

Q. A farmer applies three types of fertilizers on four separate plots. The figures on yield per acre are tabulated below.

Fertilizer	Plots			
	A	B	C	D
Nitrogen	6	4	8	6
Potash	7	6	6	9
Phosphate	8	5	10	9

Test whether there is any significant difference among mean yields of different plots and among different fertilizers. (Answer H_0 is rejected/not rejected).

Ans.

$$H_0: \mu_1 = \mu_2 = \mu_3$$

H_1 : The Means are not equal.

Plots/ Fertilizers	A	B	C	D
NITROGEN	6	4	8	6
POTASSIUM	7	6	6	9
PHOSPHATES	8	5	10	9
	(X1) $\bar{x}=7$	(X2) $\bar{x}=5$	(X3) $\bar{x}=8$	(X4) $\bar{x}=8$

$$1. \text{ Total Mean, } \bar{x} = (7+5+8+8)/4$$

$$\therefore (X)\bar{x} = 7.00$$

$$2. \text{ No. of Observations in each group: } n_1=n_2=n_3=n_4=3$$

$$3. \text{ No. of Groups: } K=4$$

$$A. \text{ Sum of Squares Between groups [SSB]} = \sum(X_i - X)^2 * n_i$$

$$\therefore SSB=18$$

$$4. \text{ Degree of Freedom: } df_1=K-1$$

$$\therefore df_1=4-1$$

$$\therefore df_1=3$$

$$B. \text{ Sum of Squares of Errors [SSE]} = \sum_k \sum (X_i - \bar{X})^2$$

Where \bar{X} is Each Data point in the ith Group.

A	$(X-7)^2$	B	$(X-5)^2$	C	$(X-8)^2$	D	$(X-7)^2$
6	1	4	1	8	0	6	4
7	0	6	1	6	4	9	1
8	1	5	0	10	4	9	1
$\bar{x}=7$	2	$\bar{x}=5$	2	$\bar{x}=8$	8	$\bar{x}=8$	6

$$\therefore SSE = 2+2+8+6 = 18$$

Total count of Obs, $N = 12$

$$df_2 = N - K$$

$$\therefore df_2 = 8$$

C. Mean Squares Between groups:

$$\mathbf{MSB = SSB / (K-1)}, \text{ where } (K-1) \text{ is } df_1$$

$$MSB = 18/3$$

$$\therefore \mathbf{MSB = 6}$$

Mean Squares of Errors:

$$\mathbf{MSE = SSE / (N-K)}, \text{ where } (N-K) \text{ is } df_2$$

$$\therefore \mathbf{MSB = 18/8}$$

$$\therefore \mathbf{MSB = 2.25}$$

D. ANOVA Test Statistics, $f(\text{Calculated})$

$$f(\text{Calculated}) = MSB / MSE$$

$$f(\text{Calculated}) = 6/2.25$$

$$f(\text{Calculated}) = 2.66$$

E. Critical Value @ $\alpha = 0.05$

$$f(\text{actual}) = f(df_1, df_2) @ \alpha = 0.05$$

$$\therefore f(\text{actual}) = 4.07$$

$$\therefore f(\text{Calculated}) < f(\text{actual})$$

\therefore We are Unable to reject the Null Hypothesis.

Hence, it is concluded that there is not enough evidence to prove that plots are significantly different in fertility.