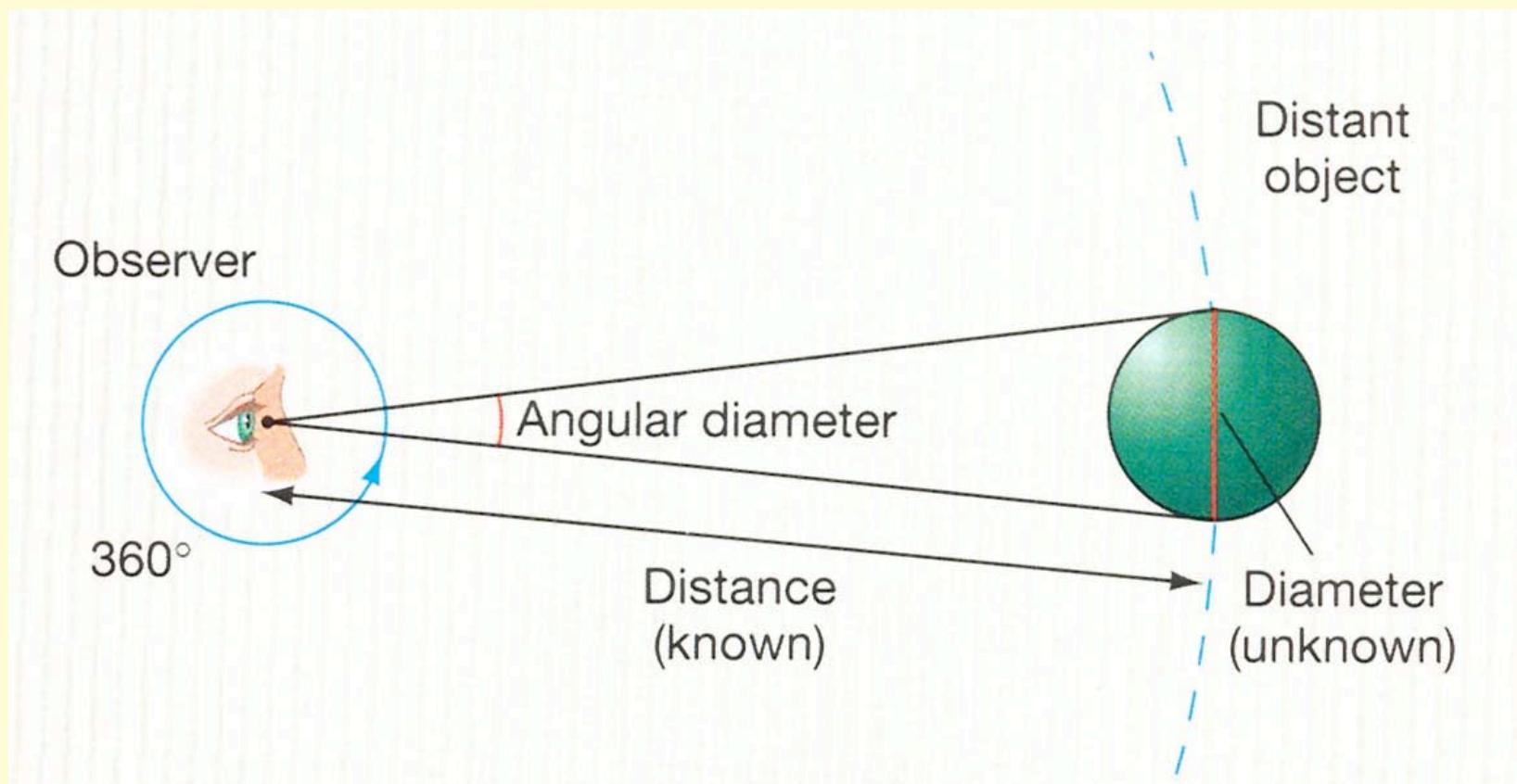


**Angular diameter of an object** --notice how you could get the distance of the object if you knew its size, or its size if you knew its distance.

