



THIRD EDITION

Image and Video Compression for
**MULTIMEDIA
ENGINEERING**

FUNDAMENTALS, ALGORITHMS, AND STANDARDS

Yun-Qing Shi and Huifang Sun



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Fundamentals, Algorithms, and Standards
Third Edition

Yun-Qing Shi and Huifang Sun



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and

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Preface to the Third Edition

When looking at the prefaces of the first and second editions of this book published in 1999 and 2008, respectively, it is observed that the most of analyses, discussion and estimation made there are still correct. The image and video compression as well as audio compression continue to play an important role in multimedia engineering. The trend of switching from analog to digital communications continues. Digital image and video, digital multimedia, Internet, world wide web (WWW) have been continuously and vigorously growing in the past 10 years. Therefore, in this third edition of the book, we have kept the most of material in the second edition with some new additions. Some major changes we have made are listed as follows.

First, in this book's third edition, one chapter has been added (new [Chapter 7](#)), which briefly introduces the digital watermarking technology. Furthermore, the so-called reversible data hiding and information forensics have been briefly introduced.

Second, two new chapters describing the recently developed video coding standard, HEVC/H.265 ([Chapter 22](#)) and IVC ([Chapter 23](#)) are added into the third edition. New [Chapter 22](#) introduces HEVC/H.265 which is the video coding standard, and has greatly improved the coding efficiency compared with currently existing video coding standards. In the new [Chapter 23](#) an MPEG royalty free video coding standards has been introduced, which is used for applications of internet video transmission. Third, for the previous [Chapter 21](#) covering the system part of MPEG, multiplexing/demultiplexing and synchronizing the coded audio, video and other data has been changed as [Chapter 24](#) in this new addition. Since we have added two new MPEG Transport standards: MPEG media transport (MMT) and MPEG DASH (Dynamic Adaptive Streaming over HTTP) into this chapter, we change the title of this chapter to MPEG Transportation Standards.

For the rest of this new edition, we just made some minor changes and, of course, we reorganized the chapter orders.



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Yun-Qing Shi and Huifang Sun

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Part I

Fundamentals



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1

Introduction

Image and video data compression¹ refers to a process in which the amount of data used to represent image and video is reduced to meet a bit rate requirement (below or at most equal to the maximum available bit rate), while the quality of the reconstructed image or video satisfies a requirement for a certain application and the complexity of computation involved is affordable for the application. The block diagram in [Figure 1.1](#) shows the functionality of image and video data compression in visual transmission and storage. Image and video data compression has been found to be necessary in these important applications, because the huge amount of data involved in these and other applications usually well-exceeds the capability of today's hardware despite rapid advancements in the semiconductor, computer, and other industries.

It is noted that information and data are two closely related yet different concepts. Data represents information and the quantity of data can be measured. In the context of digital image and video, data is usually measured in the number of binary units (bits). Information is defined as knowledge, facts, and news according to the Cambridge International Dictionary of English. That is, while data is the *representation* of knowledge, facts and news, information *is* the knowledge, facts, and news. Information, however, may also be quantitatively measured.

Bit rate (also known as coding rate), as an important parameter in image and video compression, is often expressed in a unit of bits per second (bits/sec, or simply bps), which is suitable in visual communication. In fact, an example in [Section 1.1](#) concerning videphony (a case of visual transmission) uses bit rate in terms of bps. In the application of image storage, bit rate is usually expressed in a unit of bits per pixel (bpp). The term pixel is an abbreviation for picture element and is sometimes referred to as pel. In information source coding, bit rate is sometimes expressed in a unit of bits per symbol. In [Section 1.4.2](#), when discussing noiseless source coding theorem, we consider bit rate as the average length of codewords in the unit of bits per symbol.

The required quality of the reconstructed image and video is application-dependent. In medical diagnosis and some scientific measurements, we may need the reconstructed image and video to mirror the original image and video. In other words, only reversible, information-preserving schemes are allowed. This type of compression is referred to as lossless compression. In applications such as motion picture and television (TV), a certain amount of information loss is allowed. This type of compression is called lossy compression.

From its definition, one can see that image and video data compression involves several fundamental concepts including information, data, visual quality of image and video, and computational complexity. This chapter is concerned with several fundamental concepts

¹ In this book, the terms image and video data compression, image and video compression, and image and video coding are synonymous.

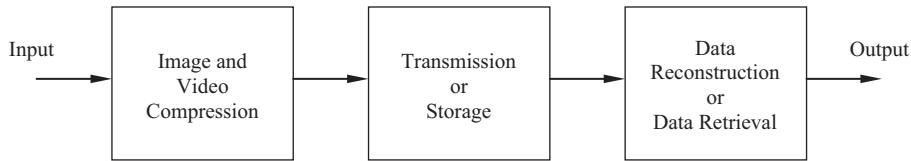


FIGURE 1.1
Image and video compression for visual transmission and storage.

in image and video compression. First, the necessity as well as the feasibility of image and video data compression are discussed. The discussion includes the utilization of several types of redundancy inherent in image and video data, and the visual perception of the human visual system (HVS). Since the quality of the reconstructed image and video is one of our main concerns, the subjective and objective measures of visual quality are addressed. Then we present some fundamental information theory results, considering they play a key role in image and video compression.

1.1 Practical Needs for Image and Video Compression

Needless to say, visual information is of vital importance for human beings to perceive, recognize, and understand the surrounding world. With the tremendous progress that has been made in advanced technologies, particularly in very large-scale integrated (VLSI) circuits and increasingly powerful computers and computations, it is becoming more possible than ever for video to be widely utilized in our daily life. Examples include videophony, videoconferencing, high-definition TV (HDTV), and digital video disk (also known as digital versatile disk (DVD)), to name a few.

Video as a sequence of video frames, however, involves a huge amount of data. Let us take a look at an illustrative example. Assume the present switch telephone network (PSTN) modem can operate at a maximum bit rate of 56,600 bps. Assume each video frame has a resolution of 288 by 352 (288 lines and 352 pixels per line), which is comparable with that of a normal TV picture and is referred to as common intermediate format (CIF). Each of the three primary colors of red, green, and blue (RGB) is represented for one pixel with eight bits, as usual, and the frame rate in transmission is 30 frames per second to provide a continuous motion video. The required bit rate, then, is $288 \times 352 \times 8 \times 3 \times 30 = 72990720$ bps. Therefore, the ratio between the required bit rate and the largest possible bit rate is about 1289. This implies that we have to compress the video data by at least 1289 times in order to accomplish the transmission described in this example. Note that an audio signal has not been accounted for yet in this illustration.

With increasingly demanding video services such as 3-D movies and 3-D games, and high video quality such as HDTV, advanced image and video data compression is necessary. It becomes an enabling technology to bridge the gap between the required huge amount of video data and the limited hardware capability.

1.2 Feasibility of Image and Video Compression

In this section, we shall see that image and video compression is not only a necessity for rapid growth of digital visual communications, but it is also feasible. Its feasibility rests with two types of redundancies, i.e., statistical redundancy and psycho-visual redundancy. By eliminating these redundancies, we can achieve image and video compression.

1.2.1 Statistical Redundancy

Statistical redundancy can be classified into two types: interpixel redundancy and coding redundancy. By interpixel redundancy we mean that pixels of an image frame, and pixels of a group of successive image or video frames, are not statistically independent. On the contrary, they are correlated to various degrees. (Note that the difference and relationship between image and video sequences are discussed in [Chapter 10](#), when we begin to discuss video compression.) This type of interpixel correlation is referred to as interpixel redundancy. Interpixel redundancy can be divided into two categories: spatial redundancy and temporal redundancy. By coding redundancy, we mean the statistical redundancy associated with coding techniques.

1.2.1.1 Spatial Redundancy

Spatial redundancy represents the statistical correlation between pixels within an image frame. Hence, it is also called intraframe redundancy.

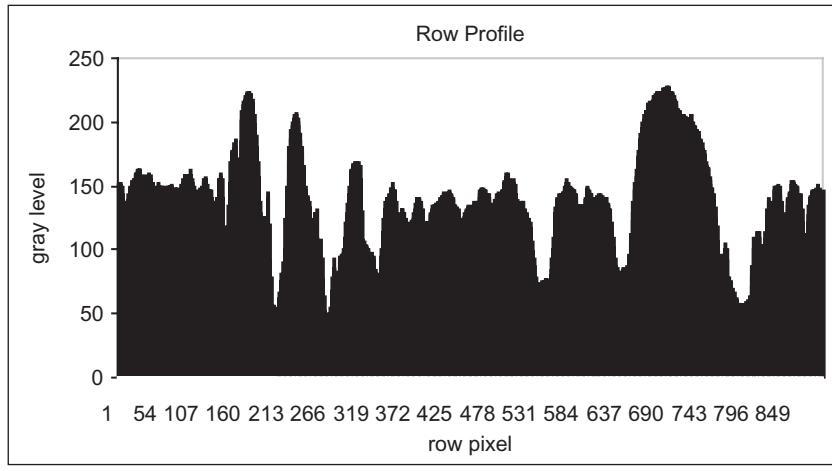
It is well known that for most properly sampled TV signals the normalized autocorrelation coefficients along a row (or a column) with a one-pixel shift are very close to the maximum value 1. That is, the intensity values of pixels along a row (or a column) have a very high autocorrelation (close to the maximum autocorrelation) with those of pixels along the same row (or the same column) but shifted by a pixel. This does not come as a surprise because most of the intensity values change continuously from pixel to pixel within an image frame except for the edge regions. This is demonstrated in [Figure 1.2](#). [Figure 1.2a](#) is a pretty normal picture—a boy and a girl in a park—and is of a resolution of 883 by 710. The intensity profiles along the 318th row and the 262th column are depicted in [Figure 1.2b](#) and [c](#), respectively. For easy reference, the positions of the 318th row and 262th column in the picture are shown in [Figure 1.2d](#). That is, the vertical axis represents intensity values, while the horizontal axis indicates the pixel position within the row or the column. These two curves indicate that often intensity values change gradually from one pixel to the other along a row and along a column.

The study of the statistical properties of video signals can be traced back to the 1950s. Knowing that we must study and understand redundancy in order to remove redundancy, Kretzmer designed some experimental devices such as a picture autocorrelator and a probiloscope to measure several statistical quantities of TV signals and published his outstanding work in Kretzmer (1952). He found that the autocorrelation in both horizontal and vertical directions exhibits similar behaviors as shown in [Figure 1.3](#). Autocorrelation functions of several pictures with different complexity were measured.

It was found that from picture to picture, the shape of autocorrelation curves ranges from remarkably linear to somewhat like exponential. The central symmetry with respect to the vertical axis and the bell-shaped distribution, however, remains generally the same. When the pixel shifting becomes small, it was found that the autocorrelation is high. This “local” autocorrelation can be as high as 0.97–0.99 for one- or two-pixel shifting. For very detailed pictures, it can be from 0.43 to 0.75. It was also found that autocorrelation generally has no preferred direction.



(a)

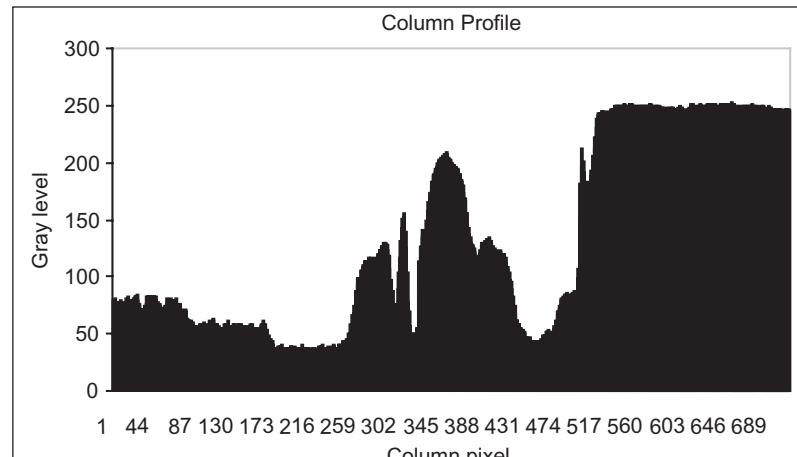


(b)

FIGURE 1.2

(a) A picture of “Boy and Girl,” (b) Intensity profile along 318th row.

(Continued)



(c)

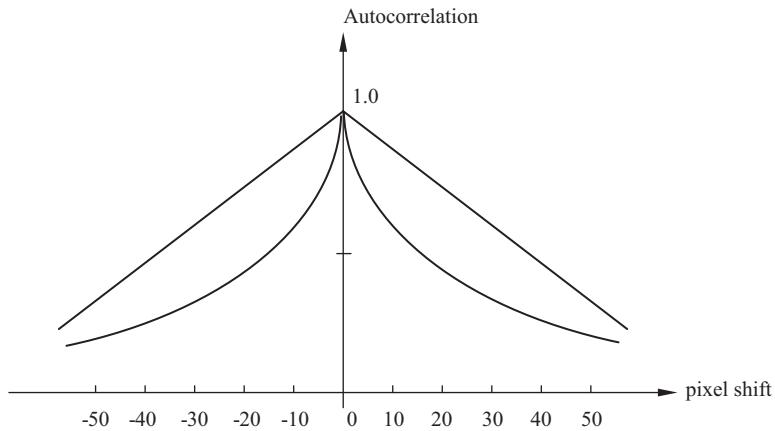


(d)

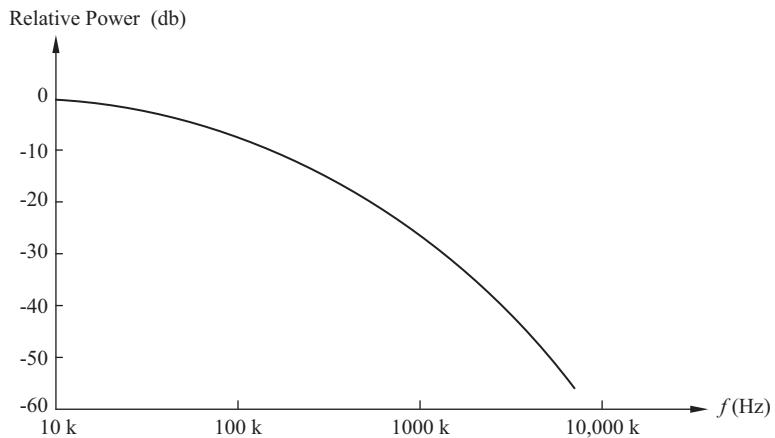
FIGURE 1.2 (Continued)

(c) Intensity profile along 262th column, (d) Positions of 318th row and 262th column.

The Fourier transform of autocorrelation, power spectrum, is known as another important function in studying statistical behavior. [Figure 1.4](#) shows a typical power spectrum of a TV signal (Fink 1957, Connor et al. 1972). It is reported that the spectrum is quite flat until 30 kHz for a broadcast TV signal. Beyond this line frequency the spectrum starts to drop at a rate of around 6 dB per octave. This reveals the heavy concentration of video signals in low frequencies, considering a nominal bandwidth of 5 MHz.

**FIGURE 1.3**

Autocorrelation in horizontal directions for some testing pictures. (From Kretzmer, E.R., *Bell Syst. Tech. J.*, 31, 751–763, 1952.)

**FIGURE 1.4**

A typical power spectrum of a TV broadcast signal. (From Fink, D.G., *Television Engineering Handbook*, McGraw-Hill, New York, 1957.)

Spatial redundancy implies that the intensity value of a pixel can be guessed from that of its neighboring pixels. In other words, it is not necessary to represent each pixel in an image frame independently. Instead, one can predict a pixel from its neighbors. Predictive coding, also known as differential coding, is based on this observation and is discussed in [Chapter 3](#). The direct consequence of recognition of spatial redundancy is that by removing a large amount of the redundancy (or utilizing the high correlation) within an image frame, we may save a lot of data in representing the frame, thus achieving data compression.

1.2.1.2 Temporal Redundancy

Temporal redundancy is concerned with the statistical correlation between pixels from successive frames in a temporal image or video sequence. Therefore, it is also called inter-frame redundancy.



FIGURE 1.5
(a) 21st frame and (b) 22nd frame of the “Miss America” sequence.

Consider a temporal image sequence. That is, a camera is fixed in the 3-D world and it takes pictures of the scene one by one as time goes by. As long as the time interval between two consecutive pictures is short enough, i.e., the pictures are taken densely enough, we can imagine that the similarity between two neighboring frames is strong. [Figure 1.5a](#) and [b](#) show, respectively, the 21st and 22nd frames of the “Miss America” sequence. The frames have a resolution of 176 by 144. Among the total of 25,344 pixels, only 3.4% change their gray value more than 1% of the maximum gray value (255 in this case) from the 21st frame to the 22nd frame. This confirms an observation made in Mounts (1969): For a videophone-like signal with moderate motion in the scene, on average, less than 10% of pixels change their gray values between two consecutive frames by an amount of 1% of the peak signal. The high interframe correlation was reported in Kretzmer (1952). There, the autocorrelation between two adjacent frames was measured for two typical motion-picture films. The measured autocorrelations are 0.80 and 0.86. In summary, pixels within successive frames usually bear a strong similarity or correlation. As a result, we may predict a frame from its neighboring frames along the temporal dimension. This is referred to as interframe predictive coding and is discussed in [Chapter 3](#). A more precise, hence, more efficient interframe predictive coding scheme, which has been in development since the 1980s, uses motion analysis. That is, it considers that the changes from one frame to the next are mainly due to the motion of some objects in the frame. Taking this motion information into consideration, we refer to the method as motion-compensated predictive coding. Both interframe correlation and motion-compensated predictive coding are covered in detail in [Chapter 10](#).

Removing a large amount of temporal redundancy leads to a great deal of data compression. At present, all the international video coding standards have adopted motion-compensated predictive coding, which has been a vital factor to the increased use of digital video in digital media.

1.2.1.3 Coding Redundancy

As we discussed, interpixel redundancy is concerned with the correlation between pixels. That is, some information associated with pixels is redundant. The psychovisual redundancy, which is discussed in the next subsection, is related to the information that is

TABLE 1.1
An Illustrative Example

| Symbol | Occurrence Probability | Code 1 | Code 2 |
|--------|------------------------|--------|--------|
| a_1 | 0.1 | 000 | 0000 |
| a_2 | 0.2 | 001 | 01 |
| a_3 | 0.5 | 010 | 1 |
| a_4 | 0.05 | 011 | 0001 |
| a_5 | 0.15 | 100 | 001 |

psychovisually redundant, i.e., to which the HVS is not sensitive. It is hence clear that both the interpixel and psychovisual redundancies are somehow associated with some information contained in image and video. Eliminating these redundancies, or utilizing these correlations, by using fewer bits to represent the information results in image and video data compression. In this sense, the coding redundancy is different. It has nothing to do with information redundancy but with the representation of information, i.e., coding itself. To see this, let us take a look at the following example.

One illustrative example is provided in [Table 1.1](#). The first column lists five distinct symbols that need to be encoded. The second column contains occurrence probabilities of these five symbols. The third column lists code 1, a set of codewords obtained by using uniform-length codeword assignment. (This code is known as the natural binary code.) The fourth column shows code 2, in which each codeword has a variable length. Therefore, code 2 is called the variable-length code. It is noted that the symbol with a higher occurrence probability is encoded with a shorter length. Let us examine the efficiency of the two different codes. That is, we will examine which one provides a shorter average length of codewords. It is obvious that the average length of codewords in code 1, $L_{avg,1}$, is three bits. The average length of codewords in code 2, $L_{avg,2}$, can be calculated as follows.

$$L_{avg,2} = 4 \times 0.1 + 2 \times 0.2 + 1 \times 0.5 + 4 \times 0.05 + 3 \times 0.15 = 1.95 \quad \text{bits/symbol.} \quad (1.1)$$

Therefore, it is concluded that code 2 with variable-length coding is more efficient than code 1 with natural binary coding.

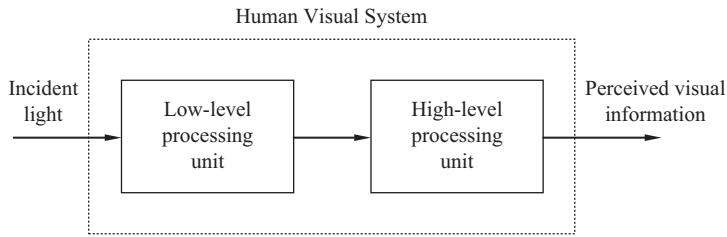
From this example, we can see that for the same set of symbols, different codes may perform differently. Some may be more efficient than others. For the same amount of information, code 1 contains some redundancy. That is, some data in code 1 is not necessary and can be removed without any effect. Huffman coding and arithmetic coding, two variable-length coding techniques, will be discussed in [Chapter 5](#).

From the study of coding redundancy, it is clear that we should search for more efficient coding techniques in order to compress image and video data.

1.2.2 Psychovisual Redundancy

While interpixel redundancy inherently rests in image and video data, psychovisual redundancy originates from the characteristics of the HVS.

It is known that the HVS perceives the outside world in a rather complicated way. Its response to visual stimuli is not a linear function of the strength of some physical attributes of the stimuli such as intensity and color. HVS perception is different from camera sensing.

**FIGURE 1.6**

A two-unit cascade model of the HVS.

In the VHS, visual information is not perceived equally; some information may be more important than other information. This implies that if we apply less data to represent less important visual information, perception will not be affected. In this sense, we see that some visual information is psychovisually redundant. Eliminating this type of psychovisual redundancy leads to data compression.

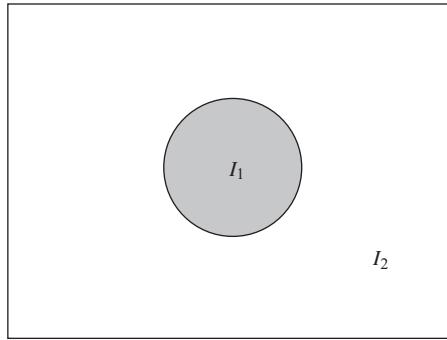
In order to understand this type of redundancy, let us study some properties of the HVS.

We may model the human vision system as a cascade of two units (Lim 1990), as depicted in Figure 1.6. The first one is a low-level processing unit, which converts incident light into a neural signal. The second one is a high-level processing unit, which extracts information from the neural signal. While much research has been carried out to investigate low-level processing, high-level processing remains wide open. The low-level processing unit is known as a nonlinear system (approximately logarithmic, as shown below). While a great body of literature exists, we will limit our discussion only to video compression-related results. That is, several aspects of the HVS, which are closely related to image and video compression, are discussed in this subsection. They are luminance masking, texture masking, frequency masking, temporal masking, and color masking. Their relevance in image and video compression is addressed. Finally, a summary is provided, in which it is pointed out that all of these features can be unified as one: differential sensitivity. This seems to be the most important feature of the human visual perception.

1.2.2.1 Luminance Masking

Luminance masking concerns the brightness perception of the HVS, which is the most fundamental aspect among the five to be discussed here. Luminance masking is also referred to as *luminance dependence* (Connor et al. 1972) and *contrast masking* (Legge and Foley 1980, Watson 1987). As pointed out in Legge and Foley (1980), the term *masking* usually refers to a destructive interaction or interference among stimuli that are closely coupled in time or space. This may result in a failure in detection or errors in recognition. Here, we are mainly concerned with the detectability of one stimulus when another stimulus is present simultaneously. The effect of one stimulus on the detectability of another, however, does not have to decrease detectability. Indeed, there are some cases in which a low-contrast masker increases the detectability of a signal. This is sometimes referred to as *facilitation*, but in this discussion, we only use the term masking.

Consider the monochrome image shown in Figure 1.7. There, a uniform disk-shaped object with a gray level (intensity value) I_1 is imposed on a uniform background with a gray level I_2 . Now the question is: Under what circumstances can the disk-shaped object be discriminated from the background by the HVS? That is, we want to study the effect of one stimulus

**FIGURE 1.7**

A uniform object with gray level I_1 imposed on a uniform background with gray level I_2 .

(the background in this example, the masker) on the detectability of another stimulus (in this example, the disk). Two extreme cases are obvious. That is, if the difference between the two gray levels is quite large, the HVS has no problem with discrimination, or in other words the HVS notices the object from the background. If, on the other hand, the two gray levels are the same, the HVS cannot identify the existence of the object. What we are concerned with here is the critical threshold in the gray level difference for discrimination to take place.

If we define the threshold ΔI as such a gray level difference $\Delta I = I_1 - I_2$ that the object can be noticed by the HVS with a 50% chance, then we have the following relation, known as *contrast sensitivity function*, according to Weber's law.

$$\frac{\Delta I}{I} \approx \text{constant}, \quad (1.2)$$

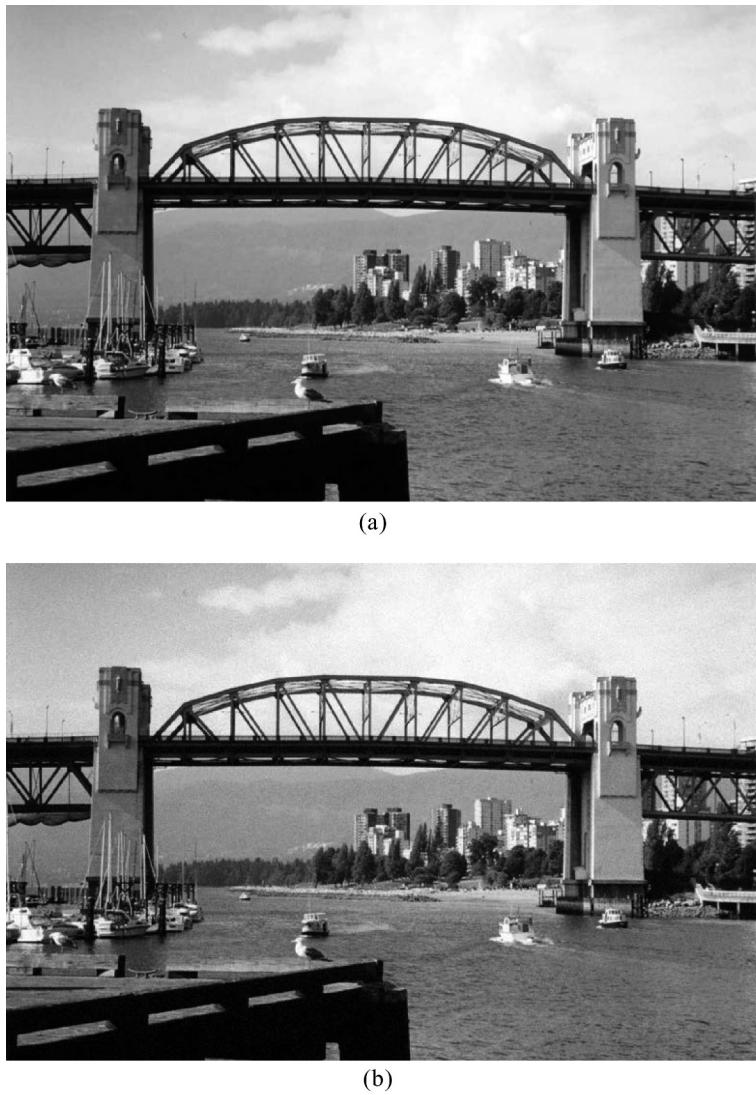
where the constant is about 0.02. Weber's law states that for a relatively very wide range of I , the threshold for discrimination, ΔI , is directly proportional to the intensity I . The implication of this result is that when the background is bright, a larger difference in gray levels is needed for the HVS to discriminate the object from the background. On the other hand, the intensity difference required could be smaller if the background is relatively dark. It is noted that Equation 1.1 implies a logarithmic response of the HVS, and Weber's law holds for all other human senses as well.

Further research has indicated that the luminance threshold ΔI increases more slowly than predicted by Weber's law. Some more accurate contrast sensitivity functions have been presented in the literature. In Legge and Foley (1980), it was reported that an exponential function replaces the linear relation in Weber's law. The following exponential expression is reported in Watson (1987).

$$\Delta I = I_0 \cdot \max \left\{ 1, \left(\frac{I}{I_0} \right)^\alpha \right\}, \quad (1.3)$$

where I_0 is the luminance detection threshold when the gray level of the background is equal to zero, i.e., $I = 0$, and α is a constant, approximately equal to 0.7.

[Figure 1.8](#) shows a picture uniformly corrupted by additive white Gaussian noise (AWGN). It can be observed that the noise is more visible in the dark area than in the bright area if comparing, for instance, the dark portion and the bright portion of the cloud above the bridge.

**FIGURE 1.8**

The bridge in Vancouver: (a) Original (Courtesy of Minhuai Shi) and (b) Uniformly corrupted by AWGN.

This indicates that the noise filtering is more necessary in the dark area than in the bright area. The lighter area can accommodate more additive noise before the noise becomes visible. This property has found application in embedding digital watermarks (Huang and Shi 1998).

The direct impact that luminance masking has on image and video compression is related to quantization, which is covered in detail in the next chapter. Roughly speaking, quantization is a process that converts a continuously distributed quantity into a set of finitely many distinct quantities. The number of these distinct quantities (known as quantization levels) is one of the keys in quantizer design. It significantly influences the resulting bit rate and the quality of the reconstructed image and video. An effective quantizer should be able to minimize the visibility of quantization error. The contrast sensitivity function provides a guideline in analysis of the visibility of quantization error. Therefore,

it can be applied to quantizer design. Luminance masking suggests a nonuniform quantization scheme that takes the contrast sensitivity function into consideration. One such example was presented in Watson (1987).

1.2.2.2 Texture Masking

Texture masking is sometimes also called *detail dependence* (Connor et al. 1972), *spatial masking* (Netravali and Prasada 1977, Lim 1990), or *activity masking*. It states that the discrimination threshold increases with increasing picture detail. That is, the stronger the texture, the larger the discrimination threshold. In [Figure 1.8](#), it can be observed that the additive random noise is less pronounced in the strong texture area than in the smooth area if comparing, for instance, the dark portion of the cloud (the top-right corner of the picture) with the water area (the bottom-right corner of the picture). This is in confirmation of texture masking.

In [Figure 1.9b](#), the number of quantization levels decreases from 256 (as in [Figure 1.9a](#)) to 16. That is, we use only four bits, instead of eight bits, to represent the intensity value for each pixel. The unnatural contours, caused by coarse quantization, can be noticed in the relative uniform regions, compared with [Figure 1.9a](#). This phenomenon was first noted in Goodall (1951) and is called *false contouring* (Gonzalez and Woods 1992). Now we see that the false contouring can be explained by using texture masking since texture masking indicates that the human eye is more sensitive to the smooth region than to the textured region, where intensity exhibits a high variation. A direct impact on image and video compression is that the number of quantization levels, which affects bit rate significantly, should be adapted according to the intensity variation of image regions.

1.2.2.3 Frequency Masking

While the above two characteristics are picture-dependent in nature, frequency masking is picture-independent. It states that the discrimination threshold increases with frequency increase. It is also referred to as *frequency dependence*.

Frequency masking can be well illustrated by using [Figure 1.9](#), which was just referred to in the previous section. In [Figure 1.9c](#), high-frequency random noise has been added to the original image before quantization. This method is referred to as the improved gray-scale (IGS) quantization (Gonzalez and Woods 1992, p. 318). With the same number of quantization levels (16) as in [Figure 1.9b](#), the picture quality of [Figure 1.9c](#) is improved dramatically compared with that of [Figure 1.9b](#): the annoying false contours have disappeared despite the increase of the root mean square value of the total noise in [Figure 1.9c](#). This is due to the fact that the low-frequency quantization error is converted to the high-frequency noise, and that the HVS is less sensitive to the high-frequency content. We thus see, as pointed out in Connor et al. (1972), that our human eyes function like a low-pass filter.

Owing to frequency masking, in the transform domain, say, the discrete cosine transform (DCT) domain, we can drop some high-frequency coefficients with small magnitudes to achieve data compression without noticeably affecting the perception of the HVS. This leads to what is called transform coding, which is discussed in [Chapter 4](#).

1.2.2.4 Temporal Masking

Temporal masking is another picture-independent feature of the HVS. It states that it takes a while for the HVS to adapt itself to the scene when the scene changes abruptly. During this transition, the HVS is not sensitive to details. The masking takes place both before and



(a)



(b)



(c)

FIGURE 1.9

Christmas in Winorlia (a) Original, (b) Four-bit quantized, and (c) Improved IGS quantized with four bits.

after the abrupt change. It is called forward temporal masking if it happens after the scene change. Otherwise, it is referred to backward temporal masking.

This implies that one should take temporal masking into consideration when allocating data in image and video coding.

1.2.2.5 Color Masking

Digital color image processing is gaining increasing popularity due to the wide application of color images in modern life. As mentioned at the beginning of the discussion about psychovisual redundancy, we are not going to cover all aspects of the perception of the HVS. Instead, we cover only those aspects related to psychovisual redundancy, thus to image and video compression. Therefore, our discussion here on color perception is by no means exhaustive.

In physics, it is known that any visible light corresponds to an electromagnetic spectral distribution. Therefore, a color, as a sensation of visible light, is an energy with an intensity as well as a set of wavelengths associated with the electromagnetic spectrum. Obviously, intensity is an attribute of visible light. The composition of wavelengths is another attribute: chrominance. There are two elements in the chrominance attribute: *hue* and *saturation*. The hue of a color is characterized by the dominant wavelength in the composition. Saturation is a measure of the purity of a color. A pure color has a saturation of 100%, whereas white light has a saturation of 0.

1.2.2.5.1 RGB Model

The RGB primary color system is the most well-known among several color systems. This is due to the following feature of the human perception of color. The color-sensitive area in the HVS consists of three different sets of cones and each set is sensitive to the light of one of the three RGB primary colors. Consequently, any color sensed by the HVS can be considered as a particular linear combination of the three primary colors. Many research results are available, the Commission Internationale de l'Eclairage (C.I.E.) chromaticity diagram being a well-known example. These results can be easily found in many classic optics and digital image processing texts.

The RGB model is used mainly in color image acquisition and display. In color signal processing including image and video compression, however, the luminance-chrominance color system is more efficient and, hence, widely used. This has something to do with the color perception of the HVS. It is known that the HVS is more sensitive to green than to red, and is least sensitive to blue. An equal representation of red, green, and blue leads to inefficient data representation when the HVS is the ultimate viewer. Allocating data only to the information that the HVS can perceive, on the other hand, can make video coding more efficient.

Luminance is concerned with the perceived brightness, while chrominance is related to the perception of hue and saturation of color. That is, roughly speaking, the luminance-chrominance representation agrees more with the color perception of the HVS. This feature makes the luminance-chrominance color models more suitable for color image processing. A good example was presented in Gonzalez and Woods (1992), about histogram equalization. It is well-known that applying histogram equalization can bring out some details originally in dark regions. Applying histogram equalization to the RGB components separately can certainly achieve the goal. In doing so, however, the chrominance elements of hue and saturation have been changed, thus leading to color distortion. With a luminance-chrominance model, histogram equalization can be applied to the luminance

component only. Hence, the details in the dark regions are brought out, whereas the chrominance elements remain unchanged, hence no color distortion. With the luminance component Y serving as a black-and-white signal, a luminance-chrominance color model offers compatibility with black-and-white TV systems. This is another merit of luminance-chrominance color models.

To be discussed next are several different luminance-chrominance color models: HSI, YUV, YCbCr, and YIQ.

1.2.2.5.2 Gamma-Correction

It is known that a nonlinear relationship (basically a power function) exists between electrical signal magnitude and light intensity for both cameras and CRT-based display monitors. That is, the light intensity is a linear function of the signal voltage raised to the power of γ . It is a common practice to correct this non-linearity before transmission. This is referred to as gamma-correction. The gamma-corrected RGB components are denoted by R' , G' , and B' , respectively. They are used in the discussion on various color models. For the sake of notational brevity, we simply use R , G , and B instead of R' , G' , and B' in the following discussion, while keeping the gamma-correction in mind.

1.2.2.5.3 HSI Model

In this model, I stands for the intensity component, H for the hue component, and S for saturation. One merit of this color system is that the intensity component is decoupled from the chromatic components. As analyzed above, this decoupling usually facilitates color image processing tasks. Another merit is that this model is closely related to the way the HVS perceives color pictures. Its main drawback is the complicated conversion between RGB and HSI models. A detailed derivation of the conversion may be found in Gonzalez and Woods (1992). Because of this complexity, the HSI model is not used in any TV systems.

1.2.2.5.4 YUV Model

In this model, Y denotes the luminance component, and U and V are the two chrominance components. The luminance Y can be determined from the RGB model via the following relation.

$$Y = 0.299R + 0.587G + 0.114B. \quad (1.4)$$

It is noted that the three weights associated with the three primary colors— R , G , and B —are not the same. Their different magnitudes reflect different responses of the HVS to different primary colors.

Instead of being directly related to hue and saturation, the other two chrominance components, U and V , are defined as color differences as follows.

$$U = 0.492(B - Y), \quad (1.5)$$

and

$$V = 0.877(R - Y). \quad (1.6)$$

In this way, the YUV model lowers computational complexity. It has been used in phase alternating line (PAL) TV systems. Note that PAL is an analog composite color TV standard and is used in most of the European countries, some Asian countries, and Australia.

