## Javelin Diagrams

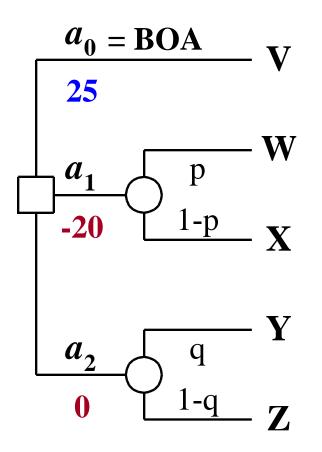
#### James C. Felli

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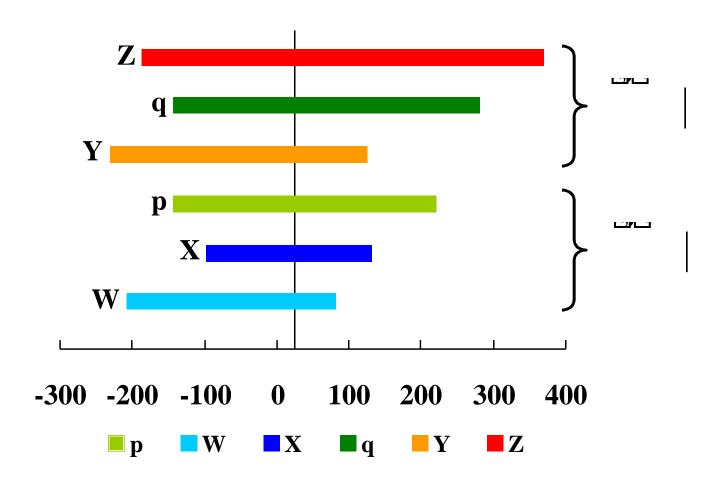
Consider the following problem



	Min	Max	Base
p	0	1	0.667
$\mathbf{q}$	0	1	0.333
$\mathbf{V}$	-350	400	25
$\mathbf{W}$	-400	0	-133.3
X	0	620	206.67
Y	-400	600	266.67
Z	-400	400	-133.3

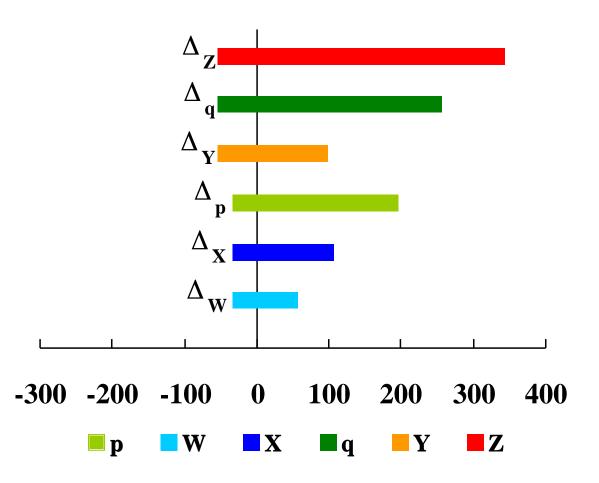
## Tornado diagram

Two tornado diagrams on a single graph

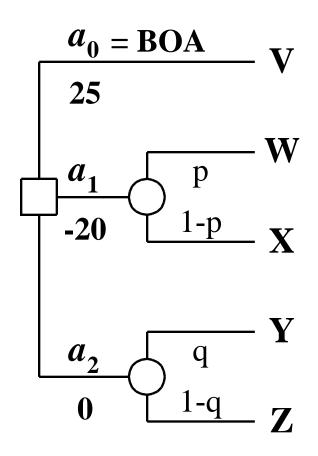


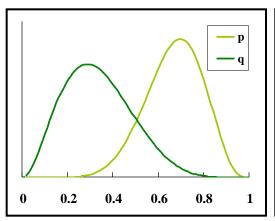
## Modify the tornado

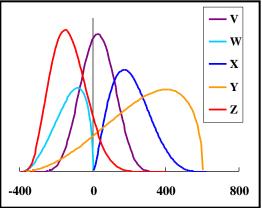
Redefine the bars:



