

June 16, 2022

APPENDICES: The Elasticity of Aggregate Output with Respect to Capital and Labor

Dietrich Vollrath
University of Houston

ABSTRACT

These appendices contain information on data matching, assumptions, and calculations used in the main paper. Additional results are also reported.

Contact information: 201C McElhinney Hall, U. of Houston, Houston, TX 77204, devollrath@uh.edu.

Contents

A.1	Data and code	2
A.2	Matching historical industry data to input/output tables	2
A.2.1	Baseline matching	3
A.2.1.1	One SIC to one NAICS:	3
A.2.1.2	One SIC to many NAICS:	4
A.2.1.3	Many SIC to one NAICS:	4
A.2.2	Government	5
A.2.3	BEA capital stock data	5
A.3	Proprietors income	6
A.4	From Input/Output tables to industry-by-industry costs	7
A.5	Comparison using BEA “After Redefinitions” table	9
A.6	Comparison of results including and excluding imported intermediates	10
A.7	Comparing elasticities and cost ratios	11
A.7.1	A simple example	11
A.7.2	Full theory	12
A.7.3	Empirical Relationships	15
A.8	Markups and profit shares	16
A.9	User cost details	17
A.9.1	Nominal interest rate	18
A.9.2	Expected inflation	19
A.9.3	Depreciation	19
A.9.4	Depreciation allowance	20
A.9.5	Corporate tax rate	20
A.10	Series breaks at matching	20
A.11	Housing and government	20
A.12	De-capitalizing IP	22
A.13	Allowing for negative costs	22
A.14	Annual estimates of elasticities	23

List of Figures

A.1	Estimates of capital elasticity, different proprietors income assumptions	24
A.2	Relationship of capital cost share to markup across industries	25
A.3	Relationship of capital cost share to intermediate use share across industries	26
A.4	Aggregate value-added markup under different capital cost assumptions	27
A.5	Profits as a share of value-added under different capital cost assumptions	28
A.6	Baseline estimates of ϵ_{Kt} , with data source breaks denoted	29
A.7	Comparison of user cost estimates of ϵ_{Kt} , with different government costs	30
A.8	Comparison of estimates when allowing negative costs or not	31

List of Tables

A.1	Industrial classification of data by year	3
A.2	Matching of SIC 1972 to NAICS, 1948-1962, Part 1	32
A.3	Matching of SIC 1972 to NAICS, 1948-1962, Part 2	33
A.4	Matching of SIC 1972 to NAICS, 1963-86, Part 1	34
A.5	Matching of SIC 1972 to NAICS, 1963-86, Part 2	35
A.6	Matching of SIC 1987 to NAICS, 1987-96, Part 1	36
A.7	Matching of SIC 1987 to NAICS, 1987-96, Part 2	37
A.8	Comparison of ϵ_{Kt} estimates before and after redefinitions, 1997-2018	38
A.9	Comparison of ϵ_{Kt} estimates before and after redefinitions, 1997-2018	39
A.10	Comparison of ϵ_{Kt} estimates with and without imports, 1997-2018	40
A.11	Comparison of ϵ_{Kt} estimates with and without imports, 1997-2018	41
A.12	Capital costs as share of factor costs and value-added, housing and government	42
A.13	Baseline annual estimates of elasticities, 1948-2018, no-profit assumption	43
A.14	Baseline annual estimates of elasticities, 1948-2018, depreciation cost assumption	44
A.15	Baseline annual estimates of elasticities, 1948-2018, investment cost assumption	45
A.16	Baseline annual estimates of elasticities, 1948-2018, user cost assumption	46

A.1 Data and code

All of the code and raw data for this paper are publicly available. The site <https://github.com/dvollrath/Elasticity> contains both. The README file contained there includes instructions for replicating all tables, figures, and calculations in the paper.

A.2 Matching historical industry data to input/output tables

As described in Section 3 of the main text, the first issue with creating the data series used in the estimates of ϵ_{Kt} is matching various data sources from the national accounts with different industrial classification schemes.

Figure A.2 is identical to Table 1 in the main text, replicated here for convenience. It shows the classification schemes used for various pieces of data. In each case the input/output is treated as the “master” and the other series are matched to it.

For each industry in a given year in the I/O table, I need information on both value-added components (value-added, labor compensation, proprietors income, gross operating surplus, taxes on production, depreciation) and capital stocks (stock and price indices for structures, equipment, IP). The industry classifications for the value-added components and capital data are not NAICS 2012, so to bring that information over I need to match the other classifications listed in Table A.2 to NAICS 2012.

The literal matches I use can be found in Tables A.14 through A.14, which are shown at the end of this appendix, as they are quite long. These tables show for each series (48-62, 63-86, 87-96)

Table A.1: Industrial classification of data by year

Series	I/O tables	Value-added	
		components	Capital stock
1948-62	NAICS 2012 (47 ind)	SIC 1972	BEA/NAICS 2012
1963-86	NAICS 2012 (65 ind)	SIC 1972	BEA/NAICS 2012
1987-96	NAICS 2012 (65 ind)	SIC 1987	BEA/NAICS 2012
1997-2018	NAICS 2012 (71 ind)	NAICS 2012	BEA/NAICS 2012

Notes: This table shows the classifications used for each range of years. The complete mapping of industry data across sources is provided in the Appendix. All data are from the BEA.

which SIC industry is matched to which NAICS 2012 industry. Each series is broken into two tables (Part 1 and Part 2) to aid in legibility.

A.2.1 Baseline matching

There are three types of matches that can be found in these tables:

A.2.1.1 One SIC to one NAICS:

These are the straightforward cases where the SIC industry lines up directly with a NAICS industry. For example for 1947-62 the SIC industry “Construction” (SIC 1972 code C) is matched to NAICS industry “Construction” (NAICS code 23).

For these matches, obtaining the value-added components for the IO industry (coded using NAICS) is straightforward, and follows equation (12) in the text. I’ve reproduced the equation here, changing some of the notation to make the matching process clearer. First, “ELEM” refers to a data element (e.g. compensation, proprietors income, production taxes, etc.). Second, the NAICS superscript refers to the NAICS industry that this element is calculated for. The superscript SIC refers to the match SIC industry.

$$ELEM_{it}^{NAICS} = VALU_{it}^{NAICS} \times \frac{ELEM_{jt}^{SIC}}{VALU_{jt}^{SIC}}. \quad (\text{A.1})$$

In the case of a one-to-one match of SIC to NAICS, this equation is simple to process. I use the ratio of the given data element in SIC to the value-added in SIC ($ELEM_{jt}^{SIC}/VALU_{jt}^{SIC}$) to multiply by the reported value-added of the NAICS industry, $VALU_{it}^{NAICS}$, to obtain the size of the data element for the NAICS industry, $ELEM_{it}^{NAICS}$.

The assumption at work here is that because of the different classification systems the absolute size of value-added in SIC and NAICS matches will not be identical. However, what I am assuming is that the breakdown of value-added in a SIC industry is informative about the breakdown of

value-added in the matched NAICS industry. This will be imperfect, given that the scope of the industries is technically different.

A.2.1.2 One SIC to many NAICS:

This is a case where the NAICS is more detailed than the SIC. An example for 1947-62 is the SIC industry “Retail trade” (SIC code G) which I match to NAICS industries “Retail trade” (NAICS code 44RT) and “Food service and drinking places” (NAICS code 722).

Here, what I am doing is using the *ratios* from same SIC industry to infer the value-added components for multiple NAICS industries. Referring back to equation (A.1) and the example given, I’m assuming that the ratio $ELEM_{jt}^{SIC}/VALU_{jt}^{SIC}$ from SIC “Retail trade” is a good proxy for the ratio of that element to value-added in NAICS “Retail trade” and “Food service and drinking places”. The proportional breakdown of value-added across different components in those two NAICS industries is thus the same, as they all are assumed to have similar breakdowns to the SIC industry.

In this case I am losing detail, as the NAICS industries presumably have at least some differences in the breakdown of value-added components. I have experimented with several versions of the matching. For example, I’ve matched “Food service and drinking places” in the NAICS to “Amusement and recreation services” in the SIC. But these changes have not created any meaningful differences in the elasticity estimates.

A.2.1.3 Many SIC to one NAICS:

The final case is where there are multiple SIC industries matched to a single NAICS. An example here is “Banking” (SIC code 60), “Credit agencies” (SIC code 61), “Security and commodity brokers” (SIC code 62), “Insurance carriers” (SIC code 63), and “Insurance agents, brokers” (SIC code 64) all being matched to NAICS industry “Finance and Insurance” (NAICS code 52).

In this case SIC has more detail than NAICS, but I have no way of taking advantage of that detail. To get the value-added components for the NAICS industries I therefore sum up the value-added elements for the SIC industries, and use the ratio for those sums. In the example just given, I first find the sum of labor compensation in SIC industries 60, 61, 62, and 63. I then find the sum of value-added in SIC industries 60, 61, 62, and 63. The ratio of this sum of labor compensation to sum of value-added is used as the ratio $ELEM_{jt}^{SIC}/VALU_{jt}^{SIC}$. I then apply this ratio according to equation (A.1) to find labor compensation for the matched NAICS industry 52.

There is a loss of information here simply because of the lack of detail in the IO tables for these years. Again, reasonable alternative matches do not appear to impact the elasticity estimates in a meaningful way.

A.2.2 Government

In the match Tables A.14-A.14 one will note that there is no SIC code associated with any of the government industries: Federal general government, Federal government enterprises, State and local general government, or State and local government enterprises. Those industries do not have specific SIC codes assigned in the data obtained from the BEA.

In each case there is a straightforward match, however, to a NAICS industry of the same level. In the code implementing this the matching is done on the text, as opposed to a SIC code per se, but otherwise these are straight one-for-one matches.

A.2.3 BEA capital stock data

Theoretically, the BEA reports capital stock data using a NAICS industrial classification system. However, their classification is not precisely identical to the NAICS system found in the input/output tables. The vast majority of industries in the I/O table do have a direct match, but there are exceptions that I outline here.

For most industries, the BEA capital stock data reports a NAICS code in four digits, with different levels of dis-aggregation indicated by non-zeros. For example, 3200 refers to “Manufacturing”, while 3210 refers to “Wood products”, and one could dis-aggregate further to 3211 for a specific type of wood product. The I/O tables report the highest level digits, without trailing zeroes. Hence the I/O table has a NAICS code of 321 for “Wood products”. It does not contain an entry for NAICS code 32, as the point of the I/O table is to show the dis-aggregated relationships. Matching in this case is straightforward, as it simply has to take into account the trailing zeros. This works for the vast majority of industries.

There are exceptions, of course. In most cases these are simply differences in transcription involving letters (e.g. 113F matching to 113FF), but there are still one-to-one matches from the BEA capital data to the I/O table.

- BEA code 110C is matched to I/O code 111CA (Farms)
- BEA code 113F is matched to I/O code 113FF (Forestry, fishing, and related)
- BEA code 336M is matched to I/O code 3361MV (Motor vehicles)
- BEA code 336O is matched to I/O code 3364OT (Other transport equipment)
- BEA code 338A is matched to I/O code 339 (Miscellaneous manufacturing)
- BEA code 311A is matched to I/O code 311FT (Food, beverage, and tobacco products)
- BEA code 487S is matched to I/O code 487OS (Other transportation)

- BEA code 5320 is matched to I/O code 532RL (Rental and leasing services)

There is one case where two industries in the BEA capital data (5210 and 5220) are matched to a single I/O industry (521CL, Federal Reserve Banks). In this case the capital stock data from the BEA is simply summed up, and the total capital stock is applied to the I/O industry 521CL.

There are two cases where a single industry in the BEA capital data is matched to multiple industries in the I/O table. The first case is where BEA code 5310 is matched to both ORE (Other real estate) and HS (Housing) in the I/O tables. This is only the case for the period 1997-2018. In this case I need to allocate the data on capital for BEA code 5310 to two different I/O industries. I assign the capital data to the two I/O industries in proportion to their value-added. This means I am assuming the capital/output ratio, depreciation/output ratio, and investment/output ratio are the same in both ORE and HS.

The second case is where BEA code 44RT is matched to four different retail industries in the I/O table, 441 (Motor vehicle and parts dealers), 445 (Food and beverage stores), 452 (General merchandise stores), 440 (Other retail). I use the same strategy with this group. I split the capital, depreciation, and investment data on BEA industry 44RT to the four industries in proportion to their value-added.

A.3 Proprietors income

In the main text the amount of proprietors income that is considered a labor cost is calculated using equation (13) according to the formula used by [Gomme and Rupert \(2004\)](#). Here I show alternative estimates of the upper and lower bounds to ϵ_{Kt} when different assumptions about proprietors income are used.

Figure [A.1](#) plots the baseline upper (no-profit) and lower (depreciation-only) bounds in black lines, as usual. The first alternative is to assume that all proprietors income is in fact a labor cost, so that $COST_{iLt} = COMP_{it} + PROP_{it}$. The bounds with this assumption are either the gray dashed line (no-profit) or gray solid line (depreciation-only). As can be seen this lowers the estimated capital elasticity bounds, because the more value-added is assumed to be a labor cost. The modification for both bounds is minor.

The opposite assumption is that all proprietors income is either a capital cost or economic profit. Mechanically, this is equivalent to assuming that $COST_{iLt} = COMP_{it}$. The estimates of ϵ_{Kt} under these assumptions are the gray o's (no-profit) or gray x's (depreciation-only). In the depreciation-only case this makes no significant difference. However, under the no-profit assumption the estimated capital elasticity is much higher, averaging about 0.4 from 1948-1995, and approaching 0.45 by 2018. The reason for this is simply that with lower labor costs, more costs are assigned to capital in the no-profit case.

A.4 From Input/Output tables to industry-by-industry costs

In the main text, my baseline results are computed using the BEA's Input/Output tables, before redefinitions, at producer value. In particular, I extract values for the industry-by-industry $COST_{ijt}$ terms found in the matrix Λ in equation (6) of the main paper that is at the heart of the calculation of the elasticities. Here I provide further information on how I arrive at those values for $COST_{ijt}$.

To recall terms, there are J total industries and I am attempting to fill in a $J \times J$ block of information on $COST_{ijt}$. The BEA Input/Output tables do not report costs on an industry-by-industry basis, however. They distinguish industries from commodities (products made by industries), although the classification of commodities is nearly identical to that of industries. For example, there is a "Petroleum and coal products" industry as well as a "Petroleum and coal products" commodity.

Nevertheless, the two concepts are distinct. A given commodity could be produced by several industries, or an industry could produce several commodities. In principle there need not be an identical number of commodities to industries. In practice the BEA records information for J commodities that match the J industries, plus an additional two commodities with no matching industry. Those two commodities are "Used/scrap" and "Noncomparable imports". Denoting the number of commodities by M , the BEA uses $M = J + 2$ commodities.

This results in two different types of input/output tables that are available on an annual basis. The "Use Table", which I denote here by U , is a $M \times J$ matrix. The generic entry u_{mj} shows the amount of a commodity m used as an input by industry j . The "Make Table", which I denote by V , is a $J \times M$ matrix. The generic entry v_{jm} shows the amount produced by industry j of commodity m . Neither the entries u_{mj} in the Use Table nor the entries v_{jm} in the Make Table are exactly equal to $COST_{ij}$, the spending by industry j on inputs from industry i .

It is possible to recover an industry-by-industry matrix of $COST_{ij}$ terms from the Use and Make Tables. To do this requires one additional piece of information. Let the vector X_M measure the gross output of each of the M commodities. Form the matrix A as

$$A = V\hat{X}_M^{-1} \tag{A.2}$$

where the \hat{X}_M notation indicates a matrix with the elements of X_M along the diagonal (and zeroes everywhere else). Thus the diagonal entries of \hat{X}_M^{-1} are just one over the final use of a commodity. A is a $J \times M$ matrix. Using i to index the industries, the typical entry a_{im} measures the share of gross output of commodity m that is produced by industry i .

Now form the matrix C as

$$C = AU = V\hat{X}_M^{-1}U. \tag{A.3}$$

C is a $J \times J$ matrix. The typical entry of C is c_{ij} , the spending by industry j on output of industry

i . The matrix A gives industry i 's share of production of commodity m . The matrix U provides the amount of commodity m used by industry j . Multiplying A by U gives us the spending by industry j on output from industry i , originating through whatever commodities industry i may produce that industry j may require.

