This is the k-nearest neighbors workbook for ECE C147/C247 Assignment #2

Please follow the notebook linearly to implement k-nearest neighbors.

Please print out the workbook entirely when completed.

We thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu). These are the functions in the cs231n folders and code in the jupyer notebook to preprocess and show the images. The classifiers used are based off of code prepared for CS 231n as well.

The goal of this workbook is to give you experience with the data, training and evaluating a simple classifier, k-fold cross validation, and as a Python refresher.

Import the appropriate libraries

```
In [1]: import numpy as np # for doing most of our calculations
import matplotlib.pyplot as plt # for plotting
from cs231n.data_utils import load_CIFAR10 # function to load the CIFAR-
10 dataset.

# Load matplotlib images inline
%matplotlib inline

# These are important for reloading any code you write in external .py f
iles.
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
n-ipython
%load_ext autoreload
%autoreload 2
```

```
In [2]: # Set the path to the CIFAR-10 data
    cifar10_dir = '/Users/jackzhang/GoogleDrive/UCLA/Academics/Junior/Q2/EC
    ENGR C247/HW2/cifar-10-batches-py' # You need to update this line
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# As a sanity check, we print out the size of the training and test dat
    a.
    print('Training data shape: ', X_train.shape)
    print('Training labels shape: ', y_train.shape)
    print('Test data shape: ', X_test.shape)
    print('Test labels shape: ', y_test.shape)
Training data shape: (50000, 32, 32, 3)
```

Training data shape: (50000, 32, 32, 3 Training labels shape: (50000,) Test data shape: (10000, 32, 32, 3) Test labels shape: (10000,)

```
In [3]: # Visualize some examples from the dataset.
        # We show a few examples of training images from each class.
        classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse'
        , 'ship', 'truck']
        num classes = len(classes)
        samples per class = 7
        for y, cls in enumerate(classes):
            idxs = np.flatnonzero(y train == y)
            idxs = np.random.choice(idxs, samples_per_class, replace=False)
            for i, idx in enumerate(idxs):
                plt_idx = i * num_classes + y + 1
                plt.subplot(samples_per_class, num_classes, plt_idx)
                plt.imshow(X_train[idx].astype('uint8'))
                plt.axis('off')
                if i == 0:
                    plt.title(cls)
        plt.show()
```



```
In [4]: # Subsample the data for more efficient code execution in this exercise
    num_training = 5000
    mask = list(range(num_training))
    X_train = X_train[mask]
    y_train = y_train[mask]

    num_test = 500
    mask = list(range(num_test))
    X_test = X_test[mask]
    y_test = y_test[mask]

# Reshape the image data into rows
    X_train = np.reshape(X_train, (X_train.shape[0], -1))
    X_test = np.reshape(X_test, (X_test.shape[0], -1))
    print(X_train.shape, X_test.shape)
```

(5000, 3072) (500, 3072)

K-nearest neighbors

In the following cells, you will build a KNN classifier and choose hyperparameters via k-fold cross-validation.

```
In [5]: # Import the KNN class
    from nndl import KNN

In [6]: # Declare an instance of the knn class.
    knn = KNN()

# Train the classifier.
    # We have implemented the training of the KNN classifier.
    # Look at the train function in the KNN class to see what this does.
    knn.train(X=X_train, y=y_train)
```

Questions

- (1) Describe what is going on in the function knn.train().
- (2) What are the pros and cons of this training step?

Answers

- (1) The train function is involves storing the training data.
- (2) The training step is fast, which may be a pro, but it does not do enough of the heavy work. Instead, it leaves much of the work to be done during the testing step, which ideally should be fast and efficient.

KNN prediction

In the following sections, you will implement the functions to calculate the distances of test points to training points, and from this information, predict the class of the KNN.

```
In [7]: # Implement the function compute_distances() in the KNN class.
# Do not worry about the input 'norm' for now; use the default definitio
n of the norm
# in the code, which is the 2-norm.
# You should only have to fill out the clearly marked sections.

import time
time_start =time.time()
dists_L2 = knn.compute_distances(X=X_test)

print('Time to run code: {}'.format(time.time()-time_start))
print('Frobenius norm of L2 distances: {}'.format(np.linalg.norm(dists_L2, 'fro')))
```

Time to run code: 40.310245752334595 Frobenius norm of L2 distances: 7906696.077040902

Really slow code

Note: This probably took a while. This is because we use two for loops. We could increase the speed via vectorization, removing the for loops.

If you implemented this correctly, evaluating np.linalg.norm(dists_L2, 'fro') should return: ~7906696

KNN vectorization

The above code took far too long to run. If we wanted to optimize hyperparameters, it would be time-expensive. Thus, we will speed up the code by vectorizing it, removing the for loops.

```
In [8]: # Implement the function compute_L2_distances_vectorized() in the KNN cl
    ass.
# In this function, you ought to achieve the same L2 distance but WITHOU
    T any for loops.
# Note, this is SPECIFIC for the L2 norm.

time_start =time.time()
    dists_L2_vectorized = knn.compute_L2_distances_vectorized(X=X_test)
    print('Time to run code: {}'.format(time.time()-time_start))
    print('Difference in L2 distances between your KNN implementations (shou ld be 0): {}'.format(np.linalg.norm(dists_L2 - dists_L2_vectorized, 'fr o')))
```

Time to run code: 0.21688604354858398
Difference in L2 distances between your KNN implementations (should be 0): 0.0

Speedup

Depending on your computer speed, you should see a 10-100x speed up from vectorization. On our computer, the vectorized form took 0.36 seconds while the naive implementation took 38.3 seconds.

Implementing the prediction

Now that we have functions to calculate the distances from a test point to given training points, we now implement the function that will predict the test point labels.

```
In [9]: # Implement the function predict labels in the KNN class.
     # Calculate the training error (num incorrect / total samples)
        from running knn.predict labels with k=1
     error = 1
     # ================= #
     # YOUR CODE HERE:
        Calculate the error rate by calling predict labels on the test
        data with k = 1. Store the error rate in the variable error.
     y pred = knn.predict labels(dists_L2_vectorized)
     hits = np.count_nonzero(y_pred == y_test)
     error = (num test - hits)/num test
     # END YOUR CODE HERE
     print(error)
     0.726
```

If you implemented this correctly, the error should be: 0.726.

This means that the k-nearest neighbors classifier is right 27.4% of the time, which is not great, considering that chance levels are 10%.

Optimizing KNN hyperparameters

In this section, we'll take the KNN classifier that you have constructed and perform cross-validation to choose a best value of k, as well as a best choice of norm.

Create training and validation folds

First, we will create the training and validation folds for use in k-fold cross validation.

```
# Create the dataset folds for cross-valdiation.
In [10]:
      num folds = 5
      X_train_folds = []
      y train folds = []
      # ================= #
      # YOUR CODE HERE:
         Split the training data into num folds (i.e., 5) folds.
         X train folds is a list, where X train folds[i] contains the
      #
           data points in fold i.
      #
         y train folds is also a list, where y train folds[i] contains
           the corresponding labels for the data in X train folds[i]
      X_train_folds = np.split(X_train, num_folds)
      y_train_folds = np.split(y_train, num_folds)
      # END YOUR CODE HERE
```

Optimizing the number of nearest neighbors hyperparameter.

