How Tight are Malthusian Constraints?

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The Historical Relevance of Malthus

"*But the logic of the Malthusian model matches the empirical evidence for the preindustrial world. While even long before the Industrial Revolution small elites had an opulent lifestyle, the average person in 1800 was no better off than his or her ancestors of the Paleolithic or Neolithic.*" - Clark (2007)

"*During the Malthusian Epoch....technologically superior countries eventually developed denser populations, but their standards of living did not reflect the degree of their technological advancements.*" - Galor (2011)

Malthusian Pressures?

"*To the extent that it left such improvements to be realized in the future, eighteenth-century European farming left more room to continue growth before encountering Malthusian constraints than was present in east Asia.*" - Pomeranz (2000)

"*Clearly the shortage of many resources grew more severe [in China] ... A major cause of these shortages was of course the continuing growth of the population under conditions of relative technological standstill.*" - Elvin (1973)

"*In both regions population grew over the period 1680 to 1850: In China from an estimated 150 million to an estimated 400-410 million and in Western Europe from some seventy-five million to some 170 million and in both there were Malthusian pressures.*" - Vries (2013)

The Continued Relevance of Malthus

"*[Africa's] countries remain mired in a Malthusian crisis of high mortality, high fertility, and rapid population growth (with an accompanying state of chronic extreme poverty)*" - Conley, McCord, and Sachs (2007)

"*The Malthusian channel by which a high level of population reduces income per capita is still relevant in poor developing countries that have large rural populations dependent on agriculture, as well as in countries that are heavily reliant on mineral or energy exports.*" - Weil and Wilde (2009)

"*Our general aim is to build a theory of economy-environment interactions capable of addressing one of the main future challenges ... how to sustain innovation-driven income per capita growth in a habitat that has a finite carrying capacity of people.*" - Peretto and Valente (2015)

Malthusian?

Some examples of usage:

- "Malthusian constraints"
- "Malthusian pressure"
- "Malthusian limits"
- "Malthusian crisis"
- "Malthusian conditions binding"

What do we mean by a "Malthusian constraint"?

Definition

For us: the Malthusian constraint is the *elasticity of output with respect to agricultural land*.

This answers:

- How important is land to production?
- How does the average product of labor change with respect to labor?
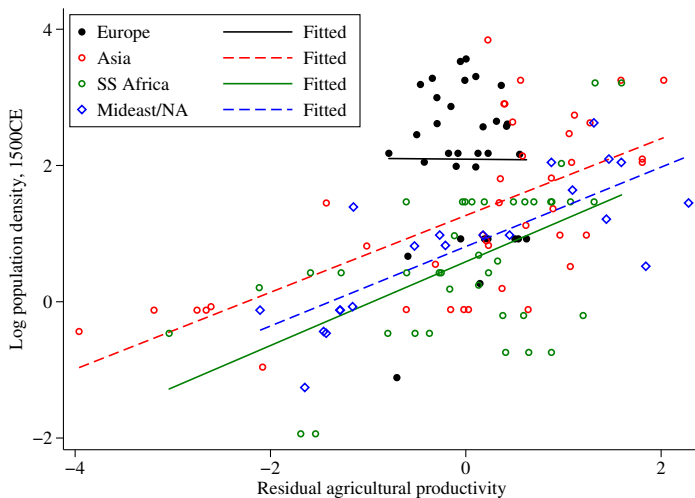- How sensitive is economy to a *change* in population?

Toy Model

Basic idea

Look at relationship of density and inherent agricultural produtivity (TFP)

- If density is sensitive to productivity ⇒ *loose* Malthusian constraint
- If density is insensitive to productivity ⇒ *tight* Malthusian constraint

Density and Productivity, by Region, 1500CE

Data from Ashraf and Galor (2010). Residual plot using their controls except continent FE.

In this paper

Estimate the Malthusian constraint:

- Use relationship of *rural* density and agro-climatic agricultural TFP
- Estimates come from *within*-province variation (province FE)
- Population data from HYDE
- Agro-climatic TFP built from Galor and Özak data on caloric suitability

We find:

- Constraints range from 0.090 to 0.308
- Variation is related to agro-climatic conditions
- Temperate, cold, regular rain $\Rightarrow$ tight Malthusian constraints
- Equatorial, hot, seasonal rain $\Rightarrow$ loose Malthusian constraints

Implications

Pattern of results:

- No strict relationship with development
- Rich places today do not (did not?) have looser Malthusian constraints

But..

- Constraint determines how sensitive real wages and agric. labor share are to shocks
- Tight constraint $\Rightarrow$ very sensitive (and v.v.)

So says something about role of following in development:

- Population shocks (epidemics, mortality transition)
- Affect response to technology shocks (new crops or better crops)

Some Related Literature:

- **Geography and development:**
- **Malthusian and UGT models:**
- **Agriculture and development:**

Two specific:

- : Pattern/date of urbanization at grid-cell level based on agro-climatic conditions
- : Spatial organization of economic activity, relationship to geograhpic conditions

A Model of Density and Productivity

Region I contains a set of districts, each denoted by i, with aggregate agricultural production

$$Y_i = A_i X_i^\beta \left(K_{Ai}^\alpha L_{Ai}^{1-\alpha} \right)^{1-\beta} \tag{1}$$

- K_{Ai} is all other inputs (e.g. capital)
- L_{Ai} is agricultural labor in district i (not a single sector)
- Assume β and α are identical *within* region (but not nec. *across* regions)
- Elasticity of Y_i/L_{Ai} w.r.t. L_{Ai} is $\alpha + \beta(1 - \alpha)$