One remaining point is that because of how the Use and Make Tables are arranged, the values of c_{ij} in C are spending by j (the column) on inputs from industry i (the row). In the main text I refer to $COST_{ij}$, where this measures spending by industry i (the row) on output from industry j (the column). Hence $COST_{ij} = c_{ji}$. Given the values of $COST_{ij}$ I can calculate the λ_{ij} terms that make up Λ in equation (9) of the main text.

Two addition pieces of information can be recovered once the industry-by-industry matrix C has been calculated. Let X_I be a $J \times 1$ vector of gross output of industries, F_I be the $J \times 1$ vector of final use of each industry, and V_I be the $J \times 1$ vector of value-added of each industry. It is the case that

$$X_I = Ce + F_I \tag{A.4}$$

$$X_I = C'e + V_I, \tag{A.5}$$

where e is a $J \times 1$ vector of ones. The first relationship breaks down the gross output of industries into uses (inputs purchased by other industries or final use) while the second relationship breaks down gross output in terms of production (purchases of inputs from other industries or value-added).

The BEA reports a vector of gross output, X_I , in the Use Table. I take this vector as given. With X_I and C , it is possible to solve for both F_I and V_I using the relationships in (A.5). The vector V_I provides the values of $VALU_{it}^{IO}$ that I refer to in the main paper, and which are used to find costs of factors like labor and capital. The values of F_I provide the values of f_i for final use of industries that form the values of γ_i that go into the vector Γ in equation (8) of the main paper.

The BEA separately reports a measure of value-added by industry in the Use Table. The vector V_I I calculate from (A.5) contains small deviations from the reported data on value-added in the Use Table. In practice the deviations are minor. To assess this, for each year I calculated the correlation between the industry-level values in V_I from equation (A.5) and the reported industry-level value-added from the BEA. The minimum correlation in the 70 years was 0.99997, while the average was 0.99999. In 48 years of the years, the correlation is exactly one. Deviations, such as they are, appear to be in part due to rounding differences in my calculation compared to the reported BEA Tables.

A.5 Comparison using BEA “After Redefinitions” table

As described in the prior section, I develop a matrix C of industry-by-industry costs from the Use and Make Tables provided by the BEA. Those Use and Make Tables are “Before Redefinitions”, meaning the BEA has not made any modifications to the classification of commodities or industries. By using the “Before Redefinitions” Tables, I am able to calculate C annually from 1948-2018. Using C , I can calculate the Total Requirement Table, T , as

$$T = \left(I - C\hat{X}_I^{-1} \right)^{-1}. \quad (\text{A.6})$$

This matrix T measures the total dollars of spending on inputs necessary from each industry i to deliver one dollar of final use of industry j .

The BEA provides a separate Total Requirements Table for 1997-2018. This Table is provided “After Redefinitions” to the Use and Make Tables. These redefinitions reassign some transactions between commodity or industries. As such, the BEA Total Requirements Table is an analogue to my matrix T , but differs numerically because of those redefinitions to the underlying Use and Make Tables.

To assess whether using “Before Redefinitions” Use and Make Tables in my baseline calculations generates any significant difference compared to the “After Redefinitions” Tables, I re-calculated all the elasticity estimates from 1997-2018 using the “After Redefinitions” Tables.

Tables A.8 and A.9 show the annual results of After and Before calculations side-by-side, for each different choice regarding capital costs. For example Column (1) of Table A.8 shows the capital elasticity using the After Redefinition Table in 1997 was 0.3663, and Column (2) shows the comparable estimate from the main paper using the Before Redefinition Table as 0.3686. The difference is -0.0022, meaning my baseline estimates are slightly overstated compared to the After Redefinitions estimate. Reading down column (3) one can see that the size of that difference increased slightly over time, but that the average difference is -0.0027. There does not appear to be a significant (in the numerical sense) difference between the After and Before Redefinition-based estimates.

Looking over the remainder of Tables A.8 and A.9, a similar story holds. Regardless of the capital cost assumption, there is no large discrepancy between the baseline results using the Before Redefinition Tables and the After Redefinition Tables. Given the small discrepancy, the advantage of the Before Redefinition Tables is that they are available annually from 1948-2018, allowing for a longer time series of results than the After Redefinition Tables, which are only available from 1997-2018.

A.6 Comparison of results including and excluding imported intermediates

The baseline results in the paper take the Use Tables as given, and those Use Tables include imports of intermediate commodities by industries. Imported intermediate goods are offset by subtracting the imports from final use (as in typical national income accounting). For certain commodities, such as Oil and Gas Extraction (NAICS 211), the amount of imports are large enough that total final use of the commodity is negative. A commodity that is entirely imported (such as noncomparable imports) has negative final use that entirely offsets intermediate use, such that gross output is zero.

For the calculation of ϵ_K in equation (9) of the main text, the presence of imports influences the weights in Γ , the vector of final-use shares. An industry i which has relatively small domestic production but whose products are heavily imported (e.g. oil and gas in most years) will have a low(er) share of final use, γ_i . An industry j that has large domestic production, and which may import a large amount of products from other industries (e.g. chemical production that uses crude oil), will have a large(r) share of final use, γ_j . Thus, in calculating ϵ_K the aggregate elasticity will be heavily influenced by the elasticity with respect to capital in industry j but not by industry i . In the end, ϵ_K will reflect the elasticity of domestic production with respect to capital, taking imports as given.

An alternative is to exclude imports entirely from the Use Table, and calculate ϵ_K based only on domestic inputs to production. This alters the cost shares, λ_{ij} , that populate the Λ matrix in equation (9), lowering the cost share for intermediates with large imports (e.g. oil and gas) and raising the cost share for intermediates that are only produced domestically (e.g. services). Excluding imported intermediates while holding gross output constant increases the implied value-added of each industry. This will thus have the greatest effect on the calculation of ϵ_K in the no-profit case. The costs associated with imports in this case are instead attributed to capital, which raises the value of ϵ_K . In the other scenarios, the value of ϵ_K may be higher or lower than in the baseline (including imports) depending on how the exclusion of imports affects the relative sizes of the λ_{ij} terms.

Tables A.10 and A.11 report results that exclude imports from the Use Tables (columns 1 and 4), and compare those to the baseline results that include imports (columns 2 and 5). Looking at the results under the no-profit scenario, for example, excluding imports yields an estimated ϵ_K of 0.3703. Including imports gives the baseline result of 0.3686. Thus excluding imports gives an estimate that is 0.0018 higher. Reading down column (3) of Table A.10, one can see that the differences can reach as large as 0.0097, but average only about 0.0044. Even in the no-profit case, excluding imports does not alter the estimated elasticity by a substantial amount.

This appears similar in the other scenarios. Table A.10 shows that under the depreciation cost scenario the average difference is only 0.0012. Table A.11 shows that the average differences in

the investment cost scenario are only 0.0009, and under the user cost scenario only 0.0021. There are cases of positive and negative differences, but the maximum difference is under 0.0066. Again, there does not appear to be substantial differences because of the inclusion of imports.

A.7 Comparing elasticities and cost ratios

Comparing the cost share, s_{Kt}^{Cost} , to the elasticity, ϵ_{Kt} , as in Section 5.2, shows that s_{Kt}^{Cost} tends to be lower than ϵ_{Kt} in the scenarios where positive profits are allowed (the labor cost share tends to be higher than the labor elasticity). Here I provide some examples and a more thorough theoretical breakdown of how and why this occurs.

A.7.1 A simple example

To set ideas, consider the following very simple economy. There are two industries. One produces final goods, Y , and the other produces an intermediate input, X , used by the first industry. Both industries use capital and labor in production.

$$Y = K^{\alpha_K} L^{\alpha_L} X^{\alpha_X} \quad (\text{A.7})$$

$$X = K^{\beta_K} L^{\beta_L}. \quad (\text{A.8})$$

In both industries, the coefficients sum to one for constant returns to scale.

From a purely technical standpoint, one can solve for

$$Y = K^{\alpha_K + \alpha_X \beta_K} L^{\alpha_L + \alpha_X \beta_L} \quad (\text{A.9})$$

as the aggregate production function for final goods. It is straightforward to confirm that this is constant returns to scale as well, so that $\alpha_K + \alpha_X \beta_K + \alpha_L + \alpha_X \beta_L = 1$. Most notably, this shows directly that the elasticity of final goods with respect to the inputs are

$$\epsilon_K = \alpha_K + \alpha_X \beta_K \quad (\text{A.10})$$

$$\epsilon_L = \alpha_L + \alpha_X \beta_L. \quad (\text{A.11})$$

The aggregate elasticities “nest” the production structure of the economy by incorporating the capital and labor elasticity of the intermediate input provider.

Assume that the final goods industry charges a markup of μ_Y , and the intermediate industry a markup of μ_X , and that the final good is the numeraire. Then for a given amount of final purchases Y , the final good industry will spend Y/μ_Y on inputs (capital, labor, the intermediate). In particular, it will spend $\alpha_K Y/\mu_Y$ on capital, $\alpha_L Y/\mu_Y$ on labor, and $\alpha_X Y/\mu_Y$ on intermediates.

The value $\alpha_X Y / \mu_Y$ forms the revenue of the intermediate good industry. The intermediate industry will spend $\alpha_X Y / \mu_Y \mu_X$ on inputs (capital and labor, and they do not use other intermediates). Here one can see the multiple marginalization that will play a role in generating a difference between factor cost shares and elasticities. The intermediate industry thus spends $\beta_K \alpha_X Y / \mu_Y \mu_X$ on capital, and $\beta_L \alpha_X Y / \mu_Y \mu_X$ on labor.

This is enough information to form the factor cost shares in this economy.

$$s_K^{Cost} = \frac{\alpha_K + \alpha_X \beta_K / \mu_X}{\alpha_K + \alpha_X \beta_K / \mu_X + \alpha_L + \alpha_X \beta_L / \mu_X} \quad (\text{A.12})$$

$$s_L^{Cost} = \frac{\alpha_L + \alpha_X \beta_L / \mu_X}{\alpha_K + \alpha_X \beta_K / \mu_X + \alpha_L + \alpha_X \beta_L / \mu_X} \quad (\text{A.13})$$

In both cases, these are not equal to the respective elasticities because of the presence of μ_X . The value of μ_Y drops out here because Y is not used as an intermediate by another industry. If $\mu_X = 1$ the denominator is equal to one in both expressions, and the cost shares equal the elasticities exactly.

From the economy's perspective, it would be efficient to spend a fraction $\alpha_K + \alpha_X \beta_K$ of its costs on capital, as that equals the aggregate elasticity of final goods with respect to capital. But the presence of μ_X distorts that because of the input/output relationships, even though both industries practice cost minimization. Of the total costs the final goods industry incurs, it spends α_K of those costs on capital. It then spends α_X of its total costs on the intermediate good. But the intermediate producer only spends α_X / μ_X on costs of production, keeping the rest as economic profit. Cost-minimizing, it spends β_K of the α_X / μ_X on capital. The same issue occurs with labor, and it spends too little (from the economy's perspective) on both inputs.

Whether this leads s_K^{Cost} to be bigger or smaller than ϵ_K depends on the relative size of the capital coefficients in the two industries. If $\alpha_K < \beta_K$, the markup of $\mu_X > 1$ results in $s_K^{Cost} < \epsilon_K$. The markup in the intermediate industry means less spending is done on factors in the intermediate industry, and so the cost share is skewed towards the cost share of the final good industry. With $\alpha_K < \beta_K$, that skew results in $s_K^{Cost} < \epsilon_K$ (and by definition would make $s_L^{Cost} > \epsilon_L$). This is what was seen in the main paper Figure 3, and the larger the markups the larger the difference between s_K^{Cost} and ϵ_K .

It is the presence of markups along the supply chain that distort the use of factors away from the efficient allocation, and generate the wedge between the factor cost shares and the elasticities.

A.7.2 Full theory

This section shows in an economy with J industries and an arbitrary network of I/O relationships, with an arbitrary set of markups, how the factor cost shares and elasticities differ.

To help in the exposition, take the matrix Λ from the main text equation (6) and split it into

four blocks

$$\Lambda' = \begin{bmatrix} L & \mathbf{0} \\ W & \mathbf{0} \end{bmatrix} \quad (\text{A.14})$$

where note that this is the transpose of Λ , purely for ease in showing results. The upper-left block L is the $J \times J$ matrix with entries λ_{ij} , the cost to industry j (the column) of intermediate good i (the row) as a share of total costs in industry j .

W is the $2 \times J$ matrix with columns λ_K and λ_L . $\lambda'_K = [\lambda_{K1}, \lambda_{K2}, \dots, \lambda_{KJ}]$, the vector of capital as a share of total costs in each industry, and λ_L is defined similarly for labor as a share of total costs. One could readily extend this to allow for n factors of production. The top right block of Λ' is a $J \times 2$ block of zeroes, and the bottom right block is a 2×2 block of zeroes.

Define a “technical requirement” matrix R as follows

$$R = (I - L)^{-1}, \quad (\text{A.15})$$

where I is $J \times J$ identity matrix. R is like a traditional Leontief inverse, but is based on intermediates as a share of total *costs*, as opposed to a share of total revenues. An element in R , r_{ij} , shows the elasticity of output in industry j (the column) with respect to output in industry i (the row).

Next, define the vector $J \times 1$ vector F to contain the elements f_j , the final use of industry j . Defining e_J as a $J \times 1$ vector of ones, this means that total final use is $e'_J F$. The γ_j terms from the main text - shares of final use - are $\gamma_j = f_j(e'_J F)^{-1}$, and the $J \times 1$ vector Γ from equation (8) is $\Gamma' = [F'(e'_J F)^{-1} \mathbf{0}]$ where there is a block of 2 trailing zeros to account for the final use of capital and labor.

As in equation (9) of the main text, the vector of elasticities E is formed by $E = \Gamma'(I - \Lambda)^{-1}$. Some tedious but straightforward matrix algebra demonstrates that the two factor elasticities in E can be written as

$$[\epsilon_K \ \epsilon_L] = WRF(e'_J F)^{-1}. \quad (\text{A.16})$$

Focusing exclusively on the elasticity with respect to capital, this is

$$\epsilon_K = \lambda'_K RF(e'_J F)^{-1}. \quad (\text{A.17})$$

The aggregate elasticity with respect to capital is the vector of industry-specific capital shares (λ_K) multiplied through by R , the technical requirements matrix, to get the “full” elasticity of each industry with respect to capital, taking into account the effect of an increase in capital in suppliers of intermediates to that industry. Those industry-specific elasticities are then weighted by the shares of final use $F(e'_J F)^{-1}$ to produce the elasticity.

Now, turn to the calculation of capital’s share of factor costs, s_K^{Costs} (it is straightforward to do this for labor as well). To do this, several additional pieces of information are needed. First, let μ_j

be the gross output markup for industry j , and let M be the $J \times J$ diagonal matrix with entries μ_j along the diagonal and zeroes elsewhere. Define X as the $J \times 1$ vector of gross output, with entry X_j denoting gross output of industry j .

Define the “total requirement” matrix T as follows

$$T = (I - M^{-1}L)^{-1} \quad (\text{A.18})$$

which is a more traditional Leontief inverse. $M^{-1}L$ gives costs of intermediates as a share of revenues (not total costs). The typical entry in T shows the dollars of revenue (inclusive of markups) created in industry i (the row) for each dollar of final use in industry j (the column), taking into account the input/output relationships among firms.

Total spending on capital in the economy is

$$\sum_{j \in J} COST_{Kj} = \lambda'_K M^{-1}TF. \quad (\text{A.19})$$

Working backwards, TF multiplies the total requirement matrix by the measure of final use, and gives a $J \times 1$ vector of total revenue in each industry. Pre-multiplying that by M^{-1} is essentially dividing each of those measures of revenue by the respective markup, and hence $M^{-1}TF$ are total costs in each industry. Pre-multiplying that by λ'_K yields the total *capital* costs across the whole economy.