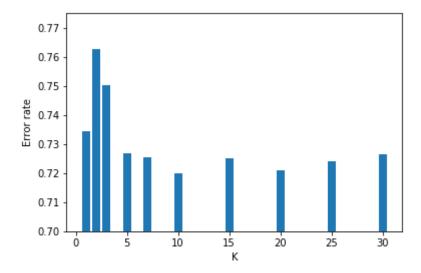
In this section, we select different numbers of nearest neighbors and assess which one has the lowest k-fold cross validation error.

Questions:

- (1) What value of k is best amongst the tested k's?
- (2) What is the cross-validation error for this value of k?

```
In [11]: time_start =time.time()
        ks = [1, 2, 3, 5, 7, 10, 15, 20, 25, 30]
        # ================= #
        # YOUR CODE HERE:
           Calculate the cross-validation error for each k in ks, testing
        #
           the trained model on each of the 5 folds. Average these errors
        #
           together and make a plot of k vs. cross-validation error. Since
        #
           we are assuming L2 distance here, please use the vectorized code!
           Otherwise, you might be waiting a long time.
        from collections import defaultdict
        errors = defaultdict(int)
        print("Doing k-fold cross validation...")
        for i in range(num folds):
           X train k = np.concatenate( X train folds[0:i] + X train folds[i+1:n
        um folds])
           X_test_k = X_train_folds[i]
           y train k = np.concatenate( y train folds[0:i] + y train folds[i+1:n
        um_folds] )
           y_test_k = y_train_folds[i]
           num_test_k = len(y_test_k)
           for k in ks:
               knn.train(X=X_train_k, y=y_train_k)
               dists kfold = knn.compute L2 distances vectorized(X=X test k)
               y pred = knn.predict labels(dists kfold, k=k)
               hits = np.count_nonzero(y_pred == y_test_k)
               error = (num test k - hits)/num test k
               errors[k] += error
        error list = []
        for k, v in errors.items():
           errors[k] /= num_folds
           error list.append(errors[k])
        f = plt.figure()
        ax = f.gca()
        ax.bar(ks, error_list, align='center')
        ax.set_ylim(0.7, 0.775)
        ax.set_xlabel("K")
        ax.set_ylabel("Error rate")
        # END YOUR CODE HERE
        best idx = np.argmin(error list)
        print('Lowest error rate achieved by %d folds, with an rate of: %.2f' %
        (ks[best idx], error list[best idx]))
        print('Computation time: %.2f'%(time.time()-time_start))
```

Doing k-fold cross validation... Lowest error rate achieved by 10 folds, with an rate of: 0.72 Computation time: 26.82



Answers:

- (1) K = 10 was the best among the tested K's.
- (2) K = 10's cross validation error was 0.72.

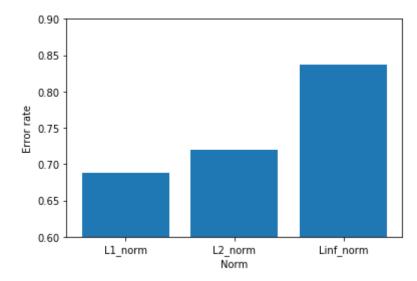
Optimizing the norm

Next, we test three different norms (the 1, 2, and infinity norms) and see which distance metric results in the best cross-validation performance.

```
In [12]: time_start =time.time()
        L1_norm = lambda x: np.linalg.norm(x, ord=1)
        L2_norm = lambda x: np.linalg.norm(x, ord=2)
        Linf norm = lambda x: np.linalq.norm(x, ord= np.inf)
        norms = [L1_norm, L2_norm, Linf_norm]
        # YOUR CODE HERE:
            Calculate the cross-validation error for each norm in norms, testing
            the trained model on each of the 5 folds. Average these errors
         #
            together and make a plot of the norm used vs the cross-validation er
        ror
        #
            Use the best cross-validation k from the previous part.
         #
         #
           Feel free to use the compute distances function. We're testing just
            three norms, but be advised that this could still take some time.
         #
            You're welcome to write a vectorized form of the L1- and Linf- norms
            to speed this up, but it is not necessary.
         errors = defaultdict(int)
        progress_total = 15
        current progress = 0
        print("Doing k-fold cross validation...")
        for i in range(num_folds):
            X train k = np.concatenate( X train folds[0:i] + X train folds[i+1:n
        um folds])
            X_test_k = X_train_folds[i]
            y train k = np.concatenate( y train folds[0:i] + y train folds[i+1:n
        um folds | )
            y_test_k = y_train_folds[i]
            num_test_k = len(y_test_k)
            for norm in norms:
                print("Training progress: %.1f%%" % (current progress/progress t
        otal * 100))
                current_progress += 1
                knn.train(X=X_train_k, y=y_train_k)
                dists kfold = knn.compute distances(X=X test k, norm=norm)
                y pred = knn.predict labels(dists kfold, k=10)
                hits = np.count_nonzero(y_pred == y_test_k)
                error = (num_test_k - hits)/num_test_k
                errors[norm] += error
        print("Training progress: 100%. Done.")
        error_list = []
        for k, v in errors.items():
            errors[k] /= num folds
            error_list.append(errors[k])
        f = plt.figure()
        ax = f.gca()
        norm_labels = ["L1_norm", "L2_norm", "Linf_norm"]
```

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```
Doing k-fold cross validation...
Training progress: 0.0%
Training progress: 6.7%
Training progress: 13.3%
Training progress: 20.0%
Training progress: 26.7%
Training progress: 33.3%
Training progress: 40.0%
Training progress: 46.7%
Training progress: 53.3%
Training progress: 60.0%
Training progress: 66.7%
Training progress: 73.3%
Training progress: 80.0%
Training progress: 86.7%
Training progress: 93.3%
Training progress: 100%. Done.
Lowest error rate achieved by the L1 norm norm, with an rate of: 0.69
Computation time: 955.32
```



Questions:

- (1) What norm has the best cross-validation error?
- (2) What is the cross-validation error for your given norm and k?

Answers:

- (1) The L1 norm had the lowest cross-validation error.
- (2) Give K = 10 and norm = L1, the cross validation error is 0.69, meaning that the KNN model is able to predict the class of an image with 31% accuracy. This constitutes an 21% improvement over random guessing.

Evaluating the model on the testing dataset.

Now, given the optimal k and norm you found in earlier parts, evaluate the testing error of the k-nearest neighbors model.

```
In [13]:
      error = 1
      # YOUR CODE HERE:
        Evaluate the testing error of the k-nearest neighbors classifier
        for your optimal hyperparameters found by 5-fold cross-validation.
      # ------ #
      knn.train(X=X_train, y=y_train)
      dists_kfold = knn.compute_distances(X=X_test, norm=L1_norm)
      y pred = knn.predict labels(dists kfold, k=10)
      hits = np.count nonzero(y pred == y test)
      error = (num_test - hits)/num_test
      # END YOUR CODE HERE
      # ------ #
      print('Error rate achieved: {}'.format(error))
```

Error rate achieved: 0.722

Question:

How much did your error improve by cross-validation over naively choosing k=1 and using the L2-norm?

Answer:

My error imped by 0.004.

