High Performance Computing with Python

Implementing distance matrices with NumPy, CuPy, Numba and dask

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NumPy is a Python library that adds support for large multi-dimensional arrays and matrices, along with a large collection of high-level mathematical functions to operate on these arrays.



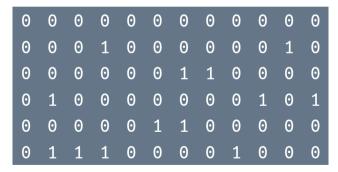
- numpy.ndarray: a powerful N-dimensional array object
- Sophisticated functions often written in C
- Linear algebra, Fourier transform, and random number capabilities
- Tools for easy binding to Fortran code (F2PY)
- Compatibility with C
- Many libraries implement the NumPy API, such as Dask and CuPy for graph and GPU computing respectively [NEP 35]



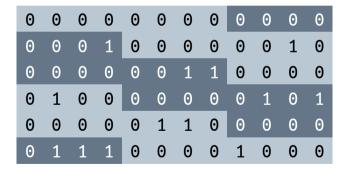


The **SciPy** library provides many user-friendly and efficient numerical routines for operations such as numerical integration, interpolation, optimization, linear algebra and statistics. SciPy builds on the numpy.ndarray and expands the set of mathematical functions included in NumPy









```
{'shape': (3, 3), 'strides': (3, 1),
 'dtypes': int8, 'ndim': 2, ...}
                                        0
0
    0
        0
              0
        0
                    0
        0
                            0
                0
                    0
        0
                0
                            0
                                         0
                0
                        0
                            0
                                         0
```

```
      {'shape': (3, 3), 'strides': (3, 1), 'dtypes': int8, 'ndim': 2, ...}

      0 0 0 0 0 0 0 0 0 0 0 0 0 0

      0 0 0 1 0 0 0 0 0 0 0 1 0

      0 0 0 0 1 0 0 0 0 0 0 0 1 0

      0 0 0 0 0 0 0 1 1 0 0 0 0
```

- The memory block is called **data buffer**.
- The metadata is used to interpret the data buffer within the python context.
- The data buffer is stored in C order (row major) by default.
- All items in the array have the same data type.

```
# # 0 1 2 3 4 5 6 7
8 9 10 11 12 13 14 15 # #
```

Data buffer

NumPy representation

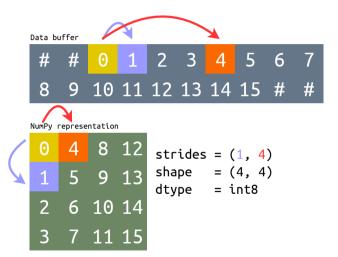
Data buffer

NumPy representation

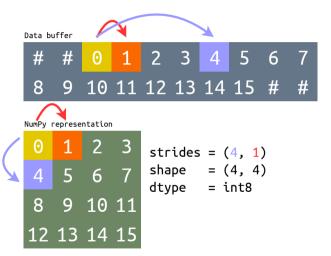
```
0 4 8 12 strides = (1, 4)
1 5 9 13 shape = (4, 4)
dtype = int8
3 7 11 15
```

```
Data buffer
     #
       10 11 12 13 14 15 #
NumPy representation
                strides = (1, 4)
                shape = (4, 4)
                dtype = int8
     6 10 14
       11 15
```

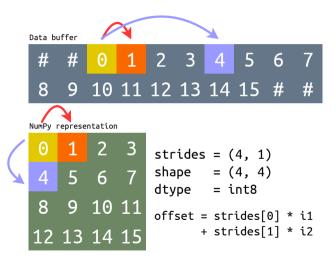














[homework] numpy.ndarray internals

• Let's open the notebook numpy/01-numpy-array-internals.ipynb and go over the questions.

There are two parts:

- Understanding strides: a few arrays are given and you are asked to determine the corresponding strides (without looking at the strides attribute)
- Metadata modification vs copying the data buffer: some operations are given and we ask you
 to explain the results or differences in execution time. (Hint: Identify if new data is created or if
 the operations can be done with only a change of metadata)



Vectorization

• Use operations over the whole array instead of over single elements.