By composite systems, we mean both the luminance and chrominance components of the TV signals are multiplexed within the same channel. For completeness, an expression of YUV in terms of RGB is listed below.

$$\begin{pmatrix} Y \\ U \\ V \end{pmatrix} = \begin{pmatrix} 0.299 & 0.587 & 0.114 \\ -0.147 & -0.289 & 0.436 \\ 0.615 & -0.515 & -0.100 \end{pmatrix} \begin{pmatrix} R \\ G \\ B \end{pmatrix} \quad (1.7)$$

1.2.2.5.5 YIQ Model

This color space has been utilized in National Television Systems Committee (NTSC) TV systems for years. Note that NTSC is an analog composite color TV standard and is used in North America and Japan. The Y component is still the luminance. The two chrominance components are the linear transformation of the U and V components defined in the YUV model. Specifically,

$$I = -0.545U + 0.839V, \quad (1.8)$$

and

$$Q = 0.839U + 0.545V. \quad (1.9)$$

Substituting the U and V expressed in Equations 1.4 and 1.5 into the above two equations, we can express YIQ directly in terms of RGB. That is,

$$\begin{pmatrix} Y \\ I \\ Q \end{pmatrix} = \begin{pmatrix} 0.299 & 0.587 & 0.114 \\ 0.596 & -0.275 & -0.321 \\ 0.212 & -0.523 & 0.311 \end{pmatrix} \begin{pmatrix} R \\ G \\ B \end{pmatrix} \quad (1.10)$$

1.2.2.5.6 YDbDr Model

The YDbDr model is used in the Sequential Couleur a Memoire (SECAM) TV system. Note that SECAM is used in France, Russia, and some Eastern European countries. The relationship between YDbDr and RGB appears below.

$$\begin{pmatrix} Y \\ Db \\ Dr \end{pmatrix} = \begin{pmatrix} 0.299 & 0.587 & 0.114 \\ -0.450 & -0.883 & 1.333 \\ -1.333 & 1.116 & -0.217 \end{pmatrix} \begin{pmatrix} R \\ G \\ B \end{pmatrix} \quad (1.11)$$

That is,

$$Db = 3.059U, \quad (1.12)$$

and

$$Dr = -2.169V. \quad (1.13)$$

1.2.2.5.7 YCbCr Model

From the above, we can see that the U and V chrominance components are differences between the gamma-corrected color B and the luminance Y, and the gamma-corrected R and the luminance Y, respectively. The chrominance component pairs I and Q and Db and Dr are both linear transforms of U and V. Hence, they are very closely related to each other. It is noted that U and V may be negative as well. In order to make chrominance components nonnegative, the Y, U, and V are scaled and shifted to produce the YCbCr model, which is used in the international coding standards JPEG and MPEG. (These two standards are covered in [Chapters 7](#) and [16](#), respectively).

$$\begin{pmatrix} Y \\ Cb \\ Cr \end{pmatrix} = \begin{pmatrix} 0.257 & 0.504 & 0.098 \\ -0.148 & -0.291 & 0.439 \\ 0.439 & -0.368 & -0.071 \end{pmatrix} \begin{pmatrix} R \\ G \\ B \end{pmatrix} + \begin{pmatrix} 16 \\ 128 \\ 128 \end{pmatrix} \quad (1.14)$$

1.2.2.6 Color Masking and Its Application in Video Compression

It is well-known that the HVS is much more sensitive to the luminance component than to the chrominance components. Following (Van Ness and Bouman 1967, Mullen 1985), Mitchell, Pennebaker, Fogg, and LeGall included a figure to quantitatively illustrate the above statement. A modified version is shown in [Figure 1.10](#). There, the abscissa represents

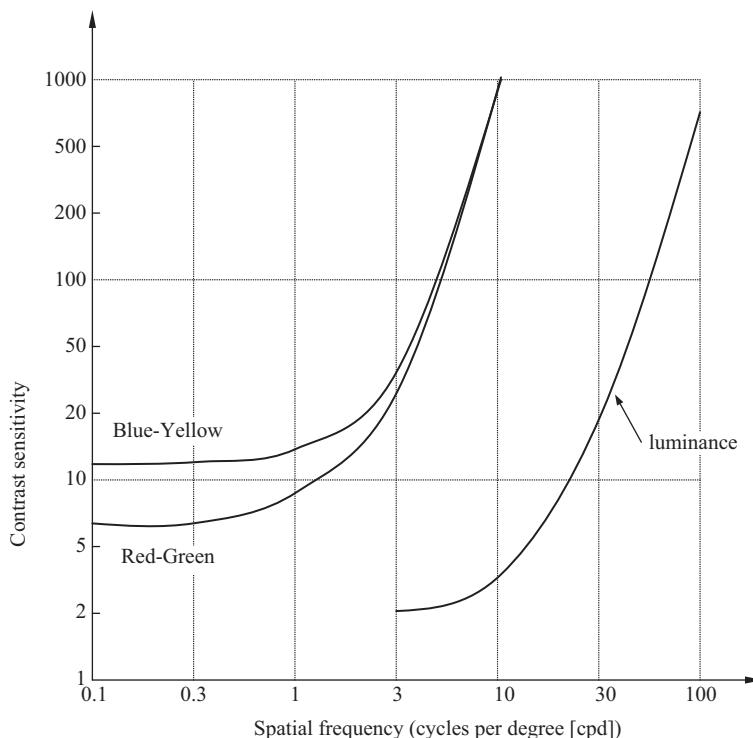


FIGURE 1.10

Contrast sensitivity versus spatial frequency. (Revised from Van Ness, F.I. and Bouman, M.A., *J. Opt. Soc. Am.*, 57, 401–406, 1967, Mullen, K.T., *J. Physiol.*, 359, 381–400, 1985.)

spatial frequency in the unit of cycles per degree (cpd), while the ordinate is the contrast sensitivity defined for the sinusoidal testing signal. Two observations are in order. First, for each of the three curves, i.e., curves for the luminance component Y and the chrominance components U and V, the contrast sensitivity increases when spatial frequency increases, in general. This agrees with frequency masking discussed previously. Second, for the same contrast sensitivity, we see that the luminance component corresponds to a much higher spatial frequency. This is an indication that the HVS is much more sensitive to luminance than to chrominance. This statement can also be confirmed, perhaps more easily, by examining those spatial frequencies at which all three curves have data available. Then we can see that the contrast sensitivity of luminance is much lower than that of the chrominance components.

The direct impact of color masking on image and video coding is that by utilizing this psychovisual feature, we can allocate more bits to the luminance component than to the chrominance components. This leads to a common practice in color image and video coding: using full resolution for the intensity component, while using a two-by-one subsampling both horizontally and vertically for the two chrominance components. This has been adopted in related international coding standards, which will be discussed in [Chapter 16](#).

1.2.2.7 Summary: Differential Sensitivity

In this subsection, we discussed luminance masking, texture masking, frequency masking, temporal masking, and color masking. Before we enter the next subsection, let us summarize what we have discussed so far.

We see that luminance masking, also known as contrast masking, is of fundamental importance among several types of masking. It states that the sensitivity of the eyes to a stimulus depends on the intensity of another stimulus. Thus, it is a differential sensitivity. Both texture (detail or activity) and frequency of another stimulus significantly influence this differential sensitivity. The same mechanism exists in color perception, where the HVS is much more sensitive to luminance than to chrominance. Therefore, we conclude that differential sensitivity is the key in studying human visual perception.

These features can be utilized to eliminate psychovisual redundancy and thus compress image and video data.

It is also noted that variable quantization, which depends on activity and luminance in different regions, seems to be reasonable from a data compression point of view. Its practical applicability, however, is somehow questionable. That is, some experimental work does not support this expectation.

It is noted that this differential sensitivity feature of the HVS is common to human perception. For instance, there is also forward and backward temporal masking in human audio perception.

1.3 Visual Quality Measurement

As the definition of image and video compression indicates, image and video quality are important factors in dealing with image and video compression. For instance, in evaluating two different compression methods, we have to base the evaluation on some definite image and video quality. When both methods achieve the same quality of reconstructed

image and video, the one that requires less data is considered to be superior to the other. Alternatively, with the same amount of data, the method providing a higher-quality reconstructed image or video is considered the better method. Note that here we have not considered other performance criteria, such as computational complexity.

Surprisingly, however, it turns out that the measurement of image and video quality is not straightforward. There are two types of visual quality assessment. One is objective assessment (using electrical measurements), and the other is subjective assessment (using human observers). Each has its merits and drawbacks. A combination of these two methods is now widely utilized in practice. In this section, we first discuss subjective visual quality measurement, followed by objective quality measurement.

1.3.1 Subjective Quality Measurement

It is natural that the visual quality of reconstructed video frames should be judged by human viewers if they are to be the ultimate receivers of the data (see [Figure 1.1](#)). Therefore, the subjective visual quality measure plays an important role in visual communications.

In subjective visual quality measurement, a set of video frames is generated with varying coding parameters. Observers are invited to subjectively evaluate the visual quality of these frames. Specifically, observers are asked to rate the pictures by giving some measure of picture quality. Alternatively, observers are requested to provide some measure of impairment to the pictures. A five-scale rating system of the degree of impairment, used by Bell Laboratories, is listed below (Sakrison 1979). It has been adopted as one of the standard scales in CCIR Recommendation 500-3 (CCIR 1986). Note that CCIR is now International Telecommunications Union-Recommendations (ITU-R).

1. Impairment is not noticeable.
2. Impairment is just noticeable.
3. Impairment is definitely noticeable, but not objectionable.
4. Impairment is objectionable.
5. Impairment is extremely objectionable.

In the subjective evaluation, there are a few things worth mentioning. In most applications there is a whole array of pictures simultaneously available for evaluation. These pictures are generated with different encoding parameters. By keeping some parameters fixed while making one parameter (or a subset of parameters) free to change, the resulting quality rating can be used to study the effect of the one parameter (or the subset of parameters) on encoding. An example using this method to study the effect of varying numbers of quantization levels on image quality can be found in Gonzalez and Woods (1992).

Another possible way to study subjective evaluation is to identify pictures with the same subjective quality measure from the whole array of pictures. From this subset of test pictures, we can produce, in the encoding parameter space, isopreference curves that can be used to study the effect of the parameter(s) under investigation. An example using this method to study the effect of varying both image resolution and numbers of quantization levels on image quality can be found in Huang (1965).

In the rating, a whole array of pictures is usually divided into columns with each column sharing some common conditions. The evaluation starts within each column with a pairwise comparison. This is because a pairwise comparison is relatively easy for the eyes. As a result, pictures in one column are arranged in an order according to visual

quality, and quality or impairment measures are then assigned to the pictures in the one column. After each column has been rated, a unification between columns is necessary. That is, different columns need to have a unified quality measurement. As pointed out in Sakrison (1979), this task is not easy since it means we may need to equate impairment that results from different types of errors.

One thing is understood from the above discussion: subjective evaluation of visual quality is costly. It needs a large number of pictures and observers. The evaluation takes a long time because human eyes are easily fatigued and bored. Some special measures have to be taken in order to arrive at an accurate subjective quality measure. Examples in this regard include averaging subjective ratings and taking their deviation into consideration. For further details on subjective visual quality measurement, readers may refer to (Sakrison 1979, Hidaka and Ozawa 1990, Webster et al. 1993).

1.3.2 Objective Quality Measurement

In this subsection, we first introduce the concept of signal-to-noise ratio (SNR), which is a popularly utilized objective quality assessment. Then we present a promising new objective visual quality assessment technique based on human visual perception.

1.3.2.1 Signal-to-Noise Ratio

Consider Figure 1.11, where $f(x, y)$ is the input image to a processing system. The system can be a low-pass filter, a subsampling system, or a compression system.

It can even represent a process in which AWGN corrupts the input image. The $g(x, y)$ is the output of the system. In evaluating the quality of $g(x, y)$, we define an error function $e(x, y)$ as the difference between the input and the output. That is,

$$e(x, y) = f(x, y) - g(x, y). \quad (1.15)$$

The mean square error is defined as E_{ms} :

$$E_{ms} = \frac{1}{MN} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} e(x, y)^2, \quad (1.16)$$

where M and N are the dimensions of the image in the horizontal and vertical directions. Note that it is sometimes denoted by MSE . The root mean square error is defined as E_{rms} :

$$E_{rms} = \sqrt{E_{ms}}. \quad (1.17)$$

It is sometimes denoted by $RMSE$.

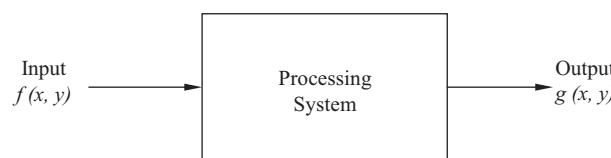


FIGURE 1.11

An image processing system.

As noted earlier, *SNR* is widely used in objective quality measurement. Depending whether mean square error or root mean square error is used, the *SNR* may be called the mean square *SNR*, SNR_{ms} , or the root mean square *SNR*, SNR_{rms} . We have

$$SNR_{ms} = 10 \log_{10} \left(\frac{\sum_{x=0}^{M-1} \sum_{y=0}^{N-1} g(x, y)^2}{MN \cdot E_{ms}} \right), \quad (1.18)$$

and

$$SNR_{rms} = \sqrt{SNR_{ms}}. \quad (1.19)$$

In image and video data compression, another closely related term, peak *SNR* (*PSNR*), which is essentially a modified version of SNR_{ms} , is widely used. It is defined as follows.

$$PSNR = 10 \log_{10} \left(\frac{255^2}{E_{ms}} \right) \quad (1.20)$$

The interpretation of the *SNR* is that the larger the *SNR* (SNR_{ms} , SNR_{rms} , or *PSNR*) the better the quality of the processed image, $g(x, y)$. That is, the closer the processed image $g(x, y)$ is to the original image $f(x, y)$. This seems correct; however, from our previous discussion about the features of the HVS, we know that the HVS does not respond to visual stimuli in a straightforward way. Its low-level processing unit is known to be nonlinear. Several masking phenomena exist. Each confirms that the visual perception of the HVS is not simple. It is worth noting that our understanding of the high-level processing unit of the HVS is far from complete. Therefore, we may understand that the *SNR* does not always provide us with reliable assessments of image quality. One good example is presented in [Section 1.2.2.3](#), which uses the IGS quantization technique to achieve high compression (using only four bits for quantization instead of the usual eight bits) without introducing noticeable false contouring. In this case, the subjective quality is high, and the *SNR* decreases due to low-frequency quantization noise and additive high-frequency random noise. Another example drawn from our discussion about the masking phenomena is that some additive noise in bright areas or in highly textured regions may be masked, while some minor artifacts in dark and uniform regions may turn out to be quite annoying. In this case, the *SNR* cannot truthfully reflect visual quality.

On the one hand, we see that the objective quality measure does not always provide reliable picture quality assessment. On the other hand, however, its implementation is much faster and easier than that of the subjective quality measure. Furthermore, objective assessment is repeatable. Owing to these merits, objective quality assessment is still widely used despite this drawback.

It is noted that combining subjective and objective assessment has been a common practice in international coding-standard activity.

1.3.2.2 An Objective Quality Measure Based on Human Visual Perception

Introduced here is a new development in visual quality assessment, which is an objective quality measurement based on human visual perception (Webster et al. 1993). Since it belongs to the category of objective assessment, it possesses merits such as repeatability

and fast and easy implementation. Because it is based on human visual perception, on the other hand, its assessment of visual quality agrees closely with that of subjective assessment. In this sense, the new method attempts to combine the merits of the two different types of assessment.

1.3.2.2.1 Motivation

Visual quality assessment is best conducted via the subjective approach since in this case the HVS is the ultimate viewer. The implementation of subjective assessment is, however, time-consuming and costly, and it lacks repeatability. On the other hand, although not always accurate, objective assessment is fast, easy, and repeatable. The motivation here is to develop an objective quality measurement system such that its quality assessment is very close to that obtained by using subjective assessment. In order to achieve this goal, this objective system is based on subjective assessment. That is, it uses the rating achieved via subjective assessment as a criterion to search for new objective measurements so as to have the objective rating as close to the subjective one as possible.

1.3.2.2.2 Methodology

The derivation of the objective quality assessment system is shown in [Figure 1.12](#). The input testing video goes through a degradation block, resulting in degraded input video. The degradation block, or impairment generator, includes various video compression codecs (coder-decoder pairs) with bit rates ranging from 56 kbits per second to 45 Mbits per second, and other video operations. The input video and degraded input video form a pair of testing videos, which are sent to a subjective assessment block as well as a statistical feature selection block.

A normal subjective visual quality assessment, as introduced in the previous subsection, is performed in the subjective assessment block, which involves a large panel of observers (e.g., 48 observers in Webster et al. [1993]). In the statistical feature selection block, a variety of statistical operations are conducted and various statistical features are selected.

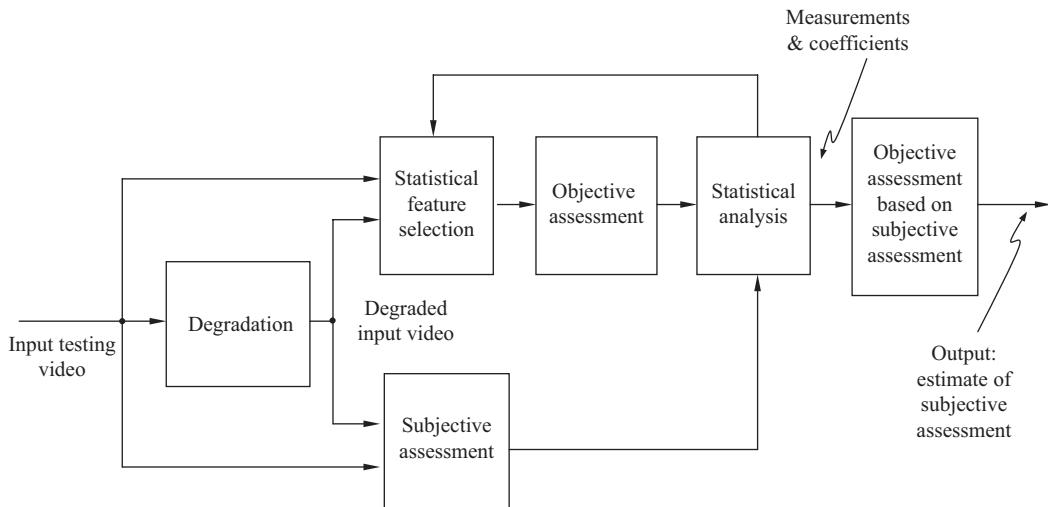


FIGURE 1.12

Block diagram of objective assessment based on subjective assessment.

Examples cover Sobel filtering, Laplacian operator, first-order differencing, moment calculation, fast Fourier transform, etc. Statistical measurements are then selected based on these statistical operations and features. An objective assessment is formed as follows.

$$\hat{s} = a_0 + \sum_{i=1}^l a_i n_i, \quad (1.21)$$

where \hat{s} denotes the output rating of the object assessment, or simply the objective measure, which is supposed to be a good estimate of the corresponding subjective score. The $n_i, i = 1, \dots, l$ are selected objective measurements. The $a_0, a_i, i = 1, \dots, l$ are coefficients in the linear model of the objective assessment.

The results of the objective assessment and subjective assessment are applied to a statistical analysis block. In the statistical analysis block, the objective assessment rating is compared with the subjective assessment rating. The result of the comparison is fed back to the statistical feature selection block. The statistical measurements obtained in the statistical feature selection block are examined according to their performance in the assessment. A statistical measurement is regarded to be good if it can reduce by a significant amount the difference between the objective assessment and the subjective assessment. The best measurement is determined via an exhaustive search among the various measurements. Note that the coefficients in Equation 1.21 are also examined in the statistical analysis block in a similar manner to that used for the measurements.

The measurements and coefficients determined after iterations result in an optimal objective assessment via Equation 1.21, which is finally passed to the last block as the output of the system. The whole process will become much clearer below.

1.3.2.2.3 Results

The results reported in Webster et al. (1993) are introduced here.

1.3.2.2.4 Information Features

As mentioned in [Section 1.2.2](#), differential sensitivity is a key in human visual perception. Two selected features—perceived spatial information (the amount of spatial detail) and perceived temporal information (the amount of temporal luminance variation)—involve pixel differencing. Spatial information (SI) is defined as shown below.

$$SI(f_n) = STD_s \{Sobel(f_n)\}, \quad (1.22)$$

where STD_s stands for the standard deviation operator in the spatial domain, $Sobel$ denotes the Sobel operation, and f_n represents the n th video frame. Temporal information (TI) is defined similarly:

$$TI(f_n) = STD_s \{\Delta f_n\}, \quad (1.23)$$

where $\Delta f_n = f_n - f_{n-1}$, i.e., the successive frame difference.

Determined Measurements

The parameter l in Equation 1.21 is chosen as three. That is,

$$\hat{s} = a_0 + a_1 n_1 + a_2 n_2 + a_3 n_3. \quad (1.24)$$

The measurements n_1 , n_2 , and n_3 are formulated based on the previously defined information features: SI and TI.

Measurement n_1 :

$$n_1 = RMS_t \left(5.81 \left| \frac{SI(of_n) - SI(df_n)}{SI(of_n)} \right| \right), \quad (1.25)$$

where RMS_t represents the root mean square value taken over the time dimension, and of_n and df_n denote the original n th frame and the degraded n th frame, respectively. It is observed that n_1 is a measure of the relative change in the SI between the original frame and the degraded frame.

Measurement n_2 :

$$n_2 = \mathfrak{J}_t \{ 0.108 \cdot MAX\{[TI(of_n) - TI(df_n)], 0\} \}, \quad (1.26)$$

where:

$$\mathfrak{J}_t \{y_t\} = STD_t \{CONV(y_t, [-1, 2, -1])\}, \quad (1.27)$$

where STD_t denotes the standard deviation operator with respect to time, and $CONV$ indicates the convolution operation between its two arguments. It is understood that TI measures temporal luminance variation (temporal motion) and the convolution kernel, $(-1, 2, -1)$, enhances the variation due to its high-pass filter nature. Therefore, n_2 measures the difference of TI between the original and degraded frames.

Measurement n_3 :

$$n_3 = MAX_t \left\{ 4.23 \cdot \log_{10} \left(\frac{TI(df_n)}{TI(of_n)} \right) \right\}, \quad (1.28)$$

where MAX_t indicates taking the maximum value over time. Therefore, measurement n_3 responds to the ratio between the TI of the degraded video and that of the original video. Distortion such as block artifacts (discussed in [Chapter 11](#)) and motion jerkiness (discussed in [Chapter 10](#)), which occurs in video coding, will cause n_3 to be large.

1.3.2.2.5 Objective Estimator

The least square error procedure is applied to testing video sequences with measurements n_i , $i = 1, 2, 3$, determined above, to minimize the difference between the rating scores obtained from the subjective assessment and the objective assessment, resulting in the estimated coefficients a_0 and a_i , $i = 1, 2, 3$. Consequently, the objective assessment of visual quality \hat{s} becomes

$$\hat{s} = 4.77 - 0.992n_1 - 0.272n_2 - 0.356n_3. \quad (1.29)$$

1.3.2.2.6 Reported Experimental Results

It was reported that the correlation coefficient between the subjective assessment score and the objective assessment score (an estimate of the subjective score) is in the

range of 0.92–0.94. It is noted that a set of 36 testing scenes containing various amounts of spatial and TI was used in the experiment. Hence, it is apparent that quite good performance was achieved.

Although there is surely room for further improvement, this work does open a new and promising way to assess visual quality by combining subjective and objective approaches. It is objective and thus fast and easy; and because it is based on the subjective measure, it is more accurate in terms of the high correlation to human perception. Theoretically, the SI measure and TI measure defined on differencing are very important. They reflect the most important aspect of human visual perception.

1.4 Information Theory Results

In the beginning of this chapter it was noted that the term information is considered one of the fundamental concepts in image and video compression. We will now address some information theory results. In this section, measure of information and the entropy of an information source are covered first. We then introduce some coding theorems, which play a fundamental role in studying image and video compression.

1.4.1 Entropy

Entropy is a very important concept in information theory and communications. So is it in image and video compression. We first define the information content of a source symbol. Then we define entropy as average information content per symbol for a discrete memory-less source.

1.4.1.1 Information Measure

As mentioned at the beginning of this chapter, information is defined as knowledge, fact, and news. It can be measured quantitatively. The carriers of information are symbols. Consider a symbol with an occurrence probability p . Its information content (i.e., the amount of information contained in the symbol), I , is defined as follows.

$$I = \log_2 \frac{1}{p} \quad \text{bits} \quad \text{or} \quad I = -\log_2 p \quad \text{bits}, \quad (1.30)$$

where the *bit* is a contraction of *binary unit*. In the above equations we set the base of the logarithmic function to equal 2. It is noted that these results can be easily converted as follows for the case where the r -ary digits are used for encoding. Hence, from now on, we restrict our discussion to binary encoding.

$$I = -\log_r 2 \cdot \log_2 p \quad \text{bits}. \quad (1.31)$$

According to Equation 1.30, the information contained within a symbol is a logarithmic function of its occurrence probability. The smaller the probability, the more information the symbol contains. This agrees with common sense. The occurrence probability is

somewhat related to the uncertainty of the symbol. A small occurrence probability means large uncertainty. In this way, we see that the information content of a symbol is about the uncertainty of the symbol. It is noted that the information measure defined here is valid for both equally probable symbols and nonequally probable symbols (Lathi 1998).

1.4.1.2 Average Information per Symbol

Now consider a discrete memoryless information source. By discreteness, we mean the source is a countable set of symbols. By memoryless, we mean the occurrence of a symbol in the set is independent of that of its preceding symbol. Take a look at a source of this type that contains m possible symbols: $\{s_i, i = 1, 2, \dots, m\}$. The corresponding occurrence probabilities are denoted by $\{p_i, i = 1, 2, \dots, m\}$. According to the discussion in the previous subsubsection, the information content of a symbol s_i , I_i , is equal to $I_i = -\log_2 p_i$ bits. Entropy is defined as the average information content per symbol of the source. Obviously, the entropy, H , can be expressed as follows.

$$H = - \sum_{i=1}^m p_i \log_2 p_i \quad \text{bits.} \quad (1.32)$$

From this definition, we see that the entropy of an information source is a function of occurrence probabilities. It is straightforward to show that the entropy reaches the maximum when all symbols in the set are equally probable.

1.4.2 Shannon's Noiseless Source Coding Theorem

Consider a discrete, memoryless, stationary information source. In what is called source encoding, a *codeword* is assigned to each symbol in the source. The number of bits in the codeword is referred to as the length of the codeword. The average length of codewords is referred to as bit rate, expressed in the unit of bits per symbol.

Shannon's noiseless source coding theorem states that for a discrete, memoryless, stationary information source, the minimum bit rate required to encode a symbol on average is equal to the entropy of the source. This theorem provides us with a lower bound in source coding. Shannon showed that the lower bound can be achieved when the *encoding delay* extends to infinity. By encoding delay, we mean the encoder waits and then encodes a certain number of symbols at once. Fortunately, with finite encoding delay, we can already achieve an average codeword length fairly close to the entropy. That is, we do not have to actually sacrifice bit rate much to avoid long encoding delay, which involves high computational complexity and a large amount of memory space.

Note that the discreteness assumption is not necessary. We assume a discrete source simply because digital image and video are the focus in this book. Stationarity assumption is necessary in deriving the noiseless source coding theorem. This assumption may not be satisfied in practice. Hence, Shannon's theorem is a theoretical guideline only. There is no doubt, however, that it is a fundamental theoretical result in information theory.

In summary, the noiseless source coding theorem, Shannon's first theorem, which was published in his celebrated paper (Shannon 1948), is concerned with the case where both the channel and the coding system are noise free. The aim under these circumstances is coding compactness. The more compact, the better the coding. This theorem specifies the lower bound, which is the source entropy, and how to reach this lower bound.

One way to evaluate the efficiency of a coding scheme is to determine its *efficiency* with respect to the lower bound, i.e., entropy. The efficiency η is defined as follows.

$$\eta = \frac{H}{L_{avg}}, \quad (1.33)$$

where H is entropy, and L_{avg} denotes the average length of the codewords in the code. Since the entropy is the lower bound, the efficiency never exceeds the unity, i.e., $\eta \leq 1$. The same definition can be generalized to calculate the relative efficiency between two codes. That is,

$$\eta = \frac{L_{avg,1}}{L_{avg,2}}, \quad (1.34)$$

where $L_{avg,1}$ and $L_{avg,2}$ represent the average codeword length for code 1 and code 2, respectively. We usually put the larger of the two in the denominator, and η is called the efficiency of code 2 with respect to code 1. A complementary parameter of coding efficiency is coding *redundancy*, ζ , which is defined as

$$\zeta = 1 - \eta. \quad (1.35)$$

1.4.3 Shannon's Noisy Channel Coding Theorem

If a code has an efficiency of $\eta = 1$, i.e., it reaches the lower bound of source encoding, then coding redundancy is $\zeta = 0$. Now consider a noisy transmission channel. In transmitting the coded symbol through the noisy channel, the received symbols may be erroneous due to the lack of redundancy. On the other hand, it is well-known that by adding redundancy (e.g., parity check bits), some errors occurring during the transmission over the noisy channel may be identified. The coded symbols are then resent. In this way, we see that adding redundancy may combat noise.

Shannon's noisy channel coding theorem states that it is possible to transmit symbols over a noisy channel without error if the bit rate is below a *channel capacity*, C . That is,

$$R < C \quad (1.36)$$

where R denotes the bit rate. The channel capacity is determined by the noise and signal power.

In conclusion, the noisy channel coding theorem, Shannon's second theorem (Shannon 1948), is concerned with a noisy, memoryless channel. By memoryless, we mean the channel output corresponding to the current input is independent of the output corresponding to previous input symbols. Under these circumstances, the aim is reliable communication. To be error-free, the bit rate cannot exceed channel capacity. That is, channel capacity sets an upper bound on the bit rate.

1.4.4 Shannon's Source Coding Theorem

As seen in the previous two subsections, the noiseless source coding theorem defines the lowest possible bit rate for noiseless source coding and noiseless channel transmission, whereas the noisy channel coding theorem defines the highest possible coding bit rate for

error-free transmission. Therefore, both theorems work for reliable (no error) transmission. In this subsection, we continue to deal with discrete memoryless information sources, but we discuss the situation in which lossy coding is encountered. As a result, distortion of the information sources takes place. For instance, quantization, which is covered in the next chapter, causes information loss. Therefore, it is concluded that if an encoding procedure involves quantization, then it is lossy coding. That is, errors occur during the coding process, even though the channel is error-free. We want to find the lower bound of the bit rate for this case.

The source coding theorem (Shannon 1948) states that for a given distortion D , there exists a rate distortion function $R(D)$ (Berger 1971), which is the minimum bit rate required to transmit the source with distortion less than or equal to D . That is, in order to have distortion not larger than D , the bit rate, R , must satisfy the following condition.

$$R \geq R(D). \quad (1.37)$$

A more detailed discussion about this theorem and the rate distortion function is given in [Chapter 15](#), when we introduce video coding.

1.4.5 Information Transmission Theorem

It is clear that by combining the noisy channel coding theorem and the source coding theorem we can derive the following relationship:

$$C \geq R(D) \quad (1.38)$$

This is called the information transmission theorem (Slepian 1973). It states that if the channel capacity of a noisy channel, C , is larger than the rate distortion function $R(D)$, then it is possible to transmit an information source with distortion D over a noisy channel.

1.5 Summary

In this chapter, we first discussed the necessity for image and video compression. It is shown that image and video compression become enabling techniques in today's exploding number of digital multimedia applications. Then, we show that the feasibility of image and video compression rests in redundancy removal. Three types of redundancy—statistical redundancy, coding redundancy, and psychovisual redundancy—are studied. Statistical redundancy comes from interpixel correlation. By interpixel correlation, we mean correlation between pixels either located in one frame (spatial or intraframe redundancy) or pixels located in successive frames (temporal or interframe redundancy). Psychovisual redundancy is based on the features (several types of masking phenomena) of human visual perception. That is, visual information is not perceived equally from the human visual point of view. In this sense, some information is psychovisually redundant. Coding redundancy is related to coding technique.

The visual quality of reconstructed image and video is a crucial criterion in the evaluation of the performance of visual transmission or storage systems. Both subjective and objective assessments are discussed. A new and promising objective technique based on subjective assessment is introduced. Since it combines the merits of both types of visual quality assessment, it achieves quite satisfactory performance. The selected statistical features reveal some possible mechanisms of the human visual perception. Further study in this regard would be fruitful.

In the last section, we introduced some fundamental information theory results that are relevant to image and video compression. The results introduced include information measurement, entropy, and several theorems. All the theorems assume discrete, memoryless, and stationary information sources. The noiseless source coding theorem points out that the entropy of an information source is the lower bound of coding bit rate that a source encoder can achieve. The source coding theorem deals with lossy coding applied in a noise-free channel. It states that for a given distortion, D , there is a rate distortion function, $R(D)$. Whenever the bit rate in the source coding is greater than $R(D)$, the reconstructed source at the receiving end satisfies the fidelity requirement defined by the D . The noisy channel coding theorem states that, in order to achieve error-free performance, the source coding bit rate must be smaller than the channel capacity. Channel capacity is a function of noise and signal power. The information transmission theorem combines the noisy channel coding theorem and the source coding theorem. It states that it is possible to have a reconstructed waveform at the receiving end, satisfying the fidelity requirement corresponding to distortion, D , if the channel capacity, C , is larger than the rate distortion function, $R(D)$. Although some of the assumptions on which these theorems were developed may not be valid in complicated practical situations, these theorems provide important theoretical limits for image and video coding. They can also be used for evaluation of the performance of different coding techniques.

Exercises

- 1.1 Using your own words, define spatial, temporal, and psychovisual redundancy, and state the impact they have on image and video compression.
- 1.2 Why is differential sensitivity considered the most important feature in human visual perception?
- 1.3 From the description of the newly developed objective assessment technique based on subjective assessment, discussed in [Section 1.3](#), what points do you think are related to and support the statement made in problem 2?
- 1.4 Interpret Weber's law using your own words.
- 1.5 What is the advantage possessed by color models that decouple the luminance component from chrominance components?
- 1.6 Why has the HIS model not been adopted by any TV systems?
- 1.7 What is the problem with the objective visual quality measure of PSNR?

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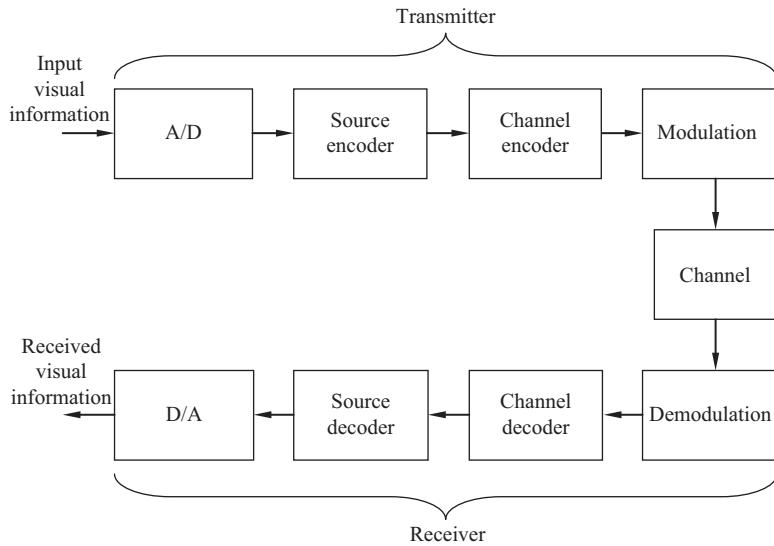
Quantization

After an introduction to image and video compression, which was presented in [Chapter 1](#), we address several fundamental aspects of image and video compression in the remaining chapters of [Part I](#). [Chapter 2](#), as the first chapter in the series, concerns quantization. Quantization is a necessary component in lossy coding and has direct impact on the bit rate and distortion of reconstructed image or video. We discuss concepts, principles, and various quantization techniques, which include uniform and nonuniform quantization, optimum quantization, and adaptive quantization.

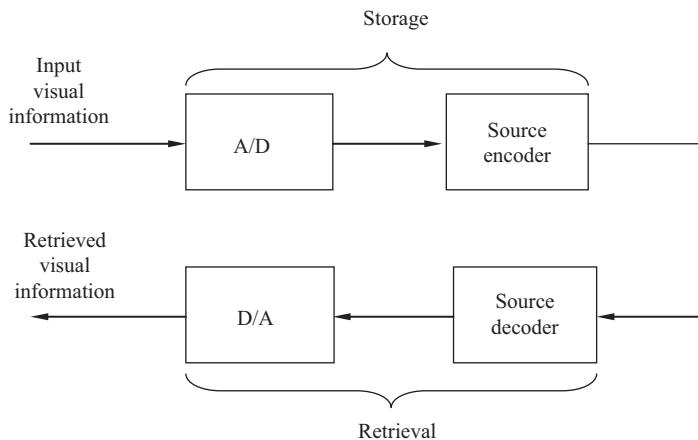
2.1 Quantization and the Source Encoder

Recall [Figure 1.1](#), in which the functionality of image and video compression in the applications of visual communications and storage is depicted. In the context of visual communications, the whole system may be illustrated as shown in [Figure 2.1](#). In the transmitter, the input analog information source is converted to a digital format in the A/D converter block. The digital format is compressed through the image and video source encoder. In the channel encoder, some redundancy is added to help combat noise and, hence, transmission error. Modulation makes digital data suitable for transmission through the analog channel, such as air space in the application of a TV broadcast. At the receiver, the counterpart blocks reconstruct the input visual information. As far as storage of visual information is concerned, the blocks of channel, channel encoder, channel decoder, modulation, and demodulation may be omitted, as shown in [Figure 2.2](#). If input and output are required to be in the digital format in some applications, then the A/D and D/A converters are omitted from the system. If they are required, however, other blocks such as encryption and decryption can be added to the system (Sklar 1988). Hence, what is depicted in [Figure 2.1](#) is a conceptually fundamental block diagram of a visual communication system.

