## Import and setups

#### **Optimization for Fully Connected Networks**

In this notebook, we will implement different optimization rules for gradient descent. We have provided starter code; however, you will need to copy and paste your code from your implementation of the modular fully connected nets in HW #3 to build upon this.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc_net import *
        from cs231n.data utils import get CIFAR10 data
        from cs231n.gradient check import eval numerical gradient, eval numerica
        l_gradient_array
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
        n-ipython
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
            """ returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y)
        ))))
In [2]: # Load the (preprocessed) CIFAR10 data.
        data = get_CIFAR10_data()
        for k in data.keys():
            print('{}: {} '.format(k, data[k].shape))
        X train: (49000, 3, 32, 32)
        y_train: (49000,)
        X_val: (1000, 3, 32, 32)
        y val: (1000,)
        X test: (1000, 3, 32, 32)
        y test: (1000,)
```

In [1]:

### **Building upon your HW #3 implementation**

Copy and paste the following functions from your HW #3 implementation of a modular FC net:

- affine\_forward in nndl/layers.py
- affine\_backward in nndl/layers.py
- relu\_forward in nndl/layers.py
- relu\_backward in nndl/layers.py
- affine\_relu\_forward in nndl/layer\_utils.py
- affine\_relu\_backwardin nndl/layer\_utils.py
- The FullyConnectedNet class in nndl/fc\_net.py

#### Test all functions you copy and pasted

```
In [3]: from nndl.layer_tests import *
        affine_forward_test(); print('\n')
        affine_backward_test(); print('\n')
        relu forward test(); print('\n')
        relu backward test(); print('\n')
        affine_relu_test(); print('\n')
        fc net test()
        If affine forward function is working, difference should be less than 1
        e-9:
        difference: 9.7698500479884e-10
        If affine backward is working, error should be less than 1e-9::
        dx error: 2.898441795179766e-10
        dw error: 1.0983218323478878e-10
        db error: 8.203769025704131e-12
        If relu_forward function is working, difference should be around 1e-8:
        difference: 4.999999798022158e-08
        If relu_forward function is working, error should be less than 1e-9:
        dx error: 3.2756139819893578e-12
        If affine relu forward and affine relu backward are working, error shou
        ld be less than 1e-9::
        dx error: 5.318884328167776e-11
        dw error: 2.0060510820706475e-10
        db error: 3.226562000039114e-11
        Running check with reg = 0
        Initial loss: 2.2988503962393203
        W1 relative error: 6.512909849721434e-07
        W2 relative error: 4.842238900298789e-07
        W3 relative error: 4.6881348245194703e-08
        b1 relative error: 3.445759767012608e-06
        b2 relative error: 1.392745058581727e-09
        b3 relative error: 1.4148581119623153e-10
        Running check with reg = 3.14
        Initial loss: 6.853302770567678
        W1 relative error: 1.769199030659722e-08
        W2 relative error: 1.1504864001521932e-06
        W3 relative error: 8.778838354252005e-08
        b1 relative error: 1.0774283968780174e-08
        b2 relative error: 5.6964133840562794e-09
        b3 relative error: 1.6093787328469607e-10
```

### Training a larger model

In general, proceeding with vanilla stochastic gradient descent to optimize models may be fraught with problems and limitations, as discussed in class. Thus, we implement optimizers that improve on SGD.

#### SGD + momentum

In the following section, implement SGD with momentum. Read the nndl/optim.py API, which is provided by CS231n, and be sure you understand it. After, implement sgd\_momentum in nndl/optim.py. Test your implementation of sgd\_momentum by running the cell below.

```
In [4]: from nndl.optim import sqd momentum
        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning rate': 1e-3, 'velocity': v}
        next_w, _ = sgd_momentum(w, dw, config=config)
        expected next w = np.asarray([
                                                    0.34096842, 0.40775789],
            [ 0.1406, 0.20738947,
                                       0.27417895,
            [ 0.47454737, 0.54133684,
                                       0.60812632,
                                                    0.67491579, 0.74170526],
            [ 0.80849474, 0.87528421,
                                       0.94207368,
                                                    1.00886316, 1.07565263],
            [ 1.14244211, 1.20923158,
                                       1.27602105,
                                                    1.34281053,
                                                                1.4096
                                                                           11)
        expected_velocity = np.asarray([
                                       0.56891579, 0.58307368, 0.59723158],
            [ 0.5406,
                          0.55475789,
            [ 0.61138947, 0.62554737,
                                       0.63970526, 0.65386316, 0.66802105],
            [ 0.68217895, 0.69633684,
                                       0.71049474, 0.72465263,
                                                                 0.73881053],
            [ 0.75296842, 0.76712632,
                                       0.78128421,
                                                    0.79544211,
                                                                 0.8096
                                                                           11)
        print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
        print('velocity error: {}'.format(rel error(expected velocity, config['v
        elocity'])))
```

next\_w error: 8.882347033505819e-09
velocity error: 4.269287743278663e-09

#### SGD + Nesterov momentum

Implement sqd nesterov momentum in ndl/optim.py.

```
In [5]: from nndl.optim import sqd nesterov momentum
        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning rate': 1e-3, 'velocity': v}
        next_w, _ = sgd_nesterov_momentum(w, dw, config=config)
        expected next w = np.asarray([
            [0.08714,
                          0.15246105,
                                       0.21778211,
                                                    0.28310316, 0.34842421],
            [0.41374526,
                           0.47906632, 0.54438737,
                                                    0.60970842,
                                                                 0.67502947],
            [0.74035053,
                          0.80567158,
                                       0.87099263,
                                                    0.93631368,
                                                                 1.00163474],
            [1.06695579,
                          1.13227684,
                                       1.19759789,
                                                    1.26291895,
                                                                 1.32824
                                                                           11)
        expected_velocity = np.asarray([
                           0.55475789, 0.56891579,
            [ 0.5406,
                                                    0.58307368,
                                                                 0.59723158],
            [0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
            [0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
            [ 0.75296842, 0.76712632,
                                       0.78128421,
                                                    0.79544211,
                                                                 0.8096
                                                                           11)
        print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
        print('velocity error: {}'.format(rel_error(expected_velocity, config['v
        elocity'])))
```

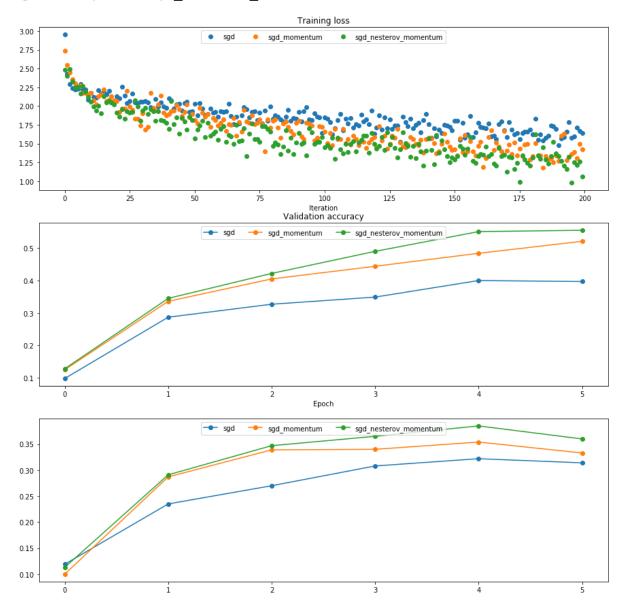
next\_w error: 1.0875186845081027e-08
velocity error: 4.269287743278663e-09

# Evaluating SGD, SGD+Momentum, and SGD+NesterovMomentum

Run the following cell to train a 6 layer FC net with SGD, SGD+momentum, and SGD+Nesterov momentum. You should see that SGD+momentum achieves a better loss than SGD, and that SGD+Nesterov momentum achieves a slightly better loss (and training accuracy) than SGD+momentum.

```
In [6]: num_train = 4000
        small data = {
            'X_train': data['X_train'][:num_train],
            'y_train': data['y_train'][:num_train],
            'X_val': data['X_val'],
             'y_val': data['y_val'],
        solvers = {}
        for update rule in ['sgd', 'sgd momentum', 'sgd_nesterov momentum']:
            print('Optimizing with {}'.format(update_rule))
            model = FullyConnectedNet([100, 100, 100, 100], weight_scale=5e
        -2)
            solver = Solver(model, small_data,
                             num_epochs=5, batch_size=100,
                             update_rule=update_rule,
                             optim config={
                               'learning rate': 1e-2,
                             },
                             verbose=False)
            solvers[update_rule] = solver
            solver.train()
            print
        fig, axes = plt.subplots(3, 1)
        ax = axes[0]
        ax.set title('Training loss')
        ax.set_xlabel('Iteration')
        ax = axes[1]
        ax.set_title('Training accuracy')
        ax.set_xlabel('Epoch')
        ax = axes[1]
        ax.set_title('Validation accuracy')
        ax.set xlabel('Epoch')
        for update_rule, solver in solvers.items():
            ax = axes[0]
            ax.plot(solver.loss_history, 'o', label=update rule)
            ax = axes[1]
            ax.plot(solver.train_acc_history, '-o', label=update_rule)
            ax = axes[2]
            ax.plot(solver.val_acc_history, '-o', label=update_rule)
        for i in [1, 2, 3]:
            ax = axes[i - 1]
            ax.legend(loc='upper center', ncol=4)
        plt.gcf().set size inches(15, 15)
        plt.show()
```

Optimizing with sgd\_momentum
Optimizing with sgd\_nesterov\_momentum



# **RMSProp**

Now we go to techniques that adapt the gradient. Implement rmsprop in nndl/optim.py. Test your implementation by running the cell below.

```
In [27]: from nndl.optim import rmsprop
         N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
         dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
         a = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
         config = {'learning rate': 1e-2, 'a': a}
         next_w, _ = rmsprop(w, dw, config=config)
         expected_next_w = np.asarray([
           [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
           [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
           [0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
           [0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
         expected_cache = np.asarray([
                         0.6126277, 0.6277108,
           [ 0.5976,
                                                   0.64284931, 0.65804321],
           [0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
           [ 0.75037008, 0.7659518,
                                      0.78158892, 0.79728144, 0.81302936],
           [ 0.82883269,  0.84469141,  0.86060554,  0.87657507,  0.8926
         print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
         print('cache error: {}'.format(rel_error(expected_cache, config['a'])))
```

next\_w error: 9.524687511038133e-08
cache error: 2.6477955807156126e-09

#### **Adaptive moments**

Now, implement adam in nndl/optim.py. Test your implementation by running the cell below.

