

## HW 1

1.7 Convert the hexadecimal number 64CD to binary and octal:

$$64CD \xrightarrow{\text{binary}} \boxed{0110 \ 0100 \ 1100 \ 1101}$$

$$\xrightarrow{\text{octal}} \begin{array}{cccccc} & 4^1 & 2^2 & 2^1 & 2^0 & 4^1 \\ 0 & 110 & 010 & 011 & 001 & 101 \\ \hline 0 & 6 & 2 & 3 & 1 & 5 \end{array} = \boxed{(62315)_8}$$

1.13 a.) Convert decimal 27.315 to binary:

$$27.315 \xrightarrow{\text{binary}} \boxed{11011.0101}$$

obtain the 1's & 2's complements of the following:

1.14 a.) 10010000

$$1's \text{ complement: } +11111111 \Rightarrow \boxed{01101111}$$

$$2's \text{ complement: } \begin{array}{c} 01101111 \\ \downarrow \\ +00000001 \end{array} \Rightarrow \boxed{01110000}$$

e.) 10100101

$$1's \text{ complement: } +11111111 \Rightarrow \boxed{01011010}$$

$$2's \text{ complement: } 01011010 + 00000001 = \boxed{01011011}$$

1.18 Perform subtraction of the following using the 2's complement of the subtrahend, where the result should be negative, find its 2's complement and affix a minus sign.

$$a) \overset{35}{10011} - \overset{34}{10010} \Rightarrow \overset{35}{10011} + \overset{00001}{2's \text{ complement of } 10010} = \overset{35}{10011} + 00001 = \boxed{00001}$$

$$\overset{35}{10011} - \overset{34}{10010}$$

$$\overset{35}{10011} - \overset{34}{10010}$$

$$2's \text{ complement with affix minus: } +0001 = \boxed{00010}$$

$$\text{b.) } \begin{array}{ccc} 100010 & - & 100110 \\ \underline{34} & & \underline{38} \end{array} = \boxed{100000} \\ + 0001 \Rightarrow \boxed{100101}$$

1.25 Represent the decimal number 6.428 in:

a.) BCD:  $\boxed{0110 \ 0010 \ 0100 \ 1000}$

b.) excess-3:  $\boxed{1000 \ 0101 \ 0111 \ 1011}$

c.) 2421 code:  $\boxed{1100 \ 0010 \ 0100 \ 1110}$

d.) 6311 code:  $\boxed{1000 \ 0011 \ 0101 \ 1011}$

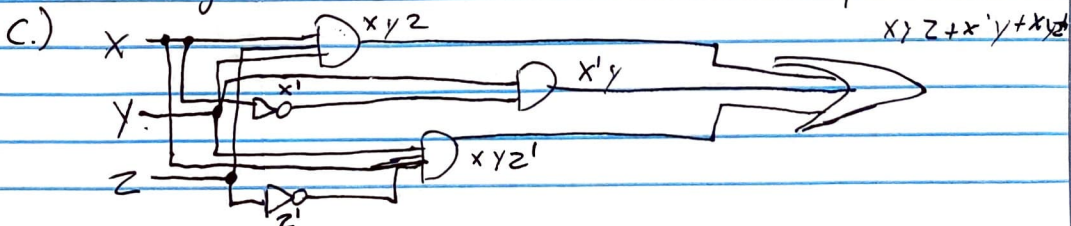
2.2 simplify the following Boolean expressions to a minimum number of literals.

