

1.

- a. $(\alpha, \text{int}, \delta, \alpha, \beta)$ and $(\text{int}, \delta, \text{char}, \beta, \delta)$.
 - Yes, $\text{int} = \alpha$; $\delta = \alpha$; $\beta = \alpha$; $\text{char} = \alpha$
 - common type: $(\alpha, \alpha, \alpha, \alpha, \alpha)$
- b. $(\beta, (\gamma, \eta), (\beta, \alpha))$ and $((\alpha, \gamma), \zeta, (\beta, \alpha))$.
 - Yes, $\beta = (\alpha, \gamma)$; $\zeta = (\gamma, \eta)$
 - Common type: $((\alpha, \gamma), (\gamma, \eta), ((\alpha, \gamma), \alpha))$

2.

- a. $[A \mapsto E, D \mapsto E \rightarrow E]$ is most general as it's mapping two distinct types to the same type, E without supporting operators
- b. None of the unifiers are most general, the first and third unifiers both map to a function with two types and one variable making them equally general

3.

- a.
 - i. $\square \quad \{X = d(Y, Z), X = d(Z, Y)\}$
 - ii. $[Y \mapsto Z] \quad \{\}$
- b.
 - i. $\square \quad \{d(a, b) = d(A, B), f(A) = f(B)\}$
 - ii. $[A \mapsto B] \quad \{d(a, b) = d(B, B)\}$
 - iii. $[A \mapsto B, a \mapsto B] \quad \{d(B, b) = d(B, B)\}$
 - iv. $[A \mapsto B, a \mapsto B, b \mapsto B] \quad \{\}$
- c.
 - i. $\square \quad \{p(X, Y) = p(X, p(X, Z)), Y = p(A, y), X = p(x, Z)\}$
 - ii. $\square \quad \{p(p(x, Z), Y) = p(p(x, Z), p(X, Z)), Y = p(A, Y), X = X\}$
 - iii. $[X \mapsto A] \quad \{p(A, Y) = p(A, p(A, Z)), Y = p(A, Y), A = p(x, Z)\}$
 - iv. $,,,,$
- d.
 - i. $\square \quad \{t(A, B, d(a, c)) = t(p(a, E), B, C), p(d(E, c), d(a, F)) = p(d(b, F), C)\}$
 - ii. $[A = p(a, E)] \quad \{t(p(a, E), B, d(a, c)) = t(p(a, E), B, C), p(d(E, c), d(a, F)) = p(d(b, F), C)\}$
 - iii. $[A = p(a, E), C = d(a, c)] \quad \{p(d(E, c), d(a, F)) = p(d(b, F), d(a, c))\}$
 - iv. $[A = p(a, E), C = d(a, c), F = E] \quad \{p(d(E, c), d(a, E)) = p(d(b, E), d(a, c))\}$
 - v. $[A = p(a, E), C = d(a, c), F = E, c = E, a = E] \quad \{\}$