Mobile Factors

The wage and return to capital in each district are given by

$$w = \phi_L \frac{Y_i}{L_i}$$

(2)

$$r = \phi_K \frac{Y_i}{K_i}$$

- ϕ_L and ϕ_K are shares of output
- No assumption that shares = elasticities
- Shares are identical *within* region (but not nec. *across* regions)
- Capital and labor are mobile *within* region (but not nec. *across* regions)

Solving for Labor Allocations

Given mobility of labor and capital within region,

$$\frac{K_i}{L_{Ai}} = \frac{w}{r}\frac{\phi_K}{\phi_L}. \tag{3}$$

Adding up condition for agricultural labor within region

$$\sum_{i \in I} L_{Ai} = L_A. \tag{4}$$

Solve for allocation of labor (relative to land) to district i

$$\frac{L_{Ai}}{X_i} = A_i^{1/\beta} \frac{L_A}{\sum_{j \in I} A_j^{1/\beta} X_j}. \tag{5}$$

Agricultural Labor Allocation

Take logs of L_{Ai}/X_i expression

$$\ln L_{Ai}/X_i = \frac{1}{\beta} \ln A_i + \ln \Gamma, \tag{6}$$

where

$$\Gamma = \frac{L_A}{\sum_{j \in I} A_j^{1/\beta} X_j}. \tag{7}$$

is a *region-specific* term.

- β can be estimated from elasticity of L_{Ai}/X_i w.r.t. A_i.
- $1/\beta$ small (tight), ag. workers spread evenly w/in region
- $1/\beta$ large (loose), ag. workers concentrated on high A_i

Agricultural Labor Allocation

Take logs L_{Ai}/X_i expression

$$\ln L_{Ai}/X_i = \frac{1}{\beta} \ln A_i + \ln \Gamma, \tag{8}$$

where

$$\Gamma = \frac{L_A}{\sum_{j \in I} A_j^{1/\beta} X_j}. \tag{9}$$

is a *region-specific* term.

- Γ is constant for all districts w/in region
- Ag labor relative to total labor (L_A/L) does not affect β or Γ
- Expression is not unique to heaviliy agricultural regions (or eras)

Using as a Specification

Re-arranging the prior expression and adding some notation:

$$\ln A_{isc} = \alpha + \beta \ln L_{Aisc}/X_{isc} + \gamma_{sc} + \delta' \mathbf{Z}_{isc} + \epsilon_{isc}. \tag{10}$$

- District i, region/state/province s, country c
- γ_{sc}, region/country FE, pick up Γ term
- $\mathbf{Z}_{isc}$ are additional controls
- ϵ_{isc} is error term

Using as a Specification

YES, we moved productivity, A_{isc} and agric. density L_{Aisc}/X_{isc} to opposite sides:

$$\ln A_{isc} = \alpha + \beta \ln L_{Aisc}/X_{isc} + \gamma_{sc} + \delta' \mathbf{Z}_{isc} + \epsilon_{isc}. \tag{11}$$

- NO, This is NOT a causal statement
- Estimating $1/\beta$ is difficult as β gets close to zero

Agricultural Density Data

L_{Aisc} comes from HYDE 3.1 database (Goldewijk et al, 2011)

- Population counts for 5 degree grid-cells built from administrative data
- We aggregate data back to administrative level (e.g. districts)
- (In progress) Validating against administrative data
- Rural population data (not agricultural)
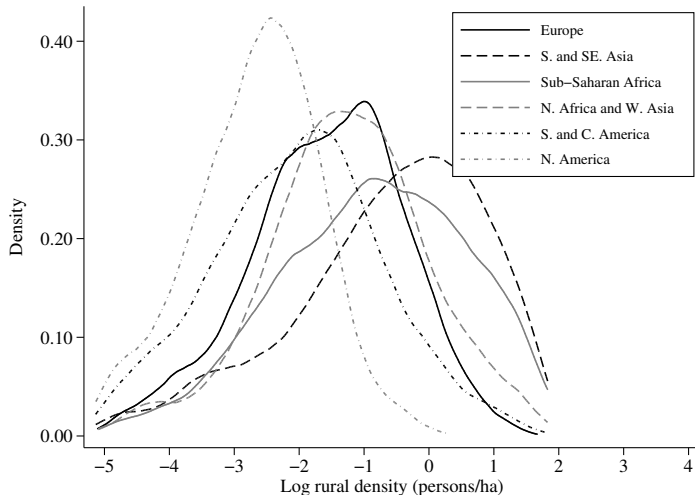- Main samples based on year 2000

X_{isc} calculated as area of a given district

- Overstates size of agricultural land

L_{Aisc}/X_{isc} data

- Trim above 99th and below 1st percentiles
- Drop if fewer than 100 total rural residents
- 29,030 total districts
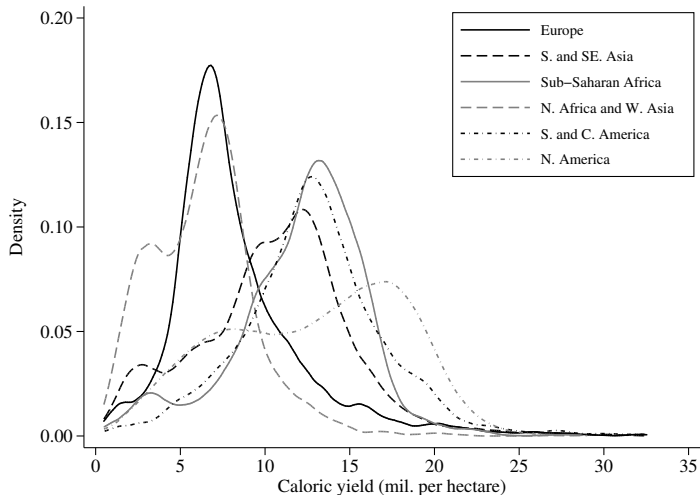
Agricultural Density Data

