## **ECSN-Test**

## April 9, 2019

## 1 ECSN Test

```
In [1]: from StarKiller.initialization import starkiller_initialize
        from StarKiller.interfaces import EosType
        from StarKiller.interfaces import BurnType
        from StarKiller.eos import Eos
        from StarKiller.network import Network
        import numpy as np
In [2]: probin_file = "probin_ecsn"
In [3]: starkiller_initialize(probin_file)
In [4]: helmholtz = Eos()
        ecsn = Network()
In [5]: def get_eps_nuc_eos(burn_state):
            ecsn.rhs(burn_state)
            print(burn_state.state)
            eos_state = burn_state.to_eos_type()
            helmholtz.evaluate(eos_state.eos_input_rt, eos_state)
            print(eos_state.state)
            Hnuc = burn_state.state.ydot[ecsn.net_ienuc]
            print("Energy generation rate: {:0.09e}".format(Hnuc))
            aion = ecsn.ActualNetworkModule.aion
            zion = ecsn.ActualNetworkModule.zion
            \# dX/dt = dY/dt * Aion
            omegadot = burn_state.state.ydot[:ecsn.nspec_evolve] * aion
            print("omegadot = {}".format(omegadot))
            cp = eos_state.state.cp
            print("cp = {:0.05e}".format(cp))
            dpdt = eos_state.state.dpdt
```

```
dpdx = eos_state.state.dpdx
            print("dpdx = {}".format(dpdx))
            dhdx = eos_state.state.dhdx
           print("dhdx = {}".format(dhdx))
           print("cp * dpdx/dpdt = {}".format(cp * dpdx/dpdt))
           print("cp * dpdx/dpdt * wdot = {:0.09e}".format(np.dot(cp * dpdx/dpdt, omegadot)))
            print("dhdx = {}".format(dhdx))
            print("dhdx * wdot = {:0.09e}".format(np.dot(dhdx, omegadot)))
            dHcompdx = (cp * dpdx/dpdt - dhdx)
            print("dHcompdx = {}".format(dHcompdx))
            Hcomp = np.dot(dHcompdx, omegadot)
            print("Composition energy generation: {:0.09e}".format(Hcomp))
            dedx = eos_state.state.dedx
            print("dedx = {}".format(dedx))
            de = -np.dot(dedx, omegadot)
            print("eps_nuc_eos = dedx * wdot (cf. MESA) = {:0.09e}".format(de))
            dabardX = (eos_state.state.abar/aion) * (aion - eos_state.state.abar)
            dzbardX = (eos_state.state.abar/aion) * (zion - eos_state.state.zbar)
            dabardt = np.dot(dabardX, omegadot)
            dzbardt = np.dot(dzbardX, omegadot)
            print("dabar/dt = {:0.09e}".format(dabardt))
            print("dzbar/dt = {:0.09e}".format(dzbardt))
           print("sum omegadot = {:0.16e}".format(np.sum(omegadot)))
           print("sum X = {:0.16e}".format(np.sum(burn_state.state.xn)))
           Htot = Hnuc + Hcomp
            print("Hnuc + Hcomp (Maestro): {:0.9e}".format(Htot))
1.1 Test 1 from Josiah
In [6]: burn_state_1 = BurnType()
        burn_state_1.state.rho = 7607783959.50421e0
        burn_state_1.state.t = 983559309.749412e0
