

# Stellar Mass-to-Light Ratios and the Tully-Fisher Relation

Bell and De Jong 2001

# Why M/L?

- Relates photometry to dynamics
- Direct impact on
  - Rotation curve decomposition
  - Passband-dependent slope of Tully-Fisher relation

# Why M/L?

- Rotation curve decomposition
- Can determine structure of dark matter halo if we understand contributions of
  - gas (well understood and small)
  - stars (not well understood and big)
- Tully-Fisher relation
- Relates integrated luminosity to global dynamics of galaxy + dark matter halo
- $L \sim V^3$  in optical
- $L \sim V^4$  in near-IR
- Possible to reproduce T-F in one passband without reproducing other passbands
  - Baryonic mass T-F

# Galaxy Evolution Models

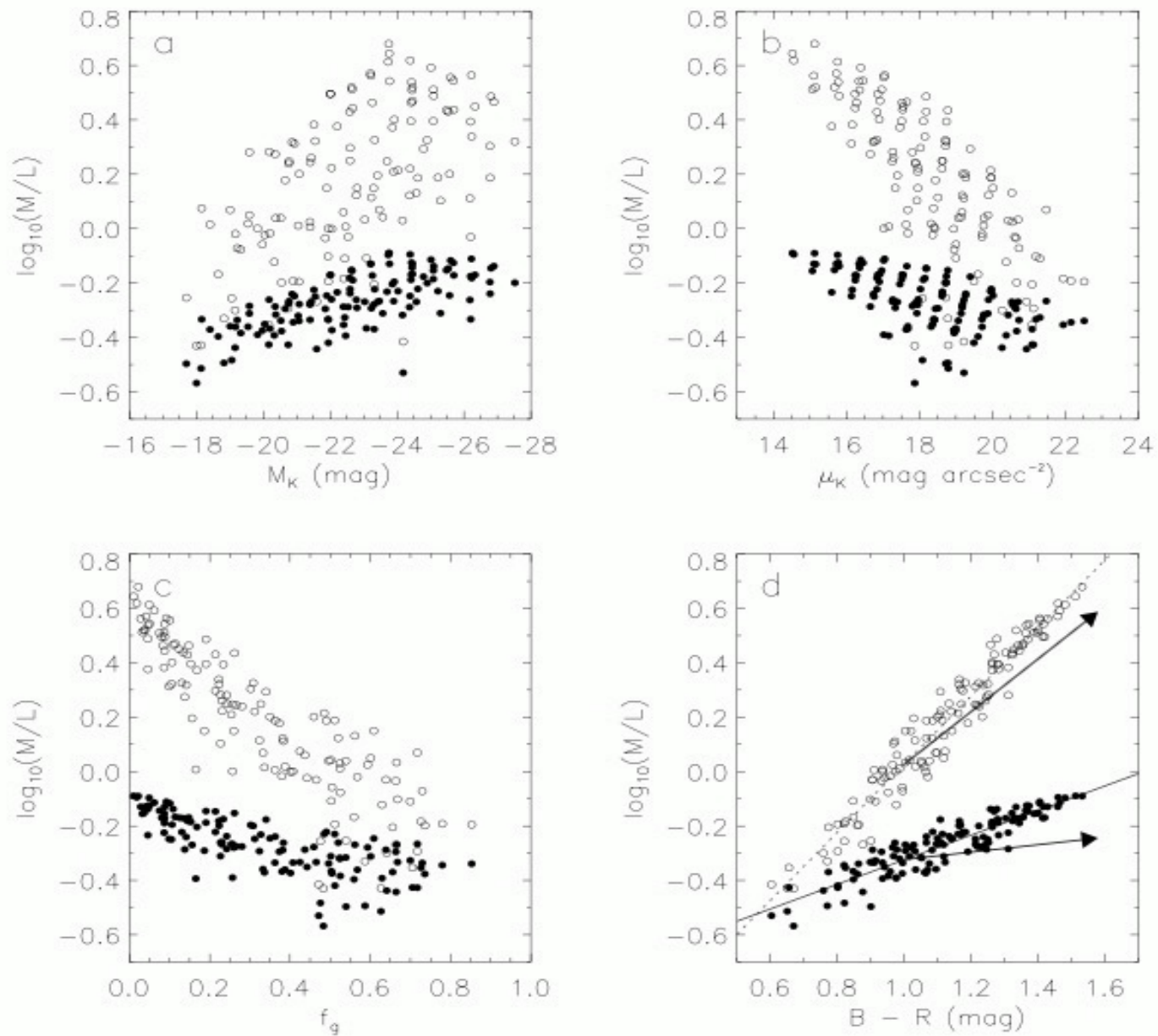
- Assumptions
  - Disk-dominated galaxies
  - Instantaneous recycling approximation (IRA)
  - SPS models of Bruzual & Charlot (2001)
  - Salpeter IMF (scaled down M/L by 0.7 to agree with observations)
  - Masses between 0.2 and 125  $M_{\text{sun}}$
  - Exponential gas disk with either Schmidt (1959) or Kennicutt (1998) star formation law