```
import numpy as np
import pdb
111111
This code was based off of code from cs231n at Stanford University,
and modified for ECE C147/C247 at UCLA.
class KNN(object):
  def __init__(self):
    pass
  def train(self, X, y):
        Inputs:
        - X is a numpy array of size (num examples, D)
        - y is a numpy array of size (num_examples, )
    self.X_train = X
    self.y_train = y
  def compute_distances(self, X, norm=None):
    Compute the distance between each test point in X and each
training point
    in self.X_train.
    Inputs:
    - X: A numpy array of shape (num_test, D) containing test data.
        - norm: the function with which the norm is taken.
    Returns:
    - dists: A numpy array of shape (num test, num train) where
dists[i, j]
      is the Euclidean distance between the ith test point and the jth
training
     point.
    if norm is None:
      norm = lambda x: np.sqrt(np.sum(x**2))
      \#norm = 2
    num test = X.shape[0]
    num train = self.X_train.shape[0]
    dists = np.zeros((num_test, num_train))
    for i in np.arange(num_test):
      for j in np.arange(num_train):
```

```
#
______#
       # YOUR CODE HERE:
              #
                 Compute the distance between the ith test point
and the jth
          training point using norm(), and store the result in
dists[i, j].
______#
      dists[i, j] = norm(X[i] - self.X train[j])
      pass
              #
              # END YOUR CODE HERE
              #
   return dists
 def compute_L2_distances_vectorized(self, X):
   Compute the distance between each test point in X and each
training point
   in self.X_train WITHOUT using any for loops.
   - X: A numpy array of shape (num_test, D) containing test data.
   - dists: A numpy array of shape (num_test, num_train) where
     is the Euclidean distance between the ith test point and the jth
training
     point.
   min
   num_test = X.shape[0]
   num train = self.X train.shape[0]
   dists = np.zeros((num test, num train))
       #
______#
       # YOUR CODE HERE:
          Compute the L2 distance between the ith test point and the
jth
      training point and store the result in dists[i, j]. You may
              NOT use a for loop (or list comprehension). You may
only use
              numpy operations.
```

```
#
                 HINT: use broadcasting. If you have a shape (N,1)
array and
            a shape (M,) array, adding them together produces a shape
(N, M)
        #
            array.
        #
    dists = np.sqrt(-2 * X.dot(self.X_train.T) +
np.sum(self.X_train**2, axis=1) + np.sum(X**2, axis=1)[:, np.newaxis])
    pass
        #
        # END YOUR CODE HERE
        #
    return dists
  def predict_labels(self, dists, k=1):
    Given a matrix of distances between test points and training
points,
    predict a label for each test point.
    Inputs:
    - dists: A numpy array of shape (num test, num train) where
dists[i, j]
      gives the distance betwen the ith test point and the jth
training point.
    Returns:
    y: A numpy array of shape (num test,) containing predicted
labels for the
      test data, where y[i] is the predicted label for the test point
X[i].
    .....
    num test = dists.shape[0]
    y_pred = np.zeros(num_test)
    for i in np.arange(num_test):
      # A list of length k storing the labels of the k nearest
neighbors to
      # the ith test point.
      closest_y = []
          #
```

```
______#
       # YOUR CODE HERE:
          Use the distances to calculate and then store the labels
of
          the k-nearest neighbors to the ith test point.
function
       #
          numpy.argsort may be useful.
       #
          After doing this, find the most common label of the k-
nearest
          neighbors. Store the predicted label of the ith
training example
       #
          as y_pred[i]. Break ties by choosing the smaller label.
       #
                             ========= #
    sortedIdxs = np.argsort(dists[i,])
    closest_y = self.y_train[sortedIdxs[:k]]
    y_pred[i] = np.argmax(np.bincount(closest_y))
    pass
______ #
       # END YOUR CODE HERE
______#
   return y_pred
```

This is the softmax workbook for ECE C147/C247 Assignment #2

Please follow the notebook linearly to implement a softmax classifier.

Please print out the workbook entirely when completed.

We thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu). These are the functions in the cs231n folders and code in the jupyer notebook to preprocess and show the images. The classifiers used are based off of code prepared for CS 231n as well.

The goal of this workbook is to give you experience with training a softmax classifier.

```
In [1]: import random
   import numpy as np
   from cs231n.data_utils import load_CIFAR10
   import matplotlib.pyplot as plt

%matplotlib inline
%load_ext autoreload
%autoreload 2
```

```
def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1
000, num dev=500):
    Load the CIFAR-10 dataset from disk and perform preprocessing to pre
pare
    it for the linear classifier. These are the same steps as we used fo
r the
    SVM, but condensed to a single function.
    # Load the raw CIFAR-10 data
    cifar10_dir = './cifar-10-batches-py' # You need to update this line
    X train, y train, X test, y test = load CIFAR10(cifar10 dir)
    # subsample the data
    mask = list(range(num_training, num_training + num_validation))
    X_val = X_train[mask]
    y_val = y_train[mask]
    mask = list(range(num_training))
    X_train = X_train[mask]
    y train = y train[mask]
    mask = list(range(num_test))
    X_{\text{test}} = X_{\text{test}}[mask]
    y_test = y_test[mask]
    mask = np.random.choice(num_training, num_dev, replace=False)
    X dev = X train[mask]
    y_dev = y train[mask]
    # Preprocessing: reshape the image data into rows
    X_train = np.reshape(X_train, (X_train.shape[0], -1))
    X_{val} = np.reshape(X_{val}, (X_{val.shape[0]}, -1))
    X_test = np.reshape(X_test, (X_test.shape[0], -1))
    X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))
    # Normalize the data: subtract the mean image
    mean_image = np.mean(X_train, axis = 0)
    X_train -= mean_image
    X_val -= mean_image
    X_test -= mean_image
    X dev -= mean image
    # add bias dimension and transform into columns
    X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
    X val = np.hstack([X val, np.ones((X val.shape[0], 1))])
    X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
    X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])
    return X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev
# Invoke the above function to get our data.
X train, y train, X val, y val, X test, y test, X dev, y dev = get CIFAR
10 data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y val.shape)
print('Test data shape: ', X_test.shape)
```

```
print('Test labels shape: ', y_test.shape)
print('dev data shape: ', X_dev.shape)
print('dev labels shape: ', y_dev.shape)

Train data shape: (49000, 3073)
Train labels shape: (49000,)
Validation data shape: (1000, 3073)
Validation labels shape: (1000,)
Test data shape: (1000, 3073)
Test labels shape: (1000,)
dev data shape: (500, 3073)
dev labels shape: (500,)
```

Training a softmax classifier.

The following cells will take you through building a softmax classifier. You will implement its loss function, then subsequently train it with gradient descent. Finally, you will choose the learning rate of gradient descent to optimize its classification performance.