```
In [30]: # Test Adam implementation; you should see errors around 1e-7 or less
         from nndl.optim import adam
         N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
         dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
         v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
         a = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
         config = {'learning_rate': 1e-2, 'v': v, 'a': a, 't': 5}
         next_w, _ = adam(w, dw, config=config)
         expected next w = np.asarray([
           [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
           [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
           [0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],
           [0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])
         expected a = np.asarray([
                      0.68908382, 0.67851319, 0.66794809, 0.65738853,],
           [ 0.69966,
           [ 0.64683452, 0.63628604, 0.6257431,
                                                   0.61520571,
                                                               0.60467385, ],
           [ 0.59414753, 0.58362676, 0.57311152,
                                                   0.56260183,
                                                               0.55209767,1,
           [ 0.54159906, 0.53110598, 0.52061845, 0.51013645,
                                                               0.49966,
                                                                          ]])
         expected_v = np.asarray([
                     0.49947368, 0.51894737, 0.53842105, 0.55789474],
           [ 0.48,
           [0.57736842, 0.59684211, 0.61631579, 0.63578947,
                                                               0.65526316],
           [ 0.67473684, 0.69421053, 0.71368421,
                                                   0.73315789,
                                                               0.75263158],
           [ 0.77210526, 0.79157895, 0.81105263, 0.83052632,
                                                               0.85
                                                                          11)
         print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
         print('a error: {}'.format(rel error(expected a, config['a'])))
         print('v error: {}'.format(rel_error(expected_v, config['v'])))
```

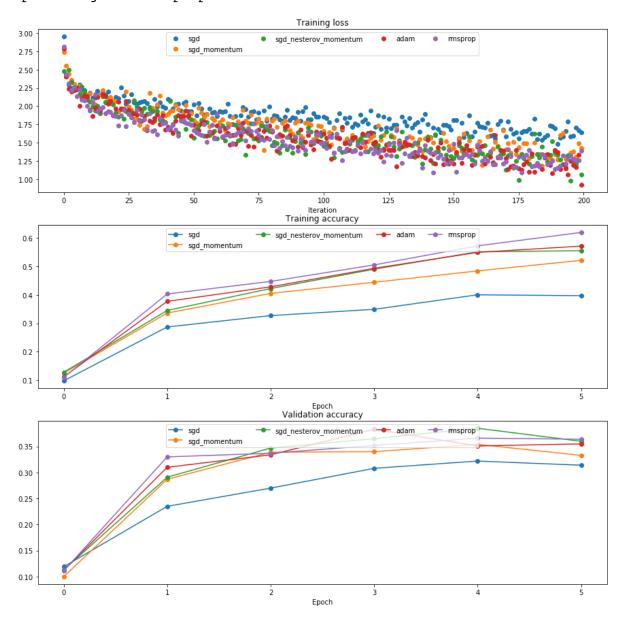
next\_w error: 1.1395691798535431e-07
a error: 4.208314038113071e-09
v error: 4.214963193114416e-09

# Comparing SGD, SGD+NesterovMomentum, RMSProp, and Adam

The following code will compare optimization with SGD, Momentum, Nesterov Momentum, RMSProp and Adam. In our code, we find that RMSProp, Adam, and SGD + Nesterov Momentum achieve approximately the same training error after a few training epochs.

```
In [31]: learning_rates = {'rmsprop': 2e-4, 'adam': 1e-3}
         for update_rule in ['adam', 'rmsprop']:
             print('Optimizing with {}'.format(update_rule))
             model = FullyConnectedNet([100, 100, 100, 100], weight scale=5e
         -2)
             solver = Solver(model, small data,
                              num epochs=5, batch size=100,
                              update_rule=update_rule,
                              optim config={
                                'learning_rate': learning_rates[update_rule]
                              },
                              verbose=False)
             solvers[update rule] = solver
             solver.train()
             print
         fig, axes = plt.subplots(3, 1)
         ax = axes[0]
         ax.set_title('Training loss')
         ax.set_xlabel('Iteration')
         ax = axes[1]
         ax.set_title('Training accuracy')
         ax.set_xlabel('Epoch')
         ax = axes[2]
         ax.set title('Validation accuracy')
         ax.set_xlabel('Epoch')
         for update rule, solver in solvers.items():
             ax = axes[0]
             ax.plot(solver.loss_history, 'o', label=update_rule)
             ax = axes[1]
             ax.plot(solver.train_acc_history, '-o', label=update_rule)
             ax = axes[2]
             ax.plot(solver.val_acc_history, '-o', label=update_rule)
         for i in [1, 2, 3]:
             ax = axes[i - 1]
             ax.legend(loc='upper center', ncol=4)
         plt.gcf().set_size_inches(15, 15)
         plt.show()
```

Optimizing with adam
Optimizing with rmsprop



## **Easier optimization**

In the following cell, we'll train a 4 layer neural network having 500 units in each hidden layer with the different optimizers, and find that it is far easier to get up to 50+% performance on CIFAR-10. After we implement batchnorm and dropout, we'll ask you to get 55+% on CIFAR-10.

```
optimizer = 'adam'
In [32]:
         best_model = None
         layer_dims = [500, 500, 500]
         weight_scale = 0.01
         learning_rate = 1e-3
         lr_decay = 0.9
         model = FullyConnectedNet(layer_dims, weight_scale=weight_scale,
                                    use_batchnorm=True)
         solver = Solver(model, data,
                          num_epochs=10, batch_size=100,
                          update_rule=optimizer,
                          optim_config={
                            'learning_rate': learning_rate,
                          },
                          lr_decay=lr_decay,
                          verbose=True, print_every=50)
         solver.train()
```

```
(Iteration 1 / 4900) loss: 2.296935
(Epoch 0 / 10) train acc: 0.156000; val acc: 0.160000
(Iteration 51 / 4900) loss: 1.793352
(Iteration 101 / 4900) loss: 1.730268
(Iteration 151 / 4900) loss: 1.712562
(Iteration 201 / 4900) loss: 1.655910
(Iteration 251 / 4900) loss: 1.609814
(Iteration 301 / 4900) loss: 1.722586
(Iteration 351 / 4900) loss: 1.808582
(Iteration 401 / 4900) loss: 1.653279
(Iteration 451 / 4900) loss: 1.635799
(Epoch 1 / 10) train acc: 0.419000; val acc: 0.430000
(Iteration 501 / 4900) loss: 1.581945
(Iteration 551 / 4900) loss: 1.637252
(Iteration 601 / 4900) loss: 1.522185
(Iteration 651 / 4900) loss: 1.701198
(Iteration 701 / 4900) loss: 1.473823
(Iteration 751 / 4900) loss: 1.506807
(Iteration 801 / 4900) loss: 1.566432
(Iteration 851 / 4900) loss: 1.390466
(Iteration 901 / 4900) loss: 1.618358
(Iteration 951 / 4900) loss: 1.439225
(Epoch 2 / 10) train acc: 0.473000; val acc: 0.453000
(Iteration 1001 / 4900) loss: 1.419714
(Iteration 1051 / 4900) loss: 1.496423
(Iteration 1101 / 4900) loss: 1.314355
(Iteration 1151 / 4900) loss: 1.217145
(Iteration 1201 / 4900) loss: 1.522215
(Iteration 1251 / 4900) loss: 1.423241
(Iteration 1301 / 4900) loss: 1.415627
(Iteration 1351 / 4900) loss: 1.378010
(Iteration 1401 / 4900) loss: 1.363004
(Iteration 1451 / 4900) loss: 1.197498
(Epoch 3 / 10) train acc: 0.502000; val acc: 0.491000
(Iteration 1501 / 4900) loss: 1.126266
(Iteration 1551 / 4900) loss: 1.318559
(Iteration 1601 / 4900) loss: 1.399456
(Iteration 1651 / 4900) loss: 1.417188
(Iteration 1701 / 4900) loss: 1.361223
(Iteration 1751 / 4900) loss: 1.244300
(Iteration 1801 / 4900) loss: 1.327750
(Iteration 1851 / 4900) loss: 1.228083
(Iteration 1901 / 4900) loss: 1.319608
(Iteration 1951 / 4900) loss: 1.148406
(Epoch 4 / 10) train acc: 0.540000; val acc: 0.500000
(Iteration 2001 / 4900) loss: 1.232102
(Iteration 2051 / 4900) loss: 1.170461
(Iteration 2101 / 4900) loss: 1.150136
(Iteration 2151 / 4900) loss: 1.312854
(Iteration 2201 / 4900) loss: 1.218821
(Iteration 2251 / 4900) loss: 1.385131
(Iteration 2301 / 4900) loss: 1.380520
(Iteration 2351 / 4900) loss: 1.165248
(Iteration 2401 / 4900) loss: 1.203299
(Epoch 5 / 10) train acc: 0.568000; val acc: 0.513000
(Iteration 2451 / 4900) loss: 1.272955
(Iteration 2501 / 4900) loss: 1.094092
```

```
(Iteration 2551 / 4900) loss: 1.080089
(Iteration 2601 / 4900) loss: 1.326507
(Iteration 2651 / 4900) loss: 1.200032
(Iteration 2701 / 4900) loss: 1.033523
(Iteration 2751 / 4900) loss: 1.222286
(Iteration 2801 / 4900) loss: 1.073262
(Iteration 2851 / 4900) loss: 0.919496
(Iteration 2901 / 4900) loss: 1.178354
(Epoch 6 / 10) train acc: 0.605000; val acc: 0.527000
(Iteration 2951 / 4900) loss: 1.046866
(Iteration 3001 / 4900) loss: 1.105564
(Iteration 3051 / 4900) loss: 1.143297
(Iteration 3101 / 4900) loss: 1.175037
(Iteration 3151 / 4900) loss: 1.244437
(Iteration 3201 / 4900) loss: 1.094552
(Iteration 3251 / 4900) loss: 0.912128
(Iteration 3301 / 4900) loss: 1.315570
(Iteration 3351 / 4900) loss: 1.132966
(Iteration 3401 / 4900) loss: 0.940354
(Epoch 7 / 10) train acc: 0.617000; val acc: 0.554000
(Iteration 3451 / 4900) loss: 1.004746
(Iteration 3501 / 4900) loss: 1.208959
(Iteration 3551 / 4900) loss: 0.975855
(Iteration 3601 / 4900) loss: 1.019452
(Iteration 3651 / 4900) loss: 1.092862
(Iteration 3701 / 4900) loss: 0.966287
(Iteration 3751 / 4900) loss: 1.139437
(Iteration 3801 / 4900) loss: 1.058727
(Iteration 3851 / 4900) loss: 0.958582
(Iteration 3901 / 4900) loss: 0.877067
(Epoch 8 / 10) train acc: 0.636000; val acc: 0.547000
(Iteration 3951 / 4900) loss: 0.914612
(Iteration 4001 / 4900) loss: 1.094349
(Iteration 4051 / 4900) loss: 0.988862
(Iteration 4101 / 4900) loss: 0.924163
(Iteration 4151 / 4900) loss: 1.014360
(Iteration 4201 / 4900) loss: 1.038937
(Iteration 4251 / 4900) loss: 1.103283
(Iteration 4301 / 4900) loss: 1.091689
(Iteration 4351 / 4900) loss: 0.859628
(Iteration 4401 / 4900) loss: 0.822187
(Epoch 9 / 10) train acc: 0.662000; val acc: 0.538000
(Iteration 4451 / 4900) loss: 1.043656
(Iteration 4501 / 4900) loss: 1.017224
(Iteration 4551 / 4900) loss: 1.111695
(Iteration 4601 / 4900) loss: 1.042493
(Iteration 4651 / 4900) loss: 0.678103
(Iteration 4701 / 4900) loss: 1.058030
(Iteration 4751 / 4900) loss: 0.779660
(Iteration 4801 / 4900) loss: 0.903205
(Iteration 4851 / 4900) loss: 0.991989
(Epoch 10 / 10) train acc: 0.702000; val acc: 0.541000
```

Validation set accuracy: 0.554 Test set accuracy: 0.516

#### **Batch Normalization**

In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [1]: ## Import and setups
         import time
         import numpy as np
         import matplotlib.pyplot as plt
         from nndl.fc net import *
         from nndl.layers import *
         from cs231n.data_utils import get_CIFAR10_data
         from cs231n.gradient_check import eval numerical_gradient, eval_numerica
         l gradient array
         from cs231n.solver import Solver
         %matplotlib inline
         plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
         plt.rcParams['image.interpolation'] = 'nearest'
         plt.rcParams['image.cmap'] = 'gray'
         # for auto-reloading external modules
         # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
         n-ipython
         %load ext autoreload
         %autoreload 2
         def rel error(x, y):
              """ returns relative error """
             return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))
         ))))
In [50]: # Load the (preprocessed) CIFAR10 data.
         data = get_CIFAR10_data()
         for k in data.keys():
             print('{}: {} '.format(k, data[k].shape))
```

y val: (1000,)

y test: (1000,)

y\_train: (49000,)

