

Calculating the Left Current

$$\hat{I}_{L} \propto -\frac{\mathrm{d}}{\mathrm{d}t} \left\langle \sum_{k \in L} \hat{a}_{k}^{\dagger} \hat{a}_{k} \right\rangle$$

$$\propto -\left\langle \sum_{k \in L} t_{k} (\hat{a}_{0}^{\dagger} \hat{a}_{k} - \hat{a}_{k}^{\dagger} \hat{a}_{0}) \right\rangle$$