Capital's share of factor costs is capital costs divided by total factor costs. Total factor costs are

$$\sum_{j \in J} (COST_{Kj} + COST_{Lj}) = e'_J R^{-1} M^{-1}TF. \quad (\text{A.20})$$

The interpretation of $M^{-1}TF$ is the same as in the above paragraph, total costs in each industry. $e'_J R^{-1}$ is a $1 \times J$ vector of the share of all factor costs in total costs by industry. Hence $e'_J R^{-1} M^{-1}TF$ are the total factor costs across all industries. The structure of $e'_J R^{-1}$ is

$$e'_J R^{-1} = \begin{bmatrix} 1 - \sum_{i \in J} \lambda_{i1} & 1 - \sum_{i \in J} \lambda_{i2} & \dots & 1 - \sum_{i \in J} \lambda_{iJ} \end{bmatrix} \quad (\text{A.21})$$

and given constant returns to scale it would hold that $1 - \sum_{i \in J} \lambda_{ij} = \lambda_{Kj} + \lambda_{Lj}$.

Combining information, we have an ability to measure both ϵ_K and s_K^{Cost} .

$$\epsilon_K = \lambda'_K R F (e'_J F)^{-1} \quad (\text{A.22})$$

$$s_K^{Cost} = \lambda'_K M^{-1}TF (e'_J R^{-1} M^{-1}TF)^{-1}. \quad (\text{A.23})$$

From here, it is possible to see why and how these two measures would differ. Mechanically, these two measures are only equal if $R = M^{-1}T$, as can be seen by examining the two equations above.

This holds only if $I = M$. In other words, $\epsilon_K = s_K^{Cost}$ only if all markups are equal to one (as in the no-profit scenario). Any markups greater than one across industries create a wedge in between ϵ_K and s_K^{Cost} .

There are two different ways in which markups create a wedge between ϵ_K and s_K^{Cost} . First are the direct effects of M^{-1} . TF determines total gross output by industry (the total requirements matrix times final use), and $M^{-1}TF$ determines gross costs by industry. If there is dispersion in the μ_j terms that make up M , then the allocation of gross costs across industries does not match the allocation of gross output. Costs are thus skewed towards industries with low markups, and thus s_K^{Cost} will be skewed towards the capital share of factor costs in those industries. Note that if all markups are identical but above one, $\mu_j = \bar{\mu} > 1$, then the two M^{-1} terms still cancel out. That is, if markups are identical across industries then there is no distortion in the allocation of gross costs across industries due to distortions in final demand.

Second, markups generate a difference between R and T , the technical and total requirement matrices. These differ because markups create distortions in costs across industries due to the markup charged by all suppliers along the supply chain. This distortion holds even if all the markups are identical across industries, $T = (I - \bar{\mu}L)^{-1} \neq (I - L)^{-1} = R$. Markups distort the allocation of costs, as each upstream industry spends less on factors (and further inputs) than it receives in payments from downstream industries.

Whether s_K^{Cost} is larger or smaller than ϵ_K depends on how markups correlate with λ_K . If μ_j and λ_{Kj} are positively correlated, then $s_K^{Cost} < \epsilon_K$. Higher markups skew costs away from those industries with large λ_{Kj} values, and hence s_K^{Cost} is driven down because more costs are coming from industries that spend low shares of their costs on capital. Further, if λ_{Kj} tend to be higher in industries that are more upstream, then markups along the supply chain will lower the share of costs in those industries, and this will also drive down s_K^{Cost} .

A.7.3 Empirical Relationships

The prior sub-section proposes two relationships that explain why $\epsilon_K > s_K^{Cost}$ in economies with positive economic profits: markups μ_j are positively associated with capital as a share of costs across industries, and capital as a share of costs is higher in industries that are more upstream. Here I show that the industry/year data is consistent with both proposed explanations.

For each industry I can calculate the gross output markup μ_{jt} as gross output of j in time t divided by total costs (capital, labor, and intermediate inputs). I also calculate capital's share of factor costs in each industry, $s_{Kj}^{Cost} = COST_{Kjt} / (COST_{Kjt} + COST_{Ljt})$. For both μ_{jt} and s_{Kj}^{Cost} I do this under the depreciation cost assumption on capital costs. The results are similar using either the investment cost or user cost assumption.

In Figure A.2 I plot the relationship between s_{Kj}^{Cost} and μ_{jt} , controlling for year fixed effects. As there are a total of 4,477 industry/year observations, the Figure plots the “binned” relationship

by collecting observations into 100 quantiles.¹ The overall positive relationship is apparent and is statistically significant (point estimate 0.407, standard error 0.009) even though there are obvious fluctuations in the relationship. The quantiles with the largest markups (which make up about 2% of the observations) tend to be for housing and real estate. Removing those from the relationship still shows a significant positive relationship.

Next, I calculate a measure of how “upstream” each industry is, u_{jt} . This is defined as $u_{jt} = 1 - f_{jt}/GO_{jt}$, where f_{jt} is final use of industry j at time t , and GO_{jt} is gross output. u_{jt} is the share of gross output that is used by other industries as an intermediate input, as opposed to being for final use. High values of u_{jt} indicate an industry that is “upstream” in the sense of supplying many intermediates relative to its final use.

Figure A.3 plots the relationship of s_{Kj}^{Cost} to u_{jt} , controlling for year fixed effects, and again using 100 quantiles to clarify the relationship. Here the positive relationship is apparent, with a point estimate of 0.065 and a standard error of 0.007. In the Figure one can see that for some industries u_{jt} is above one, indicating that intermediate use is greater than gross output (and that final use was negative). These industry/year observations represent situations where there were significant imports of products from that industry, and these observations (about 1% of the total) tend to be for the mining and extractive industries (e.g. oil). Excluding these does not change the overall positive relationship. Again, the relationship in Figure A.3 is consistent with the logic from the prior sub-section that $\epsilon_K > s_K^{Cost}$ when capital costs as a share of factor costs tend to be large for industries that are more upstream (and subject to more layers of markups).

A.8 Markups and profit shares

This section provides equations for exactly how the gross output markup, value-added markup, gross output profit share, and value-added profit share are calculated and related in theory.

As in the main text, I defined

$$\mu_t^{GO} = \frac{\sum_{j=1}^J GO_{jt}}{\sum_{j=1}^J COST_{jMt} + COST_{jKt} + COST_{jLt}}. \quad (\text{A.24})$$

To simplify terms, let $GO_t = \sum_{j=1}^J GO_{jt}$ be total gross output, so that

$$\mu_t^{GO} = \frac{GO_t}{COST_{Mt} + COST_{Kt} + COST_{Lt}} \quad (\text{A.25})$$

where the terms in the denominator are similarly defined to be sums across all industries.

¹The “binscatter” technique of displaying regression results for large-N datasets was developed in [Chetty, Friedman and Saez \(2013\)](#).

Let the value-added markup be

$$\mu_t^{VA} = \frac{VA_t}{COST_{Kt} + COST_{Lt}} = \frac{GO_t - COST_{Mt}}{COST_{Kt} + COST_{Lt}}. \quad (\text{A.26})$$

Both μ_t^{GO} and μ_t^{VA} can be calculated directly from the industry-level data given the observed values for gross output, value-added, cost of intermediates, costs of labor, and the costs of capital (which depend on the choice of method for estimating that: depreciation costs, no-profits, etc.). These two markups are related as follows,

$$\mu_t^{VA} = \frac{\mu_t^{GO}(1 - COST_{Mt}/GO_t)}{1 - \mu_t^{GO}COST_{Mt}/GO_t}. \quad (\text{A.27})$$

As can be seen here, the distinction between the two measures of markups is the size of the ratio $COST_{Mt}/GO_t$, or the share of intermediates in gross output. Based on the data in this paper, that ratio runs around 0.52 to 0.56 throughout the period 1948-2018.

The profit share of gross output is

$$\pi_t^{GO} = \frac{(\mu_t^{GO} - 1)(COST_{Mt} + COST_{Kt} + COST_{Lt})}{GO_t} = 1 - \frac{1}{\mu_t^{GO}} \quad (\text{A.28})$$

and the profit share of value-added is

$$\pi_t^{VA} = \frac{(\mu_t^{GO} - 1)(COST_{Mt} + COST_{Kt} + COST_{Lt})}{VA_t} = \frac{\mu_t^{GO} - 1}{\mu_t^{GO} - COST_{Mt}/GO_t}. \quad (\text{A.29})$$

Figure 5 in the main paper plots series μ_t^{GO} under different capital cost assumptions. In this Appendix, Figure A.4 plots μ_t^{VA} under those same scenarios, and Figure A.5 plots π_t^{VA} under the same scenarios.

A.9 User cost details

As described in the text, one of the alternative series used for estimating ϵ_{Kt} involves a user cost formula, as in Hall and Jorgenson (1967), and similar to what is used in Barkai (2017); Rognlie (2015). This appendix section provides more detail on the construction of those user costs of capital.

The cost of capital is, replicating the equation from the main text,

$$COST_{iKt}^{User} = \sum_{j \in \{st, eq, ip\}} K_{ijt} R_{ijt}. \quad (\text{A.30})$$

where there are three types of capital j for each industry i at time t . The stock, K_{ijt} , comes from the BEA (U.S Bureau of Economic Analysis, 2020b,c). The rate of return for each industry/capital

type/time, R_{ijt} is calculated according to the following formula, also from the main text.

$$R_{ijt} = (Int_{it} - E[\pi_{ijt}] + \delta_{ijt}) \frac{1 - z_{jt}\tau_t}{1 - \tau_t} \quad (\text{A.31})$$

A.9.1 Nominal interest rate

The nominal rate Int_{it} is industry/time specific, but not specific to the type of capital. Hence I assume that within each industry all capital is financed at the same nominal rate.

That nominal rate is a combination of several nominal rates, which can vary by the type of financing.

$$Int_{it} = \sum_m s_{imt} Int_{mt} \quad (\text{A.32})$$

where m is the type of financing, and s_{imt} is the share of financing of type m used by industry i at time t . Int_{mt} is the nominal interest rate of asset type m . Hence the industry-specific nature of the nominal interest rate comes from its mix of financing across types, but each industry faces the same nominal rate on a given financing type. For example, all corporate AAA bonds are assumed to have the same rate (Int_{mt}), but industries vary in what share of their financing (s_{imt}) comes from corporate AAA bonds.

The financing types m used are 10-year Treasury bonds, municipal bonds, corporate AAA bonds, corporate Baa bonds, 30-year mortgage rate, Fed Funds rate, the 10-year Treasury plus the S&P 500 dividend rate as a proxy for equity returns ([Board of Governors of the Federal Reserve System, 2020](#); [Freddie Mac, 2020](#); [Moody's, 2020](#)).

For private industries, I use the integrated macroeconomic accounts of the U.S. ([U.S Bureau of Economic Analysis, 2020a](#)) to find industry-level balances of liabilities from corporate bonds, corporate paper, loans, and equity. Specifically, I use Table S.5.a-A (annual totals). Corporate paper is series FL103169100, corporate bonds are series FL103163003, loans are series FL104123005, and equity is series FL103181005. I sum these four liabilities, and then form shares s_{imt} by dividing the specific liability by this total. Note that these shares are common to all private industries. The distinction across industries i will come as a difference between private industries, housing, and government.

One note is that the integrated account only begin in 1960. I extrapolate values for 1948-1959 by taking the average shares s_{imt} for 1960-1969, and using those for each year 1948-1959. I am thus assuming that the structure of private business financing was the same 1948-1959.

For any federal government industry, I assume all financing is coming from 10-year Treasury bonds, so that $s_{Fed,T-bond,t} = 1$ for federal industries, and zero for all other kinds of financing. For state and local government, all financing is assumed to come from municipal bonds, or $s_{SL,Muni,t} = 1$ and zero on all other sources. For housing I assume all financing comes from 30-year mortgages, or

$s_{HS,Mort,t} = 1$ and all other sources are zero.

The actual nominal interest on each source of financing, Int_{mt} , are drawn from several sources (Board of Governors of the Federal Reserve System, 2020; Freddie Mac, 2020; Moody's, 2020; National Bureau of Economic Research, 2020). A single rate for each year is obtained.

- The corporate bond rate is equal to the first observation of Moody's AAA rate in a given year, retrieved from FRED
- The corporate paper rate is set equal to the first observation of the Fed Funds rate in a given year, retrieved from FRED
- The loan rate is set equal to the first observation of the Moody's Baa rate in a given year, retrieved from FRED.
- The equity rate is set equal to the first observation of the 10-year Treasury bond rate in a given year, retrieved from FRED, plus the S&P 500 dividend yield, also obtained from FRED.
- The 10-year Treasury rate is equal to the first observation of the 10-year Treasury bond rate in a given year, retrieved from FRED, for 1953-2018. For 1948-1953, the historical series of federal bond yields from the NBER is used.
- The municipal bond rate is equal to the first observation of the corporate Baa rate in a given year, retrieved from FRED, minus two percentage points
- The 30-year mortgage rate is equal to the first observation of the mortgage rate in a given year, obtained from FRED for 1971-2018. This is combined with historical mortgage rates from the NBER for 1949-1965. Rates from 1966-1970 are imputed from the prime lending rate (obtained from FRED) plus 1 percentage point. The rate for 1948 is set to 4.32 percent, identical to the rate for 1949.

A.9.2 Expected inflation

The second term in the user cost formula is $E[\pi_{ijt}]$, meaning there is an expected inflation for industry i on capital type j at time t . From the BEA capital stock data (U.S Bureau of Economic Analysis, 2020b) I obtain a price index for each capital type j in each industry i at time t . For the basic user cost formula, I calculate actual inflation in period t , and set $E[\pi_{ijt}] = \pi_{ijt}$.

A.9.3 Depreciation

BEA capital stock data (U.S Bureau of Economic Analysis, 2020b) includes an amount of depreciation by capital type j for industry i at time t , $DEPR_{ijt}$. In addition I have the capital stock of type j for industry i at time t , K_{ijt} , from the same source. The depreciation rate in the user cost formula is found as $\delta_{ijt} = DEPR_{ijt}/K_{ijt}$.

A.9.4 Depreciation allowance

The user cost formula contains an adjustment for depreciation allowance in the tax code by capital type, z_{jt} . Data from [Horvát and Webb \(2020\)](#) contains information on this allowance by country, and I use the U.S. values here. The data runs only from 1979-2012, and for 2018. For 2013-2017, I use the 2012 value for each capital type: 0.35 for structures, 0.63 for intellectual property, and 0.877 for equipment. Prior to 1979, I use a value of 0.561 for structures (matching the 1979 value), 0.98 for equipment (matching the 1979 value), and 0 for intellectual property (matching the 1979 value).

A.9.5 Corporate tax rate

The corporate tax rate is assumed to be the same across industries, but can vary with time, τ_t . The only deviation is that the federal and state/local government industries are assumed to face a zero tax rate. I find the effective corporate tax rate by using aggregate profits after tax (*After*), and aggregate profits before (*Before*) tax, and setting $\tau_t = (Before - After)/Before$.

A.10 Series breaks at matching

As noted in the main text, and summarized in Table [A.2](#), the sources used differ across time periods. It is possible that the estimates of ϵ_{Kt} differ over time based simply on the matching process or vintage of data.

Figure [A.6](#) shows the baseline results, with vertical lines indicating the break in data series. For the 1962-63 and 1986-87 breaks there is no apparent shift in the estimates. For 1996-97, one can see that each individual series appears higher in 1997 than in 1996. It is possible that the results for the 1997-2018 period are shifted up relative to earlier values due to the change in number of industries reported by the BEA and/or the change in source of value-added components from the SIC-reported data that I match to the I/O tables to direct NAICS-matched data.

Across the four different series, the increase from 1996 to 1997 in the estimated ϵ_{Kt} is approximately 0.02. One could assert that with better data, the 1948-1996 estimates would be approximately 0.02 higher, leaving the upper bound just over 0.33. This does not appear to change the general conclusions presented in the paper.

A.11 Housing and government

In section 6.1 I calculate ϵ_{Kt} for the private business sector, which excludes owner-occupied housing and government industries. In this appendix I show summary statistics on the cost shares of those

industries, which helps to illustrate why they (and housing in particular) pull the elasticity estimate up so much when included.

Panel A of Table A.12 shows the ratios s_{Kt}^{COST} and s_{Kt}^{VA} for owner-occupied housing. The cost ratio for capital is 0.942 on average under the no-profit assumption, and is 0.797 even in the depreciation only assumption. The capital cost share of housing is massive compared to any other industry, and hence when housing is included, as in the baseline estimates of ϵ_{Kt} , this elasticity is larger. Once housing is excluded, the estimate of ϵ_{Kt} falls, even absent any input-output relationships.