X train: (49000, 3, 32, 32)

X\_val: (1000, 3, 32, 32)

X\_test: (1000, 3, 32, 32)

#### **Batchnorm forward pass**

Implement the training time batchnorm forward pass, batchnorm\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [98]: # Check the training-time forward pass by checking means and variances
         # of features both before and after batch normalization
         # Simulate the forward pass for a two-layer network
         N, D1, D2, D3 = 200, 50, 60, 3
         X = np.random.randn(N, D1)
         W1 = np.random.randn(D1, D2)
         W2 = np.random.randn(D2, D3)
         a = np.maximum(0, X.dot(W1)).dot(W2)
         print('Before batch normalization:')
         print(' means: ', a.mean(axis=0))
         print(' stds: ', a.std(axis=0))
         # Means should be close to zero and stds close to one
         print('After batch normalization (gamma=1, beta=0)')
         a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode': 'tr
         ain'})
         print('
                  mean: ', a norm.mean(axis=0))
         print(' std: ', a norm.std(axis=0))
         # Now means should be close to beta and stds close to gamma
         gamma = np.asarray([1.0, 2.0, 3.0])
         beta = np.asarray([11.0, 12.0, 13.0])
         a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
         print('After batch normalization (nontrivial gamma, beta)')
         print(' means: ', a_norm.mean(axis=0))
                 stds: ', a_norm.std(axis=0))
         print('
         Before batch normalization:
           means: [ 13.70727584  7.3511623  -13.90352129]
           stds: [ 32.26519471 36.03895895 25.38472842]
         After batch normalization (gamma=1, beta=0)
           mean: [ 1.33226763e-16
                                     7.21644966e-17
                                                       1.02140518e-16]
           std: [ 1.
                                           0.999999991
                               1.
         After batch normalization (nontrivial gamma, beta)
           means: [ 11. 12. 13.]
           stds: [ 1.
                                1.99999999 2.999999981
```

Implement the testing time batchnorm forward pass, batchnorm\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [106]: # Check the test-time forward pass by running the training-time
          # forward pass many times to warm up the running averages, and then
          # checking the means and variances of activations after a test-time
          # forward pass.
          N, D1, D2, D3 = 200, 50, 60, 3
          W1 = np.random.randn(D1, D2)
          W2 = np.random.randn(D2, D3)
          bn_param = {'mode': 'train'}
          gamma = np.ones(D3)
          beta = np.zeros(D3)
          for t in np.arange(50):
              X = np.random.randn(N, D1)
              a = np.maximum(0, X.dot(W1)).dot(W2)
              batchnorm_forward(a, gamma, beta, bn_param)
          bn_param['mode'] = 'test'
          X = np.random.randn(N, D1)
          a = np.maximum(0, X.dot(W1)).dot(W2)
          a norm, = batchnorm forward(a, gamma, beta, bn param)
          # Means should be close to zero and stds close to one, but will be
          # noisier than training-time forward passes.
          print('After batch normalization (test-time):')
          print(' means: ', a_norm.mean(axis=0))
          print(' stds: ', a_norm.std(axis=0))
          After batch normalization (test-time):
            means: [-0.12520334 0.03169338 -0.10871976]
```

#### **Batchnorm backward pass**

Implement the backward pass for the batchnorm layer, batchnorm\_backward in nndl/layers.py. Check your implementation by running the following cell.

stds: [ 0.98302246 1.06115622 0.9800847 ]

```
In [107]: # Gradient check batchnorm backward pass
          N, D = 4, 5
          x = 5 * np.random.randn(N, D) + 12
          gamma = np.random.randn(D)
          beta = np.random.randn(D)
          dout = np.random.randn(N, D)
          bn param = {'mode': 'train'}
          fx = lambda x: batchnorm forward(x, gamma, beta, bn_param)[0]
          fg = lambda a: batchnorm forward(x, gamma, beta, bn param)[0]
          fb = lambda b: batchnorm_forward(x, gamma, beta, bn_param)[0]
          dx num = eval numerical gradient array(fx, x, dout)
          da_num = eval_numerical_gradient_array(fg, gamma, dout)
          db_num = eval_numerical_gradient_array(fb, beta, dout)
          _, cache = batchnorm_forward(x, gamma, beta, bn_param)
          dx, dgamma, dbeta = batchnorm_backward(dout, cache)
          print('dx error: ', rel error(dx num, dx))
          print('dgamma error: ', rel_error(da_num, dgamma))
          print('dbeta error: ', rel_error(db_num, dbeta))
```

dx error: 1.07887042453e-08
dgamma error: 3.91230230411e-12
dbeta error: 3.275632498e-12

# Implement a fully connected neural network with batchnorm layers

Modify the FullyConnectedNet() class in nndl/fc\_net.py to incorporate batchnorm layers. You will need to modify the class in the following areas:

- (1) The gammas and betas need to be initialized to 1's and 0's respectively in init .
- (2) The batchnorm\_forward layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in loss. You may find it helpful to write an affine batchnorm relu() layer in nndl/layer utils.py although this is not necessary.
- (3) The batchnorm backward layer has to be appropriately inserted when calculating gradients.

After you have done the appropriate modifications, check your implementation by running the following cell.

Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of 1e-4.

```
In [110]: N, D, H1, H2, C = 2, 15, 20, 30, 10
          X = np.random.randn(N, D)
          y = np.random.randint(C, size=(N,))
          for reg in [0, 3.14]:
              print('Running check with reg = ', reg)
              model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                                         reg=reg, weight scale=5e-2, dtype=np.float
          64,
                                         use_batchnorm=True)
              loss, grads = model.loss(X, y)
              print('Initial loss: ', loss)
              for name in sorted(grads):
                  f = lambda _: model.loss(X, y)[0]
                  grad num = eval numerical_gradient(f, model.params[name], verbos
          e=False, h=1e-5)
                  print('{} relative error: {}'.format(name, rel_error(grad_num, g
          rads[name])))
              if reg == 0: print('\n')
          Running check with reg = 0
          Initial loss: 2.37550324114
          W1 relative error: 2.5250800155846695e-05
          W2 relative error: 3.1560116076513482e-06
          W3 relative error: 3.7607669218777525e-09
          b1 relative error: 8.881784197001252e-08
          b2 relative error: 1.7763568394002505e-07
          b3 relative error: 9.715024840958827e-11
          beta1 relative error: 3.806370367623448e-09
          beta2 relative error: 9.177122630132558e-09
          gamma1 relative error: 3.7867058979219295e-09
          gamma2 relative error: 2.192083533359919e-08
          Running check with reg = 3.14
          Initial loss: 6.78691714346
          W1 relative error: 1.3602838123779969e-05
          W2 relative error: 8.535026950236369e-05
          W3 relative error: 1.4038802449162061e-08
          b1 relative error: 2.7755575615628914e-09
          b2 relative error: 2.7755575615628914e-09
          b3 relative error: 2.0053175255047105e-10
```

# Training a deep fully connected network with batch normalization.

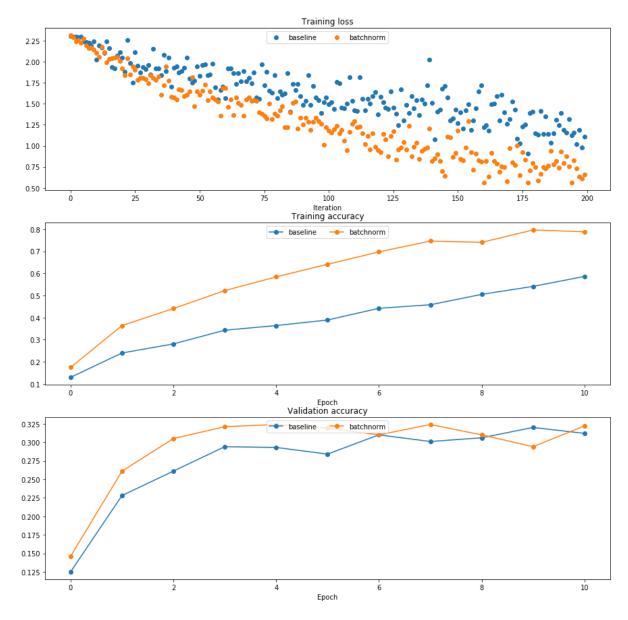
beta1 relative error: 1.3458169561958081e-08 beta2 relative error: 4.947752574014418e-08 gamma1 relative error: 2.505266413628674e-08 gamma2 relative error: 2.205089720209133e-08

To see if batchnorm helps, let's train a deep neural network with and without batch normalization.

```
In [73]:
         # Try training a very deep net with batchnorm
         hidden dims = [100, 100, 100, 100, 100]
         num_train = 1000
         small_data = {
              'X train': data['X_train'][:num_train],
              'y_train': data['y_train'][:num_train],
             'X val': data['X val'],
              'y_val': data['y_val'],
         }
         weight_scale = 2e-2
         bn model = FullyConnectedNet(hidden dims, weight scale=weight scale, use
          batchnorm=True)
         model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_ba
         tchnorm=False)
         bn_solver = Solver(bn_model, small_data,
                          num epochs=10, batch size=50,
                          update rule='adam',
                          optim config={
                            'learning_rate': 1e-3,
                          },
                          verbose=True, print every=200)
         bn_solver.train()
         solver = Solver(model, small data,
                          num_epochs=10, batch_size=50,
                          update_rule='adam',
                          optim config={
                            'learning_rate': 1e-3,
                          verbose=True, print_every=200)
         solver.train()
```

```
(Iteration 1 / 200) loss: 2.311435
(Epoch 0 / 10) train acc: 0.175000; val acc: 0.146000
(Epoch 1 / 10) train acc: 0.364000; val acc: 0.261000
(Epoch 2 / 10) train acc: 0.441000; val_acc: 0.305000
(Epoch 3 / 10) train acc: 0.522000; val acc: 0.321000
(Epoch 4 / 10) train acc: 0.584000; val acc: 0.324000
(Epoch 5 / 10) train acc: 0.641000; val acc: 0.319000
(Epoch 6 / 10) train acc: 0.697000; val acc: 0.310000
(Epoch 7 / 10) train acc: 0.746000; val acc: 0.324000
(Epoch 8 / 10) train acc: 0.740000; val_acc: 0.310000
(Epoch 9 / 10) train acc: 0.796000; val acc: 0.294000
(Epoch 10 / 10) train acc: 0.788000; val acc: 0.322000
(Iteration 1 / 200) loss: 2.302186
(Epoch 0 / 10) train acc: 0.130000; val acc: 0.125000
(Epoch 1 / 10) train acc: 0.240000; val acc: 0.228000
(Epoch 2 / 10) train acc: 0.281000; val_acc: 0.261000
(Epoch 3 / 10) train acc: 0.343000; val acc: 0.294000
(Epoch 4 / 10) train acc: 0.364000; val acc: 0.293000
(Epoch 5 / 10) train acc: 0.389000; val acc: 0.284000
(Epoch 6 / 10) train acc: 0.442000; val acc: 0.310000
(Epoch 7 / 10) train acc: 0.458000; val acc: 0.301000
(Epoch 8 / 10) train acc: 0.505000; val_acc: 0.306000
(Epoch 9 / 10) train acc: 0.541000; val acc: 0.320000
(Epoch 10 / 10) train acc: 0.586000; val acc: 0.312000
```

```
In [74]: fig, axes = plt.subplots(3, 1)
         ax = axes[0]
         ax.set_title('Training loss')
         ax.set_xlabel('Iteration')
         ax = axes[1]
         ax.set title('Training accuracy')
         ax.set_xlabel('Epoch')
         ax = axes[2]
         ax.set_title('Validation accuracy')
         ax.set_xlabel('Epoch')
         ax = axes[0]
         ax.plot(solver.loss_history, 'o', label='baseline')
         ax.plot(bn_solver.loss_history, 'o', label='batchnorm')
         ax = axes[1]
         ax.plot(solver.train acc history, '-o', label='baseline')
         ax.plot(bn_solver.train_acc_history, '-o', label='batchnorm')
         ax = axes[2]
         ax.plot(solver.val_acc_history, '-o', label='baseline')
         ax.plot(bn_solver.val_acc_history, '-o', label='batchnorm')
         for i in [1, 2, 3]:
             ax = axes[i - 1]
             ax.legend(loc='upper center', ncol=4)
         plt.gcf().set_size_inches(15, 15)
         plt.show()
```



