Numerical Solutions of Differential Equations : HW1

Thomas Garrett & Weicker David $8^{\rm th}$ February 2016

Introduction

This is the introduction bitches!

1 Conservation laws

blabla

2 Heat Equation

2.1 Flux vector

2.2 Q(t)

We are now interested in computing:

$$Q(t) = \int_0 \int_0 q(x, y, t) dx dy$$

Using the fundamental theorem of calculus, we have :

$$Q(t) = Q(0) + \int_0 Q'(\tau)d\tau$$

The initial condition gives :

$$Q(0) = \int_0 \int_0 q(x, y, 0) dx dy = \int_0 \int_0 0 dx dy = 0$$

We also know that (using the definition of Q):

$$Q'(t) = \int_0 \int_0 q_t(x, y, t) dx dy$$

We are now going to use the PDE to substitute q_t . This yields:

$$Q'(t) = \int_0 \int_0 q_t(x, y, t) dx dy = \int_0 \int_0 \nabla \cdot (\nabla q(x, y, t)) dx dy + \int_0 \int_0 S(x, y, t) dx dy$$

3 Discretization and implementation

blabla

4 Numerical results

blabla bitches

5 Refinements

blabla