# Galaxy Evolution Models

- 1) Closed-box, no gas infall or outflow, 12 Gyr, Schmidt law
- 2) + gas infall
- 3) + metal-enriched outflow
- 4) Kennicutt law (no infall or outflow)
- 5) Mass-dependent galaxy formation epoch with no infall or outflow
- 6) “Burst”, mass-dependent galaxy formation epoch, no infall or outflow, SFR varies on 0.5 Gyr scale with lognormal distribution of width 2 ← default model, best reproduces observations

# How to construct galaxy model?

- SPS
- Convert into solar units
- Use IRA to construct stellar masses (instead of full gas mass-loss histories from SPS)
  - Error  $< 5\%$



**Figure 1**  
 Open circle – B  
 Filled circle – K  
 Arrows – dust  
 extinction vectors

# Important points

- Significant trends in all passbands
  - Factors of  $\sim 7$  in B,  $\sim 3$  in I,  $\sim 2$  in K  $\rightarrow$  K-band important for observations where you want to minimize M/L scatter
- For all models, in all optical and near-IR passbands M/L correlates strongly with galaxy color
- Assuming universal IMF, “workers determining the stellar M/L ratios of spiral galaxies will [...] observe trends in stellar M/L ratio that correlate most tightly with galaxy color.”
- Color gradients in spiral galaxies  $\rightarrow$  significant gradients in stellar M/L (outer regions have lower M/L than inner regions)



# Color-M/L Correlation

- SPS with different metallicities from Bruzual and Charlot
- Exponentially declining SFR
  - Parametrized by e-folding timescale  $\tau$
  - M/L computed after lifetime of 12 Gyr
- Strong correlation between B-R color and M/L ratio independent of metallicity or SFH