In this book, we are mainly concerned with source encoding and source decoding. To this end, we take a step further. That is, we show block diagrams of a source encoder and decoder in [Figure 2.3](#). As shown in [Figure 2.3a](#), there are three components in the source encoding: transformation, quantization, and codeword assignment. After the transformation, some form of an input information source is presented to a quantizer. In other words, the transformation block decides which types of quantities from the input image and video are to be encoded. It is not necessary that the original image and video waveform be quantized and coded: we will show that some formats obtained from the input image and video are more suitable for encoding. An example is the difference signal. From the discussion of interpixel correlation in [Chapter 1](#), it is known that a pixel is normally highly correlated with its immediately horizontal or vertical neighboring pixel. Therefore, a better strategy is to encode the difference of gray level values between a pixel and its neighbor.

**FIGURE 2.1**

Block diagram of a visual communication system.

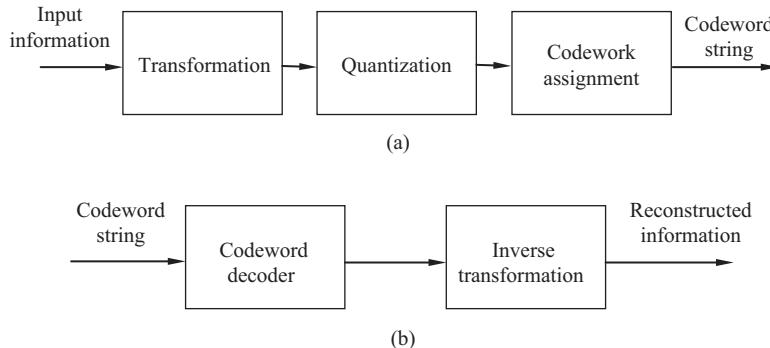
**FIGURE 2.2**

Block diagram of a visual storage system.

Since these data are highly correlated, the difference usually has a smaller dynamic range. Consequently, the encoding is more efficient. This idea is discussed in [Chapter 3](#) in detail.

Another example is what is called transform coding, which is addressed in [Chapter 4](#). There, instead of encoding the original input image and video, we encode a transform of the input image and video. Since the redundancy in the transform domain is reduced greatly, the coding efficiency is much higher compared with directly encoding the original image and video.

Note that the term transformation in [Figure 2.3a](#) is sometimes referred to as *mapper* and *signal processing* in the literature (Gonzalez and Woods 1992, Li and Zhang 1995). Quantization refers to a process that converts input data into a set of finitely many different values. Often, the input data to a quantizer is continuous in magnitude.

**FIGURE 2.3**

Block diagram of (a) source encoder and (b) source decoder.

Hence, quantization is essentially discretization in magnitude, which is an important step in the lossy compression of digital image and video. (The reason that the term lossy compression is used here will be shown shortly.) The input and output of quantization can be either scalars or vectors. The quantization with scalar input and output is called *scalar quantization*, whereas that with vector input and output is referred to as *vector quantization*. In this chapter, we discuss scalar quantization. Vector quantization will be addressed in [Chapter 9](#).

After quantization, codewords are assigned to finitely many different values, the output of the quantizer. Natural binary code (NBC) and variable-length code (VLC), introduced in [Chapter 1](#), are two examples of this. Other examples are the widely utilized entropy code (including Huffman code and arithmetic code), dictionary code, and run-length code (RLC) (frequently used in facsimile transmission), which are covered in [Chapters 5 and 6](#).

The source decoder, as shown in [Figure 2.3b](#), consists of two blocks: codeword decoder and inverse transformation. They are counterparts of the codeword assignment and transformation in the source encoder. Note that there is no block that corresponds to quantization in the source decoder. The implication of this observation is the following. First, quantization is an irreversible process. That is, in general there is no way to find the original value from the quantized value. Second, quantization is, therefore, a source of information loss. In fact, quantization is a critical stage in image and video compression. It has significant impact on the distortion of reconstructed image and video as well as the bit rate of the encoder. Obviously, coarse quantization results in more distortion and lower bit rate than fine quantization.

In this chapter, uniform quantization, which is the simplest yet the most important case, is discussed first. Nonuniform quantization is covered after that, followed by optimum quantization for both uniform and nonuniform cases. Then, a discussion of adaptive quantization is provided. Finally, pulse code modulation (PCM) is described as the best established and most frequently implemented digital coding method involving quantization.

2.2 Uniform Quantization

Uniform quantization is the simplest yet very popular quantization technique. Conceptually, it is of great importance. Hence, we start our discussion on quantization with uniform quantization. Several fundamental concepts of quantization are introduced in this section.

2.2.1 Basics

This subsection concerns several basic aspects of uniform quantization. They are some fundamental terms, quantization distortion, and quantizer design.

2.2.1.1 Definitions

Take a look at [Figure 2.4](#). The horizontal axis denotes the input to a quantizer, while the vertical axis represents the output of the quantizer. The relationship between the input and the output best characterizes this quantizer; this type of curve is referred to as the input-output characteristic of the quantizer. From the curve, it can be seen that there are nine intervals along the x -axis. Whenever the input falls in one of the intervals, the output assumes a corresponding value. The input-output characteristic of the quantizer is staircase-like and, hence, clearly nonlinear.

The end points of the intervals are called *decision levels*, denoted by d_i with i being the index of intervals. The output of the quantization is referred to as the *reconstruction level* (also known as *quantizing level* [Musmann 1979]), denoted by y_i with i being its index. The length of the interval is called the *step size* of the quantizer, denoted by Δ . With the above terms defined, we can now mathematically define the function of the quantizer in [Figure 2.4](#) as follows.

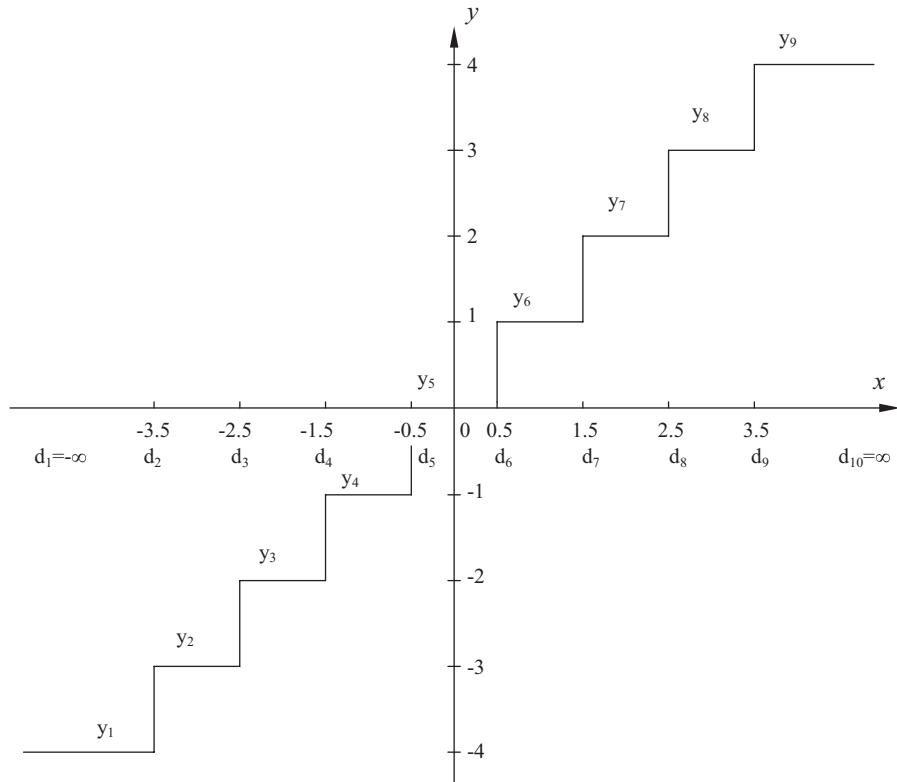


FIGURE 2.4

Input-output characteristic of a uniform midtread quantizer.

$$y_i = Q(x) \quad \text{if} \quad x \in (d_i, d_{i+1}), \quad (2.1)$$

where $i = 1, 2, \dots, 9$ and $Q(x)$ is the output of the quantizer with respect to the input x .

It is noted that in Figure 2.4, $\Delta = 1$. The decision levels and reconstruction levels are evenly spaced. It is a uniform quantizer because it possesses the following two features.

1. Except possibly the right-most and left-most intervals, all intervals (hence, decision levels) along the x -axis are uniformly spaced. That is, each inner interval has the same length.
2. Except possibly the outer intervals, the reconstruction levels of the quantizer are also uniformly spaced. Furthermore, each inner reconstruction level is the arithmetic average of the two decision levels of the corresponding interval along the x -axis.

The uniform quantizer depicted in Figure 2.4 is called a *midtread* quantizer. Its counterpart is called a *midrise* quantizer, in which the reconstructed levels do not include the value of zero. A midrise quantizer having step size $\Delta = 1$ is shown in Figure 2.5. While midtread quantizers are usually utilized for an odd number of reconstruction levels, midrise quantizers are used for an even number of reconstruction levels.

Note that the input-output characteristic of both the midtread and midrise uniform quantizers as depicted in Figures 2.4 and 2.5, respectively, is odd symmetric with respect

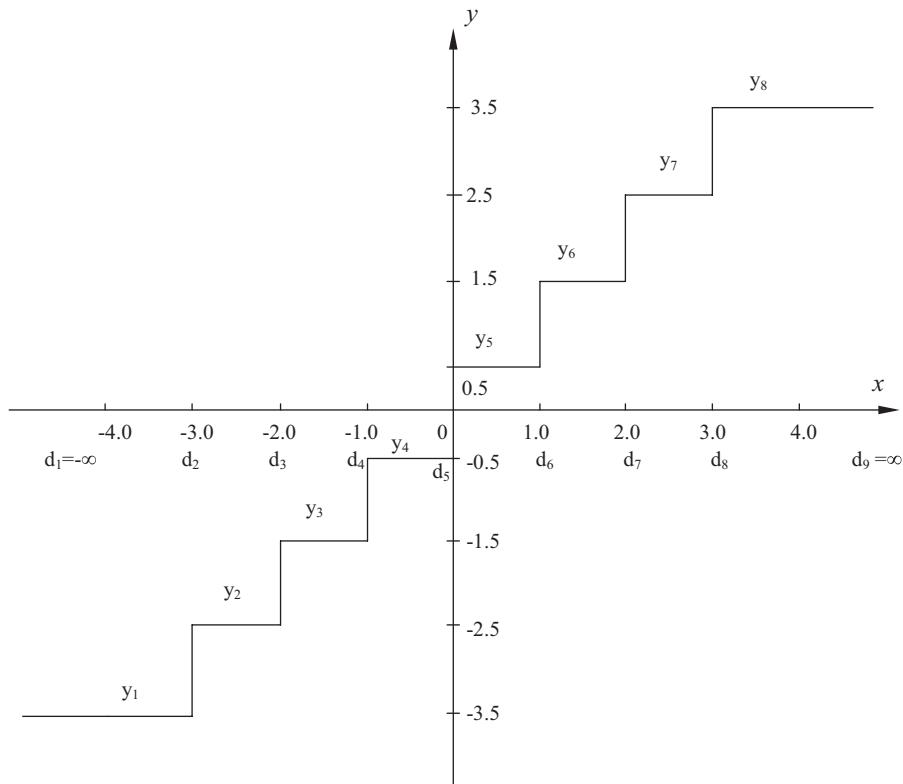


FIGURE 2.5

Input-output characteristic of a uniform midrise quantizer.

to the vertical axis $x = 0$. In the rest of this chapter, our discussion develops under this symmetry assumption. The results thus derived will not lose generality since we can always subtract the statistical mean of input x from the input data and thus achieve this symmetry. After quantization, we can add the mean value back.

Denote by N the total number of reconstruction levels of a quantizer. A close look at [Figures 2.4](#) and [2.5](#) reveals that if N is even, then the decision level $d_{(N/2)+1}$ is located in the middle of the input x -axis, i.e., $d_{(N/2)+1} = 0$. If N is odd, on the other hand, then the reconstruction level $y_{(N+1)/2} = 0$. This convention is important in understanding the design tables of quantizers in the literature.

2.2.1.2 Quantization Distortion

The source coding theorem presented in [Chapter 1](#) states that for a certain distortion D , there exists a rate distortion function $R(D)$, such that, as long as the bit rate used is larger than $R(D)$, it is possible to transmit the source with a distortion smaller than D . Since we cannot afford an infinite bit rate to represent an original source, some distortion in quantization is inevitable. In other words, we can say that since quantization causes information loss irreversibly, we encounter *quantization error* and, consequently, an issue: how to evaluate the quality or, equivalently, the distortion of quantization. According to our discussion on visual quality assessment in [Chapter 1](#), we know that there are two ways to do so: subjective evaluation and objective evaluation.

In terms of subjective evaluation, in [Section 1.3.1](#) we introduced a five-scale rating adopted in CCIR Recommendation 500-3. We also described the false contouring phenomenon, which is caused by coarse quantization. That is, our human eyes are more sensitive to the relatively uniform regions in an image plane. Therefore, an insufficient number of reconstruction levels results in annoying false contours. In other words, more reconstruction levels are required in relatively uniform regions than in relatively nonuniform regions.

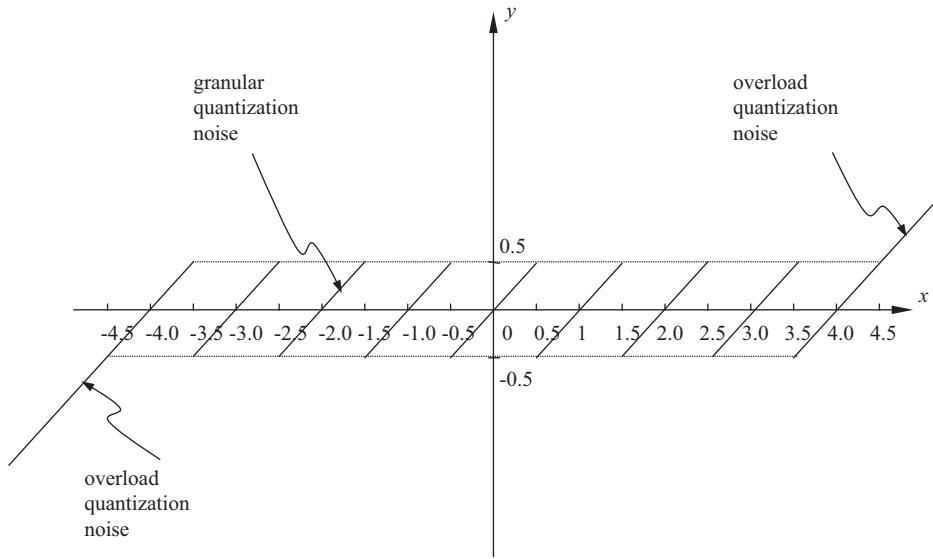
In terms of objective evaluation, in [Section 1.3.2](#) we defined mean square error (MSE) and root mean square error ($RMSE$), signal-to-noise ratio (SNR) and peak signal-to-noise ratio ($PSNR$). In dealing with quantization, we define quantization error, e_q , as the difference between the input signal and the quantized output:

$$e_q = x - Q(x), \quad (2.2)$$

where x and $Q(x)$ are input and quantized output, respectively. Quantization error is often referred to as *quantization noise*. It is a common practice to treat input x as a random variable with a probability density function (*pdf*) $f_x(x)$. Mean square quantization error, MSE_q , can thus be expressed as

$$MSE_q = \sum_{i=1}^N \int_{d_i}^{d_{i+1}} (x - Q(x))^2 f_x(x) dx \quad (2.3)$$

where N is the total number of reconstruction levels. Note that the outer decision levels may be $-\infty$ or ∞ , as shown in [Figures 2.4](#) and [2.5](#). It is clear that, when the *pdf*, $f_x(x)$, remains unchanged, fewer reconstruction levels (smaller N) result in more distortion. That is, coarse quantization leads to large quantization noise. This confirms the statement that quantization is a critical component in a source encoder, which significantly influences

**FIGURE 2.6**

Quantization noise of the uniform midtread quantizer shown in Figure 2.4.

both bit rate and distortion of the encoder. As mentioned, the assumption we made above that the input-output characteristic is odd symmetric with respect to the $x = 0$ axis implies that the mean of the random variable, x , is equal to zero, i.e., $E(x) = 0$. Therefore, the mean square quantization error MSE_q is the variance of x , i.e., $MSE_q = \sigma_q^2$.

The quantization noise associated with the midtread quantizer depicted in Figure 2.4 is shown in Figure 2.6. It is clear that the quantization noise is signal dependent. It is observed that, associated with the inner intervals, the quantization noise is bounded by $\pm 0.5\Delta$. This type of quantization noise is referred to as *granular noise*. The noise associated with the right-most and the left-most intervals are unbounded as the input x approaches either $-\infty$ or ∞ . This type of quantization noise is called *overload noise*. Denoting the mean square granular noise and overload noise by $MSE_{q,g}$ and $MSE_{q,o}$, respectively, we then have the following relations:

$$MSE_q = MSE_{q,g} + MSE_{q,o} \quad (2.4)$$

and

$$MSE_{q,g} = \sum_{i=2}^{N-1} \int_{d_i}^{d_{i+1}} (x - Q(x))^2 f_X(x) dx \quad (2.5)$$

$$MSE_{q,o} = 2 \int_{d_1}^{d_2} (x - Q(x))^2 f_X(x) dx \quad (2.6)$$

2.2.1.3 Quantizer Design

The design of a quantizer (either uniform or nonuniform) involves choosing the number of reconstruction levels, N (hence, the number of decision levels, $N + 1$), and selecting

the values of decision levels and reconstruction levels (deciding where to locate them). In other words, the design of a quantizer is equivalent to specifying its input-output characteristic.

The *optimum* quantizer design can be stated as follows. For a given *pdf* of the input random variable, $f_X(x)$, determine the number of reconstruction levels, N , choose a set of decision levels $\{d_i, i = 1, \dots, N+1\}$ and a set of reconstruction levels $\{y_i, i = 1, \dots, N\}$ such that the mean square quantization error, MSE_q , defined in Equation 2.3, is minimized.

In the uniform quantizer design, the total number of reconstruction levels, N , is usually given. According to the two features of uniform quantizers described in Section 2.2.1.1, we know that the reconstruction levels of a uniform quantizer can be derived from the decision levels. Hence, only one of these two sets is independent. Furthermore, both decision levels and reconstruction levels are uniformly spaced except possibly the outer intervals. These constraints together with the symmetry assumption lead to the following observation: There is in fact only one parameter that needs to be decided in uniform quantizer design, which is the step size Δ . As to the optimum uniform quantizer design, a different *pdf* leads to a different step size.

2.2.2 Optimum Uniform Quantizer

In this subsection, we first discuss optimum uniform quantizer design when the input x obeys uniform distribution. Then, we cover optimum uniform quantizer design when the input x has other types of probabilistic distributions.

2.2.2.1 Uniform Quantizer with Uniformly Distributed Input

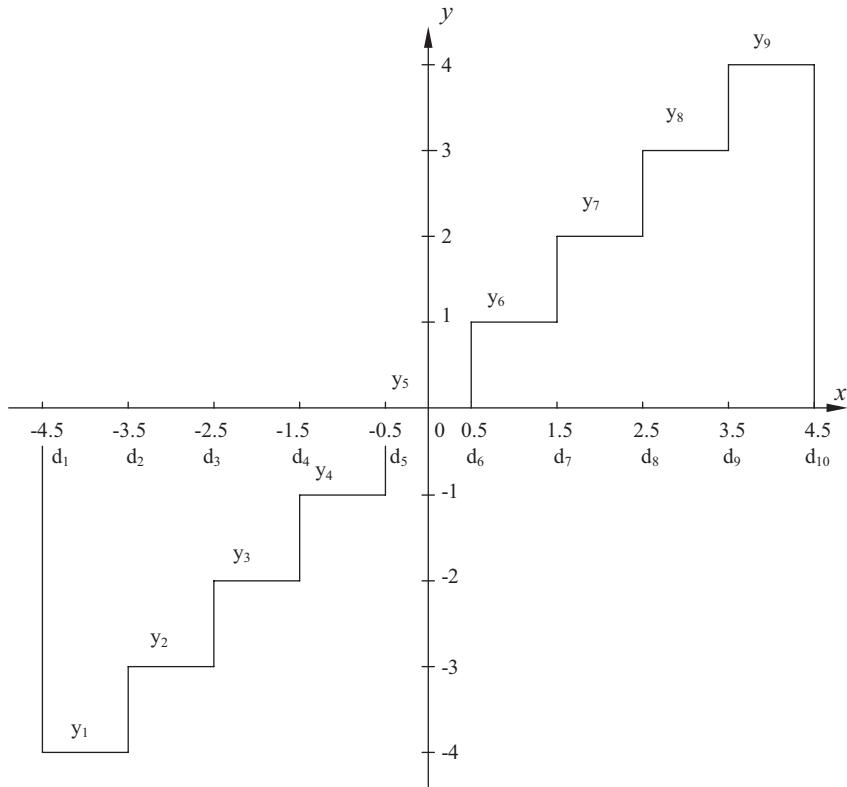
Let us return to Figure 2.4, where the input-output characteristic of a nine-reconstruction-level midtread quantizer is shown. Now, consider that the input x is a uniformly distributed random variable. Its input-output characteristic is shown in Figure 2.7. We notice that the new characteristic is restricted within a finite range of x , i.e., $-4.5 \leq x \leq 4.5$. This is due to the definition of uniform distribution. Consequently, the overload quantization noise does not exist in this case, which is shown in Figure 2.8.

The mean square quantization error is found to be

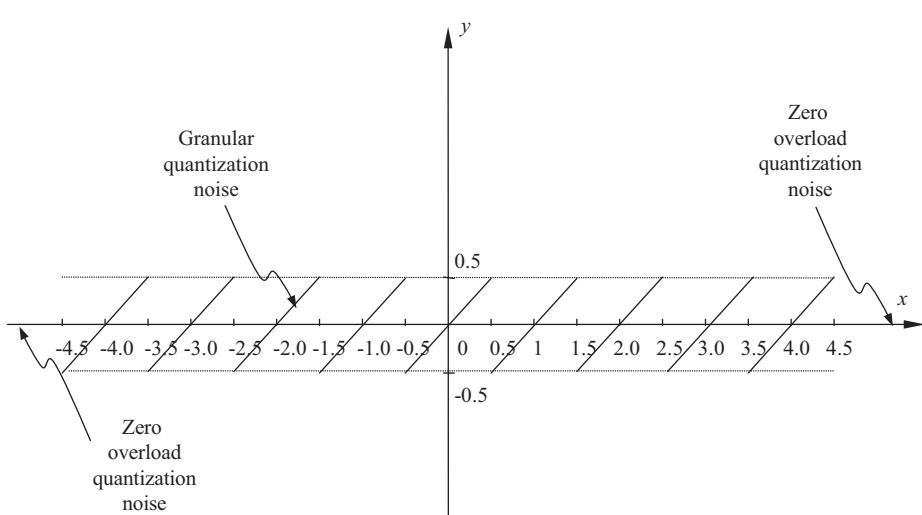
$$\begin{aligned} MSE_q &= N \int_{d_1}^{d_2} (x - Q(x))^2 \frac{1}{N\Delta} dx \\ MSE_q &= \frac{\Delta^2}{12}. \end{aligned} \tag{2.7}$$

This result indicates that if the input to a uniform quantizer has a uniform distribution and the number of reconstruction levels is fixed, then the mean square quantization error is directly proportional to the square of the quantization step size. Or, in other words, the root mean square quantization error (the standard deviation of the quantization noise) is directly proportional to the quantization step. The larger the step size, the larger (according to square law) the mean square quantization error. This agrees with our previous observation: coarse quantization leads to large quantization error.

As mentioned above, the mean square quantization error is equal to the variance of the quantization noise, i.e., $MSE_q = \sigma_q^2$. In order to find the SNR of the uniform quantization

**FIGURE 2.7**

Input-output characteristic of a uniform midtread quantizer with input x having uniform distribution in $[-4.5, 4.5]$.

**FIGURE 2.8**

Quantization noise of the quantizer shown in [Figure 2.7](#).

in this case, we need to determine the variance of the input x . Note that we assume the input x to be a zero mean uniform random variable. So, according to probability theory, we have

$$\sigma_x^2 = \frac{(N\Delta)^2}{12}. \quad (2.8)$$

Therefore, the mean square SNR SNR_{ms} , defined in [Chapter 1](#), is equal to

$$SNR_{ms} = 10 \log_{10} \frac{\sigma_x^2}{\sigma_q^2} = 10 \log_{10} N^2. \quad (2.9)$$

Note that here we use the subscript ms to indicate the SNR in the mean square sense, as defined in the previous chapter. If we assume $N = 2^n$, we then have

$$SNR_{ms} = 20 \log_{10} 2^n = 6.02n \text{ dB}. \quad (2.10)$$

The interpretation of the above result is as follows. If we use the NBC to code the reconstruction levels of a uniform quantizer with a uniformly distributed input source, then every increased bit in the coding brings out a 6.02 dB increase in the SNR_{ms} . An equivalent statement can be derived from Equation 2.7. That is, whenever the step size of the uniform quantizer decreases by a half, the mean square quantization error decreases four times.

2.2.2.2 Conditions of Optimum Quantization

The conditions under which the mean square quantization error MSE_q is minimized were derived (Lloyd 1957, 1982, Max 1960) for a given *pdf* of the quantizer input, $f_X(x)$.

The mean square quantization error MSE_q was given in Equation 2.3. The necessary conditions for optimum (minimum MSE) quantization are as follows. That is, the derivatives of MSE_q with respect to the d_i and y_i have to be zero.

$$(d_i - y_{i-1})^2 f_X(d_i) - (d_i - y_i)^2 f_X(d_i) = 0 \quad i = 2, \dots, N \quad (2.11)$$

$$-\int_{d_i}^{d_{i+1}} (x - y_i) f_X(x) dx = 0 \quad i = 1, \dots, N \quad (2.12)$$

The sufficient conditions can be derived accordingly by involving the second-order derivatives (Max 1960, Fleischer 1964). The symmetry assumption of the input-output characteristic made earlier holds here as well. These sufficient conditions are listed below.

$$1. \quad x_1 = -\infty \text{ and } x_{N+1} = +\infty \quad (2.13)$$

$$2. \quad \int_{d_i}^{d_{i+1}} (x - y_i) f_X(x) dx = 0 \quad i = 1, 2, \dots, N \quad (2.14)$$

$$3. \quad d_i = \frac{1}{2}(y_{i-1} + y_i) \quad i = 2, \dots, N \quad (2.15)$$

Note that the first condition is for an input x whose range is $-\infty < x < \infty$. The interpretation of the above conditions is that each decision level (except for the outer intervals) is the arithmetic average of the two neighboring reconstruction levels, and each reconstruction level is the centroid of the area under the *pdf* $f_X(x)$ between the two adjacent decision levels.

Note that the above conditions are general in the sense that there is no restriction imposed on the *pdf*. In the next subsubsection, we discuss the optimum uniform quantization when the input of quantizer assumes different distributions.

2.2.2.3 Optimum Uniform Quantizer with Different Input Distributions

Let us return to our discussion on the optimum quantizer design whose input has uniform distribution. Since the input has uniform distribution, the outer intervals are also finite. For uniform distribution, Equation 2.14 implies that each reconstruction level is the arithmetic average of the two corresponding decision levels. Considering the two features of a uniform quantizer, presented in [Section 2.2.1.1](#), we see that a uniform quantizer is optimum (minimizing the mean square quantization error) when the input has uniform distribution.

When the input x is uniformly distributed in $[-1,1]$, the step size Δ of the optimum uniform quantizer is listed in [Table 2.1](#) for the number of reconstruction levels, N , equal to 2, 4, 8, 16, and 32. From the table, we notice that the MSE_q of the uniform quantization with a uniformly distributed input decreases four times as N doubles. As mentioned in [Section 2.2.2.1](#), this is equivalent to an increase of SNR_{ms} by 6.02 dB as N doubles.

The derivation above is a special case, i.e., the uniform quantizer is optimum for a uniformly distributed input. Normally, if the *pdf* is not uniform, the optimum quantizer is not a uniform quantizer. Due to the simplicity of uniform quantization, however, it may sometimes be desirable to design an optimum uniform quantizer for an input with an other-than-uniform distribution.

Under these circumstances, however, Equations 2.13 through 2.15 are not a set of simultaneous equations one can hope to solve with any ease. Numerical procedures were suggested to solve for design of optimum uniform quantizers. Max derived uniform quantization step size Δ for an input with a Gaussian distribution (Max 1960). Paez and Glisson found step size Δ for Laplacian and Gamma distributed input signals (Paez and Glisson 1972). These results are listed in [Table 2.1](#). Note that all three distributions have a zero mean and unit standard deviation. If the mean is not zero, only a shift in input is needed when applying these results. If the standard deviation is not unit, the tabulated step size needs to be multiplied by the standard deviation. The theoretical MSE is also listed in [Table 2.1](#). Note that the subscript q associated with MSE has been dropped for the sake of notational brevity from now on in the chapter as long as it does not cause confusion.

TABLE 2.1

Optimal Symmetric Uniform Quantizer for Uniform, Gaussian, Laplacian, and Gamma Distributions (Having Zero Mean and Unit Variance)

| N | Uniform | | | Gaussian | | | Laplacian | | | Gamma | | |
|------|---------|--------|--------------------------|----------|--------------------------|--------------------------|-----------|----------------------------|---------------------------|--------|----------------------------|-------|
| | d_i | y_i | MSE | d_i | y_i | MSE | d_i | y_i | MSE | d_i | y_i | MSE |
| | | | | 1.596 | -0.798 | 0.363 | -1.414 | -0.707 | 0.500 | -1.154 | -0.577 | 0.668 |
| 2 | -1.000 | -0.500 | 8.33 $\times 10^{-2}$ | 0.000 | 0.798 | 0.000 | 1.414 | 0.707 | 0.500 | 1.154 | 0.577 | 0.668 |
| | 0.000 | 0.500 | | 1.596 | | | 1.414 | | | 1.596 | | |
| | [1.000] | | | | | | | | | | | |
| 4 | -1.000 | -0.750 | 2.08 $\times 10^{-2}$ | -1.991 | -1.494 | 0.119 | -2.174 | -1.631 | 1.963 $\times 10^{-1}$ | -2.120 | -1.590 | 0.320 |
| | -0.500 | -0.250 | | -0.996 | -0.498 | | -1.087 | -0.544 | | -1.060 | -0.530 | |
| | 0.000 | 0.250 | | 0.000 | 0.498 | | 0.000 | 0.544 | | 0.000 | 0.500 | |
| 8 | [0.500] | 0.750 | | 0.996 | 1.494 | | 1.087 | | | 1.060 | | |
| | 1.000 | -0.875 | 5.21 $\times 10^{-3}$ | 1.991 | 3.74 $\times 10^{-2}$ | -2.051 | 2.174 | -2.559 | 7.17 $\times 10^{-2}$ | -3.184 | -2.786 | 0.132 |
| | -0.750 | -0.625 | | -1.758 | -1.465 | | -2.193 | -1.828 | | -2.388 | -1.990 | |
| 16 | -0.500 | -0.375 | | -1.172 | -0.879 | | -1.462 | -1.097 | | -1.592 | -1.194 | |
| | -0.250 | -0.125 | | -0.586 | -0.293 | | -0.731 | -0.366 | | -0.796 | -0.398 | |
| | 0.000 | 0.125 | | 0.000 | 0.293 | | 0.000 | 0.366 | | 0.000 | 0.398 | |
| 32 | [0.250] | 0.375 | | 0.586 | 0.879 | | 0.731 | 1.097 | | 0.796 | 1.194 | |
| | 0.500 | 0.625 | | 1.172 | 1.465 | | 1.462 | 1.828 | | 1.592 | 1.990 | |
| | 0.750 | 0.875 | | 1.758 | 2.051 | | 2.193 | 2.559 | | 2.388 | 2.786 | |
| 64 | 1.000 | -0.938 | 1.30 $\times 10^{-3}$ | 2.344 | | 1.15 $\times 10^{-2}$ | 2.924 | | | 3.184 | | |
| | -0.875 | -0.813 | | -2.680 | -2.513 | | -3.648 | -3.420 | | -4.320 | -4.050 | |
| | -0.750 | -0.688 | | -2.345 | -2.178 | | -3.192 | -2.964 $\times 10^{-2}$ | | -3.780 | -3.510 $\times 10^{-2}$ | |
| 128 | -0.625 | -0.563 | | -2.010 | -1.843 | | -2.736 | -2.508 | | -3.240 | -2.970 | |
| | -0.500 | -0.438 | | -1.675 | -1.508 | | -2.280 | -2.052 | | -2.700 | -2.430 | |
| | -0.375 | -0.313 | | -1.340 | -1.173 | | -1.824 | -1.596 | | -2.160 | -1.890 | |
| 256 | -0.250 | -0.188 | | -1.005 | -0.838 | | -1.368 | -1.140 | | -1.620 | -1.350 | |
| | -0.125 | -0.063 | | -0.670 | -0.503 | | -0.912 | -0.684 | | -1.080 | -0.810 | |
| | 0.000 | 0.063 | | -0.335 | -0.168 | | -0.456 | -0.228 | | -0.540 | -0.270 | |
| 512 | [0.125] | 0.188 | | 0.000 | 0.168 | | 0.000 | 0.228 | | 0.000 | 0.270 | |
| | 0.250 | 0.313 | | 0.335 | 0.503 | | 0.456 | 0.684 | | 0.540 | 0.810 | |
| | 0.375 | 0.438 | | 1.005 | 1.173 | | 0.912 | 1.140 | | 1.080 | 1.350 | |
| 1024 | 0.500 | 0.563 | | 1.340 | 1.508 | | 1.368 | 1.596 | | 1.620 | 1.890 | |
| | 0.625 | 0.688 | | 1.675 | 1.843 | | 2.280 | 2.508 | | 2.160 | 2.430 | |
| | 0.750 | 0.813 | | 2.010 | 2.178 | | 2.736 | 2.964 | | 3.240 | 3.510 | |
| 2048 | 0.875 | 0.938 | | 2.345 | 2.513 | | 3.192 | 3.420 | | 3.780 | 4.050 | |
| | 1.000 | | | 2.680 | | | 3.648 | | | 4.320 | | |

Source: Max, J., *IRE Trans. Inform. Theory*, 6, 7-12, 1960; Paez, M.D. and Glisson, T.H., *IEEE Trans. Comm.*, 20, 225-230, 1972.

Note: The Numbers enclosed in rectangles are the step sizes.

2.3 Nonuniform Quantization

It is not difficult to see that, except for the special case of the uniformly distributed input variable x , the optimum (minimum MSE, also denoted sometimes by MMSE) quantizers should be nonuniform. Consider a case in which the input random variable obeys the Gaussian distribution with a zero mean and unit variance, and the number of reconstruction levels is finite. We naturally consider that having decision levels more densely located around the middle of the x -axis, $x = 0$ (high probability density region), and choosing decision levels more coarsely distributed in the range far away from the center of the x -axis (low probability density region) will lead to less MSE. The strategy adopted here is analogous to the superiority of VLC over fixed-length code discussed in the previous chapter.

2.3.1 Optimum (Nonuniform) Quantization

Conditions of optimum quantization were discussed in [Section 2.2.2](#). With some constraints these conditions were solved in a closed form (Panter and Dite 1951). The equations characterizing these conditions, however, cannot be solved in a closed form in general. Lloyd and Max proposed an iterative procedure to numerically solve the equations. The optimum quantizers thus designed are called Lloyd-Max quantizers.

The solution to optimum quantizer design for finitely many reconstruction levels N when input x obeys Gaussian distribution was obtained (Lloyd 1957, 1982, Max 1960). That is, the decision levels and reconstruction levels together with theoretical minimum MSE and optimum SNR have been determined. Following this procedure, the designs for Laplacian and Gamma distribution were tabulated in Paez and Glisson (1972). These results are contained in [Table 2.2](#). As stated before, we see in the table once again, that uniform quantization is optimal if the input x is a uniform random variable.

[Figure 2.9](#) (Max 1960) gives a performance comparison between optimum uniform quantization and optimum quantization for the case of a Gaussian-distributed input with a zero mean and unit variance. The abscissa represents the number of reconstruction levels, N , and the ordinate the ratio between the error of the optimum quantizer and the error of the optimum uniform quantizer. It can be seen that when N is small, the ratio is close to one. That is, the performances are close. When N increases, the ratio decreases. Specifically, when N is large the nonuniform quantizer is about 20% to 30% more efficient than the uniform optimum quantizer for the Gaussian distribution with a zero mean and unit variance.