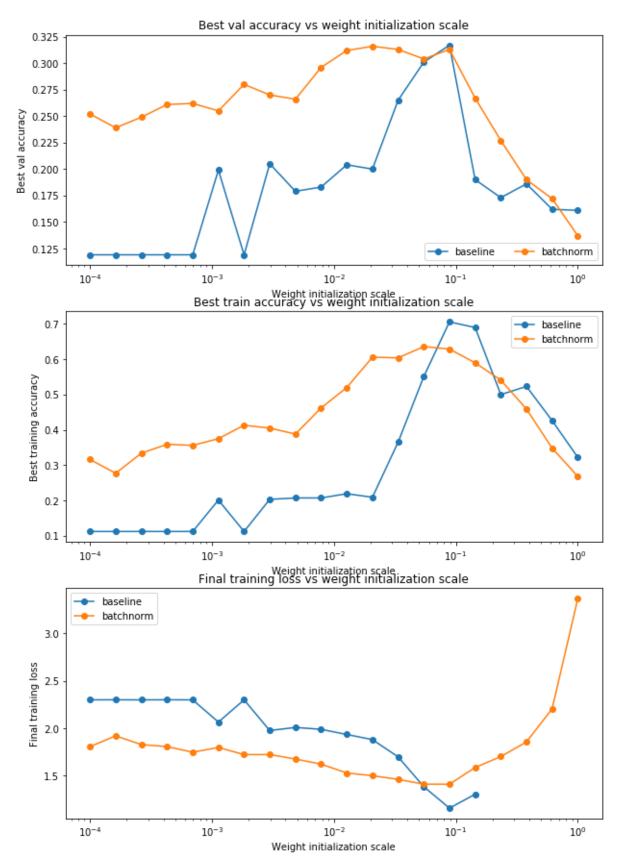
### **Batchnorm and initialization**

The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included.

```
# Try training a very deep net with batchnorm
hidden dims = [50, 50, 50, 50, 50, 50, 50]
num_train = 1000
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}
bn_solvers = {}
solvers = {}
weight scales = np.logspace(-4, 0, num=20)
for i, weight_scale in enumerate(weight_scales):
    print('Running weight scale {} / {}'.format(i + 1, len(weight_scales
)))
    bn model = FullyConnectedNet(hidden dims, weight scale=weight scale,
use batchnorm=True)
    model = FullyConnectedNet(hidden dims, weight scale=weight scale, us
e batchnorm=False)
    bn_solver = Solver(bn_model, small_data,
                    num_epochs=10, batch_size=50,
                    update_rule='adam',
                    optim_config={
                       'learning_rate': 1e-3,
                     },
                    verbose=False, print_every=200)
    bn solver.train()
    bn_solvers[weight_scale] = bn_solver
    solver = Solver(model, small_data,
                    num_epochs=10, batch_size=50,
                    update_rule='adam',
                    optim config={
                       'learning_rate': 1e-3,
                    verbose=False, print every=200)
    solver.train()
    solvers[weight_scale] = solver
```

```
Running weight scale 1 / 20
Running weight scale 2 / 20
Running weight scale 3 / 20
Running weight scale 4 / 20
Running weight scale 5 / 20
Running weight scale 6 / 20
Running weight scale 7 / 20
Running weight scale 8 / 20
Running weight scale 9 / 20
Running weight scale 10 / 20
Running weight scale 11 / 20
Running weight scale 12 / 20
Running weight scale 13 / 20
Running weight scale 14 / 20
Running weight scale 15 / 20
Running weight scale 16 / 20
/Users/jackzhang/GoogleDrive/UCLA/Academics/Junior/Q2/EC ENGR C247/HW4/
nndl/layers.py:434: RuntimeWarning: divide by zero encountered in log
 return loss, dx
Running weight scale 17 / 20
Running weight scale 18 / 20
Running weight scale 19 / 20
Running weight scale 20 / 20
```

```
In [76]: # Plot results of weight scale experiment
         best train accs, bn best train accs = [], []
         best_val_accs, bn_best_val_accs = [], []
         final_train_loss, bn_final_train_loss = [], []
         for ws in weight scales:
             best_train_accs.append(max(solvers[ws].train_acc_history))
             bn best train accs.append(max(bn solvers[ws].train acc history))
             best_val_accs.append(max(solvers[ws].val_acc_history))
             bn best val accs.append(max(bn solvers[ws].val acc history))
             final train loss.append(np.mean(solvers[ws].loss history[-100:]))
             bn final train loss.append(np.mean(bn solvers[ws].loss history[-100
         :]))
         plt.subplot(3, 1, 1)
         plt.title('Best val accuracy vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Best val accuracy')
         plt.semilogx(weight_scales, best_val_accs, '-o', label='baseline')
         plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
         plt.legend(ncol=2, loc='lower right')
         plt.subplot(3, 1, 2)
         plt.title('Best train accuracy vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Best training accuracy')
         plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
         plt.semilogx(weight scales, bn best train accs, '-o', label='batchnorm')
         plt.legend()
         plt.subplot(3, 1, 3)
         plt.title('Final training loss vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Final training loss')
         plt.semilogx(weight scales, final train loss, '-o', label='baseline')
         plt.semilogx(weight_scales, bn_final_train_loss, '-o', label='batchnorm'
         )
         plt.legend()
         plt.gcf().set size inches(10, 15)
         plt.show()
```



### **Question:**

In the cell below, summarize the findings of this experiment, and WHY these results make sense.

#### **Answer:**

In the graphs, we can see that batch normalization helps to increase accuracy and decrease loss. This makes sense since normalizing the hidden layers helps keep changes predictable when updating all the weights at the same time.

Also, we can see that batch normalization greatly outperforms the base model for extreme weight initializations. For example, at around 0.1, the base model's performance is similar to the batch normalization model's performance. However, as soon as the weight begins to deviate from 0.1, we see an extreme dropoff in the base model's performance. The reason is that without batch normalization, there is a strong dependence on choosing the correct weight initilizations. This is also why the batch normalization model still works after the 16th training iteration, when the weight initialization becomes too large and the base model begins to encounter problems.

### **Dropout**

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [1]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc net import *
        from nndl.layers import *
        from cs231n.data_utils import get_CIFAR10_data
        from cs231n.gradient_check import eval numerical_gradient, eval_numerica
        l gradient array
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
        n-ipython
        %load ext autoreload
        %autoreload 2
        def rel error(x, y):
            """ returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))
        ))))
In [2]: # Load the (preprocessed) CIFAR10 data.
```

```
In [2]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
    y_val: (1000,)
    X_test: (1000, 3, 32, 32)
    y test: (1000,)
```

#### **Dropout forward pass**

Implement the training and test time dropout forward pass, dropout\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [3]: x = np.random.randn(500, 500) + 10

for p in [0.3, 0.6, 0.75]:
    out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
    out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})

    print('Running tests with p = ', p)
    print('Mean of input: ', x.mean())
    print('Mean of train-time output: ', out.mean())
    print('Mean of test-time output: ', out_test.mean())
    print('Fraction of train-time output set to zero: ', (out == 0).mean
())
    print('Fraction of test-time output set to zero: ', (out_test == 0).
    mean())
```

```
Running tests with p = 0.3
Mean of input: 10.0009276157
Mean of train-time output: 10.0184373302
Mean of test-time output: 10.0009276157
Fraction of train-time output set to zero: 0.699484
Fraction of test-time output set to zero:
Running tests with p = 0.6
Mean of input: 10.0009276157
Mean of train-time output: 9.99599440569
Mean of test-time output: 10.0009276157
Fraction of train-time output set to zero: 0.40014
Fraction of test-time output set to zero:
Running tests with p = 0.75
Mean of input: 10.0009276157
Mean of train-time output: 9.98951728772
Mean of test-time output: 10.0009276157
Fraction of train-time output set to zero: 0.250892
Fraction of test-time output set to zero: 0.0
```

#### **Dropout backward pass**

Implement the backward pass, dropout\_backward, in nndl/layers.py. After that, test your gradients by running the following cell:

```
In [12]: x = np.random.randn(10, 10) + 10
    dout = np.random.randn(*x.shape)

dropout_param = {'mode': 'train', 'p': 0.8, 'seed': 123}
    out, cache = dropout_forward(x, dropout_param)
    dx = dropout_backward(dout, cache)
    dx_num = eval_numerical_gradient_array(lambda xx: dropout_forward(xx, dropout_param)[0], x, dout)

print('dx relative error: ', rel_error(dx, dx_num))
```

dx relative error: 5.4456110067e-11

# Implement a fully connected neural network with dropout layers

Modify the FullyConnectedNet() class in nndl/fc\_net.py to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

- (1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.
- (2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

```
In [29]: N, D, H1, H2, C = 2, 15, 20, 30, 10
         X = np.random.randn(N, D)
         y = np.random.randint(C, size=(N,))
         for dropout in [0.5, 0.75, 1.0]:
             print('Running check with dropout = ', dropout)
             model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                                       weight scale=5e-2, dtype=np.float64,
                                       dropout=dropout, seed=123)
             loss, grads = model.loss(X, y)
             print('Initial loss: ', loss)
             for name in sorted(grads):
                 f = lambda _: model.loss(X, y)[0]
                 grad num = eval numerical_gradient(f, model.params[name], verbos
         e=False, h=1e-5)
                 print('{} relative error: {}'.format(name, rel error(grad num, g
         rads[name])))
             print('\n')
         Running check with dropout = 0.5
         Initial loss: 2.29788023816
         W1 relative error: 1.4081197329537414e-06
         W2 relative error: 2.2537391051352578e-08
         W3 relative error: 4.103582939046388e-08
         b1 relative error: 3.0008795128604203e-08
         b2 relative error: 1.1540244338464926e-09
         b3 relative error: 1.2912061432212848e-10
         Running check with dropout = 0.75
         Initial loss: 2.30823414062
         W1 relative error: 2.6453375927214743e-07
         W2 relative error: 1.3070188356021375e-07
         W3 relative error: 2.223975213558462e-07
         b1 relative error: 7.112910572926549e-09
         b2 relative error: 5.347954717817801e-09
         b3 relative error: 1.0886215791527195e-10
         Running check with dropout = 1.0
         Initial loss: 2.30662260831
         W1 relative error: 2.998747145573698e-07
         W2 relative error: 1.4466533842741292e-06
         W3 relative error: 8.24336812277723e-08
         b1 relative error: 1.5773079555112075e-08
         b2 relative error: 6.4687895564047865e-09
         b3 relative error: 1.223192314770519e-10
```