B-band

K-band

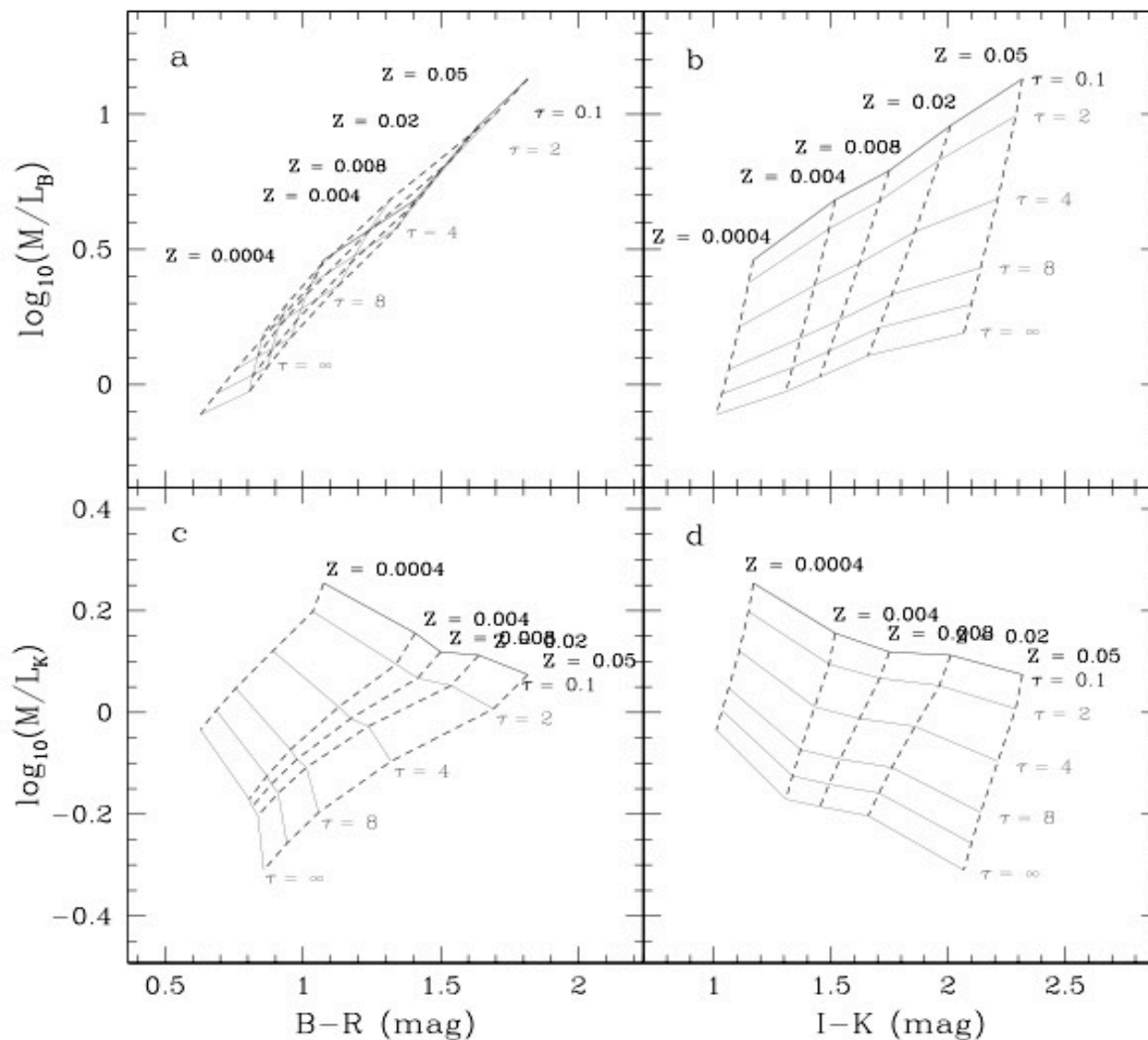
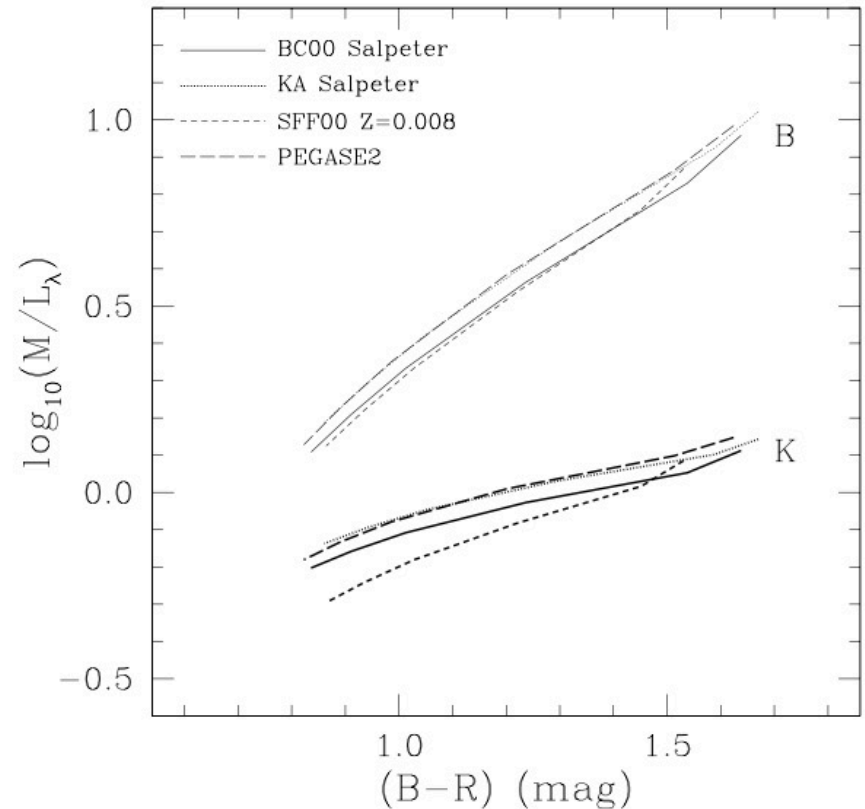


Figure 2  
Solid line – different  $\tau$ ,  
same metallicity  
Dashed line – same  $\tau$ ,  
different metallicity

