This is the svm workbook for ECE C147/C247 Assignment #2

Please follow the notebook linearly to implement a linear support vector machine.

Please print out the workbook entirely when completed.

We thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu). These are the functions in the cs231n folders and includes code to preprocess and show the images. The classifiers used are based off of code prepared for CS 231n as well.

The goal of this workbook is to give you experience with training an SVM classifier via gradient descent.

Importing libraries and data setup

```
In [1]: import numpy as np # for doing most of our calculations
import matplotlib.pyplot as plt# for plotting
from cs23ln.data_utils import load_CIFAR10 # function to load the CIFAR-
10 dataset.
import pdb

# Load matplotlib images inline
%matplotlib inline

# These are important for reloading any code you write in external .py f
iles.
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
n-ipython
%load_ext autoreload
%autoreload 2
```

```
In [2]: # Set the path to the CIFAR-10 data
    cifar10_dir = './cifar-10-batches-py' # You need to update this line
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# As a sanity check, we print out the size of the training and test dat
    a.
    print('Training data shape: ', X_train.shape)
    print('Training labels shape: ', y_train.shape)
    print('Test data shape: ', X_test.shape)
    print('Test labels shape: ', y_test.shape)
```

```
Training data shape: (50000, 32, 32, 3)
Training labels shape: (50000,)
Test data shape: (10000, 32, 32, 3)
Test labels shape: (10000,)
```

```
In [3]: # Visualize some examples from the dataset.
        # We show a few examples of training images from each class.
        classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse'
        , 'ship', 'truck']
        num_classes = len(classes)
        samples per class = 7
        for y, cls in enumerate(classes):
            idxs = np.flatnonzero(y train == y)
            idxs = np.random.choice(idxs, samples_per_class, replace=False)
            for i, idx in enumerate(idxs):
                plt_idx = i * num_classes + y + 1
                plt.subplot(samples_per_class, num_classes, plt_idx)
                plt.imshow(X_train[idx].astype('uint8'))
                plt.axis('off')
                if i == 0:
                    plt.title(cls)
        plt.show()
```



```
In [4]: # Split the data into train, val, and test sets. In addition we will
        # create a small development set as a subset of the training data;
        # we can use this for development so our code runs faster.
        num_training = 49000
        num validation = 1000
        num test = 1000
        num_dev = 500
        # Our validation set will be num validation points from the original
        # training set.
        mask = range(num training, num training + num validation)
        X_val = X_train[mask]
        y_val = y_train[mask]
        # Our training set will be the first num train points from the original
        # training set.
        mask = range(num training)
        X_train = X_train[mask]
        y_train = y_train[mask]
        # We will also make a development set, which is a small subset of
        # the training set.
        mask = np.random.choice(num training, num dev, replace=False)
        X_dev = X_train[mask]
        y dev = y train[mask]
        # We use the first num test points of the original test set as our
        # test set.
        mask = range(num_test)
        X test = X test[mask]
        y_test = y_test[mask]
        print('Train data shape: ', X_train.shape)
        print('Train labels shape: ', y_train.shape)
        print('Validation data shape: ', X_val.shape)
        print('Validation labels shape: ', y_val.shape)
        print('Test data shape: ', X_test.shape)
        print('Test labels shape: ', y_test.shape)
print('Dev data shape: ', X_dev.shape)
        print('Dev labels shape: ', y_dev.shape)
        Train data shape: (49000, 32, 32, 3)
        Train labels shape: (49000,)
        Validation data shape: (1000, 32, 32, 3)
        Validation labels shape: (1000,)
        Test data shape: (1000, 32, 32, 3)
        Test labels shape: (1000,)
        Dev data shape: (500, 32, 32, 3)
```

Dev labels shape: (500,)

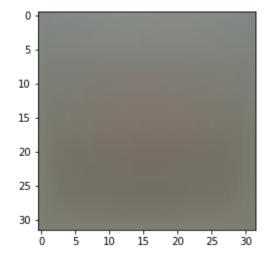
```
In [5]: # Preprocessing: reshape the image data into rows
X_train = np.reshape(X_train, (X_train.shape[0], -1))
X_val = np.reshape(X_val, (X_val.shape[0], -1))
X_test = np.reshape(X_test, (X_test.shape[0], -1))
X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))

# As a sanity check, print out the shapes of the data
print('Training data shape: ', X_train.shape)
print('Validation data shape: ', X_val.shape)
print('Test data shape: ', X_test.shape)
print('dev data shape: ', X_dev.shape)
```