In comparison the government industries, as a whole, have cost shares that are similar to the overall economy, and hence their inclusion or exclusion has little impact on the overall estimate of ϵ_{Kt} . Government does display one curious aspect to the cost shares, however. Note that both s_{Kt}^{COST} and s_{Kt}^{VA} are smaller under the no-profit scenario than in the other scenarios. For example, the mean factor cost share under no-profits in government is 0.197, while under the depreciation assumption it is 0.221. This occurs because for many years government industries list labor compensation as *larger* than their value-added, implying negative capital costs in the no-profit assumption.

More broadly, the proper measurement of capital costs for government is open to question. The BEA presumes that capital costs for government are equal to depreciation only, and adds that to labor compensation costs to find government value-added. Hence the BEA presumes that capital costs for government have no opportunity cost, simply depreciation. Because of this, the “no-profit” and “depreciation only” capital costs are identical for the government industry. In practice this acts to squeeze the bounds together for the aggregate ϵ_{Kt} , although the quantitative effect of this is small (note that the gap between the bounds is similar in the private business sector that excludes government).

When I do the user cost calculation of capital costs, for government I apply the same formula as for other industries, assuming that they pay either municipal bond rates (state/local) or 10-year Treasury rates (federal) as their nominal cost, as described in A.9. Assuming government treats capital decisions similar to private industries may not be reasonable. An alternative is to leave government capital costs equal to depreciation only, but to apply the user cost formula to all private industries.

Figure A.7 plots two estimates of ϵ_{Kt} . The dark dashed line is the baseline user cost estimate, where government capital costs are calculated with the user cost formula described in Section A.9. The gray dashed line is the alternative where user costs are used for all private industries, but government capital costs are set equal to depreciation only. As can be seen, these two series are very similar. The only notable deviation is in the early 1980s, where the implied elasticity is somewhat lower when government is assumed to have depreciation costs. This occurs because the user costs for government in those years are presumed to be quite high due to high Treasury bond rates.

A.12 De-capitalizing IP

In section 6.2 of the main paper I calculate ϵ_{Kt} estimates after de-capitalizing intellectual property from the national accounts, as in [Koh, Santaaulàlia-Llopis and Zheng \(2020\)](#). The details of that de-capitalizing process are as follows.

For each industry i , value-added without IP is $VALU_{it}^{NoIP} = VALU_{it} - INV_{i,IP,t}$, where $INV_{i,IP,t}$ is own-account investment spending on IP. Second, total investment by industry i is set to $INV_{it}^{NoIP} = INV_{it} - INV_{i,IP,t}$. Third, total depreciation by industry i is set to $DEPR_{it}^{IP} = DEPR_{it} - DEPR_{i,IP,t}$. Finally, the stock of capital in industry i is set to $K_{it}^{NoIP} = K_{it} - K_{i,IP,t}$.

What these adjustments do not account for are IP products that are purchased from other industries. In the national aggregates, [Koh, Santaaulàlia-Llopis and Zheng \(2020\)](#) have information on total flows of these purchases, and can make adjustments for it. In the input/output accounts at the industry level, there is no information on these flows, and so there is no way to make this adjustment. Thus my de-capitalization process is not complete, and I am understating the effect of de-capitalization on the elasticity estimates.

A.13 Allowing for negative costs

For some industry/year observations, the amount of labor compensation is larger than reported value-added. In the no-profit scenario, capital costs are equal to value-added minus labor compensation, and hence capital costs in these cases are negative. In the baseline calculations of the paper, I allow such negative capital costs in the industry-year. These negative costs assert that the sum of factor costs in the no-profit scenario does not add up to more than value added in an industry.

An alternative is to allow the combined cost of capital and labor to be larger than value-added, and avoid negative costs. In this case I would set capital costs set to zero if labor compensation is reported higher than value-added. As this changes the distribution of costs across factors, it would change the estimated elasticities. To see whether the baseline assumption allowing negative costs is driving the no-profit results, I re-estimated the elasticities with the constraint $COST_{Kit} \geq 0$ and $COST_{Lit} \leq VALU_{it}$.

Figure [A.8](#) plots the bounds from the baseline (dark lines) allowing for negative costs, and the bounds in the alternative (gray lines) where negative costs are not allowed in the no-profit scenario. As can be seen, there is essentially no difference in the two series.

For the other capital cost assumptions, this issue does not arise. For depreciation costs, investment costs, and user costs, the capital costs are separately estimated, and do not rely on the difference between value-added and labor compensation.

A.14 Annual estimates of elasticities

Tables A.14-A.14 show annual estimates of the four elasticities (labor, structures, equipment, and IP) under the baseline assumptions made in the main text. In particular, estimates are made splitting proprietors income according to Gomme and Rupert (2004), with all industries included, and with intellectual capital included in the capital stock. The four Tables differ in the assumption used to calculate capital costs: no-profit, depreciation cost, investment cost, and user cost.

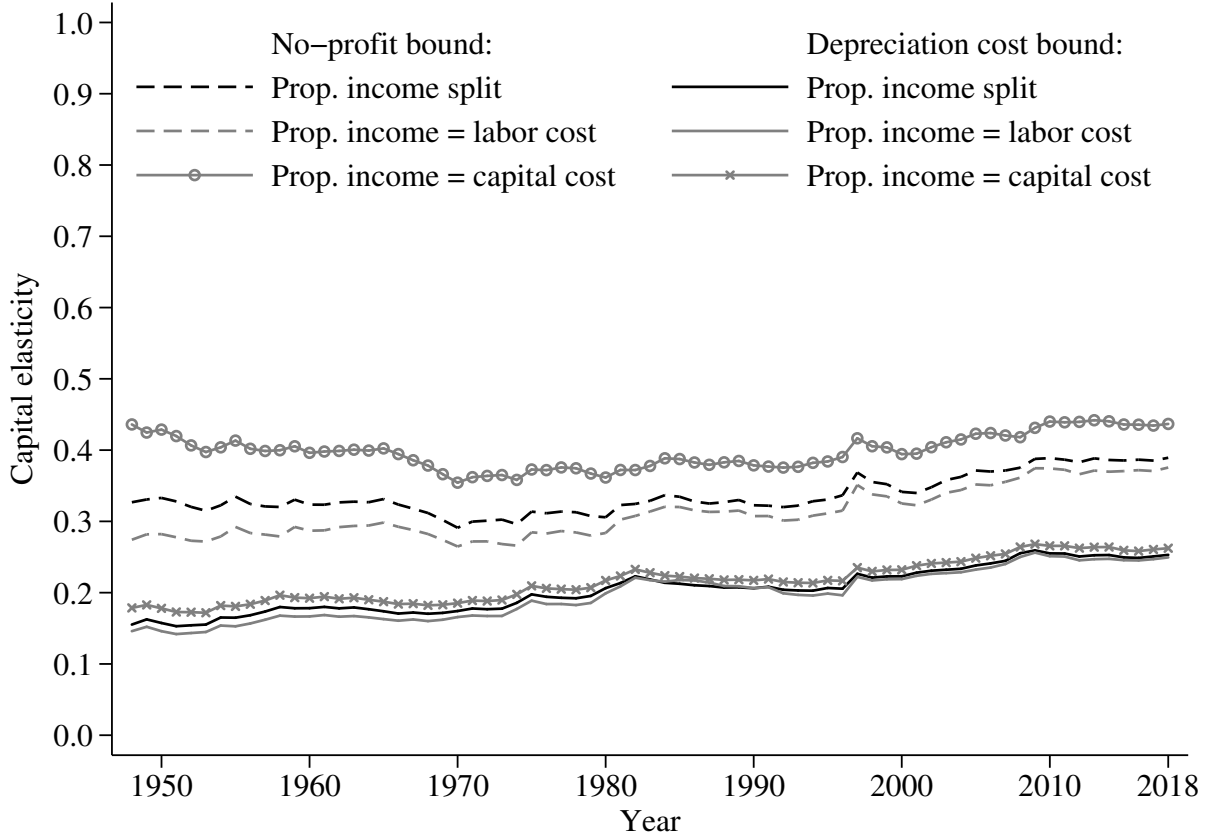
References

- Barkai, Simcha.** 2017. “Declining labor and capital shares.” Stigler Center for the Study of the Economy and the State.
- Board of Governors of the Federal Reserve System.** 2020. “Table H.15 Selected Interest Rates.” Retrieved from FRED, Federal Reserve Bank of St. Louis, <https://fred.stlouisfed.org/>.
- Chetty, Raj, John N. Friedman, and Emmanuel Saez.** 2013. “Using Differences in Knowledge across Neighborhoods to Uncover the Impacts of the EITC on Earnings.” *American Economic Review*, 103(7): 2683–2721.
- Freddie Mac.** 2020. “30-year Fixed Rate Mortgage Average in the U.S.” Retrived from FRED, Federal Reserve Bank of St. Louis, <https://fred.stlouisfed.org>.
- Gomme, Paul, and Peter Rupert.** 2004. “Measuring labors share of income.” Federal Reserve Bank of Cleveland Policy Discussion Papers Nov.
- Hall, Robert E, and Dale W. Jorgenson.** 1967. “Tax Policy and Investment Behavior.” *American Economic Review*, 57.
- Horvát, Peter, and Colin Webb.** 2020. “The OECD STAN Database for industrial analysis.” <https://www.oecd-ilibrary.org/content/paper/ece98fd3-en>.
- Koh, Dongya, Raül Santaeulàlia-Llopis, and Yu Zheng.** 2020. “Labor Share Decline and Intellectual Property Products Capital.” *Econometrica*, 88(6): 2609–2628.
- Moody’s.** 2020. “Moody’s AAA and Baa corporate bond rates.” Retrieved from FRED, Federal Reserve Bank of St. Louis, <https://fred.stlouisfed.org/series>.
- National Bureau of Economic Research.** 2020. “Historical Mortgage and Treasury Yields.” Retrieved from Macrohistory Database <https://www.nber.org/research/data/nber-macrohistory-database>.
- Rognlie, Matthew.** 2015. “Deciphering the Fall and Rise in the Net Capital Share: Accumulation or Scarcity?” *Brookings Papers on Economic Activity*, 46(1 (Spring): 1–69.
- U.S Bureau of Economic Analysis.** 2020a. “Integrated Macroeconomic Accounts.” Retrieved October, 2020 from https://apps.bea.gov/national/nipaweb/Ni_FedBeaSna/SS_Data/Section1All_xls.xlsx.

U.S Bureau of Economic Analysis. 2020*b*. “Section 3 Private Fixed Assets by Industry.” Retrieved October, 2020 from https://apps.bea.gov/national/FixedAssets/Release/XLS/Section3All_xls.xlsx.

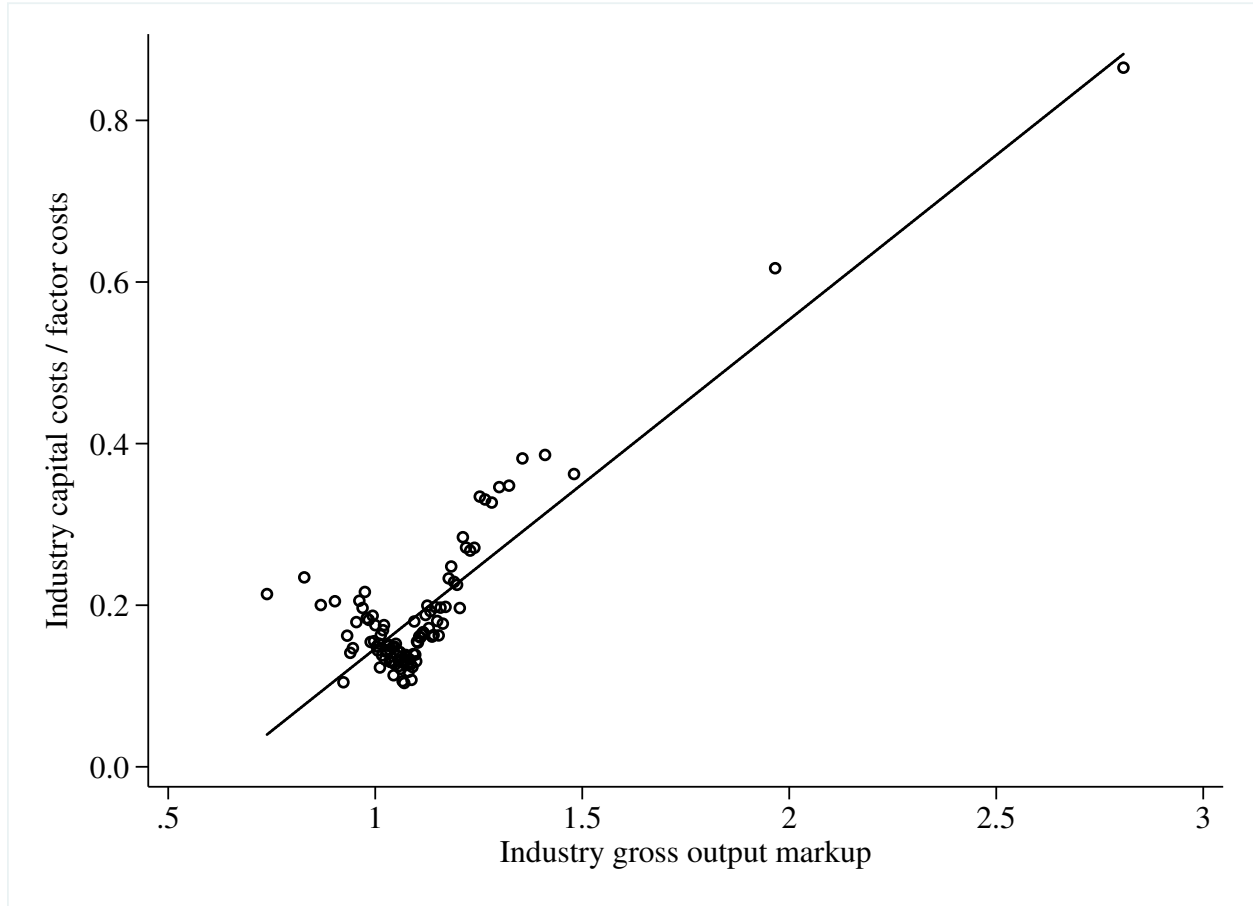
U.S Bureau of Economic Analysis. 2020*c*. “Section 7 Government Fixed Assets.” Retrieved October, 2020 from https://apps.bea.gov/national/FixedAssets/Release/XLS/Section7All_xls.xlsx.