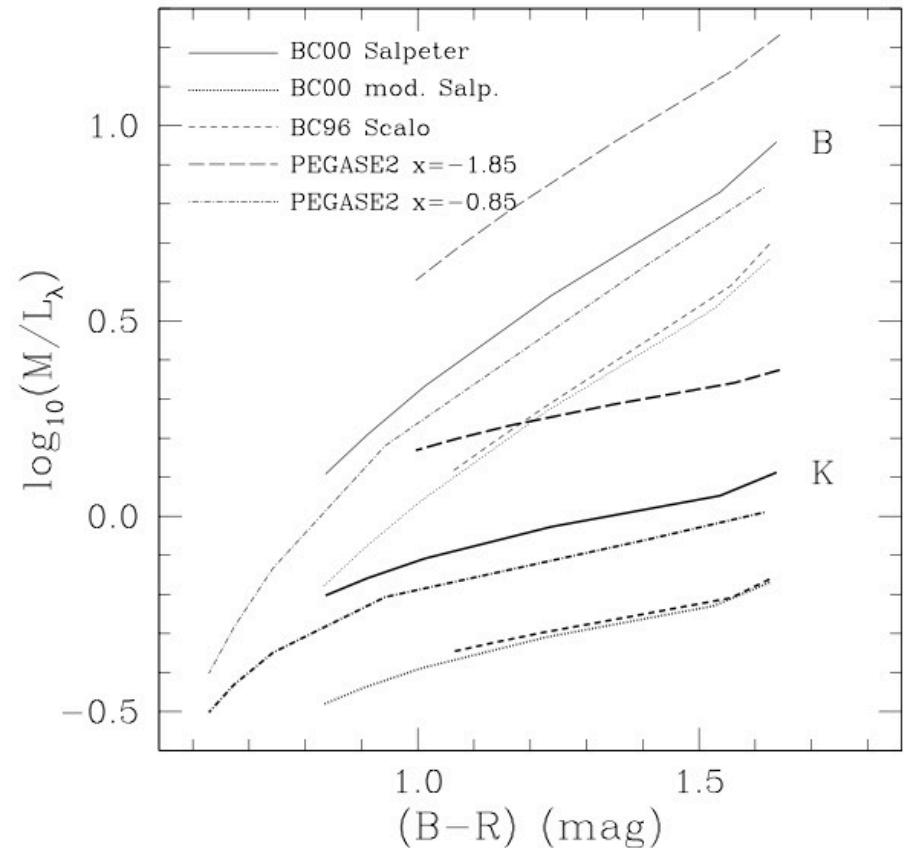
# SPS uncertainties

- Salpeter IMF, solar metallicity  $\tau$  models in B and K band
- Bruzual & Charlot (solid line)
- Kodama & Arimoto (dotted line)
- Schulz, Fritze-von Alvensleben, Fricke (short-dashed line)
- Fioc & Rocca-Volmerange (long-dashed line)
- Conclusion: similar slopes and zero points for M/L-color relation



# IMF effect

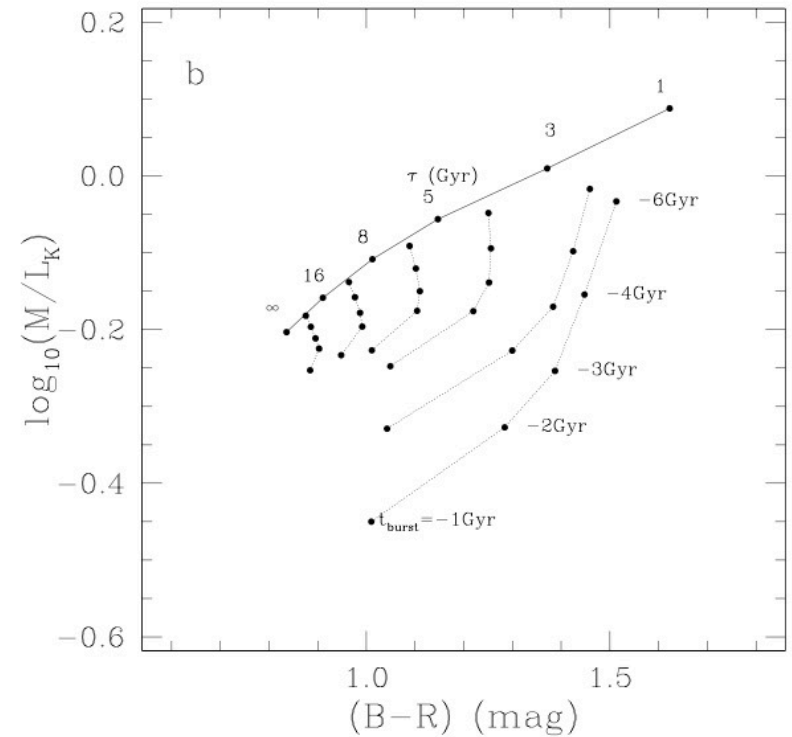
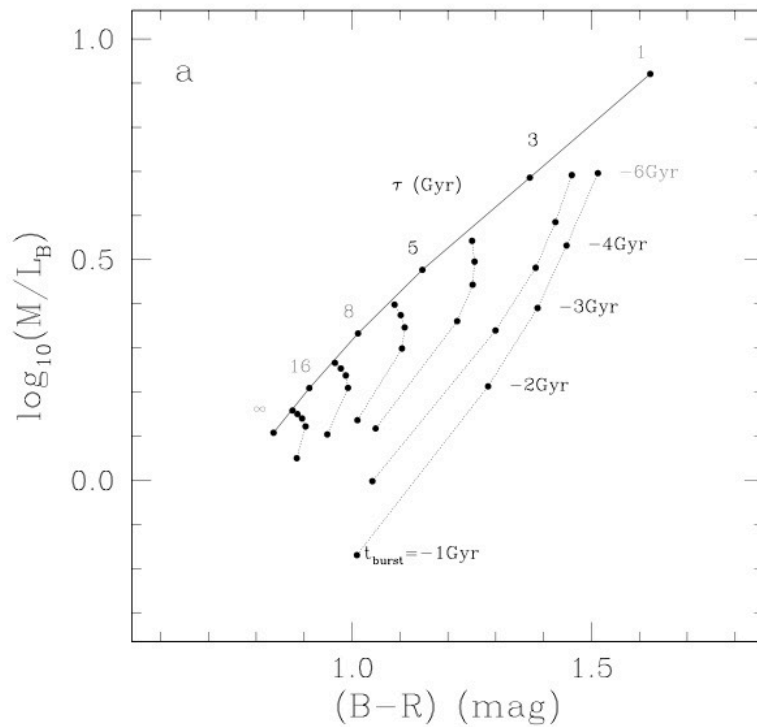
- Bruzual & Charlot
  - + Salpeter IMF (solid line)
  - + modified Salpeter IMF with  $x=0$  below  $0.6 M_{\text{sun}}$  (dotted line)
  - + Scalo IMF (dashed line)
- Fioc & Rocca-Volmerange
  - +  $x=-1.85$  IMF (long-dashed line)
  - +  $x=-0.85$  IMF (short-dashed line)
- Slopes are independent of IMF



