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2.8 $p = 1373$ $g = 2$

a. $a = 947$

$$g^a \equiv 177 \pmod{1373}$$

b. $b = 716$ $m = 583$ $k = 877$ $C_1 = g^k$ $C_2 = m \cdot g^k$

$$(C_1, C_2) = (719, \cancel{877} 623)$$

c. $a = 299$ $A = 34$ $C_1 = g^k$, $C_2 = mA^k$

$$(C_1, C_2) = (661, 1325)$$

$$x = C_1^a \rightarrow x = 392$$

$$\bar{x}^{-1} = x^{p-1-1} = x^{p-2} \rightarrow \bar{x}^{-1} = 683$$

$$\bar{x}^{-1} C_2 = m \rightarrow m = \cancel{13} 168$$

\rightarrow

d. $2^b = 893 \pmod{1373}$ $(C_1, C_2) = (693, 793)$

$$\rightarrow b = 219$$

$$x = C_1^b \rightarrow x = 431$$

$$\bar{x}^{-1} = x^{p-2} \rightarrow \bar{x}^{-1} = 532$$

$$\bar{x}^{-1} C_2 = m \rightarrow m = 365$$