Figure A.1: Estimates of capital elasticity, different proprietors income assumptions



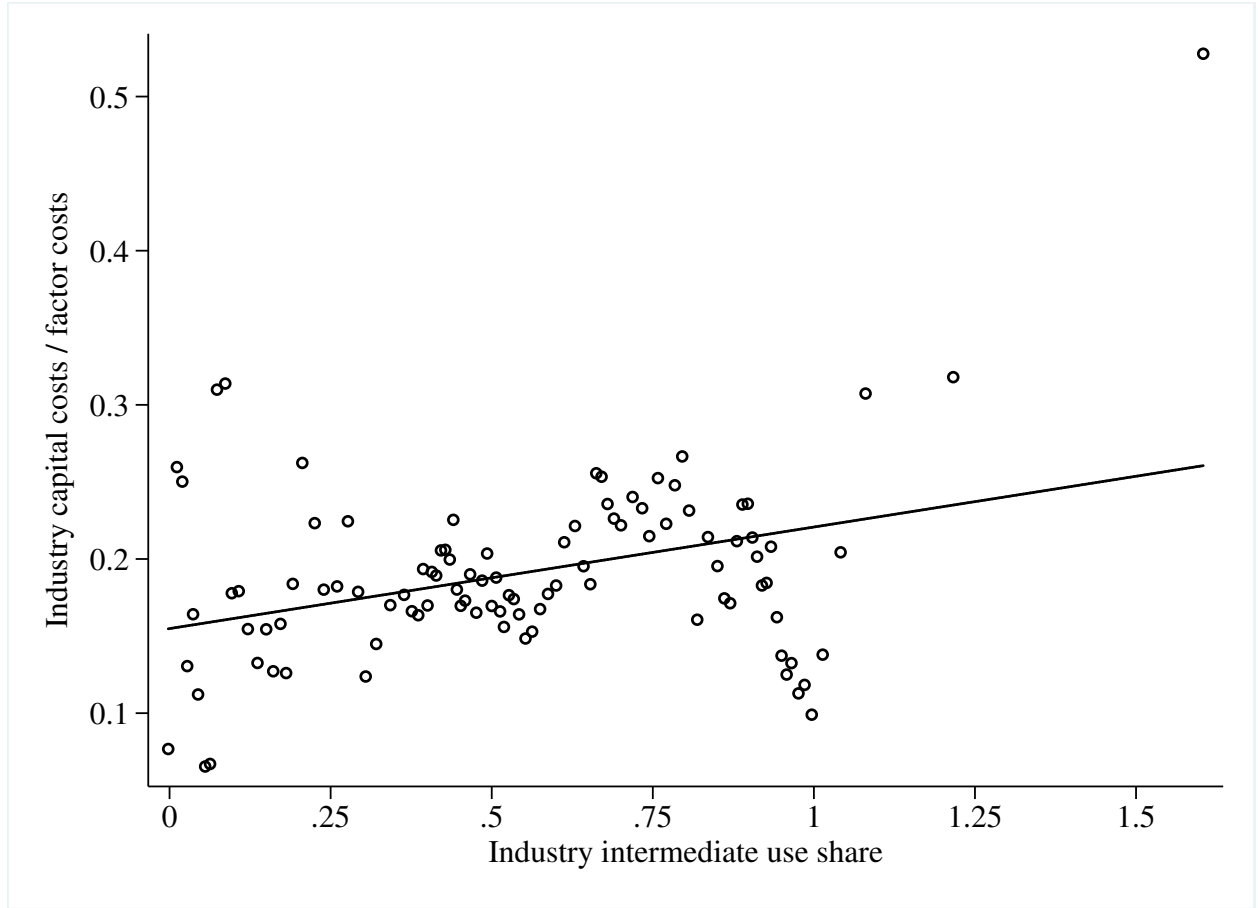
Notes: The estimate of the capital elasticity ϵ_{Kit} , is made using equation (9) in the main text. The no-profit upper bounds differ by the assumption about proprietors income. The baseline is “split” where proprietors income is split between labor and capital costs according to equation (13) in the main text. “Labor cost” means all proprietors income is assumed to be a labor cost, and “capital cost” means all proprietors income is assumed to be a capital cost. The same distinctions apply to the depreciation-only lower bounds.

Figure A.2: Relationship of capital cost share to markup across industries



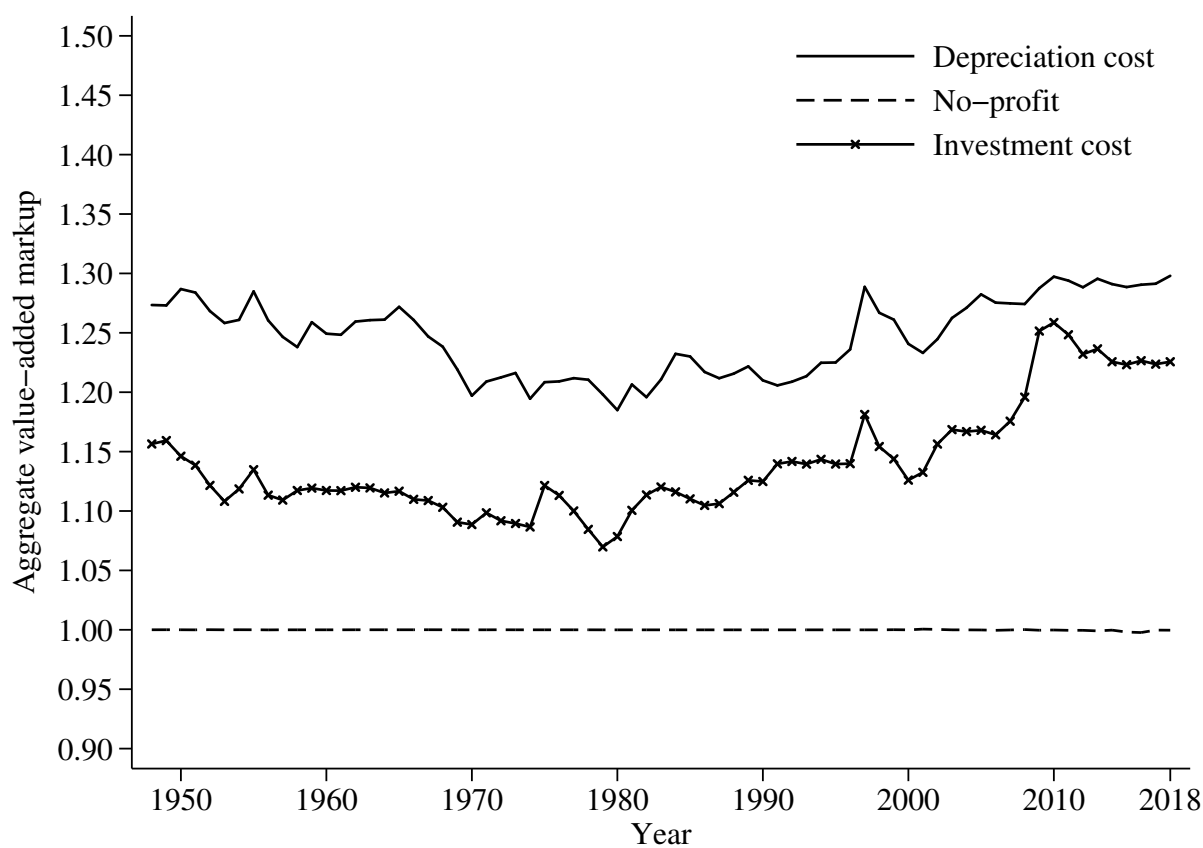
Notes: This shows the “binscatter” relationship of industry/year observations of capital shares of factor costs, s_{Kjt}^{Cost} , to the industry/year gross output markup, μ_{jt} . Both are calculated using the depreciation cost assumption on capital costs, and are described in more detail in the text. The estimated relationship between the two in the Figure is from the regression of s_{Kjt}^{Cost} on μ_{jt} and a set of year dummies. The point estimate of the slope of the relationship is 0.407, with a standard error of 0.009.

Figure A.3: Relationship of capital cost share to intermediate use share across industries



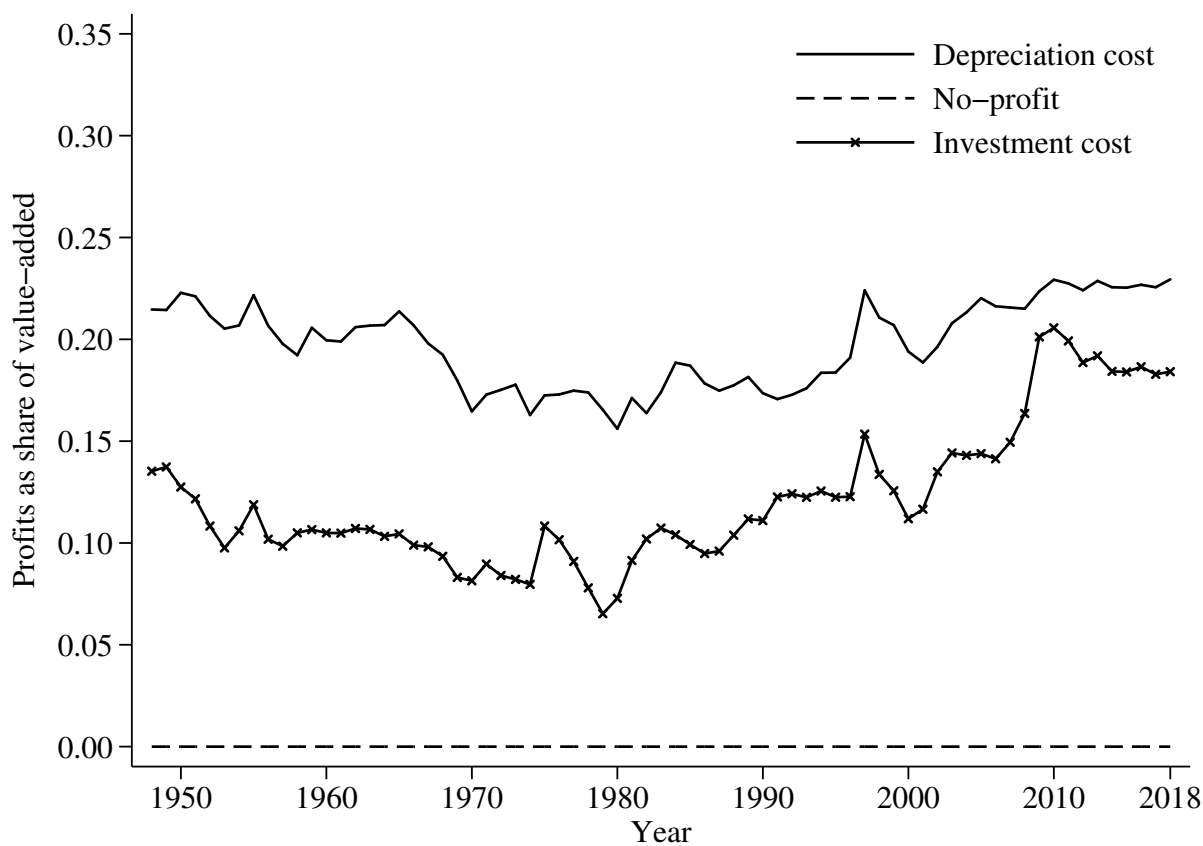
Notes: This shows the “binscatter” relationship of industry/year observations of capital shares of factor costs, s_{Kjt}^{Cost} , to the industry/year share of intermediate use of industry output, u_{jt} . Both are calculated using the depreciation cost assumption on capital costs, and are described in more detail in the text. The estimated relationship between the two in the Figure is from the regression of s_{Kjt}^{Cost} on u_{jt} and a set of year dummies. The point estimate of the slope of the relationship is 0.065, with a standard error of 0.007.

Figure A.4: Aggregate value-added markup under different capital cost assumptions



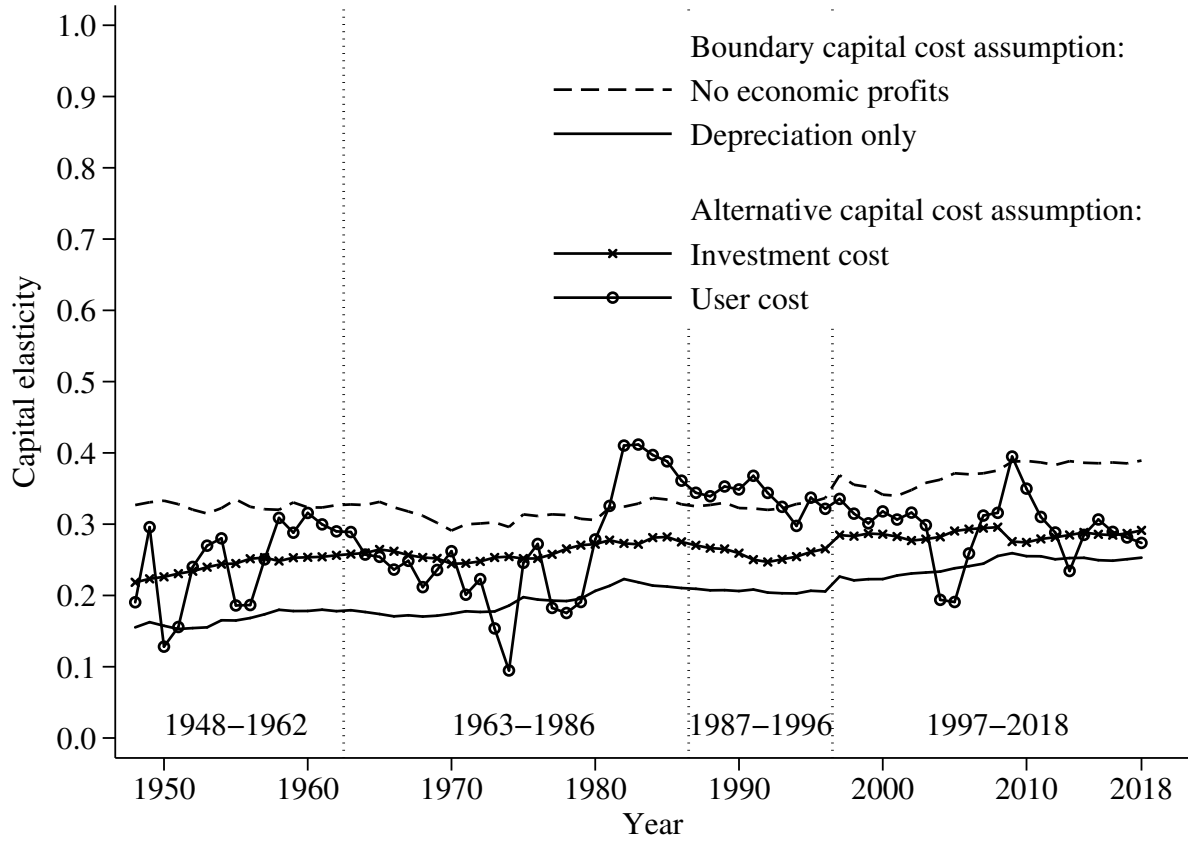
Notes: This shows the time series of μ_t^{VA} , the aggregate value-added markup, under three different assumptions on capital costs: no-profits (by construction the markup is one), investment costs, and depreciation costs. These series are based on the baseline estimates, including all industries.

Figure A.5: Profits as a share of value-added under different capital cost assumptions



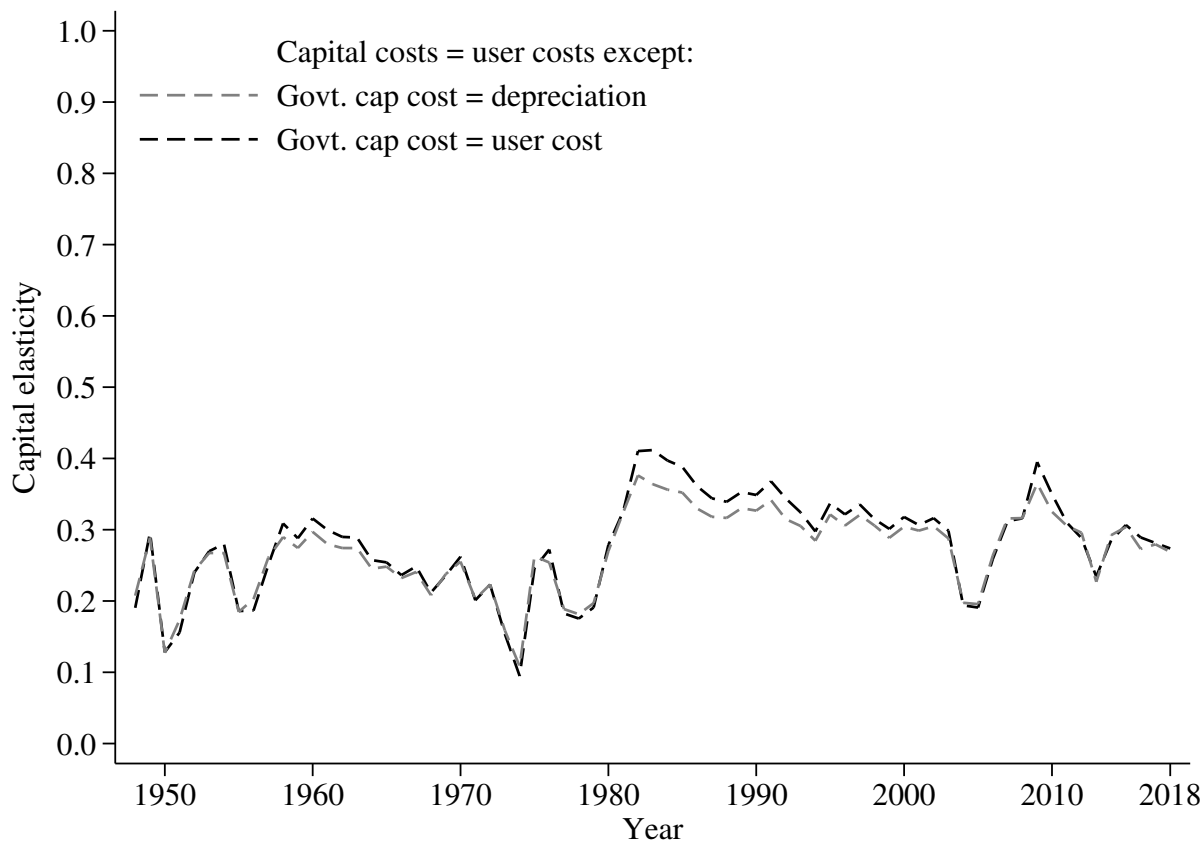
Notes: This shows the time series of π_t^{VA} , the aggregate value-added markup, under three different assumptions on capital costs: no-profits (by construction the markup is one), investment costs, and depreciation costs. These series are based on the baseline estimates, including all industries.