2.3.2 Companding Quantization

It is known that a speech signal usually has a large dynamic range. Moreover, its statistical distribution reveals that very low speech volumes predominate in most voice communications. Specifically, by a 50% chance, the voltage characterizing detected speech energy is less than 25% of the root mean square (rms) value of the signal. Large amplitude values are rare: only by a 15% chance does the voltage exceed the rms value (Sklar 1988). These statistics naturally lead to the need for nonuniform quantization with relatively dense decision levels in the small magnitude range and relatively coarse decision levels in the large magnitude range.

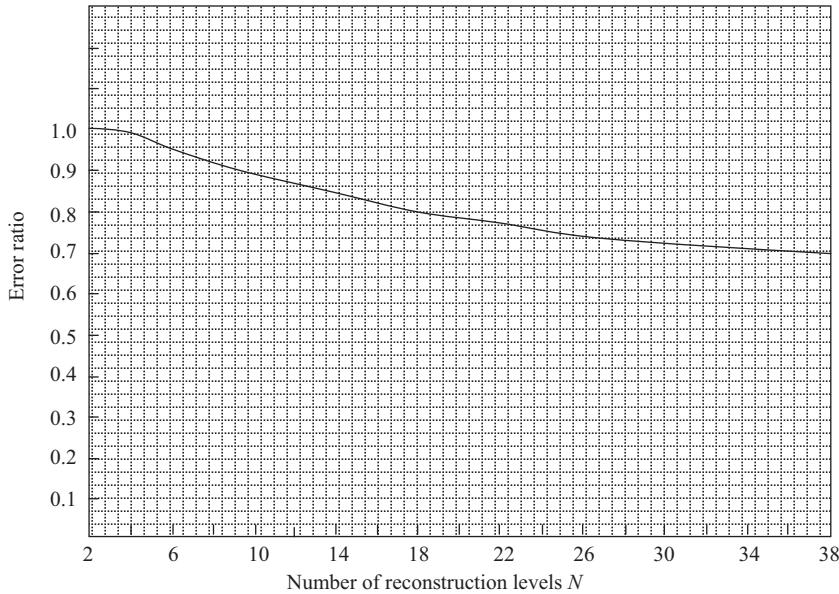
When the bit rate is eight bits/sample, the following companding technique (Smith 1957), which realizes nonuniform quantization, is found to be extremely useful. Though speech

TABLE 2.2

Optimal Symmetric Quantizer for Uniform, Gaussian, Laplacian, and Gamma Distributions (The Uniform Distribution is between $[-1, 1]$, the Other Three Distributions Have Zero Mean and Unit Variance)

| N | Uniform | | | Gaussian | | | Laplacian | | | Gamma | | |
|-----|---------|----------|--------------------------|-----------|--------|--------------------------|-----------|--------|--------------------------|-----------|--------|--------------------------|
| | d_i | y_i | MSE | d_i | y_i | MSE | d_i | y_i | MSE | d_i | y_i | MSE |
| 2 | -1.000 | -0.500 | 8.33 $\times 10^{-2}$ | $-\infty$ | -0.799 | 0.363 | $-\infty$ | -0.707 | 0.500 | $-\infty$ | -0.577 | 0.668 |
| | 0.000 | 0.500 | ∞ | 0.000 | 0.799 | ∞ | 0.000 | 0.707 | 0.500 | 0.000 | 0.577 | |
| | 1.000 | ∞ | | | | | | | | | | |
| | -1.000 | -0.750 | 2.08 $\times 10^{-2}$ | $-\infty$ | -1.510 | 0.118 | $-\infty$ | -1.834 | 1.76510 $^{-1}$ | $-\infty$ | -2.108 | 0.233 |
| 4 | -1.000 | -0.250 | 0.08 $\times 10^{-2}$ | -0.982 | -0.453 | ∞ | -1.127 | -0.420 | 0.420 | -1.205 | -0.302 | |
| | -0.500 | 0.250 | ∞ | 0.000 | 0.453 | ∞ | 0.000 | 0.420 | 0.000 | 0.000 | 0.302 | |
| | 0.000 | ∞ | | -0.982 | 1.510 | ∞ | 1.127 | 1.834 | ∞ | 1.205 | 2.108 | |
| | 0.500 | 0.750 | | | | | | | | | | |
| 8 | 1.000 | ∞ | | | | | | | | | | |
| | -1.000 | -0.875 | 5.21 $\times 10^{-3}$ | $-\infty$ | -2.152 | 3.45 $\times 10^{-2}$ | $-\infty$ | -3.087 | 5.48 $\times 10^{-2}$ | $-\infty$ | -3.799 | 7.12 $\times 10^{-2}$ |
| | -0.750 | -0.625 | ∞ | -1.748 | -1.344 | ∞ | -2.377 | -1.673 | ∞ | -2.872 | -1.944 | |
| | -0.500 | -0.375 | ∞ | -1.050 | -0.756 | ∞ | -1.253 | -0.833 | ∞ | -1.401 | -0.859 | |
| 16 | -0.250 | -0.125 | ∞ | -0.501 | -0.245 | ∞ | -0.533 | -0.233 | ∞ | -0.504 | -0.149 | |
| | 0.000 | 0.125 | ∞ | 0.000 | 0.245 | ∞ | 0.000 | 0.233 | ∞ | 0.000 | 0.149 | |
| | 0.250 | 0.375 | ∞ | 0.501 | 0.756 | ∞ | 0.533 | 0.833 | ∞ | 0.504 | 0.859 | |
| | 0.500 | 0.625 | ∞ | 1.050 | 1.344 | ∞ | 1.253 | 1.673 | ∞ | 1.401 | 1.944 | |
| 32 | 0.750 | 0.875 | ∞ | 1.748 | 2.152 | ∞ | 2.377 | 3.087 | ∞ | 2.872 | 3.799 | |
| | 1.000 | ∞ | | | | | | | | | | |
| | -1.000 | -0.938 | 1.30 $\times 10^{-3}$ | $-\infty$ | -2.733 | 9.50 $\times 10^{-3}$ | $-\infty$ | -4.316 | 1.54 $\times 10^{-2}$ | $-\infty$ | -6.085 | 1.96 $\times 10^{-2}$ |
| | -0.875 | -0.813 | ∞ | -2.401 | -2.069 | ∞ | -3.605 | -2.895 | ∞ | -5.050 | -4.015 | |
| 64 | -0.750 | -0.688 | ∞ | -1.844 | -1.618 | ∞ | -2.499 | -2.103 | ∞ | -3.407 | -2.798 | |
| | -0.625 | -0.563 | ∞ | -1.437 | -1.256 | ∞ | -1.821 | -1.540 | ∞ | -2.372 | -1.945 | |
| | -0.500 | -0.438 | ∞ | -1.099 | -0.942 | ∞ | -1.317 | -1.095 | ∞ | -1.623 | -1.300 | |
| | -0.375 | -0.313 | ∞ | -0.800 | -0.657 | ∞ | -0.910 | -0.726 | ∞ | -1.045 | -0.791 | |
| 128 | -0.250 | -0.188 | ∞ | -0.522 | -0.388 | ∞ | -0.566 | -0.407 | ∞ | -0.588 | -0.386 | |
| | -0.125 | -0.063 | ∞ | -0.258 | -0.128 | ∞ | -0.266 | -0.126 | ∞ | -0.229 | -0.072 | |
| | 0.000 | 0.063 | ∞ | 0.000 | 0.128 | ∞ | 0.000 | 0.126 | ∞ | 0.000 | 0.072 | |
| | 0.125 | 0.188 | ∞ | 0.258 | 0.388 | ∞ | 0.266 | 0.407 | ∞ | 0.229 | 0.386 | |
| 256 | 0.250 | 0.313 | ∞ | 0.522 | 0.657 | ∞ | 0.566 | 0.726 | ∞ | 0.588 | 0.791 | |
| | 0.375 | 0.438 | ∞ | 0.800 | 0.942 | ∞ | 0.910 | 1.095 | ∞ | 1.045 | 1.300 | |
| | 0.500 | 0.563 | ∞ | 1.099 | 1.256 | ∞ | 1.317 | 1.540 | ∞ | 1.623 | 1.945 | |
| | 0.625 | 0.688 | ∞ | 1.437 | 1.618 | ∞ | 1.821 | 2.103 | ∞ | 2.372 | 2.798 | |
| 512 | 0.750 | 0.813 | ∞ | 1.844 | 2.069 | ∞ | 2.499 | 2.895 | ∞ | 3.407 | 4.015 | |
| | 0.875 | 0.938 | ∞ | 2.401 | 2.733 | ∞ | 3.605 | 4.316 | ∞ | 5.050 | 6.085 | |
| | 1.000 | ∞ | | | | | | | | | | |

Source: Lloyd, S.P., *Least Squares Quantization in PCM*, Institute of Mathematical Statistics Meeting, Atlantic City, NJ, 1957; Lloyd, S.P., IEEE Trans. Inform. Theory, 28, 129-136, 1982; Max, J., IRE Trans. Inform. Theory, 6, 7-12, 1960; Paez, M.D. and Glisson, T.H., IEEE Trans. Comm., 20, 225-230, 1972.

**FIGURE 2.9**

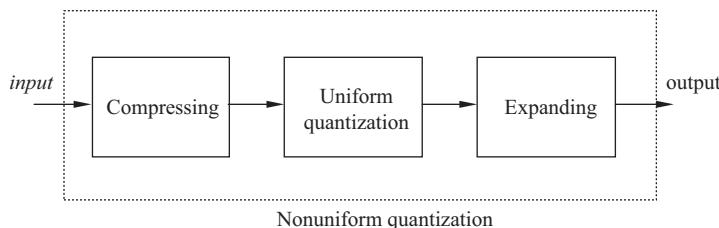
Ratio of error for optimal quantizer to error for optimum uniform quantizer vs. number of reconstruction levels N . (Minimum MSE for Gaussian distributed input with a zero mean and unit variance). (Data from Max, J., *IRE Trans. Inform. Theory*, 6, 7–12, 1960.)

coding is not the main focus of this book, we briefly discuss the companding technique here as an alternative way to achieve nonuniform quantization.

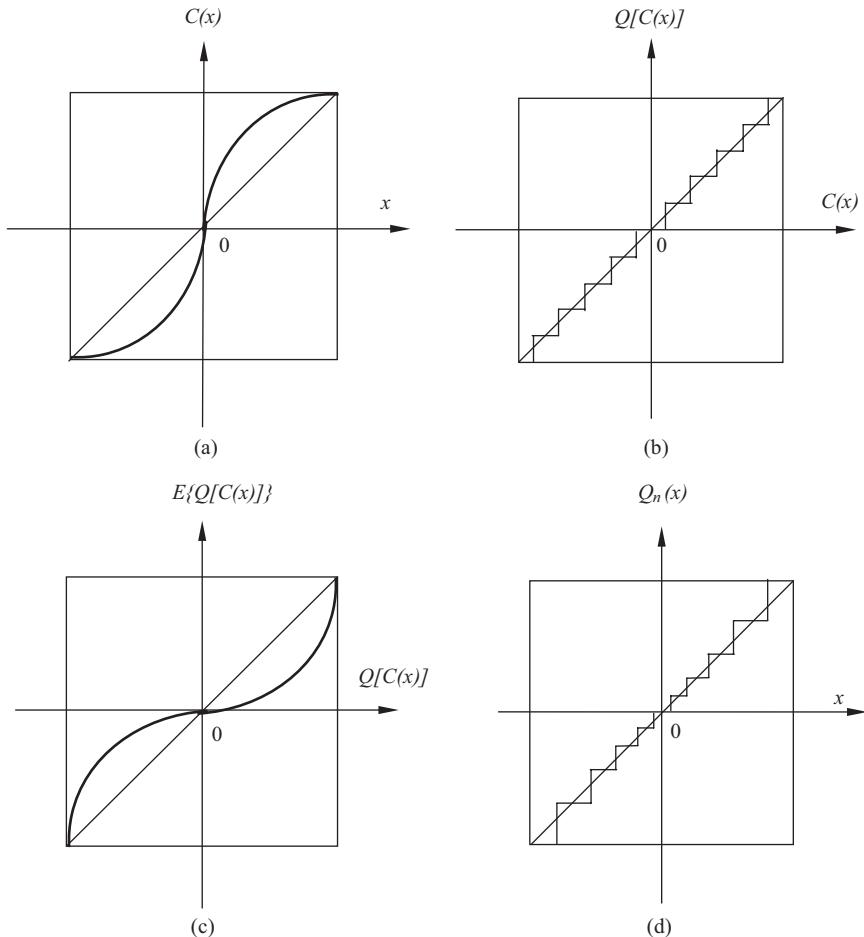
The companding technique, also known as logarithmic quantization, consists of the following three stages: compressing, uniform quantization, and expanding (Gersho 1977), as shown in Figure 2.10. It first compresses the input signal with a logarithmic characteristic, and then it quantizes the compressed input using a uniform quantizer. Finally, the uniformly quantized results are expanded inversely. An illustration of the characteristics of these three stages and the resultant nonuniform quantization are shown in Figure 2.11.

In practice, a piecewise linear approximation of the logarithmic compression characteristic is used. There are two different ways. In North America, a μ -law compression characteristic is used, which is defined as follows.

$$c(x) = x_{\max} \frac{\ln[1 + \mu(|x| / x_{\max})]}{\ln(1 + \mu)} \operatorname{sgn} x, \quad (2.16)$$

**FIGURE 2.10**

Companding technique in achieving quantization.

**FIGURE 2.11**

Characteristics of companding techniques. (a) Compressing characteristic, (b) Uniform quantizer characteristic, (c) Expanding characteristic, and (d) Nonuniform quantizer characteristic.

where sgn is a sign function defined as

$$\text{sgn } x = \begin{cases} +1 & \text{if } x \geq 0 \\ -1 & \text{if } x < 0 \end{cases} \quad (2.17)$$

The μ -law compression characteristic is shown in [Figure 2.12a](#). The standard value of μ is 255. Note from the figure that the case of $\mu = 0$ corresponds to uniform quantization.

In Europe, the A-law characteristic is used. The A-law characteristic is depicted in [Figure 2.12b](#) and is defined as follows.

$$c(x) = \begin{cases} x_{\max} \frac{A(|x|/x_{\max})}{1+\ln A} \text{sgn } x & 0 < \frac{|x|}{x_{\max}} \leq \frac{1}{A} \\ x_{\max} \frac{1+\ln[A(|x|/x_{\max})]}{1+\ln A} \text{sgn } x & \frac{1}{A} < \frac{|x|}{x_{\max}} < 1 \end{cases} \quad (2.18)$$

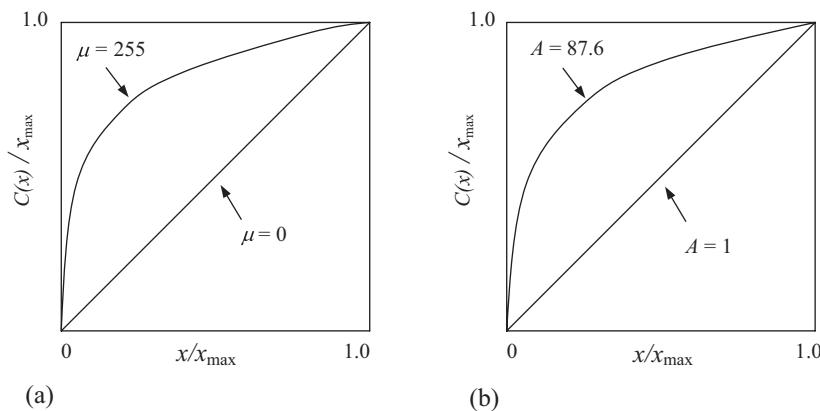


FIGURE 2.12
Compression characteristics (a) μ law and (b) A law.

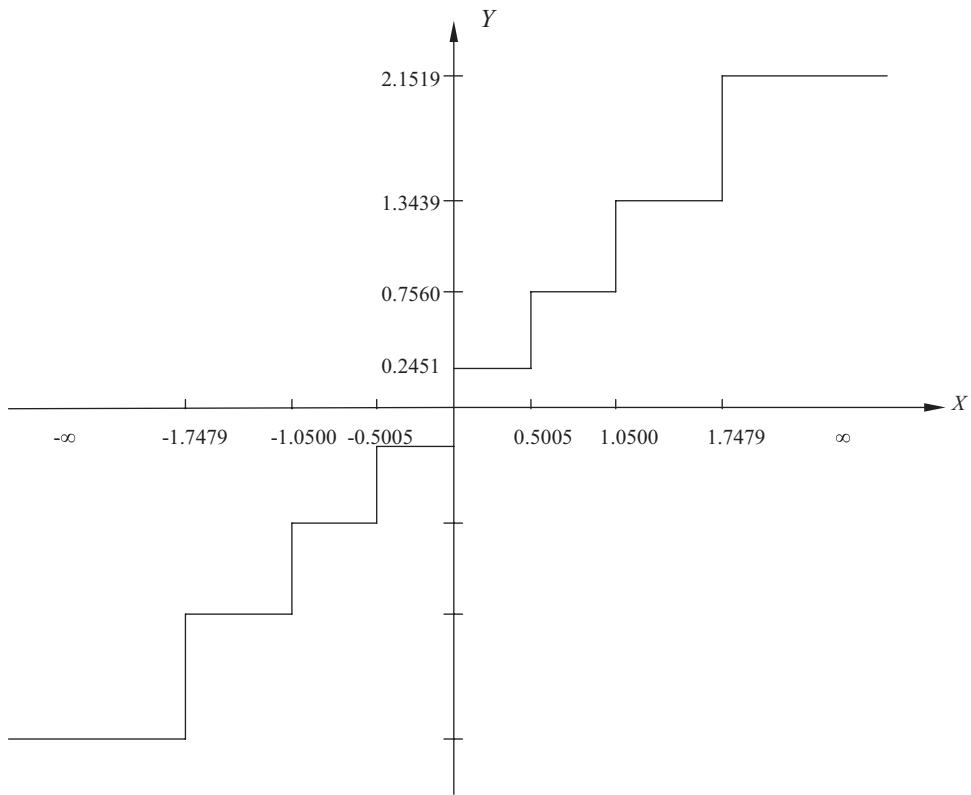
It is noted that the standard value of A is 87.6. The case of $A = 1$ corresponds to uniform quantization.

2.4 Adaptive Quantization

In the previous section, we studied nonuniform quantization, whose motivation is to minimize mean square quantization error MSE_q . We found that nonuniform quantization is necessary if the *pdf* of the input random variable x is not uniform. Consider an optimum quantizer for a Gaussian distributed input when the number of reconstruction levels N is eight. Its input-output characteristic can be derived from Table 2.2 and is shown in Figure 2.13. This curve reveals that the decision levels are densely located in the central region of the x -axis and coarsely elsewhere. In other words, the decision levels are densely distributed in the region having a higher probability of occurrence and coarsely distributed in other regions. A logarithmic companding technique also allocates decision levels densely in the small magnitude region, which corresponds to a high occurrence probability, but in a different way. We conclude that nonuniform quantization achieves minimum mean square quantization error by distributing decision levels according to the statistics of the input random variable.

These two types of nonuniform quantizers are both time-invariant. That is, they are not designed for nonstationary input signals. Moreover, even for a stationary input signal, if its *pdf* deviates from that with which the optimum quantizer is designed, then what is called *mismatch* will take place and the performance of the quantizer will deteriorate. There are two main types of mismatch. One is called variance mismatch. That is, the *pdf* of input signal is matched, while the variance is mismatched. Another type is *pdf* mismatch. Noted that these two kinds of mismatch also occur in optimum uniform quantization, since there the optimization is also achieved based on the input statistics assumption. For a detailed analysis of the effects of the two types of mismatch on quantization, readers are referred to Jayant and Noll (1984).

Adaptive quantization attempts to make the quantizer design adapt to the varying input statistics in order to achieve better performance. It is a means to combat the mismatch

**FIGURE 2.13**

Input-output characteristic of the optimal quantizer for Gaussian distribution with zero mean, unit variance, and $N = 8$.

problem discussed above. By statistics, we mean the statistic mean, variance (or the dynamic range), and type of input *pdf*. When the mean of the input changes, differential coding (discussed in the next chapter) is a suitable method to handle the variation. For other types of cases, adaptive quantization is found to be effective. The price paid in adaptive quantization is processing delay and an extra storage requirement, as seen below.

There are two different types of adaptive quantization: forward adaptation and backward adaptation. Before we discuss these, however, let us describe an alternative way to define quantization (Jayant and Noll 1984). Look at [Figure 2.14](#). Quantization can be viewed as a two-stage process. The first stage is the quantization encoder and the second stage is the quantization decoder. In the encoder, the input to quantization is converted to the index of an interval into which the input x falls. This index is mapped to (the codeword that represents) the reconstruction level corresponding to the interval in the decoder. Roughly speaking, this definition considers a quantizer as a communication system in which the quantization encoder is in the transmitter side while the quantization decoder is in the receiver side. In this sense, this definition is broader than that of quantization defined in [Figure 2.3a](#).

2.4.1 Forward Adaptive Quantization

A block diagram of forward adaptive quantization is shown in [Figure 2.15](#). There, the input to the quantizer, x , is first split into blocks, each with a certain length. Blocks are

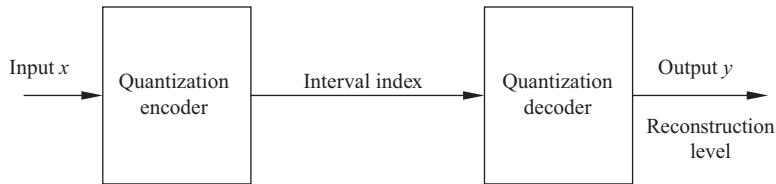


FIGURE 2.14
A two-stage model of quantization.

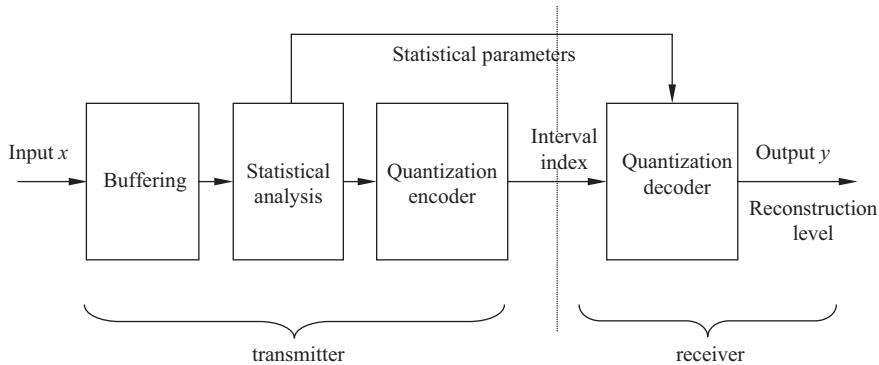


FIGURE 2.15
Forward adaptive quantization.

stored in a buffer one at a time. A statistical analysis is then carried out with respect to the block in the buffer. Based on the analysis, the quantization encoder is set up, and the input data within the block are assigned indexes of respective intervals. In addition to these indexes, the encoder setting parameters are sent to the quantization decoder as *side* information. The term *side* comes from the fact that the number of bits used for coding the setting parameter is usually a small fraction of the total number of bits used.

The selection of block size is a critical issue. If the size is small, the adaptation to the local statistics will be effective, but the side information needs to be sent frequently. That is, more bits are used for sending the side information. If the size is large, the bits used for side information decrease. On the other hand, the adaptation becomes less sensitive to changing statistics, and both processing delay and storage required increase. In practice, a proper compromise between quantity of side information and effectiveness of adaptation produces a good selection of the block size.

Examples of using forward manner to adapt quantization to a changing input variance (to combat variance mismatch) can be found in Jayant and Noll (1984) and Sayood (1996).

2.4.2 Backward Adaptive Quantization

Figure 2.16 shows a block diagram of backward adaptive quantization. A close look at the block diagram reveals that in both the quantization encoder and decoder the buffering and the statistical analysis are carried out with respect to the output of quantization encoder. In this way, there is no need to send side information. The sensitivity of adaptation to the changing statistics will be degraded, however, since, instead of the original input, only is the output of the quantization encoder used in the statistical analysis. That is, the quantization noise is involved in the statistical analysis.

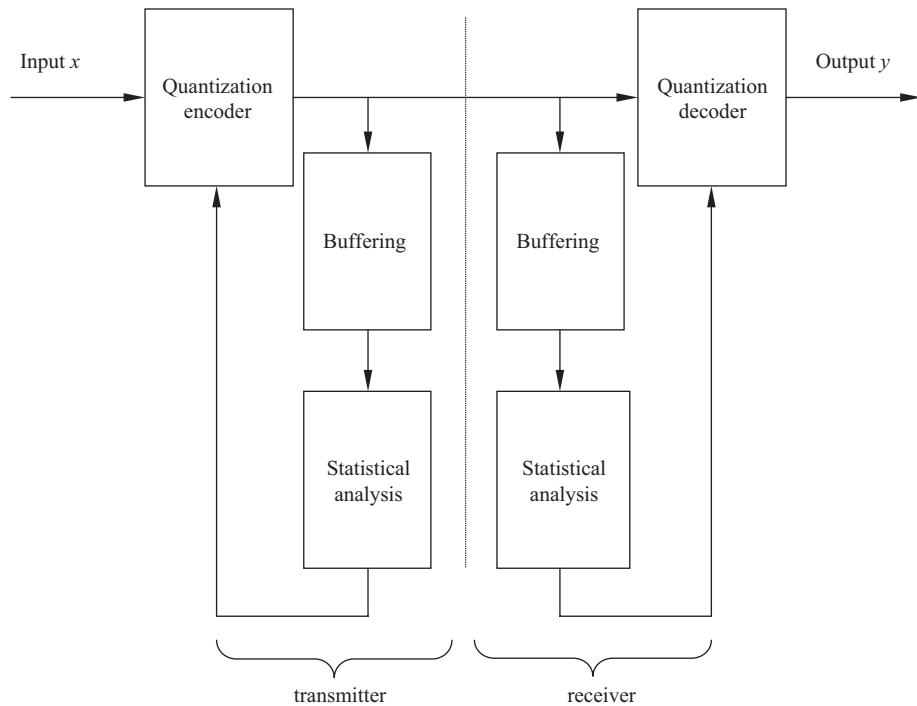


FIGURE 2.16
Backward adaptive quantization.

2.4.3 Adaptive Quantization with a One-Word Memory

Intuitively, it is expected that observing a sufficient large number of input or output (quantized) data is necessary in order to track the changing statistics and then adapt the quantizer setting in adaptive quantization. Through an analysis, Jayant showed that effective adaptations can be realized with an explicit memory of only one word. That is, either one input sample, x , in forward adaptive quantization or a quantized output, y , in backward adaptive quantization is sufficient (Jayant 1973).

In Jayant and Noll (1984), examples on step size adaptation (with the number of total reconstruction levels larger than four) were given. The idea is as follows. If at moment t_i the input sample x_i falls into the outer interval, then the step size at the next moment t_{i+1} will be enlarged by a factor of m_i (multiplying the current step size by m_i , $m_i > 1$). On the other hand, if the input x_i falls into an inner interval close to $x = 0$ then, the multiplier is less than 1, i.e., $m_i < 1$. That is, the multiplier m_i is small in the interval near $x = 0$ and monotonically increases for an increased x . Its range varies from a small positive number less than 1 to a number larger than 1. In this way, the quantizer adapts itself to the input to avoid *overload* as well as *underload* to achieve better performance.

2.4.4 Switched Quantization

This is another adaptive quantization scheme. A block diagram is shown in Figure 2.17. It consists of a bank of L quantizers. Each quantizer in the bank is fixed, but collectively they form a bank of quantizers with a variety of input-output characteristics. Based on a statistical analysis of recent input or output samples, a switch connects the current input to one

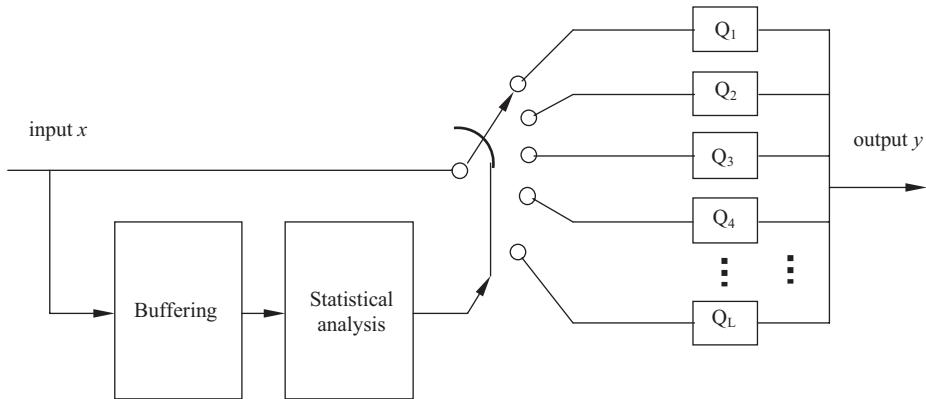


FIGURE 2.17
Switched quantization.

of the quantizers in the bank such that the best possible performance may be achieved. It is reported that in both video and speech applications, this scheme has shown improved performance even when the number of quantizers in the bank, L , is two (Jayant and Noll 1984). Interestingly, it is noted that as $L \rightarrow \infty$, the switched quantization converges to the adaptive quantizer discussed above.

2.5 PCM

PCM is closely related to quantization, the focus of this chapter. Furthermore, as pointed in Jayant and Noll (1984), PCM is the earliest, best established, and most frequently applied coding system despite the fact that it is the most bit-consuming digitizing system (since it encodes each pixel independently) as well as a very demanding system in terms of bit error rate on the digital channel. Therefore, we discuss the PCM technique in this section.

PCM is now the most important form of pulse modulation. The other forms of pulse modulation are pulse amplitude modulation (PAM), pulse width modulation (PWM), and pulse position modulation (PPM), which are covered in most communication texts. Briefly speaking, pulse modulation links an analog signal to a pulse train in the following way. The analog signal is first sampled (a discretization in time domain). The sampled values are used to modulate a pulse train. If the modulation is carried out through the amplitude of the pulse train, it is called PAM. If the modified parameter of the pulse train is the pulse width, we then have PWM. If the pulse width and magnitude are constant—only the position of pulses is modulated by the sample values—we then encounter PPM. An illustration of these pulse modulations is shown in [Figure 2.18](#).

In PCM, an analog signal is first sampled. The sampled value is then quantized. Finally, the quantized value is encoded, resulting in a bit stream. [Figure 2.19](#) provides an example of PCM. We see that through a sampling and a uniform quantization the PCM system

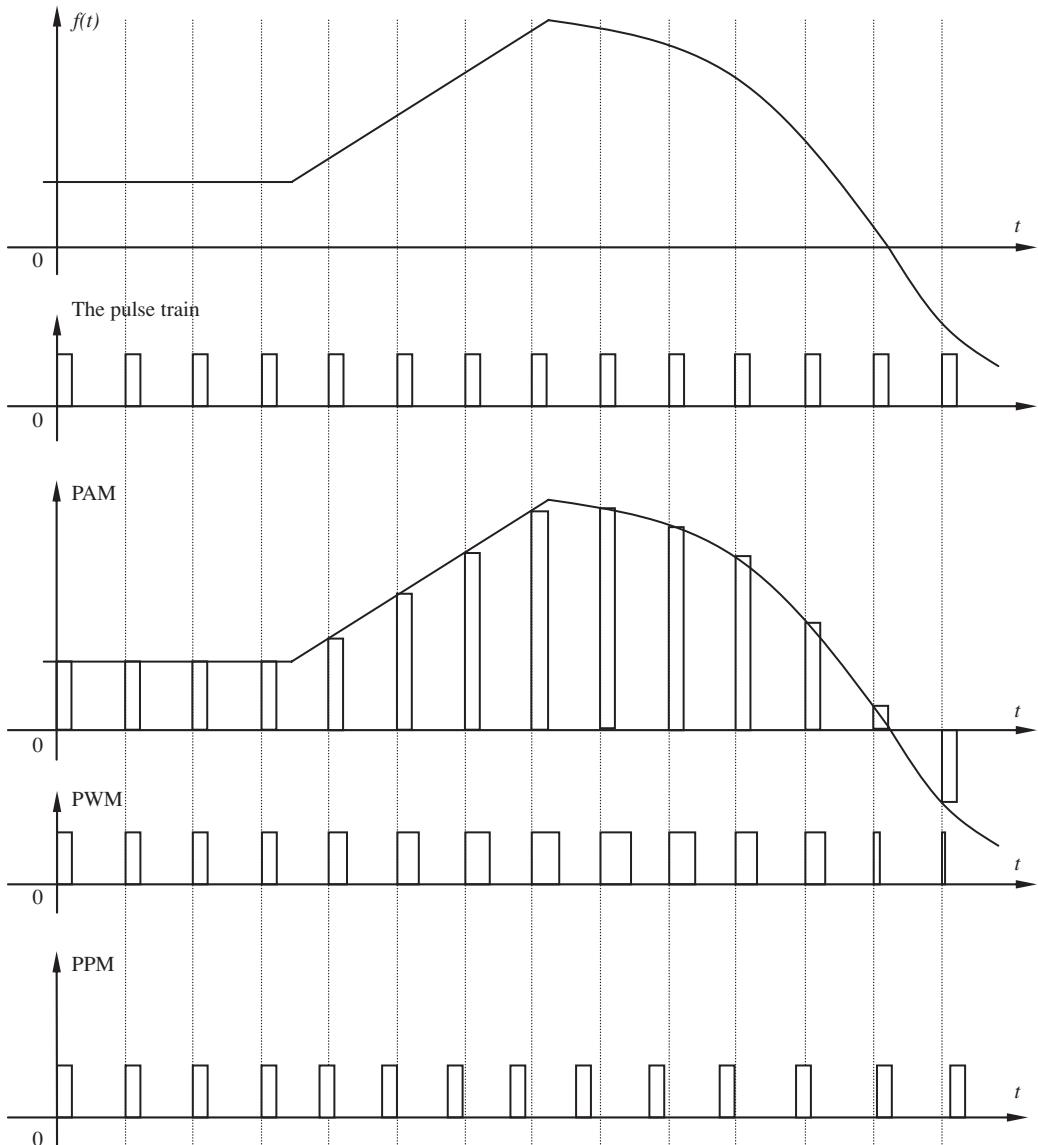


FIGURE 2.18
Pulse modulation.

converts the input analog signal, which is continuous in both time and magnitude, into a digital signal (discretized in both time and magnitude) in the form of an NBC sequence. In this way, an analog signal modulates a pulse train with an NBC.

By far, PCM is more popular than other types of pulse modulation since the *code* modulation is much more robust against various noises than amplitude modulation, width modulation, and position modulation. In fact, almost all coding techniques include a PCM

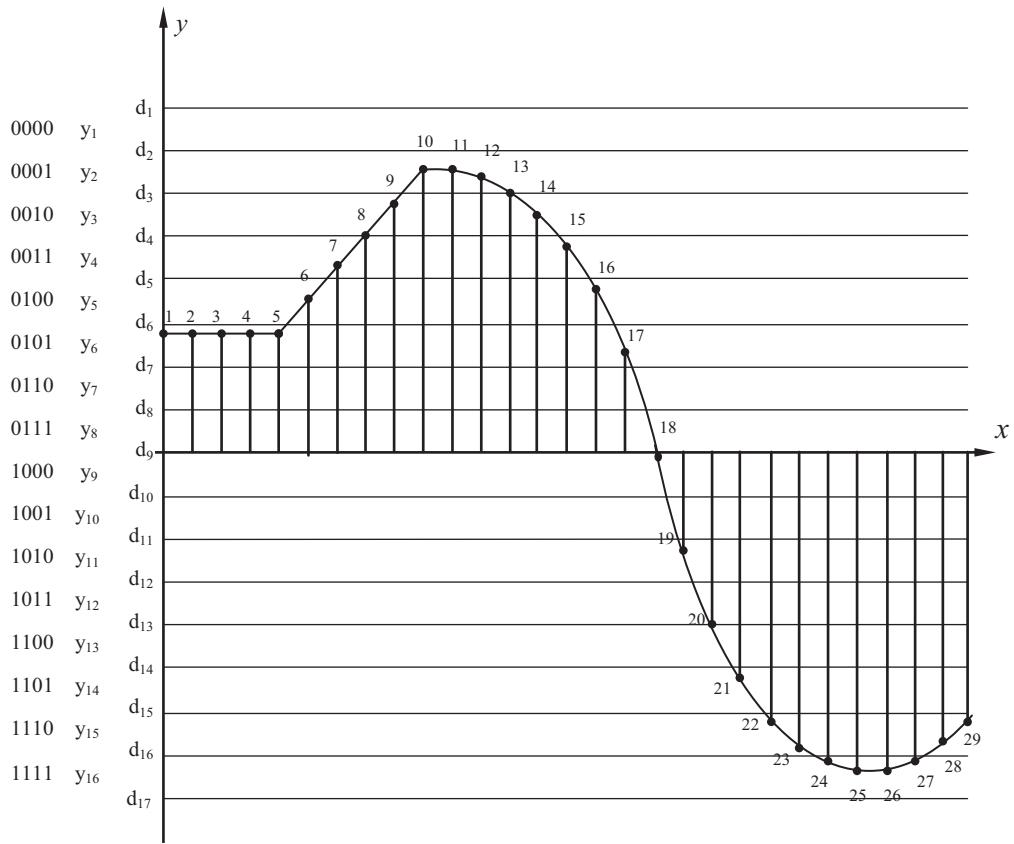


FIGURE 2.19
PCM.

component. In digital image processing, given digital images usually appear in PCM format. It is known that an acceptable PCM representation of monochrome picture requires six to eight bits per pixel (Huang 1965). It is used so commonly in practice that its performance normally serves as a standard against which other coding techniques are compared.