        burn_state_1.state.xn[ecsn.species_map["h1"]] = 0.0
        burn_state_1.state.xn[ecsn.species_map["he4"]] = 1.14998095787427E-18
```

print("dpdt = {:0.05e}".format(dpdt))

```
burn_state_1.state.xn[ecsn.species_map["o16"]] = 0.5955320774
        burn_state_1.state.xn[ecsn.species_map["o20"]] = 0.203902681
        burn_state_1.state.xn[ecsn.species_map["f20"]] = 1.17278643621995E-07
        burn_state_1.state.xn[ecsn.species_map["ne20"]] = 0.19753136
        burn state 1.state.xn[ecsn.species map["mg24"]] = 0.0
        burn_state_1.state.xn[ecsn.species_map["al27"]] = 0.0
        burn state 1.state.xn[ecsn.species map["si28"]] = 0.0027259815
        burn_state_1.state.xn[ecsn.species_map["p31"]] = 0.0
        burn state 1.state.xn[ecsn.species map["s32"]] = 0.0
In [7]: get_eps_nuc_eos(burn_state_1)
<burn t>{
   rho: 7607783959.50421,
   t: 983559309.749412,
   e: 2.490743133790312e+18,
   xn: array([0.0000000e+00, 1.14998096e-18, 5.95532077e-01, 2.03902681e-01,
       1.17278644e-07, 1.97531360e-01, 0.00000000e+00, 0.00000000e+00,
       2.72598150e-03, 0.00000000e+00, 0.00000000e+00]),
   cv: 14444247.553061701,
   cp: 14486626.878325198,
   y_e : 0.47945583462538965,
    eta: 87.75746182063078,
   cs: 1099451413.7881703,
   dx : 0.0,
   abar: 17.42469332287015,
   zbar: 8.354370880208164,
   t old: 6.91452328486113e-310,
   dcvdt: 4.6613249073456e-310,
   dcpdt: 4.66132490734757e-310,
   ydot: array([ 1.16695205e-11, -7.26850364e-12, -4.11345965e-11, 5.79382894e-11,
        7.42255606e-12, -5.81959032e-11, 2.16734518e-12, 0.00000000e+00,
        4.23112889e-12, 1.16695205e-11, 5.05156388e-16, -3.95207429e+01,
       -5.72522257e+08]),
    jac : array([[4.66132491e-310, 4.66132491e-310, 5.30498948e-313,
        0.00000000e+000, 6.91451145e-310, 1.38338381e-322,
        4.94065646e-324, 6.91455022e-310, 6.91452328e-310,
        1.01855798e-312, 2.54639621e-313, 6.91455065e-310,
       8.27578359e-313],
       [4.24400499e-314, 6.91455635e-310, 2.96439388e-323,
        1.97626258e-323, 0.00000000e+000, 6.91455065e-310,
        2.47032823e-323, 0.00000000e+000, 4.66132491e-310,
        1.48539705e-313, 2.96439388e-323, 4.94065646e-324,
        4.24399158e-314],
       [0.00000000e+000, 4.94065646e-324, 4.66132491e-310,
        1.23516411e-322, 0.00000000e+000, 1.48539705e-313,
        1.38338381e-322, 0.00000000e+000, 0.00000000e+000,
        4.66132491e-310, 1.23516411e-322, 1.48539839e-313,
```

```
4.66132491e-310],
[0.00000000e+000, 1.48219694e-323, 4.66132491e-310,
4.66132491e-310, 4.88059032e-313, 0.00000000e+000,
6.91455065e-310, 8.27578359e-313, 0.00000000e+000,
4.66132491e-310, 4.66132491e-310, 4.66839074e-313,
5.43472210e-323],
[4.94065646e-324, 1.23516411e-322, 0.00000000e+000,
6.91455635e-310, 2.96439388e-323, 2.47032823e-323,
4.24399158e-314, 1.48219694e-323, 1.28457068e-322,
2.33419663e-313, 6.91455635e-310, 1.23516411e-322,
2.12200857e-314],