Figure A.6: Baseline estimates of ϵ_{Kt} , with data source breaks denoted



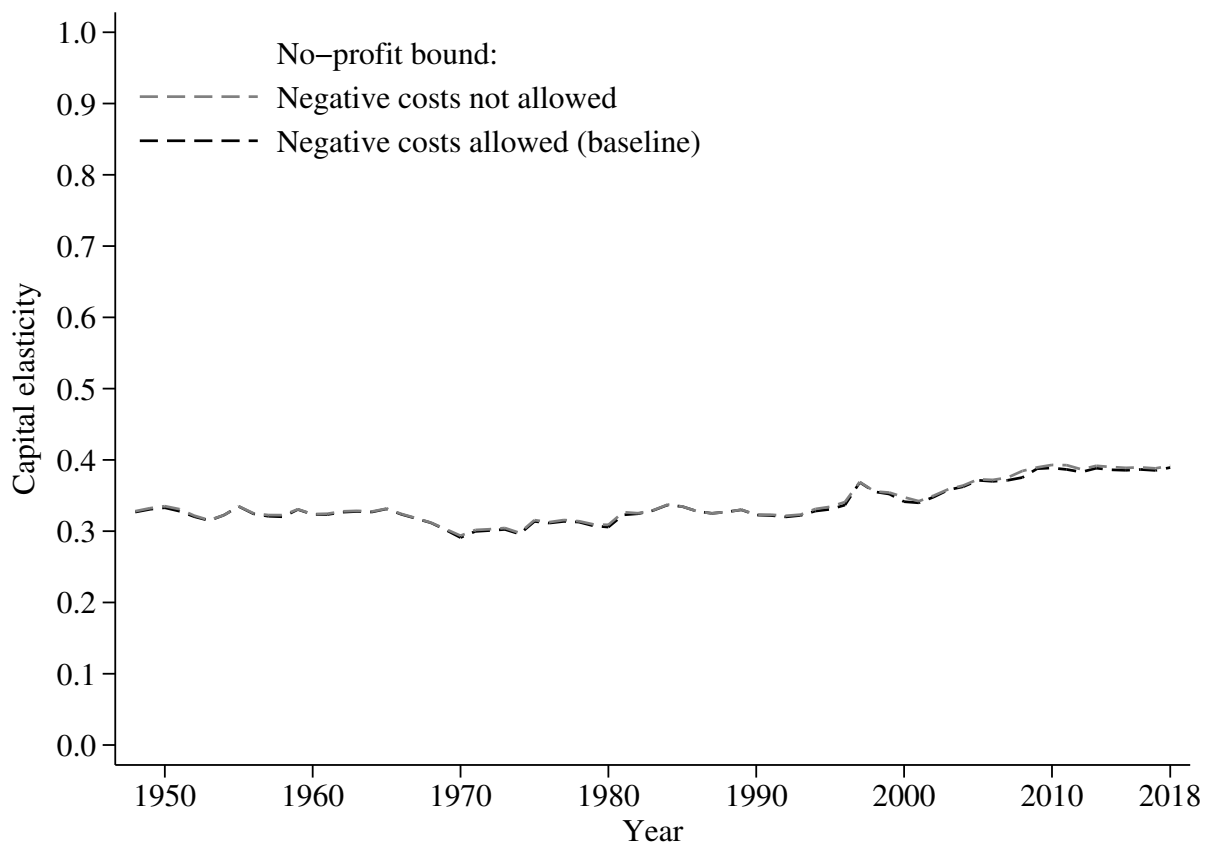
Notes: This plots the four baseline estimates of ϵ_{Kt} (no-profit, depreciation, investment cost, user cost), as in the main text. The vertical dotted lines denote the breaks in data sources listed in Table A.2.

Figure A.7: Comparison of user cost estimates of ϵ_{Kt} , with different government costs



Notes: The two series plot estimates of ϵ_{Kt} where capital costs are assumed to be equal to user costs for all private industries. The black dashed line shows the elasticity when government capital costs are calculated with the user cost formula described in Appendix A.9 and main text. The gray dashed line shows the elasticity when government capital costs are equal to depreciation costs only, as the BEA assumes.

Figure A.8: Comparison of estimates when allowing negative costs or not



Notes: The estimate of the aggregate capital elasticity, ϵ_K , is made using equation (9) under the no-profit assumption. The difference in estimates is allowing for negative costs of capital (dark lines) or not (gray lines).

Table A.2: Matching of SIC 1972 to NAICS, 1948-1962, Part 1

SIC 1972:		NAICS 1948-62:	
Code	Code text	Code	Code text
01-02	Farms	111CA	Farms
07-09	Agricultural services, fores	113FF	Forestry, fishing, and related activitie
B	Mining	213	Support activities for mining
10	Metal mining	212	Mining, except oil and gas
12	Coal mining	212	Mining, except oil and gas
13	Oil and gas extraction	211	Oil and gas extraction
14	Nonmetallic minerals, except	327	Nonmetallic mineral products
C	Construction	23	Construction
24	Lumber and wood products	321	Wood products
25	Furniture and fixtures	337	Furniture and related products
33	Primary metal industries	331	Primary metals
34	Fabricated metal products	332	Fabricated metal products
35	Machinery, except electrical	333	Machinery
36	Electric and electronic equipment	334	Computer and electronic products
36	Electric and electronic equipment	335	Electrical equipment, appliances, and co
371	Motor vehicles and equipment	3361MV	Motor vehicles, bodies and trailers, and
37ex371	Other transportation equipment	3364OT	Other transportation equipment
39	Miscellaneous manufacturing industries	339	Miscellaneous manufacturing
20	Food and kindred products	311FT	Food and beverage and tobacco products
22	Textile mill products	313TT	Textile mills and textile product mills
23	Apparel and other textile products	315AL	Apparel and leather and allied products
26	Paper and allied products	322	Paper products
27	Printing and publishing	323	Printing and related support activities
28	Chemicals and allied products	325	Chemical products
29	Petroleum and coal products	324	Petroleum and coal products
30	Rubber and miscellaneous plastics produc	326	Plastics and rubber products
40-45	Transportation	48	Transportation
42	Trucking and warehousing	493	Warehousing and storage

Notes: This table shows the the SIC 1972 industry matched to each NAICS industry for the years 1948-62. There are cases where the same SIC 1972 industry is matched to multiple NAICS industries, and where the same NAICS industry is matched to multiple SIC 1972 industries. The consequences of that are explained in the text. The matching is the authors based on crosswalks and personal judgement.

Table A.3: Matching of SIC 1972 to NAICS, 1948-1962, Part 2

SIC 1972:		NAICS 1948-62:	
Code	Code text	Code	Code text
48	Communications	51	Information
49	Electric, gas, and sanitary ser	22	Utilities
F	Wholesale trade	42	Wholesale trade
G	Retail trade	44RT	Retail trade
G	Retail trade	722	Food services and drinking places
60	Banking	52	Finance and insurance
61	Credit agencies other than banks	52	Finance and insurance
62	Security and commodity brokers	52	Finance and insurance
63	Insurance carriers	52	Finance and insurance
64	Insurance agents, brokers, a	52	Finance and insurance
65	Real estate /2/	531	Real estate
67	Holding and other investment offices	52	Finance and insurance
70	Hotels and other lodging places	721	Accommodation
72	Personal services	81	Other services, except government
73	Business services	54	Professional, scientific, and technical
73	Business services	532RL	Rental and leasing services and lessors
73	Business services	55	Management of companies and enterprises
79	Amusement and recreation services	71	Arts, entertainment, and recreation
80	Health services	62	Health care and social assistance
81	Legal services	54	Professional, scientific, and technical
82	Educational services	61	Educational services
83	Social services	62	Health care and social assistance
87	Miscellaneous professional services	54	Professional, scientific, and technical
87	Miscellaneous professional services	56	Administrative and waste management serv
	Federal general government	GFG	Federal general government
	Federal government enterprises	GFE	Federal government enterprises
	State and local general government	GSLG	State and local general government
	State and local government enterprises	GSLE	State and local government enterprises

Notes: This table shows the the SIC 1972 industry matched to each NAICS industry for the years 1948-62. There are cases where the same SIC 1972 industry is matched to multiple NAICS industries, and where the same NAICS industry is matched to multiple SIC 1972 industries. The consequences of that are explained in the text. The matching is the authors based on crosswalks and personal judgement.

Table A.4: Matching of SIC 1972 to NAICS, 1963-86, Part 1

SIC 1972:		NAICS 1963-86:	
Code	Code text	Code	Code text
01-02	Farms	111CA	Farms
07-09	Agricultural services, fores	113FF	Forestry, fishing, and related activitie
B	Mining	213	Support activities for mining
10	Metal mining	212	Mining, except oil and gas
12	Coal mining	212	Mining, except oil and gas
13	Oil and gas extraction	211	Oil and gas extraction
14	Nonmetallic minerals, except	327	Nonmetallic mineral products
C	Construction	23	Construction
24	Lumber and wood products	321	Wood products
25	Furniture and fixtures	337	Furniture and related products
33	Primary metal industries	331	Primary metals
34	Fabricated metal products	332	Fabricated metal products
35	Machinery, except electrical	333	Machinery
36	Electric and electronic equipment	334	Computer and electronic products
36	Electric and electronic equipment	335	Electrical equipment, appliances, and co
371	Motor vehicles and equipment	3361MV	Motor vehicles, bodies and trailers, and
37ex371	Other transportation equipment	3364OT	Other transportation equipment
39	Miscellaneous manufacturing industries	339	Miscellaneous manufacturing
20	Food and kindred products	311FT	Food and beverage and tobacco products
22	Textile mill products	313TT	Textile mills and textile product mills
23	Apparel and other textile products	315AL	Apparel and leather and allied products
26	Paper and allied products	322	Paper products
27	Printing and publishing	323	Printing and related support activities
28	Chemicals and allied products	325	Chemical products
29	Petroleum and coal products	324	Petroleum and coal products
30	Rubber and miscellaneous plastics produc	326	Plastics and rubber products
40	Railroad transportation	482	Rail transportation
41	Local and interurban passenger transit	485	Transit and ground passenger transportat
42	Trucking and warehousing	493	Warehousing and storage
42	Trucking and warehousing	484	Truck transportation
44	Water transportation	483	Water transportation
45	Transportation by air	481	Air transportation
46	Pipelines, except natural ga	486	Pipeline transportation
47	Transportation services	487OS	Other transportation and support activit

Notes: This table shows the the SIC 1972 industry matched to each NAICS industry for the years 1963-86. There are cases where the same SIC 1972 industry is matched to multiple NAICS industries, and where the same NAICS industry is matched to multiple SIC 1972 industries. The consequences of that are explained in the text. The matching is the authors based on crosswalks and personal judgement.

Table A.5: Matching of SIC 1972 to NAICS, 1963-86, Part 2

SIC 1972:		NAICS 1963-86:	
Code	Code text	Code	Code text
48	Communications	514	Data processing, internet publishing, an
481-482	Telephone and telegraph	513	Broadcasting and telecommunications
483	Radio and television	513	Broadcasting and telecommunications
49	Electric, gas, and sanitary ser	22	Utilities
F	Wholesale trade	42	Wholesale trade
G	Retail trade	44RT	Retail trade
G	Retail trade	722	Food services and drinking places
60	Banking	521CI	Federal Reserve banks, credit intermedia
61	Credit agencies other than banks	521CI	Federal Reserve banks, credit intermedia
62	Security and commodity brokers	523	Securities, commodity contracts, and inv
63	Insurance carriers	524	Insurance carriers and related activitie
64	Insurance agents, brokers, a	524	Insurance carriers and related activitie
65	Real estate /2/	531	Real estate
67	Holding and other investment offices	525	Funds, trusts, and other financial vehic
70	Hotels and other lodging places	721	Accommodation
72	Personal services	81	Other services, except government
73	Business services	561	Administrative and support services
73	Business services	55	Management of companies and enterprises
73	Business services	511	Publishing industries, except internet (
73	Business services	532RL	Rental and leasing services and lessors
73	Business services	5415	Computer systems design and related serv
78	Motion pictures	512	Motion picture and sound recording indus
79	Amusement and recreation services	711AS	Performing arts, spectator sports, museu
79	Amusement and recreation services	713	Amusements, gambling, and recreation ind
80	Health services	621	Ambulatory health care services
80	Health services	622HO	Hospitals and nursing and residential ca
81	Legal services	5411	Legal services
82	Educational services	61	Educational services
83	Social services	624	Social assistance
87	Miscellaneous professional services	5412OP	Miscellaneous professional, scientific,
87	Miscellaneous professional services	562	Waste management and remediation service
	Federal general government	GFG	Federal general government
	Federal government enterprises	GFE	Federal government enterprises
	State and local general government	GSLG	State and local general government
	State and local government enterprises	GSLE	State and local government enterprises

Notes: This table shows the the SIC 1972 industry matched to each NAICS industry for the years 1963-86. There are cases where the same SIC 1972 industry is matched to multiple NAICS industries, and where the same NAICS industry is matched to multiple SIC 1972 industries. The consequences of that are explained in the text. The matching is the authors based on crosswalks and personal judgement.

Table A.6: Matching of SIC 1987 to NAICS, 1987-96, Part 1

SIC 1987:		NAICS 1987-96:	
Code	Code text	Code	Code text
01-02	Farms	111CA	Farms
07-09	Agricultural services, fores	113FF	Forestry, fishing, and related activitie
B	Mining	213	Support activities for mining
10	Metal mining	212	Mining, except oil and gas
12	Coal mining	212	Mining, except oil and gas
13	Oil and gas extraction	211	Oil and gas extraction
14	Nonmetallic minerals, except	327	Nonmetallic mineral products
C	Construction	23	Construction
24	Lumber and wood products	321	Wood products
25	Furniture and fixtures	337	Furniture and related products
33	Primary metal industries	331	Primary metals
34	Fabricated metal products	332	Fabricated metal products
35	Industrial machinery and equipment	333	Machinery
36	Electronic and other electric equipment	335	Electrical equipment, appliances, and co
36	Electronic and other electric equipment	334	Computer and electronic products
371	Motor vehicles and equipment	3361MV	Motor vehicles, bodies and trailers, and
37ex371	Other transportation equipment	3364OT	Other transportation equipment
39	Miscellaneous manufacturing industries	339	Miscellaneous manufacturing
20	Food and kindred products	311FT	Food and beverage and tobacco products
22	Textile mill products	313TT	Textile mills and textile product mills
23	Apparel and other textile products	315AL	Apparel and leather and allied products
26	Paper and allied products	322	Paper products
27	Printing and publishing	323	Printing and related support activities
28	Chemicals and allied products	325	Chemical products
29	Petroleum and coal products	324	Petroleum and coal products
30	Rubber and miscellaneous plastics produc	326	Plastics and rubber products
40	Railroad transportation	482	Rail transportation
41	Local and interurban passenger transit	485	Transit and ground passenger transportat
42	Trucking and warehousing	493	Warehousing and storage
42	Trucking and warehousing	484	Truck transportation
44	Water transportation	483	Water transportation
45	Transportation by air	481	Air transportation
46	Pipelines, except natural ga	486	Pipeline transportation
47	Transportation services	487OS	Other transportation and support activit

Notes: This table shows the the SIC 1987 industry matched to each NAICS industry for the years 1987-96. There are cases where the same SIC 1987 industry is matched to multiple NAICS industries, and where the same NAICS industry is matched to multiple SIC 1987 industries. The consequences of that are explained in the text. The matching is the authors based on crosswalks and personal judgement.