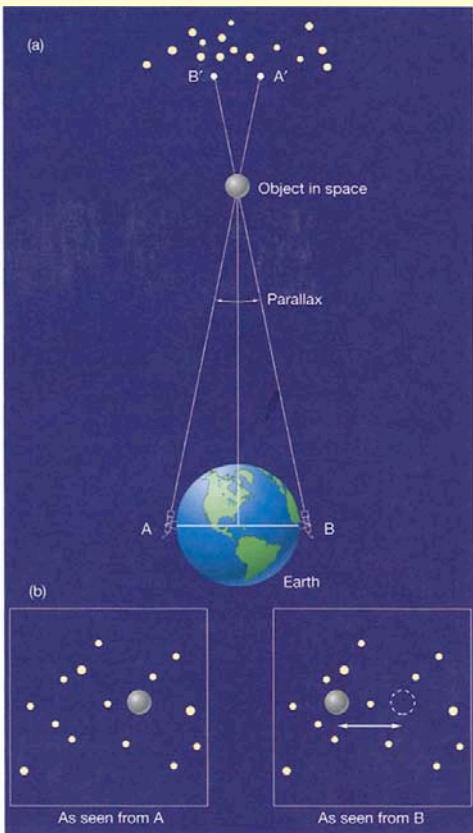
(The formula is that diameter = distance x angular diameter (in "radians.)

But if you can't "resolve" the object, then you can't use this method at all (e.g. for stars).

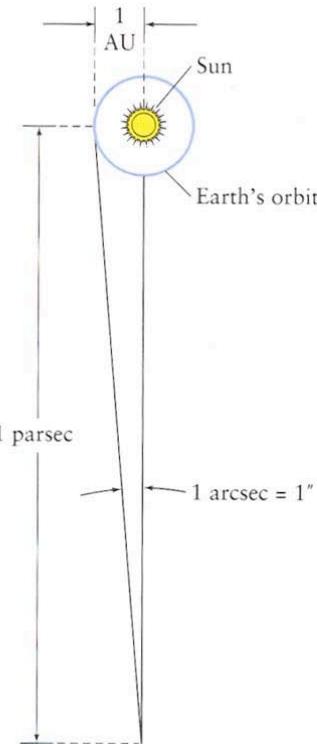
*Make sure you understand what that last sentence means!*



## Distances from Parallax Angle (sec. 1.7 in text)



**▲ FIGURE 1.31** Parallax (a) This imaginary triangle extends from Earth to a nearby object in space (such as a planet). The group of stars at the top represents a background field of very distant stars. (b) Hypothetical photographs of the same star field showing the nearby object's apparent displacement, or shift, relative to the distant, undisplaced stars.



**A Parsec** The parsec, a unit of length commonly used by astronomers, is equal to 3.26 light-years. The parsec is defined as the distance at which 1 AU perpendicular to the observer's line of sight subtends an angle of 1 arcsec.

**Left:** Parallax using diameter of Earth. Understand why baseline is too small for stellar distances.

**Right:** Parallax using 1AU defines the unit of distance called a “parsec” (for distance of object whose parallax is one second of arc (one arcsec). This is abbreviated pc, as in “That star is 6.3 pc away.”