```
In [4]: from nndl import Softmax
In [15]: # Declare an instance of the Softmax class.
# Weights are initialized to a random value.
# Note, to keep people's first solutions consistent, we are going to use a random seed.

np.random.seed(1)

num_classes = len(np.unique(y_train))
num_features = X_train.shape[1]

softmax = Softmax(dims=[num_classes, num_features])
```

Softmax loss

```
In [16]: ## Implement the loss function of the softmax using a for loop over
# the number of examples
loss = softmax.loss(X_train, y_train)
In [17]: print(loss)
2.327760702804897
```

Question:

You'll notice the loss returned by the softmax is about 2.3 (if implemented correctly). Why does this make sense?

Answer:

You fill this out.

Softmax gradient

```
In [33]:
         ## Calculate the gradient of the softmax loss in the Softmax class.
         # For convenience, we'll write one function that computes the loss
             and gradient together, softmax.loss and grad(X, y)
         # You may copy and paste your loss code from softmax.loss() here, and th
         en
         #
             use the appropriate intermediate values to calculate the gradient.
         loss, grad = softmax.loss_and_grad(X_dev,y_dev)
         # Compare your gradient to a gradient check we wrote.
         # You should see relative gradient errors on the order of 1e-07 or less
          if you implemented the gradient correctly.
         softmax.grad check sparse(X dev, y dev, grad)
         numerical: 0.562437 analytic: 0.748704, relative error: 1.420647e-01
         numerical: 0.305438 analytic: -0.379973, relative error: 1.000000e+00
         numerical: -3.502289 analytic: -1.823858, relative error: 3.151304e-01
         numerical: -0.365661 analytic: -0.107569, relative error: 5.453823e-01
         numerical: 0.390667 analytic: -0.102664, relative error: 1.000000e+00
         numerical: -2.804612 analytic: -1.763484, relative error: 2.279130e-01
         numerical: -1.706104 analytic: 2.509280, relative error: 1.000000e+00
         numerical: 0.480570 analytic: -0.732089, relative error: 1.000000e+00
         numerical: -1.176266 analytic: -0.280261, relative error: 6.151659e-01
         numerical: -1.647541 analytic: 1.179013, relative error: 1.000000e+00
```

A vectorized version of Softmax

To speed things up, we will vectorize the loss and gradient calculations. This will be helpful for stochastic gradient descent.

```
In [31]: import time
```

```
In [40]:
         ## Implement softmax.fast loss and grad which calculates the loss and gr
              WITHOUT using any for loops.
         # Standard loss and gradient
         tic = time.time()
         loss, grad = softmax.loss_and_grad(X_dev, y_dev)
         toc = time.time()
         print('Normal loss / grad_norm: {} / {} computed in {}s'.format(loss, np
         .linalg.norm(grad, 'fro'), toc - tic))
         tic = time.time()
         loss vectorized, grad vectorized = softmax.fast loss and grad(X dev, y d
         ev)
         toc = time.time()
         print('Vectorized loss / grad: {} / {} computed in {}s'.format(loss_vect
         orized, np.linalg.norm(grad_vectorized, 'fro'), toc - tic))
         # The losses should match but your vectorized implementation should be m
         uch faster.
         print('difference in loss / grad: {} /{} '.format(loss - loss_vectorized
         , np.linalg.norm(grad - grad_vectorized)))
         # You should notice a speedup with the same output.
```

```
Normal loss / grad_norm: 1.843227423994661 / 355.66429796093706 compute d in 0.034364938735961914s

Vectorized loss / grad: 1.8432274239946609 / 321.1914085995837 computed in 0.003840923309326172s

difference in loss / grad: 2.220446049250313e-16 /427.1678171924219
```

Stochastic gradient descent

We now implement stochastic gradient descent. This uses the same principles of gradient descent we discussed in class, however, it calculates the gradient by only using examples from a subset of the training set (so each gradient calculation is faster).

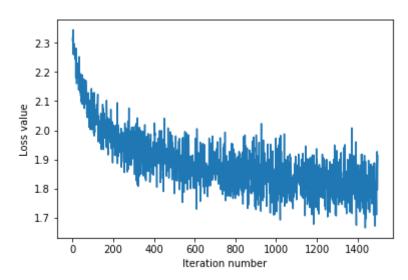
Question:

How should the softmax gradient descent training step differ from the svm training step, if at all?

Answer:

You fill this out.

```
iteration 0 / 1500: loss 2.316168370885791
iteration 100 / 1500: loss 2.116057123972999
iteration 200 / 1500: loss 1.9870478571324697
iteration 300 / 1500: loss 1.9791564604652032
iteration 400 / 1500: loss 1.882831676356327
iteration 500 / 1500: loss 1.7824244670893632
iteration 600 / 1500: loss 1.8007030338381145
iteration 700 / 1500: loss 1.8358270212594863
iteration 800 / 1500: loss 1.8114792230132881
iteration 900 / 1500: loss 1.7743496237590566
iteration 1000 / 1500: loss 1.8227673260549329
iteration 1100 / 1500: loss 1.7615025897697387
iteration 1200 / 1500: loss 1.8958686538899827
iteration 1300 / 1500: loss 1.8350510961395958
iteration 1400 / 1500: loss 1.8548663975072008
That took 8.6178719997406s
```



Evaluate the performance of the trained softmax classifier on the validation data.

```
In [23]: ## Implement softmax.predict() and use it to compute the training and te
    sting error.

y_train_pred = softmax.predict(X_train)
    print('training accuracy: {}'.format(np.mean(np.equal(y_train,y_train_pr
    ed), )))
    y_val_pred = softmax.predict(X_val)
    print('validation accuracy: {}'.format(np.mean(np.equal(y_val, y_val_pre
    d)), ))

training accuracy: 0.3821428571428571
```

training accuracy: 0.3821428571428571 validation accuracy: 0.39

Optimize the softmax classifier

You may copy and paste your optimization code from the SVM here.

```
In [26]: np.finfo(float).eps
```

Out[26]: 2.220446049250313e-16

```
In [41]:
       # ----- #
        # YOUR CODE HERE:
           Train the Softmax classifier with different learning rates and
        #
             evaluate on the validation data.
        #
           Report:
             - The best learning rate of the ones you tested.
             - The best validation accuracy corresponding to the best validatio
        n error.
        #
        #
           Select the softmax that achieved the best validation error and repor
        t
             its error rate on the test set.
        learning_rates = np.array([1e-7, 5e-7, 1e-6, 5e-6, 1e-5, 5e-5, 1e-4, 5e-
        4, 1e-3, 5e-3, 1e-2, 5e-2, 1e-1, 5e-1, 1, 5, 10])
       val accs = np.zeros like(learning rates)
        for idx, learning_rate in enumerate(learning_rates):
           softmax.train(X train, y train, learning rate=learning rate)
           y val pred = softmax.predict(X val)
           val_accs[idx] = np.mean(np.equal(y val, y val pred))
       best val acc idx = np.argmax(val accs)
        best val acc = val accs[best val acc idx]
       best_learning rate = learning rates[best_val_acc_idx]
       print("The best learning rate is {}, with a validation accuracy of {}.".
        format(best_learning_rate, best_val_acc))
        softmax.train(X_train, y_train, learning_rate=best learning_rate)
       y_test_pred = softmax.predict(X_test)
        test_acc = np.mean(np.equal(y_test, y_test_pred))
       print("The best learning rate of {} had a test error of {}.".format(best
        _learning_rate, 1 - test_acc))
        # END YOUR CODE HERE
```