Training data shape: (49000, 3072) Validation data shape: (1000, 3072) Test data shape: (1000, 3072) dev data shape: (500, 3072)

In [6]: # Preprocessing: subtract the mean image
 # first: compute the image mean based on the training data
 mean_image = np.mean(X_train, axis=0)
 print(mean_image[:10]) # print a few of the elements
 plt.figure(figsize=(4,4))
 plt.imshow(mean_image.reshape((32,32,3)).astype('uint8')) # visualize th
 e mean image
 plt.show()

[130.64189796 135.98173469 132.47391837 130.05569388 135.34804082 131.75402041 130.96055102 136.14328571 132.47636735 131.48467347]



In [7]: # second: subtract the mean image from train and test data
 X_train -= mean_image
 X_val -= mean_image
 X_test -= mean_image
 X_dev -= mean_image

```
In [8]: # third: append the bias dimension of ones (i.e. bias trick) so that our
    SVM
    # only has to worry about optimizing a single weight matrix W.
    X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
    X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
    X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
    X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])
    print(X_train.shape, X_val.shape, X_test.shape, X_dev.shape)
(49000, 3073) (1000, 3073) (1000, 3073) (500, 3073)
```

Question:

(1) For the SVM, we perform mean-subtraction on the data. However, for the KNN notebook, we did not. Why?

Answer:

(1) For the SVM, we need to normalize the data so that each feature has a similar range. This helps prevent one feature which has a broad range of values from governing the Euclidean distance. It also helps the gradient to act uniformly.

Training an SVM

The following cells will take you through building an SVM. You will implement its loss function, then subsequently train it with gradient descent. Finally, you will choose the learning rate of gradient descent to optimize its classification performance.

```
In [9]: from nndl.svm import SVM

In [10]: # Declare an instance of the SVM class.
    # Weights are initialized to a random value.
    # Note, to keep people's initial solutions consistent, we are going to u se a random seed.
    np.random.seed(1)
    num_classes = len(np.unique(y_train))
    num_features = X_train.shape[1]
    svm = SVM(dims=[num_classes, num_features])
```

SVM loss

```
In [11]: ## Implement the loss function for in the SVM class(nndl/svm.py), svm.lo
    ss()

print(y_train)
    loss = svm.loss(X_train, y_train)
    print('The training set loss is {}.'.format(loss))

# If you implemented the loss correctly, it should be 15569.98

[6 9 9 ... 4 9 3]
The training set loss is 15569.977915410193.
```

SVM gradient

```
In [12]: ## Calculate the gradient of the SVM class.
         # For convenience, we'll write one function that computes the loss
             and gradient together. Please modify svm.loss and grad(X, y).
         # You may copy and paste your loss code from svm.loss() here, and then
             use the appropriate intermediate values to calculate the gradient.
         loss, grad = svm.loss and grad(X dev,y dev)
         # Compare your gradient to a numerical gradient check.
         # You should see relative gradient errors on the order of 1e-07 or less
          if you implemented the gradient correctly.
         svm.grad check sparse(X dev, y dev, grad)
         numerical: -4.312075 analytic: -4.312075, relative error: 2.119391e-09
         numerical: 2.843858 analytic: 2.843857, relative error: 2.244579e-07
         numerical: -4.943769 analytic: -4.943770, relative error: 7.134826e-08
         numerical: 15.302841 analytic: 15.302842, relative error: 9.304742e-09
         numerical: 3.442246 analytic: 3.442246, relative error: 2.000714e-08
         numerical: 4.725199 analytic: 4.725198, relative error: 6.270475e-08
         numerical: -4.374034 analytic: -4.374033, relative error: 9.348043e-08
         numerical: -6.198758 analytic: -6.198758, relative error: 2.671336e-08
         numerical: -1.547739 analytic: -1.547739, relative error: 6.451178e-08
         numerical: -22.857156 analytic: -22.857157, relative error: 2.719112e-0
         8
```