Table A.7: Matching of SIC 1987 to NAICS, 1987-96, Part 2

SIC 1987:		NAICS 1987-96:	
Code	Code text	Code	Code text
48	Communications	513	Broadcasting and telecommunications
48	Communications	514	Data processing, internet publishing, an
49	Electric, gas, and sanitary ser	22	Utilities
F	Wholesale trade	42	Wholesale trade
G	Retail trade	44RT	Retail trade
G	Retail trade	722	Food services and drinking places
60	Depository institutions	521CI	Federal Reserve banks, credit intermedia
61	Nondepository institutions	521CI	Federal Reserve banks, credit intermedia
62	Security and commodity brokers	523	Securities, commodity contracts, and inv
63	Insurance carriers	524	Insurance carriers and related activitie
64	Insurance agents, brokers, a	524	Insurance carriers and related activitie
65	Real Estate /2/	531	Real estate
67	Holding and other investment offices	525	Funds, trusts, and other financial vehic
70	Hotels and other lodging places	721	Accommodation
72	Personal services	81	Other services, except government
73	Business services	562	Waste management and remediation service
73	Business services	561	Administrative and support services
73	Business services	55	Management of companies and enterprises
73	Business services	5415	Computer systems design and related serv
73	Business services	532RL	Rental and leasing services and lessors
73	Business services	511	Publishing industries, except internet (
78	Motion pictures	512	Motion picture and sound recording indus
79	Amusement and recreation services	713	Amusements, gambling, and recreation ind
79	Amusement and recreation services	711AS	Performing arts, spectator sports, museu
80	Health services	621	Ambulatory health care services
80	Health services	622HO	Hospitals and nursing and residential ca
81	Legal services	5411	Legal services
82	Educational services	61	Educational services
83	Social services	624	Social assistance
87	Other services	81	Other services, except government
87	Other services	5412OP	Miscellaneous professional, scientific,
	Federal general government	GFG	Federal general government
	Federal government enterprises	GFE	Federal government enterprises
	State and local general government	GSLG	State and local general government
	State and local government enterprises	GSLE	State and local government enterprises

Notes: This table shows the the SIC 1987 industry matched to each NAICS industry for the years 1987-96. There are cases where the same SIC 1987 industry is matched to multiple NAICS industries, and where the same NAICS industry is matched to multiple SIC 1987 industries. The consequences of that are explained in the text. The matching is the authors based on crosswalks and personal judgement.

Table A.8: Comparison of ϵ_{Kt} estimates before and after redefinitions, 1997-2018

Year	No-profit scenario:			Depreciation scenario:		
	After Redef. (1)	Before Redef. (2)	Difference (3)	After Redef. (4)	Before Redef. (5)	Difference (6)
1997	0.3663	0.3686	-0.0022	0.2241	0.2265	-0.0024
1998	0.3531	0.3553	-0.0022	0.2188	0.2211	-0.0023
1999	0.3499	0.3522	-0.0023	0.2204	0.2229	-0.0025
2000	0.3385	0.3414	-0.0029	0.2205	0.2230	-0.0024
2001	0.3376	0.3398	-0.0022	0.2260	0.2281	-0.0021
2002	0.3457	0.3479	-0.0022	0.2289	0.2309	-0.0020
2003	0.3557	0.3580	-0.0023	0.2301	0.2322	-0.0021
2004	0.3602	0.3624	-0.0023	0.2315	0.2335	-0.0021
2005	0.3691	0.3714	-0.0024	0.2360	0.2381	-0.0022
2006	0.3674	0.3700	-0.0026	0.2387	0.2411	-0.0024
2007	0.3690	0.3714	-0.0025	0.2427	0.2447	-0.0019
2008	0.3720	0.3753	-0.0034	0.2532	0.2553	-0.0022
2009	0.3854	0.3877	-0.0023	0.2573	0.2594	-0.0021
2010	0.3863	0.3887	-0.0024	0.2533	0.2551	-0.0019
2011	0.3837	0.3866	-0.0030	0.2522	0.2549	-0.0028
2012	0.3799	0.3831	-0.0032	0.2478	0.2507	-0.0030
2013	0.3853	0.3884	-0.0031	0.2497	0.2525	-0.0028
2014	0.3827	0.3862	-0.0035	0.2494	0.2528	-0.0034
2015	0.3824	0.3854	-0.0030	0.2462	0.2495	-0.0032
2016	0.3836	0.3866	-0.0030	0.2454	0.2488	-0.0033
2017	0.3821	0.3853	-0.0032	0.2471	0.2509	-0.0038
2018	0.3856	0.3893	-0.0037	0.2487	0.2530	-0.0043
Mean	0.3692	0.3719	-0.0027	0.2395	0.2420	-0.0026

Notes: The table shows the estimates, by year, of ϵ_{Kt} , based on different assumptions regarding the input/output tables used and the assumption on capital costs (no-profits and depreciation costs only). Columns (1) and (4) use the Total Requirements tables After Redefinition. Columns (2) and (5) use Before Redefinitions Tables, as in the main text. Columns (3) and (6) show the difference in the estimates using the two methods. Due to rounding, the differences in (3) and (6) may not be exactly equal to the differences between the preceding columns.

Table A.9: Comparison of ϵ_{Kt} estimates before and after redefinitions, 1997-2018

Year	Investment cost scenario:			User cost scenario:		
	After Redef. (1)	Before Redef. (2)	Difference (3)	After Redef. (4)	Before Redef. (5)	Difference (6)
1997	0.2826	0.2846	-0.0020	0.3333	0.3355	-0.0022
1998	0.2813	0.2832	-0.0019	0.3125	0.3148	-0.0023
1999	0.2851	0.2869	-0.0018	0.2988	0.3012	-0.0024
2000	0.2840	0.2860	-0.0020	0.3157	0.3179	-0.0023
2001	0.2807	0.2827	-0.0020	0.3044	0.3065	-0.0021
2002	0.2753	0.2770	-0.0018	0.3143	0.3162	-0.0019
2003	0.2773	0.2790	-0.0017	0.2966	0.2987	-0.0021
2004	0.2805	0.2822	-0.0017	0.1919	0.1939	-0.0020
2005	0.2886	0.2904	-0.0018	0.1888	0.1908	-0.0020
2006	0.2910	0.2930	-0.0020	0.2569	0.2589	-0.0020
2007	0.2925	0.2945	-0.0020	0.3102	0.3121	-0.0019
2008	0.2935	0.2958	-0.0023	0.3138	0.3159	-0.0021
2009	0.2733	0.2756	-0.0023	0.3930	0.3950	-0.0020
2010	0.2725	0.2745	-0.0020	0.3479	0.3499	-0.0019
2011	0.2763	0.2793	-0.0030	0.3077	0.3102	-0.0025
2012	0.2786	0.2816	-0.0031	0.2854	0.2883	-0.0030
2013	0.2820	0.2849	-0.0029	0.2309	0.2344	-0.0035
2014	0.2849	0.2884	-0.0034	0.2821	0.2850	-0.0029
2015	0.2827	0.2858	-0.0031	0.3034	0.3066	-0.0032
2016	0.2817	0.2847	-0.0030	0.2855	0.2892	-0.0037
2017	0.2837	0.2870	-0.0033	0.2778	0.2814	-0.0035
2018	0.2874	0.2913	-0.0039	0.2692	0.2737	-0.0045
Mean	0.2825	0.2849	-0.0024	0.2918	0.2944	-0.0025

Notes: The table shows the estimates, by year, of ϵ_{Kt} , based on different assumptions regarding the input/output tables used and the assumption on capital costs (no-profits and depreciation costs only). Columns (1) and (4) use the Total Requirements tables After Redefinition. Columns (2) and (5) use Before Redefinitions Tables, as in the main text. Columns (3) and (6) show the difference in the estimates using the two methods. Due to rounding, the differences in (3) and (6) may not be exactly equal to the differences between the preceding columns.

Table A.10: Comparison of ϵ_{Kt} estimates with and without imports, 1997-2018

Year	No-profit scenario:			Depreciation scenario:		
	Excluding Imports (1)	Including Imports (2)	Difference (3)	Excluding Imports (4)	Including Imports (5)	Difference (6)
1997	0.3703	0.3686	0.0018	0.2268	0.2265	0.0003
1998	0.3556	0.3553	0.0003	0.2209	0.2211	-0.0002
1999	0.3523	0.3522	0.0001	0.2228	0.2229	-0.0000
2000	0.3431	0.3414	0.0016	0.2239	0.2230	0.0009
2001	0.3406	0.3398	0.0008	0.2288	0.2281	0.0007
2002	0.3490	0.3479	0.0010	0.2314	0.2309	0.0006
2003	0.3606	0.3580	0.0026	0.2331	0.2322	0.0009
2004	0.3665	0.3624	0.0041	0.2345	0.2335	0.0010
2005	0.3774	0.3714	0.0060	0.2396	0.2381	0.0014
2006	0.3772	0.3700	0.0072	0.2422	0.2411	0.0011
2007	0.3787	0.3714	0.0073	0.2460	0.2447	0.0013
2008	0.3827	0.3753	0.0074	0.2586	0.2553	0.0033
2009	0.3910	0.3877	0.0033	0.2608	0.2594	0.0014
2010	0.3959	0.3887	0.0071	0.2578	0.2551	0.0027
2011	0.3964	0.3866	0.0097	0.2582	0.2549	0.0032
2012	0.3925	0.3831	0.0095	0.2537	0.2507	0.0029
2013	0.3964	0.3884	0.0080	0.2549	0.2525	0.0024
2014	0.3930	0.3862	0.0068	0.2550	0.2528	0.0022
2015	0.3889	0.3854	0.0035	0.2499	0.2495	0.0004
2016	0.3892	0.3866	0.0026	0.2489	0.2488	0.0002
2017	0.3883	0.3853	0.0030	0.2511	0.2509	0.0002
2018	0.3927	0.3893	0.0033	0.2535	0.2530	0.0004
Mean	0.3763	0.3719	0.0044	0.2433	0.2420	0.0012

Notes: The table shows the estimates, by year, of ϵ_{Kt} , excluding imports of intermediates and including them (the baseline) and the assumption on capital costs (no-profits and depreciation costs only). Columns (1) and (4) subtract imported intermediates from the Use Table to calculate ϵ_K . Columns (2) and (5) use the Use Table, as in the main text. Columns (3) and (6) show the difference in the estimates using the two methods. Due to rounding, the differences in (3) and (6) may not be exactly equal to the differences between the preceding columns.

Table A.11: Comparison of ϵ_{Kt} estimates with and without imports, 1997-2018

Year	Investment cost scenario:			User cost scenario:		
	Excluding Imports (1)	Including Imports (2)	Difference (3)	Excluding Imports (4)	Including Imports (5)	Difference (6)
1997	0.2842	0.2846	-0.0005	0.3363	0.3355	0.0008
1998	0.2821	0.2832	-0.0011	0.3152	0.3148	0.0004
1999	0.2855	0.2869	-0.0014	0.3012	0.3012	0.0000
2000	0.2855	0.2860	-0.0004	0.3192	0.3179	0.0013
2001	0.2825	0.2827	-0.0002	0.3079	0.3065	0.0014
2002	0.2763	0.2770	-0.0007	0.3173	0.3162	0.0011
2003	0.2785	0.2790	-0.0006	0.3003	0.2987	0.0016
2004	0.2814	0.2822	-0.0008	0.1981	0.1939	0.0042
2005	0.2907	0.2904	0.0002	0.1964	0.1908	0.0056
2006	0.2933	0.2930	0.0002	0.2607	0.2589	0.0017
2007	0.2964	0.2945	0.0019	0.3132	0.3121	0.0012
2008	0.3001	0.2958	0.0044	0.3180	0.3159	0.0021
2009	0.2777	0.2756	0.0021	0.3965	0.3950	0.0016
2010	0.2771	0.2745	0.0026	0.3519	0.3499	0.0020
2011	0.2825	0.2793	0.0032	0.3129	0.3102	0.0027
2012	0.2855	0.2816	0.0038	0.2924	0.2883	0.0040
2013	0.2887	0.2849	0.0038	0.2410	0.2344	0.0066
2014	0.2909	0.2884	0.0025	0.2883	0.2850	0.0033
2015	0.2860	0.2858	0.0002	0.3078	0.3066	0.0012
2016	0.2845	0.2847	-0.0002	0.2907	0.2892	0.0015
2017	0.2869	0.2870	-0.0002	0.2818	0.2814	0.0004
2018	0.2914	0.2913	0.0001	0.2750	0.2737	0.0012
Mean	0.2858	0.2849	0.0009	0.2965	0.2944	0.0021

Notes: The table shows the estimates, by year, of ϵ_{Kt} , excluding imports of intermediates and including them (the baseline) and the assumption on capital costs (investment and user costs only). Columns (1) and (4) subtract imported intermediates from the Use Table to calculate ϵ_K . Columns (2) and (5) use the Use Table, as in the main text. Columns (3) and (6) show the difference in the estimates using the two methods. Due to rounding, the differences in (3) and (6) may not be exactly equal to the differences between the preceding columns.

Table A.12: Capital costs as share of factor costs and value-added, housing and government

Variant	Summary statistics, 1948-2018:							
	Capital costs/Factor costs, s_{Kt}^{Cost}				Capital costs/Value-added, s_{Kt}^{VA}			
	Mean (1)	Median (2)	Minimum (3)	Maximum (4)	Mean (5)	Median (6)	Minimum (7)	Maximum (8)
Panel A: Housing								
No-profit	0.942	0.942	0.930	0.954	0.942	0.942	0.930	0.954
Investment cost	0.892	0.893	0.827	0.935	0.509	0.508	0.221	0.922
User cost	0.832	0.913	0.225	0.970	0.596	0.616	0.015	1.828
Depreciation cost	0.797	0.796	0.764	0.838	0.227	0.226	0.187	0.277
Panel B: Government								
No-profit	0.197	0.202	0.143	0.327	0.197	0.202	0.143	0.327
Investment cost	0.298	0.276	0.252	0.394	0.343	0.317	0.256	0.498
User cost	0.281	0.278	0.089	0.525	0.336	0.303	0.077	0.937
Depreciation cost	0.221	0.218	0.195	0.320	0.228	0.224	0.198	0.316

Notes: The panels of the table refer to different sectors of the economy. Owner-occupied housing refers to NAICS codes HS, ORE, and 531. Government refers to NAICS codes GFGD, GFGN, GFE, GSLG, GSLE, and GFG, which covers federal, state, and local government, both general and enterprises. In each row, the assumption made to calculate capital costs is labeled, as described in the text. Columns (1)-(4) are summary statistics over 1948-2018 for the total estimated capital costs divided by total factor costs (the sum of capital costs and labor costs). Columns (5)-(9) are summary statistics over 1948-2018 for total capital costs divided by value-added.