Recall the false contouring phenomenon discussed in [Chapter 1](#), when we discussed texture masking. It states that our eyes are more sensitive to relatively uniform regions in an image plane. If the number of reconstruction levels is not large enough (coarse quantization), then some unnatural contours will appear. When frequency masking was discussed, it was noted that by adding some high-frequency signal before quantization, the false contouring can be eliminated to a great extent. This technique is called dithering. The high-frequency signal used is referred to as a dither signal. Both false contouring and dithering were first reported in Goodall (1951).

2.6 Summary

Quantization is a process in which a quantity having possibly infinitely many values is converted to another quantity having only finitely many values. It is an important element in source encoding that has significant impact on both bit rate and distortion of reconstructed images and video in visual communication systems. Depending on whether the quantity is a scalar or a vector, quantization is called either scalar quantization or vector quantization. In this chapter, we considered only scalar quantization.

Uniform quantization is the simplest and yet the most important case. In uniform quantization, except for outer intervals, both decision levels and reconstruction levels are uniformly spaced. Moreover, a reconstruction level is the arithmetic average of the two corresponding decision levels. In uniform quantization design, the step size is usually the only parameter that needs to be specified.

Optimum quantization implies minimization of the mean square quantization error. When the input has a uniform distribution, uniform quantization is optimum. For the sake of simplicity, a uniform optimum quantizer is sometimes desired even when the input does not obey uniform distribution. The design under these circumstances involves an iterative procedure. The design problem in cases where the input has Gaussian, Laplacian, or Gamma distribution was solved and the parameters are available.

When the constraint of uniform quantization is removed, the conditions for optimum quantization are derived. The resultant optimum quantizer is normally nonuniform. An iterative procedure to solve the design is established and the optimum design parameters for Gaussian, Laplacian, and Gamma distribution are tabulated.

The companding technique is an alternative way to implement nonuniform quantization. Both nonuniform quantization and companding are time-invariant and hence not suitable for nonstationary input. Adaptive quantization deals with nonstationary input and combats the mismatch that occurs in optimum quantization design.

In adaptive quantization, buffering is necessary to store some recent input or sampled output data. A statistical analysis is carried out with respect to the stored recent data. Based on the analysis, the quantizer's parameters are adapted to changing input statistics to achieve better quantization performance. There are two types of adaptive quantization: forward and backward adaptive quantization. With the forward type, the statistical analysis is derived from the original input data, while with the backward type, quantization noise is involved in the analysis. Therefore, the forward manner usually achieves more effective adaptation than the backward manner. The latter, however, does not need to send quantizer-setting parameters as side information to the receiver side, since the output values of quantization encoder (based on which the statistics are analyzed and quantizer's parameters are adapted) are available in both the transmitter and receiver sides.

Switched quantization is another type of adaptive quantization. In this scheme, a bank of fixed quantizers is utilized, each quantizer having different input-output characteristics. A statistical analysis based on recent input decides which quantizer in the bank is suitable for the present input. The system then connects the input to this particular quantizer.

Nowadays, PCM is the most frequently used form of pulse modulation due to its robustness against noise. PCM consists of three stages: sampling, quantization, and encoding. Analog signals are first sampled with a proper sampling frequency. The sampled data are then quantized using a uniform quantizer. Finally, the quantized values are encoded with NBC. It is the best-established and most-applied coding system. Despite its bit-consuming feature, it is utilized in almost all coding systems.

Exercises

- 2.1 Using your own words, define quantization and uniform quantization. What are the two features of uniform quantization?
 - 2.2 What is optimum quantization? Why is uniform quantization sometimes desired, even when the input has a *pdf* different from uniform? How was this problem solved? Draw an input-output characteristic of an optimum uniform quantizer with an input obeying Gaussian *pdf* having zero mean, unit variance, and the number of reconstruction levels, N , equal to 8.
 - 2.3 What are the conditions of optimum nonuniform quantization? From [Table 2.2](#), what observations can you make?
 - 2.4 Define variance mismatch and *pdf* mismatch. Discuss how you can resolve the mismatch problem.
 - 2.5 What is the difference between forward and backward adaptive quantization? Comment on the merits and drawbacks for each.
 - 2.6 What are PAM, PWM, PPM, and PCM? Why is PCM the most popular type of pulse modulation?
-

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3

Differential Coding

Instead of encoding a signal directly, the *differential coding* technique codes the difference between the signal itself and its prediction. Therefore, it is also known as *predictive coding*. By utilizing spatial and/or temporal interpixel correlation, differential coding is an efficient and yet computationally simple coding technique. In this chapter, we first describe the differential technique in general. Two components of differential coding—prediction and quantization—are discussed. There is an emphasis on (optimum) prediction, since quantization was discussed in [Chapter 2](#). When the difference signal (also known as prediction error) is quantized, the differential coding is called differential pulse code modulation (DPCM). Some issues in DPCM are discussed, after which delta modulation (DM) as a special case of DPCM is covered. The idea of differential coding involving image sequences is briefly discussed in this chapter. More detailed coverage is presented in Parts III and IV, starting from [Chapter 10](#). If quantization is not included, the differential coding is referred to as information-preserving differential coding. This is discussed at the end of the chapter.

3.1 Introduction to DPCM

As depicted in [Figure 2.3](#), a source encoder consists of the following three components: transformation, quantization, and codeword assignment. The transformation converts input into a format for quantization followed by codeword assignment. In other words, the component of transformation decides which format of input to be encoded. As mentioned in the previous chapter, input itself is not necessarily the most suitable format for encoding.

Consider the case of monochrome image encoding. The input is usually a 2-D array of gray-level values of an image obtained via PCM coding. The concept of spatial redundancy, discussed in [Section 1.2.1.1](#), tells us that neighboring pixels of an image are usually highly correlated. Therefore, it is more efficient to encode the gray difference between two neighboring pixels instead of encoding the gray-level values of each pixel. At the receiver, the decoded difference is added back to reconstruct the gray-level value of the pixel. Since neighboring pixels are highly correlated, their gray-level values bear a great similarity. Hence, we expect that the variance of the difference signal will be smaller than that of the original signal. Assume uniform quantization and natural binary coding for the sake of simplicity. Then we see that for the same bit rate (bits per sample) the quantization error will be smaller, i.e., a higher quality of reconstructed signal can be achieved. Or, for the same quality of reconstructed signal, we need a lower bit rate.

Assume a bit rate of eight bits/sample in the quantization. We can see that although the dynamic range of the difference signal is theoretically doubled, from 256 to 512, the variance of the difference signal is actually much smaller. This can be confirmed from the histograms of the “Boy and Girl” image (refer to [Figure 1.2](#)) and its difference image obtained by horizontal pixel-to-pixel differencing, shown in [Figure 3.1a](#) and [b](#), respectively. [Figure 3.1b](#) and its close-up (c) indicate that by a rate of 42.44% the difference values fall into the range of $-1, 0$ and $+1$. In other words, the histogram of the difference signal is much more narrowly concentrated than that of the original signal.

3.1.1 Simple Pixel-to-Pixel DPCM

Denote the gray-level values of pixels along a row of an image as $z_i, i = 1, \dots, M$, where M is the total number of pixels within the row. Using the immediately preceding pixel's gray-level value, z_{i-1} , as a prediction of that of the present pixel, \hat{z}_i , i.e.,

$$\hat{z}_i = z_{i-1}, \quad (3.1)$$

we then have the difference signal

$$d_i = z_i - \hat{z}_i = z_i - z_{i-1}. \quad (3.2)$$

A block diagram of the scheme described above is shown in [Figure 3.2](#). There z_i denotes the sequence of pixels along a row, d_i is the corresponding difference signal, and \hat{d}_i is the quantized version of the difference, i.e.,

$$\hat{d}_i = Q(d_i) = d_i + e_q \quad (3.3)$$

where e_q represents quantization error. In the decoder, \bar{z}_i represents the reconstructed pixel gray value, and we have

$$\bar{z}_i = \bar{z}_{i-1} + \hat{d}_i. \quad (3.4)$$

This simple scheme, however, suffers from an accumulated quantization error. We can see this clearly from the following derivation (Sayood 1996), where we assume the initial value z_0 is available for both the encoder and the decoder.

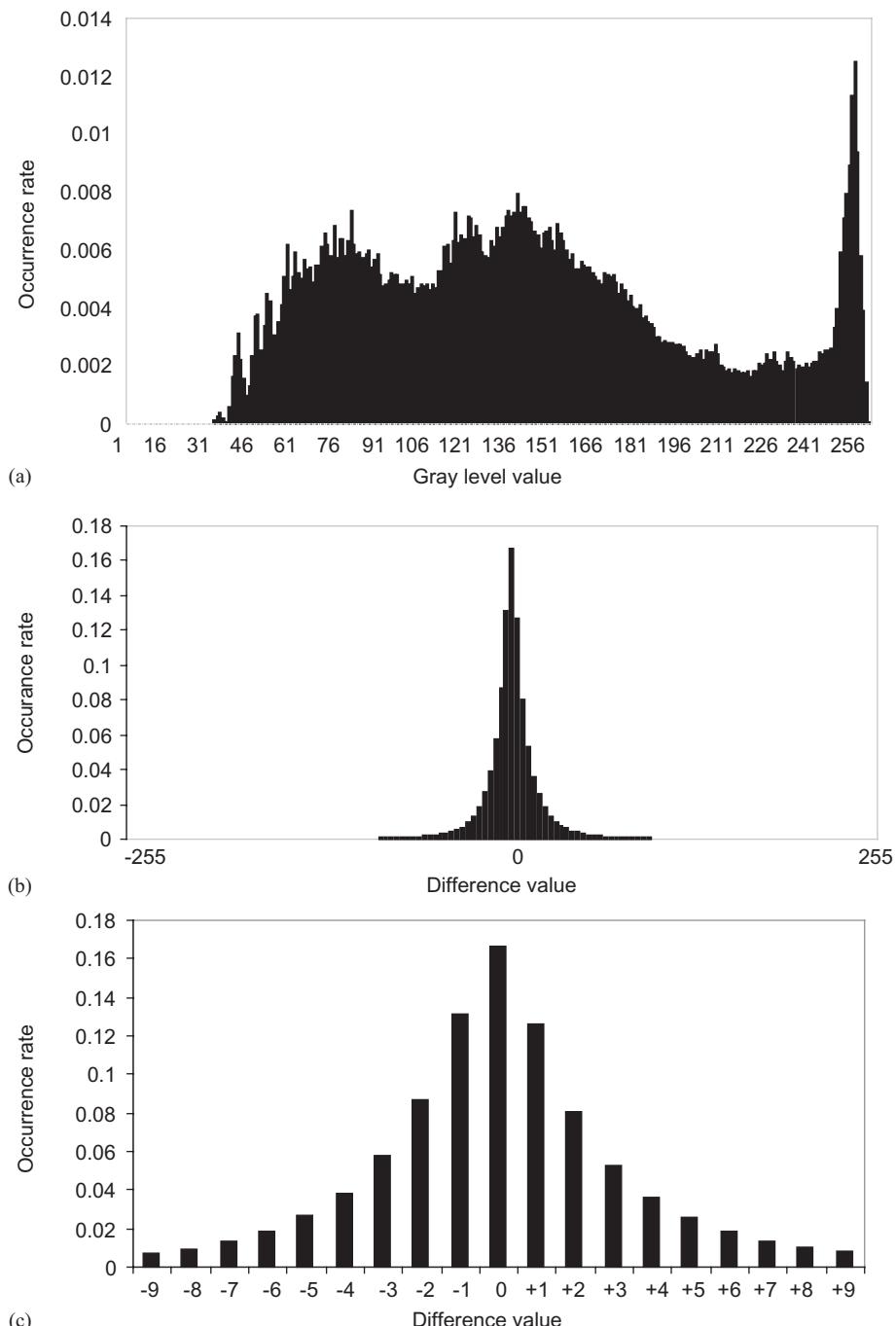
$$\text{as } i = 1, \quad d_1 = z_1 - z_0$$

$$\hat{d}_1 = d_1 + e_{q,1}$$

$$\bar{z}_1 = z_0 + \hat{d}_1 = z_0 + d_1 + e_{q,1} = z_1 + e_{q,1}. \quad (3.5)$$

Similarly, we can have

$$\text{as } i = 2, \quad \bar{z}_2 = z_2 + e_{q,1} + e_{q,2} \quad (3.6)$$

**FIGURE 3.1**

(a) Histogram of the original “Boy and Girl” image, (b) Histogram of the difference image obtained by using horizontal pixel-to-pixel differencing, and (c) A close-up of the central portion of the histogram of the difference image.

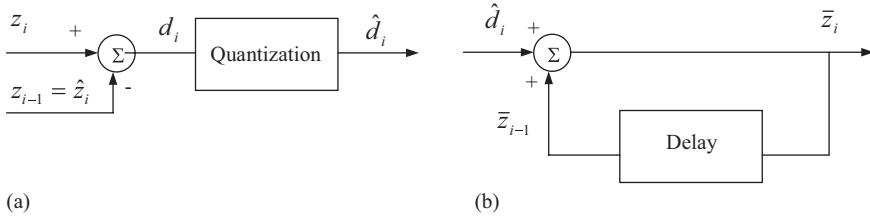


FIGURE 3.2
Block diagram of a pixel-to-pixel differential coding system (a) Encoder and (b) Decoder.

and, in general,

$$\bar{z}_i = z_i + \sum_{j=1}^i e_{q,j}. \quad (3.7)$$

This problem can be remedied by the following scheme, shown in [Figure 3.3](#). Now, we see that in both the encoder and the decoder, the reconstructed signal is generated in the same way, i.e.,

$$\bar{z}_i = \bar{z}_{i-1} + \hat{d}_i, \quad (3.8)$$

and in the encoder the difference signal changes to

$$d_i = z_i - \bar{z}_{i-1}. \quad (3.9)$$

That is, the previous reconstructed \bar{z}_{i-1} is used as the prediction, \hat{z}_i , i.e.,

$$\hat{z}_i = \bar{z}_{i-1}. \quad (3.10)$$

In this way, we have

$$\begin{aligned} \text{as } & i=1, \quad d_1 = z_1 - z_0 \\ & \hat{d}_1 = d_1 + e_{q,1} \end{aligned}$$

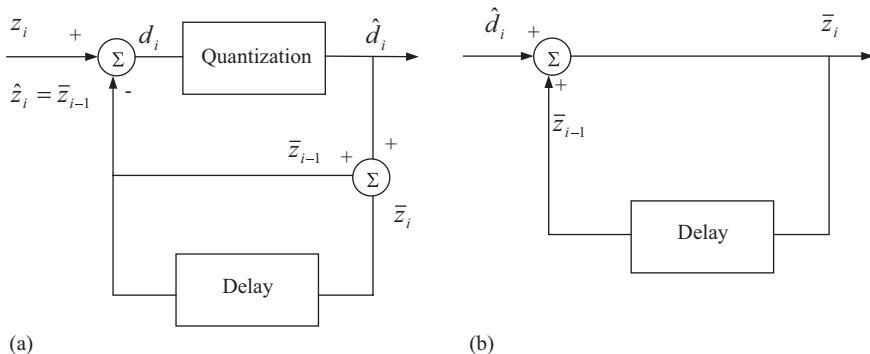


FIGURE 3.3
Block diagram of a practical pixel-to-pixel differential coding system (a) Encoder and (b) Decoder.

$$\bar{z}_1 = z_0 + \hat{d}_1 = z_0 + d_1 + e_{q,1} = z_1 + e_{q,1}. \quad (3.11)$$

Similarly, we have

$$\text{as } i = 2, \quad d_2 = z_2 - \bar{z}_1$$

$$\hat{d}_2 = d_2 + e_{q,2}$$

$$\bar{z}_2 = \bar{z}_1 + \hat{d}_2 = z_2 + e_{q,2}. \quad (3.12)$$

In general,

$$\bar{z}_i = z_i + e_{q,i}. \quad (3.13)$$

Thus, we see that the problem of quantization error accumulation has been resolved by having both the encoder and the decoder work in the same fashion, as indicated in [Figure 3.3](#), or in Equations 3.3, 3.9, and 3.10.

3.1.2 General DPCM Systems

In the above discussion, we can view the reconstructed neighboring pixel's gray value as a prediction of that of the pixel being coded. Now, we generalize this simple pixel-to-pixel DPCM. In a general DPCM system, a pixel's gray-level value is first predicted from the preceding reconstructed pixels' gray-level values. The difference between the pixel's gray-level value and the predicted value is then quantized. Finally, the quantized difference is encoded and transmitted to the receiver. A block diagram of this general differential coding scheme is shown in [Figure 3.4](#), where the codeword assignment in the encoder and its counterpart in decoder are not included.

It is noted that, instead of using the previous reconstructed sample, \bar{z}_{i-1} , as a predictor, we now have the predicted version of z_i , \hat{z}_i , as a function of the n previous reconstructed samples, $\bar{z}_{i-1}, \bar{z}_{i-2}, \dots, \bar{z}_{i-n}$. That is,

$$\hat{z}_i = f(\bar{z}_{i-1}, \bar{z}_{i-2}, \dots, \bar{z}_{i-n}). \quad (3.14)$$

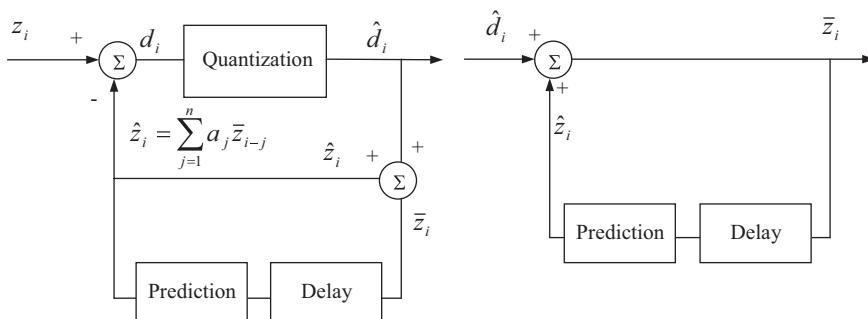


FIGURE 3.4

Block diagram of a general DPCM system.

Linear prediction, i.e., the function f in Equation 3.14, is linear, is of particular interest, and is widely used in differential coding. In linear prediction, we have

$$\hat{z}_i = \sum_{j=1}^n a_j \bar{z}_{i-j}, \quad (3.15)$$

where a_j are real parameters. Hence, we see that the simple pixel-to-pixel differential coding is a special case of general differential coding with linear prediction, i.e., $n = 1$ and $a_1 = 1$.

In [Figure 3.4](#), d_i is the difference signal and is equal to the difference between the original signal, z_i , and the prediction \hat{z}_i . That is,

$$d_i = z_i - \hat{z}_i. \quad (3.16)$$

The quantized version of d_i is denoted by \hat{d}_i . The reconstructed version of z_i is represented by \bar{z}_i , and

$$\bar{z}_i = \hat{z}_i + \hat{d}_i. \quad (3.17)$$

Note that this is true for both the encoder and the decoder. Recall that the accumulation of the quantization error can be remedied by using this method.

The difference between the original input and the predicted input is called prediction error, which is denoted by e_p . That is,

$$e_p = z_i - \hat{z}_i, \quad (3.18)$$

where the e_p is understood as the prediction error associated with the index i . Quantization error, e_q , is equal to the reconstruction error or coding error, e_r , defined as the difference between the original signal, z_i , and the reconstructed signal, \bar{z}_i , when the transmission is error free:

$$\begin{aligned} e_q &= d_i - \hat{d}_i \\ &= (z_i - \hat{z}_i) - (\bar{z}_i - \hat{z}_i) \\ &= z_i - \bar{z}_i = e_r. \end{aligned} \quad (3.19)$$

This indicates that quantization error is the only source of information loss with an error-free transmission channel.

The DPCM system depicted [Figure 3.4](#) is also called closed-loop DPCM with feedback around the quantizer (Jayant 1984). This term reflects the feature in DPCM structure.

Before we leave this section, let us take a look at the history of the development of differential image coding. According to an excellent early article on differential image coding (Musmann 1979), the first theoretical and experimental approaches to image coding involving linear prediction began in 1952 at the Bell Telephone Laboratories (Harrison 1952, Kretzmer 1952, Oliver 1952). The concepts of DPCM and DM were also developed in 1952 (Cutler 1952, DeJager 1952). Predictive coding capable of preserving information for a PCM signal was established at the Massachusetts Institute of Technology (Elias 1955).

The differential coding technique has played an important role in image and video coding. In the international coding standard for still images, JPEG, which is covered in [Chapter 7](#), we can see that the differential coding is used in lossless mode and in DCT-based

mode for coding DC coefficients. Motion-compensated (MC) coding has been a major development in video coding since 1980s and has been adopted by all the international video coding standards, such as H.261 and H.263 (covered in [Chapter 19](#)), MPEG 1 and MPEG 2 (covered in [Chapter 16](#)). MC coding is essentially a predictive coding technique applied to video sequences involving displacement motion vectors.

3.2 Optimum Linear Prediction

[Figure 3.4](#) indicates that a differential coding system consists of two major components: prediction and quantization. Quantization was discussed in the previous chapter. Hence, in this chapter, we emphasize prediction. Below, we formulate the optimum linear prediction problem and then present a theoretical solution to the problem.

3.2.1 Formulation

Optimum linear prediction can be formulated as follows. Consider a discrete-time random process z . At a typical moment i , it is a random variable z_i . We have n previous observations $\bar{z}_{i-1}, \bar{z}_{i-2}, \dots, \bar{z}_{i-n}$ available and would like to form a prediction of z_i , denoted by \hat{z}_i . The output of the predictor, \hat{z}_i , is a linear function of the n previous observations. That is,

$$\hat{z}_i = \sum_{j=1}^n a_j \bar{z}_{i-j}, \quad (3.20)$$

with $a_j, j=1, 2, \dots, n$ being a set of real coefficients. An illustration of a linear predictor is shown in [Figure 3.5](#). As defined above, the prediction error, e_p , is

$$e_p = z_i - \hat{z}_i \quad (3.21)$$

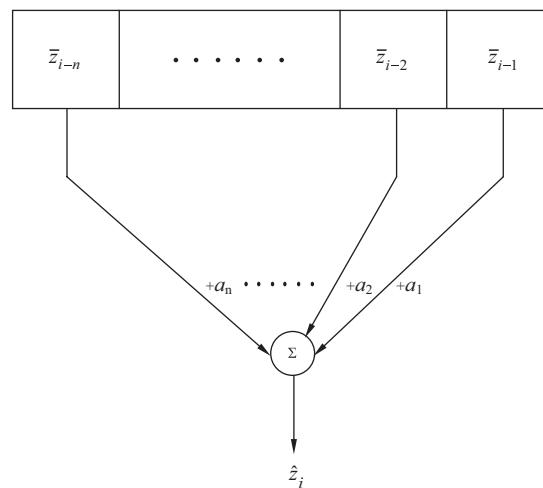


FIGURE 3.5

An illustration of a linear predictor.

The mean square prediction error, MSE_p , is

$$MSE_p = E[(e_p)^2] = E[(z_i - \bar{z}_{i-j})^2] \quad (3.22)$$

The optimum prediction then refers to the determination of a set of coefficients $a_j, j = 1, 2, \dots, n$ such that the mean square prediction error, MSE_p , is minimized.

This optimization problem turns out to be computationally intractable for most practical cases due to the feedback around the quantizer shown in [Figure 3.4](#) and the nonlinear nature of the quantizer. Therefore, the optimization problem is solved in two separate stages. That is, the best linear predictor is first designed ignoring the quantizer. Then, the quantizer is optimized for the distribution of the difference signal (Habibi 1971). Although the predictor thus designed is suboptimal, ignoring the quantizer in the optimum predictor design allows us to substitute the reconstructed \bar{z}_{i-j} by z_{i-j} for $j = 1, 2, \dots, n$, according to Equation 3.19. Consequently, we can apply the theory of optimum linear prediction to handle the design of the optimum predictor as shown below.

3.2.2 Orthogonality Condition and Minimum Mean Square Error

By taking the differentiation of MSE_p with respect to coefficient a_j s, one can derive the following necessary conditions, which are usually referred to as the *orthogonality condition*.

$$E[e_p \cdot z_{i-j}] = 0 \quad \text{for } j = 1, 2, \dots, n. \quad (3.23)$$

The interpretation of Equation 3.23 is that the prediction error, e_p , must be orthogonal to all the observations, which are now the preceding samples: $z_{i-j}, j = 1, 2, \dots, n$, according to our discussion made in [Section 3.2.1](#). These are equivalent to

$$R_z(m) = \sum_{j=1}^n a_j R_z(m-j) \quad \text{for } m = 1, 2, \dots, n, \quad (3.24)$$

where R_z represents the autocorrelation function of z . In a vector-matrix format, the above orthogonal conditions can be written as

$$\begin{bmatrix} R_z(1) \\ R_z(2) \\ \vdots \\ R_z(n) \end{bmatrix} = \begin{bmatrix} R_z(0) & R_z(1) & \dots & \dots & R_z(n-1) \\ R_z(1) & R_z(2) & \dots & \dots & R_z(n-2) \\ \vdots & \vdots & \dots & \dots & \vdots \\ \vdots & \vdots & \dots & \dots & \vdots \\ R_z(n-1) & R_z(n) & \dots & \dots & R_z(0) \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_n \end{bmatrix} \quad (3.25)$$

Equations 3.24 and 3.25 are called Yule-Walker equations.

The minimum mean square prediction error is then found to be

$$MSE_p = R_z(0) - \sum_{j=1}^n a_j R_z(j). \quad (3.26)$$

These results can be found in texts on random processes, e.g., in Leon-Garcia (1994).

3.2.3 Solution to Yule-Walker Equations

Once autocorrelation data are available, the Yule-Walker equation can be solved by matrix inversion. A recursive procedure was developed by Levinson to solve the Yule-Walker equations (Leon-Garcia 1994). When the number of previous samples used in the linear predictor is large, i.e., the dimension of the matrix is high, the Levinson recursive algorithm becomes more attractive. Note that in the field of image coding the autocorrelation function of various types of video frames is derived from measurements (O'Neal 1966, Habibi 1971).

3.3 Some Issues in the Implementation of DPCM

Several related issues in the implementation of DPCM are discussed in this section.

3.3.1 Optimum DPCM System

Since DPCM consists mainly of two parts, prediction and quantization, its optimization should not be carried out separately. The interaction between the two parts is quite complicated, however, and thus combined optimization of the whole DPCM system is difficult. Fortunately, with the mean square error criterion, the relation between quantization error and prediction error has been found as

$$MSE_q \approx \frac{9}{2N^2} MSE_p, \quad (3.27)$$

where N is the total number of reconstruction levels in the quantizer (O'Neal 1966, Musmann 1979). That is, the mean square error of quantization is approximately proportional to the mean square error of prediction. With this approximation, we can optimize two parts separately as mentioned in [Section 3.2.1](#). While the optimization of quantization was addressed in [Chapter 2](#), the optimum predictor was discussed in [Section 3.2](#). A large amount of work has been done in this subject. For instance, the optimum predictor for color image coding was designed and tested in Pirsch and Stenger (1977).

3.3.2 1-D, 2-D, and 3-D DPCM

In [Section 3.1.2](#), we expressed linear prediction in Equation 3.15. However, so far, we have not really discussed how to predict a pixel's gray-level value by using its neighboring pixels' coded gray-level values.

Recall that a practical pixel-to-pixel differential coding system was discussed in [Section 3.1.1](#). There, the reconstructed intensity of the immediately preceding pixel along the same scan line is used as a prediction of the pixel intensity being coded. This type of differential coding is referred to as 1-D DPCM. In general, 1-D DPCM may use the reconstructed gray-level values of more than one preceding pixel within the same scan line to predict that of a pixel being coded. By far, however, the immediately preceding

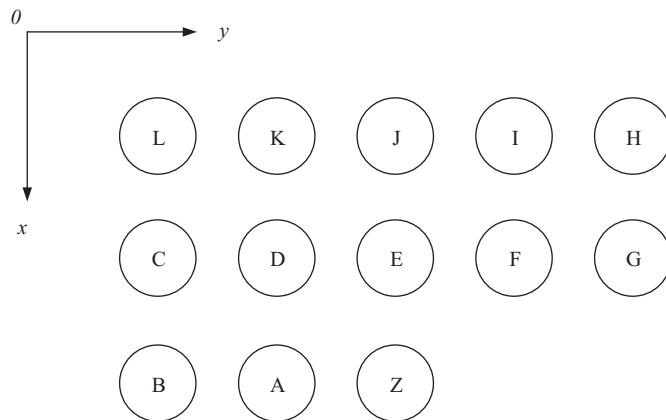


FIGURE 3.6
Pixel arrangement in 1-D and 2-D prediction.

pixel in the same scan line is most frequently used in 1-D DPCM. That is, pixel A in [Figure 3.6](#) is often used as a prediction of pixel Z, which is being DPCM coded.

Sometimes in DPCM image coding, both the decoded intensity values of adjacent pixels within the same scan line and the decoded intensity values of neighboring pixels in the different scan lines are involved in the prediction. This is called 2-D DPCM. A typical pixel arrangement in 2-D predictive coding is shown in [Figure 3.6](#). Note that the pixels involved in the prediction are restricted to be either in the lines above the line where the pixel being coded, Z, is located or on the left-hand side of pixel Z if they are in the same line. Traditionally, a TV frame is scanned from top to bottom and from left to right. Hence, the above restriction indicates that only those pixels that have been coded, available in both the transmitter and the receiver, are used in the prediction. In 2-D system theory, this support is referred to as recursively computable (Bose 1982). An often used 2-D prediction involves pixels A, D, and E.

Obviously, 2-D predictive coding utilizes not only the spatial correlation existing within a scan line but also that existing in neighboring scan lines. In other words, the spatial correlation is utilized both horizontally and vertically. It was reported that 2-D predictive coding outperforms 1-D predictive coding by decreasing the prediction error by a factor of two, or equivalently 3dB in SNR. The improvement in subjective assessment is even larger (Musmann 1979). Furthermore, the transmission error in 2-D predictive image coding is much less severe than in 1-D predictive image coding. This is discussed in [Section 3.6](#).

In the context of image sequences, neighboring pixels may be located not only in the same image frame but also in successive frames. That is, neighboring pixels along the time dimension are also involved. If the prediction of a DPCM system involves three types of neighboring pixels—those along the same scan line, those in the different scan lines of the same image frame, and those in the different frames—the DPCM is then called 3-D differential coding. It will be discussed in [Section 3.5](#).

3.3.3 Order of Predictor

The number of coefficients in the linear prediction, n , is referred to as the order of the predictor. The relation between the mean square prediction error, MSE_p , and the order of the predictor, n , has been studied. As shown in [Figure 3.7](#), the MSE_p decreases as n increases quite effectively, but the performance improvement becomes negligible as $n > 3$ (Habibi 1971).

3.3.4 Adaptive Prediction

Adaptive DPCM means adaptive prediction and adaptive quantization. As adaptive quantization was discussed in [Chapter 2](#), here we discuss adaptive prediction only.

Similar to the discussion on adaptive quantization, adaptive prediction can be done in two different ways: forward adaptive and backward adaptive prediction. In the former, adaptation is based on the input of a DPCM system, while in the latter, adaptation is based on the output of the DPCM. Therefore, forward adaptive prediction is more sensitive to changes in local statistics. Prediction parameters (the coefficients of the predictor), however,

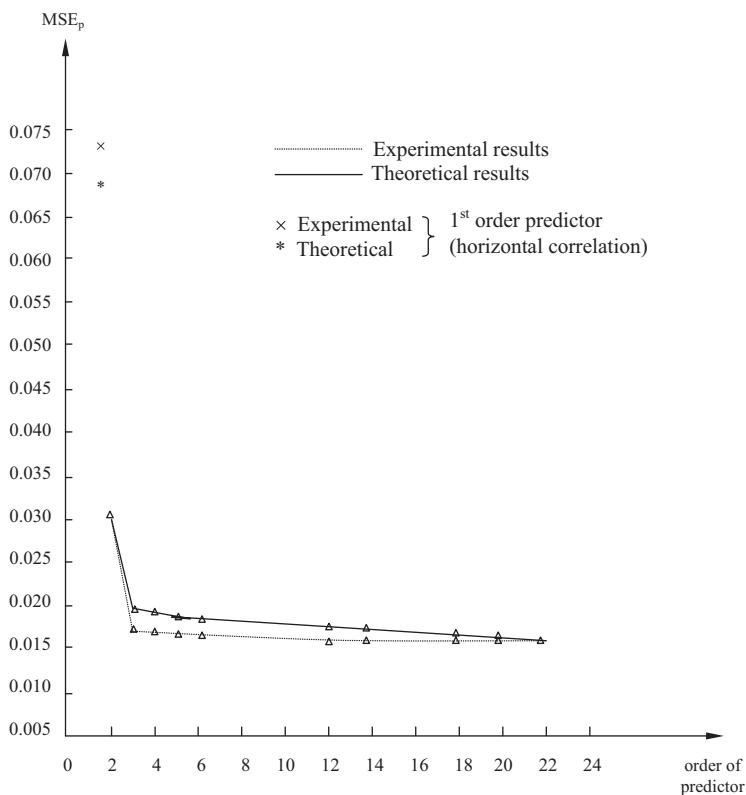


FIGURE 3.7

Mean square prediction error versus order of predictor. (From Habibi, A., *IEEE Trans. Commun. Technol.*, 19, 948–956, 1971.)

need to be transmitted as side information to the decoder. On the other hand, quantization error is involved in backward adaptive prediction. Hence, the adaptation is less sensitive to local changing statistics. However, it does not need to transmit side information.

In either case, the data (either input or output) has to be buffered. Autocorrelation coefficients are analyzed, based on which the prediction parameters are determined.

3.3.5 Effect of Transmission Errors

Transmission error caused by channel noise may reverse the binary bit information from 0 to 1 or 1 to 0 with what is known as *bit error probability*, or *bit error rate*. The effect of transmission error on reconstructed images varies depending on different coding techniques.

In the case of the PCM-coding technique, each pixel is coded independently of the others. Therefore, bit reversal in the transmission only affects the gray-level value of the corresponding pixel in the reconstructed image. It does not affect other pixels in the reconstructed image.

In DPCM, however, the effect caused by transmission errors becomes more severe. Consider a bit reversal occurring in transmission. It causes error in the corresponding pixel. However, this is not the end of the effect. The affected pixel causes errors in reconstructing those pixels towards which the erroneous gray-level value was used in the prediction. In this way, the transmission error propagates.

Interestingly, it is reported that the error propagation is more severe in 1-D differential image coding than in 2-D differential coding. This may be explained as follows. In 1-D differential coding, usually the immediately preceding pixel in the same scan line is involved in prediction. Therefore, an error will be propagated along the scan line until the beginning of the next line, where the pixel gray-level value is reinitialized. In 2-D differential coding, the prediction of a pixel gray-level value depends not only on the reconstructed gray-level values of pixels along the same scan line but also on the reconstructed gray-level values of the vertical neighbors. Hence, the effect caused by a bit reversal transmission error is less severe than in the 1-D differential coding.

For this reason, the bit error rate required by DPCM coding is lower than that required by PCM coding. For instance, while a bit error rate of less than $5 \cdot 10^{-6}$ is normally required for PCM to provide broadcast TV quality, for the same application a bit error rate of less than 10^{-7} and 10^{-9} are required for DPCM coding with 2-D prediction and 1-D prediction, respectively (Musmann 1979).

Channel encoding with an error correction capability was applied to lower the bit error rate. For instance, to lower the bit error rate from the order of 10^{-6} to the order of 10^{-9} for DPCM coding with 1-D prediction, an error correction code by adding 3% redundancy in channel coding has been used (Bruders et al. 1978).

3.4 Delta Modulation

DM is an important, simple, special case of DPCM, as discussed above. It has been widely applied and is thus an important coding technique in and of itself.

The above discussion and characterization of DPCM systems are applicable to DM systems. This is because DM is essentially a special type of DPCM, with the following two features.

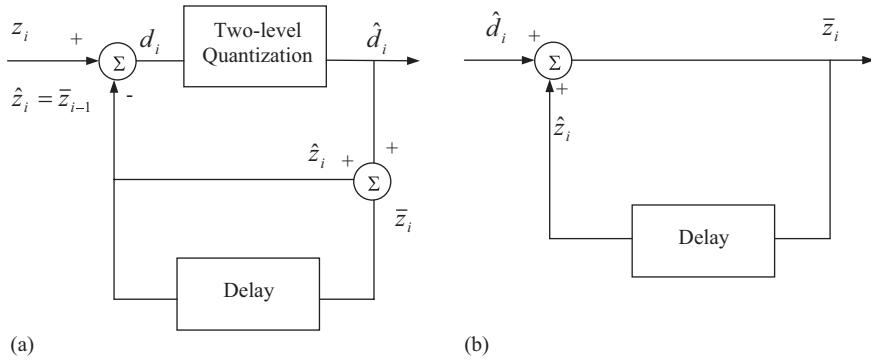


FIGURE 3.8
Block diagram of DM systems (a) Encoder and (b) Decoder.