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```
y = np.exp(x) # x = np.array([...])

z = x @ y # equivalent to np.matmul(x, y)
```

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y = np.exp(x) # x = np.array([...])

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```

• Adapt your solutions to use the two points above.

Broadcasting

$$\begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} + \begin{bmatrix} y_0 & y_1 & y_2 & \cdots & y_n \end{bmatrix}$$

$$(n, 1) \qquad (1, n)$$

Broadcasting

$$\begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} + \begin{bmatrix} y_0 & y_1 & y_2 & \cdots & y_n \end{bmatrix} = \begin{bmatrix} x_0 + y_0 & x_0 + y_1 & \cdots & x_0 + y_n \\ x_1 + y_0 & x_1 + y_1 & \cdots & x_1 + y_n \\ x_2 + y_0 & x_2 + y_1 & \cdots & x_2 + y_n \\ \vdots & \vdots & \ddots & \vdots \\ x_n + y_0 & x_n + y_1 & \cdots & x_n + y_n \end{bmatrix}$$

$$(n, 1) \qquad (1, n) \qquad (n, n)$$

[lab] Broadcasting

• Let's open the notebook numpy/02-broadcasting.ipynb and go over the cells and the questions. The goal of this notebook is to understand the broadcasting operations presented there.



$$d_{\mathbf{e}} \begin{pmatrix} \begin{bmatrix} x_{11} & x_{12} & x_{13} \\ x_{21} & x_{22} & x_{23} \\ \vdots & \vdots & \vdots \\ x_{n1} & x_{n2} & x_{n3} \end{bmatrix}, \begin{bmatrix} y_{11} & y_{12} & y_{13} \\ y_{21} & y_{22} & y_{23} \\ \vdots & \vdots & \vdots \\ y_{n1} & y_{n2} & y_{n3} \end{bmatrix} \end{pmatrix} = \begin{bmatrix} \sum (x_{1i} - y_{1i})^2 & \sum (x_{1i} - y_{2i})^2 & \dots & \sum (x_{1i} - y_{ni})^2 \\ \sum (x_{2i} - y_{1i})^2 & \sum (x_{2i} - y_{2i})^2 & \dots & \sum (x_{2i} - y_{ni})^2 \\ \vdots & \vdots & \vdots & \vdots \\ \sum (x_{ni} - y_{1i})^2 & \sum (x_{ni} - y_{2i})^2 & \dots & \sum (x_{ni} - y_{ni})^2 \end{bmatrix}$$

$$d_{\mathsf{e}} \left(\begin{bmatrix} x_{11} & x_{12} & x_{13} \\ x_{21} & x_{22} & x_{23} \\ \dots & \dots & \dots \\ x_{n1} & x_{n2} & x_{n3} \end{bmatrix}, \begin{bmatrix} y_{11} & y_{12} & y_{13} \\ y_{21} & y_{22} & y_{23} \\ \dots & \dots & \dots \\ y_{n1} & y_{n2} & y_{n3} \end{bmatrix} \right) = \begin{bmatrix} \sum (x_{1i} - y_{1i})^2 & \sum (x_{1i} - y_{2i})^2 & \dots & \sum (x_{1i} - y_{ni})^2 \\ \sum (x_{2i} - y_{1i})^2 & \sum (x_{2i} - y_{2i})^2 & \dots & \sum (x_{2i} - y_{ni})^2 \\ \dots & \dots & \dots & \dots \\ \sum (x_{ni} - y_{1i})^2 & \sum (x_{ni} - y_{2i})^2 & \dots & \sum (x_{ni} - y_{ni})^2 \end{bmatrix}$$

$$d_{\mathsf{e}} \left(\begin{bmatrix} x_{11} & x_{12} & x_{13} \\ x_{21} & x_{22} & x_{23} \\ \dots & \dots & \dots \\ x_{n1} & x_{n2} & x_{n3} \end{bmatrix}, \begin{bmatrix} y_{11} & y_{12} & y_{13} \\ y_{21} & y_{22} & y_{23} \\ \dots & \dots & \dots \\ y_{n1} & y_{n2} & y_{n3} \end{bmatrix} \right) = \begin{bmatrix} \sum (x_{1i} - y_{1i})^2 & \sum (x_{1i} - y_{2i})^2 & \dots & \sum (x_{1i} - y_{ni})^2 \\ \sum (x_{2i} - y_{1i})^2 & \sum (x_{2i} - y_{2i})^2 & \dots & \sum (x_{2i} - y_{ni})^2 \\ \dots & \dots & \dots & \dots \\ \sum (x_{ni} - y_{1i})^2 & \sum (x_{ni} - y_{2i})^2 & \dots & \sum (x_{ni} - y_{ni})^2 \end{bmatrix}$$