Agricultural Productivity Data

A_{isc} is built similar to Galor and Özak (2016) caloric suitability index

- Data from GAEZ on agro-climatic possible yield (in raw tons) for each crop
- Combine with nutritional information by crop (total calories per raw ton)
- For each grid cell, determine max calories
- Total max calories across grid cells in district, divide by total area
- As in Galor and Özak, yield is holding technology constant
- Trim above 99th and below 1st percentile

Agricultural Productivity Data

Agricultural Productivity Data

Control Variables

Henderson et al (2016) on spatial distribution of economic activity

- Urban activity correlated with (caused by?) high agricultural productivity (in some places)
- Low rural density because of urban activity
- $Corr(\epsilon_{isc}, \ln L_{isc}/X_{isc}) < 0$

Include two controls at the district level in $\mathbf{Z}_{isc}$ for urban/economic activity:

- Night lights density: follows Henderson et al (2016) using Global Radiance Calibrated data
- Urban percent of population: from HYDE
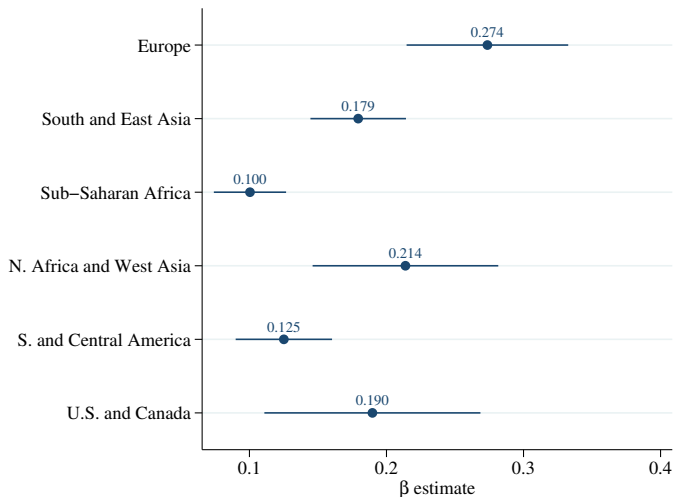
Spatial Errors and Hypothesis Testing

Assume ϵ_{isc} has spatial auto-correlation. Use Conley s.e. (1000km window).

Two hypothesis tests:

- Is the land constraint binding?
  - $H_0 : \beta = 0$ vs. two-sided alt
- Is the land constraint the same in two samples (e.g. Europe and Sub-Saharan Africa)?
  - $H_0 : \beta = \beta^{Ref}$ vs. two-sided alt
  - β^{Ref} from ad hoc "reference" sample
  - Implemented with interaction regression combining given and reference sample
  - In practice, choice of reference sample won't be crucial
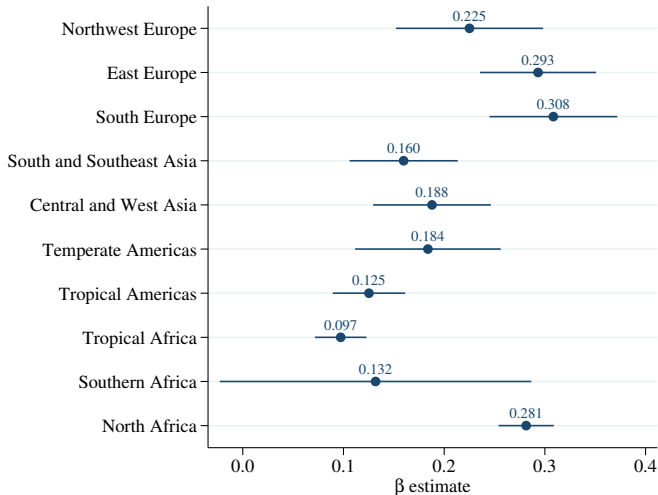
Interaction

Results by Major Region

Results by Major Region

Dependent Variable: Log caloric yield (A_{isc})

	Europe (1)	East & South Asia (2)	Sub-Saharan Africa (3)	North Africa & West Asia (4)	South & Central America (5)	U.S. and Canada (6)
				Region:		
Log rural density	0.274	0.179	0.100	0.214	0.125	0.190
	(0.030)	(0.018)	(0.013)	(0.035)	(0.018)	(0.040)
p-value $\beta = 0$	0.000	0.000	0.000	0.000	0.000	0.000
p-value $\beta = \beta^{Eur}$	.	0.007	0.000	0.190	0.000	0.095
Countries	34	24	43	18	25	2
Observations	7514	6761	3210	2762	9131	2782
Adjusted R-square	0.27	0.23	0.23	0.24	0.16	0.24

Results by Sub-Region

Results by Sub-Region

Dependent Variable in both panels: Log caloric yield (A_{isc})

