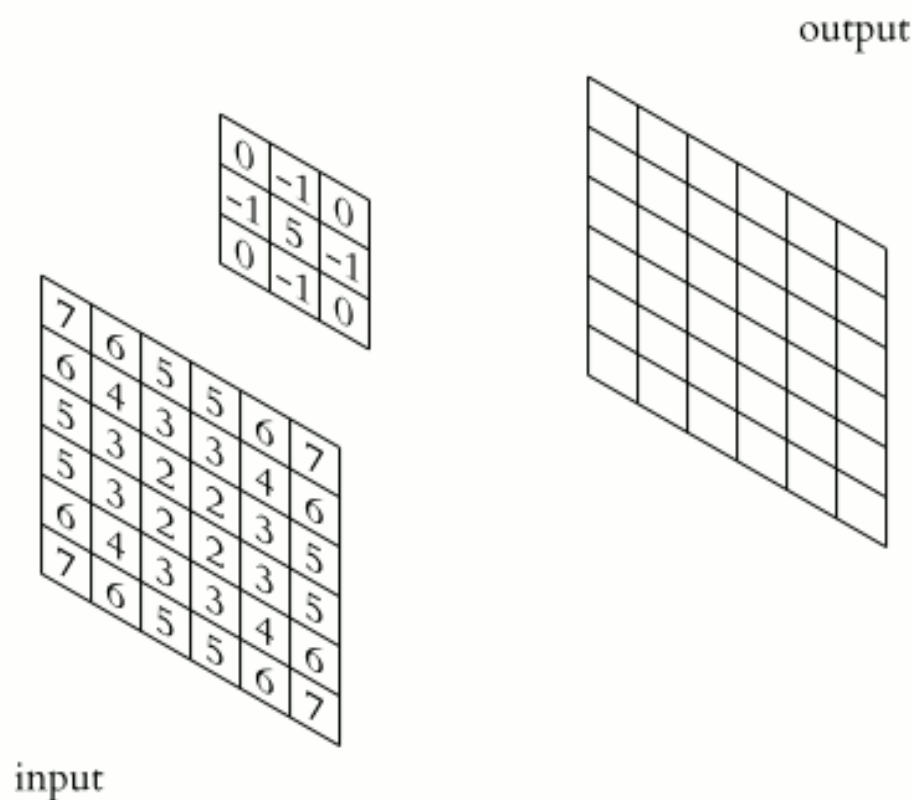


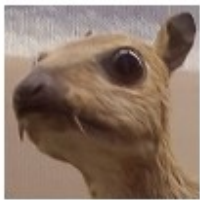




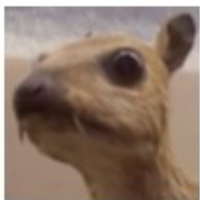
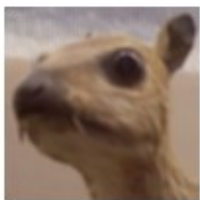
Image Filtering, Convolution

- Image filtered by convolving with a filter kernel
- Convolution denoted by “*”