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$$d_{\mathsf{e}} \begin{pmatrix} \begin{bmatrix} x_{11} & x_{12} & x_{13} \\ \frac{x_{21}}{2} & \frac{x_{22}}{2} & \frac{x_{23}}{2} \\ \dots & \dots & \dots \\ x_{n1} & x_{n2} & x_{n3} \end{bmatrix}, \begin{bmatrix} y_{11} & y_{12} & y_{13} \\ y_{21} & y_{22} & y_{23} \\ \dots & \dots & \dots \\ y_{n1} & y_{n2} & y_{n3} \end{bmatrix} \end{pmatrix} = \begin{bmatrix} \sum (x_{1i} - y_{1i})^2 & \sum (x_{1i} - y_{2i})^2 & \dots & \sum (x_{1i} - y_{ni})^2 \\ \sum (x_{2i} - y_{1i})^2 & \sum (x_{2i} - y_{2i})^2 & \dots & \sum (x_{2i} - y_{ni})^2 \\ \dots & \dots & \dots & \dots \\ \sum (x_{ni} - y_{1i})^2 & \sum (x_{ni} - y_{2i})^2 & \dots & \sum (x_{ni} - y_{ni})^2 \end{bmatrix}$$

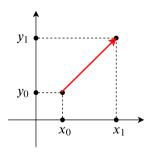
$$d_{\mathsf{e}} \left(\begin{bmatrix} x_{11} & x_{12} & x_{13} \\ x_{21} & x_{22} & x_{23} \\ \dots & \dots & \dots \\ x_{n1} & x_{n2} & x_{n3} \end{bmatrix}, \begin{bmatrix} y_{11} & y_{12} & y_{13} \\ y_{21} & y_{22} & y_{23} \\ \dots & \dots & \dots \\ y_{n1} & y_{n2} & y_{n3} \end{bmatrix} \right) = \begin{bmatrix} \sum (x_{1i} - y_{1i})^2 & \sum (x_{1i} - y_{2i})^2 & \dots & \sum (x_{1i} - y_{ni})^2 \\ \sum (x_{2i} - y_{1i})^2 & \sum (x_{2i} - y_{2i})^2 & \dots & \sum (x_{2i} - y_{ni})^2 \\ \dots & \dots & \dots & \dots \\ \sum (x_{ni} - y_{1i})^2 & \sum (x_{ni} - y_{2i})^2 & \dots & \sum (x_{ni} - y_{ni})^2 \end{bmatrix}$$

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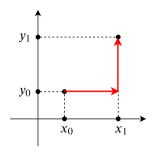
$$d_{\mathbf{e}} \begin{pmatrix} \begin{bmatrix} x_{11} & x_{12} & x_{13} \\ x_{21} & x_{22} & x_{23} \\ \vdots & \vdots & \vdots \\ x_{n1} & x_{n2} & x_{n3} \end{bmatrix}, \begin{bmatrix} y_{11} & y_{12} & y_{13} \\ y_{21} & y_{22} & y_{23} \\ \vdots & \vdots & \vdots \\ y_{n1} & y_{n2} & y_{n3} \end{bmatrix} \end{pmatrix} = \begin{bmatrix} \sum (x_{1i} - y_{1i})^2 & \sum (x_{1i} - y_{2i})^2 & \dots & \sum (x_{1i} - y_{ni})^2 \\ \sum (x_{2i} - y_{1i})^2 & \sum (x_{2i} - y_{2i})^2 & \dots & \sum (x_{2i} - y_{ni})^2 \\ \vdots & \vdots & \vdots & \vdots \\ \sum (x_{ni} - y_{1i})^2 & \sum (x_{ni} - y_{2i})^2 & \dots & \sum (x_{ni} - y_{ni})^2 \end{bmatrix}$$



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$$\begin{bmatrix}
\sum (x_{1i} - y_{1i})^2 & \sum (x_{1i} - y_{2i})^2 & \dots & \sum (x_{1i} - y_{ni})^2 \\
\sum (x_{2i} - y_{1i})^2 & \sum (x_{2i} - y_{2i})^2 & \dots & \sum (x_{2i} - y_{ni})^2 \\
\dots & \dots & \dots & \dots \\
\sum (x_{ni} - y_{1i})^2 & \sum (x_{ni} - y_{2i})^2 & \dots & \sum (x_{ni} - y_{ni})^2
\end{bmatrix}$$

Cityblock distance matrix



$$d_{\mathsf{cb}} \begin{pmatrix} \begin{bmatrix} x_{11} & x_{12} & x_{13} \\ x_{21} & x_{22} & x_{23} \\ \dots & \dots & \dots \\ x_{n1} & x_{n2} & x_{n3} \end{bmatrix}, \begin{bmatrix} y_{11} & y_{12} & y_{13} \\ y_{21} & y_{22} & y_{23} \\ \dots & \dots & \dots \\ y_{n1} & y_{n2} & y_{n3} \end{bmatrix} \end{pmatrix} = \\ \begin{bmatrix} \sum |x_{1i} - y_{1i}| & \sum |x_{1i} - y_{2i}| & \dots & \sum |x_{1i} - y_{ni}| \\ \sum |x_{2i} - y_{1i}| & \sum |x_{2i} - y_{2i}| & \dots & \sum |x_{2i} - y_{ni}| \\ \dots & \dots & \dots \\ \sum |x_{ni} - y_{1i}| & \sum |x_{ni} - y_{2i}| & \dots & \sum |x_{ni} - y_{ni}| \end{bmatrix}$$

- Use operations over the whole array instead of over single elements.
- ✓ When working with arrays, use ufuncs and general NumPy's functions.
- **X** Adapt your solutions to use the two points above.



