

Final Project Due Date Extension: Devon Webb

The date I would like to extend my final project to is December 1.

The project I am accomplishing is to implement a version of the algorithm called Square Root SAM described in the paper found at this link: <https://www.cc.gatech.edu/~dellaert/pub/Dellaert06ijrr.pdf>. The Square root SAM algorithm is a least squares approach to solving the least squares problem using a cholesky factorization of a sparse jacobian matrix. I currently have a 1D of this problem working in C++ and it involves solving the following equation. (taken from the above article).

$$x^* = \operatorname{argmin}_x \|Ax - b\|$$

Where  $b$  contains odometry and landmark measurement data recorded by a robot,  $x$  contains all poses that a robot reaches along its trajectory as well as the location of each landmark in reference to the world plane, and  $A$  contains jacobians relating the poses and landmarks to the various odometry. Solving this problem involves first redefining the problem as

$$x^* = \operatorname{argmin}_x \|A'A x - A'b\|$$

and then doing a cholesky decomposition of the, now square, matrix  $A'A$  which we define as  $I$ . This  $I$  matrix is factored into a  $LL'$  where  $L$  is a lower Left hand matrix. Which is then used to solve for the  $\operatorname{argmin}$  value of  $x$ .

For 1D with 25 poses and 5 landmarks you end up with an  $A$  matrix that is  $30 \times 85$  and do a cholesky decomposition on a  $30 \times 30$  matrix. But, because a 1D example only contains linear jacobians, the  $A$  matrix is filled with only -1, 1, and zero which is not very interesting. So to finish the project I am continuing the square root SAM process on a 2D example with non linear jacobians which should lead to a more interesting least squares problem than the linear case. For this 2D example I have generated a  $b$  vector with “measurement data” that corresponds to a predefined ground truth for robot poses and landmark positions. I have also calculated the Jacobians for 2D. The last thing I have to do for my project is write a function that inserts the Jacobian into the  $A$  matrix properly for square root SAM. Then the algorithm for solving least squares should be the same as 1D.