# Galaxy evolution uncertainties

- All 6 models are consistent, age change of  $\pm 3$  Gyr  
→ M/L change of  $\pm 0.05$  dex [check Appendix]
- What about larger bursts?
  - 10% mass fraction added in 0.5 Gyr starbursts
  - Larger effect on red earlier type galaxies
  - Bias M/L ratio to lower values at a give color
  - Unlikely to occur and likely to be selected against in sample selection

# Galaxy evolution uncertainties



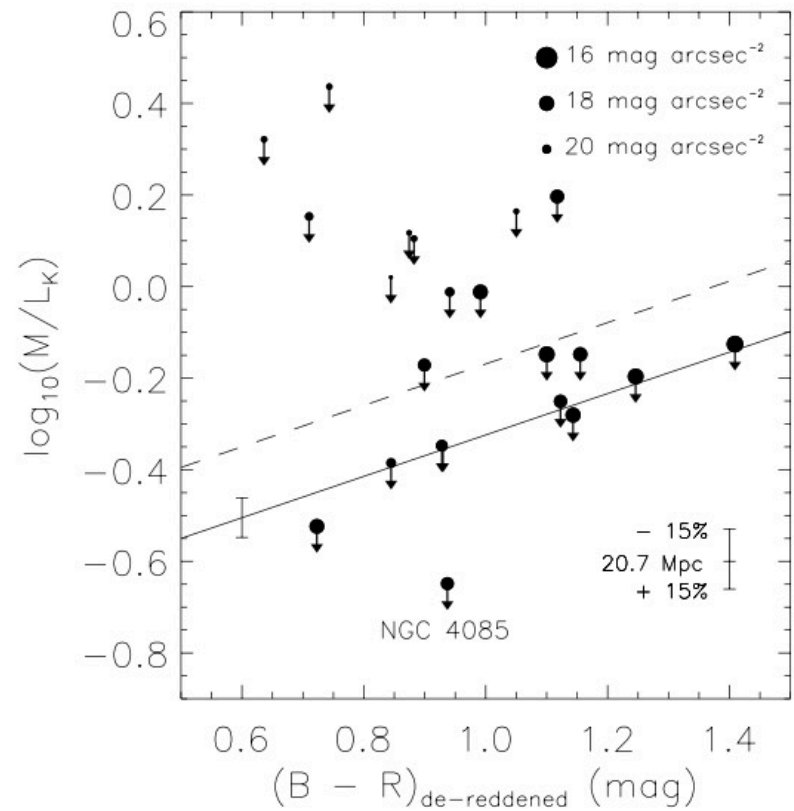
# Uncertainties summary

- Color-M/L is robust in relative sense (within passband and between passbands) provided there is no change in IMF
- Model, galaxy evolution, small bursts, dust  $\rightarrow$  0.1-0.2 dex or less
- IMF gives the largest uncertainty
  - IMFs in literature give uncertainties in absolute normalization of at least a factor of 2

# Rotation curves and normalization

- Constraints from maximum disk hypothesis (stellar disk makes maximum possible contribution to rotation velocity)
- Salpeter  $x=-1.35$  IMF overpredicts (dashed line)
- Salpeter IMF  $x=-1.35$  with  $x=0$  below  $0.35 M_{\text{sun}}$  (scaling by down by factor of 0.7) (solid line)

Ursa Major Cluster





# Rotation curves and normalization

- Zero-point constrained to match observations, but no reason to expect slope of model to match observations
  - Galaxies with maximum disk have similar IMFs