~~a.)  $x + x' = 1$~~

c.)  $xyz + x'y + xyz' = xy(z + z') + x'y$   
 $\Rightarrow xy + x'y = y(x + x') = \boxed{y}$

d.)  $(x+y)'(x'+y')' \Rightarrow (x'y')((x')' + (y')')$   
 $= (x'y')(xy) = \cancel{x'x} y'y = \boxed{0}$

2.5 Draw logic diagrams of the circuits that implement the original & simplified expressions in problem 2.2.





(2.9) Find the complement of the following expressions:

a.)  $xy' + x'y$

complement:  ~~$(xy' + x'y)' = (xy')'(x'y)' = (x'+y')(x+y)$~~   
 ~~$= x'x + x'y' + yx + y'y'$~~   
 ~~$= x'x + x'y' + yx + y'y'$~~

$\Rightarrow (xy' + x'y)' = (xy')'(x'y)' = (x'+y')(x+y)$

~~$(x'x + x'y' + yx + y'y')$~~   
 ~~$= x'x + x'y' + yx + y'y'$~~   
 ~~$(\text{complement: } x)$~~   
 $= \boxed{x'y' + xy}$

b.)  $(a+c)(a+b')(a'+b+c')$

complement:  $((a+c)(a+b')(a'+b+c'))' = \boxed{(a'c') + (a'b) + (ab'c')}$

c.)  $z + z'(v'w + xy)$

complement:  $(z + z'(v'w + xy))' = \text{ ~~$z' + z(v'w + xy)$~~ }$

$= (z' + (v'w + xy)') = (v'w)(x'y') = \boxed{vx' + vy' + w'x' + w'y'}$

~~$= z' + (v'w + xy)$~~

(2.17) Obtain the truth table of the following functions, & express each function in sum-of-minterms & product-of-maxs.

c.)  $(c' + d)(b + c')$

Truth table:

a	b	c	d	$c' + d$	$b + c'$	F
0	0	0	0	1	0	0
0	0	0	1	1	0	0
0	0	1	0	0	1	0
0	0	1	1	1	1	1
0	1	0	0	1	1	1
0	1	0	1	1	1	1
0	1	1	0	0	1	0
0	1	1	1	1	1	1
1	0	0	0	1	0	0
1	0	0	1	1	0	0
1	0	1	0	0	1	0
1	0	1	1	1	1	1
1	1	0	0	1	1	1
1	1	0	1	1	1	1
1	1	1	0	0	1	0
1	1	1	1	1	1	1

Sum of min term:  $F = a'b'c'd + a'b'cd + a'bc'd + a'bcd + ab'cd + abc'd + abcd$

Sum of max-terms:  $F = (a+b+c'+d')(a+b+c'+d'')$

$$\cdot (a+b'+c+d') (a'+b+c'+d) (a'+b+c'+d') (a'+b'+d'+c)$$

a	b	c	d	$bd' = (acd' + ab'c' + a'c')$	$F$
0	0	0	0	0	1
0	0	0	1	0	1
0	0	1	0	0	0
0	0	1	1	0	0
0	1	0	0	0	1
0	1	0	1	0	1
0	1	1	0	0	1
0	1	1	1	0	0
1	0	0	0	0	0
1	0	0	1	0	0
1	0	1	0	1	1
1	0	1	1	0	1
1	1	0	0	0	1
1	1	0	1	0	0
1	1	1	0	1	1
1	1	1	1	0	0

Sum of max terms:  $F = (a+b+c'+d')(a+b+c'+d') \cdot (a+b'+c'+d')(a'+b+c+d)(a'+b+c+d)(a'+b'+c+d')(a'+b'+c+d')$



2.22  
✓

2.22 Convert each of the following expressions into sum of products & product of sums.  
(SOP) (POS)

a.)  $(u+xw)(x+u'v)$

SOP:  $\Rightarrow ux + uu'v + xw + u'vwx = ux + wx + u'wx$   
 $= ux + wx(1 + u'v) = \boxed{ux + wx}$

POS:  $ux + wx = \boxed{(u+w)x}$

b.)  $x' + x(x+y')(y+z')$

SOP:  $\Rightarrow (x' + x)(x' + (x+y'))(x' + (y+z'))$   
 $= (x' + x + y')(x' + y + z') = (x' + x) + y'(x' + y + z')$   
 $= (1 + y')(x' + y + z') = (x' + y + z')$   
 $= \boxed{x' + y + z'}$

~~SOP~~ POS:  $\boxed{(x' + y + z')}$