[4.94065646e-324, 4.66132491e-310, 1.06099924e-313,
4.94065646e-324, 4.66132491e-310, 1.23516411e-322,
0.00000000e+000, 4.66132491e-310, 4.66132491e-310,
0.00000000e+000, 4.94065646e-324, 4.66132491e-310,
1.28457068e-322],
[4.66132491e-310, 6.91455562e-310, 0.00000000e+000,
1.97626258e-323, 4.66132491e-310, 4.66132491e-310,
4.66839074e-313, 3.16202013e-320, 4.66132491e-310,
0.00000000e+000, 2.96439388e-323, 6.91451135e-310,
4.66132491e-310],
[1.27319748e-313, 9.88131292e-324, 1.48219694e-323,
1.23516411e-322, 0.00000000e+000, 6.91455635e-310,
1.06099790e-313, 0.00000000e+000, 9.88131292e-324,
2.47032823e-323, 1.23516411e-322, 4.94065646e-324,
4.66132491e-310],
[6.91455065e-310, 1.48219694e-323, 4.94065646e-324,
4.66132491e-310, 0.00000000e+000, 4.94065646e-324,
4.66132491e-310, 1.28457068e-322, 2.47032823e-323,
4.94065646e-324, 4.66132491e-310, 4.66839074e-313,
4.94065646e-324],
[4.94065646e-324, 8.48798317e-314, 4.66132491e-310,
6.91455635e-310, 1.27319875e-313, 2.47032823e-323,
6.91451135e-310, 4.66132491e-310, 8.39911598e-323,
4.66132491e-310, 6.91455022e-310, 8.89318163e-323,
4.66839074e-313],
[1.48539839e-313, 6.91451145e-310, 1.38338381e-322,
1.27319747e-313, 1.97626258e-323, 1.23516411e-322,
1.27319747e-313, 4.66132491e-310, 6.91451145e-310,
1.38338381e-322, 4.94065646e-324, 6.91451135e-310,
1.06099790e-313],
[1.48219694e-323, 2.96439388e-323, 6.91455065e-310,
1.97626258e-323, 4.94065646e-324, 4.66132491e-310,
4.66839074e-313, 4.94065646e-324, 1.27319875e-313,
6.91455065e-310, 2.96439388e-323, 7.58884832e-320,
4.66132491e-310],
[1.23516411e-322, 2.12200857e-314, 4.94065646e-324,
8.39911598e-323, 4.66132491e-310, 6.91455022e-310,
```

```
8.89318163e-323, 4.66839074e-313, 0.00000000e+000,
       4.94065646e-324, 1.27319748e-313, 0.00000000e+000,
       0.0000000e+000]]),
   self_heat : 25856,
   i:6,
   j: 26,
   k:0,
   n_rhs : -1280125512,
   n_jac : 21966,
   time: 4.6613249074211e-310,
    success : 2}
<eos t>{
   rho: 7607783959.50421,
   t: 983559309.749412,
   p: 6.87649058595149e+27,
   e: 2.490743133790312e+18,
   h: 3.3946187725511716e+18,
   s: 46493486.57937405,
   xn: array([0.00000000e+00, 1.14998096e-18, 5.95532077e-01, 2.03902681e-01,
       1.17278644e-07, 1.97531360e-01, 0.00000000e+00, 0.00000000e+00,
       2.72598150e-03, 0.00000000e+00, 0.00000000e+00]),
   aux : array([], dtype=float64),
   dpdt: 5.482451265458468e+16,
   dpdr: 1.2052571947699988e+18,
   dedt: 14444247.553061701,
   dedr: 117877656.67151032,
    dhdt: 21650618.41564302,
    dhdr: 157492550.78698152,
   dsdt: 0.014685690440713491,
   dsdr : -0.0009472365278694044,
   dpde: 3795594921.3127203,
   dpdr_e : 7.578413597713697e+17,
    cv: 14444247.553061701,
    cp: 14486626.878325198,
   xne : 2.196634277233492e+33,
   xnp : 0.0,
   eta: 87.75746182063078,
   pele: 6.958956124711135e+27,
   ppos : 0.0,
   mu: 1.668408683623596e-257,
