## Problem-1)

- a) For this algorithm, I would use merge sort or heap sort algorithms. Because if I would use a quick sort algorithm, the worst case time could be  $\Theta(n^2)$ . Since, I use merge sort (or heap sort), the worst case time is  $\Theta(nlogn)$  for sorting these n elements. When we perform a merge sort algorithm, we will have the sorted elements at the end. We can put these k smallest elements in an array. Putting k smallest numbers in the array will take  $\Theta(k)$  time. So at the end, our algorithm takes  $\Theta(k+nlogn)$  time. Since  $k \le n$ , the best asymptotic worst-case running time is  $\Theta(nlogn)$ .
- b) I use the SELECT algorithm to find the k'th largest number. This takes  $\Theta(n)$  time. Partition around that number to get the k smallest numbers, takes also  $\Theta(n)$  time. Now, I have to use a comparison-based sorting algorithm to sort these k smallest numbers. I can use merge sort or heap sort for this purpose. Since we will sort k smallest numbers (which means that I have k elements), with merge sort (or heap sort) this takes  $\Theta(klogk)$  time. At the end our algorithm takes  $\Theta(n+klogk)$  time. Since  $k \le n$ , the best asymptotic worst-case running time is  $\Theta(nlogn)$ .

I would use the second algorithm (part b) because when k is a small value, this algorithm will take  $\Theta(n)$  time (nearly). For the first algorithm, for smaller k values it will take  $\Theta(nlogn)$  time. So, the second algorithm is always asymptotically better than the first algorithm.

## Problem-2)

a) For the radix sort algorithm for integers, we sort digit by digit. For the first iteration, we need to look for the least-significant digit. For the last iteration, we need to look for the most significant digit. For example if we have [3,10, 22, 100], for the first iteration, we will have [10, 100, 22, 3]. For the second iteration, we will have [100, 3, 10, 22]. For the last iteration, we will have [3, 10, 22, 100].

If we want to implement this algorithm for strings, we will do the same logic with a little difference. We can not characters by using their applications. But what if their length will

If we want to implement this algorithm for strings, we will do the same logic with a little difference. We can sort characters by using their ascii values. But what if their length will be different? Since for integers, we think that for the previous example above [003, 010, 022, 100] to sort the digits. For strings, if their lengths are different, then we can use '\*' character as an empty character. For example if we have ["CS", "COURSE"] we can think as ["CS\*\*", "ANTH"]. So, at the last iteration, we have ["ANTH", "CS\*\*"] since 'A' becomes first.

b) ["AYSU", "BERK", "ESRA", "ILAYDA", "SELIN"] think as:

["AYSU\*\*", "BERK\*\*", "ESRA\*\*", "ILAYDA", "SELIN\*"]

For the first iteration we have:
["AYSU\*\*", "BERK\*\*", "ESRA\*\*", "SELIN\*", "ILAYDA"]

For the second iteration we have:
["AYSU\*\*", "BERK\*\*", "ESRA\*\*", "ILAYDA", "SELIN\*"]

For the third iteration we have:
["ESRA\*\*", "SELIN\*", "BERK\*\*", "AYSU\*\*", "ILAYDA"]

For the fourth iteration we have:
["ILAYDA", "SELIN\*", "ESRA\*\*", "BERK\*\*", "AYSU\*\*"]

For the fifth iteration we have:
["SELIN\*", "BERK\*\*", "ILAYDA", "ESRA\*\*", "AYSU\*\*"]

For the last iteration we have:

["AYSU\*\*", "BERK\*\*", "ESRA\*\*", "ILAYDA", "SELIN\*"]

c) Radix sort takes O(d \* (n + b)) where n is the number of items to sort, d is the number of digits in each item, and b is the number of values each digit can have. Since, we only modified b (for integers, it was 10; for strings, it is 26), complexity will be greater than before but still it takes O(d \* n) time.