```
/Users/jackzhang/GoogleDrive/UCLA/Academics/Junior/Q2/EC ENGR C247/HW2/
nndl/softmax.py:143: RuntimeWarning: divide by zero encountered in log
  loss = np.sum(np.log(np.sum(np.exp(scores).T, axis=0)) - scores[selec
tor]) / num_train
/Users/jackzhang/GoogleDrive/UCLA/Academics/Junior/Q2/EC ENGR C247/HW2/
nndl/softmax.py:147: RuntimeWarning: invalid value encountered in true_
divide
  temp = e_exp_a/sums[:, np.newaxis]
/Users/jackzhang/GoogleDrive/UCLA/Academics/Junior/Q2/EC ENGR C247/HW
2/.env/lib/python3.6/site-packages/numpy/core/_methods.py:26: RuntimeWa
rning: invalid value encountered in reduce
  return umr_maximum(a, axis, None, out, keepdims)
The best learning rate is 5e-07, with a validation accuracy of 0.356.
```

The best learning rate of 5e-07 had a test error of 0.646.

```
import numpy as np
class Softmax(object):
  def init (self, dims=[10, 3073]):
   self.init_weights(dims=dims)
  def init weights(self, dims):
       Initializes the weight matrix of the Softmax classifier.
       Note that it has shape (C, D) where C is the number of
       classes and D is the feature size.
   self.W = np.random.normal(size=dims) * 0.0001
  def loss(self, X, y):
   Calculates the softmax loss.
   Inputs have dimension D, there are C classes, and we operate on
minibatches
   of N examples.
   Inputs:
   - X: A numpy array of shape (N, D) containing a minibatch of data.
   - y: A numpy array of shape (N,) containing training labels; y[i]
= c means
     that X[i] has label c, where 0 \le c < C.
   Returns a tuple of:

    loss as single float

   .....
   # Initialize the loss to zero.
   loss = 0.0
   #
   # YOUR CODE HERE:
           Calculate the normalized softmax loss. Store it as the
variable loss.
       (That is, calculate the sum of the losses of all the training
   #
       set margins, and then normalize the loss by the number of
               training examples.)
   #
   num_train = X.shape[0]
   num_classes = self.W.shape[0]
   for i in np.arange(num_train):
```

```
cum = 0
      aix = self.W[y[i]].dot(X[i])
      logk = -np.max(aix)
      for j in np.arange(num_classes):
         cum += np.exp(self.W[j].dot(X[i]) + logk)
      loss += np.log(cum) - (aix + logk)
   loss /= num_train
   # END YOUR CODE HERE
   return loss
 def loss_and_grad(self, X, y):
       Same as self.loss(X, y), except that it also returns the
gradient.
       Output: grad -- a matrix of the same dimensions as W
containing
             the gradient of the loss with respect to W.
       .....
   # Initialize the loss and gradient to zero.
   loss = 0.0
   grad = np.zeros_like(self.W)
   #
   # YOUR CODE HERE:
          Calculate the softmax loss and the gradient. Store the
gradient
          as the variable grad.
   #
   num train = X.shape[0]
   num_classes = self.W.shape[0]
   for i in np.arange(num_train):
      cum = 0
      aix = self.W[y[i]].dot(X[i])
      logk = -np.max(aix)
```

```
for j in np.arange(num classes):
           cum += np.exp(self.W[j].dot(X[i]) + logk)
       loss += np.log(cum) - (aix + logk)
       qrad[y[i]] = X[i]
    loss /= num train
   grad /= num_train
   # END YOUR CODE HERE
    return loss, grad
  def grad_check_sparse(self, X, y, your_grad, num_checks=10, h=1e-5):
    sample a few random elements and only return numerical
    in these dimensions.
    .....
    for i in np.arange(num_checks):
      ix = tuple([np.random.randint(m) for m in self.W.shape])
     oldval = self.W[ix]
     self.W[ix] = oldval + h # increment by h
     fxph = self.loss(X, y)
      self.W[ix] = oldval - h # decrement by h
     fxmh = self.loss(X,y) # evaluate f(x - h)
     self.W[ix] = oldval # reset
     qrad numerical = (fxph - fxmh) / (2 * h)
     grad_analytic = your_grad[ix]
      rel error = abs(grad numerical - grad analytic) /
(abs(grad_numerical) + abs(grad_analytic))
     print('numerical: %f analytic: %f, relative error: %e' %
(grad numerical, grad analytic, rel error))
  def fast_loss_and_grad(self, X, y):
   A vectorized implementation of loss_and_grad. It shares the same
        inputs and ouptuts as loss and grad.
    .....
    loss = 0.0
   grad = np.zeros(self.W.shape) # initialize the gradient as zero
   #
```

```
# YOUR CODE HERE:
            Calculate the softmax loss and gradient WITHOUT any for
loops.
   # =========
#
   num train = X.shape[0]
    selector = np.arange(num train), y
    scores = X.dot(self.W.T)
    scores -= np.max(scores)
    loss = np.sum(np.log(np.sum(np.exp(scores).T, axis=0)) -
scores[selector]) / num_train
    e_exp_a = np.exp(scores)
    sums = np.sum(e_exp_a, axis=1)
    temp = e exp a/sums[:, np.newaxis]
    temp[selector] -= 1
   grad = temp.T.dot(X) / num_train
   #
    # END YOUR CODE HERE
    return loss, grad
  def train(self, X, y, learning_rate=1e-3, num_iters=100,
           batch_size=200, verbose=False):
   .....
   Train this linear classifier using stochastic gradient descent.
   Inputs:
   - X: A numpy array of shape (N, D) containing training data; there
are N
     training samples each of dimension D.
   - y: A numpy array of shape (N,) containing training labels; y[i]
= c
     means that X[i] has label 0 \le c < C for C classes.

    learning rate: (float) learning rate for optimization.

   - num_iters: (integer) number of steps to take when optimizing

    batch size: (integer) number of training examples to use at each

step.
    - verbose: (boolean) If true, print progress during optimization.
   Outputs:
   A list containing the value of the loss function at each training
iteration.
```

```
.....
   num train, dim = X.shape
   num_classes = np.max(y) + 1 # assume y takes values 0...K-1 where
K is number of classes
   self.init weights(dims=[np.max(y) + 1, X.shape[1]])
initializes the weights of self.W
   # Run stochastic gradient descent to optimize W
   loss_history = []
   for it in np.arange(num_iters):
    X_batch = None
    y_batch = None
           =========
    # YOUR CODE HERE:
       Sample batch_size elements from the training data for use in
    #
        gradient descent. After sampling,
         X_batch should have shape: (dim, batch_size)
             - y_batch should have shape: (batch_size,)
           The indices should be randomly generated to reduce
correlations
           in the dataset. Use np.random.choice. It's okay to
sample with
           replacement.
    #
______#
    indices = np.random.choice(num_train, batch_size)
    X_batch, y_batch = X[indices], y[indices]
    #
______ #
    # END YOUR CODE HERE
______ #
    # evaluate loss and gradient
    loss, grad = self.fast_loss_and_grad(X_batch, y_batch)
    loss history.append(loss)
         # YOUR CODE HERE:
       Update the parameters, self.W, with a gradient step
    #
```

______#