```
def euclidean_distance_matrix(x, y):
    diff = x[:, np.newaxis, :] - y[np.newaxis, :, :]
    return (diff * diff).sum(axis=2)
```

$$\sum_{i} (x_{ik} - y_{jk})^2 = (\vec{x}_i - \vec{y}_j) \cdot (\vec{x}_i - \vec{y}_j) = \vec{x}_i \cdot \vec{x}_i + \vec{y}_j \cdot \vec{y}_j - 2\vec{x}_i \cdot \vec{y}_j$$

$$\sum_{k} (x_{ik} - y_{jk})^2 = (\vec{x}_i - \vec{y}_j) \cdot (\vec{x}_i - \vec{y}_j) = \vec{x}_i \cdot \vec{x}_i + \vec{y}_j \cdot \vec{y}_j - 2\vec{x}_i \cdot \vec{y}_j$$

 $\vec{x}_i \cdot \vec{y}_j
ightarrow \mathbf{x}$ @ y.T

: Matrix product of $\{\vec{x}\}$ and $\{\vec{y}\}$

$$\sum_{i} (x_{ik} - y_{jk})^2 = (\vec{x}_i - \vec{y}_j) \cdot (\vec{x}_i - \vec{y}_j) = \vec{x}_i \cdot \vec{x}_i + \vec{y}_j \cdot \vec{y}_j - 2\vec{x}_i \cdot \vec{y}_j$$

$$ec{x}_i \cdot ec{y}_j
ightarrow {\sf x}$$
 (e.g., Y) $ec{x}_i \cdot ec{y}_j
ightarrow {\sf x}$ (e.g., Y) $ec{x}_i \cdot ec{y}_j
ightarrow {\sf x}$ (e.g., Y) $ec{x}_i \cdot ec{y}_j
ightarrow {\sf x}$

$$ec{x}_i \cdot ec{x}_i o$$
 (x * x).sum(axis=1) : A vector of elements $\sum_j x_{ij} x_{ij} \equiv \sum_j x_{ij}^2$

$$ec{y}_j \cdot ec{y}_j o$$
 (y * y).sum(axis=1) : A vector of elements $\sum_j y_{ij} y_{ij} \equiv \sum_j y_{ij}^2$

$$\sum_{i} (x_{ik} - y_{jk})^2 = (\vec{x}_i - \vec{y}_j) \cdot (\vec{x}_i - \vec{y}_j) = \vec{x}_i \cdot \vec{x}_i + \vec{y}_j \cdot \vec{y}_j - 2\vec{x}_i \cdot \vec{y}_j$$

$$\vec{x}_i \cdot \vec{y}_j
ightarrow \mathsf{x}$$
 @ y.T

$$\vec{x}_i \cdot \vec{x}_i \rightarrow (x * x).sum(axis=1)[:, np.newaxis]$$

$$ec{y}_j \cdot ec{y}_j
ightarrow$$
 (y * y).sum(axis=1)[np.newaxis, :]

