Initial Conditions

$$\min(Z^{-1}(\omega)) = 0$$
 $\max(Z^{-1}(\omega)) = 1$ $n = 0$ $n = 1$ $\sum_{k=1}^{\infty} Z^{-1}(\omega)$

$$n_i = \begin{cases} 0 & \text{if } \chi_i < (1 + e^{-\beta(\epsilon_i - \mu_i)})^{-1}, \\ 1 & \text{otherwise.} \end{cases}$$

$$\langle n \rangle = 0 \cdot P(0) + 1 \cdot P(1)$$

= $1 \cdot (1 - P(0)) = 1 - Z^{-1}(\omega)$
= $\frac{(1 + e^{-\beta \omega}) - 1}{1 + e^{-\beta \omega}} = \frac{1}{e^{+\beta \omega} + 1} = f(\omega; \beta)$