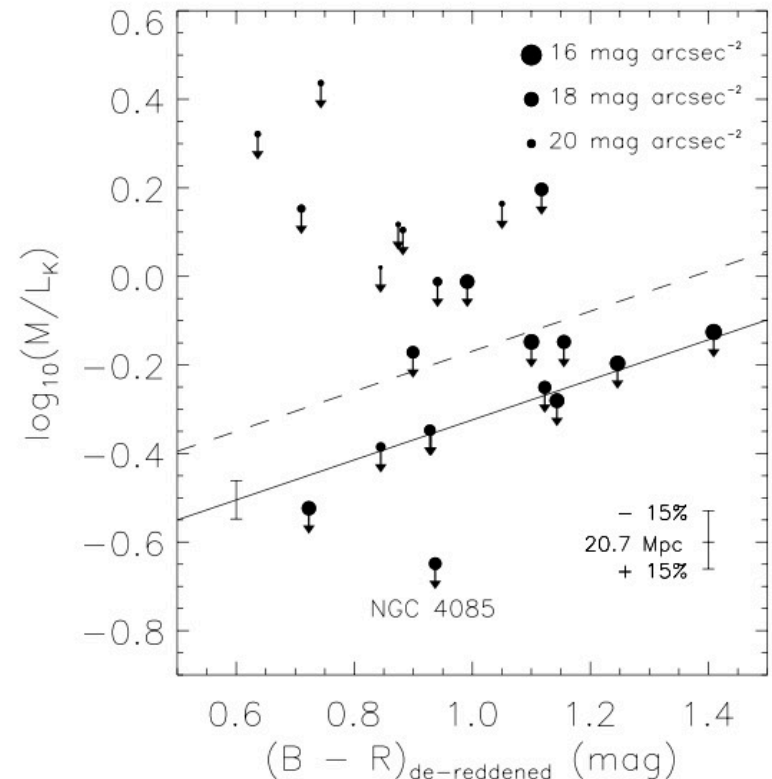


TABLE 1

STELLAR  $M/L$  RATIO AS A FUNCTION OF COLOR FOR THE FORMATION EPOCH MODEL WITH BURSTS, ADOPTING A SCALED SALPETER IMF

Color	$a_B$	$b_B$	$a_V$	$b_V$	$a_R$	$b_R$	$a_I$	$b_I$	$a_J$	$b_J$	$a_H$	$b_H$	$a_K$	$b_K$
$B-V$ .....	-0.994	1.804	-0.734	1.404	-0.660	1.222	-0.627	1.075	-0.621	0.794	-0.663	0.704	-0.692	0.652
$B-R$ .....	-1.224	1.251	-0.916	0.976	-0.820	0.851	-0.768	0.748	-0.724	0.552	-0.754	0.489	-0.776	0.452
$V-I$ .....	-1.919	2.214	-1.476	1.747	-1.314	1.528	-1.204	1.347	-1.040	0.987	-1.030	0.870	-1.027	0.800
$V-J$ .....	-1.903	1.138	-1.477	0.905	-1.319	0.794	-1.209	0.700	-1.029	0.505	-1.014	0.442	-1.005	0.402
$V-H$ .....	-2.181	0.978	-1.700	0.779	-1.515	0.684	-1.383	0.603	-1.151	0.434	-1.120	0.379	-1.100	0.345
$V-K$ .....	-2.156	0.895	-1.683	0.714	-1.501	0.627	-1.370	0.553	-1.139	0.396	-1.108	0.346	-1.087	0.314

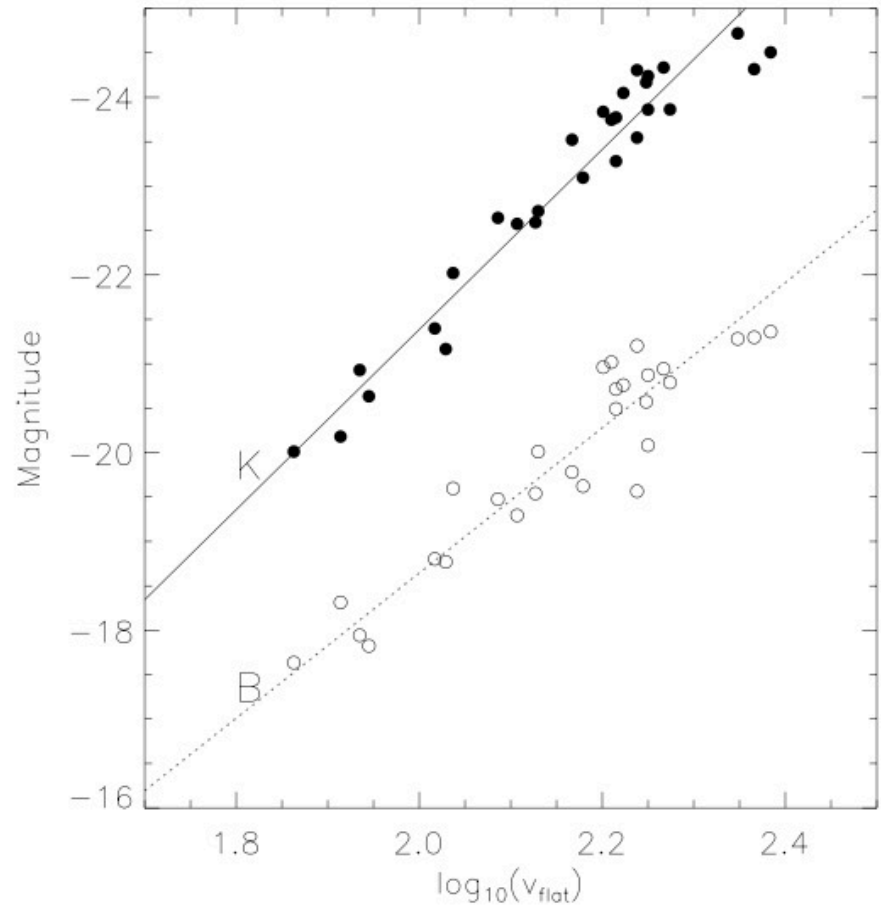
NOTE.— $\log_{10} (M/L) = a_\lambda + b_\lambda \text{Color}$ . Note that the stellar  $M/L$  values can be estimated for any combination of the above colors by a simple linear combination of the above fits. Note also that if *all* (even very high surface brightness) disks are submaximal, the above zero points should be modified by subtracting a constant from the above relations.