Panel A				Sub-Region:	
					Excl. China
	North & Western Europe (1)	Eastern Europe (2)	Southern Europe (3)	South & Southeast Asia (4)	Central & West Asia (5)
Log rural density	0.225 (0.037)	0.293 (0.029)	0.308 (0.032)	0.160 (0.027)	0.188 (0.030)
p-value $\beta = 0$	0.000	0.000	0.000	0.000	0.000
p-value $\beta = \beta^{NWEur}$	.	0.140	0.061	0.157	0.435
Countries	16	9	9	13	18
Observations	1628	4772	1114	3921	2762
Adjusted R-square	0.13	0.28	0.20	0.15	0.15

Results by Sub-Region

Dependent Variable in both panels: Log caloric yield (A_{isc})

Panel B			Sub-Region:		
	Temperate Americas	Tropical Americas	Tropical Africa	South Africa	North Africa
Log rural density	0.184 (0.037)	0.125 (0.018)	0.097 (0.013)	0.132 (0.079)	0.281 (0.014)
p-value $\beta = 0$	0.000	0.000	0.000	0.095	0.000
p-value $\beta = \beta^{NWEur}$	0.431	0.016	0.001	0.285	0.158
Countries	5	22	39	4	5
Observations	3183	8730	3032	178	1147
Adjusted R-square	0.14	0.09	0.10	0.12	0.20

Results for China, Japan, Korea

Dependent Variable: Log caloric yield (A_{isc})					
	All China (1)	Temperate China (2)	Sub-Trop China (3)	Japan (4)	N. & S. Korea (5)
Residuals	0.416 (0.088)	0.522 (0.063)	0.118 (0.023)	0.178 (0.009)	0.214 (0.061)
p-value $\beta = 0$	0.000	0.000	0.000	0.000	0.001
p-value $\beta = \beta^{Temp}$			0.000		
Observations	266	130	136	1039	311
Adjusted R-square	0.59	0.72	0.14	0.18	0.27

Results by Province

Regions and sub-regions assume β constant within region/sub-region.
Instead, estimate β individually for each province

- Only provinces with 6 or more districts (1,340 provinces)
- ... so really big SE on any individual estimate
- Look at pattern of β's for each sub-region

Results by Province
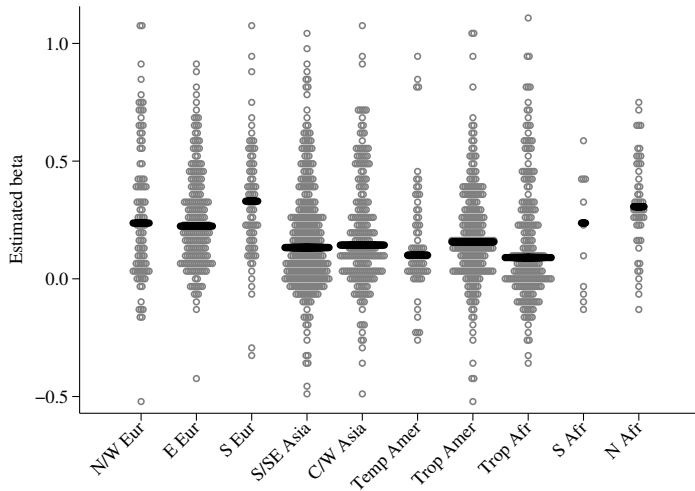
Results by Province

| Sub-region	Prov.	Mean	SD	Percentiles:				
				10th	25th	50th	75th	90th
Northwest Europe	96	0.25	0.40	-0.09	0.04	0.23	0.46	0.73
Eastern Europe	192	0.26	0.23	0.04	0.10	0.22	0.40	0.56
Southern Europe	73	0.29	0.38	0.07	0.16	0.33	0.48	0.60
South and S. East Asia	290	0.19	0.27	-0.05	0.02	0.14	0.31	0.55
Central and West. Asia	211	0.22	0.32	-0.06	0.03	0.14	0.35	0.55
Temperate Americas	70	0.15	0.23	-0.05	0.02	0.10	0.24	0.39
Tropical Americas	224	0.17	0.29	-0.07	0.04	0.15	0.31	0.44
Tropical Africa	209	0.18	0.53	-0.11	-0.01	0.09	0.29	0.58
Southern Africa	12	0.07	0.49	-0.11	-0.09	0.17	0.41	0.43
Northern Africa	53	0.30	0.36	0.03	0.22	0.31	0.48	0.64

Results by Crop

Region and sub-region results appear correlated with agro-climatic zones:

- Run samples defined by agro-climatic zones
- Zones based on GAEZ suitability indices for each crop (0 to 100)
- Index is based purely on climate and soil characteristics
- Define samples using 0 vs > 0 suitability
- Not estimating a crop-specific production function

