$$\sqrt{n-n^2+\lambda} \implies n \in \left[\frac{1}{2} - \sqrt{\frac{1}{4}+\lambda}, \frac{1}{2} + \sqrt{\frac{1}{4}+\lambda}\right]$$