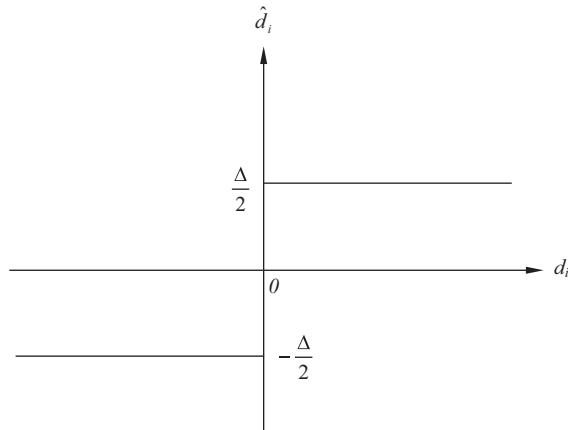


FIGURE 3.9
Input-output characteristic of two-level quantization in DM.

The linear predictor is of the first order, with the coefficient a_1 equal to 1.

The quantizer is a one-bit quantizer. That is, depending on whether the difference signal is positive or negative, the output is either $+\Delta/2$ or $-\Delta/2$.

To perceive these two features, let us take a look at the block diagram of a DM system and the input-output characteristic of its one-bit quantizer, shown in Figures 3.8 and 3.9, respectively. Due to the first feature listed above, we have

$$\hat{z}_i = \bar{z}_{i-1}. \quad (3.28)$$

Next, we see that there are only two reconstruction levels in quantization because of the second feature. That is,

$$\hat{d}_i = \begin{cases} +\Delta/2 & \text{if } z_i > \bar{z}_{i-1}, \\ -\Delta/2 & \text{if } z_i < \bar{z}_{i-1}. \end{cases} \quad (3.29)$$

From the relation between the reconstructed value and the predicted value of DPCM discussed above and the fact that DM is a special case of DPCM, we have

$$\bar{z}_i = \hat{z}_i + \hat{d}_i. \quad (3.30)$$

Combining Equations 3.28, 3.29, and 3.30, we have

$$\bar{z}_i = \begin{cases} \bar{z}_{i-1} + \Delta / 2 & \text{if } z_i > \bar{z}_{i-1} \\ \bar{z}_{i-1} - \Delta / 2 & \text{if } z_i < \bar{z}_{i-1} \end{cases}. \quad (3.31)$$

The above mathematical relationships are of importance in understanding DM systems. For instance, Equation 3.31 indicates that the step size Δ of DM is a crucial parameter. We notice that a large step size compared with the magnitude of the difference signal causes granular error, as shown in [Figure 3.10](#). Therefore, in order to reduce the granular error, we should choose a small step size. On the other hand, a small step size compared with the magnitude of the difference signal will lead to the overload error discussed in [Chapter 2](#) for quantization. Since in DM systems it is the difference signal that is quantized, however, the overload error in DM becomes *slope overload* error, as shown in [Figure 3.10](#). That is, it takes a while (multiple steps) for the reconstructed samples to catch up with the

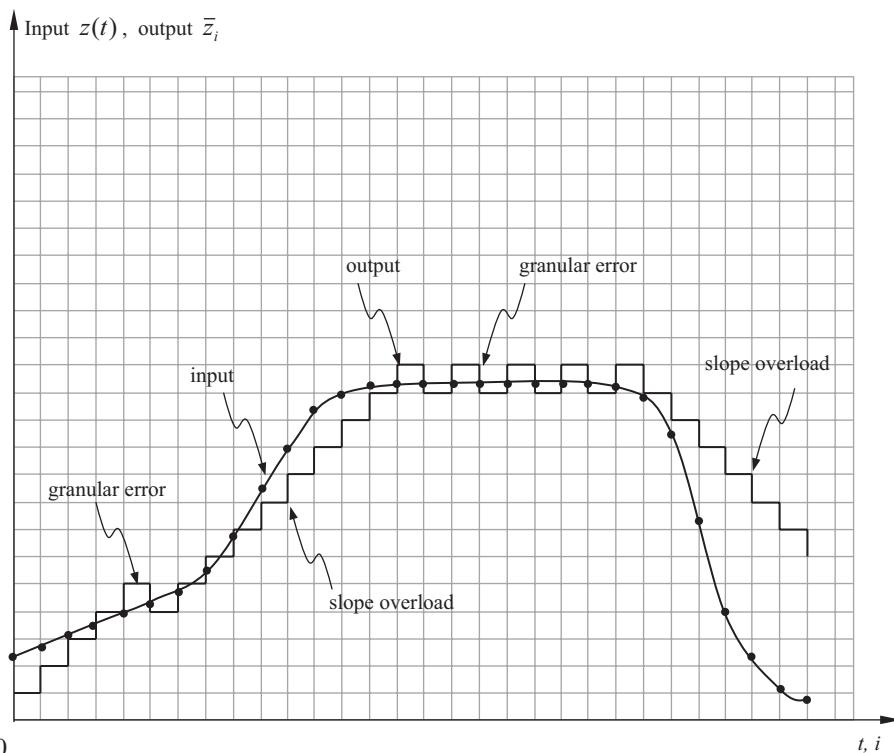


FIGURE 3.10
DM with fixed step size.

sudden change in input. Therefore, the step size should be large in order to avoid the slope overload. Considering these two conflicting factors, a proper compromise in choosing the step size is common practice in DM.

To improve the performance of DM, an oversampling technique is often applied. That is, the input is oversampled prior to the application of DM. By oversampling, we mean that the sampling frequency is higher than the sampling frequency used in obtaining the original input signal. The increased sample density caused by oversampling decreases the magnitude of the difference signal. Consequently, a relatively small step size can be used so as to decrease the granular noise without increasing the slope overload error. At the last, the resolution of the DM coded image is kept the same as that of the original input (Jayant 1984, Lim 1990).

To achieve better performance for changing inputs, an adaptive technique can be applied in DM. That is, either input (forward adaptation) or output (backward adaptation) data are buffered and the data variation is analyzed. The step size is then chosen accordingly. If it is forward adaptation, side information is required for transmission to the decoder. [Figure 3.11](#) demonstrates step size adaptation. We see the same input as that shown in [Figure 3.10](#). However, the step size is now not fixed. Instead, the step size is adapted according to the varying input. When the input changes with a large slope, the step size increases to avoid the slope overload error. On the other hand, when the input changes slowly, the step size decreases to reduce the granular error.

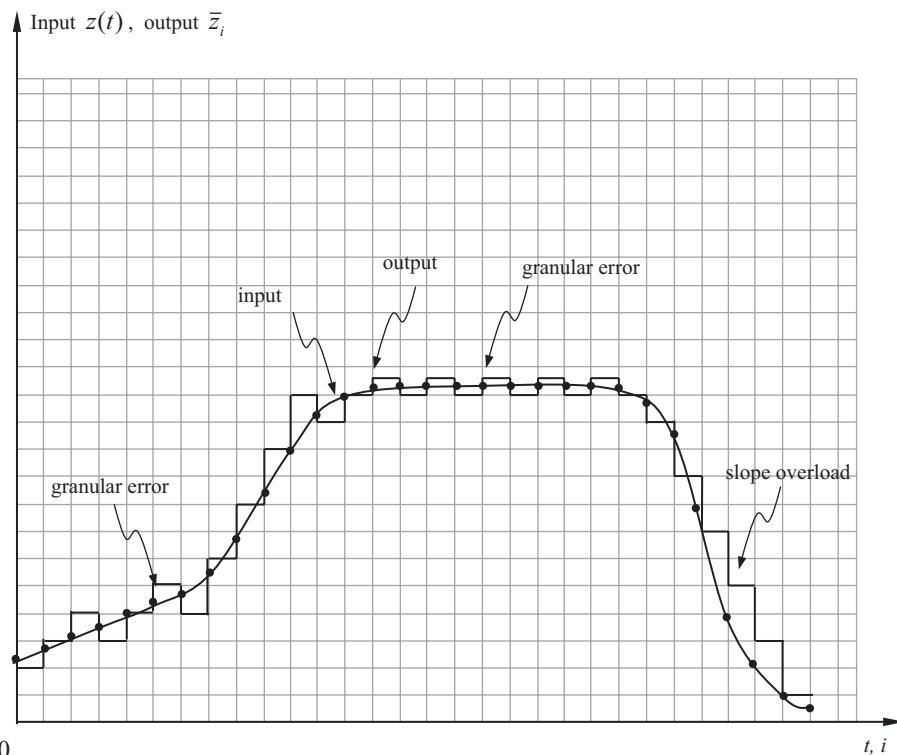


FIGURE 3.11
Adaptive DM.

3.5 Interframe Differential Coding

As was mentioned in [Section 3.3.2](#), 3-D differential coding involves an image sequence. Consider a sensor located in 3-D world space. For instances, in applications such as videophony and videoconferencing, the sensor is fixed in position for a while and it takes pictures. As time goes by, the images form a temporal image sequence. The coding of such an image sequence is referred to as interframe coding. The subject of image sequence and video coding is addressed in Parts III and IV. In this section, we briefly discuss how differential coding is applied to interframe coding.

3.5.1 Conditional Replenishment

Recognizing the great similarity between consecutive TV frames, a conditional replenishment coding technique was proposed and developed (Mounts 1969). It was regarded one of the first real demonstrations of interframe coding exploiting interframe redundancy (Netravali and Robbins 1979).

In this scheme, the previous frame is used as a reference for the present frame. Consider a pair of pixels: one in the previous frame, the other in the present frame—both occupying the same spatial position in the frames. If the gray level difference between the pair of pixels exceeds a certain criterion, then the pixel is considered a *changing* pixel. The present pixel gray-level value and its position information are transmitted to the receiving side, where the pixel is replenished. Otherwise, the pixel is considered *unchanged*. At the receiver, its previous gray level is repeated. A block diagram of conditional replenishment is shown in [Figure 3.12](#). There, a frame memory unit in the transmitter is used to store frames. The differencing and thresholding of corresponding pixels in two consecutive frames can then be conducted there. A buffer in the transmitter is used to smooth the transmission data rate. This is necessary because the data rate varies from region to region within an image frame and from frame to frame within an image sequence. A buffer in the receiver is needed for a similar consideration. In the frame memory unit, the replenishment is carried out for the changing pixels and the gray-level values in the receiver are repeated for the unchanged pixels.

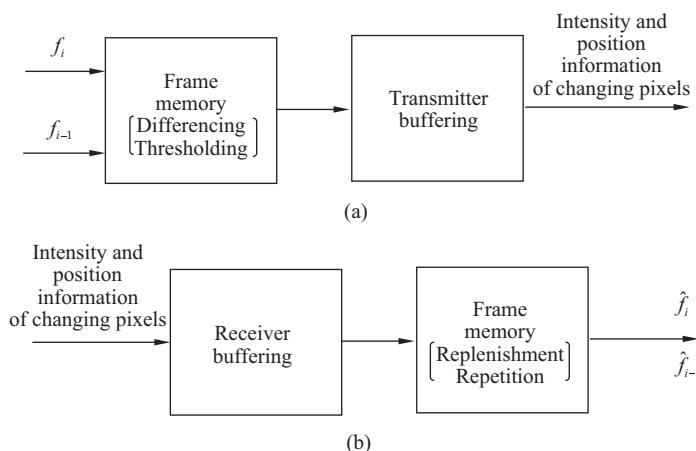


FIGURE 3.12

Block diagram of conditional replenishment (a) Transmitter and (b) Receiver.

With conditional replenishment, a considerable savings in bit rate was achieved in applications such as videophony, videoconferencing, and TV broadcasting. Experiments in real time using the head-and-shoulder view of a person in animated conversation as the video source demonstrated an average bit rate of one bit/pixel with a quality of reconstructed video comparable with standard eight bits/pixel PCM transmission (Mounts 1969). Compared with pixel-to-pixel 1-D DPCM, the most popularly used coding technique at the time, the conditional replenishment technique is more efficient due to the exploitation of high interframe redundancy. As pointed out in Mounts (1969) there is more correlation between television pixels along the frame-to-frame temporal dimension than there is between adjacent pixels within a signal frame. That is, the temporal redundancy is normally higher than spatial redundancy for TV signals.

Tremendous efforts have been made to improve the efficiency of this rudimentary technique. For an excellent review, readers are referred to Haskell et al. (1972) and Haskell (1979). 3-D DPCM coding is among the improvements and is discussed next.

3.5.2 3-D DPCM

It is soon realized that it is more efficient to transmit the gray-level difference than to transmit the gray level itself, resulting in interframe differential coding. Furthermore, instead of treating each pixel independently of its neighboring pixels, it is more efficient to utilize spatial redundancy as well as temporal redundancy, resulting in 3-D DPCM.

Consider two consecutive TV frames, each consisting of an odd and an even field. Figure 3.13 demonstrates the small neighborhood of a pixel, Z, in the context. As with the 1-D and 2-D DPCM discussed before, the prediction can only be based on the previously encoded pixels. If the pixel under consideration, Z, is located in the even field of the present frame, then the odd field of the present frame and both odd and even fields of the previous frame are available. As mentioned in Section 3.3.2, it is assumed that in the even field of the present frame, only those pixels in the lines above the line where pixel Z lies and those pixels left of the Z in the line where Z lies are used for prediction.

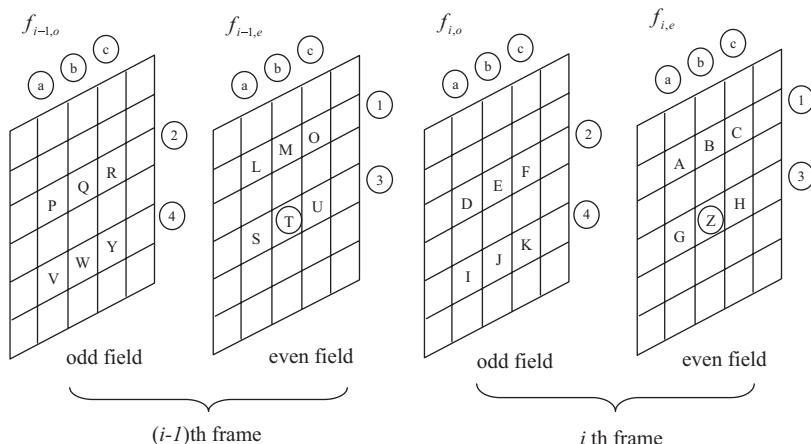


FIGURE 3.13

Pixel arrangement in two TV frames. (From Haskell, B. G., Frame replenishment coding of television, in *Image Transmission Techniques*, W. K. Pratt (Ed.), New York: Academic Press, 1979.)

TABLE 3.1

Some Linear Prediction Schemes

| | Original Signal (Z) | Prediction Signal (\hat{Z}) | Differential Signal (d_z) |
|--|---------------------|-------------------------------------|---|
| Element difference | Z | G | $Z-G$ |
| Field difference | Z | $\frac{E+J}{2}$ | $Z - \frac{E+J}{2}$ |
| Frame difference | Z | T | $Z-T$ |
| Element difference of frame difference | Z | $T+G-S$ | $(Z-G)-(T-S)$ |
| Line difference of frame difference | Z | $T+B-M$ | $(Z-B)-(T-M)$ |
| Element difference of field difference | Z | $T + \frac{E+J}{2} - \frac{Q+W}{2}$ | $\left(Z - \frac{E+J}{2}\right) - \left(T - \frac{Q+W}{2}\right)$ |

Source: Haskell, B. G., Frame replenishment coding of television, in *Image Transmission Techniques*, W.K. Pratt (Ed.), Academic Press, New York, 1979.

Table 3.1 lists several utilized linear prediction scheme. It is recognized that the case of *element difference* is a 1-D predictor since the immediately preceding pixel is used as the predictor. The field difference is defined as the arithmetic average of two immediately vertical neighboring pixels in the previous odd field. Since the odd field is generated first, followed by the even field, this predictor cannot be regarded as a pure 2-D predictor. Instead, it should be considered a 3-D predictor. The remaining cases are all 3-D predictors. One thing is common in all the cases: the gray levels of pixels used in the prediction have already been coded and thus are available in both the transmitter and the receiver.

The prediction error of each changing pixel Z identified in the thresholding process is then quantized and coded.

An analysis of the relationship between the entropy of moving areas (bits per changing pixel) and the motion speeds (pixels per frame interval) in the scenery containing a moving mannequin's head was studied with different linear predictions, listed in **Table 3.1** (Haskell 1979). It was found that the element difference of field difference generally corresponds to the lowest entropy, meaning that this prediction is the most efficient. The frame difference and element difference correspond to higher entropy. It is recognized that, in the circumstances, transmission error will be propagated if the pixels in the previous line are used in prediction (Connor 1973). Hence, the linear predictor should use only pixels from the same line or the same line in the previous frame when bit reversal error in transmission needs to be considered. Combining these two factors, the element difference of frame difference prediction is preferred.

3.5.3 Motion-Compensated Predictive Coding

When frames are taken densely enough, changes in successive frames can be attributed to the motion of objects during the interval between frames. Under this assumption, if we can analyze object motion from successive frames, then we should be able to predict objects in the next frame based on their positions in the previous frame and the estimated motion. The difference between the original frame and the predicted frame thus generated and the motion vectors are then quantized and coded. If the motion estimation is accurate enough, the MC prediction error can be smaller than 3-D DPCM. In other words, the variance of the prediction error will be smaller, resulting in more efficient coding. Take motion into consideration—this differential technique is called MC predictive coding. This has been a major development in image sequence coding since the 1980s. It has been adopted by all international video coding standards. A more detailed discussion is provided in [Chapter 10](#).

3.6 Information-Preserving Differential Coding

As emphasized in [Chapter 2](#), quantization is not reversible in the sense that it causes information loss permanently. The DPCM technique, discussed above, includes quantization and hence is lossy coding. In applications such as those involving scientific measurements, information preserving is required. In this section, the following question is addressed: Under these circumstances how should we apply differential coding in order to reduce bit rate while preserving information?

[Figure 3.14](#) shows a block diagram of information-preserving differential coding. First, we see that there is no quantizer. Therefore, the irreversible information loss associated with quantization does not exist in this technique. Second, we observe that prediction and differencing are still used. That is, the differential (predictive) technique still applies. Hence, it is expected that the variance of the difference signal is smaller than that of the original signal, as explained in [Section 3.1](#). Consequently, the higher-peaked histograms make coding more efficient. Third, an efficient lossless coder is utilized. Since quantizers cannot be used here, PCM with natural binary coding is not used here. Since the histogram of the difference signal is narrowly concentrated about its mean, lossless coding techniques such as an efficient Huffman coder (discussed in [Chapter 5](#)) is naturally a suitable choice here.

As mentioned before, input images are normally in a PCM coded format with a bit rate of eight bits/pixel for monochrome pictures. The difference signal is therefore integer-valued. Having no quantization and using an efficient lossless coder, the coding system depicted in [Figure 3.14](#) is, therefore, an information-preserving differential coding technique.

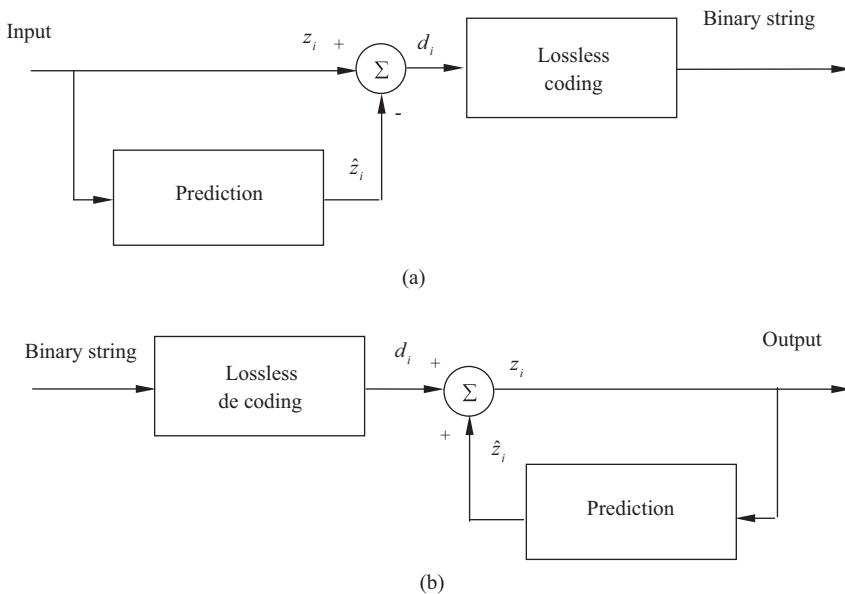


FIGURE 3.14

Block diagram of information-preserving differential coding (a) Encoder and (b) Decoder.

3.7 Summary

Rather than coding the signal itself, differential coding, also known as predictive coding, encodes the difference between the signal and its prediction. Utilizing spatial and/or temporal correlation between pixels in the prediction, the variance of the difference signal can be much smaller than that of the original signal, thus making differential coding quite efficient.

Among differential coding methods, DPCM is used most widely. In DPCM coding, the difference signal is quantized and codewords are assigned to the quantized difference. Prediction and quantization are therefore two major components in the DPCM systems. Since quantization was addressed in [Chapter 2](#), this chapter emphasizes prediction. The theory of optimum linear prediction is introduced. Here, optimum means minimization of mean square prediction error. The formulation of optimum linear prediction, the orthogonality condition, and the minimum mean square prediction error are presented. The orthogonality condition states that the prediction error must be orthogonal to each observation, i.e., the reconstructed sample intensity values used in the linear prediction. By solving the Yule-Walker equation, the optimum prediction coefficients may be determined.

In addition, some fundamental issues in implementing the DPCM technique are discussed. One issue is the dimensionality of the predictor in DPCM. We discussed 1-D, 2-D, and 3-D predictors. DPCM with a 2-D predictor demonstrates better performance than that with 1-D predictor, since 2-D DPCM utilizes more spatial correlation, i.e., not only horizontally but also vertically. As a result, a 3dB improvement in SNR was reported. 3-D prediction is encountered in what is known as interframe coding. There, temporal correlation exists. 3-D DPCM utilizes both spatial and temporal correlation between neighboring pixels in successive frames. Consequently, more redundancy can be removed. MC predictive coding as a very powerful technique in video coding belongs to differential coding. It uses a more advanced translational motion model in the prediction, however, and it is covered in Parts III and IV.

Another issue is the order of predictors and its effect on the performance of prediction in terms of mean square prediction error. Increasing prediction order can lower mean square prediction error effectively, but the performance improvement becomes insignificant after the third order.

Adaptive prediction is another issue. Similar to adaptive quantization, discussed in [Chapter 2](#), we can adapt the prediction coefficients in the linear predictor to varying local statistics.

The last issue is concerned with the effect of transmission error. Bit reversal in transmission causes a different effect on reconstructed images depending on what type of coding technique is used. PCM is known to be bit-consuming. (An acceptable PCM representation of monochrome images requires six to eight bits/pixel.) However, one-bit reversal only affects an individual pixel. For the DPCM coding technique, however, a transmission error may propagate from one pixel to the other. In particular, DPCM with a 1-D predictor suffers from error propagation more severely than DPCM with a 2-D predictor.

DM is an important special case of DPCM, in which the predictor is of the first order. Specifically, the immediately preceding coded sample is used as a prediction of the present input sample. Furthermore, the quantizer has only two reconstruction levels.

Finally, an information-preserving differential coding technique is discussed. As mentioned in [Chapter 2](#), quantization is an irreversible process: it causes information loss. In order to be able to preserve information, there is no quantizer in this type of system. To be efficient, lossless codes such as Huffman code or arithmetic code are used for difference signal encoding.

Exercises

Justify the necessity of the closed-loop DPCM with feedback around quantizers. That is, convince yourself why the quantization error will be accumulated if, instead of using the reconstructed preceding samples, we use the immediately preceding sample as the prediction of the sample being coded in DPCM.

- 3.1 Why does the overload error encountered in quantization appear to be the slope overload in DM?
- 3.2 What advantage does oversampling bring up in the DM technique?
- 3.3 What are the two features of DM that make it a subclass of DPCM?
- 3.4 Explain why DPCM with a 1-D predictor suffers from bit reversal transmission error more severely than DPCM with a 2-D predictor.
- 3.5 Explain why no quantizer can be used in information-preserving differential coding, and why the differential system can work without a quantizer.
- 3.6 Why do all the pixels involved in prediction of differential coding have to be in a recursively computable order from the point of view of the pixel being coded?
- 3.7 Discuss the similarity and dissimilarity between DPCM and MC predictive coding.

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4

Transform Coding

As introduced in the previous chapter, differential coding achieves high coding efficiency by utilizing the correlation between pixels existing in image frames. Transform coding (TC), the focus of this chapter, is another efficient coding scheme based on utilization of interpixel correlation. As we will see in [Chapter 7](#), TC has become a fundamental technique recommended by the international still image coding standard JPEG. Moreover, TC has been found to be efficient in coding prediction error in motion-compensated predictive coding. As a result, TC was also adopted by the international video coding standards such as H.261, H.263, and MPEG 1, 2, and 4. This will be discussed in [Part IV](#).

4.1 Introduction

Recall the block diagram of source encoders shown in [Figure 2.3](#). There are three components in a source encoder: transformation, quantization, and codeword assignment. It is the transformation component that decides which format of input source is quantized and encoded. In DPCM, for instance, the difference between an original signal and a predicted version of the original signal is quantized and encoded. As long as the prediction error is small enough, i.e., the prediction resembles the original signal well (by using correlation between pixels), differential coding is efficient.

In TC, the main idea is that if the transformed version of a signal is less correlated compared with the original signal, then quantizing and encoding the transformed signal may lead to data compression. At the receiver, the encoded data are decoded and transformed back to reconstruct the signal. Therefore, in TC, the transformation component illustrated in [Figure 2.3](#) is a transform. Quantization and codeword assignment are carried out with respect to the transformed signal, or, in other words, carried out in the transformed domain.

We begin with the Hotelling transform, using it as an example of how a transform may decorrelate a signal in the transform domain.

4.1.1 Hotelling Transform

Consider an N -dimensional vector \vec{z}_s . The ensemble of such vectors, $\{\vec{z}_s\} s \in I$, where I represents the set of all vector indexes, can be modeled by a random vector \vec{z} with each of its component z_i $i = 1, 2, \dots, N$ as a random variable. That is,

$$\vec{z} = (z_1, z_2, \dots, z_N)^T, \quad (4.1)$$

where T stands for the operator of matrix transposition. The mean vector of the population, $m_{\vec{z}}$, is defined as

$$m_{\vec{z}} = E[\vec{z}] = (m_1, m_2, \dots, m_N)^T, \quad (4.2)$$

where E stands for the expectation operator. Note that $m_{\bar{z}}$ is an N -dimensional vector with the i th component, m_i , being the expectation value of the i th random variable component in \bar{z} .

$$m_i = E[z_i] \quad i = 1, 2, \dots, N. \quad (4.3)$$

The covariance matrix of the population, denoted by $C_{\bar{z}}$, is equal to

$$C_{\bar{z}} = E[(\bar{z} - m_{\bar{z}})(\bar{z} - m_{\bar{z}})^T]. \quad (4.4)$$

Note that the product inside the E operator is referred to as the *outer product* of the vector $(\bar{z} - m_{\bar{z}})$. Denote an entry at the i th row and j th column in the covariance matrix by $c_{i,j}$. From Equation 4.4, it can be seen that $c_{i,j}$ is the covariance between the i th and j th components of the random vector \bar{z} . That is,

$$c_{i,j} = E[(z_i - m_i)(z_j - m_j)] = Cov(z_i, z_j) \quad (4.5)$$

On the main diagonal of the covariance matrix $C_{\bar{z}}$, the element $c_{i,i}$ is the variance of the i th component of \bar{z} , z_i .

Obviously, the covariance matrix $C_{\bar{z}}$ is a real and symmetric matrix. It is real because of the definition of random variables. It is symmetric because $Cov(z_i, z_j) = Cov(z_j, z_i)$. According to the theory of linear algebra, it is always possible to find a set of N orthonormal eigenvectors of the matrix $C_{\bar{z}}$, with which we can convert the real symmetric matrix $C_{\bar{z}}$ into a full-ranked diagonal matrix. This statement can be found in texts of linear algebra, e.g., in Strang (1998).

Denote the set of N orthonormal eigenvectors and their corresponding eigenvalues of the covariance matrix $C_{\bar{z}}$ by \vec{e}_i and λ_i , $i = 1, 2, \dots, N$, respectively. Note that eigenvectors are column vectors. Form a matrix Φ such that its rows comprise the N eigenvectors. That is,

$$\Phi = (\vec{e}_1, \vec{e}_2, \dots, \vec{e}_N)^T \quad (4.6)$$

Now, consider the following transformation.

$$\vec{y} = \Phi(\bar{z} - m_{\bar{z}}). \quad (4.7)$$

It is easy to verify that the transformed random vector \vec{y} has the following two characteristics.

1. The mean vector, $m_{\vec{y}}$, is a zero vector. That is,

$$m_{\vec{y}} = 0. \quad (4.8)$$

2. The covariance matrix of the transformed random vector $C_{\vec{y}}$ is

$$C_{\vec{y}} = \Phi C_{\bar{z}} \Phi^T = \begin{bmatrix} \lambda_1 & & & & 0 \\ & \lambda_2 & & & \\ & & \ddots & & \\ & & & \ddots & \\ 0 & & & & \lambda_N \end{bmatrix}. \quad (4.9)$$

This transform is called the Hotelling transform (Hotelling 1933), or eigenvector transform (Tasto and Wintz 1971, Wintz 1972).

The inverse Hotelling transform is defined as

$$\vec{z} = \Phi^{-1}\vec{y} + m_{\vec{z}}, \quad (4.10)$$

where Φ^{-1} is the inverse matrix of Φ . It is easy to see from its formation discussed above that the matrix Φ is orthogonal. Therefore, we have $\Phi^T = \Phi^{-1}$. Hence, the inverse Hotelling transform can be expressed as

$$\vec{z} = \Phi^T \vec{y} + m_{\vec{z}}. \quad (4.11)$$

Note that in implementing the Hotelling transform, the mean vector $m_{\vec{z}}$ and the covariance matrix $C_{\vec{z}}$ can be calculated approximately by using a given set of K sample vectors (Gonzalez 1992).

$$m_{\vec{z}} = \frac{1}{K} \sum_{s=1}^K \vec{z}_s \quad (4.12)$$

$$C_{\vec{z}} = \frac{1}{K} \sum_{s=1}^K \vec{z}_s \vec{z}_s^T - m_{\vec{z}} m_{\vec{z}}^T \quad (4.13)$$

The analogous transform for continuous data was devised by Karhunen (1947) and Loéve (1948). Alternatively, the Hotelling transform can be viewed as the discrete version of the Karhunen-Loéve transform (KLT). We observe that the covariance matrix $C_{\vec{y}}$ is a diagonal matrix. The elements in the diagonal are the eigenvalues of the covariance matrix $C_{\vec{z}}$. That is, the two covariance matrices have the same eigenvalues and eigenvectors because the two matrices are similar. The fact that zero values are everywhere except along the main diagonal in $C_{\vec{y}}$ indicates that the components of the transformed vector \vec{y} are uncorrelated. That is, the correlation previously existing between the different components of the random vector \vec{z} has been removed in the transformed domain. Therefore, if the input is split into *blocks* and the Hotelling transform is applied blockwise, the coding may be more efficient since the data in the transformed block are uncorrelated. At the receiver, we may produce a replica of the input with an inverse transform. This basic idea behind TC will be further illustrated next. Note that TC is also referred to as block quantization (Huang and Schultheiss 1963).

4.1.2 Statistical Interpretation

Let us continue our discussion of the 1-D Hotelling transform. Recall that the covariance matrix of the transformed vector \vec{y} , $C_{\vec{y}}$, is a diagonal matrix. The elements in the main diagonal are eigenvalues of the covariance matrix $C_{\vec{y}}$. According to the definition of covariance matrix, these elements are the variances of the components of vector \vec{y} , denoted by $\sigma_{y,1}^2, \sigma_{y,2}^2, \dots, \sigma_{y,N}^2$. Let us arrange the eigenvalues (variances) in a nonincreasing order. That is, $\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_N$. Choose an integer L , and $L < N$. Using the corresponding L eigenvectors, $\vec{e}_1, \vec{e}_2, \dots, \vec{e}_L$, we form a matrix $\vec{\Phi}$ with these L eigenvectors (transposed) as its L rows.

Obviously, the matrix $\bar{\Phi}$ is of $L \times N$. Hence, using the matrix $\bar{\Phi}$ in Equation 4.7 will have the transformed vector \vec{y} of $L \times 1$. That is,

$$\vec{y} = \bar{\Phi}(\vec{z} - m_{\vec{z}}). \quad (4.14)$$

The inverse transform changes accordingly:

$$\vec{z}' = \bar{\Phi}^T \vec{y} + m_{\vec{z}}. \quad (4.15)$$

Note that the reconstructed vector \vec{z} , denoted by \vec{z}' , is still an $N \times 1$ column vector. It can be shown (Wintz 1972) that the mean square reconstruction error between the original vector \vec{z} and the reconstructed vector \vec{z}' is given by

$$MSE_r = \sum_{i=L+1}^N \sigma_{y,i}^2. \quad (4.16)$$

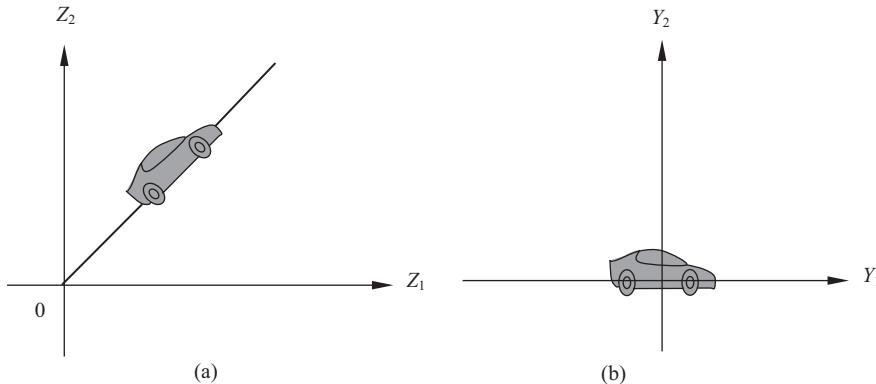
This equation indicates that the mean square reconstruction error equals the sum of variances of the discarded components. Note that although we discuss the reconstruction error here, we have not considered the quantization error and transmission error involved. Equation 4.15 implies that if, in the transformed vector \vec{y} , the first L components have their variances occupy a large percentage of the total variances, the mean square reconstruction error will not be large even though only the first L components are kept, i.e., the $(N-L)$ remaining components in the \vec{y} are discarded. Quantizing and encoding only L components of vector \vec{y} in the transform domain lead to higher coding efficiency. This is the basic idea behind TC.

4.1.3 Geometrical Interpretation

Transforming a set of statistically dependent data into another set of uncorrelated data, then discarding the insignificant transform coefficients (having small variances) illustrated above using the Hotelling transform, can be viewed as a statistical interpretation of TC. Here, we give a geometrical interpretation of TC. For this purpose, we use 2-D vectors instead of N -D vectors.

Consider a binary image of a car in [Figure 4.1a](#). Each pixel in the shaded object region corresponds to a 2-D vector with its two components being coordinates z_1 and z_2 , respectively. Hence, the set of all pixels associated with the object forms a population of vectors. We can determine its mean vector and covariance matrix using Equations 4.12 and 4.13, respectively. We can then apply the Hotelling transform by using Equation 4.7. [Figure 4.1b](#) depicts the same object after the application of the Hotelling transform in the $y_1 - y_2$ coordinate system. We notice that the origin of the new coordinate system is now located at the centroid of the binary object. Furthermore, the new coordinate system is aligned with the two eigenvectors of the covariance matrix $C_{\vec{z}}$.

As mentioned, the elements along the main diagonal of $C_{\vec{y}}$ (two eigenvalues of the $C_{\vec{y}}$ and $C_{\vec{z}}$) are the two variances of the two components of the \vec{y} population. Since the covariance matrix $C_{\vec{y}}$ is a diagonal matrix, the two components are uncorrelated after the transform. Since one variance (along the y_1 direction) is larger than the other (along the y_2 direction), it is possible for us to achieve higher coding efficiency by ignoring the component associated with the smaller variance without too much sacrifice of the reconstructed image quality.

**FIGURE 4.1**

(a) A binary object in the z_1 - z_2 coordinate system and (b) After the Hotelling transform, the object is aligned with its principal axes.

It is noted that the alignment of the object with the eigenvectors of the covariance matrix is of importance in pattern recognition (Gonzalez 1992).