Table A.13: Baseline annual estimates of elasticities, 1948-2018, no-profit assumption

Year	Elasticity with respect to:				Year	Elasticity with respect to:			
	Labor	Structures	Equipment	IP		Labor	Structures	Equipment	IP
1948	0.6731	0.1455	0.1593	0.0220	1984	0.6632	0.1636	0.1345	0.0387
1949	0.6692	0.1433	0.1650	0.0225	1985	0.6654	0.1659	0.1312	0.0375
1950	0.6671	0.1439	0.1646	0.0244	1986	0.6721	0.1580	0.1317	0.0383
1951	0.6719	0.1441	0.1650	0.0190	1987	0.6749	0.1546	0.1287	0.0418
1952	0.6796	0.1450	0.1539	0.0214	1988	0.6730	0.1507	0.1313	0.0449
1953	0.6851	0.1448	0.1467	0.0234	1989	0.6700	0.1513	0.1319	0.0469
1954	0.6774	0.1550	0.1430	0.0246	1990	0.6774	0.1517	0.1240	0.0469
1955	0.6653	0.1554	0.1500	0.0293	1991	0.6780	0.1482	0.1238	0.0501
1956	0.6756	0.1585	0.1394	0.0265	1992	0.6799	0.1455	0.1238	0.0507
1957	0.6790	0.1557	0.1373	0.0280	1993	0.6779	0.1447	0.1259	0.0515
1958	0.6798	0.1606	0.1299	0.0297	1994	0.6717	0.1442	0.1325	0.0516
1959	0.6695	0.1577	0.1379	0.0348	1995	0.6693	0.1470	0.1321	0.0516
1960	0.6764	0.1625	0.1297	0.0313	1996	0.6634	0.1492	0.1343	0.0531
1961	0.6766	0.1626	0.1278	0.0330	1997	0.6314	0.1558	0.1429	0.0699
1962	0.6733	0.1624	0.1293	0.0350	1998	0.6447	0.1486	0.1388	0.0679
1963	0.6723	0.1630	0.1296	0.0351	1999	0.6478	0.1484	0.1342	0.0696
1964	0.6731	0.1600	0.1316	0.0353	2000	0.6586	0.1486	0.1274	0.0654
1965	0.6687	0.1590	0.1367	0.0356	2001	0.6602	0.1543	0.1203	0.0652
1966	0.6764	0.1528	0.1370	0.0338	2002	0.6521	0.1521	0.1226	0.0732
1967	0.6821	0.1521	0.1325	0.0332	2003	0.6420	0.1540	0.1272	0.0768
1968	0.6882	0.1490	0.1278	0.0350	2004	0.6376	0.1524	0.1305	0.0795
1969	0.6981	0.1453	0.1248	0.0319	2005	0.6286	0.1589	0.1331	0.0794
1970	0.7089	0.1463	0.1163	0.0285	2006	0.6300	0.1582	0.1330	0.0788
1971	0.7003	0.1513	0.1157	0.0327	2007	0.6286	0.1650	0.1292	0.0772
1972	0.6990	0.1498	0.1180	0.0332	2008	0.6247	0.1724	0.1260	0.0769
1973	0.6975	0.1492	0.1233	0.0300	2009	0.6123	0.1725	0.1242	0.0909
1974	0.7039	0.1519	0.1202	0.0239	2010	0.6113	0.1601	0.1364	0.0923
1975	0.6863	0.1577	0.1281	0.0280	2011	0.6134	0.1608	0.1355	0.0903
1976	0.6886	0.1523	0.1283	0.0308	2012	0.6169	0.1593	0.1332	0.0906
1977	0.6862	0.1496	0.1327	0.0315	2013	0.6116	0.1610	0.1360	0.0915
1978	0.6871	0.1496	0.1336	0.0296	2014	0.6138	0.1641	0.1311	0.0911
1979	0.6925	0.1478	0.1322	0.0276	2015	0.6146	0.1634	0.1298	0.0922
1980	0.6942	0.1581	0.1227	0.0250	2016	0.6134	0.1649	0.1257	0.0960
1981	0.6770	0.1652	0.1297	0.0281	2017	0.6147	0.1658	0.1253	0.0942
1982	0.6755	0.1670	0.1255	0.0320	2018	0.6107	0.1662	0.1256	0.0975
1983	0.6711	0.1630	0.1283	0.0376

Notes: This table shows the estimated values of the elasticities for the four factors of production - labor and three types of capital (structures, equipment, and IP) - in the baseline calculations of the paper using the assumption of no profits to calculate capital costs. Proprietors income is split according to [Gomme and Rupert \(2004\)](#), all industries are included, and intellectual property is included as a type of capital. Details on those assumptions are available in the main text.

Table A.14: Baseline annual estimates of elasticities, 1948-2018, depreciation cost assumption

Year	Elasticity with respect to:				Year	Elasticity with respect to:			
	Labor	Structures	Equipment	IP		Labor	Structures	Equipment	IP
1948	0.8447	0.0734	0.0712	0.0107	1984	0.7861	0.0976	0.0842	0.0320
1949	0.8375	0.0767	0.0741	0.0117	1985	0.7875	0.0958	0.0838	0.0330
1950	0.8425	0.0736	0.0723	0.0115	1986	0.7896	0.0924	0.0839	0.0341
1951	0.8470	0.0726	0.0695	0.0109	1987	0.7906	0.0894	0.0845	0.0355
1952	0.8458	0.0719	0.0708	0.0116	1988	0.7928	0.0872	0.0835	0.0366
1953	0.8447	0.0713	0.0719	0.0120	1989	0.7925	0.0869	0.0831	0.0375
1954	0.8348	0.0750	0.0766	0.0135	1990	0.7938	0.0856	0.0824	0.0382
1955	0.8351	0.0748	0.0754	0.0147	1991	0.7917	0.0851	0.0828	0.0404
1956	0.8316	0.0769	0.0765	0.0150	1992	0.7959	0.0833	0.0805	0.0403
1957	0.8265	0.0779	0.0784	0.0173	1993	0.7969	0.0834	0.0787	0.0410
1958	0.8201	0.0799	0.0815	0.0186	1994	0.7972	0.0830	0.0789	0.0410
1959	0.8218	0.0782	0.0793	0.0206	1995	0.7934	0.0847	0.0799	0.0420
1960	0.8218	0.0792	0.0777	0.0214	1996	0.7944	0.0833	0.0799	0.0424
1961	0.8199	0.0812	0.0764	0.0225	1997	0.7735	0.0978	0.0832	0.0456
1962	0.8220	0.0811	0.0740	0.0229	1998	0.7789	0.0951	0.0801	0.0460
1963	0.8207	0.0821	0.0746	0.0226	1999	0.7771	0.0960	0.0792	0.0477
1964	0.8232	0.0804	0.0734	0.0230	2000	0.7770	0.0965	0.0779	0.0485
1965	0.8261	0.0784	0.0722	0.0234	2001	0.7719	0.1007	0.0779	0.0494
1966	0.8293	0.0762	0.0711	0.0235	2002	0.7691	0.1026	0.0773	0.0510
1967	0.8278	0.0757	0.0718	0.0247	2003	0.7678	0.1053	0.0755	0.0515
1968	0.8296	0.0745	0.0710	0.0249	2004	0.7665	0.1090	0.0732	0.0513
1969	0.8283	0.0754	0.0710	0.0252	2005	0.7619	0.1152	0.0722	0.0507
1970	0.8258	0.0766	0.0713	0.0263	2006	0.7589	0.1187	0.0719	0.0505
1971	0.8222	0.0798	0.0709	0.0271	2007	0.7553	0.1212	0.0720	0.0515
1972	0.8232	0.0803	0.0697	0.0269	2008	0.7447	0.1275	0.0742	0.0537
1973	0.8224	0.0827	0.0687	0.0262	2009	0.7406	0.1245	0.0775	0.0574
1974	0.8142	0.0879	0.0711	0.0268	2010	0.7449	0.1206	0.0761	0.0585
1975	0.8024	0.0918	0.0782	0.0276	2011	0.7451	0.1202	0.0763	0.0584
1976	0.8057	0.0891	0.0778	0.0273	2012	0.7493	0.1167	0.0759	0.0582
1977	0.8072	0.0878	0.0779	0.0270	2013	0.7475	0.1161	0.0769	0.0595
1978	0.8078	0.0873	0.0780	0.0268	2014	0.7472	0.1173	0.0759	0.0596
1979	0.8046	0.0900	0.0789	0.0265	2015	0.7505	0.1134	0.0757	0.0604
1980	0.7936	0.0969	0.0822	0.0273	2016	0.7512	0.1118	0.0755	0.0616
1981	0.7865	0.1002	0.0849	0.0283	2017	0.7491	0.1146	0.0742	0.0620
1982	0.7770	0.1042	0.0881	0.0307	2018	0.7470	0.1162	0.0737	0.0631
1983	0.7815	0.1008	0.0861	0.0316

Notes: This table shows the estimated values of the elasticities for the four factors of production - labor and three types of capital (structures, equipment, and IP) - in the baseline calculations of the paper using depreciation costs to calculate capital costs. Proprietors income is split according to [Gomme and Rupert \(2004\)](#), all industries are included, and intellectual property is included as a type of capital. Details on those assumptions are available in the main text.

Table A.15: Baseline annual estimates of elasticities, 1948-2018, investment cost assumption

Year	Elasticity with respect to:				Year	Elasticity with respect to:			
	Labor	Structures	Equipment	IP		Labor	Structures	Equipment	IP
1948	0.7816	0.1206	0.0832	0.0146	1984	0.7189	0.1442	0.0984	0.0385
1949	0.7766	0.1257	0.0831	0.0145	1985	0.7179	0.1455	0.0969	0.0398
1950	0.7739	0.1307	0.0809	0.0145	1986	0.7248	0.1404	0.0945	0.0402
1951	0.7694	0.1277	0.0899	0.0130	1987	0.7297	0.1371	0.0919	0.0413
1952	0.7660	0.1292	0.0902	0.0146	1988	0.7336	0.1321	0.0922	0.0421
1953	0.7603	0.1298	0.0940	0.0159	1989	0.7347	0.1294	0.0925	0.0434
1954	0.7560	0.1387	0.0870	0.0183	1990	0.7407	0.1269	0.0882	0.0443
1955	0.7551	0.1396	0.0861	0.0191	1991	0.7497	0.1192	0.0848	0.0462
1956	0.7485	0.1422	0.0870	0.0223	1992	0.7530	0.1179	0.0836	0.0455
1957	0.7469	0.1398	0.0892	0.0241	1993	0.7494	0.1193	0.0864	0.0449
1958	0.7516	0.1420	0.0806	0.0258	1994	0.7455	0.1204	0.0901	0.0440
1959	0.7471	0.1416	0.0851	0.0262	1995	0.7390	0.1227	0.0933	0.0450
1960	0.7465	0.1427	0.0841	0.0267	1996	0.7346	0.1255	0.0937	0.0462
1961	0.7458	0.1432	0.0820	0.0290	1997	0.7154	0.1354	0.0977	0.0515
1962	0.7436	0.1437	0.0835	0.0292	1998	0.7168	0.1338	0.0971	0.0522
1963	0.7419	0.1448	0.0823	0.0310	1999	0.7131	0.1345	0.0975	0.0550
1964	0.7404	0.1437	0.0842	0.0318	2000	0.7140	0.1355	0.0950	0.0554
1965	0.7355	0.1434	0.0884	0.0327	2001	0.7173	0.1406	0.0874	0.0546
1966	0.7380	0.1369	0.0922	0.0329	2002	0.7230	0.1385	0.0831	0.0555
1967	0.7433	0.1337	0.0897	0.0333	2003	0.7210	0.1417	0.0814	0.0559
1968	0.7467	0.1336	0.0861	0.0335	2004	0.7178	0.1442	0.0823	0.0557
1969	0.7481	0.1325	0.0863	0.0331	2005	0.7096	0.1509	0.0840	0.0555
1970	0.7556	0.1299	0.0826	0.0319	2006	0.7070	0.1516	0.0859	0.0555
1971	0.7549	0.1371	0.0767	0.0313	2007	0.7055	0.1521	0.0857	0.0567
1972	0.7522	0.1385	0.0782	0.0311	2008	0.7042	0.1533	0.0836	0.0588
1973	0.7467	0.1389	0.0847	0.0296	2009	0.7244	0.1396	0.0733	0.0627
1974	0.7455	0.1376	0.0876	0.0293	2010	0.7255	0.1285	0.0829	0.0631
1975	0.7482	0.1355	0.0862	0.0301	2011	0.7207	0.1281	0.0876	0.0636
1976	0.7480	0.1342	0.0871	0.0307	2012	0.7184	0.1283	0.0903	0.0631
1977	0.7423	0.1348	0.0925	0.0304	2013	0.7151	0.1300	0.0906	0.0643
1978	0.7346	0.1385	0.0969	0.0300	2014	0.7116	0.1351	0.0898	0.0635
1979	0.7294	0.1408	0.0992	0.0306	2015	0.7142	0.1339	0.0879	0.0640
1980	0.7280	0.1448	0.0958	0.0314	2016	0.7153	0.1337	0.0843	0.0666
1981	0.7224	0.1465	0.0980	0.0332	2017	0.7130	0.1371	0.0838	0.0660
1982	0.7270	0.1431	0.0940	0.0359	2018	0.7087	0.1380	0.0853	0.0680
1983	0.7282	0.1414	0.0931	0.0374

Notes: This table shows the estimated values of the elasticities for the four factors of production - labor and three types of capital (structures, equipment, and IP) - in the baseline calculations of the paper using investment costs to calculate capital costs. Proprietors income is split according to [Gomme and Rupert \(2004\)](#), all industries are included, and intellectual property is included as a type of capital. Details on those assumptions are available in the main text.

Table A.16: Baseline annual estimates of elasticities, 1948-2018, user cost assumption

Year	Elasticity with respect to:				Year	Elasticity with respect to:			
	Labor	Structures	Equipment	IP		Labor	Structures	Equipment	IP
1948	0.8096	0.1253	0.0544	0.0108	1984	0.6029	0.2332	0.1192	0.0447
1949	0.7042	0.1912	0.0862	0.0184	1985	0.6119	0.2298	0.1102	0.0481
1950	0.8718	0.0432	0.0629	0.0221	1986	0.6390	0.2057	0.1037	0.0517
1951	0.8442	0.0645	0.0759	0.0153	1987	0.6559	0.1930	0.1027	0.0485
1952	0.7600	0.1365	0.0833	0.0203	1988	0.6608	0.1917	0.1024	0.0451
1953	0.7302	0.1726	0.0756	0.0216	1989	0.6471	0.1945	0.1040	0.0545
1954	0.7199	0.1735	0.0873	0.0194	1990	0.6512	0.1967	0.0979	0.0542
1955	0.8140	0.0842	0.0769	0.0249	1991	0.6321	0.2145	0.0997	0.0537
1956	0.8134	0.1030	0.0605	0.0231	1992	0.6561	0.1866	0.1022	0.0551
1957	0.7494	0.1508	0.0753	0.0245	1993	0.6757	0.1645	0.1013	0.0585
1958	0.6912	0.1984	0.0833	0.0271	1994	0.7024	0.1428	0.0994	0.0553
1959	0.7119	0.1761	0.0836	0.0283	1995	0.6627	0.1794	0.1016	0.0563
1960	0.6842	0.1961	0.0874	0.0323	1996	0.6784	0.1597	0.1037	0.0581
1961	0.7003	0.1758	0.0907	0.0332	1997	0.6645	0.1598	0.1137	0.0620
1962	0.7101	0.1699	0.0856	0.0344	1998	0.6852	0.1417	0.1099	0.0632
1963	0.7110	0.1691	0.0872	0.0327	1999	0.6988	0.1425	0.1057	0.0530
1964	0.7426	0.1348	0.0894	0.0332	2000	0.6821	0.1559	0.1051	0.0570
1965	0.7458	0.1328	0.0885	0.0329	2001	0.6935	0.1384	0.1061	0.0620
1966	0.7637	0.1156	0.0851	0.0356	2002	0.6838	0.1521	0.1025	0.0617
1967	0.7514	0.1334	0.0815	0.0337	2003	0.7013	0.1374	0.1023	0.0589
1968	0.7883	0.0893	0.0856	0.0367	2004	0.8061	0.0208	0.1044	0.0686
1969	0.7642	0.1149	0.0852	0.0357	2005	0.8092	0.0136	0.1119	0.0653
1970	0.7379	0.1408	0.0842	0.0372	2006	0.7411	0.1048	0.0916	0.0626
1971	0.7989	0.0641	0.0960	0.0410	2007	0.6879	0.1637	0.0905	0.0579
1972	0.7770	0.0924	0.0929	0.0378	2008	0.6841	0.1669	0.0864	0.0626
1973	0.8463	0.0181	0.1008	0.0349	2009	0.6050	0.2525	0.0831	0.0593
1974	0.9052	0.0106	0.0512	0.0329	2010	0.6501	0.1964	0.0906	0.0629
1975	0.7542	0.1474	0.0616	0.0368	2011	0.6898	0.1572	0.0882	0.0648
1976	0.7277	0.1485	0.0864	0.0374	2012	0.7117	0.1357	0.0885	0.0641
1977	0.8175	0.0443	0.0979	0.0403	2013	0.7656	0.0580	0.1085	0.0678
1978	0.8246	0.0426	0.0940	0.0388	2014	0.7150	0.1202	0.0968	0.0681
1979	0.8092	0.0562	0.0980	0.0367	2015	0.6934	0.1483	0.0919	0.0665
1980	0.7214	0.1538	0.0881	0.0367	2016	0.7108	0.1239	0.0976	0.0677
1981	0.6743	0.1721	0.1139	0.0397	2017	0.7186	0.1279	0.0881	0.0654
1982	0.5897	0.2484	0.1193	0.0426	2018	0.7263	0.1148	0.0878	0.0712
1983	0.5883	0.2541	0.1168	0.0408

Notes: This table shows the estimated values of the elasticities for the four factors of production - labor and three types of capital (structures, equipment, and IP) - in the baseline calculations of the paper using user costs to calculate capital costs. Proprietors income is split according to [Gomme and Rupert \(2004\)](#), all industries are included, and intellectual property is included as a type of capital. Details on those assumptions are available in the main text.