```
______#
   # END YOUR CODE HERE
if verbose and it % 100 == 0:
     print('iteration {} / {}: loss {}'.format(it, num_iters,
loss))
  return loss_history
 def predict(self, X):
  Inputs:
  - X: N x D array of training data. Each row is a D-dimensional
point.
  Returns:
  - y_pred: Predicted labels for the data in X. y_pred is a 1-
dimensional
   array of length N, and each element is an integer giving the
predicted
   class.
  .....
  y_pred = np.zeros(X.shape[1])
  #
  # YOUR CODE HERE:
     Predict the labels given the training data.
  #
  scores = X.dot(self.W.T)
  y_pred = np.argmax(scores, axis=1)
  #
  # END YOUR CODE HERE
```

self.W -= learning rate * grad

return y_pred

This is the svm workbook for ECE C147/C247 Assignment #2

Please follow the notebook linearly to implement a linear support vector machine.

Please print out the workbook entirely when completed.

We thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu). These are the functions in the cs231n folders and includes code to preprocess and show the images. The classifiers used are based off of code prepared for CS 231n as well.

The goal of this workbook is to give you experience with training an SVM classifier via gradient descent.

Importing libraries and data setup

```
In [1]: import numpy as np # for doing most of our calculations
import matplotlib.pyplot as plt# for plotting
from cs23ln.data_utils import load_CIFAR10 # function to load the CIFAR-
10 dataset.
import pdb

# Load matplotlib images inline
%matplotlib inline

# These are important for reloading any code you write in external .py f
iles.
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
n-ipython
%load_ext autoreload
%autoreload 2
```

```
In [2]: # Set the path to the CIFAR-10 data
    cifar10_dir = './cifar-10-batches-py' # You need to update this line
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# As a sanity check, we print out the size of the training and test dat
    a.
    print('Training data shape: ', X_train.shape)
    print('Training labels shape: ', y_train.shape)
    print('Test data shape: ', X_test.shape)
    print('Test labels shape: ', y_test.shape)
```

```
Training data shape: (50000, 32, 32, 3)
Training labels shape: (50000,)
Test data shape: (10000, 32, 32, 3)
Test labels shape: (10000,)
```

```
In [3]: # Visualize some examples from the dataset.
        # We show a few examples of training images from each class.
        classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse'
        , 'ship', 'truck']
        num_classes = len(classes)
        samples per class = 7
        for y, cls in enumerate(classes):
            idxs = np.flatnonzero(y train == y)
            idxs = np.random.choice(idxs, samples_per_class, replace=False)
            for i, idx in enumerate(idxs):
                plt_idx = i * num_classes + y + 1
                plt.subplot(samples_per_class, num_classes, plt_idx)
                plt.imshow(X_train[idx].astype('uint8'))
                plt.axis('off')
                if i == 0:
                    plt.title(cls)
        plt.show()
```



```
In [4]: # Split the data into train, val, and test sets. In addition we will
        # create a small development set as a subset of the training data;
        # we can use this for development so our code runs faster.
        num_training = 49000
        num validation = 1000
        num test = 1000
        num_dev = 500
        # Our validation set will be num validation points from the original
        # training set.
        mask = range(num training, num training + num validation)
        X_val = X_train[mask]
        y_val = y_train[mask]
        # Our training set will be the first num train points from the original
        # training set.
        mask = range(num training)
        X_train = X_train[mask]
        y_train = y_train[mask]
        # We will also make a development set, which is a small subset of
        # the training set.
        mask = np.random.choice(num training, num dev, replace=False)
        X_dev = X_train[mask]
        y dev = y train[mask]
        # We use the first num test points of the original test set as our
        # test set.
        mask = range(num_test)
        X test = X test[mask]
        y_test = y_test[mask]
        print('Train data shape: ', X_train.shape)
        print('Train labels shape: ', y_train.shape)
        print('Validation data shape: ', X_val.shape)
        print('Validation labels shape: ', y_val.shape)
        print('Test data shape: ', X_test.shape)
        print('Test labels shape: ', y_test.shape)
print('Dev data shape: ', X_dev.shape)
        print('Dev labels shape: ', y_dev.shape)
        Train data shape: (49000, 32, 32, 3)
        Train labels shape: (49000,)
        Validation data shape: (1000, 32, 32, 3)
        Validation labels shape: (1000,)
        Test data shape: (1000, 32, 32, 3)
        Test labels shape: (1000,)
        Dev data shape: (500, 32, 32, 3)
```

Dev labels shape: (500,)

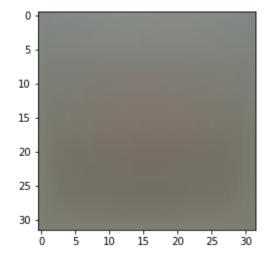
```
In [5]: # Preprocessing: reshape the image data into rows
X_train = np.reshape(X_train, (X_train.shape[0], -1))
X_val = np.reshape(X_val, (X_val.shape[0], -1))
X_test = np.reshape(X_test, (X_test.shape[0], -1))
X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))

# As a sanity check, print out the shapes of the data
print('Training data shape: ', X_train.shape)
print('Validation data shape: ', X_val.shape)
print('Test data shape: ', X_test.shape)
print('dev data shape: ', X_dev.shape)
```

Training data shape: (49000, 3072) Validation data shape: (1000, 3072) Test data shape: (1000, 3072) dev data shape: (500, 3072)

In [6]: # Preprocessing: subtract the mean image
 # first: compute the image mean based on the training data
 mean_image = np.mean(X_train, axis=0)
 print(mean_image[:10]) # print a few of the elements
 plt.figure(figsize=(4,4))
 plt.imshow(mean_image.reshape((32,32,3)).astype('uint8')) # visualize th
 e mean image
 plt.show()

[130.64189796 135.98173469 132.47391837 130.05569388 135.34804082 131.75402041 130.96055102 136.14328571 132.47636735 131.48467347]



In [7]: # second: subtract the mean image from train and test data
 X_train -= mean_image
 X_val -= mean_image
 X_test -= mean_image
 X_dev -= mean_image

```
In [8]: # third: append the bias dimension of ones (i.e. bias trick) so that our
    SVM
    # only has to worry about optimizing a single weight matrix W.
    X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
    X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
    X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
    X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])
    print(X_train.shape, X_val.shape, X_test.shape, X_dev.shape)
(49000, 3073) (1000, 3073) (1000, 3073) (500, 3073)
```

Question:

(1) For the SVM, we perform mean-subtraction on the data. However, for the KNN notebook, we did not. Why?

Answer:

(1) For the SVM, we need to normalize the data so that each feature has a similar range. This helps prevent one feature which has a broad range of values from governing the Euclidean distance. It also helps the gradient to act uniformly.

Training an SVM

The following cells will take you through building an SVM. You will implement its loss function, then subsequently train it with gradient descent. Finally, you will choose the learning rate of gradient descent to optimize its classification performance.