4.1.4 Basis Vector Interpretation

Basis vector expansion is another interpretation of TC. For simplicity, in this subsection we assume a zero mean vector. Under this assumption, the Hotelling transform and its inverse transform become

$$\vec{y} = \Phi \vec{z} \quad (4.17)$$

$$\vec{z} = \Phi^T \vec{y} \quad (4.18)$$

Recall that the row vectors in the matrix Φ are the transposed eigenvectors of the covariance matrix $C_{\vec{z}}$. Therefore, Equation 4.18 can be written as

$$\vec{z} = \sum_{i=1}^N y_i \vec{e}_i. \quad (4.19)$$

In the above equation, we can view vector \vec{z} as a linear combination of *basis vectors* \vec{e}_i , $i = 1, 2, \dots, N$. The components of the transformed vector \vec{y} , $y_i, i = 1, 2, \dots, N$, serve as coefficients in the linear combination, or weights in the weighted sum of basis vectors. The coefficient $y_i, i = 1, 2, \dots, N$ can be produced according to Equation 4.17:

$$y_i = \vec{e}_i^T \vec{z}. \quad (4.20)$$

That is, y_i is the *inner product* between vectors \vec{e}_i and \vec{z} . Therefore, the coefficient y_i can be interpreted as the amount of correlation between the basis vector \vec{e}_i and the original signal \vec{z} .

In the Hotelling transform the coefficients $y_i, i = 1, 2, \dots, N$ are uncorrelated. The variance of y_i can be arranged in a nonincreasing order. For $i > L$, the variance of the coefficient becomes insignificant. We can then discard these coefficients without introducing significant error in the linear combination of basis vectors and achieve higher coding efficiency.

In the above three interpretations of TC, we see that the linear unitary transform can provide the following two functions.

1. Decorrelate input data; i.e., transform coefficients are less correlated than the original data.
2. Have some transform coefficients more significant than others (with large variance, eigenvalue, or weight in basis vector expansion) such that transform coefficients can be treated differently: some can be discarded, some can be coarsely quantized, and some can be finely quantized.

Note that the definition of *unitary* transform is given shortly in [Section 4.2.1.3](#).

4.1.5 Procedures of Transform Coding

Prior to leaving this section, we summarize the procedures of TC. There are three steps in TC as shown in [Figure 4.2](#). First, the input data (frame) is divided into blocks (sub-images). Each block is then linearly transformed. The transformed version is then truncated, quantized, and encoded. These last three functions, which are discussed in [Section 4.4](#), can be grouped and termed as bit allocation. The output of the encoder is a bit stream.

In the receiver, the bit stream is decoded and then inversely transformed to form reconstructed blocks. All the reconstructed blocks collectively produce a replica of the input image.

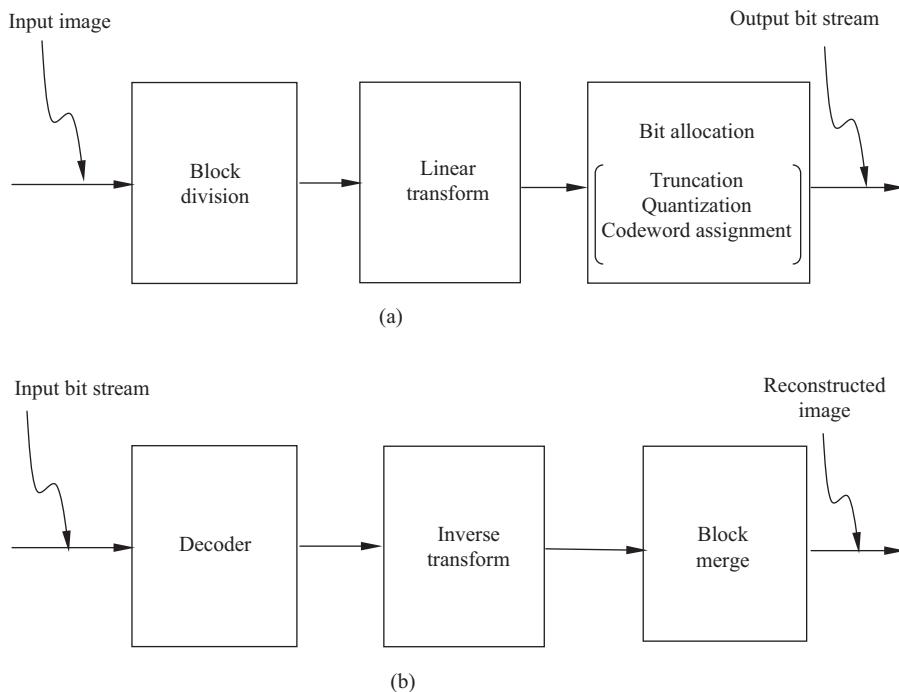


FIGURE 4.2

Block diagram of TC (a) Transmitter and (b) Receiver.

4.2 Linear Transforms

In this section, we first discuss a general formulation of a linear unitary 2-D image transform. Then, a basis image interpretation of TC is given.

4.2.1 2-D Image Transformation Kernel

There are two different ways to handle image transformation. With the first way, we convert a 2-D array representing a digital image into a 1-D array via row-by-row stacking, for example. That is, from the second row on, the beginning of each row in the 2-D array is cascaded to the end of its previous row. Then we transform this 1-D array using a 1-D transform. After the transformation, we can convert the 1-D array back to a 2-D array. With the second way, a 2-D transform is directly applied to the 2-D array corresponding to an input image, resulting in a transformed 2-D array. These two ways are essentially the same. It can be straightforwardly shown that the difference between the two is simply a matter of notation (Wintz 1972). In this section, we use the second way to handle image transformation. That is, we work on 2-D image transformation.

Assume a digital image is represented by a 2-D array $g(x, y)$, where (x, y) is the coordinates of a pixel in the 2-D array, while g is the gray-level value (also often called intensity or brightness) of the pixel. Denote the 2-D transform of $g(x, y)$ by $T(u, v)$, where (u, v) is the coordinates in the transformed domain. Assume that both $g(x, y)$ and $T(u, v)$ are a square 2-D array of $N \times N$; i.e., $0 \leq x, y, u, v \leq N - 1$.

The 2-D forward and inverse transforms are defined as

$$T(u, v) = \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} g(x, y) f(x, y, u, v), \quad (4.21)$$

$$g(x, y) = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} T(u, v) i(x, y, u, v), \quad (4.22)$$

where $f(x, y, u, v)$ and $i(x, y, u, v)$ are referred to as the forward and inverse *transformation kernels*, respectively.

A few characteristics of transforms are discussed below.

4.2.1.1 Separability

A transformation kernel is called separable (hence, the transform is said to be separable) if the following conditions are satisfied.

$$f(x, y, u, v) = f_1(x, u) f_2(y, v), \quad (4.23)$$

$$i(x, y, u, v) = i_1(x, u) i_2(y, v). \quad (4.24)$$

Note that a 2-D separable transform can be decomposed into two 1-D transforms. That is, a 2-D transform can be implemented by a 1-D transform row-wise followed by another 1-D transform column-wise. That is,

$$T_1(x, v) = \sum_{y=0}^{N-1} g(x, y) f_2(y, v), \quad (4.25)$$

where $0 \leq x, v \leq N - 1$, and

$$T(u, v) = \sum_{x=0}^{N-1} T_1(x, v) f_1(x, u), \quad (4.26)$$

where $0 \leq u, v \leq N - 1$. Of course, the 2-D transform can also be implemented in a reverse order with two 1-D transforms, i.e., column-wise first followed by row-wise. The counterparts of Equations 4.25 and 4.26 for the inverse transform can be derived similarly.

4.2.1.2 Symmetry

The transformation kernel is symmetric (hence, the transform is symmetric) if the kernel is separable and the following condition is satisfied:

$$f_1(y, v) = f_2(y, v). \quad (4.27)$$

That is, f_1 is functionally equivalent to f_2 .

4.2.1.3 Matrix Form

If a transformation kernel is symmetric (hence, separable) then the 2-D image transform discussed above can be expressed compactly in the following matrix form. Denote an *image matrix* by G and $G = \{g_{i,j}\} = \{g(i-1, j-1)\}$. That is, a typical element (at the i th row and j th column) in the matrix G is the pixel gray-level value in the 2-D array $g(x, y)$ at the same geometrical position. Note that the subtraction of one in the notation $g(i-1, j-1)$ comes from Equations 4.21 and 4.22. Namely, the indexes of a square 2-D image array are conventionally defined from 0 to $N-1$, while the indexes of a square matrix are from 1 to N . Denote the *forward transform matrix* by F and $F = \{f_{i,j}\} = \{f_1(i-1, j-1)\}$. We then have the following matrix form of a 2-D transform:

$$T = F^T G F, \quad (4.28)$$

where T at the left-hand side of the equation denotes the matrix corresponding to the transformed 2-D array in the same fashion as that used in defining the G matrix. The inverse transform can be expressed as

$$G = I^T T I, \quad (4.29)$$

where the matrix I is the *inverse transform matrix* and $I = \{i_{j,k}\} = \{i_1(j-1, k-1)\}$. The forward and inverse transform matrices have the following relation:

$$I = F^{-1}. \quad (4.30)$$

Note that all of the matrices defined above, G , T , F , and I are of $N \times N$.

It is known that the discrete Fourier transform (DFT) involves complex quantities. In this case, the counterparts of Equations 4.28, 4.29 and 4.30 become Equations 4.31 through 4.33, respectively:

$$T = F^{*^T} GF \quad (4.31)$$

$$G = I^{*^T} TI \quad (4.32)$$

$$I = F^{-1} = F^{*^T}, \quad (4.33)$$

where $*$ indicates complex conjugation. Note that the transform matrices F and I contain complex quantities and satisfy Equation 4.33. They are called unitary matrices and the transform is referred to as a unitary transform.

4.2.1.4 Orthogonality

A transform is said to be orthogonal if the transform matrix is orthogonal. That is,

$$F^T = F^{-1}. \quad (4.34)$$

Note that an orthogonal matrix (orthogonal transform) is a special case of a unitary matrix (unitary transform), where only real quantities are involved. We will see that all the 2-D image transforms, presented in [Section 4.3](#), are separable, symmetric, and unitary.

4.2.2 Basis Image Interpretation

Here we study the concept of *basis images* or *basis matrices*. Recall that we discussed basis vectors when we considered the 1-D transform. That is, the components of the transformed vector (also referred to as the transform coefficients) can be interpreted as the coefficients in the basis vector expansion of the input vector. Each coefficient is essentially the amount of correlation between the input vector and the corresponding basis vector. The concept of basis vectors can be extended to basis images in the context of 2-D image transforms.

Recall that the 2-D inverse transform introduced at the beginning of this section is defined as

$$g(x, y) = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} T(u, v) i(x, y, u, v), \quad (4.35)$$

where $0 \leq x, y \leq N - 1$. This equation can be viewed as a *component* form of the inverse transform. As defined above in [Section 4.2.1.3](#), the whole image $\{g(x, y)\}$ is denoted by the image matrix G of $N \times N$. We now denote the “image” formed by the inverse transformation kernel $\{i(x, y, u, v), 0 \leq x, y \leq N - 1\}$ as a 2-D array $I_{u,v}$ of $N \times N$ for a specific pair of (u, v) with $0 \leq u, v \leq N - 1$. Recall that a digital image can be represented by a 2-D array of gray-level values. In turn the 2-D array can be arranged into a matrix. Namely, we treat the

following three—a digital image, a 2-D array (with proper resolution), and a matrix (with proper indexing)—interchangeably. We then have

$$I_{u,v} = \begin{bmatrix} i(0,0,u,v) & i(0,1,u,v) & \dots & \dots & i(0,N-1,u,v) \\ i(1,0,u,v) & i(1,1,u,v) & \dots & \dots & i(1,N-1,u,v) \\ \vdots & \vdots & \dots & \dots & \vdots \\ \vdots & \vdots & \dots & \dots & \vdots \\ i(N-1,0,u,v) & i(N-1,1,u,v) & \dots & \dots & i(N-1,N-1,u,v) \end{bmatrix} \quad (4.36)$$

The 2-D array $I_{u,v}$ is referred to as a basis image. There are N^2 basis images in total since $0 \leq u, v \leq N-1$. The inverse transform expressed in Equation 4.35 can then be written in a *collective* form as

$$G = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} T(u,v) I_{u,v}. \quad (4.37)$$

We can interpret this equation as a series expansion of the original image G into a set of N^2 basis images $I_{u,v}$. The transform coefficients $T(u, v)$, $0 \leq u, v \leq N-1$, become the coefficients of the expansion. Alternatively, the image G is said to be a weighted sum of basis images. Note that, similar to the 1-D case, the coefficient or the weight $T(u, v)$ is a correlation measure between the image G and the basis image $I_{u,v}$ (Wintz 1972).

Note that basis images have nothing to do with the input image. Instead, it is completely defined by the transform itself. That is, basis images are the attribute of 2-D image transforms. Different transforms have different sets of basis images.

The motivation behind TC is that with a proper transform, hence, a proper set of basis images, the transform coefficients are more independent than the gray scales of the original input image. In the ideal case, the transform coefficients are statistically independent. We can then optimally encode the coefficients independently, which can make coding more efficient and simpler. As pointed out in Wintz (1972), however, this is generally impossible because of the following two reasons. First, it requires the joint probability density function of the N^2 pixels, which have not been deduced from basic physical laws and cannot be measured. Second, even if the joint probability density functions were known, the problem of devising a reversible transform that can generate independent coefficients is unsolved. The optimum linear transform we can have results in uncorrelated coefficients. When Gaussian distribution is involved, we can have independent transform coefficients. In addition to the uncorrelatedness of coefficients, the variance of the coefficients varies widely. Insignificant coefficients can be ignored without introducing significant distortion in the reconstructed image. Significant coefficients can be allocated more bits in encoding. The coding efficiency is thus enhanced.

As shown in [Figure 4.3](#), TC can be viewed as expanding the input image into a set of basis images, then quantizing and encoding the coefficients associated with the basis images separately. At the receiver, the coefficients are reconstructed to produce a replica of the input image. This strategy is similar to that of subband coding, which is discussed in [Chapter 8](#). From this point of view, TC can be considered a special case of subband coding, though TC was devised much earlier than subband coding.

It is worth mentioning an alternative way to define basis images. That is, a basis image with indexes (u, v) , $I_{u,v}$, of a transform can be constructed as the *outer product* of the u th

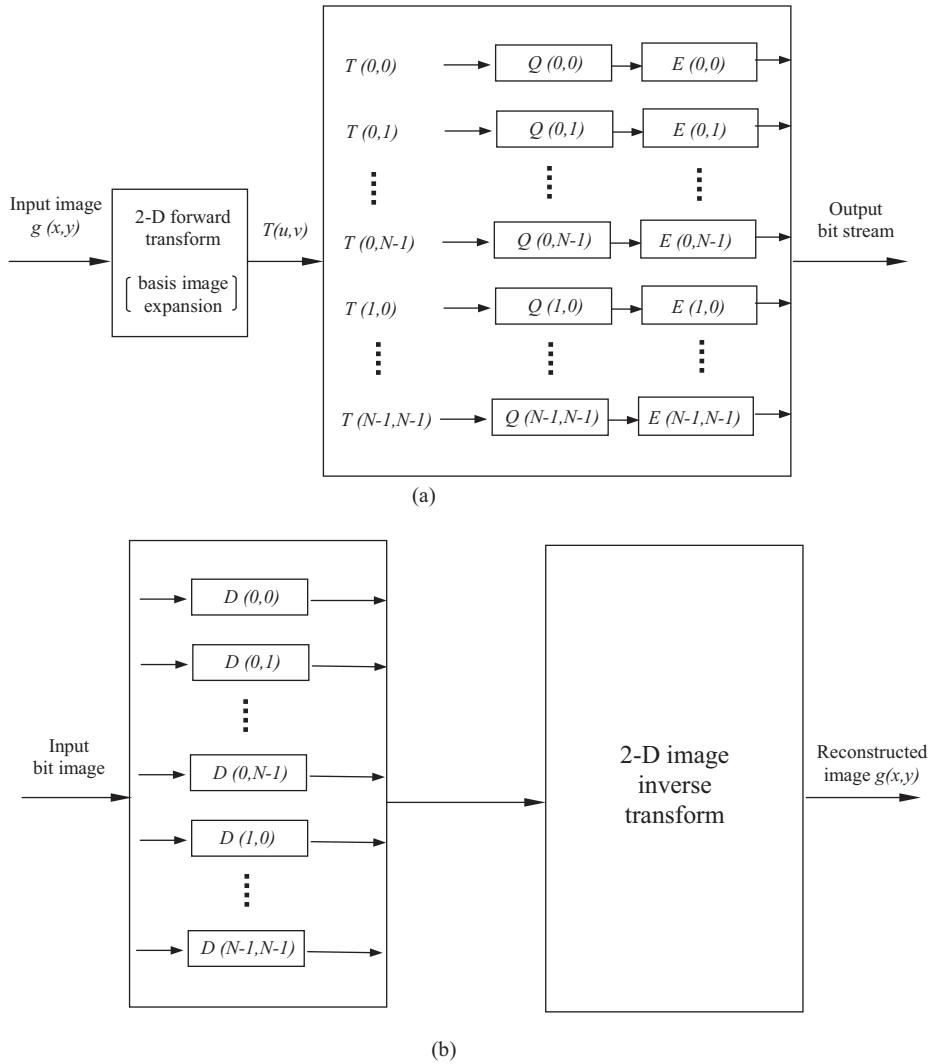


FIGURE 4.3
Basis image interpretation of TC (Q: quantizer, E: encoder, D: decoder) (a) Transmitter and (b) Receiver.

basis vector, \vec{b}_u , and the v th basis vector, \vec{b}_v , of the transform. The basis vector, \vec{b}_u , is the u th column vector of the inverse transform matrix I (Jayant and Noll 1984). That is,

$$I_{u,v} = \vec{b}_u \vec{b}_v^T. \quad (4.38)$$

4.2.3 Sub-image Size Selection

The selection of sub-image (block) size, N , is important. Normally, the larger the size the more decorrelation the TC can achieve. It has been shown, however, that the correlation between image pixels becomes insignificant when the distance between pixels becomes large, e.g., it exceeds 20 pixels (Habibi and Wintz 1971a). On the other hand, a large size

causes some problems. In adaptive TC, a large block cannot adapt to local statistics well. As will be seen later in this chapter, a transmission error in TC affects the whole associated sub-image. Hence, a large size implies a possibly severe effect of transmission error on reconstructed images. As will be shown in video coding ([Part III](#) and [Part IV](#)), TC is used together with motion-compensated coding. Consider that large block size is not used in motion estimation; sub-image sizes of 4, 8, and 16 are used most often. In particular, $N = 8$ is adopted by the international still image coding standard JPEG as well as video coding standards H.261, H.263, H. 264, and MPEG 1, 2, and 4.

4.3 Transforms of Particular Interest

Several commonly used image transforms are discussed in this section. They include the DFT, the discrete Walsh transform (DWT), the discrete Hadamard transform (DHT), and the discrete Cosine and Sine transforms. All of these transforms are symmetric (hence, separable as well), unitary, and reversible. For each transform, we define its transformation kernel and discuss its basis images.

4.3.1 Discrete Fourier Transform

The DFT is of great importance in the field of digital signal processing. Owing to the fast Fourier transform (FFT) based on the algorithm developed in Cooley and Tukey (1965), the DFT is widely utilized for various tasks of digital signal processing. It has been discussed in many signal and image processing texts. Here, we only define it by using the transformation kernel just introduced above. The forward and inverse transformation kernels of the DFT are

$$f(x, y, u, v) = \frac{1}{N} \exp\{-j2\pi(xu + yv) / N\}, \quad (4.39)$$

$$i(x, y, u, v) = \frac{1}{N} \exp(j2\pi(xu + yv) / N). \quad (4.40)$$

Clearly, since complex quantities are involved in the DFT transformation kernels, the DFT is generally complex. Hence, we use the unitary matrix to handle the DFT (refer to [Section 4.2.1.3](#)). The basis vector of the DFT \vec{b}_u is an $N \times 1$ column vector and is defined as

$$\vec{b}_u = \frac{1}{\sqrt{N}} \left[1, \exp\left(j2\pi \frac{u}{N}\right), \exp\left(j2\pi \frac{2u}{N}\right), \dots, \exp\left(j2\pi \left(\frac{(N-1)u}{N}\right)\right) \right]^T. \quad (4.41)$$

As mentioned, the basis image with index (u, v) , $I_{u,v}$, is equal to $\vec{b}_u \vec{b}_v^T$. A few basis images are listed below for $N = 4$.

$$I_{0,0} = \frac{1}{4} \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{pmatrix} \quad (4.42)$$

$$I_{0,1} = \frac{1}{4} \begin{pmatrix} 1 & j & -1 & -j \\ 1 & j & -1 & -j \\ 1 & j & -1 & -j \\ 1 & j & -1 & -j \end{pmatrix} \quad (4.43)$$

$$I_{1,2} = \frac{1}{4} \begin{pmatrix} 1 & 1 & 1 & -1 \\ j & -j & j & -j \\ -1 & 1 & -1 & 1 \\ -j & -j & -j & j \end{pmatrix} \quad (4.44)$$

$$I_{3,3} = \frac{1}{4} \begin{pmatrix} 1 & -j & -1 & j \\ -j & -1 & j & 1 \\ -1 & j & 1 & -j \\ j & 1 & -j & -1 \end{pmatrix} \quad (4.45)$$

4.3.2 Discrete Walsh Transform

The transformation kernels of the DWT (Walsh 1923) are defined as

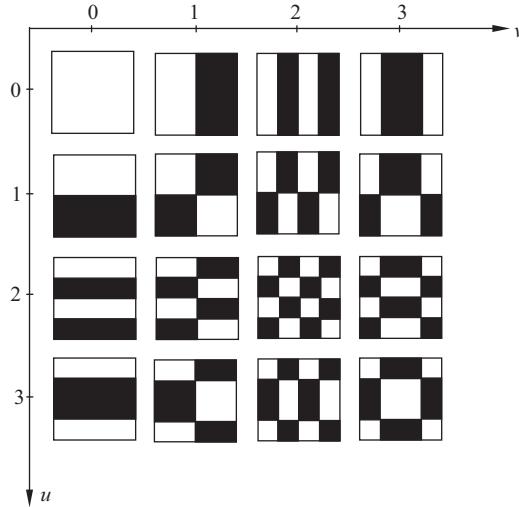
$$f(x, y, u, v) = \frac{1}{N} \prod_{i=0}^{n-1} [(-1)^{p_i(x)p_{n-1-i}(u)} (-1)^{p_i(y)p_{n-1-i}(v)}], \quad (4.46)$$

$$i(x, y, u, v) = f(x, y, u, v). \quad (4.47)$$

where $n = \log_2 N$, $p_i(\arg)$ represents the i th bit in the natural binary representation of the arg, the 0th bit corresponds to the least significant bit, and the $(n-1)$ th bit corresponds to the most significant bit. For instance, consider $N = 16$, then $n = 4$. The natural binary code of number 8 is 1000. Hence, $p_0(8) = p_1(8) = p_2(8) = 0$, and $p_3(8) = 1$. We see that if the factor $1/N$ is put aside then the forward transformation kernel is always an integer: either +1 or -1. In addition, the inverse transformation kernel is the same as the forward transformation kernel. Therefore, we conclude that the implementation of the DWT is simple.

When $N = 4$, the 16 basis images of the DWT are shown in [Figure 4.4](#). Each corresponds to a specific pair of (u, v) and is of resolution 4×4 in $x-y$ coordinate system. They are binary images, where the bright represents +1, while the dark -1. The transform matrix of the DWT is shown below for $N = 4$.

$$F = \frac{1}{2} \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & 1 & -1 \\ 1 & -1 & -1 & 1 \end{pmatrix} \quad (4.48)$$

**FIGURE 4.4**

When $N = 4$, a set of 16 basis images of DWT.

4.3.3 Discrete Hadamard Transform

The DHT (Hadamard 1893) is closely related to the DWT. This can be seen from the following definition of the transformation kernels.

$$f(x, y, u, v) = \frac{1}{N} \prod_{i=0}^n [(-1)^{p_i(x)p_i(u)} (-1)^{p_i(y)p_i(v)}], \quad (4.49)$$

$$i(x, y, u, v) = f(x, y, u, v), \quad (4.50)$$

where the definition of n , i , and $p_i(\arg)$ are the same as in the DWT. For this reason, the term Walsh-Hadamard transform (DWHT) is frequently used to represent either of the two transforms.

When N is a power of 2, the transform matrices of the DWT and DHT have the same row (or column) vectors except that the order of row (or column) vectors in the matrices are different. This is the only difference between the DWT and DHT under the circumstance: $N = 2^n$. Because of this difference, while the DWT can be implemented by using the FFT algorithm with a straightforward modification, the DHT needs more work to use the FFT algorithm. On the other hand, the DHT possesses the following recursive feature, while the DWT does not:

$$F_2 = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}, \quad (4.51)$$

$$F_{2N} = \begin{bmatrix} F_N & F_N \\ F_N & -F_N \end{bmatrix}, \quad (4.52)$$

where the subscripts indicate the size of the transform matrices. It is obvious that the transform matrix of the DHT can be easily derived by using the recursion.

Note that the number of sign changes between consecutive entries in a row (or a column) of a transform matrix (from positive to negative and from negative to positive) is known as *sequency*. It is observed that the sequency does not monotonically increase as the order number of rows (or columns) increases in the DHT. Since sequency bears some similarity to frequency in the Fourier transform, sequency is desired as an increasing function of the order number of rows (or columns). This is realized by the *ordered* Hadamard transform (Gonzalez 1992).

The transformation kernel of the ordered Hadamard transform is defined as

$$f(x, y, u, v) = \frac{1}{N} \prod_{i=0}^{N-1} [(-1)^{p_i(x)d_i(u)} (-1)^{p_i(y)d_i(v)}], \quad (4.53)$$

where the definition of $i, p_i(\arg)$ are the same as defined above for the DWT and DHT. The $d_i(\arg)$ is defined as below.

$$\begin{aligned} d_0(\arg) &= b_{n-1}(\arg) \\ d_1(\arg) &= b_{n-1}(\arg) + b_{n-2}(\arg) \\ &\vdots \\ d_{n-1}(\arg) &= b_1(\arg) + b_0(\arg) \end{aligned} \quad (4.54)$$

The 16 basis images of the ordered Hadamard transform are shown in [Figure 4.5](#) for $N = 4$. It is observed that the variation of the binary basis images becomes more frequent monotonically when u and v increase. Also, we see that the basis image expansion is similar to the frequency expansion of the Fourier transform in the sense that an image is decomposed into components with different variations. In TC, these components with different coefficients are treated differently.

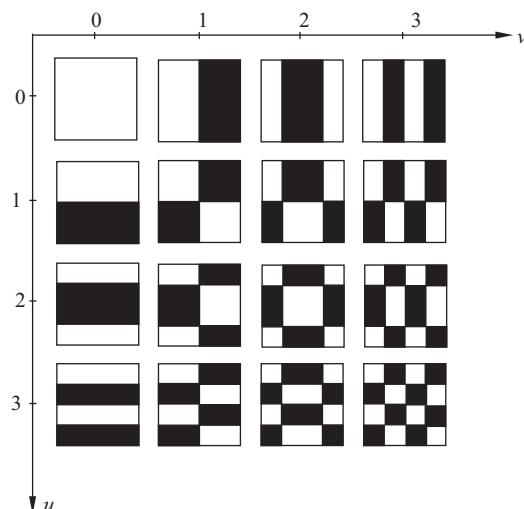


FIGURE 4.5

When $N = 4$, a set of 16 basis images of the ordered DHT.

4.3.4 Discrete Cosine Transform

The discrete cosine transform (DCT) is the most commonly used transform for image and video coding.

4.3.4.1 Background

The DCT, which plays an extremely important role in image and video coding, was established by Ahmed, Natarajan, and Rao (1974). There, it was shown that the *basis member* $\cos[(2x+1)u\pi / 2N]$ is the u th Chebyshev polynomial $T_u(\xi)$ evaluated at the x th zero of $T_N(\xi)$. Recall that the Chebyshev polynomials are defined as

$$T_0(\xi) = 1 / \sqrt{2} \quad (4.55)$$

$$T_K(\xi) = \cos[k \cos^{-1}(\xi)], \quad (4.56)$$

where $T_K(\xi)$ is the k order Chebyshev polynomial and it has k zeros, starting from the 1st zero to the k th zero. Furthermore, it was demonstrated that the basis vectors of 1-D DCT provide a good approximation to the eigenvectors of the class of Toeplitz matrices defined as

$$\begin{bmatrix} 1 & \rho & \rho^2 & \dots & \rho^{N-1} \\ \rho & 1 & \rho & \dots & \rho^{N-2} \\ \rho^2 & \rho & 1 & \dots & \rho^{N-3} \\ \vdots & \vdots & \vdots & \dots & \vdots \\ \rho^{N-1} & \rho^{N-2} & \rho^{N-3} & \dots & 1 \end{bmatrix}, \quad (4.57)$$

where $0 < \rho < 1$.

4.3.4.2 Transformation Kernel

The transformation kernel of the 2-D DCT can be extended straightforwardly from that of 1-D DCT as follows.

$$f(x, y, u, v) = C(u)C(v) \cos\left(\frac{(2x+1)u\pi}{2N}\right) \cos\left(\frac{(2y+1)v\pi}{2N}\right), \quad (4.58)$$

where

$$C(u) = \begin{cases} \sqrt{\frac{1}{N}} & \text{for } u = 0 \\ \sqrt{\frac{2}{N}} & \text{for } u = 1, 2, \dots, N-1 \end{cases} \quad (4.59)$$

$$i(x, y, u, v) = f(x, y, u, v). \quad (4.60)$$

Note that the $C(v)$ is defined the same way as in Equation 4.59. The 64 basis images of the DCT are shown in [Figure 4.6](#) for $N = 8$.

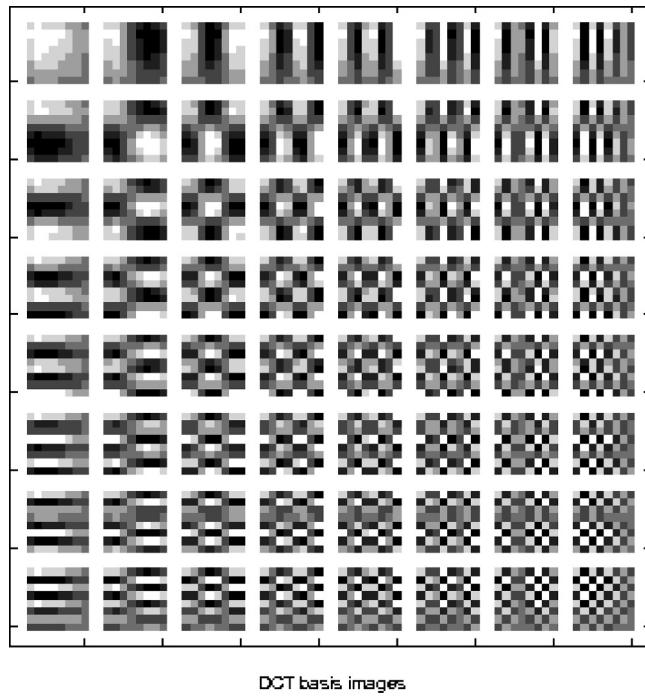


FIGURE 4.6
When $N = 8$, a set of 64 basis images of the DCT.

4.3.4.3 Relationship with DFT

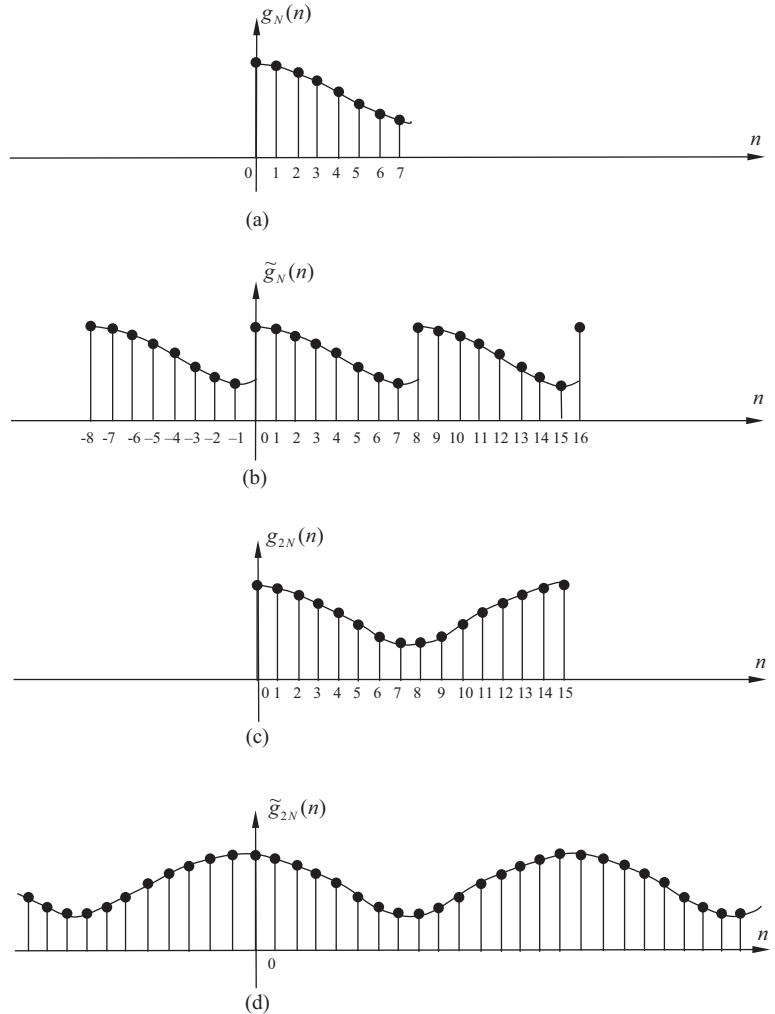
The DCT is closely related to the DFT. This can be examined from an alternative method of defining the DCT. It is known that applying the DFT to an N -point sequence $g_N(n)$, $n = 0, 1, \dots, N - 1$, is equivalent to the following:

1. Repeating $g_N(n)$ every N points, form a periodic sequence, $\tilde{g}_N(n)$, with a fundamental period N . That is,

$$\tilde{g}_N(n) = \sum_{i=-\infty}^{\infty} g_N(n-iN). \quad (4.61)$$

2. Determine the Fourier series expansion of the periodic sequence $\tilde{g}_N(n)$. That is, determine all the coefficients in the Fourier series, which are known to be periodic with the same fundamental period N .
3. Truncate the sequence of the Fourier series coefficients so as to have the same support as that of the given sequence $g_N(n)$. That is, only keep the N coefficients with indexes $0, 1, \dots, N - 1$, and set all the others to equal zero. These N Fourier series coefficients form the DFT of the given N -point sequence $g_N(n)$.

An N -point sequence $g_N(n)$ and the periodic sequence $\tilde{g}_N(n)$, generated from $g_N(n)$, are shown in [Figure 4.7a](#) and [b](#), respectively. In summary, the DFT can be viewed as a correspondence

**FIGURE 4.7**

An example to illustrate the differences and similarities between DFT and DCT (a) Original 1-D input sequence, (b) Formation of a periodic sequence with a fundamental period of N (DFT), (c) Formation of a back-to-back $2N$ sequence, and (d) Formation of a periodic sequence with a fundamental period of $2N$ (DCT).

between two periodic sequences. One is the periodic sequence $\tilde{g}_N(n)$, which is formed by periodically repeating $g_N(n)$. The other is the periodic sequence of Fourier series coefficients of $\tilde{g}_N(n)$.

The DCT of an N -point sequence is obtained via the following three steps.

1. Flip over the given sequence with respect to the end point of the sequence to form a $2N$ -point sequence, $g_{2N}(n)$, as shown in Figure 4.7c. Then form a periodic sequence $\tilde{g}_{2N}(n)$, shown in Figure 4.7d, according to

$$\tilde{g}_{2N}(n) = \sum_{i=-\infty}^{\infty} g_{2N}(n-2iN) \quad (4.62)$$

2. Find the Fourier series coefficients of the periodic sequences $\tilde{g}_{2N}(n)$.
3. Truncate the resultant periodic sequence of the Fourier series coefficients to have the support of the given finite sequence $g_N(n)$. That is, only keep the N coefficients with indexes $0, 1, \dots, N-1$ and set all the others to equal zero. These N Fourier series coefficients form the DCT of the given N -point sequence $g_N(n)$.

A comparison between [Figure 4.7b](#) and [d](#) reveals that the periodic sequence $\tilde{g}_N(n)$ is not smooth. There exist discontinuities at the beginning and end of each period. These end-head discontinuities cause a high-frequency distribution in the corresponding DFT. On the contrary, the periodic sequence $\tilde{g}_{2N}(n)$ does not have this type of discontinuity due to flipping over the given finite sequence. As a result, there is no high-frequency component corresponding to the end-head discontinuities. Hence, the DCT possesses better energy compaction in the low frequencies than the DFT. By energy compaction, we mean more energy is compacted in a fraction of transform coefficients. For instance, it is known that the most energy of an image is contained in a small region of low frequency in the DFT domain. Vivid examples can be found in [Gonzalez \(1992\)](#). In terms of energy compaction, when compared with the KLT (the Hotelling transform is its discrete version), which is known as the optimal, the DCT is the best among the DFT, DWT, DHT, and discrete Harr transform.