Results by Crop
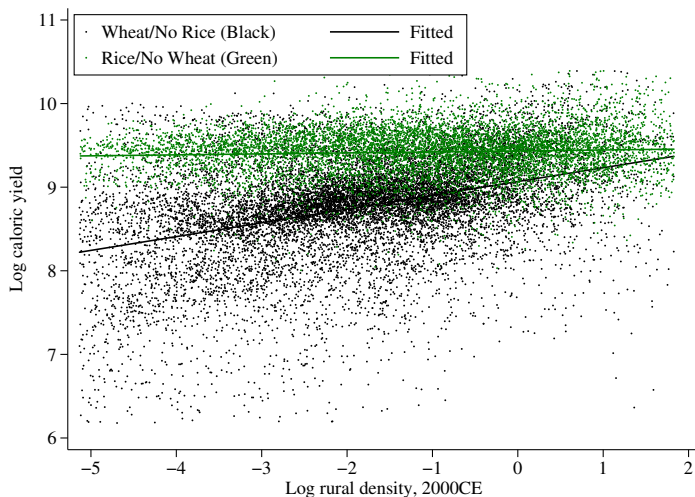
Results by Crop
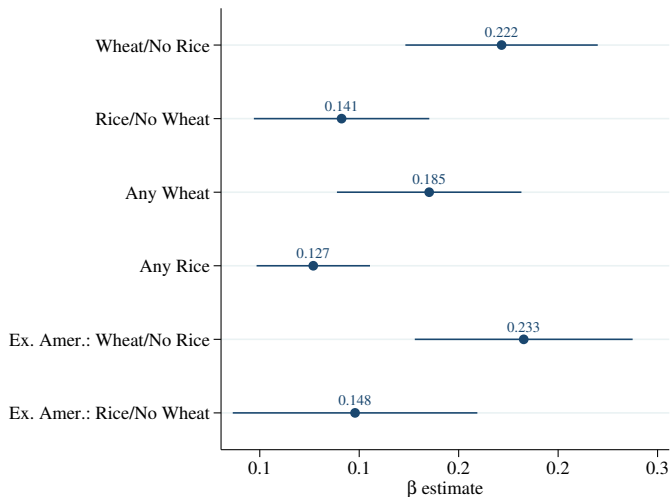
Results by Crop

Dependent Variable in all panels: Log caloric yield (A_{isc})

Panel A: Wheat and rice

| | Inclusion by crop suitability: | | | | | |
| | Entire world: | | | | Ex. Americas: | |
	Wheat>0 Rice=0 (1)	Wheat=0 Rice>0 (2)	Wheat>0 (3)	Rice>0 (4)	Wheat>0 Rice=0 (5)	Wheat=0 Rice>0 (6)
Log rural density	0.222 (0.025)	0.141 (0.022)	0.185 (0.024)	0.127 (0.015)	0.233 (0.028)	0.148 (0.031)
p-value $\beta = 0$	0.000	0.000	0.000	0.000	0.000	0.000
Countries	106	74	135	132	86	52
Observations	12627	7796	24431	19600	10185	4439
Adjusted R-square	0.18	0.14	0.15	0.12	0.21	0.14

Results by Crop

Dependent Variable in all panels: Log caloric yield (A_{isc})

Panel B: Tropical crops

	Cassava>0	Cowpea>0	Maize>0	Pearl Millet>0	Sweet Potato>0	Yams>0
				Inclusion is wheat suitability = 0, but:		
Log rural density	0.143	0.146	0.146	0.158	0.147	0.143
	(0.022)	(0.021)	(0.021)	(0.021)	(0.021)	(0.021)
p-value $\beta = 0$	0.000	0.000	0.000	0.000	0.000	0.000
Countries	74	80	78	72	77	78
Observations	8052	8312	8377	6590	8354	8269
Adjusted R-square	0.14	0.13	0.13	0.14	0.13	0.13

Results by Crop

Dependent Variable in all panels: Log caloric yield (A_{isc})

Panel C: Temperate crops

	Barley>0	Buck-wheat>0	Oats>0	Flax>0	Rye>0	White Potato>0
			Inclusion is rice suitability = 0, but:			
Log rural density	0.222	0.222	0.229	0.222	0.229	0.222
	(0.025)	(0.026)	(0.025)	(0.026)	(0.025)	(0.024)
p-value $\beta = 0$	0.000	0.000	0.000	0.000	0.000	0.000
Countries	106	76	72	74	72	105
Observations	12627	11162	11089	11035	11106	12494
Adjusted R-square	0.18	0.19	0.20	0.20	0.20	0.19

Results by Climate Zone

Results by Climate Zone
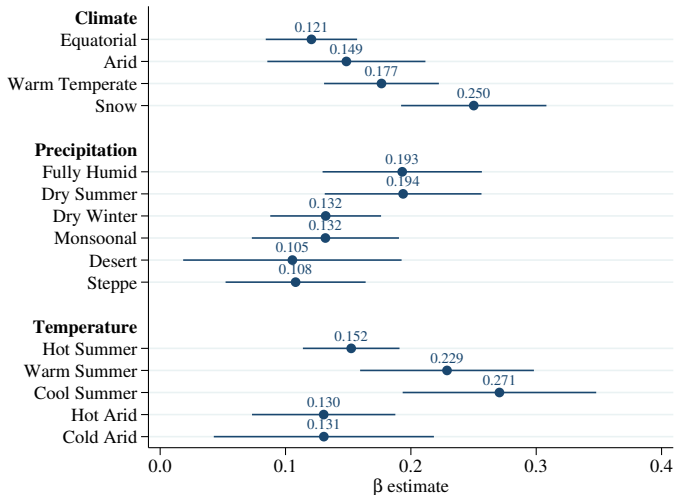
Robustness

"Robust" meaning

- Absolute and relative size of β estimates across samples are similar
- Hypothesis tests return similar results

Robustness checks:

- Use province level data (with country FE) `Results`
- Use rural density from 1900 from HYDE `Results`
- Use untrimmed samples of rural density and/or agricultural productivity
- Use districts with fewer than 100 rural residents
- Clustered standard errors (at province level)

Measurement Error

Measurement error in rural density data

- Creates attentuation bias
- Is measurement error more pronounced in some regions (e.g. SE Asia) and driving results?
- True variance of $\ln L_{Aisc}/X_{isc}$ would have to be one-third of measured variance
- Implies one-third of districts have rural density mis-stated by factor of > 2 or < 0.5

Measurement Error

Measurement error of land area, X_{isc}, specifically

- We are using total land area, not agricultural area, so X_{isc} always overstated
- Systematic mismeasurement of districts within a province not a problem
- Variation in systematic mismeasurement across provinces not a problem (FE)
- Problem is *variation in variation of mismeasurement* across provinces
- Some provinces have more geographic variation across districts?
- Provinces with low β estimates do not have higher variance of geographic characteristics

Mobility of Workers?