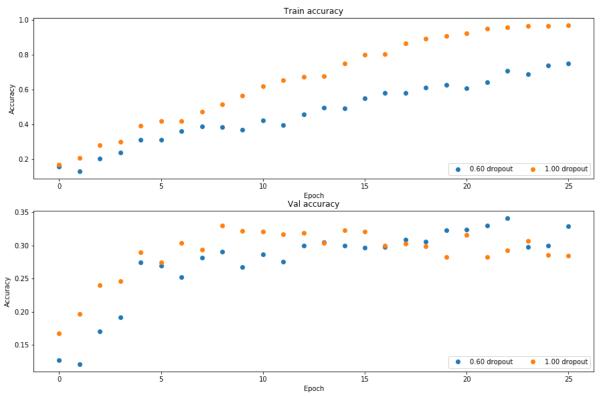
# Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

```
In [30]: # Train two identical nets, one with dropout and one without
         num_train = 500
         small_data = {
              'X_train': data['X_train'][:num_train],
              'y_train': data['y_train'][:num_train],
              'X val': data['X_val'],
              'y_val': data['y_val'],
         }
         solvers = {}
         dropout_choices = [0.6, 1.0]
         for dropout in dropout_choices:
             model = FullyConnectedNet([100, 100, 100], dropout=dropout)
             solver = Solver(model, small_data,
                              num_epochs=25, batch_size=100,
                              update_rule='adam',
                              optim_config={
                                'learning rate': 5e-4,
                              },
                              verbose=True, print_every=100)
             solver.train()
             solvers[dropout] = solver
```

```
(Iteration 1 / 125) loss: 2.300199
(Epoch 0 / 25) train acc: 0.158000; val acc: 0.127000
(Epoch 1 / 25) train acc: 0.132000; val acc: 0.121000
(Epoch 2 / 25) train acc: 0.204000; val_acc: 0.170000
(Epoch 3 / 25) train acc: 0.240000; val acc: 0.192000
(Epoch 4 / 25) train acc: 0.312000; val acc: 0.274000
(Epoch 5 / 25) train acc: 0.314000; val acc: 0.269000
(Epoch 6 / 25) train acc: 0.364000; val acc: 0.252000
(Epoch 7 / 25) train acc: 0.390000; val acc: 0.281000
(Epoch 8 / 25) train acc: 0.386000; val_acc: 0.290000
(Epoch 9 / 25) train acc: 0.372000; val acc: 0.267000
(Epoch 10 / 25) train acc: 0.424000; val acc: 0.286000
(Epoch 11 / 25) train acc: 0.396000; val acc: 0.275000
(Epoch 12 / 25) train acc: 0.458000; val acc: 0.299000
(Epoch 13 / 25) train acc: 0.496000; val acc: 0.305000
(Epoch 14 / 25) train acc: 0.492000; val_acc: 0.299000
(Epoch 15 / 25) train acc: 0.550000; val acc: 0.296000
(Epoch 16 / 25) train acc: 0.584000; val acc: 0.297000
(Epoch 17 / 25) train acc: 0.582000; val acc: 0.309000
(Epoch 18 / 25) train acc: 0.612000; val acc: 0.306000
(Epoch 19 / 25) train acc: 0.628000; val acc: 0.323000
(Epoch 20 / 25) train acc: 0.608000; val_acc: 0.324000
(Iteration 101 / 125) loss: 1.369535
(Epoch 21 / 25) train acc: 0.644000; val acc: 0.330000
(Epoch 22 / 25) train acc: 0.708000; val acc: 0.341000
(Epoch 23 / 25) train acc: 0.690000; val_acc: 0.297000
(Epoch 24 / 25) train acc: 0.740000; val acc: 0.300000
(Epoch 25 / 25) train acc: 0.750000; val_acc: 0.329000
(Iteration 1 / 125) loss: 2.300607
(Epoch 0 / 25) train acc: 0.172000; val acc: 0.167000
(Epoch 1 / 25) train acc: 0.210000; val acc: 0.197000
(Epoch 2 / 25) train acc: 0.284000; val_acc: 0.240000
(Epoch 3 / 25) train acc: 0.302000; val acc: 0.246000
(Epoch 4 / 25) train acc: 0.392000; val acc: 0.289000
(Epoch 5 / 25) train acc: 0.420000; val_acc: 0.274000
(Epoch 6 / 25) train acc: 0.420000; val acc: 0.304000
(Epoch 7 / 25) train acc: 0.474000; val acc: 0.293000
(Epoch 8 / 25) train acc: 0.516000; val acc: 0.330000
(Epoch 9 / 25) train acc: 0.566000; val acc: 0.322000
(Epoch 10 / 25) train acc: 0.620000; val acc: 0.321000
(Epoch 11 / 25) train acc: 0.656000; val_acc: 0.317000
(Epoch 12 / 25) train acc: 0.676000; val acc: 0.319000
(Epoch 13 / 25) train acc: 0.680000; val acc: 0.304000
(Epoch 14 / 25) train acc: 0.752000; val acc: 0.323000
(Epoch 15 / 25) train acc: 0.802000; val acc: 0.321000
(Epoch 16 / 25) train acc: 0.804000; val_acc: 0.300000
(Epoch 17 / 25) train acc: 0.868000; val acc: 0.303000
(Epoch 18 / 25) train acc: 0.894000; val acc: 0.298000
(Epoch 19 / 25) train acc: 0.910000; val acc: 0.282000
(Epoch 20 / 25) train acc: 0.926000; val acc: 0.316000
(Iteration 101 / 125) loss: 0.245816
(Epoch 21 / 25) train acc: 0.950000; val acc: 0.282000
(Epoch 22 / 25) train acc: 0.958000; val_acc: 0.292000
(Epoch 23 / 25) train acc: 0.966000; val acc: 0.307000
(Epoch 24 / 25) train acc: 0.966000; val acc: 0.285000
(Epoch 25 / 25) train acc: 0.970000; val acc: 0.284000
```

```
# Plot train and validation accuracies of the two models
train_accs = []
val_accs = []
for dropout in dropout_choices:
    solver = solvers[dropout]
    train_accs.append(solver.train_acc_history[-1])
    val accs.append(solver.val acc history[-1])
plt.subplot(3, 1, 1)
for dropout in dropout_choices:
    plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropou
t' % dropout)
plt.title('Train accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')
plt.subplot(3, 1, 2)
for dropout in dropout choices:
    plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout'
% dropout)
plt.title('Val accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')
plt.gcf().set_size_inches(15, 15)
plt.show()
```



# Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

## **Answer:**

As we can see in the training accuracy graph, when dropout is occuring, activations are being thrown away, causing the model to be less powerful, but more generalized. Thus, the model with dropout avoids overfitting the training data. Our validation accuracy graph supports this, as the model with dropout narrowly beats the model without after around 16 epochs.

## Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

min(floor((X - 32%)) / 23%, 1) where if you get 55% or higher validation accuracy, you get full points.

```
# ----- #
In [32]:
      # YOUR CODE HERE:
         Implement a FC-net that achieves at least 55% validation accuracy
         on CIFAR-10.
      # ============ #
      optimizer = 'adam'
      best_model = None
      layer_dims = [500, 500, 500]
      weight scale = 0.01
      learning_rate = 1e-3
      lr_decay = 0.9
      model = FullyConnectedNet(layer_dims, weight_scale=weight_scale,
                         use_batchnorm=True, dropout=0.6)
      solver = Solver(model, data,
                  num_epochs=10, batch_size=100,
                  update rule=optimizer,
                  optim_config={
                   'learning_rate': learning_rate,
                  lr decay=lr decay,
                  verbose=True, print_every=50)
      solver.train()
      # END YOUR CODE HERE
```

```
(Iteration 1 / 4900) loss: 2.315670
(Epoch 0 / 10) train acc: 0.172000; val acc: 0.159000
(Iteration 51 / 4900) loss: 1.985675
(Iteration 101 / 4900) loss: 1.752022
(Iteration 151 / 4900) loss: 1.637101
(Iteration 201 / 4900) loss: 1.849953
(Iteration 251 / 4900) loss: 1.622382
(Iteration 301 / 4900) loss: 1.635581
(Iteration 351 / 4900) loss: 1.430959
(Iteration 401 / 4900) loss: 1.632563
(Iteration 451 / 4900) loss: 1.690440
(Epoch 1 / 10) train acc: 0.452000; val acc: 0.462000
(Iteration 501 / 4900) loss: 1.366797
(Iteration 551 / 4900) loss: 1.400385
(Iteration 601 / 4900) loss: 1.649626
(Iteration 651 / 4900) loss: 1.725212
(Iteration 701 / 4900) loss: 1.291366
(Iteration 751 / 4900) loss: 1.458295
(Iteration 801 / 4900) loss: 1.475591
(Iteration 851 / 4900) loss: 1.621632
(Iteration 901 / 4900) loss: 1.426365
(Iteration 951 / 4900) loss: 1.594802
(Epoch 2 / 10) train acc: 0.494000; val acc: 0.486000
(Iteration 1001 / 4900) loss: 1.598037
(Iteration 1051 / 4900) loss: 1.504805
(Iteration 1101 / 4900) loss: 1.474550
(Iteration 1151 / 4900) loss: 1.545481
(Iteration 1201 / 4900) loss: 1.501066
(Iteration 1251 / 4900) loss: 1.226699
(Iteration 1301 / 4900) loss: 1.376705
(Iteration 1351 / 4900) loss: 1.310161
(Iteration 1401 / 4900) loss: 1.475299
(Iteration 1451 / 4900) loss: 1.367088
(Epoch 3 / 10) train acc: 0.518000; val acc: 0.501000
(Iteration 1501 / 4900) loss: 1.479137
(Iteration 1551 / 4900) loss: 1.766190
(Iteration 1601 / 4900) loss: 1.358386
(Iteration 1651 / 4900) loss: 1.297767
(Iteration 1701 / 4900) loss: 1.356515
(Iteration 1751 / 4900) loss: 1.300821
(Iteration 1801 / 4900) loss: 1.404942
(Iteration 1851 / 4900) loss: 1.595150
(Iteration 1901 / 4900) loss: 1.428987
(Iteration 1951 / 4900) loss: 1.248848
(Epoch 4 / 10) train acc: 0.551000; val acc: 0.524000
(Iteration 2001 / 4900) loss: 1.256842
(Iteration 2051 / 4900) loss: 1.317723
(Iteration 2101 / 4900) loss: 1.351787
(Iteration 2151 / 4900) loss: 1.359591
(Iteration 2201 / 4900) loss: 1.378969
(Iteration 2251 / 4900) loss: 1.211360
(Iteration 2301 / 4900) loss: 1.364973
(Iteration 2351 / 4900) loss: 1.313382
(Iteration 2401 / 4900) loss: 1.263512
(Epoch 5 / 10) train acc: 0.583000; val acc: 0.559000
(Iteration 2451 / 4900) loss: 1.348116
(Iteration 2501 / 4900) loss: 1.174153
```

```
(Iteration 2551 / 4900) loss: 1.235559
(Iteration 2601 / 4900) loss: 1.203556
(Iteration 2651 / 4900) loss: 1.390703
(Iteration 2701 / 4900) loss: 1.180792
(Iteration 2751 / 4900) loss: 1.442741
(Iteration 2801 / 4900) loss: 1.121575
(Iteration 2851 / 4900) loss: 1.213788
(Iteration 2901 / 4900) loss: 1.299856
(Epoch 6 / 10) train acc: 0.601000; val acc: 0.548000
(Iteration 2951 / 4900) loss: 1.331210
(Iteration 3001 / 4900) loss: 1.147929
(Iteration 3051 / 4900) loss: 1.180255
(Iteration 3101 / 4900) loss: 1.293730
(Iteration 3151 / 4900) loss: 1.164596
(Iteration 3201 / 4900) loss: 1.238197
(Iteration 3251 / 4900) loss: 1.171942
(Iteration 3301 / 4900) loss: 1.323456
(Iteration 3351 / 4900) loss: 1.256149
(Iteration 3401 / 4900) loss: 1.414370
(Epoch 7 / 10) train acc: 0.593000; val acc: 0.564000
(Iteration 3451 / 4900) loss: 1.392587
(Iteration 3501 / 4900) loss: 1.355776
(Iteration 3551 / 4900) loss: 1.209341
(Iteration 3601 / 4900) loss: 1.105936
(Iteration 3651 / 4900) loss: 1.300336
(Iteration 3701 / 4900) loss: 1.323444
(Iteration 3751 / 4900) loss: 1.149997
(Iteration 3801 / 4900) loss: 1.178634
(Iteration 3851 / 4900) loss: 1.216717
(Iteration 3901 / 4900) loss: 1.178940
(Epoch 8 / 10) train acc: 0.643000; val acc: 0.565000
(Iteration 3951 / 4900) loss: 1.142942
(Iteration 4001 / 4900) loss: 1.104936
(Iteration 4051 / 4900) loss: 1.169886
(Iteration 4101 / 4900) loss: 1.374895
(Iteration 4151 / 4900) loss: 1.298176
(Iteration 4201 / 4900) loss: 1.123109
(Iteration 4251 / 4900) loss: 1.226131
(Iteration 4301 / 4900) loss: 1.226938
(Iteration 4351 / 4900) loss: 1.363159
(Iteration 4401 / 4900) loss: 1.035636
(Epoch 9 / 10) train acc: 0.609000; val acc: 0.571000
(Iteration 4451 / 4900) loss: 1.307827
(Iteration 4501 / 4900) loss: 1.255807
(Iteration 4551 / 4900) loss: 1.253609
(Iteration 4601 / 4900) loss: 1.087653
(Iteration 4651 / 4900) loss: 1.070275
(Iteration 4701 / 4900) loss: 1.171748
(Iteration 4751 / 4900) loss: 1.228380
(Iteration 4801 / 4900) loss: 1.149847
(Iteration 4851 / 4900) loss: 0.974690
(Epoch 10 / 10) train acc: 0.665000; val acc: 0.567000
```

```
import numpy as np
import pdb
.....
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use
in the
ECE 239AS class at UCLA. This includes the descriptions of what code
implement as well as some slight potential changes in variable names
to be
consistent with class nomenclature. We thank Justin Johnson & Serena
Yeung for
permission to use this code. To see the original version, please
cs231n.stanford.edu.
.....
def affine_forward(x, w, b):
   Computes the forward pass for an affine (fully-connected) layer.
   The input x has shape (N, d_1, \ldots, d_k) and contains a minibatch
of N
   examples, where each example x[i] has shape (d_1, \ldots, d_k). We
will
   reshape each input into a vector of dimension D = d_1 * ... * d_k,
and
   then transform it to an output vector of dimension M.
   Inputs:

    x: A numpy array containing input data, of shape (N, d_1, ...,

dk)
   w: A numpy array of weights, of shape (D, M)
   - b: A numpy array of biases, of shape (M,)
   Returns a tuple of:
   out: output, of shape (N, M)
   - cache: (x, w, b)
   1111111
   out = None
   #
   # YOUR CODE HERE:
       Calculate the output of the forward pass. Notice the
dimensions
       of w are D x M, which is the transpose of what we did in
earlier
       assignments.
```

```
#
   rx = x.reshape(x.shape[0], -1)
   out = rx.dot(w) + b
   #
   # END YOUR CODE HERE
   cache = (x, w, b)
   return out, cache
def affine_backward(dout, cache):
   Computes the backward pass for an affine layer.
   Inputs:

    dout: Upstream derivative, of shape (N, M)

   - cache: Tuple of:
     x: A numpy array containing input data, of shape (N, d_1, ...,
d_k)
     w: A numpy array of weights, of shape (D, M)
     b: A numpy array of biases, of shape (M,)
   Returns a tuple of:
   - dx: Gradient with respect to x, of shape (N, d1, ..., d_k)

    dw: Gradient with respect to w, of shape (D, M)

    db: Gradient with respect to b, of shape (M,)

   1111111
   x, w, b = cache
   dx, dw, db = None, None, None
   #
   # YOUR CODE HERE:
      Calculate the gradients for the backward pass.
   # Notice:
      dout is N x M
      dx should be N x d1 x ... x dk; it relates to dout through
multiplication with w, which is D \times M
      dw should be D \times M; it relates to dout through multiplication
with x, which is N \times D after reshaping
   # db should be M; it is just the sum over dout examples
   #
   rx = x.reshape(x.shape[0], -1)
```

```
dx = dout.dot(w.T).reshape(x.shape)
  dw = rx.T.dot(dout)
  db = np.sum(dout.T, axis=1)
  #
  # END YOUR CODE HERE
  #
  return dx, dw, db
def relu_forward(x):
  Computes the forward pass for a layer of rectified linear units
(ReLUs).
  Input:
  - x: Inputs, of any shape
  Returns a tuple of:
  - out: Output, of the same shape as x
  - cache: x
  # YOUR CODE HERE:
     Implement the ReLU forward pass.
         -----
#
  out = x * (x > 0)
  #
  # END YOUR CODE HERE
  #
  cache = x
  return out, cache
def relu_backward(dout, cache):
  Computes the backward pass for a layer of rectified linear units
(ReLUs).
  Input:
```

```
    dout: Upstream derivatives, of any shape

   - cache: Input x, of same shape as dout
   Returns:

    dx: Gradient with respect to x

   x = cache
   #
   # YOUR CODE HERE:
       Implement the ReLU backward pass
   dx = dout * (x > 0)
   # END YOUR CODE HERE
#
   return dx
def batchnorm_forward(x, gamma, beta, bn_param):
   Forward pass for batch normalization.
   During training the sample mean and (uncorrected) sample variance
are
   computed from minibatch statistics and used to normalize the
incoming data.
   During training we also keep an exponentially decaying running
mean of the mean
   and variance of each feature, and these averages are used to
normalize data
   at test-time.
   At each timestep we update the running averages for mean and
variance using
   an exponential decay based on the momentum parameter:
   running_mean = momentum * running_mean + (1 - momentum) *
sample_mean
   running_var = momentum * running_var + (1 - momentum) * sample_var
   Note that the batch normalization paper suggests a different test-
time
   behavior: they compute sample mean and variance for each feature
```

```
using a
    large number of training images rather than using a running
average. For
   this implementation we have chosen to use running averages instead
since
    they do not require an additional estimation step; the torch7
implementation
   of batch normalization also uses running averages.
   Input:
   - x: Data of shape (N, D)
   gamma: Scale parameter of shape (D,)
   - beta: Shift paremeter of shape (D,)
   - bn_param: Dictionary with the following keys:
     - mode: 'train' or 'test'; required
     - eps: Constant for numeric stability
     - momentum: Constant for running mean / variance.
      - running_mean: Array of shape (D,) giving running mean of
features
      - running_var Array of shape (D,) giving running variance of
features
   Returns a tuple of:
   - out: of shape (N, D)

    cache: A tuple of values needed in the backward pass

   mode = bn param['mode']
    eps = bn_param.get('eps', 1e-5)
   momentum = bn_param.get('momentum', 0.9)
   N, D = x.shape
    running_mean = bn_param.get('running_mean', np.zeros(D,
dtvpe=x.dtvpe))
    running var = bn param.get('running var', np.zeros(D,
dtype=x.dtype))
   out, cache = None, None
    if mode == 'train':
       #
______#
       # YOUR CODE HERE:
           A few steps here:
             (1) Calculate the running mean and variance of the
minibatch.
             (2) Normalize the activations with the running mean and
variance.
             (3) Scale and shift the normalized activations. Store
this
                 as the variable 'out'
       #
```

```
(4) Store any variables you may need for the backward
pass in
            the 'cache' variable.
______#
     num train = x.shape[0]
     sample_mean = (np.sum(x, axis=0)) / num_train
     sample_var = (np.sum((x - sample_mean)**2, axis=0)) /
num_train
     running_mean = momentum * running_mean + (1 - momentum) *
sample_mean
     running_var = momentum * running_var + (1 - momentum) *
sample_var
     x_{hat} = (x - sample_mean) / np.sqrt(sample_var + eps)
     out = x_hat * gamma + beta
     cache = (x, x_hat, sample_mean, sample_var, eps, gamma, beta)
     #
______ #
     # END YOUR CODE HERE
______#
  elif mode == 'test':
______#
     # YOUR CODE HERE:
        Calculate the testing time normalized activation.
Normalize using
        the running mean and variance, and then scale and shift
appropriately.
        Store the output as 'out'.
     #
______#
     x_hat = (x - running_mean) / np.sqrt(running_var + eps)
     out = x hat * gamma + beta
          # END YOUR CODE HERE
______ #
  else:
```

```
raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
   # Store the updated running means back into bn param
   bn_param['running_mean'] = running_mean
   bn param['running var'] = running var
   return out, cache
def batchnorm backward(dout, cache):
   Backward pass for batch normalization.
   For this implementation, you should write out a computation graph
for
   batch normalization on paper and propagate gradients backward
through
   intermediate nodes.
   Inputs:

    dout: Upstream derivatives, of shape (N, D)

   - cache: Variable of intermediates from batchnorm_forward.
   Returns a tuple of:

    dx: Gradient with respect to inputs x, of shape (N, D)

   - dgamma: Gradient with respect to scale parameter gamma, of shape
(D,)

    dbeta: Gradient with respect to shift parameter beta, of shape

(D,)
   dx, dgamma, dbeta = None, None, None
   #
   # YOUR CODE HERE:
       Implement the batchnorm backward pass, calculating dx, dgamma,
and dbeta.
   #
   x, x_hat, sample_mean, sample_var, eps, gamma, beta = cache
   num\_train = x.shape[0]
   dldy = dout
   dldbeta = np.sum(dldy, axis=0)
   dldgamma = np.sum(dldy * x_hat, axis=0)
   dldx_hat = dldy * gamma
   dlda = 1 / np.sqrt(sample_var + eps) * dldx_hat
   dldb = (x - sample_mean) * dldx_hat
   dldc = -1 / (sample var + eps) * dldb
   dlde = -1 / (2 * (sample_var + eps)**(3/2)) * dldb
```

```
dldv = np.sum(dlde, axis=0)
   dldmu = -1 / np.sqrt(sample_var + eps) * np.sum(dldx_hat, axis=0)
- dldv * 2 * np.mean(x - sample_mean, axis=0)
   dvdx = 2 / num_train * (x - sample_mean)
   dldx = dlda + dvdx * dldv + 1 / num train * dldmu
   dx = dldx
   dgamma = dldgamma
   dbeta = dldbeta
   #
   # END YOUR CODE HERE
   return dx, dgamma, dbeta
def dropout_forward(x, dropout_param):
   Performs the forward pass for (inverted) dropout.
   Inputs:
   - x: Input data, of any shape
   - dropout_param: A dictionary with the following keys:
     - p: Dropout parameter. We keep each neuron output with
probability p.
     - mode: 'test' or 'train'. If the mode is train, then perform
dropout;
       if the mode is test, then just return the input.

    seed: Seed for the random number generator. Passing seed makes

this
       function deterministic, which is needed for gradient checking
but not in
       real networks.
   Outputs:

    out: Array of the same shape as x.

   cache: A tuple (dropout param, mask). In training mode, mask is
the dropout
     mask that was used to multiply the input; in test mode, mask is
None.
   p, mode = dropout_param['p'], dropout_param['mode']
   if 'seed' in dropout param:
       np.random.seed(dropout_param['seed'])
   mask = None
   out = None
```

```
if mode == 'train':
______ #
     # YOUR CODE HERE:
       Implement the inverted dropout forward pass during
training time.
       Store the masked and scaled activations in out, and store
the
     #
       dropout mask as the variable mask.
     #
______ #
     mask = (np.random.rand(*x.shape) < p) / p</pre>
     out = mask * x
         # END YOUR CODE HERE
______ #
  elif mode == 'test':
     #
         -_____ #
     # YOUR CODE HERE:
       Implement the inverted dropout forward pass during test
time.
______#
     out = x
         # END YOUR CODE HERE
______ #
  cache = (dropout_param, mask)
  out = out.astype(x.dtype, copy=False)
  return out, cache
def dropout_backward(dout, cache):
  Perform the backward pass for (inverted) dropout.
  Inputs:

    dout: Upstream derivatives, of any shape
```

```
dropout_param, mask = cache
  mode = dropout param['mode']
  dx = None
  if mode == 'train':
______#
    # YOUR CODE HERE:
       Implement the inverted dropout backward pass during
training time.
______#
    dx = mask * dout
______#
    # END YOUR CODE HERE
______ #
  elif mode == 'test':
     # YOUR CODE HERE:
       Implement the inverted dropout backward pass during test
time.
______#
    dx = dout
      # END YOUR CODE HERE
______#
  return dx
def svm_loss(x, y):
  Computes the loss and gradient using for multiclass SVM
classification.
  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for
the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for
```