   mu_e : 2.085697842808241,
   y_e : 0.47945583462538965,
   dedx: array([4.33966224e+18, 2.88111110e+17, 1.47145182e+17, -5.59790031e+17,
      -2.11021289e+17, 1.37747453e+17, 1.31482301e+17, -1.17194771e+15,
       1.27007192e+17, 1.19026957e+16,
                                         1.23650860e+17]),
    dpdx: array([ 1.19073140e+28, 8.14581090e+26, 3.98775309e+26, -1.51484702e+27,
       -5.71896050e+26, 3.71054924e+26, 3.52574667e+26, -6.93324382e+24,
       3.39374483e+26, 2.75321273e+25, 3.29474346e+26),
```

```
dhdx: array([4.34886659e+18, 2.88740781e+17, 1.47453435e+17, -5.60961007e+17,
       -2.11463364e+17, 1.38034278e+17, 1.31754841e+17, -1.17730710e+15,
        1.27269528e+17, 1.19239780e+16, 1.23905544e+17]),
    gam1: 1.3373448286956426,
    cs: 1099451413.7881703,
    abar: 17.42469332287015,
    zbar: 8.354370880208164,
    dpda: -5.2622655581624275e+26,
    dpdz: 1.0823157183836253e+27,
    deda: -1.9440978481690643e+17,
    dedz: 4.003155009345395e+17,
    conductivity: 4.11e-321}
Energy generation rate: -5.725222567e+08
omegadot = [1.16695205e-11 -2.90740146e-11 -6.58153544e-10 1.15876579e-09]
  1.48451121e-10 -1.16391806e-09 5.20162842e-11 0.00000000e+00
  1.18471609e-10 3.61755137e-10 1.61650044e-14]
cp = 1.44866e+07
dpdt = 5.48245e+16
dpdx = [ 1.19073140e+28 8.14581090e+26 3.98775309e+26 -1.51484702e+27
 -5.71896050e+26 3.71054924e+26 3.52574667e+26 -6.93324382e+24
  3.39374483e+26 2.75321273e+25 3.29474346e+26]
dhdx = \begin{bmatrix} 4.34886659e+18 & 2.88740781e+17 & 1.47453435e+17 & -5.60961007e+17 \end{bmatrix}
 -2.11463364e+17 1.38034278e+17 1.31754841e+17 -1.17730710e+15
  1.27269528e+17 1.19239780e+16 1.23905544e+17]
cp * dpdx/dpdt = [ 3.14634469e+18 2.15241901e+17 1.05370916e+17 -4.00277586e+17
 -1.51115701e+17 9.80461836e+16 9.31630287e+16 -1.83201476e+15
  8.96750609e+16 7.27498770e+15 8.70590851e+16]
cp * dpdx/dpdt * wdot = -6.211677313e+08
dhdx = \begin{bmatrix} 4.34886659e+18 & 2.88740781e+17 & 1.47453435e+17 & -5.60961007e+17 \end{bmatrix}
 -2.11463364e+17 1.38034278e+17 1.31754841e+17 -1.17730710e+15
  1.27269528e+17 1.19239780e+16 1.23905544e+17]
dhdx * wdot = -8.705208662e+08
dHcompdx = [-1.20252190e+18 -7.34988800e+16 -4.20825188e+16 1.60683420e+17]
  6.03476628e+16 -3.99880947e+16 -3.85918119e+16 -6.54707656e+14
 -3.75944671e+16 -4.64899032e+15 -3.68464585e+16]
Composition energy generation: 2.493531349e+08
dedx = \begin{bmatrix} 4.33966224e+18 & 2.88111110e+17 & 1.47145182e+17 & -5.59790031e+17 \end{bmatrix}
 -2.11021289e+17 1.37747453e+17 1.31482301e+17 -1.17194771e+15
  1.27007192e+17 1.19026957e+16 1.23650860e+17]
eps_nuc_eos = dedx * wdot (cf. MESA) = 8.687036959e+08
dabar/dt = 3.491671084e-09
dzbar/dt = -4.743475369e-10
sum omegadot = -2.0731264589208190e-27
sum X = 9.9969221717864365e-01
Hnuc + Hcomp (Maestro): -3.231691217e+08
```

## 1.2 Test 2 from Josiah

```
In [8]: burn state 2 = BurnType()