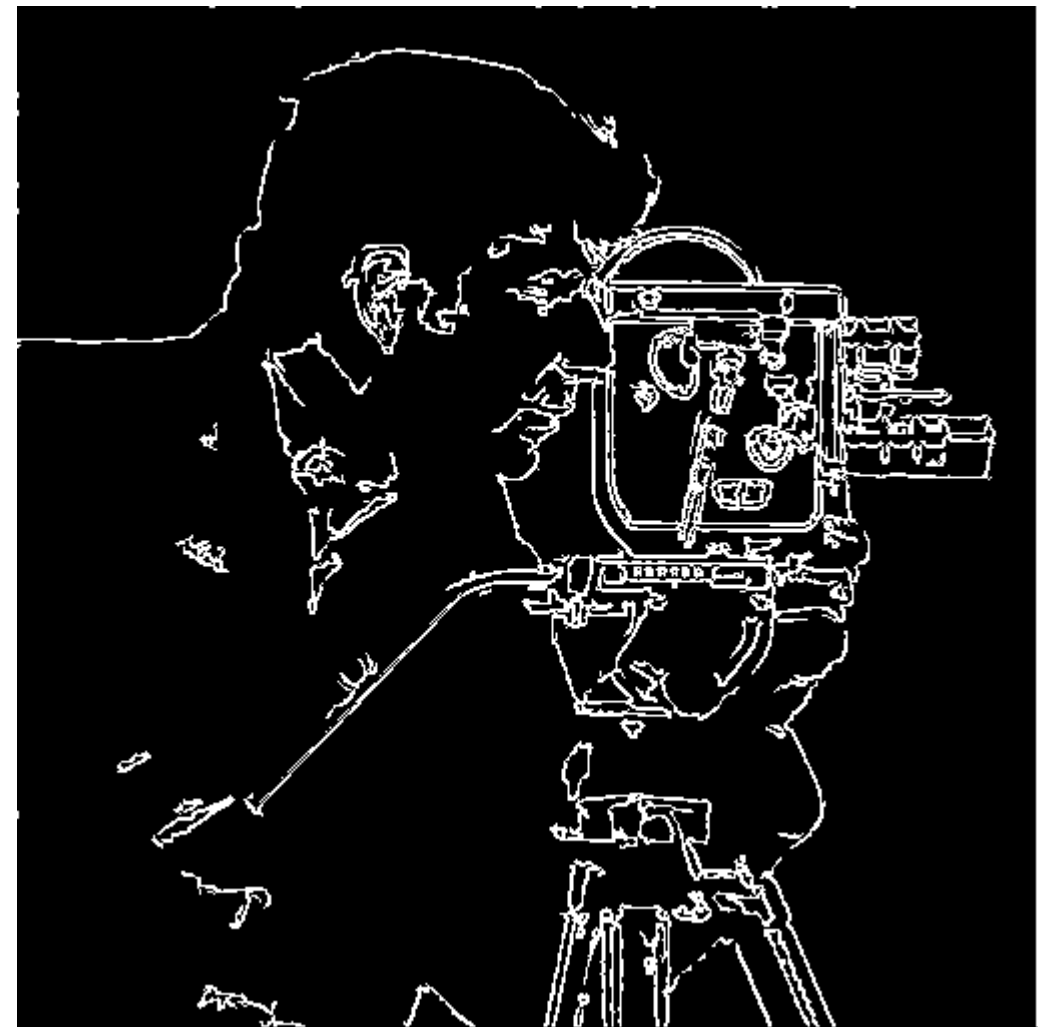
$$I_{output} = k * I_{input}$$



[http://en.wikipedia.org/wiki/Kernel_\(image_processing\)](http://en.wikipedia.org/wiki/Kernel_(image_processing))

Original	$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	
Edge-Detect	$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 0 & 0 \\ -1 & 0 & 1 \end{bmatrix}$	
	$\begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$	
	$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$	
Sharpen	$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$	
Blur*	$\begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$	
	$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$	

Exercise 2 - Edge Detection

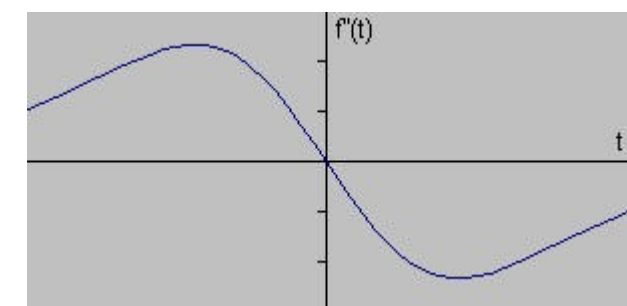
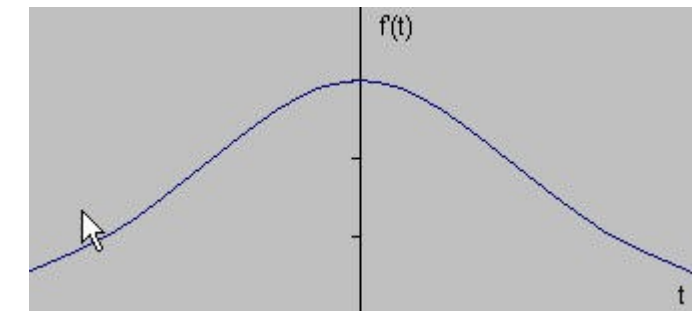
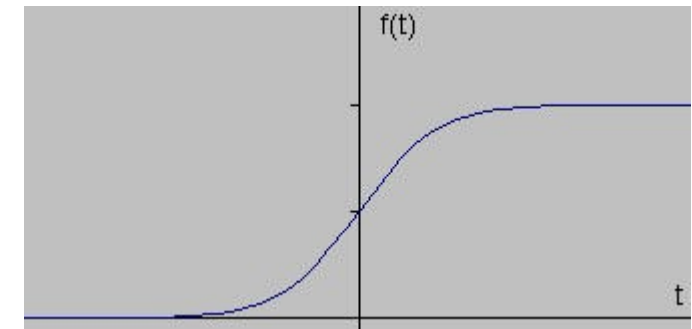


http://vision.cs.arizona.edu/nvs/research/image_analysis/edge.html

Edges

Edges in images are areas with strong intensity contrasts

- Change is measured by derivative in 1D
- Biggest change, derivative has maximum magnitude
- Or 2nd derivative is zero



<http://www.pages.drexel.edu/~weg22/edge.html>

Gradient Method

Gradient Vector $\mathbf{g}(x, y) = \begin{bmatrix} g_x(x, y) \\ g_y(x, y) \end{bmatrix} = \begin{bmatrix} (k_x * f)(x, y) \\ (k_y * f)(x, y) \end{bmatrix}$

Gradient Magnitude $|\mathbf{g}| = (g_x^2 + g_y^2)^{1/2}$

Direction $\theta = \tan^{-1} \left(\frac{g_y}{g_x} \right)$

Sobel kernel

Approximate of the 2D derivative of an image

$$k_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} \quad k_y = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