# Tully-Fisher relation

- Relates dynamical mass to luminosity
- Limited by passband-dependent slope
  - $L \sim V^3$  in blue
  - $L \sim V^4$  in near-IR
- Possible for theory to match T-F in one passband, but not in others
- Goal is to use previous results (Table 1) to find a single, passband-independent T-F relation

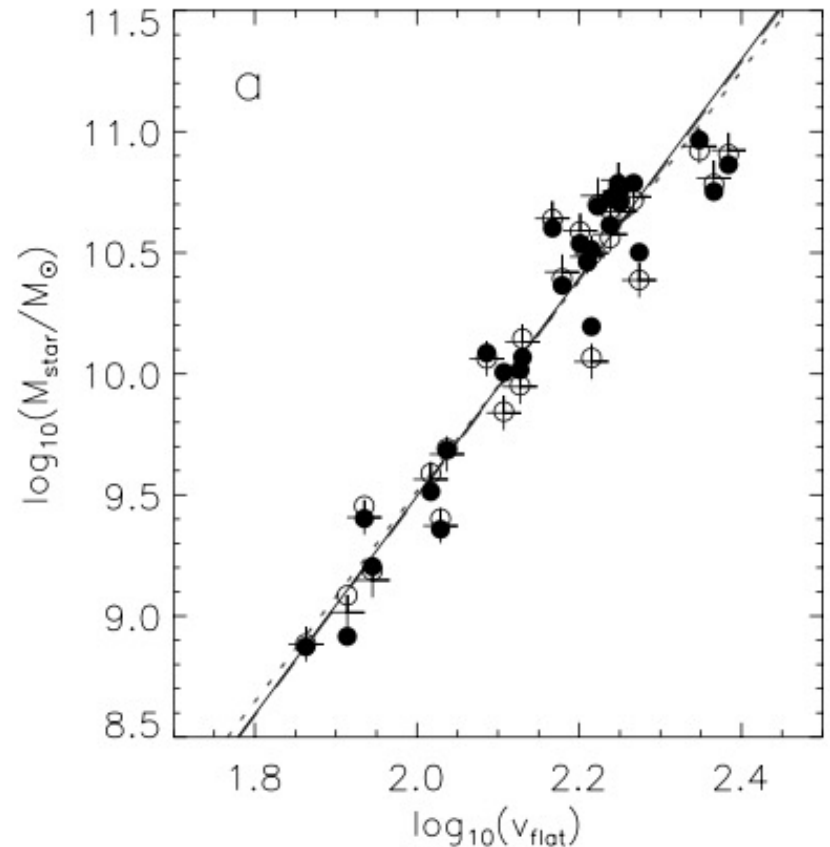
# Tully-Fisher relation

- Ursa Major Cluster data
- Foreground galactic extinction
- Internal extinction
- T-F shallower in bluer passbands than in near-IR



