$quantum_algo_exercises$

1

1.a

QFT



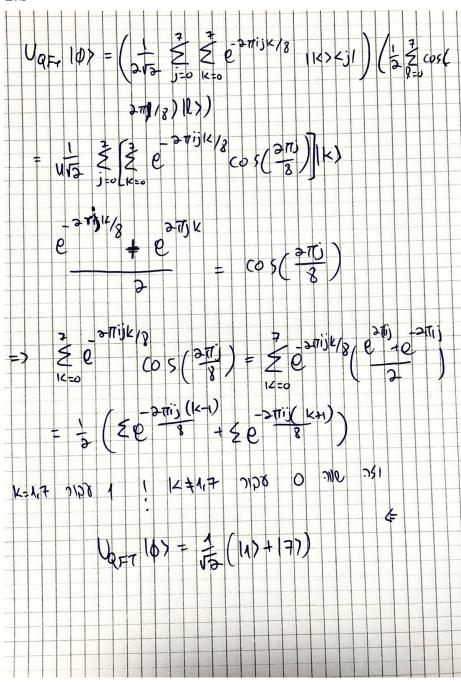
Figure 1: QFT

Inverse QFT



Figure 2: Inverse QFT

1.b

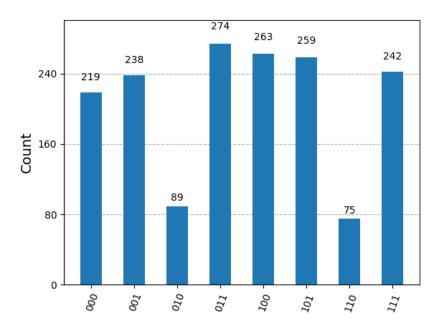


1.c

The result from b is encoded to the circuit with simple operations, then to reconstruct the original stage we used the inverse QFT and then $InverseQFT*QFT*\phi=\phi$. For more info see the src code: src/HW1.py

1.d

We can see that for j=2,6 the value is low, this is the excepted result from the origi-



nal stage.