Mobility of workers across districts within a province?

- If workers immobile, may create similar densities across districts
- Estimated β would be falsely high?
- Would have to be that frictions more prevalent in high-β places (e.g. Europe or N. Africa)

Mobility of Workers?

Mobility of workers across districts within a province?

- If workers immobile, may create similar densities across districts
- Estimated β would be falsely high?
- Would have to be that frictions more prevalent in high-β places (e.g. Europe or N. Africa)
- Or, workers immobile, but demographic behavior varies widely by district?
- Estimated β would be falsely low?
- Would have to be demography is more variable in low-β places (e.g. Sub-Saharan Africa)

Elasticity of Substitution?

What if land and labor do not have elasticity of subs. equal to one?

- Elasticity of output w.r.t. land depends on rural density L_A/X
- With EOS more than one, higher density, lower elasticity
- Do results fit this?
    - South/SE Asia, some SS Afr are high density, low β
    - ..but C/S America, other SS Afr are low density, low β
    - ..but N America lowest density, not highest β

Density?

Back to the model

If each person consumes c_A in agric. goods, with L people, then:

$$c_A L = \sum_{i \in I} A_i X_i^{\beta} \left(K_{Ai}^{\alpha} L_{Ai}^{1-\alpha} \right)^{1-\beta}, \tag{12}$$

Assume that capital and labor are mobile between districts within region I, but also between agric. and non-agric. Can solve for

$$\frac{L_A}{L} = \left(\frac{c_A L^{\beta}}{(K/L)^{\alpha(1-\beta)} \left(\sum_{i \in I} A_i^{1/\beta} X_i \right)^{\beta}} \right)^{1/(1-\beta)} \tag{13}$$

where K/L is aggregate capital/labor ratio.

Real Wage

With labor mobile between agric. and non-agric., then

$$p_N w_N = p_A w_A \tag{14}$$

where p_j is nominal price of good j, and w_j is wage in terms of output in j.
Combine with $w_A = \phi_L Y_A / L_A$ definition from before to get

$$\frac{p_N w_N}{p_A} = \frac{\phi_L c_A}{L_A / L}. \tag{15}$$

This is a "grain wage". Non-agricultural nominal wage deflated by the price of agricultural goods.

Elasticities

With respect to population shocks

- $\frac{\partial L_A/L}{\partial L} \frac{L}{L_A/L} = \frac{\beta}{1-\beta}$
- $\frac{\partial p_N w_N/p_A}{\partial L} \frac{L}{p_N w_N/p_A} = -\frac{\beta}{1-\beta}$

With respect to productivity shocks in agric. (equal across all districts)

- $\frac{\partial L_A/L}{\partial A} \frac{A}{L_A/L} = \frac{1}{1-\beta}$
- $\frac{\partial p_N w_N/p_A}{\partial A} \frac{A}{p_N w_N/p_A} = -\frac{1}{1-\beta}$
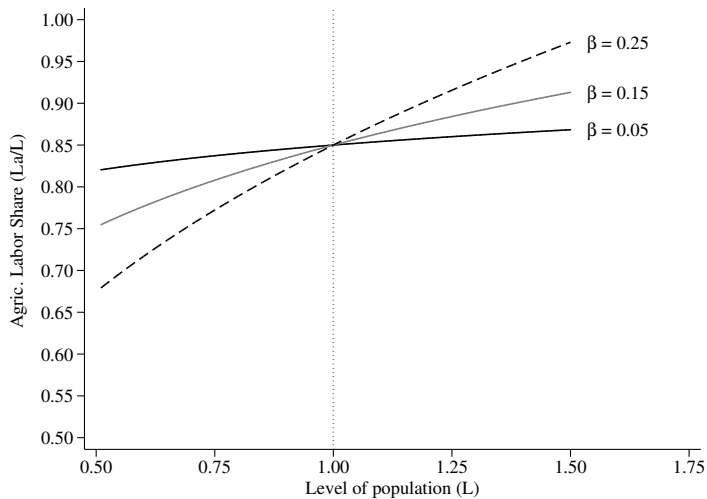
A Toy Calibration