## Distances and sizes in the universe

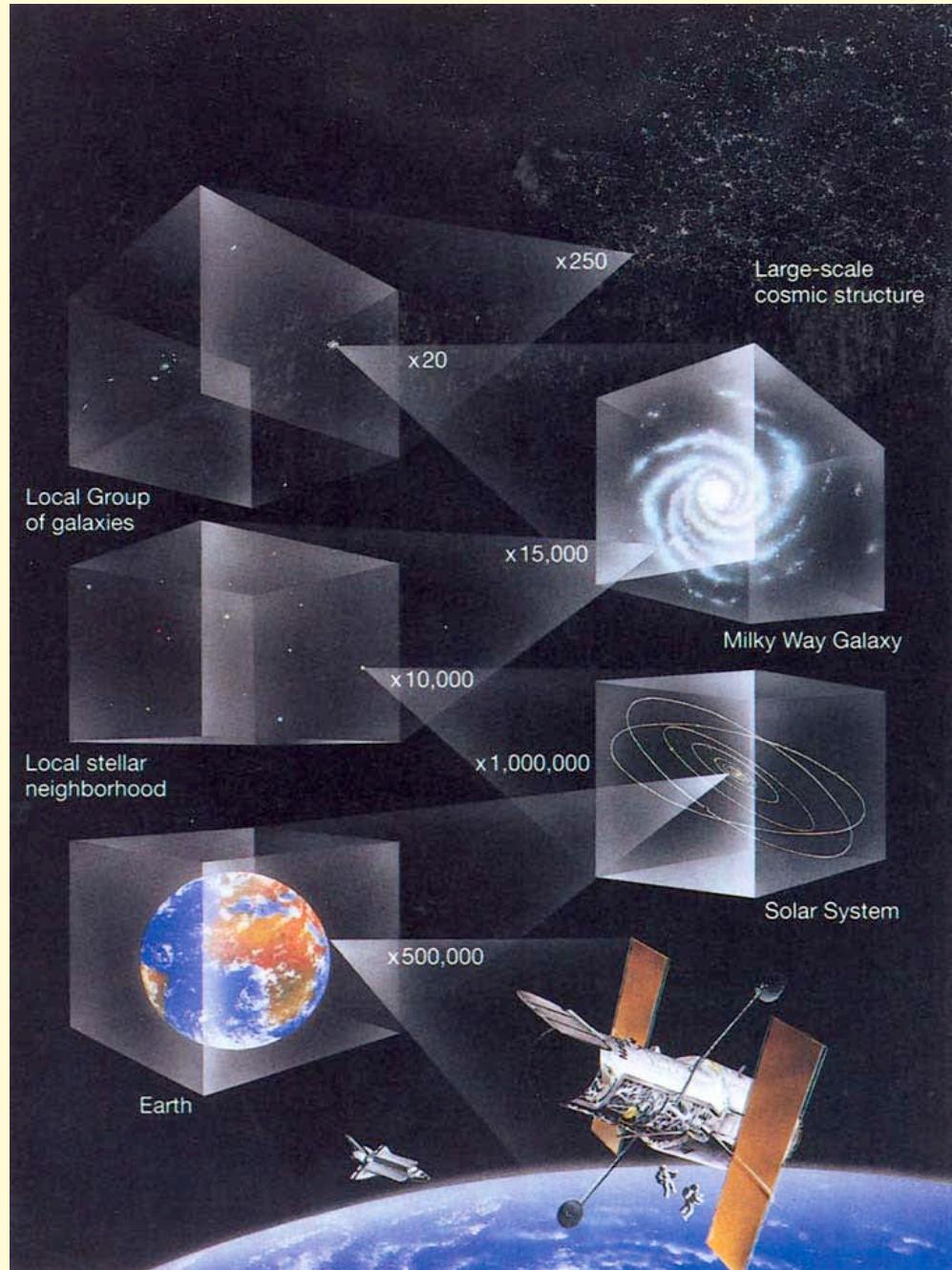
The measurement of distances to stars by parallax is the first step in a long line of methods to learn about the scale of the universe at larger and larger distances.

**Can you explain why distances are so important to astronomy?**

- Can only use *parallax* for nearest ~ few 100 pc (because stars more distant than that have parallaxes so small that they can't be measured (yet), even from space.  
Be able to explain this!

*What we end up with is an amazing range of sizes and distances of various objects in the universe, as shown in the illustration to the right (from your text; good idea to stare at it a while).*

*But parallax is only the first step...  
(we'll take this up repeatedly throughout the course)*