```
def euclidean_distance_matrix(x, y):
    x2 = (x * x).sum(axis=1)[:, np.newaxis]
    y2 = (y * y).sum(axis=1)[np.newaxis, :]
    xy = x @ y.T
    return np.abs(x2 + y2 - 2. * xy)
```

[lab] Euclidean distance matrix with NumPy

• Let's open the notebook numpy/03-euclidean-distance-matrix-numpy.ipynb and check step by step what the function euclidean trick does.



CuPy is an open-source array library accelerated with NVIDIA CUDA. It provides GPU accelerated computing with Python

- CuPy uses CUDA-related libraries including cuBLAS, cuDNN, cuRand, cuSolver, cuSPARSE, cuFFT and NCCL
- CuPy's interface is highly compatible with NumPy: in most cases it can be used as a drop-in replacement
- It compiles a kernel code optimized for the shapes and dtypes of given arguments, sends it to the GPU device, and executes the kernel

[lab] Euclidean distance matrix with CuPy

• Let's go together through the notebook cupy/euclidean-cupy.ipynb.



Cityblock distance matrix

$$\sum_{k} |x_{ik} - y_{jk}|$$

The trick we used for the Euclidean distance matrix doesn't work here!



Numba is an open source just-in-time (JIT) compiler that translates a subset of Python and NumPy code into fast machine code.



- Translation of python functions to machine code at runtime using the LLVM compiler library
- Designed to be used with NumPy arrays
- Options to parallelize code for CPUs and GPUs and automatic SIMD Vectorization
- Support for both NVIDIA's CUDA and AMD's ROCm driver allowing to write parallel GPU code from Python.



```
def reduce(x):
    x_sum = 0.0
    for i in range(x.shape[0]):
        x_sum += x[i]
    return x_sum
```



import numba

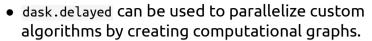
```
@numba.jit(nopython=True)
def reduce(x):
    x_sum = 0.0
    for i in range(x.shape[0]):
        x_sum += x[i]
    return x_sum
```

[lab] Cityblock distance matrix with Numba's just-in-time compilation

- Let's run the notebooks in the numba directory.
 - Notice that the function to be decorated with @numba.jit is not written in a pythonic style.
 Instead, with the loops it resembles more the C or Fortran styles.



dask is a flexible library for parallel computing in Python. It provides dynamic task scheduling optimized for computation as well as big data collections like parallel arrays, dataframes, and lists that extend common interfaces like NumPy and Pandas to larger-than-memory or distributed environments.



```
# regular code
                         # with dask
x = func1(\langle args \rangle)
                     x = dask.delayed(func1)(<args>)
y = func2(<args>)
                         y = dask.delayed(func2)(<args>)
z = func3(x, y)
                         z = dask.delayed(func3)(x, y)
                                 func1
                                         func2
                                    func3
                         z.compute(scheduler='threads')
```



• dask.delayed can be used to parallelize custom algorithms by creating computational graphs.