Set up three economies, each with

- $L = 1$
- $A = 1$
- $X = 1$

but where the value of β takes on values (0.05, 0.15, 0.25). Initial value of c_A is set so that $L_A/L = 0.85$ in each.
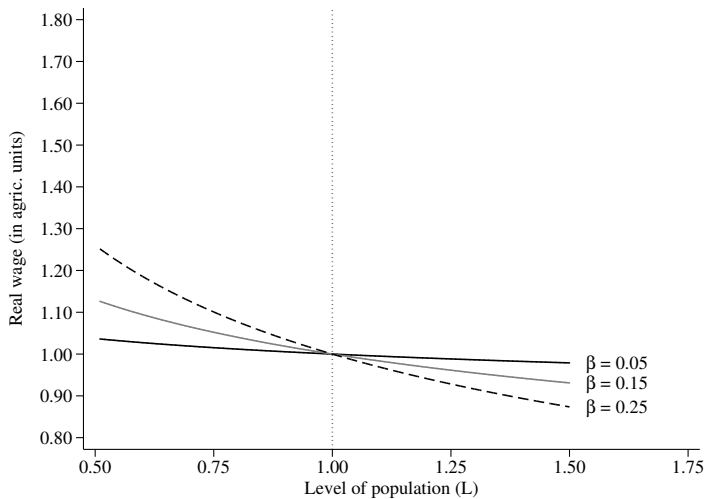
Look at effect of variation in L and A on
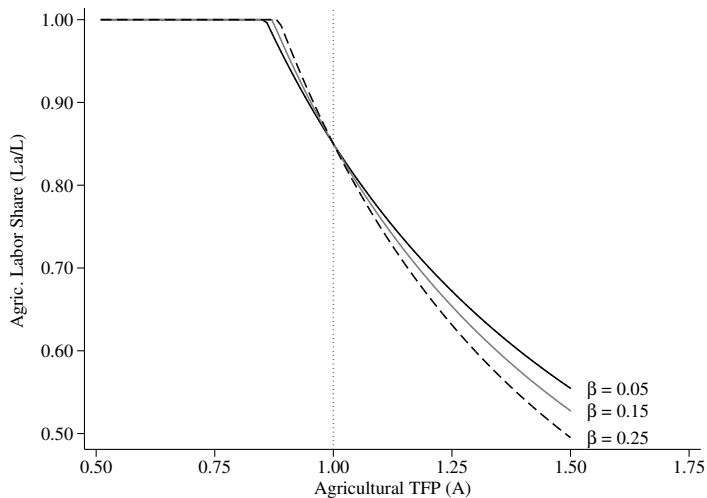
- L_A/L
- Real wage

A Toy Calibration

A Toy Calibration

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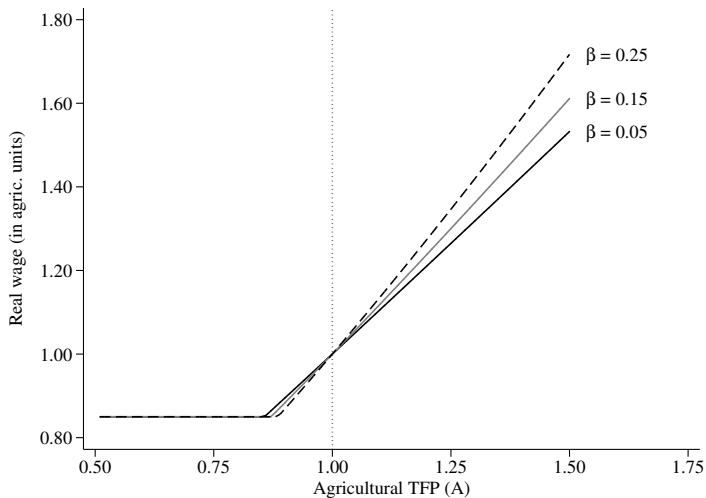
Conclusion

- Define the Malthusian constraint as the elasticity of output w.r.t. land
- Estimate constraint from variation in rural density within provinces
- Constraint is "tight" (0.20-0.30) in temperate areas (N. China, Europe, US/Canada, S. Africa)
- Constraint is "loose" (0.05-0.10) in tropical areas (S. China, SE Asia, C. Africa, S/C America)
- Constraint dictates the sensitivity of L_A/L and real wage to population and productivity

A Toy Model

Single sector production with produtivity, A, fixed factor, X, and labor, L.

$$Y = AX^\beta L^{1-\beta} \tag{16}$$

Average product of labor is:

$$\frac{Y}{L} = A\left(\frac{X}{L}\right)^\beta. \tag{17}$$

Elasticity of average product with respect to L depends on β.

A Toy Model

Assume population process works such that average product is always c, density is

$$\frac{L}{X} = \left(\frac{A}{c}\right)^{1/\beta}. \tag{18}$$

- Density does not tell us whether land constraint is tight or loose
- But β tells us how sensitive density is to productivity

Return

Interaction Regression

Combine a given sample with the reference sample (denoted by *Ref*). Run the following regression with interaction terms

$$\ln A_{isc} = \beta \ln L_{Aisc}/X_{isc} + (\beta^{Ref} - \beta) \ln L_{Aisc}/X_{isc} \times I(Ref) \qquad (19)$$
$$+ \gamma_{sc} + \delta' \mathbf{Z}_{isc} + (\delta^{Ref} - \delta)' \mathbf{Z}_{isc} \times I(Ref) + \epsilon_{isc}.$$

where $I(Ref)$ is an indicator for the reference region. Our hypothesis test is $H_0 : \beta^{Ref} - \beta = 0$, the coefficient on the interaction term for rural density.