```
In [9]: from nndl.svm import SVM

In [10]: # Declare an instance of the SVM class.
    # Weights are initialized to a random value.
    # Note, to keep people's initial solutions consistent, we are going to u se a random seed.
    np.random.seed(1)
    num_classes = len(np.unique(y_train))
    num_features = X_train.shape[1]
    svm = SVM(dims=[num_classes, num_features])
```

SVM loss

```
In [11]: ## Implement the loss function for in the SVM class(nndl/svm.py), svm.lo
    ss()

print(y_train)
    loss = svm.loss(X_train, y_train)
    print('The training set loss is {}.'.format(loss))

# If you implemented the loss correctly, it should be 15569.98

[6 9 9 ... 4 9 3]
The training set loss is 15569.977915410193.
```

SVM gradient

```
In [12]: ## Calculate the gradient of the SVM class.
         # For convenience, we'll write one function that computes the loss
             and gradient together. Please modify svm.loss and grad(X, y).
         # You may copy and paste your loss code from svm.loss() here, and then
             use the appropriate intermediate values to calculate the gradient.
         loss, grad = svm.loss and grad(X dev,y dev)
         # Compare your gradient to a numerical gradient check.
         # You should see relative gradient errors on the order of 1e-07 or less
          if you implemented the gradient correctly.
         svm.grad check sparse(X dev, y dev, grad)
         numerical: -4.312075 analytic: -4.312075, relative error: 2.119391e-09
         numerical: 2.843858 analytic: 2.843857, relative error: 2.244579e-07
         numerical: -4.943769 analytic: -4.943770, relative error: 7.134826e-08
         numerical: 15.302841 analytic: 15.302842, relative error: 9.304742e-09
         numerical: 3.442246 analytic: 3.442246, relative error: 2.000714e-08
         numerical: 4.725199 analytic: 4.725198, relative error: 6.270475e-08
         numerical: -4.374034 analytic: -4.374033, relative error: 9.348043e-08
         numerical: -6.198758 analytic: -6.198758, relative error: 2.671336e-08
         numerical: -1.547739 analytic: -1.547739, relative error: 6.451178e-08
         numerical: -22.857156 analytic: -22.857157, relative error: 2.719112e-0
         8
```

A vectorized version of SVM

To speed things up, we will vectorize the loss and gradient calculations. This will be helpful for stochastic gradient descent.

```
In [13]: import time
```

```
In [14]:
         ## Implement sym.fast loss and grad which calculates the loss and gradie
         #
              WITHOUT using any for loops.
         # Standard loss and gradient
         tic = time.time()
         loss, grad = svm.loss_and_grad(X_dev, y_dev)
         toc = time.time()
         print('Normal loss / grad_norm: {} / {} computed in {}s'.format(loss, np
         .linalg.norm(grad, 'fro'), toc - tic))
         tic = time.time()
         loss vectorized, grad vectorized = svm.fast loss and grad(X dev, y dev)
         toc = time.time()
         print('Vectorized loss / grad: {} / {} computed in {}s'.format(loss_vect
         orized, np.linalg.norm(grad_vectorized, 'fro'), toc - tic))
         # The losses should match but your vectorized implementation should be m
         uch faster.
         print('difference in loss / grad: {} / {}'.format(loss - loss vectorized
         , np.linalg.norm(grad - grad_vectorized)))
         # You should notice a speedup with the same output, i.e., differences on
         the order of 1e-12
```

```
Normal loss / grad_norm: 16882.900643099136 / 2286.977873936257 compute d in 0.08017802238464355s

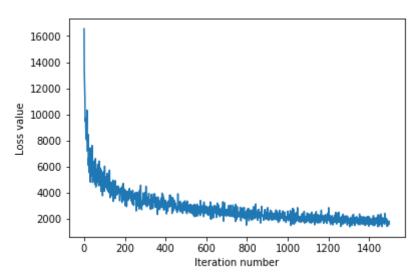
Vectorized loss / grad: 16882.90064309911 / 2286.977873936257 computed in 0.006361961364746094s

difference in loss / grad: 2.546585164964199e-11 / 4.320403166978369e-1
```

Stochastic gradient descent

We now implement stochastic gradient descent. This uses the same principles of gradient descent we discussed in class, however, it calculates the gradient by only using examples from a subset of the training set (so each gradient calculation is faster).

```
iteration 0 / 1500: loss 16557.38000190916
iteration 100 / 1500: loss 4701.089451272714
iteration 200 / 1500: loss 4017.333137942788
iteration 300 / 1500: loss 3681.9226471953625
iteration 400 / 1500: loss 2732.616437398899
iteration 500 / 1500: loss 2786.6378424645054
iteration 600 / 1500: loss 2837.0357842782664
iteration 700 / 1500: loss 2206.2348687399317
iteration 800 / 1500: loss 2269.03882411698
iteration 900 / 1500: loss 2543.23781538592
iteration 1000 / 1500: loss 2566.6921357268266
iteration 1100 / 1500: loss 2182.068905905164
iteration 1200 / 1500: loss 1861.1182244250447
iteration 1300 / 1500: loss 1982.9013858528251
iteration 1400 / 1500: loss 1927.5204158582114
That took 3.085602045059204s
```



Evaluate the performance of the trained SVM on the validation data.

Optimize the SVM

Note, to make things faster and simpler, we won't do k-fold cross-validation, but will only optimize the hyperparameters on the validation dataset (X_val, y_val).

```
In [18]:
       # =================== #
        # YOUR CODE HERE:
           Train the SVM with different learning rates and evaluate on the
        #
             validation data.
        #
           Report:
        #
             - The best learning rate of the ones you tested.
             - The best VALIDATION accuracy corresponding to the best VALIDATIO
        N error.
        #
        #
           Select the SVM that achieved the best validation error and report
        #
             its error rate on the test set.
           Note: You do not need to modify SVM class for this section
        learning_rates = np.array([1e-7, 5e-7, 1e-6, 5e-6, 1e-5, 5e-5, 1e-4, 5e-
        4, 1e-3, 5e-3, 1e-2, 5e-2, 1e-1, 5e-1, 1, 5, 10])
        val accs = np.zeros like(learning rates)
        for idx, learning rate in enumerate(learning rates):
           svm.train(X train, y train, learning rate=learning rate)
           y val pred = svm.predict(X val)
           val_accs[idx] = np.mean(np.equal(y val, y val pred))
        best val acc idx = np.argmax(val accs)
        best val acc = val accs[best val acc idx]
        best_learning rate = learning rates[best_val_acc_idx]
        print("The best learning rate is {}, with a validation accuracy of {}.".
        format(best_learning_rate, best_val_acc))
        svm.train(X train, y train, learning rate=best learning rate)
        y_test_pred = svm.predict(X_test)
        test_acc = np.mean(np.equal(y_test, y_test_pred))
        print("The best learning rate of {} had a test error of {}.".format(best
        _learning_rate, 1 - test_acc))
        # END YOUR CODE HERE
```

The best learning rate is 0.05, with a validation accuracy of 0.317. The best learning rate of 0.05 had a test error of 0.74.