Now include parameter density information





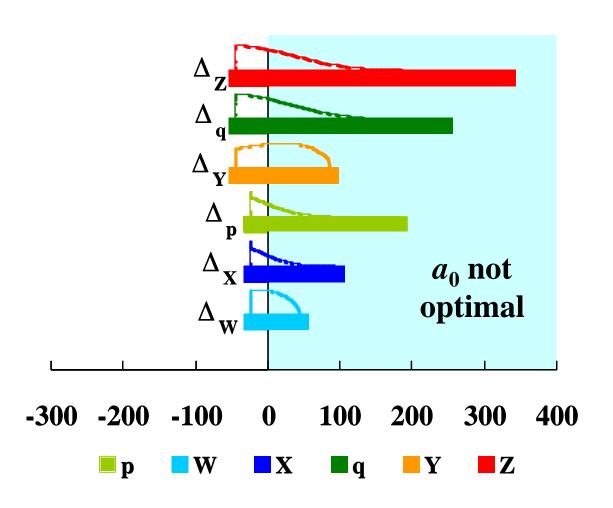


Parameter	Beta a	Beta b	lower	upper	mean
р	9	4.5	0	1	0.6667
$\mathbf{q}$	3	6	0	1	0.3333
$\mathbf{V}$	8	8	-350	400	25
$\mathbf{W}$	3.15	1.575	-400	0	-133.3
X	2.475	4.95	0	620	206.67
Y	3	1.5	-400	600	266.67
${f Z}$	4.875	9.75	-400	400	-133.3

## Building a javelin



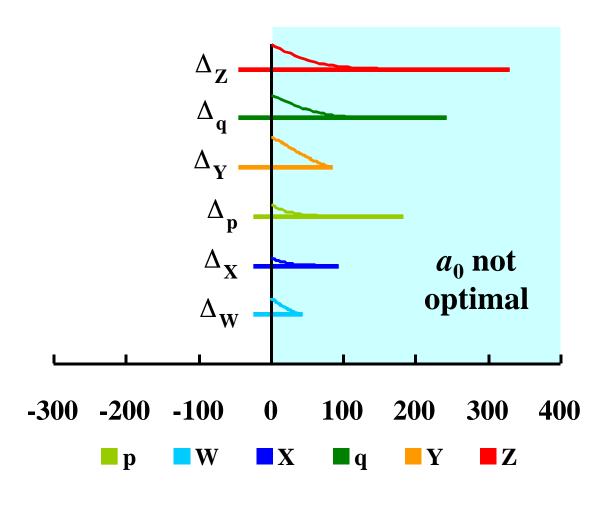
over the range of improvement



## Building a javelin

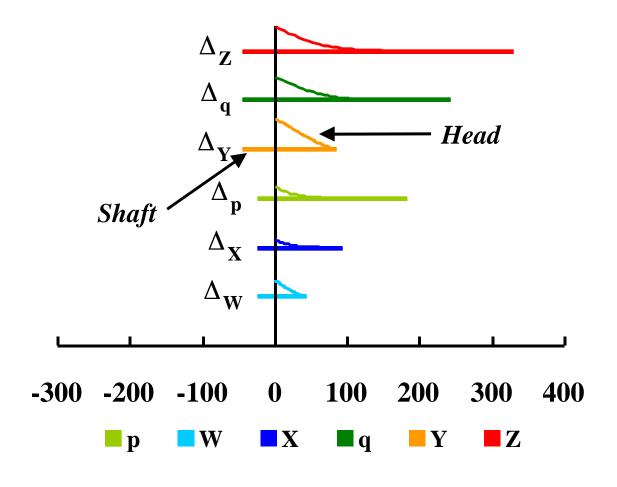


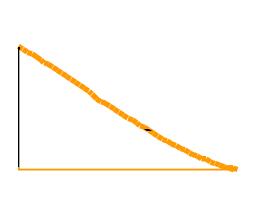
over the range of improvement



## Javelin diagram

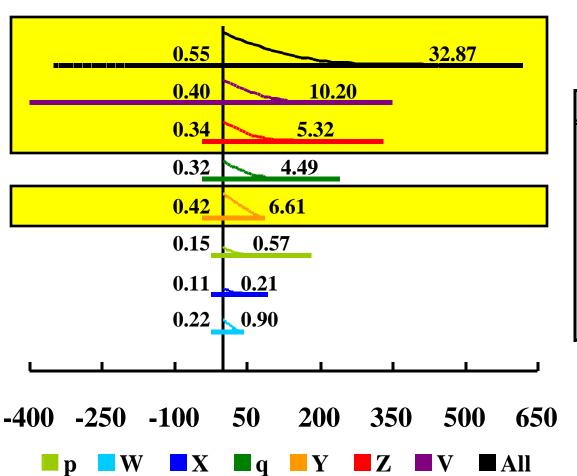
Now we have a javelin diagram!