A vectorized version of SVM

To speed things up, we will vectorize the loss and gradient calculations. This will be helpful for stochastic gradient descent.

```
In [13]: import time
```

```
In [14]:
         ## Implement sym.fast loss and grad which calculates the loss and gradie
         #
              WITHOUT using any for loops.
         # Standard loss and gradient
         tic = time.time()
         loss, grad = svm.loss_and_grad(X_dev, y_dev)
         toc = time.time()
         print('Normal loss / grad_norm: {} / {} computed in {}s'.format(loss, np
         .linalg.norm(grad, 'fro'), toc - tic))
         tic = time.time()
         loss vectorized, grad vectorized = svm.fast loss and grad(X dev, y dev)
         toc = time.time()
         print('Vectorized loss / grad: {} / {} computed in {}s'.format(loss_vect
         orized, np.linalg.norm(grad_vectorized, 'fro'), toc - tic))
         # The losses should match but your vectorized implementation should be m
         uch faster.
         print('difference in loss / grad: {} / {}'.format(loss - loss vectorized
         , np.linalg.norm(grad - grad_vectorized)))
         # You should notice a speedup with the same output, i.e., differences on
         the order of 1e-12
```

```
Normal loss / grad_norm: 16882.900643099136 / 2286.977873936257 compute d in 0.08017802238464355s

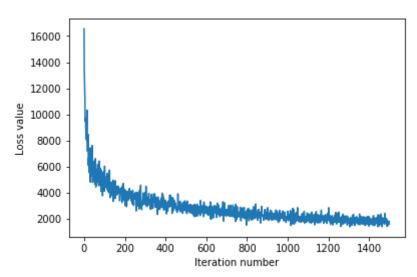
Vectorized loss / grad: 16882.90064309911 / 2286.977873936257 computed in 0.006361961364746094s

difference in loss / grad: 2.546585164964199e-11 / 4.320403166978369e-1
```

Stochastic gradient descent

We now implement stochastic gradient descent. This uses the same principles of gradient descent we discussed in class, however, it calculates the gradient by only using examples from a subset of the training set (so each gradient calculation is faster).

```
iteration 0 / 1500: loss 16557.38000190916
iteration 100 / 1500: loss 4701.089451272714
iteration 200 / 1500: loss 4017.333137942788
iteration 300 / 1500: loss 3681.9226471953625
iteration 400 / 1500: loss 2732.616437398899
iteration 500 / 1500: loss 2786.6378424645054
iteration 600 / 1500: loss 2837.0357842782664
iteration 700 / 1500: loss 2206.2348687399317
iteration 800 / 1500: loss 2269.03882411698
iteration 900 / 1500: loss 2543.23781538592
iteration 1000 / 1500: loss 2566.6921357268266
iteration 1100 / 1500: loss 2182.068905905164
iteration 1200 / 1500: loss 1861.1182244250447
iteration 1300 / 1500: loss 1982.9013858528251
iteration 1400 / 1500: loss 1927.5204158582114
That took 3.085602045059204s
```



Evaluate the performance of the trained SVM on the validation data.

Optimize the SVM

Note, to make things faster and simpler, we won't do k-fold cross-validation, but will only optimize the hyperparameters on the validation dataset (X_val, y_val).

```
In [18]:
       # ================== #
        # YOUR CODE HERE:
           Train the SVM with different learning rates and evaluate on the
        #
             validation data.
        #
           Report:
        #
             - The best learning rate of the ones you tested.
             - The best VALIDATION accuracy corresponding to the best VALIDATIO
        N error.
        #
        #
           Select the SVM that achieved the best validation error and report
        #
             its error rate on the test set.
           Note: You do not need to modify SVM class for this section
        learning_rates = np.array([1e-7, 5e-7, 1e-6, 5e-6, 1e-5, 5e-5, 1e-4, 5e-
        4, 1e-3, 5e-3, 1e-2, 5e-2, 1e-1, 5e-1, 1, 5, 10])
        val accs = np.zeros like(learning rates)
        for idx, learning rate in enumerate(learning rates):
           svm.train(X train, y train, learning rate=learning rate)
           y val pred = svm.predict(X val)
           val_accs[idx] = np.mean(np.equal(y val, y val pred))
        best val acc idx = np.argmax(val accs)
        best val acc = val accs[best val acc idx]
        best_learning rate = learning rates[best_val_acc_idx]
        print("The best learning rate is {}, with a validation accuracy of {}.".
        format(best_learning_rate, best_val_acc))
        svm.train(X train, y train, learning rate=best learning rate)
        y_test_pred = svm.predict(X_test)
        test_acc = np.mean(np.equal(y_test, y_test_pred))
        print("The best learning rate of {} had a test error of {}.".format(best
        _learning_rate, 1 - test_acc))
        # END YOUR CODE HERE
```

The best learning rate is 0.05, with a validation accuracy of 0.317. The best learning rate of 0.05 had a test error of 0.74.