```
list delayed = [dask.delayed(func1)(<args>),
                dask.delayed(func2)(<arqs>).
                dask.delayed(func3)(<args>)]
```



- dask.array implements a subset of the NumPy array interface using blocked algorithms, cutting up the large array into chunks of small arrays.
- dask.bag parallelizes computations across a large collection of generic Python objects.
- dask.dataframe is a large parallel DataFrame composed of many smaller Pandas DataFrames which may live on disk for larger-than-memory computing on a single machine or a cluster.



[lab] Simple dask graphs

- Let's run the notebook dask/01-dask-intro.ipynb.
 - The goal is the go over the cells and questions and annotate the code with dask.delayed to make the execution lazy.
 - Before running predict how much time it will take.
 - The processor on Piz Daint's 'gpu' nodes have 24 threads. Try a number of tasks higher and lower than 24 a see what happens.

[lab] Cityblock distance matrix with SciPy and dask

- Let's run the notebook dask/02-exercise-cityblock-distance-matrix-scipy.dask.ipynb.
- scipy.spatial.distance.cdist can be used to compute the cityblock distance matrix. It is fast but doesn't use OpenMP threads. We can easily write a distributed Cityblock distance matrix function based on cdist with the help of dask.
 - Same as the previous exercise, go over the cells and annotate the code to execute it lazily. This time you have to go
 over the notebook and find what needs to be changed.
 - While timing cdist check with top that it runs on a single thread.
 - Why is it relevant for the implementation of such distributed function that cdist runs on a single thread?
 - Check that when we create the list of delayed functions the execution is deferred to when compute is called.
- Run all cells and compare the execution times of the different approaches.
- While running the %timett function calls, you may open a terminal and check with top that the new distributed function is runnig in multiple threads.

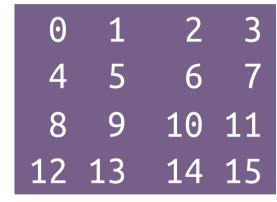


[lab] dask.delayed threads vs processes

- Let's run the notebook dask/06-dask-processes-vs-threads.ipynb.
 - Run the notebook and reply the questions.



dask array





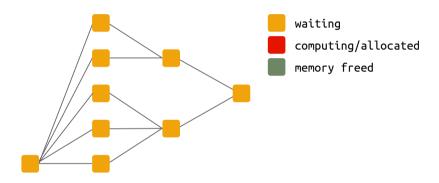
dask array

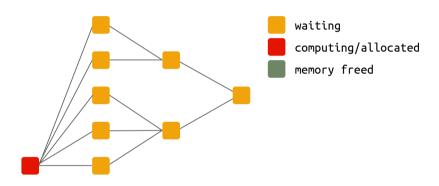
0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15



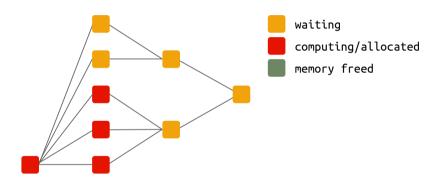
— Dask Arr NumPy Array	NumPy Array	NumPy Array	NumPy Array
NumPy	NumPy	NumPy	NumPy
Array	Array	Array	Array
NumPy	NumPy	NumPy	NumPy
Array	Array	Array	Array

- A dask array consists of many NumPy arrays arranged into a grid
- Those NumPy arrays may live on memory, disk or remote machines
- dask.array implements many of the numpy functions but in block-wise fashion and are executed through a graph.
- For equal sizes, operations on dask arrays are in general slower than the corresponding NumPy ones.

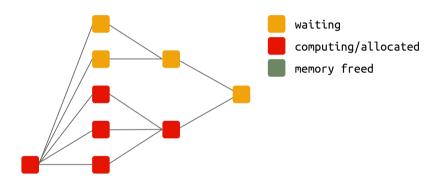




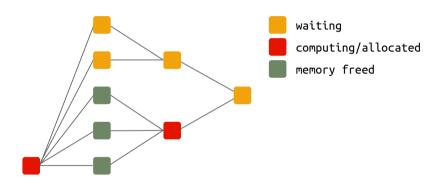




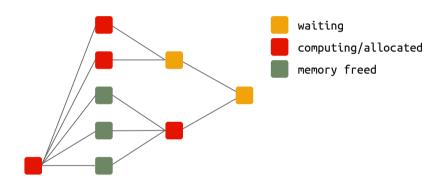




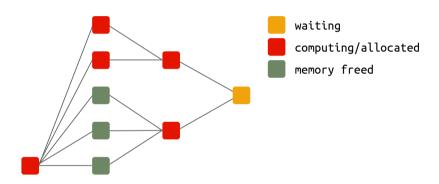


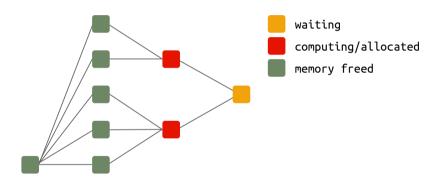


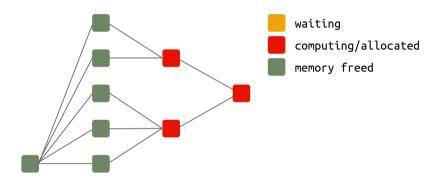


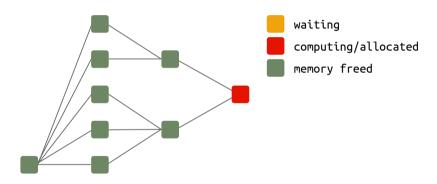


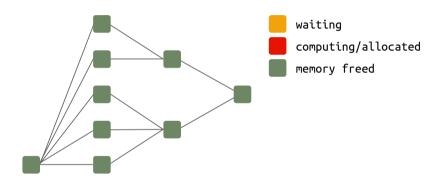














[lab] dask arrays

• Let's run together the notebooks dask/03-dask-array.ipynb and 04-dask-array-from-file.ipynb





Thank you for your attention!