        burn state 2.state.rho = 8346403698.95185e0
        burn_state_2.state.t = 656536305.140964e0
        burn state 2.state.xn[ecsn.species map["h1"]] = 0.0
        burn_state_2.state.xn[ecsn.species_map["he4"]] = 8.89957317703129E-23
        burn_state_2.state.xn[ecsn.species_map["o16"]] = 0.5999942706e0
        burn_state_2.state.xn[ecsn.species_map["020"]] = 0.3926652894e0
        burn_state_2.state.xn[ecsn.species_map["f20"]] = 0.0000000002e0
        burn_state_2.state.xn[ecsn.species_map["ne20"]] = 0.0073364571e0
        burn_state_2.state.xn[ecsn.species_map["mg24"]] = 0.0
        burn_state_2.state.xn[ecsn.species_map["al27"]] = 0.0
        burn_state_2.state.xn[ecsn.species_map["si28"]] = 3.518236231242E-06
        burn state 2.state.xn[ecsn.species map["p31"]] = 0.0
        burn_state_2.state.xn[ecsn.species_map["s32"]] = 0.0
In [9]: get_eps_nuc_eos(burn_state_2)
<burn t>{
   rho: 8346403698.95185,
   t: 656536305.140964,
   e: 2.4366503017450455e+18,
   xn : array([0.0000000e+00, 8.89957318e-23, 5.99994271e-01, 3.92665289e-01,
       2.00000000e-09, 7.33645710e-03, 0.00000000e+00, 0.00000000e+00,
       3.51823623e-06, 0.00000000e+00, 0.00000000e+00]),
    cv: 13444158.983137527,
    cp: 13470518.44019436,
   y e: 0.46073323962811563,
    eta: 133.98527882572262,
   cs: 1086123519.6557314,
   dx : 0.0,
   abar: 17.391348207658748,
   zbar: 8.012772201215236,
    t old: 6.91452328486113e-310,
   dcvdt: 4.66132490582783e-310,
   dcpdt: 4.6613249058298e-310,
   ydot : array([ 3.75545872e-17, -2.13349498e-17, -1.35886276e-16, 1.24835159e-12,
        1.35222972e-13, -1.38354101e-12, 5.60711361e-19, 0.00000000e+00,
        1.33342876e-17, 3.75545872e-17, 4.90756421e-25, 3.57280937e-62,
       -1.61389226e+07]),
    jac : array([[4.66132491e-310, 4.66132491e-310, 5.30498948e-313,
        0.00000000e+000, 6.91451145e-310, 4.24399160e-314,
        4.94065646e-324, 6.91451135e-310, 1.48539705e-313,
        1.01855798e-312, 0.00000000e+000, 6.91455065e-310,
        8.27578359e-313],
       [6.01334510e-154, 6.91455635e-310, 2.96439388e-323,
        1.97626258e-323, 2.12201147e-314, 6.91455360e-310,
```

```
2.47032823e-323, 2.12199781e-313, 4.66132491e-310,
2.96439388e-323, 2.96439388e-323, 4.94065646e-324,
1.48219694e-323],
[3.67294518e-062, 1.39642613e-076, 4.66132491e-310,
1.69759663e-313, 0.00000000e+000, 4.94065646e-324,
2.12199580e-314, 0.00000000e+000, 0.00000000e+000,
4.66132491e-310, 1.23516411e-322, 0.00000000e+000,
4.66132491e-310],
[3.92639286e+179, 1.48219694e-323, 4.66132491e-310,
4.66132491e-310, 4.88059032e-313, 1.27319874e-313,
6.91455065e-310, 8.27578359e-313, 3.41498174e-320,
4.66132491e-310, 4.66132491e-310, 4.66839074e-313,
0.00000000e+000],
[4.94065646e-324, 1.74652330e-076, 4.66132491e-310,
6.91455635e-310, 6.36598738e-314, 2.47032823e-323,
4.94065646e-324, 1.27319747e-313, 1.28457068e-322,
1.58101007e-322, 6.91455635e-310, 1.23516411e-322,