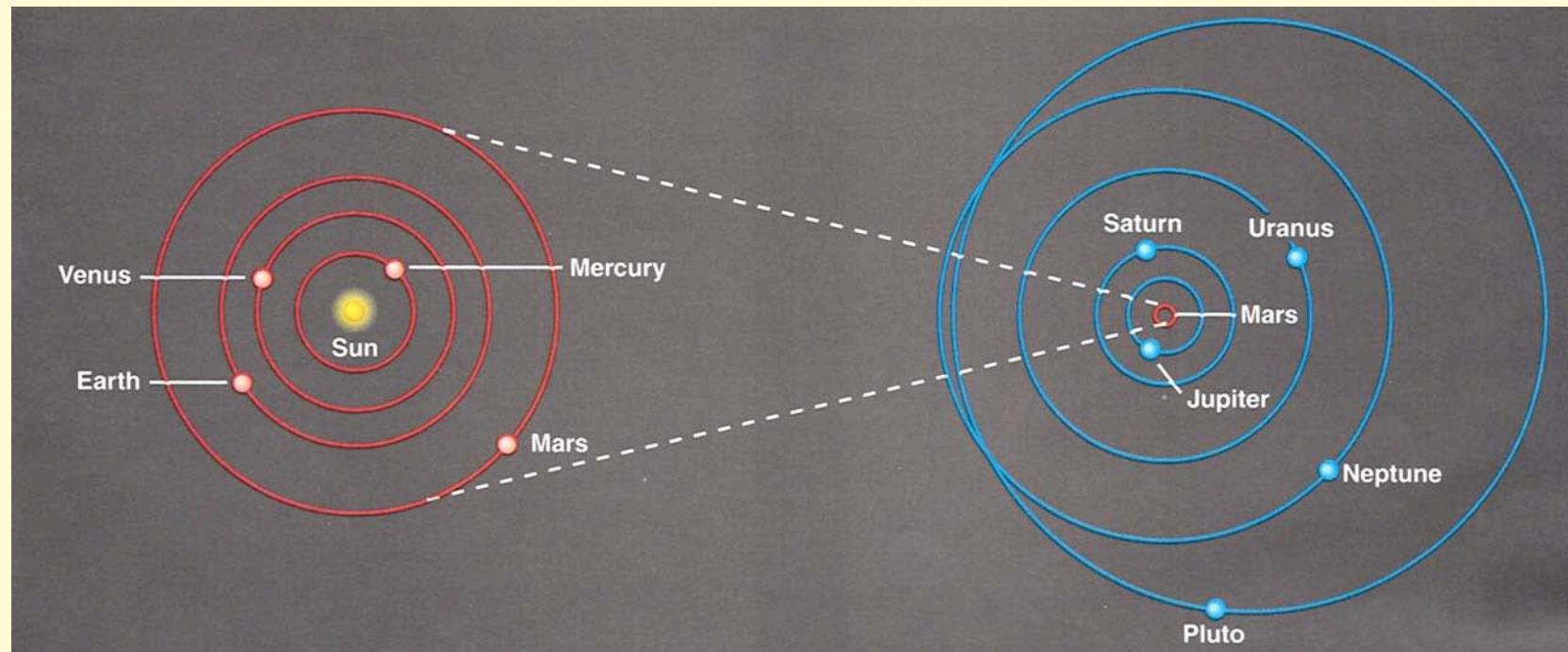
**Distances:** We'll return to parallax in more detail later in the course: for now you should just get the basic idea, and how it relates to the unit of distance called "**parsec**."

→ **Nearest stars** are about 1 pc (a few light years) away. This is also the average distance between neighboring stars in most galaxies. **It is a number that you should remember.**