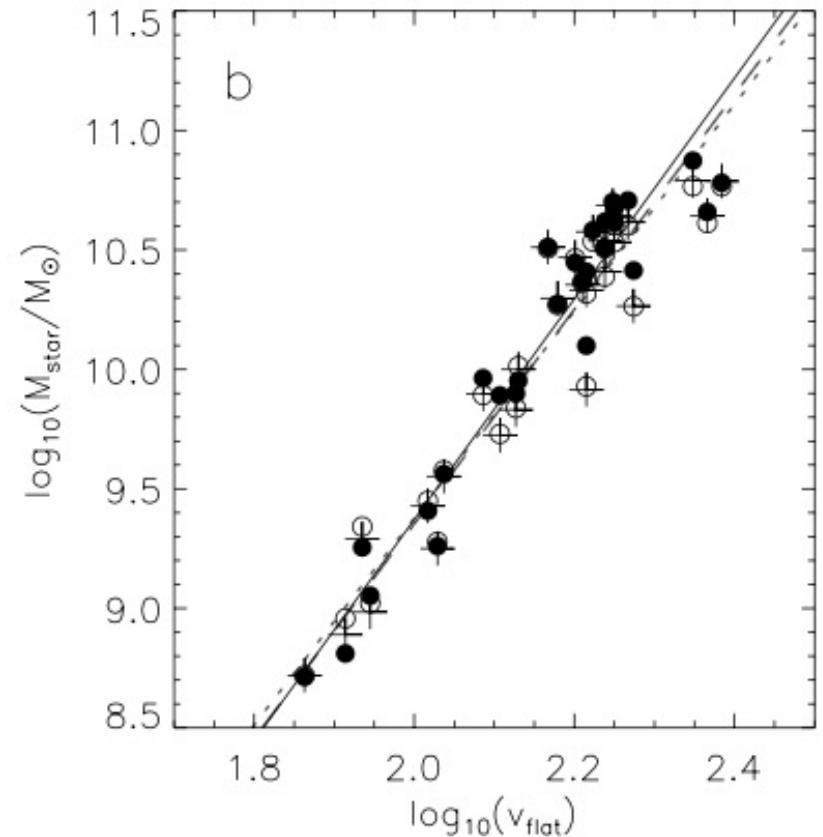
# Stellar mass T-F

- Mass-dependent extinction correction
- B, R – open circles
- I – crosses
- K – filled circles
- Passband-independent relation, consistent within  $\sim 10\%$  rms
  - $L \sim V^{4.4 \pm 0.2}$



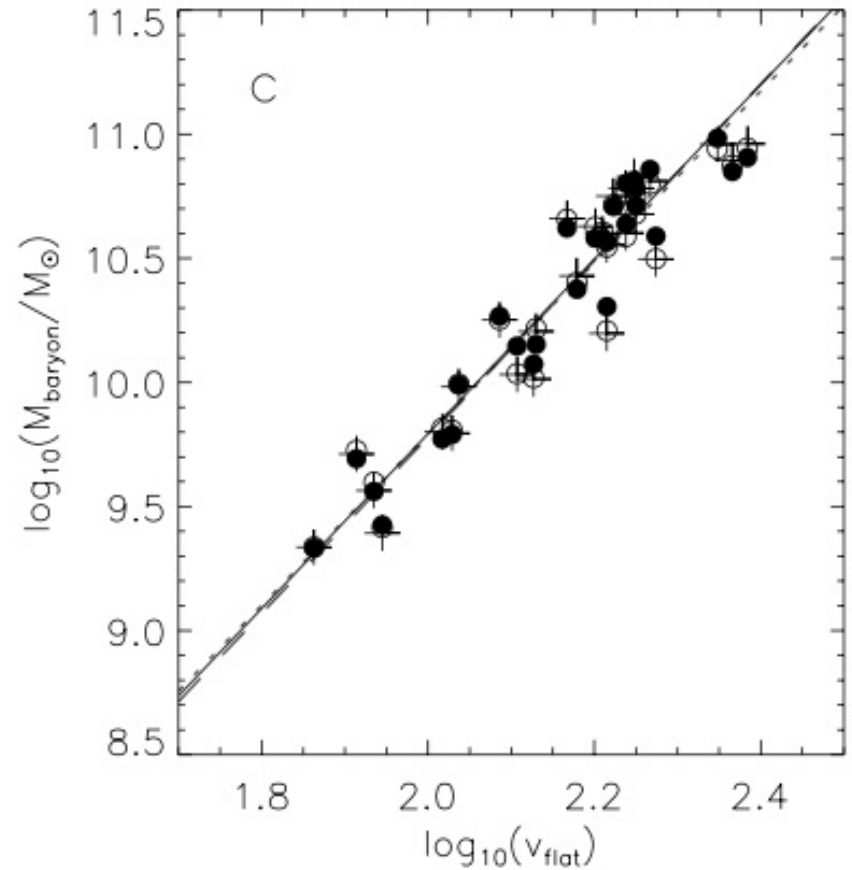
# Stellar mass T-F

- Mass-independent extinction correction
- Almost the same as for mass-dependent extinction case
- B,R fits – dotted line
- I fit – dashed line
- K fit – solid line



# Baryonic mass T-F

- $M_{\text{baryon}} \sim V^{3.5 \pm 0.2}$



# Summary

- Under several assumptions:
  - Variations in M/L correlate strongly with color
  - Low surface brightness, high gas fraction, low-luminosity galaxies have lower M/L ratios
  - Color correlation is robust to uncertainties in SP and galaxy evolution models
  - Stellar IMF is main uncertainty
- Modified Salpeter IMF best fits the observations
- Slope of stellar T-F of Ursa Major Cluster is  $4.4 \pm 0.2$
- Slope of baryonic T-F of Ursa Major Cluster is  $3.5 \pm 0.2$