0.00000000e+000],
[4.94065646e-324, 4.66132491e-310, 4.66132491e-310,
2.12199579e-314, 4.66132491e-310, 1.23516411e-322,
1.26480805e-321, 4.66132491e-310, 4.66132491e-310,
1.69759790e-313, 4.94065646e-324, 4.66132491e-310,
1.28457068e-322],
[4.66132491e-310, 6.91455562e-310, 4.24400625e-314,
1.97626258e-323, 4.66132491e-310, 4.66132491e-310,
4.66839074e-313, 0.00000000e+000, 4.66132491e-310,
0.00000000e+000, 2.96439388e-323, 6.91451135e-310,
4.66132491e-310],
[6.01182197e-067, 5.20843611e-090, 1.48219694e-323,
1.23516411e-322, 3.81959376e-313, 6.91455635e-310,
1.23516411e-322, 1.69759820e-313, 9.88131292e-324,
2.47032823e-323, 1.69759663e-313, 4.94065646e-324,
4.66132491e-310],
[6.91455360e-310, 1.48219694e-323, 4.94065646e-324,
4.66132491e-310, 0.00000000e+000, 4.94065646e-324,
4.66132491e-310, 1.28457068e-322, 2.47032823e-323,
4.94065646e-324, 4.66132491e-310, 4.66839074e-313,
4.24399158e-314],
[6.01346930e-154, 2.62395791e+179, 4.66132491e-310,
6.91455635e-310, 0.00000000e+000, 2.47032823e-323,
6.91451135e-310, 4.66132491e-310, 2.12199580e-314,
4.66132491e-310, 6.91455022e-310, 4.24399159e-314,
4.66839074e-313],
[1.36922931e-071, 6.91451145e-310, 1.38338381e-322,
9.88131292e-324, 1.97626258e-323, 1.23516411e-322,
4.94065646e-324, 4.66132491e-310, 6.91451145e-310,
1.38338381e-322, 4.94065646e-324, 6.91451135e-310,
1.48219694e-323],
```

```
[1.48219694e-323, 3.24245662e-086, 6.91455360e-310,
        1.97626258e-323, 4.94065646e-324, 4.66132491e-310,
        4.66839074e-313, 4.94065646e-324, 0.00000000e+000,
        6.91455360e-310, 2.96439388e-323, 0.00000000e+000,
        4.66132491e-310],
       [3.70155530e-033, 1.39804329e-076, 2.12199579e-313,
        8.39911598e-323, 4.66132491e-310, 6.91455022e-310,
        8.89318163e-323, 4.66839074e-313, 1.26480805e-321,
        4.94065646e-324, 1.38338381e-322, 2.12201615e-314,
        0.0000000e+000]]),
   self_heat : 0,
    i:0,
   j: 26,
   k: 10,
   n_rhs : -1280156232,
   n_jac : 21966,
   time: 4.6613249059033e-310,
   success : 2}
<eos_t>{
   rho: 8346403698.95185,
   t: 656536305.140964,
   p: 7.364917477765657e+27,
   e: 2.4366503017450455e+18,
   h: 3.3190563946459377e+18,
   s: 40474438.71911317,
   xn: array([0.00000000e+00, 8.89957318e-23, 5.99994271e-01, 3.92665289e-01,
       2.00000000e-09, 7.33645710e-03, 0.00000000e+00, 0.00000000e+00,
       3.51823623e-06, 0.00000000e+00, 0.00000000e+00]),
   aux : array([], dtype=float64),
   dpdt: 5.73841729147549e+16,
   dpdr: 1.1773559024964984e+18,
   dedt: 13444158.983137527,
   dedr: 105182091.4988295,
   dhdt: 20319476.183761463,
    dhdr: 140520642.1170612,
   dsdt: 0.02047740372903058,
   dsdr: -0.0008237460646059265,
   dpde: 4268334894.4868603,
   dpdr_e : 7.284035110769347e+17,
    cv: 13444158.983137527,
    cp: 13470518.44019436,
   xne : 2.315793919641922e+33,
   xnp : 0.0,
   eta: 133.98527882572262,