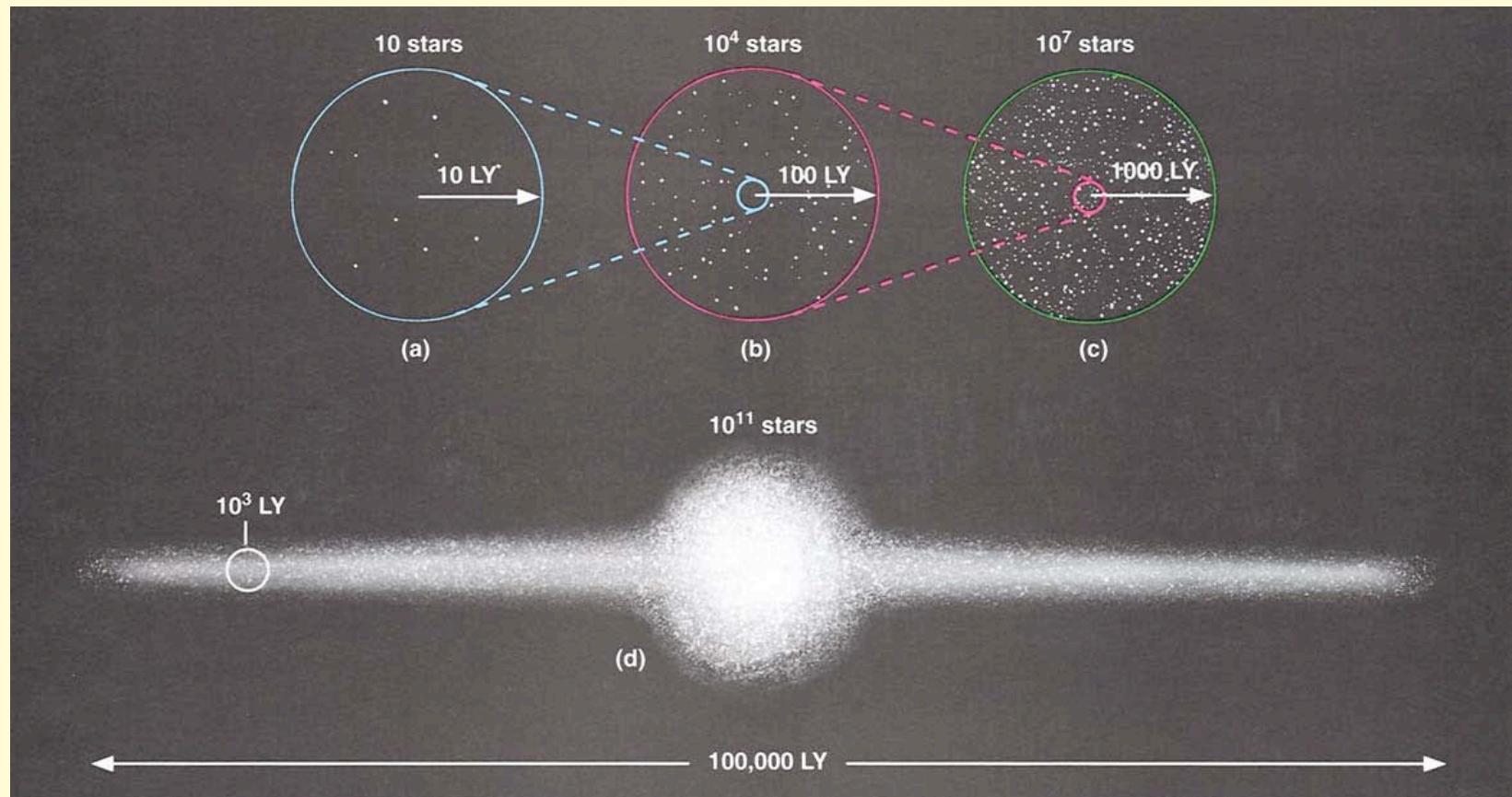
→ **Size of our Galaxy** and many others is about 10,000 pc, and the distances between galaxies range from millions (Mpc) to billions of pc (1000 Mpc—make sure you are comfortable with what this means--see preceding figure again).

→ For **distances in the solar system**, see sec. 2.6. Average distance from Earth to Sun defined as "**astronomical unit**" (1AU) ( $\sim 10^{-3}$  pc), size of our solar system  $\sim 100$  AU.

See picture below.



As we move out from the solar system to see the nearest stars, the scale of distances expands enormously--100AU is *tiny* compared to the average distances between stars, and nearly infinitesimal compared to the sizes of galaxies or larger structures in the universe.



## End of “units”

**Next:** Leading up to *Kepler’s “laws”* and then, most importantly, *Newton’s three laws of motion*, and his *law of gravity*.

*For next class (Monday), you should read the textbook through Kepler’s laws and begin Newton’s laws. Then try to answer this apparently boring question:*

Gravity is what makes objects orbit around other objects.

→ So why doesn’t the mass of the objects appear in Kepler’s 3rd law?