- cache: (dropout param, mask) from dropout forward.

```
x[i] and
      0 \le y[i] < C
    Returns a tuple of:
    loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
    111111
    N = x.shape[0]
    correct_class_scores = x[np.arange(N), y]
    margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] +
1.0)
    margins[np.arange(N), y] = 0
    loss = np.sum(margins) / N
    num_pos = np.sum(margins > 0, axis=1)
    dx = np.zeros_like(x)
    dx[margins > 0] = 1
    dx[np.arange(N), y] -= num_pos
    dx /= N
    return loss, dx
def softmax_loss(x, y):
    Computes the loss and gradient for softmax classification.
    Inputs:
    - x: Input data, of shape (N, C) where x[i, j] is the score for
the jth class
     for the ith input.
    - y: Vector of labels, of shape (N,) where y[i] is the label for
x[i] and
      0 \le y[i] < C
    Returns a tuple of:
    loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
    .....
    probs = np.exp(x - np.max(x, axis=1, keepdims=True))
    probs /= np.sum(probs, axis=1, keepdims=True)
    N = x.shape[0]
    loss = -np.sum(np.log(probs[np.arange(N), y])) / N
    dx = probs \cdot copy()
    dx[np.arange(N), y] = 1
    dx /= N
    return loss, dx
```

```
from .layers import *
.....
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use
in the
ECE 239AS class at UCLA. This includes the descriptions of what code
implement as well as some slight potential changes in variable names
consistent with class nomenclature. We thank Justin Johnson & Serena
Yeung for
permission to use this code. To see the original version, please
visit
cs231n.stanford.edu.
def affine_relu_forward(x, w, b):
    Convenience layer that performs an affine transform followed by a
ReLU
    Inputs:
    - x: Input to the affine layer
    - w, b: Weights for the affine layer
    Returns a tuple of:
    - out: Output from the ReLU

    cache: Object to give to the backward pass

    a, fc_cache = affine_forward(x, w, b)
    out, relu_cache = relu_forward(a)
    cache = (fc cache, relu cache)
    return out, cache
def affine batchnorm relu forward(x, w, b, gamma, beta, bn param):
    Convenience layer that performs an affine transform followed by a
batch normalization and ReLU
    Inputs:
    - x: Input to the affine layer
    - w, b: Weights for the affine layer
    Returns a tuple of:
    - out: Output from the ReLU
    - cache: Object to give to the backward pass
    a, fc_cache = affine_forward(x, w, b)
    a_bn, bn_cache = batchnorm_forward(a, gamma, beta, bn_param)
```

```
out, relu cache = relu forward(a bn)
    cache = (fc_cache, bn_cache, relu_cache)
    return out, cache
def affine_relu_backward(dout, cache):
    Backward pass for the affine-relu convenience layer
    fc_cache, relu_cache = cache
    da = relu_backward(dout, relu_cache)
    dx, dw, db = affine_backward(da, fc_cache)
    return dx, dw, db
def affine_batchnorm_relu_backward(dout, cache):
    Backward pass for the affine-relu convenience layer
    fc_cache, bn_cache, relu_cache = cache
    da = relu_backward(dout, relu_cache)
    da_bn, dgamma, dbeta = batchnorm_backward(da, bn_cache)
    dx, dw, db = affine_backward(da_bn, fc_cache)
    return dx, dw, db, dgamma, dbeta
```

## import numpy as np

#### .....

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ECE 239AS class at UCLA. This includes the descriptions of what code to

implement as well as some slight potential changes in variable names to be

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....

#### .....

This file implements various first-order update rules that are commonly used for

training neural networks. Each update rule accepts current weights and the

gradient of the loss with respect to those weights and produces the next set of

weights. Each update rule has the same interface:

def update(w, dw, config=None):

## Inputs:

- w: A numpy array giving the current weights.
- dw: A numpy array of the same shape as w giving the gradient of the

loss with respect to w.

 config: A dictionary containing hyperparameter values such as learning rate,

momentum, etc. If the update rule requires caching values over many

iterations, then config will also hold these cached values.

## Returns:

- next w: The next point after the update.
- config: The config dictionary to be passed to the next iteration of the

update rule.

NOTE: For most update rules, the default learning rate will probably not perform

well; however the default values of the other hyperparameters should work well

for a variety of different problems.

```
For efficiency, update rules may perform in-place updates, mutating w
setting next w equal to w.
.....
def sgd(w, dw, config=None):
   Performs vanilla stochastic gradient descent.
   config format:
   - learning_rate: Scalar learning rate.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   w -= config['learning_rate'] * dw
   return w, config
def sgd_momentum(w, dw, config=None):
   Performs stochastic gradient descent with momentum.
   config format:
   learning_rate: Scalar learning rate.
   - momentum: Scalar between 0 and 1 giving the momentum value.
     Setting momentum = 0 reduces to sgd.
   - velocity: A numpy array of the same shape as w and dw used to
store a moving
     average of the gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('momentum', 0.9) # set momentum to 0.9 if it
wasn't there
   v = config.get('velocity', np.zeros_like(w)) # gets velocity,
else sets it to zero.
   #
   # YOUR CODE HERE:
       Implement the momentum update formula. Return the updated
weights
   # as next_w, and the updated velocity as v.
   #
   v = config['momentum']*v - config['learning_rate']*dw
```

```
next w = w + v
   #
   # END YOUR CODE HERE
   #
   config['velocity'] = v
   return next w, config
def sgd_nesterov_momentum(w, dw, config=None):
   Performs stochastic gradient descent with Nesterov momentum.
   config format:
   learning_rate: Scalar learning rate.
   - momentum: Scalar between 0 and 1 giving the momentum value.
     Setting momentum = 0 reduces to sgd.
   - velocity: A numpy array of the same shape as w and dw used to
store a moving
     average of the gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('momentum', 0.9) # set momentum to 0.9 if it
wasn't there
   v = config.get('velocity', np.zeros_like(w)) # gets velocity,
else sets it to zero.
#
   # YOUR CODE HERE:
      Implement the momentum update formula. Return the updated
weights
      as next_w, and the updated velocity as v.
   #
   v old = v
   v = config['momentum']*v - config['learning rate']*dw
   next_w = w + v + config['momentum']*(v-v_old)
   # END YOUR CODE HERE
```

```
config['velocity'] = v
   return next_w, config
def rmsprop(w, dw, config=None):
   Uses the RMSProp update rule, which uses a moving average of
squared gradient
   values to set adaptive per-parameter learning rates.
   config format:
   learning_rate: Scalar learning rate.
   - decay_rate: Scalar between 0 and 1 giving the decay rate for the
squared
     gradient cache.
   - epsilon: Small scalar used for smoothing to avoid dividing by
zero.

    beta: Moving average of second moments of gradients.

   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('decay_rate', 0.99)
   config.setdefault('epsilon', 1e-8)
   config.setdefault('a', np.zeros_like(w))
   next_w = None
#
   # YOUR CODE HERE:
       Implement RMSProp. Store the next value of w as next w. You
need
       to also store in config['a'] the moving average of the second
       moment gradients, so they can be used for future gradients.
Concretely,
       config['a'] corresponds to "a" in the lecture notes.
   #
   config['a'] = config['decay_rate'] * config['a'] + (1-
config['decay rate']) * dw * dw
   next_w = w - dw * (config['learning_rate'] / (np.sqrt(config['a'])
+ config['epsilon']))
   #
   # END YOUR CODE HERE
```

```
return next_w, config
def adam(w, dw, config=None):
   Uses the Adam update rule, which incorporates moving averages of
both the
   gradient and its square and a bias correction term.
   config format:
   learning_rate: Scalar learning rate.
   - beta1: Decay rate for moving average of first moment of
gradient.
   - beta2: Decay rate for moving average of second moment of
gradient.
   - epsilon: Small scalar used for smoothing to avoid dividing by
zero.
   - m: Moving average of gradient.
   - v: Moving average of squared gradient.
   t: Iteration number.
   .....
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-3)
   config.setdefault('beta1', 0.9)
   config.setdefault('beta2', 0.999)
   config.setdefault('epsilon', 1e-8)
   config.setdefault('v', np.zeros_like(w))
   config.setdefault('a', np.zeros_like(w))
   config.setdefault('t', 0)
   next w = None
   #
   # YOUR CODE HERE:
       Implement Adam. Store the next value of w as next_w. You
need
       to also store in config['a'] the moving average of the second
   #
       moment gradients, and in config['v'] the moving average of the
   #
       first moments. Finally, store in config['t'] the increasing
time.
   config['t'] += 1
```