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```
results = aer_sim.run(qobj).result()
answer = results.get_counts()
plot_histogram(answer)
```

/tmp/spykernel_5723/1318575361.py:6: DeprecationWarning: Using a qobj for run() is deprecated as of qiskit-aer 0.14 and will be removed no sooner than 3 months from that release date. Transpiled circuits should now be passed directly using 'backend.run(circuits.**run.options).
results = aer_sim.run(qobj).result()

(8): 2818 2818 2400 800 722 800 68 149 9 8 8 9 9 7 7 8 9 52 42

We are expecting the result $\theta=0.3333...$, and we see our most likely results are $\theta1\theta(bin)=2(dec)$ and $\theta11(bin)=3(dec)$. These two results would tell us that $\theta=0.25$ (off by 25%) and $\theta=0.375$ (off by 13%) respectively. The true value of θ lies between the values we can get from our counting bits, and this gives us uncertainty and imprecision.

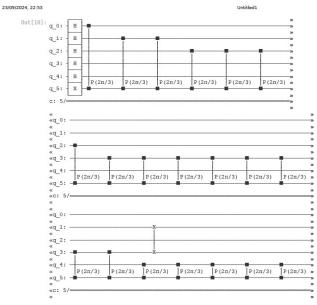
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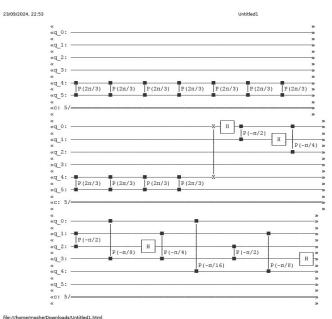
```
The second question is for t=5
```

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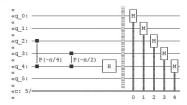


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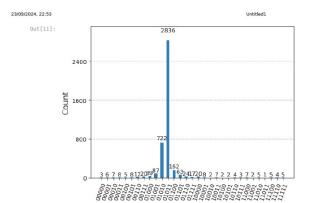
In [1]: # Let's see the results!
 # aer_sim = Aer.get_backend('aer_simulator')
 shots = 4096
 t_qpa3 = transpile(qpe3, aer_sim)
 qobj = assemble(t_qpe3, shots=shots)
 results = aer_sim.run(qobj).result()
 answer = results.get_counts()

plot_histogram(answer)

/tmp/ipykernel_5723/652080245.py:6: DeprecationWarming: Using a qobj for run() is deprecated as of qiskit-aer 0.14 a nd will be removed no sconer than 3 months from that release date. Transpiled circuits should now be passed directly using backed.run(circuits, **run options). results = aer_sim.run(qobj).result()

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The two most likely measurements are now $\theta 1\theta 11$ (decimal 11) and $\theta 1\theta 10$ (decimal 10). Measuring these results would tell us θ is:

$$\theta = \frac{11}{2^5} = 0.344$$
, or $\theta = \frac{10}{2^5} = 0.313$

These two results differ from $\frac{1}{3}$ by 3% and 6% respectively. A much better precision!

In []

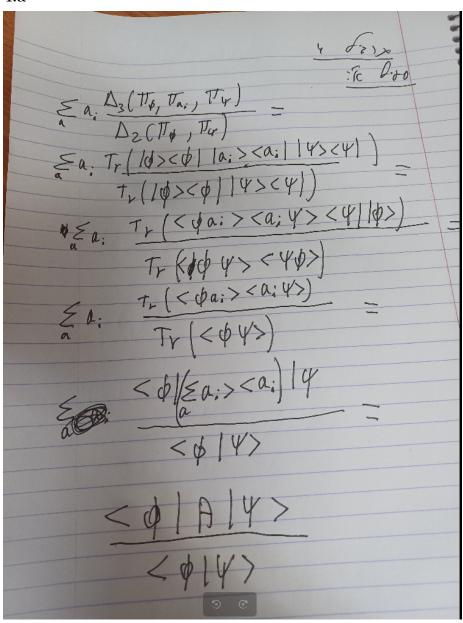
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Bi(i) = 21 if T[i] [Ti: 1102 0 otherwice Sister of the cities of the sister 20. N-15 Phy -ikisk g 0,21/6 12 (2)

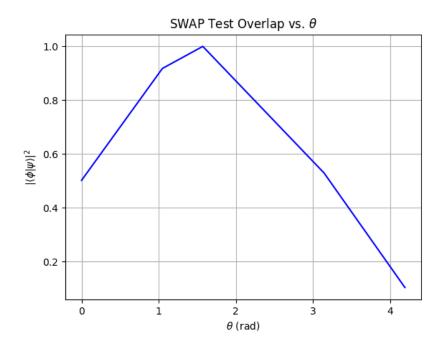
14>= 8, \(\text{Vi} \) | 1/3 | 5/2 \(\text{Visite} \) \(\text{Visi Painte & Cfor of Every (3) 6,0,410,0 Mess than ... (El C.)

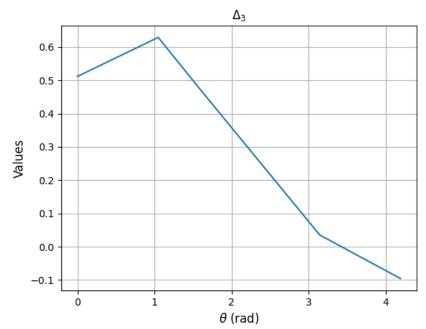
4.a



4.b

(i)





(ii)

Note that

$$\Delta_3(\Pi_\phi, |1\rangle\langle 1|\Pi_\psi)$$

is computed as:
$$\Delta_3(\Pi_\phi, |1\rangle\langle 1|\Pi_\psi) = \text{Tr}(\Pi_\phi |1\rangle\langle 1|\Pi_\psi) = \text{Tr}(\langle 1|\Pi_\psi\Pi_\phi |1\rangle) = \Pi_\psi\Pi_\phi(2,2) = \text{Tr}(\Pi_\psi\Pi_\phi) - (\Pi_\psi\Pi_\phi)(1,1) = \Delta_2(\Pi_\psi\Pi_\phi) - \Delta_3(\Pi_\phi |0\rangle\langle 0|\Pi_\psi)$$

Since the right-hand side has already been calculated, we can now compute the left-hand side directly without any further measurements. ### Answer Recall that Z is defined as:

$$Z = 1 \cdot |0\rangle\langle 0| + (-1) \cdot |1\rangle\langle 1|$$

We will now use the identity proven in part 4(a), along with the previously computed values of Δ_2 and Δ_3 , to compute Z_w :

$$Z_w = \frac{\Delta_3(\Pi_\phi|0\rangle\langle 0|\Pi_\psi)}{\Delta_2(\Pi_\phi\Pi_\psi)} - \frac{\Delta_3(\Pi_\phi|1\rangle\langle 1|\Pi_\psi)}{\Delta_2(\Pi_\phi\Pi_\psi)}$$

The result Z_w can be computed directly using the above equation.