## Geocentric vs. heliocentric model (sec. 2.2-2.4)

The important historical progression is the following:

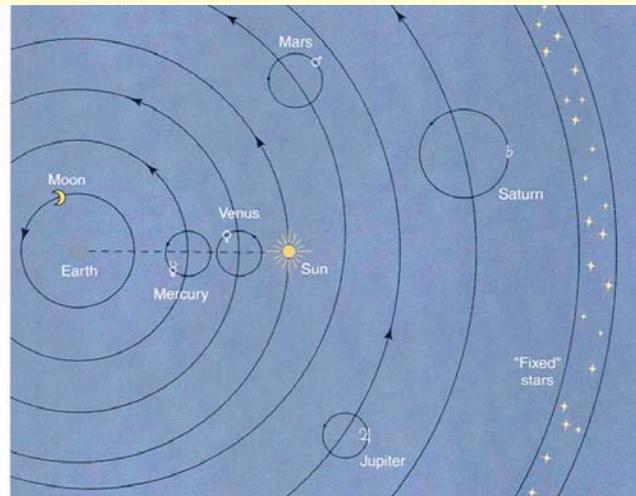
→ Ptolemy (~140 AD) ... Copernicus (~1500 AD), Galileo (~1600), Tycho Brahe,  
Kepler (2.5), Newton (2.6).

It is important to recognize the change in world view brought about by this transition:

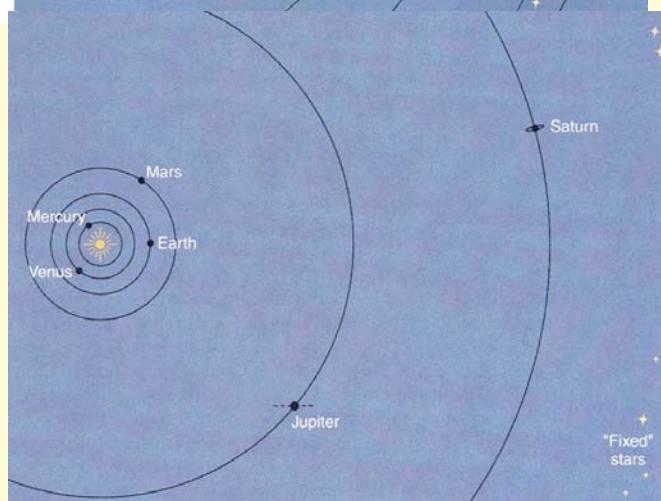
*Geocentric model* (Ptolemy, epicycles, planets and Sun orbit the Earth)

→ *Heliocentric model* (Copernicus, planets orbit the Sun)

The solar system as conceived by Ptolemaic astronomers between about 100 and 1500. Ptolemaic astronomers made rough predictions of planetary motions, using a theory in which the Sun and other planets moved in circular orbits around a stationary, central Earth. Superimposed on the larger orbits were smaller circular motions called epicycles, introduced to try to make the theory more accurate.



The solar system as it might have been conceived around 1700, at the end of the Copernican revolution. The diagram shows the orbits of the 10 known planets to true scale. The view is correct except that the outermost planets (Uranus, Neptune, and Pluto) and the asteroids had not yet been discovered. Compare with Figure 3-2 to see the change from the Ptolemaic view.



# Kepler's Laws

**Empirical**, based on observations; NOT a theory (in the sense of Newton's laws). So they are "laws" in the sense of *formulas that express some regularity or correlation*, but they don't explain the observed phenomena in terms of something more basic (e.g. laws of motion, gravity--that waited for Newton)

## Kepler's 1st law:

- 1. Orbits of planets are ellipses (not circles), with Sun at one focus.

Must get used to terms *period* (time for one orbit), *semimajor axis* ("size" of orbit), eccentricity (how "elongated" the orbit is), *perihelion* (position of smallest distance to Sun), *aphelion* (position of greatest distance to Sun)

