Correcting Choice of Lambda

	\hat{S}^2	\(\)
classical	s^2	0
quantum	s(s+1)	$\frac{1}{2}$
Langer modification	$\left(s+\frac{1}{2}\right)^2$	$\frac{3}{4}$

Value selected based on short-time analysis of 2-state populations and many-electron currents

Mapping Multiple States

$$\left\langle \mathbf{n}' \middle| \hat{a}_i^{\dagger} \hat{a}_j \middle| \mathbf{n} \right\rangle = \delta_{n_i, n'_i + 1} \, \delta_{n_j, n'_j - 1} \prod_{p=i+1}^{j-1} (-1)^{n_p} \prod_{q \neq i, j} \delta_{n_q, n'_q}$$

This is the direct product of 2x2 matrices for each dof!