   pele: 7.464603358528272e+27,
   ppos : 0.0,
   mu: 1.668408683623596e-257,
   mu_e : 2.1704533426048394,
```

```
y_e : 0.46073323962811563,
    dedx : array([ 4.47058940e+18, 4.09184168e+17, 2.82554706e+17, -4.36864735e+17,
       -8.13759969e+16, 2.74112742e+17, 2.68484765e+17, 1.33695616e+17,
       2.64464783e+17, 1.47456812e+17, 2.61449795e+17]),
    dpdx : array([ 1.33454960e+28, 1.23271936e+27, 8.37705760e+26, -1.29517292e+27,
       -2.41900702e+26, 8.11371520e+26, 7.93815360e+26, 3.93961115e+26,
       7.81275246e+26, 4.34228656e+26, 7.71870160e+26]),
    dhdx: array([4.47671966e+18, 4.09750419e+17, 2.82939506e+17, -4.37459674e+17,
      -8.14871141e+16, 2.74485446e+17, 2.68849405e+17, 1.33876583e+17,
       2.64823662e+17, 1.47656275e+17, 2.61804354e+17]),
    gam1: 1.336872341929589,
    cs: 1086123519.6557314,
    abar: 17.391348207658748,
   zbar: 8.012772201215236,
   dpda: -5.650331154459965e+26,
   dpdz: 1.211260000488575e+27,
   deda: -1.905857130636209e+17,
   dedz: 4.088110181833375e+17,
   conductivity : 4.11e-321}
Energy generation rate: -1.613892258e+07
omegadot = [ 3.75545872e-17 -8.53397992e-17 -2.17418042e-15 2.49670318e-11
  2.70445944e-12 -2.76708202e-11 1.34570727e-17 0.00000000e+00
  3.73360052e-16 1.16419220e-15 1.57042055e-23]
cp = 1.34705e+07
dpdt = 5.73842e+16
-2.41900702e+26 8.11371520e+26 7.93815360e+26 3.93961115e+26
 7.81275246e+26 4.34228656e+26 7.71870160e+26]
dhdx = \begin{bmatrix} 4.47671966e+18 & 4.09750419e+17 & 2.82939506e+17 & -4.37459674e+17 \end{bmatrix}
-8.14871141e+16 2.74485446e+17 2.68849405e+17 1.33876583e+17
 2.64823662e+17 1.47656275e+17 2.61804354e+17]
cp * dpdx/dpdt = [ 3.13275840e+18 2.89371931e+17 1.96645352e+17 -3.04032451e+17
-5.67844354e+16 1.90463580e+17 1.86342399e+17 9.24795147e+16
  1.83398698e+17 1.01932028e+17 1.81190922e+17]
cp * dpdx/dpdt * wdot = -1.301478750e+07
dhdx = \begin{bmatrix} 4.47671966e+18 & 4.09750419e+17 & 2.82939506e+17 & -4.37459674e+17 \end{bmatrix}
-8.14871141e+16 2.74485446e+17 2.68849405e+17 1.33876583e+17
  2.64823662e+17 1.47656275e+17 2.61804354e+17]
dhdx * wdot = -1.873789321e+07
dHcompdx = [-1.34396126e+18 -1.20378488e+17 -8.62941542e+16 1.33427223e+17]
 2.47026787e+16 -8.40218653e+16 -8.25070060e+16 -4.13970679e+16
 -8.14249637e+16 -4.57242475e+16 -8.06134319e+16]
Composition energy generation: 5.723105706e+06
dedx = \begin{bmatrix} 4.47058940e+18 & 4.09184168e+17 & 2.82554706e+17 & -4.36864735e+17 \end{bmatrix}
 -8.13759969e+16 2.74112742e+17 2.68484765e+17 1.33695616e+17
  2.64464783e+17 1.47456812e+17 2.61449795e+17]
eps_nuc_eos = dedx * wdot (cf. MESA) = 1.871242553e+07
dabar/dt = 1.048602276e-14
```

$$\label{eq:dzbar/dt} \begin{split} \text{dzbar/dt} &= -4.576791284e{-}11\\ \text{sum omegadot} &= -4.7384837197298319e{-}27\\ \text{sum X} &= 9.9999953733623126e{-}01\\ \text{Hnuc} &+ \text{Hcomp (Maestro): } -1.041581688e{+}07 \end{split}$$