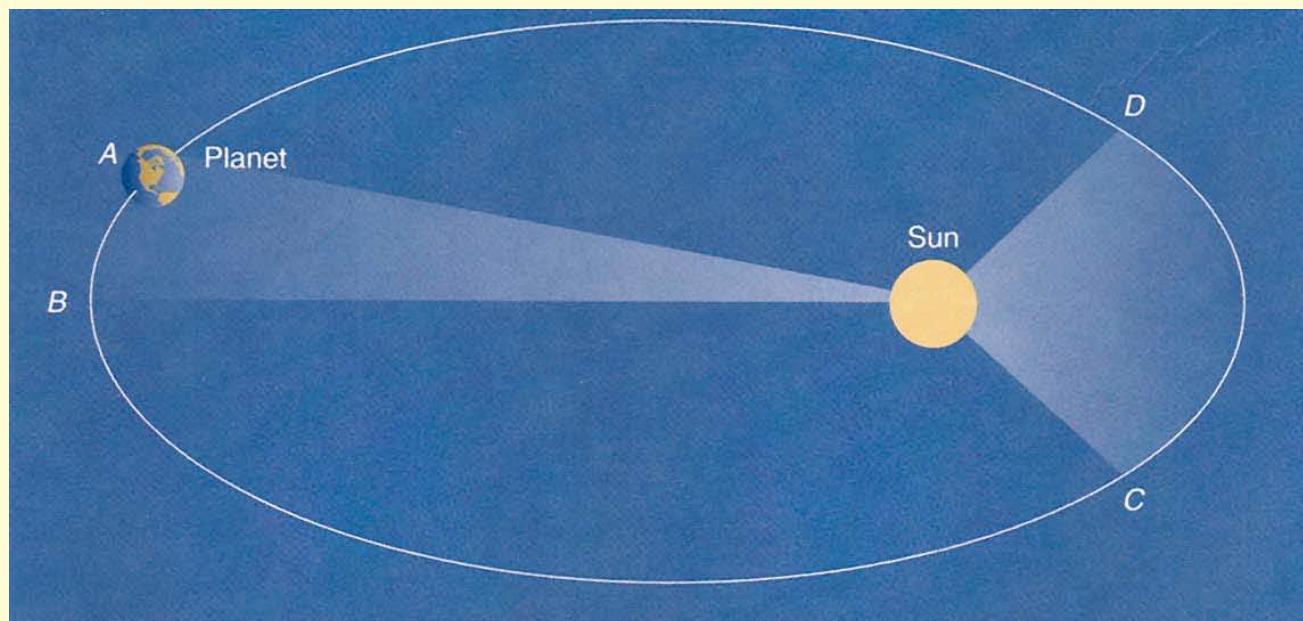
Examples: comets, planets: *Why do you think these have such different eccentricities?*

(*Don't expect to be able to answer this, just find whether you understand the question.*)

- *Escaping from the assumption of perfect circles for orbits was a major leap, that even Copernicus was unwilling to take.*

Kepler's 2nd law:  
→ 2. Equal areas swept out in equal times  
i.e. planet moves faster when closer to the sun.

Good example: comets (very eccentric orbits, explained in class).



Kepler's second law of planetary motion. The orbit sweeps out an ellipse where an imaginary line connecting the planet to the Sun sweeps out equal areas in equal time intervals. The time taken to move from A to B equals the time taken to move from C to D. In other words, planets travel faster when they are close to the Sun and more slowly when they are far from the Sun. The true planet orbits are much closer to circles, and the speed only changes by a small percentage along the orbit.

## Kepler's 3rd law

→ Square of the period "P" is proportional to the cube of the semimajor axis "a"

$$P^2 = a^3$$

IF P is expressed in Earth years and "a" is in units of A.U. (astronomical unit; average distance from Earth to Sun). A graph of the periods vs. the distances from the sun (a) is shown below. (Absolute size of A.U. unit determined from radar observations of Venus and Mercury, and other methods--see textbook.)

→ Kepler's 3rd law, as modified by Newton (coming up), will be a cornerstone of much of this course, because it allows us to estimate masses of astronomical objects (e.g. masses of stars, galaxies, the existence of black holes and the mysterious "dark matter").

### **Example of use of Kepler's 3rd law:**

The planet Saturn has a period of about 30 years; how far is it from the Sun?

Kepler's third law of planetary motion. The period of a planet's orbit increases with increasing distance from the Sun. Planets discovered after the invention of the telescope obey this law, too. Notice that according to Kepler's law, planets can have properties that place them anywhere on this curve. The planets of the solar system have a particular pattern in their spacing from the Sun.