config['v'] = config['beta1'] \* config['v'] + (1 -

config['a'] = config['beta2'] \* config['a'] + (1 -

config['beta1']) \* dw

config['beta2']) \* dw \* dw

```
import numpy as np
import pdb
from .layers import *
from .layer utils import *
.....
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use
ECE 239AS class at UCLA. This includes the descriptions of what code
implement as well as some slight potential changes in variable names
consistent with class nomenclature. We thank Justin Johnson & Serena
Yeung for
permission to use this code. To see the original version, please
visit
cs231n.stanford.edu.
class TwoLayerNet(object):
    A two-layer fully-connected neural network with ReLU nonlinearity
and
    softmax loss that uses a modular layer design. We assume an input
    of D, a hidden dimension of H, and perform classification over C
classes.
    The architecure should be affine - relu - affine - softmax.
    Note that this class does not implement gradient descent; instead,
it
    will interact with a separate Solver object that is responsible
for running
    optimization.
    The learnable parameters of the model are stored in the dictionary
    self.params that maps parameter names to numpy arrays.
    def __init__(self, input_dim=3*32*32, hidden_dims=100,
num classes=10,
                 dropout=0, weight_scale=1e-3, reg=0.0):
        Initialize a new network.
        Inputs:
        - input_dim: An integer giving the size of the input
```

```
- hidden dims: An integer giving the size of the hidden layer
       - num classes: An integer giving the number of classes to
classify

    dropout: Scalar between 0 and 1 giving dropout strength.

       - weight scale: Scalar giving the standard deviation for
random
        initialization of the weights.
       - reg: Scalar giving L2 regularization strength.
       self.params = {}
       self.reg = reg
______#
       # YOUR CODE HERE:
          Initialize W1, W2, b1, and b2. Store these as
self.params['W1'],
          self.params['W2'], self.params['b1'] and
self.params['b2']. The
          biases are initialized to zero and the weights are
initialized
          so that each parameter has mean 0 and standard deviation
weight_scale.
          The dimensions of W1 should be (input_dim, hidden_dim) and
the
       #
          dimensions of W2 should be (hidden_dims, num_classes)
       #
______ #
       self.params['W1'] = np.random.normal(scale=weight scale,
size=(input_dim, hidden_dims))
       self.params['b1'] = np.zeros(hidden_dims)
       self.params['W2'] = np.random.normal(scale=weight scale,
size=(hidden dims, num classes))
       self.params['b2'] = np.zeros(num_classes)
       #
 ______#
       # END YOUR CODE HERE
       #
______#
   def loss(self, X, y=None):
       Compute loss and gradient for a minibatch of data.
       Inputs:
       - X: Array of input data of shape (N, d_1, ..., d_k)
       - y: Array of labels, of shape (N,). y[i] gives the label for
X[i].
```

```
If y is None, then run a test-time forward pass of the model
      - scores: Array of shape (N, C) giving classification scores,
where
        scores[i, c] is the classification score for X[i] and class
C.
      If y is not None, then run a training-time forward and
backward pass and
      return a tuple of:
      - loss: Scalar value giving the loss

    grads: Dictionary with the same keys as self.params, mapping

parameter
        names to gradients of the loss with respect to those
parameters.
      scores = None
           # YOUR CODE HERE:
         Implement the forward pass of the two-layer neural
network. Store
         the class scores as the variable 'scores'. Be sure to use
the layers
      #
         you prior implemented.
      #
______ #
      hidden, cache1 = affine_relu_forward(X, self.params["W1"],
self.params["b1"])
      scores, cache2 = affine forward(hidden, self.params["W2"],
self.params["b2"])
      #
______ #
      # END YOUR CODE HERE
      #
______#
      # If y is None then we are in test mode so just return scores
      if y is None:
         return scores
      loss, grads = 0, \{\}
        # YOUR CODE HERE:
```

Returns:

```
#
           Implement the backward pass of the two-layer neural net.
Store
           the loss as the variable 'loss' and store the gradients in
       #
the
           'grads' dictionary. For the grads dictionary, grads['W1']
       #
holds
           the gradient for W1, grads['b1'] holds the gradient for
b1, etc.
           i.e., grads[k] holds the gradient for self.params[k].
           Add L2 regularization, where there is an added cost
0.5*self.reg*W^2
           for each W. Be sure to include the 0.5 multiplying factor
       #
to
           match our implementation.
       #
       #
       #
           And be sure to use the layers you prior implemented.
       #
       l, g = softmax_loss(scores, y)
       reg_loss = 0.5 * self.reg * (np.sum(self.params["W1"]**2) +
np.sum(self.params["W2"]**2))
       dldx2, grads["W2"], grads["b2"] = affine_backward(g, cache2)
       dldx1, grads["W1"], grads["b1"] = affine_relu_backward(dldx2,
cache1)
       loss = l + reg_loss
       grads["W1"] += self.reg * self.params["W1"]
       grads["W2"] += self.reg * self.params["W2"]
______ #
       # END YOUR CODE HERE
______#
       return loss, grads
class FullyConnectedNet(object):
   A fully-connected neural network with an arbitrary number of
hidden layers,
   ReLU nonlinearities, and a softmax loss function. This will also
implement
   dropout and batch normalization as options. For a network with L
```

the architecture will be

```
{affine - [batch norm] - relu - [dropout]} x (L - 1) - affine -
softmax
    where batch normalization and dropout are optional, and the \{\ldots\}
block is
    repeated L - 1 times.
    Similar to the TwoLayerNet above, learnable parameters are stored
    self.params dictionary and will be learned using the Solver class.
    def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
               dropout=1, use_batchnorm=False, reg=0.0,
               weight_scale=1e-2, dtype=np.float32, seed=None):
        .....
        Initialize a new FullyConnectedNet.
        Inputs:
        - hidden_dims: A list of integers giving the size of each
hidden layer.
        - input_dim: An integer giving the size of the input.
        - num_classes: An integer giving the number of classes to
classify.
        - dropout: Scalar between 0 and 1 giving dropout strength. If
dropout=1 then
          the network should not use dropout at all.
        - use batchnorm: Whether or not the network should use batch
normalization.

    reg: Scalar giving L2 regularization strength.

        - weight scale: Scalar giving the standard deviation for
random
          initialization of the weights.
        - dtype: A numpy datatype object; all computations will be
performed using
          this datatype. float32 is faster but less accurate, so you
should use
          float64 for numeric gradient checking.
        - seed: If not None, then pass this random seed to the dropout
layers. This
          will make the dropout layers deteriminstic so we can
gradient check the
         model.
        self.use_batchnorm = use_batchnorm
        self.use_dropout = dropout < 1</pre>
        self.reg = reg
        self.num_layers = 1 + len(hidden_dims)
        self.dtype = dtype
```

```
self.params = {}
                    ______#
        # YOUR CODE HERE:
            Initialize all parameters of the network in the
self params dictionary.
           The weights and biases of layer 1 are W1 and b1; and in
general the
           weights and biases of layer i are Wi and bi. The
           biases are initialized to zero and the weights are
initialized
           so that each parameter has mean 0 and standard deviation
weight_scale.
        #
           BATCHNORM: Initialize the gammas of each layer to 1 and
the beta
           parameters to zero. The gamma and beta parameters for
layer 1 should
           be self.params['gamma1'] and self.params['beta1']. For
layer 2, they
            should be gamma2 and beta2, etc. Only use batchnorm if
self.use_batchnorm
            is true and DO NOT do batch normalize the output scores.
        n = len(hidden_dims)
        self.params["W1"] = np.random.normal(scale=weight_scale,
size=(input dim, hidden dims[0]))
        self.params["b1"] = np.zeros(hidden_dims[0])
        for i in range(1, n):
            self.params["W" + str(i+1)] =
np.random.normal(scale=weight_scale, size=(hidden_dims[i-1],
hidden dims[i]))
            self.params["b" + str(i+1)] = np.zeros(hidden dims[i])
        self.params["W" + str(n+1)] =
np.random.normal(scale=weight scale, size=(hidden dims[n-1],
num classes))
        self.params["b" + str(n+1)] = np.zeros(num classes)
        if self.use batchnorm:
            for i in range(self.num_layers - 1):
                self.params["gamma" + str(i+1)] =
np.ones(hidden_dims[i])
                self.params["beta" + str(i+1)] =
np.zeros(hidden_dims[i])
```

```
# END YOUR CODE HERE
       #
______#
       # When using dropout we need to pass a dropout param
dictionary to each
       # dropout layer so that the layer knows the dropout
probability and the mode
       # (train / test). You can pass the same dropout param to each
dropout layer.
       self.dropout_param = {}
       if self.use dropout:
           self.dropout_param = {'mode': 'train', 'p': dropout}
       if seed is not None:
           self.dropout param['seed'] = seed
       # With batch normalization we need to keep track of running
means and
       # variances, so we need to pass a special bn_param object to
each batch
       # normalization layer. You should pass self.bn params[0] to
the forward pass
       # of the first batch normalization layer, self.bn_params[1] to
the forward
       # pass of the second batch normalization layer, etc.
       self.bn_params = []
       if self.use_batchnorm:
           self.bn_params = [{'mode': 'train'} for i in
np.arange(self.num_layers - 1)]
       # Cast all parameters to the correct datatype
       for k, v in self.params.items():
           self.params[k] = v.astype(dtype)
   def loss(self, X, y=None):
       Compute loss and gradient for the fully-connected net.
       Input / output: Same as TwoLayerNet above.
       X = X.astype(self.dtype)
       mode = 'test' if y is None else 'train'
       # Set train/test mode for batchnorm params and dropout param
since they
       # behave differently during training and testing.
       if self.dropout_param is not None:
```

```
self.dropout param['mode'] = mode
       if self.use batchnorm:
           for bn_param in self.bn_params:
              bn param[mode] = mode
       scores = None
______#
       # YOUR CODE HERE:
           Implement the forward pass of the FC net and store the
output
           scores as the variable "scores".
       #
       #
           BATCHNORM: If self.use_batchnorm is true, insert a
bathnorm layer
           between the affine_forward and relu_forward layers.
                                                          You
may
           also write an affine_batchnorm_relu() function in
layer_utils.py.
       #
           DROPOUT: If dropout is non-zero, insert a dropout layer
after
       #
           every ReLU layer.
       #
______ #
       caches = []
       dp_caches = []
       fwd in = X
       for i in range(self.num_layers - 1):
           if self.use batchnorm:
               fwd_in, cache = affine_batchnorm_relu_forward(fwd_in,
                                                 self.params["W"
+ str(i+1)],
                                                 self.params["b"
+ str(i+1)],
self.params["gamma" + str(i+1)],
self.params["beta" + str(i+1)],
self.bn_params[i])
               caches append (cache)
           else:
               fwd_in, cache = affine_relu_forward(fwd_in,
self.params["W" + str(i+1)], self.params["b" + str(i+1)])
              caches.append(cache)
           if self.use_dropout:
```

```
fwd in, dp cache = dropout forward(fwd in,
self.dropout param)
              dp_caches.append(dp_cache)
       scores, cache = affine forward(fwd in, self.params["W" +
str(self.num_layers)], self.params["b" + str(self.num_layers)])
       caches.append(cache)
       #
           ______ #
       # END YOUR CODE HERE
       #
        ______#
       # If test mode return early
       if mode == 'test':
          return scores
       loss, grads = 0.0, \{\}
       # YOUR CODE HERE:
          Implement the backwards pass of the FC net and store the
gradients
          in the grads dict, so that grads[k] is the gradient of
self.params[k]
          Be sure your L2 regularization includes a 0.5 factor.
       #
       #
          BATCHNORM: Incorporate the backward pass of the batchnorm.
       #
       #
          DROPOUT: Incorporate the backward pass of dropout.
       #
______#
       l, g = softmax_loss(scores, y)
       reg loss = 0.5 * self.reg * (sum([np.sum(self.params["W" +
str(i)]**2) for i in range(1, self.num layers + 1)]))
       upstream deriv = q
       upstream_deriv, grads["W" + str(self.num_layers)], grads["b" +
str(self.num layers)] = affine backward(upstream deriv,
caches[self.num_layers - 1])
       for i in range(self.num_layers - 2, -1, -1):
           if self.use dropout:
              upstream_deriv = dropout_backward(upstream_deriv,
dp_caches[i])
           if self.use batchnorm:
              upstream_deriv, grads["W" + str(i+1)], grads["b" +
```