```
import numpy as np
import pdb
.....
This code was based off of code from cs231n at Stanford University,
and modified for ECE C147/C247 at UCLA.
class SVM(object):
  def __init__(self, dims=[10, 3073]):
    self.init weights(dims=dims)
  def init_weights(self, dims):
        Initializes the weight matrix of the SVM. Note that it has
shape (C, D)
        where C is the number of classes and D is the feature size.
    self.W = np.random.normal(size=dims)
  def loss(self, X, y):
   Calculates the SVM loss.
    Inputs have dimension D, there are C classes, and we operate on
minibatches
   of N examples.
   Inputs:
    - X: A numpy array of shape (N, D) containing a minibatch of data.
   - y: A numpy array of shape (N,) containing training labels; y[i]
= c means
     that X[i] has label c, where 0 \le c < C.
   Returns a tuple of:

    loss as single float

   .....
   # compute the loss and the gradient
   num classes = self.W.shape[0]
   num_train = X.shape[0]
    loss = 0.0
    for i in np.arange(num_train):
   #
   # YOUR CODE HERE:
              Calculate the normalized SVM loss, and store it as
'loss'.
       (That is, calculate the sum of the losses of all the training
```

```
#
      set margins, and then normalize the loss by the number of
                training examples.)
   #
     for j in np.arange(num_classes):
      if y[i] != j:
          loss += \max(0, 1 + \text{self.W[i].dot}(X[i]) -
self.W[y[i]].dot(X[i]))
   loss /= num_train
   # END YOUR CODE HERE
   return loss
 def loss_and_grad(self, X, y):
       Same as self.loss(X, y), except that it also returns the
gradient.
       Output: grad -- a matrix of the same dimensions as W
containing
              the gradient of the loss with respect to W.
       .....
   # compute the loss and the gradient
   num classes = self.W.shape[0]
   num train = X.shape[0]
   loss = 0.0
   grad = np.zeros like(self.W)
   for i in np.arange(num train):
   #
   # YOUR CODE HERE:
          Calculate the SVM loss and the gradient. Store the
gradient in
      the variable grad.
   #
     for j in np.arange(num_classes):
       if y[i] != j:
        zj = 1 + self.W[j].dot(X[i]) - self.W[y[i]].dot(X[i])
        loss += max(0, zj)
        grad[i] += 0 if zi <= 0 else X[i]</pre>
        grad[y[i]] += 0 if zj <= 0 else -X[i]
```

```
#
   # END YOUR CODE HERE
   #
   loss /= num train
   grad /= num_train
   return loss, grad
 def grad_check_sparse(self, X, y, your_grad, num_checks=10, h=1e-5):
   sample a few random elements and only return numerical
   in these dimensions.
   .....
   for i in np.arange(num_checks):
     ix = tuple([np.random.randint(m) for m in self.W.shape])
     oldval = self.W[ix]
     self.W[ix] = oldval + h # increment by h
     fxph = self.loss(X, y)
     self.W[ix] = oldval - h # decrement by h
     fxmh = self.loss(X,y) # evaluate f(x - h)
     self.W[ix] = oldval # reset
     grad_numerical = (fxph - fxmh) / (2 * h)
     grad analytic = your grad[ix]
     rel_error = abs(grad_numerical - grad_analytic) /
(abs(grad_numerical) + abs(grad_analytic))
     print('numerical: %f analytic: %f, relative error: %e' %
(grad numerical, grad analytic, rel error))
 def fast_loss_and_grad(self, X, y):
   A vectorized implementation of loss_and_grad. It shares the same
       inputs and ouptuts as loss and grad.
   .....
   loss = 0.0
   grad = np.zeros(self.W.shape) # initialize the gradient as zero
   #
   # YOUR CODE HERE:
          Calculate the SVM loss WITHOUT any for loops.
```

```
scores = X.dot(self.W.T)
   num_train = X.shape[0]
   losses = np.ones like(scores) + scores -
scores[np.arange(num train), y].reshape(scores.shape[0], 1)
   losses[losses < 0] = 0
   losses[np.arange(num_train), y] = 0
   loss = np.sum(losses) / num train
#
   # END YOUR CODE HERE
            # YOUR CODE HERE:
          Calculate the SVM grad WITHOUT any for loops.
#
   selector = losses.T
   selector[selector > 0] = 1
   selector[y, np.arange(num_train)] = np.sum(selector, axis=0) *
(-1)
   grad = selector.dot(X) / num_train
   #
   # END YOUR CODE HERE
   #
   return loss, grad
 def train(self, X, y, learning_rate=1e-3, num_iters=100,
          batch_size=200, verbose=False):
   .....
   Train this linear classifier using stochastic gradient descent.
   Inputs:
   - X: A numpy array of shape (N, D) containing training data; there
are N
     training samples each of dimension D.
   y: A numpy array of shape (N,) containing training labels; y[i]
= c
     means that X[i] has label 0 <= c < C for C classes.

    learning rate: (float) learning rate for optimization.

   - num_iters: (integer) number of steps to take when optimizing
```

```
- batch size: (integer) number of training examples to use at each
step.

    verbose: (boolean) If true, print progress during optimization.

   Outputs:
   A list containing the value of the loss function at each training
iteration.
   num_train, dim = X.shape
   num_classes = np.max(y) + 1 # assume y takes values 0...K-1 where
K is number of classes
   self.init_weights(dims=[np.max(y) + 1, X.shape[1]])
initializes the weights of self.W
   # Run stochastic gradient descent to optimize W
   loss history = []
   for it in np.arange(num_iters):
     X batch = None
     y_batch = None
______#
     # YOUR CODE HERE:
        Sample batch_size elements from the training data for use in
     #
     #
        gradient descent. After sampling,
          X_batch should have shape: (dim, batch_size)
               - y_batch should have shape: (batch_size,)
          #
             The indices should be randomly generated to reduce
correlations
             in the dataset. Use np.random.choice. It's okay to
sample with
             replacement.
     #
______#
     indices = np.random.choice(num_train, batch_size)
     X batch, y batch = X[indices], y[indices]
______#
     # END YOUR CODE HERE
# evaluate loss and gradient
     loss, grad = self.fast_loss_and_grad(X_batch, y_batch)
     loss history.append(loss)
```

```
#
_____#
   # YOUR CODE HERE:
      Update the parameters, self.W, with a gradient step
self.W -= learning_rate * grad
# END YOUR CODE HERE
______ #
   if verbose and it % 100 == 0:
     print('iteration {} / {}: loss {}'.format(it, num_iters,
loss))
  return loss_history
 def predict(self, X):
  Inputs:
  - X: N x D array of training data. Each row is a D-dimensional
point.
  - y_pred: Predicted labels for the data in X. y_pred is a 1-
dimensional
   array of length N, and each element is an integer giving the
predicted
   class.
  y_pred = np.zeros(X.shape[1])
  #
  # YOUR CODE HERE:
     Predict the labels given the training data with the parameter
self.W.
  #
  scores = X.dot(self.W.T)
  y_pred = np.argmax(scores, axis=1)
  # END YOUR CODE HERE
```

#

return y_pred