Results by Major Region, 1900 CE

Dependent Variable: Log caloric yield (A_{isc})						
				Region:		
	Europe (1)	East & South Asia (2)	Sub-Saharan Africa (3)	North Africa & West Asia (4)	South & Central America (5)	U.S. and Canada (6)
Log rural density	0.413 (0.046)	0.254 (0.054)	0.061 (0.032)	0.269 (0.035)	0.070 (0.029)	0.316 (0.064)
p-value $\beta = 0$	0.000	0.000	0.054	0.000	0.016	0.000
p-value $\beta = \beta^{Eur}$	.	0.025	0.000	0.013	0.000	0.217
Countries	34	24	43	18	25	2
Observations	7514	6761	3210	2762	9131	2782
Adjusted R-square	0.43	0.34	0.31	0.37	0.24	0.40

Return

Results by Sub-Region, 1900 CE

Dependent Variable in both panels: Log caloric yield (A_{isc})

Panel A				Sub-Region:	
					Excl. China
	North & Western Europe (1)	Eastern Europe (2)	Southern Europe (3)	South & Southeast Asia (4)	Central & West Asia (5)
Log rural density	0.363 (0.055)	0.414 (0.027)	0.291 (0.025)	0.090 (0.035)	0.264 (0.062)
p-value $\beta = 0$	0.000	0.000	0.000	0.010	0.000
p-value $\beta = \beta^{NWEur}$	.	0.247	0.323	0.000	0.232
Countries	16	9	9	13	18
Observations	1628	4772	1114	3921	2762
Adjusted R-square	0.35	0.45	0.31	0.24	0.26

Return

Results by Sub-Region, 1900 CE

Dependent Variable in both panels: Log caloric yield (A_{isc})

Panel B			Sub-Region:		
	Temperate Americas	Tropical Americas	Tropical Africa	South Africa	North Africa
Log rural density	0.200 (0.059)	0.080 (0.028)	0.049 (0.033)	0.257 (0.091)	0.296 (0.041)
p-value $\beta = 0$	0.001	0.004	0.130	0.005	0.000
p-value $\beta = \beta^{NWEur}$	0.042	0.000	0.000	0.316	0.322
Countries	5	22	39	4	5
Observations	3183	8730	3032	178	1147
Adjusted R-square	0.22	0.12	0.16	0.34	0.30

Return

Results by Major Region, 2000 CE, Provinces

Dependent Variable: Log caloric yield (A_{isc})

	Europe (1)	East & South Asia (2)	Sub-Saharan Africa (3)	North Africa & West Asia (4)	South & Central America (5)	U.S. and Canada (6)
				Region:		
Log rural density	0.385	0.267	0.124	0.382	0.027	0.111
	(0.101)	(0.092)	(0.044)	(0.112)	(0.068)	(0.280)
p-value $\beta = 0$	0.000	0.004	0.005	0.001	0.697	0.693
p-value $\beta = \beta^{Eur}$	.	0.389	0.018	0.983	0.003	0.358
Countries	34	23	43	18	23	2
Observations	507	570	525	282	355	47
Adjusted R-square	0.16	0.19	0.13	0.19	0.08	0.13

Return

Results by Sub-Region, 2000 CE, Provinces

Dependent Variable in both panels: Log caloric yield (A_{isc})

Panel A			Sub-Region:		
				Excl. China	
	North & Western Europe (1)	Eastern Europe (2)	Southern Europe (3)	South & Southeast Asia (4)	Central & West Asia (5)
Log rural density	0.662 (0.114)	0.343 (0.074)	0.169 (0.102)	0.044 (0.016)	0.384 (0.069)
p-value $\beta = 0$	0.000	0.000	0.099	0.007	0.000
p-value $\beta = \beta^{NWEur}$	.	0.006	0.004	0.000	0.037
Countries	16	9	9	13	18
Observations	166	206	135	370	303
Adjusted R-square	0.20	0.24	0.15	0.17	0.24

Return

Results by Sub-Region, 2000 CE, Provinces

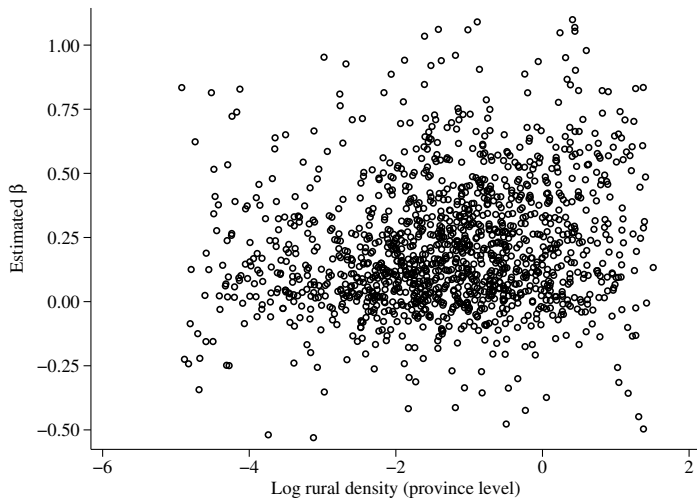Dependent Variable in both panels: Log caloric yield (A_{isc})

Panel B			Sub-Region:		
	Temperate Americas	Tropical Americas	Tropical Africa	South Africa	North Africa
Log rural density	0.162	0.014	0.115	0.406	0.621
	(0.122)	(0.070)	(0.044)	(0.224)	(0.133)
p-value $\beta = 0$	0.188	0.839	0.009	0.071	0.000
p-value $\beta = \beta^{NWEur}$	0.003	0.000	0.000	0.310	0.818
Countries	5	20	39	4	5
Observations	85	317	497	28	88
Adjusted R-square	0.14	0.08	0.13	0.21	0.28

Return

Relationship fo β to rural density, by province