Prewitt kernel

Approximate of the 2D derivative of an image

$$k_x = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$$

$$k_y = \begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

Canny Edge Detection

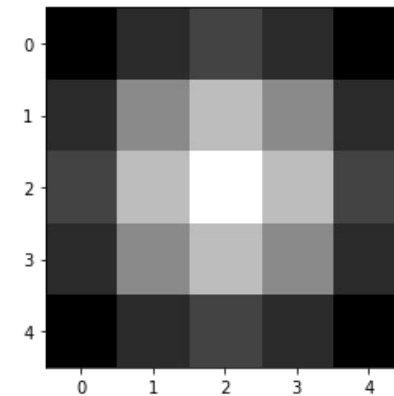
Combine noise reduction and edge enhancement.

1. Apply derivative of Gaussian filter
2. Non-maximum suppression
 - Thin multi-pixel wide “ridges” down to single pixel width
3. Hysteresis
 - Accept all edges over low threshold that are connected to edge over high threshold

Derivative of Gaussian kernel

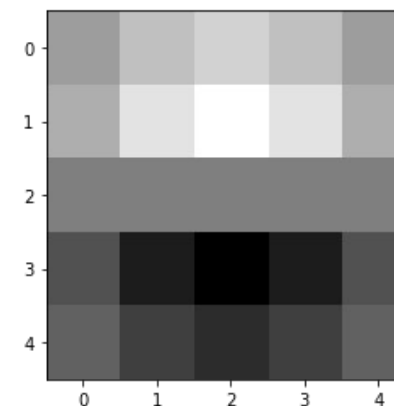
- Need smoothing to reduce noise prior to taking derivative

0.0121	0.0261	0.0337	0.0261	0.0121
0.0261	0.0561	0.0724	0.0561	0.0261
0.0337	0.0724	0.0935	0.0724	0.0337
0.0261	0.0561	0.0724	0.0561	0.0261
0.0121	0.0261	0.0337	0.0261	0.0121



- We can use derivative of Gaussian filters
 - because differentiation is convolution, and convolution is associative:

$$D * (G * I) = (D * G) * I$$



Non-maximum suppression

- The edge direction angle is rounded to one of four angles representing vertical, horizontal and the two diagonals.
- Select the single maximum point across the width of an edge.
- Maximum: The gradient magnitudes of the two neighbors in edge normal direction are smaller.



courtesy of G. Loy

Hysteresis

- Idea: Maintain two thresholds T_{high} and T_{low}
 - Use T_{high} to find strong edges to start edge chain
 - Use T_{low} to find weak edges which continue edge chain
- Typical ratio of thresholds is roughly

$$T_{\text{high}} / T_{\text{low}} = 2$$

Hysteresis

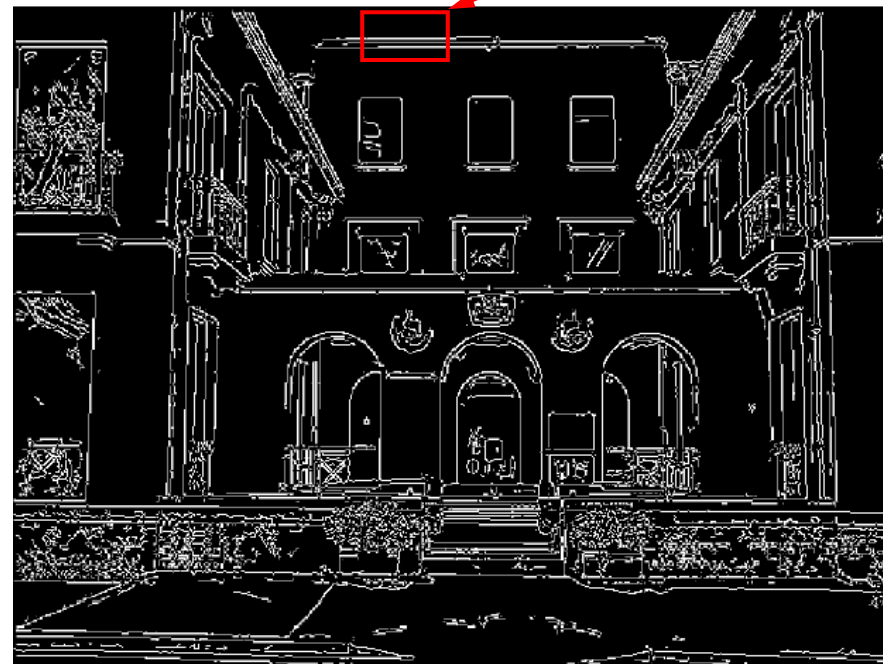
Strong
edges
only
 $> T_{\text{high}}$



Weak
edges
 $> T_{\text{low}}$



gap is gone



Strong +
connected
weak edges

courtesy of G. Loy

Test Image