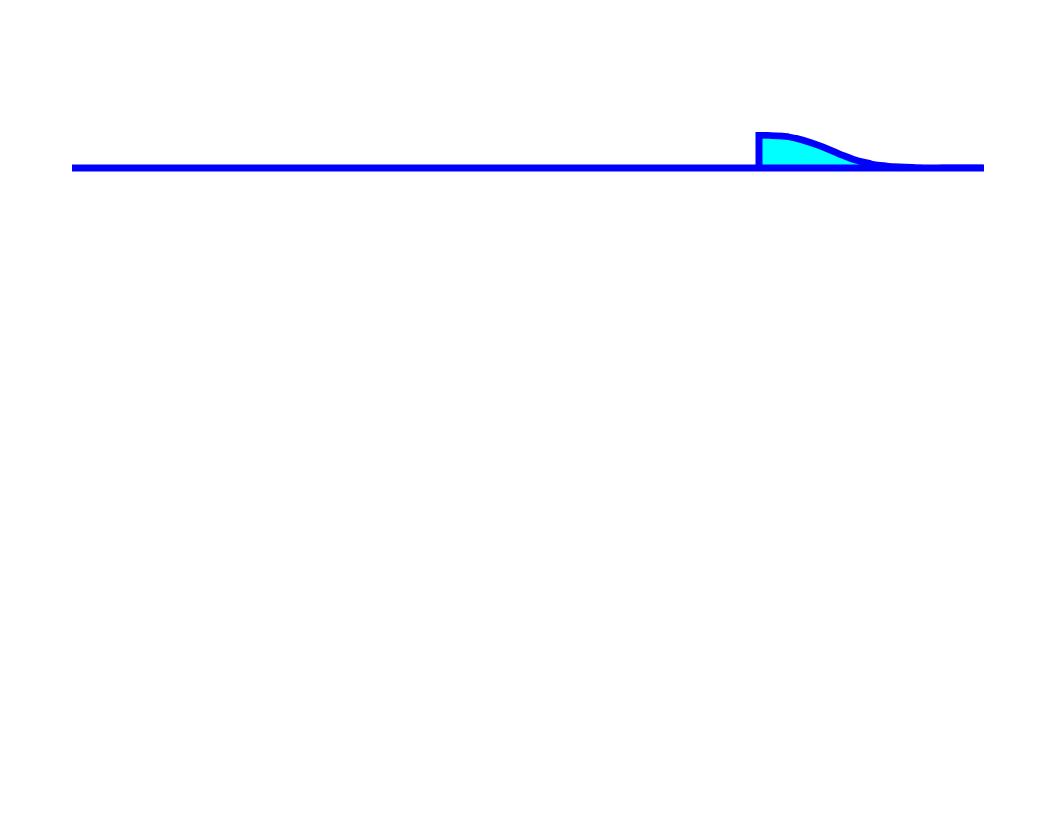
## Javelin diagram

Javelins can include any parameter set

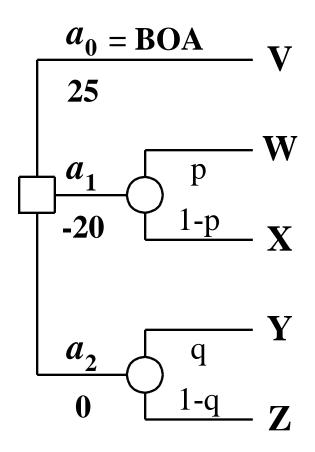


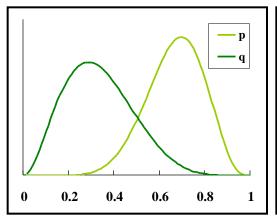
If MSI=5

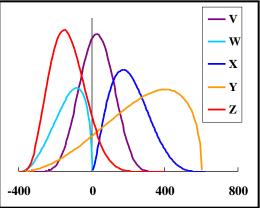
Parameter	Beta a	Beta b	
p	9	4.5	
${f q}$	3	6	
${f V}$	8	8	
$\mathbf{W}$	3.15	1.575	
X	2.475	4.95	
Y	3	1.5	
Z	4.875	9.75	



Case 1 parameter densities:

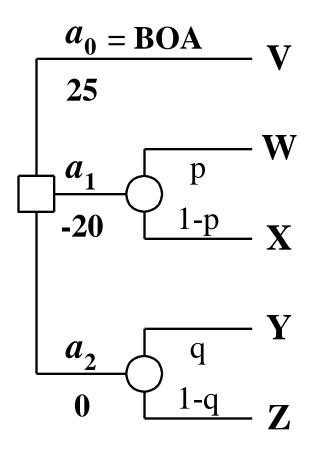


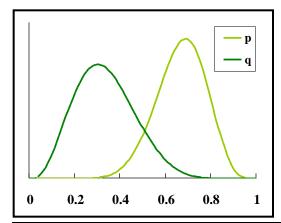


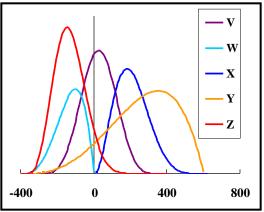


Parameter	Beta a	Beta b	lower	upper	mean
р	9	4.5	0	1	0.6667
$\mathbf{q}$	3	6	0	1	0.3333
$\mathbf{V}$	8	8	-350	400	25
$\mathbf{W}$	3.15	1.575	-400	0	-133.3
X	2.475	4.95	0	620	206.67
Y	3	1.5	-400	600	266.67
Z	4.875	9.75	-400	400	-133.3

#### Case 2 parameter densities



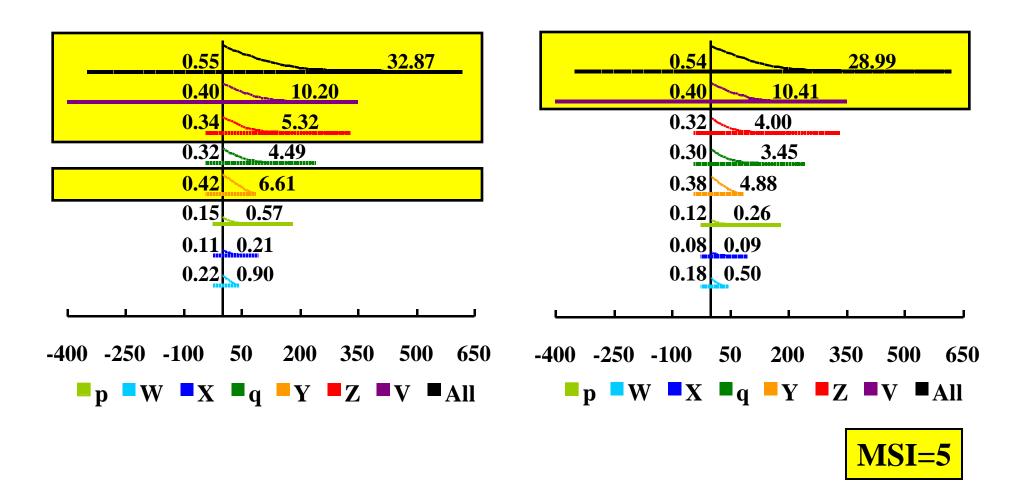




Parameter	Beta a	Beta b	lower	upper	mean
р	12	6	0	1	0.6667
$\mathbf{q}$	4	8	0	1	0.3333
$\mathbf{V}$	8	8	-350	400	25
$\mathbf{W}$	4.2	2.1	-400	0	-133.3
X	3.3	6.6	0	620	206.67
Y	4	2	-400	600	266.67
${f Z}$	6.5	13	-400	400	-133.3

#### Javelin diagrams

Comparison of the two javelin diagrams



## Javelin advantages

- ➤ Includes all alternatives in single diagram
- > Reference point of zero highlights benefits
- > Shows range of potentially foregone benefits
- > Shows **probability** of the BOA losing optimality
- > Provides EVPI as additional sensitivity measure

# That's all, folks!