Besides this advantage, the DCT can be implemented using the FFT. This can be seen from the above discussion. There, it has been shown that the DCT of an N -point sequence, $g_N(n)$, can be obtained from the DFT of the $2N$ -point sequence $g_{2N}(n)$. Furthermore, the even symmetry in $\tilde{g}_{2N}(n)$ makes the computation required for the DCT of an N -point equal to that required for the DFT of the N -point sequence. Because of these two merits, the DCT is the most popular image transform used in image and video coding. No other transform has been proven to be better than the DCT from a practical standpoint ([Haskell 1996](#)).

4.3.5 Performance Comparison

In this subsection, we compare the performance of a few commonly used transforms in terms of energy compaction, mean square reconstruction error, and computational complexity.

4.3.5.1 Energy Compaction

Since all the transforms we discussed are symmetric (hence, separable) and unitary, the matrix form of the 2-D image transform can be expressed as $T = F^T G F$, as discussed in [Section 4.2.1.3](#). In the 1-D case, the transform matrix F is the counterpart of the matrix Φ discussed in the Hotelling transform. Using the F , one can transform a 1-D column vector \bar{z} into another 1-D column vector \bar{y} . The components of the vector \bar{y} are transform coefficients. The variances of these transform coefficients, and therefore the signal energy associated with the transform coefficients, can be arranged in a nondecreasing order. It can be shown that the total energy before and after the transform remains the same. Therefore, the more energy compacted in a fraction of total coefficients, the better energy compaction the transform has. One measure of energy compaction is the *transform coding gain* G_{TC} , which is defined as the ratio between the arithmetic mean and the geometric mean of the variances of all the components in the transformed vector ([Jayant and Noll 1984](#)).

$$G_{TC} = \frac{\frac{1}{N} \sum_{i=0}^{N-1} \sigma_i^2}{\left(\prod_{i=0}^{N-1} \sigma_i^2 \right)^{\frac{1}{N}}}. \quad (4.63)$$

A larger G_{TC} indicates higher energy compaction. The TC gains for a first-order autoregressive source with $\rho = 0.95$ achieved by using the DCT, DFT, and KLT was reported in Zelinski and Noll (1975), Jayant and Noll (1984). The TC gain afforded by the DCT compares very closely to that of the optimum KLT.

4.3.5.2 Mean Square Reconstruction Error

The performance of the transforms can be compared in terms of the mean square reconstruction error as well. This was mentioned in [Section 4.1.2](#) when we provided a statistical interpretation for TC. That is, after arranging all the N transformed coefficients according to their variances in a nonincreasing order, if $L < N$ and we discard the last $(N - L)$ coefficients to reconstruct the original input signal \bar{z} (similar to what we did with the Hotelling transform), then the mean square reconstruction error is

$$MSE_r = E \left[\|(\bar{z} - \bar{z}')\|^2 \right] = \sum_{i=L+1}^N \sigma_i^2, \quad (4.64)$$

where \bar{z}' denotes the reconstructed vector. Note that in the mean square reconstruction error defined here, the quantization error and transmission error have not been included. Hence, it is sometimes referred to as the mean square approximation error.

Therefore, it is desired to choose a transform so that the transformed coefficients are “more independent” and more energy is concentrated in the first L coefficients. Then it is possible to discard the remaining coefficients to save coding bits without causing significant distortion in input signal reconstruction.

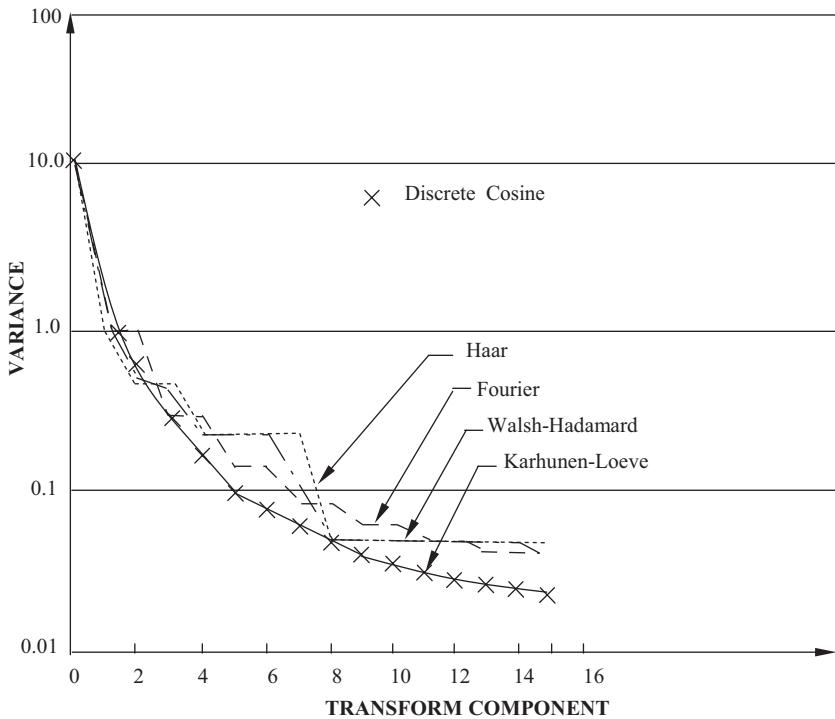
In terms of the mean square reconstruction error, the performance of the DCT, KLT, DFT, DWT, and discrete Haar transform for the 1-D case was reported in Ahmed et al. (1974). The variances of the 16 transform coefficients are shown in [Figure 4.8](#) when $N = 16$, $\rho = 0.95$. Note that N stands for the dimension of the 1-D vector, while the parameter ρ is shown in the Toeplitz matrix (refer to [Equation 4.57](#)). We can see that the DCT compares most closely to the KLT, which is known to be optimum.

Note that the unequal variance distribution among transform coefficients also found application in the field of pattern recognition. Similar results to those in Ahmed et al. (1974) for the DFT, DWT, and Harr transform were reported in Andrews (1971).

A similar analysis can be carried out for the 2-D case (Wintz 1972). Recall that an image $g(x, y)$ can be expressed as a weighted sum of basis images $I_{u,v}$. That is,

$$G = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} T(u, v) I_{u,v}, \quad (4.65)$$

where the weights are transform coefficients. We arrange the coefficients according to their variances in a nonincreasing order. For some choices of the transform (hence, basis images),

**FIGURE 4.8**

Transform coefficient variances when $N = 16$, $\rho = 0.95$. (From Ahmed, N.T et al., *IEEE Trans. Comp.*, 100, 90–93, 1974.)

the coefficients become insignificant after the first L terms, and the image can be approximated well by truncating the coefficients after L . That is,

$$G = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} T(u, v) I_{u,v} \approx \sum_{u=0}^L \sum_{v=0}^L T(u, v) I_{u,v}. \quad (4.66)$$

The mean square reconstruction error is given by

$$MSE_r = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} \sigma_{u,v}^2 \quad (4.67)$$

A comparison among the KLT, DHT, and DFT in terms of the mean square reconstruction error for 2-D array of 16×16 (i.e., 256 transform coefficients) was reported in Figure 5, Wintz (1972). Note that the discrete KLT is image dependent. In the comparison, the KLT is calculated with respect to an image named “Cameraman.” It shows that while the KLT achieves best performance, the other transforms perform closely.

In essence, the criteria of mean square reconstruction error and energy compaction are closely related. It has been shown that the discrete KLT, also known as the Hotelling transform, is the optimum in terms of energy compaction and mean square reconstruction error. The DWT, DHT, DFT, and DCT are close to the optimum (Wintz 1972, Ahmed et al. 1974); however, the DCT is the best among these several *suboptimum* transforms.

Note that the performance comparison among various transforms in terms of bit rate versus distortion in the reconstructed image was reported in Pearl et al. (1972), Ahmed et al. (1974). The same conclusion was drawn. That is, the KLT is optimum, while the DFT, DWT, DCT, and Harr transforms are close in performance. Among the suboptimum transforms, the DCT is the best.

4.3.5.3 Computational Complexity

Note that while the DWT, DHT, DFT, and DCT are input image independent, the discrete KLT (the Hotelling transform) is input dependent. More specifically, the row vectors of the Hotelling transform matrix are transposed eigenvectors of the covariance matrix of the input random vector. So far, there is no fast transform algorithm available. This computational complexity prohibits the Hotelling transform from practical usage. It can be shown that the DWT, DFT, and DCT can be implemented using the FFT algorithm.

4.3.5.4 Summary

As pointed out above, the DCT is the best among the suboptimum transforms in terms of energy compaction. Moreover, the DCT can be implemented using the FFT. Even though a $2N$ -point sequence is involved, the even symmetry makes the computation involved in the N -point DCT equivalent to that of the N -point FFT. For these two reasons, the DCT finds the widest application in image and video coding.

4.4 Bit Allocation

As shown in [Figure 4.2](#), in TC, an input image is first divided into blocks (sub-images). Then a 2-D linear transform is applied to each block. The transformed blocks go through truncation, quantization, and codeword assignment. The last three functions—truncation, quantization, and codeword assignment—are combined and called bit allocation.

From the previous section, it is known that the applied transform decorrelates sub-images. Moreover, it redistributes image energy in the transform domain in such a way that most of the energy is compacted into a small fraction of coefficients. Therefore, it is possible to discard the majority of transform coefficients without introducing significant distortion.

As a result, we see that in TC there are mainly three types of error involved. One is due to truncation. That is, the majority of coefficients are truncated to zero. The other comes from quantization. Transmission error is the third type of error. (Note that truncation can also be considered a special type of quantization.) Recall that the mean square reconstruction error discussed in [Section 4.3.5.2](#) is in fact only related to truncation error. For this reason, it was referred to more precisely as mean square approximation error. In general, the reconstruction error, i.e., the error between the original image signal and the reconstructed image at the receiver, includes three types of error: truncation error, quantization error, and transmission error.

There are two different ways to truncate transform coefficients. One is called *zonal coding*, while the other is *threshold coding*. They are discussed below.

4.4.1 Zonal Coding

In zonal coding, also known as *zonal sampling*, a zone in the transformed block is pre-defined according to a statistical average obtained from many blocks. All transform coefficients in the zone are retained, while all coefficients outside the zone are set to zero. As mentioned in [Section 4.3.5.1](#), the total energy of the image remains the same after applying the transforms discussed there. Since it is known that the DC and low-frequency AC coefficients of the DCT occupy most of the energy, the zone is located in the top-left portion of the transformed block when the transform coordinate system is set conventionally. (Note that by DC we mean $u = v = 0$. By AC we mean u and v do not equal zero simultaneously.) That is, the origin is at the top-left corner of the transformed block. Two typical zones are shown in [Figure 4.9](#). The simplest uniform quantization with natural binary coding can be used to quantize and encode the retained transform coefficients. With this simple technique, there is no overhead side information that needs to be sent to the receiver, since the structure of the zone, the scheme of the quantization, and encoding are known at both the transmitter and receiver.

The coding efficiency, however, may not be very high. This is because the zone is pre-defined based on average statistics. Therefore, some coefficients outside the zone might be large in magnitude, while some coefficients inside the zone may be small in quantity. Uniform quantization and natural binary encoding are simple, but they are known not to be efficient enough.

For further improvement of coding efficiency, an adaptive scheme has to be used. There, a two-pass procedure is applied. In the first pass, the variances of transform coefficients are measured or estimated. Based on the statistics, the quantization and encoding schemes are determined. In the second pass, quantization and encoding are carried out (Habibi and Wintz 1971a, Chen and Smith 1977).

4.4.2 Threshold Coding

In threshold coding, also known as threshold sampling, there is not a predefined zone. Instead, each transform coefficient is compared with a threshold. If it is smaller than the threshold, then it is set to zero. If it is larger than the threshold, it will be retained for quantization and encoding. Compared with zonal coding, this scheme is adaptive in truncation

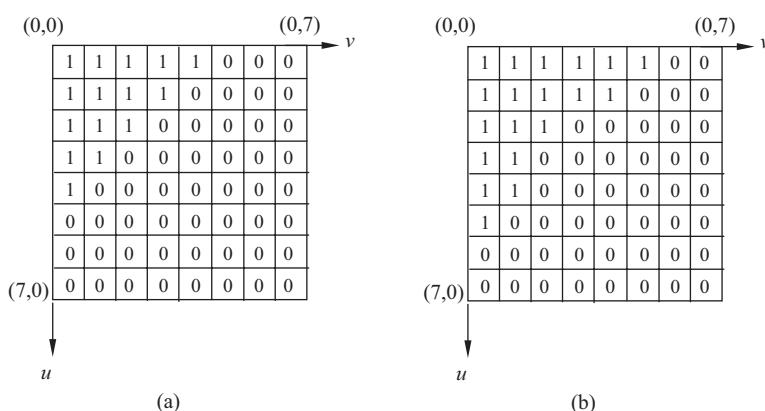


FIGURE 4.9

Two illustrations of zonal coding (a) There are 15 nonzero elements and (b) There are 19 nonzero elements.

in the sense that the coefficients with more energy are retained no matter where they are located. The address of these retained coefficients, however, has to be sent to the receiver as side information. Furthermore, the threshold is determined after an evaluation of all coefficients. Hence, it was usually a two-pass adaptive technique.

Chen and Pratt devised an efficient adaptive scheme to handle threshold coding (Chen and Pratt 1984). It is a one-pass adaptive scheme, in contrast to two-pass adaptive schemes. Hence, it is fast in implementation. With several effective techniques that will be addressed here, it achieved excellent results in TC. Specifically, it demonstrated satisfied quality of reconstructed frames at a bit rate of 0.4 bits/pixel for coding of color images, which corresponds to real-time color television transmission over a 1.5 Mbits/sec channel. This scheme has been adopted by the international still coding standard JPEG. A block diagram of the threshold coding proposed by Chen and Pratt is shown in [Figure 4.10](#). More details and modification made by JPEG will be described in [Chapter 7](#).

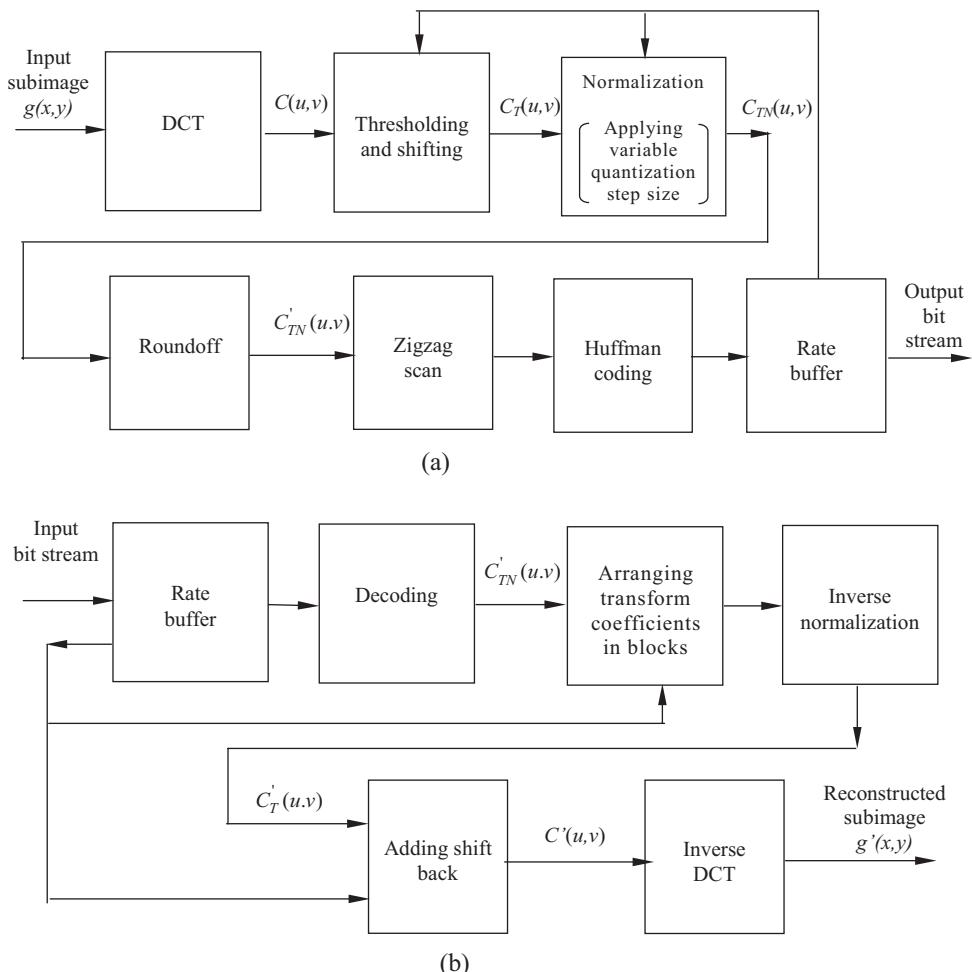


FIGURE 4.10

Block diagram of the algorithm proposed by Chen and Pratt (a) Transmitter and (b) Receiver. (From Chen, W.H. and Pratt, W.K., *IEEE Trans. Commun.*, 32, 225–232, 1984.)

4.4.2.1 Thresholding and Shifting

The DCT is used in the scheme because of its superiority, described in [Section 4.3](#). Here we use $C(u,v)$ to denote the DCT coefficients. The DC coefficient, $C(0,0)$, is processed differently. As mentioned in [Chapter 3](#), the DC coefficients are encoded with differential coding technique. For more detail, refer to [Chapter 7](#). For all the AC coefficients, the following thresholding and shifting are carried out:

$$C_T(u,v) = \begin{cases} C(u,v) - T & \text{if } C(u,v) > T \\ 0 & \text{if } C(u,v) \leq T \end{cases} \quad (4.68)$$

where T on the right-hand side is the threshold. Note that the above equation also implies a shifting of transform coefficients by T . The input-output characteristic of the thresholding and shifting is shown in [Figure 4.11](#).

[Figure 4.12](#) demonstrates that more than 60% of the DCT coefficients normally fall below a threshold value as low as 5. This indicates that with a properly selected threshold value it is possible to set most of the DCT coefficients equal to zero. The threshold value is adjusted by the feedback from the rate buffer, or by the desired bit rate.

4.4.2.2 Normalization and Roundoff

The threshold subtracted transform coefficients $C_T(u,v)$ are normalized before roundoff. The normalization is implemented as follows:

$$C_{TN}(u,v) = \frac{C_T(u,v)}{\Gamma_{u,v}}, \quad (4.69)$$

where the normalization factor $\Gamma_{u,v}$ is controlled by the rate buffer. The roundoff process converts floating point to integer as follows.

$$R[C_{TN}(u,v)] = C_{TN}^*(u,v) = \begin{cases} \lfloor C_{TN}(u,v) + 0.5 \rfloor & \text{if } C_{TN}(u,v) \geq 0 \\ \lceil C_{TN}(u,v) - 0.5 \rceil & \text{if } C_{TN}(u,v) < 0 \end{cases} \quad (4.70)$$

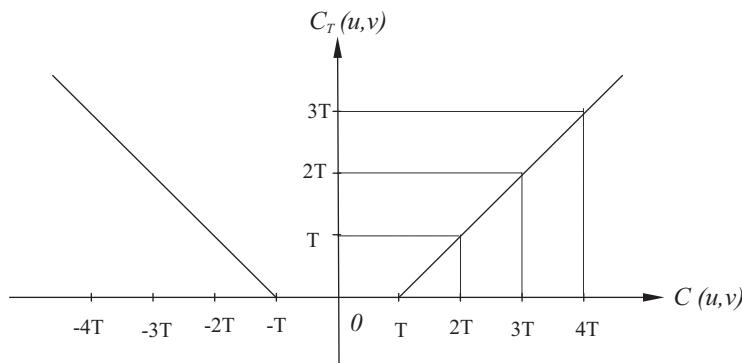


FIGURE 4.11

Input-output characteristic of thresholding and shifting.

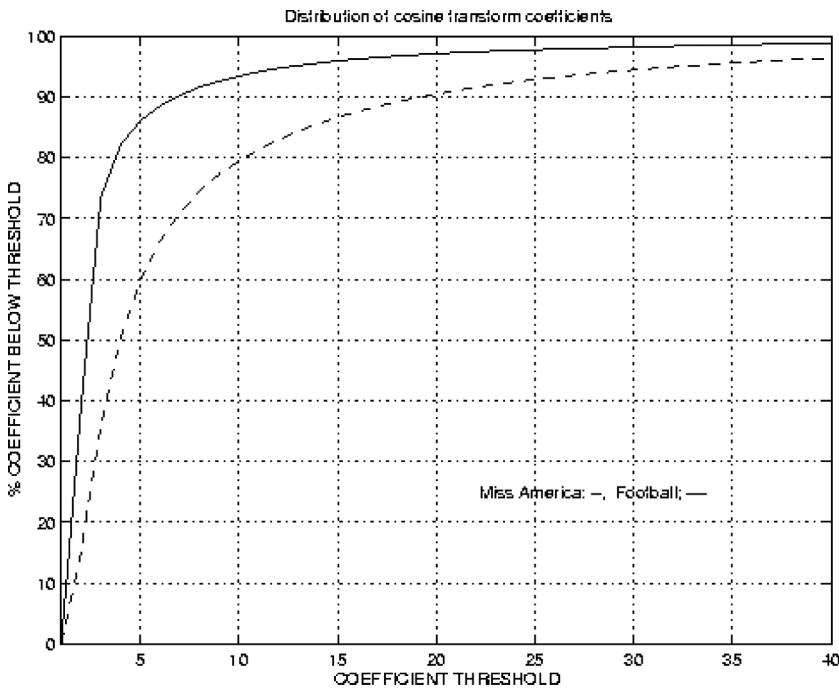


FIGURE 4.12
Amplitude distribution of the DCT coefficients.

where the operator $\lfloor x \rfloor$ means the largest integer smaller than or equal to x and the operator $\lceil x \rceil$ means the smallest integer larger than or equal to x . The input-output characteristics of the normalization and roundoff are shown in Figure 4.13a and b, respectively.

From these input-output characteristics, we can see that the roundoff is a uniform midtread quantizer with a unit quantization step. The combination of normalization and roundoff is equivalent to a uniform midtread quantizer with the quantization step size equal to the normalization factor $\Gamma_{u,v}$. Normalization is a scaling process, which makes the resultant uniform midtread quantizer adapt to the dynamic range of the associated transform coefficient. It is therefore possible for one quantizer design to be applied to various coefficients with different ranges. Obviously, by adjusting the parameter $\Gamma_{u,v}$ (quantization step size), variable bit rate and mean square quantization error can be achieved. The selection of the normalization factors for different transform coefficients can hence take the statistical feature of the images and the characteristics of the human visual system (HVS) into consideration. In general, most image energy is contained in the DC and low-frequency AC transform coefficients. The HVS is more sensitive to a relatively uniform region than to a relatively detailed region, as discussed in Chapter 1. Chapter 1 also mentions that, with regard to the color image, the HVS is more sensitive to the luminance component than to the chrominance components.

These have been taken into consideration in JPEG. A matrix consisting of all the normalization factors is called a quantization table in JPEG. A luminance quantization table and a chrominance quantization table used in JPEG are shown in Figure 4.14. We observe that in general in both tables the small normalization factors are assigned to the DC and

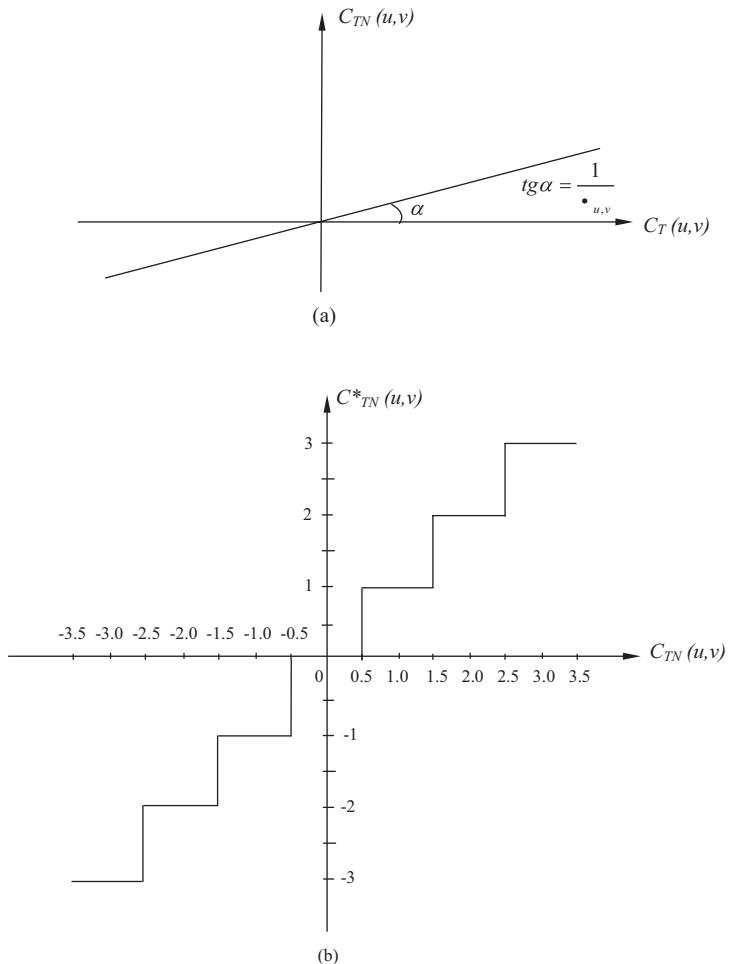


FIGURE 4.13
Input-output characteristic of (a) normalization and (b) roundoff.

| | | | | | | | |
|----|----|----|----|-----|-----|-----|-----|
| 16 | 11 | 10 | 16 | 24 | 40 | 51 | 61 |
| 12 | 12 | 14 | 19 | 26 | 58 | 60 | 55 |
| 14 | 13 | 16 | 24 | 40 | 57 | 69 | 56 |
| 14 | 17 | 22 | 29 | 51 | 87 | 80 | 62 |
| 18 | 22 | 37 | 56 | 68 | 109 | 103 | 77 |
| 24 | 35 | 55 | 64 | 81 | 104 | 113 | 92 |
| 49 | 64 | 78 | 87 | 103 | 121 | 120 | 101 |
| 72 | 92 | 95 | 98 | 112 | 100 | 103 | 99 |

(a)

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| 17 | 18 | 24 | 47 | 99 | 99 | 99 | 99 |
| 18 | 21 | 26 | 66 | 99 | 99 | 99 | 99 |
| 24 | 26 | 56 | 99 | 99 | 99 | 99 | 99 |
| 47 | 66 | 99 | 99 | 99 | 99 | 99 | 99 |
| 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |

(b)

FIGURE 4.14
Quantization tables (a) Luminance quantization table and (b) Chrominance quantization table.

low-frequency AC coefficients. The large Γ 's are associated with the high-frequency transform coefficients. Compared with the luminance quantization table, the chrominance quantization table has larger quantization step sizes for the low- and middle-frequency coefficients and almost the same step sizes for the DC and high-frequency coefficients, indicating that the chrominance components are relatively coarsely quantized, compared with the luminance component.

4.4.2.3 Zigzag Scan

As mentioned at the beginning of this section, while threshold coding is adaptive to the local statistics and hence is more efficient in truncation, threshold coding needs to send the address of retained coefficients to the receiver as overhead side information. An efficient scheme, called zigzag scan, was proposed in Chen and Pratt (1984) and is shown in [Figure 4.15](#). As shown in [Figure 4.12](#), a great majority of transform coefficients has magnitude smaller than a threshold of 3. Consequently, most quantized coefficients are zero. Hence, in the 1-D sequence obtained by zigzag scanning, most of the numbers are zero. A code known as run-length code, discussed in [Chapter 6](#), is very efficient under these circumstances to encode the address information of nonzero coefficients. Run-length of zero coefficients is understood as the number of consecutive zeros in the zigzag scan. Zigzag scanning minimizes the use of run-length codes in the block, hence making codes most efficient.

4.4.2.4 Huffman Coding

Statistical studies of the magnitude of nonzero DCT coefficients and the run-length of zero DCT coefficients in zigzag scanning were conducted in Chen and Pratt (1984). The domination of the coefficients with small amplitude and the short run-lengths was found and is shown in [Figures 4.16](#) and [4.17](#). This justifies the application of the Huffman coding to the magnitude of nonzero transform coefficients and run-lengths of zeros.

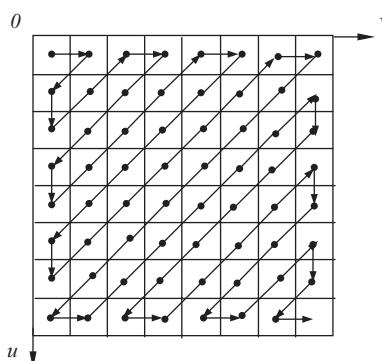
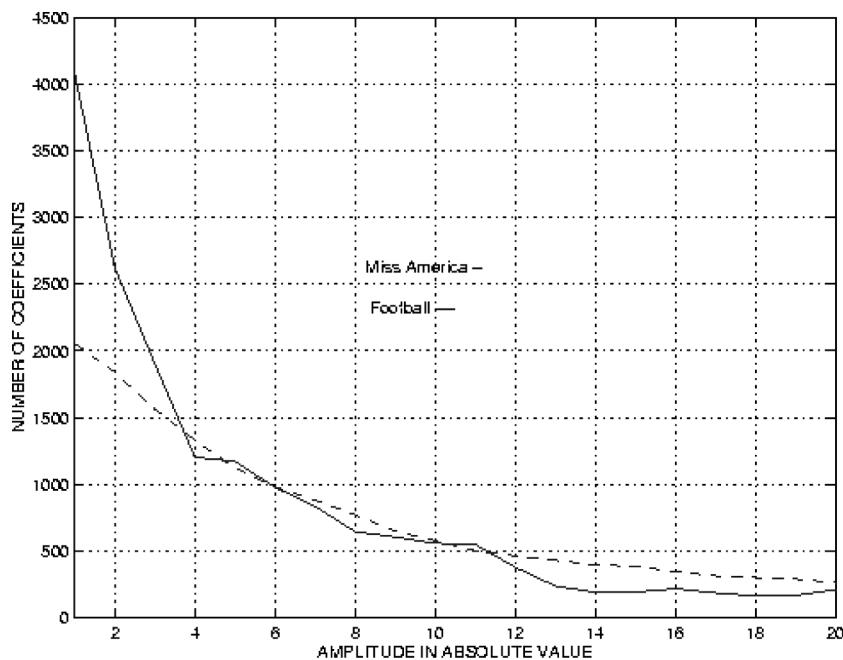
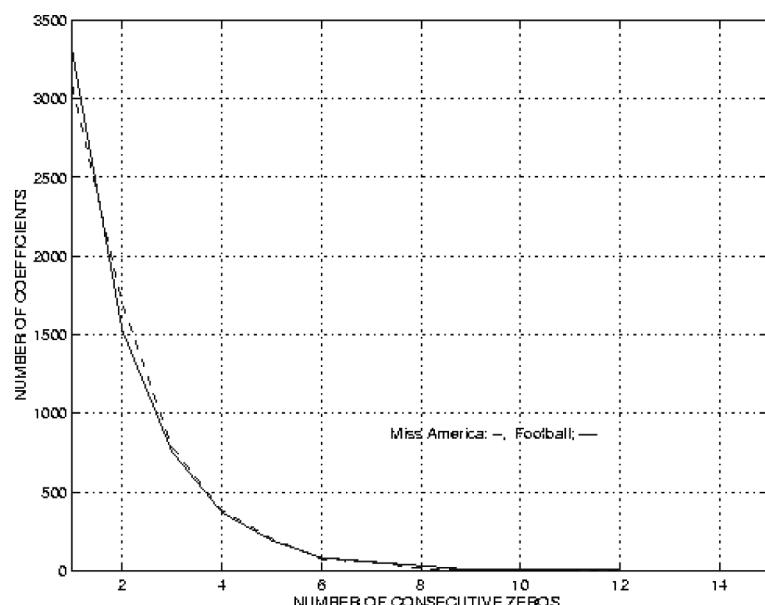


FIGURE 4.15
Zigzag scan of DCT coefficients within an 8×8 block.

**FIGURE 4.16**

Histogram of DCT coefficients in absolute amplitude.

**FIGURE 4.17**

Histogram of zero run length.

4.4.2.5 Special Codewords

Two special codewords were used in Chen and Pratt (1984). One is called *end of block* (EOB). Another is called *run-length prefix*. Once the last nonzero DCT coefficients in the zigzag are coded, EOB is appended, indicating the termination of coding the block. This further saves bits used in coding. Run-length prefix is used to discriminate the run-length codewords from the amplitude codewords.

4.4.2.6 Rate Buffer Feedback and Equalization

As shown in [Figure 4.10](#), a rate buffer accepts a variable-rate data input from the encoding process and provides a fixed-rate data output to the channel. The status of the rate buffer is monitored and fed back to control the threshold and the normalization factor. In this fashion a one-pass adaptation is achieved.

4.5 Some Issues

4.5.1 Effect of Transmission Error

In TC, each pixel in the reconstructed image relies on all transform coefficients in the sub-image where the pixel is located. Hence, a bit reversal transmission error will be spread. That is, an error in a transform coefficient will lead to errors in all the pixels within the sub-image. As discussed in [Section 4.2.3](#), this is one of the reasons the selected sub-image size cannot be very large. Depending on which coefficient is in error, the effect caused by a bit reversal error on the reconstructed image varies. For instance, an error in the DC or a low-frequency AC coefficient may be objectionable, while an error in the high-frequency coefficient may be less noticeable.

4.5.2 Reconstruction Error Sources

As discussed, three sources—truncation (discarding transform coefficients with small variances), quantization, and transmission—contribute to the reconstruction error. It is noted that in TC transform is applied block by block. Quantization and encoding of transform coefficients are also conducted blockwise. At the receiver, reconstructed blocks are put together to form the whole reconstructed image. In the process, block artifacts are produced. Sometimes, even though it may not severely affect an objective assessment of the reconstructed image quality, block artifacts can be annoying to the HVS, especially when the coding rate is low.

To alleviate the blocking effect, several techniques have been proposed. One is to overlap blocks in the source image. Another is to postfilter the reconstructed image along block boundaries. The selection of advanced transforms is an additional possible method (Lim 1990).

In the block overlapping method, when the blocks are finally organized to form the reconstructed image, each pixel in the overlapped regions takes an average value of all its reconstructed gray-level values from multiple blocks. In this method, extra bits are used for those pixels involved in the overlapped regions. For this reason, the overlapped region is usually only one pixel wide.

Due to the sharp transition along block boundaries, block artifacts are of high frequency in nature. Low-pass filtering is hence normally used in the postfiltering method. To avoid the blurring effect caused by low-pass filtering on the nonboundary image area, low-pass postfiltering is only applied to block boundaries. Unlike the block overlapping method, the postfiltering method does not need extra bits. Moreover, it has been shown that the postfiltering method can achieve better results in combating block artifacts (Reeve and Lim 1984, Ramamurthi and Gersho 1986). For these two reasons, the postfiltering method has been adopted by the international coding standards.

4.5.3 Comparison Between DPCM and TC

As mentioned at the beginning of the chapter, both differential coding and TC utilize interpixel correlation and are efficient coding techniques. Comparisons between these two techniques have been reported (Habibi 1971b). Take a look at the techniques discussed in the previous chapter and in this chapter. We can see that differential coding is simpler than TC. This is because the linear prediction and differencing involved in differential coding are simpler than the 2-D transform involved in TC. In terms of the memory requirement and processing delay, differential coding such as DPCM is superior to TC. That is, DPCM needs less memory and has less processing delay than TC. The design of the DPCM system, however, is sensitive to image-to-image variation, and so is its performance. That is, an optimum DPCM design is matched to the statistics of a certain image. When the statistics change, the performance of the DPCM will be affected. On the contrary, TC is less sensitive to the variation in the image statistics. In general, the optimum DPCM coding system with a third- or higher-order predictor performs better than TC when the bit rate is about two to three bits per pixel for single images. When the bit rate is below two to three bits per pixel, TC is normally preferred. As a result, the international still image coding standard JPEG is based on TC, whereas, in JPEG, DPCM is used for coding the DC coefficients of DCT, and information-preserving differential coding is used for lossless still image coding.

4.5.4 Hybrid Coding

A method called hybrid transform/waveform coding, or simply hybrid coding, was devised in order to combine the merits of the two methods. By waveform coding, we mean coding techniques that code the waveform of a signal instead of the transformed signal. DPCM is a waveform coding technique. Hybrid coding combines TC and DPCM coding. That is, TC can be applied first row-wise followed by DPCM coding column-wise, or vice versa. In this way, the two techniques complement each other. That is, the hybrid coding technique simultaneously has TC's small sensitivity to variable image statistics and DPCM's simplicity in implementation.

It is worth mentioning a successful hybrid coding scheme in interframe coding: predictive coding along the temporal domain. Specifically, it uses motion-compensated predictive coding. That is, the motion analyzed from successive frames is used to more accurately predict a frame. The prediction error (in the 2-D spatial domain) is transform coded. This hybrid coding scheme has been very efficient and was adopted by the international video coding standards H.261, H.263, and MPEG 1, 2, and 4.

4.6 Summary

In TC, instead of the original image or some function of the original image in the spatial and/or temporal domain, the image in the transform domain is quantized and encoded. The main idea behind TC is that the transformed version of the image is less correlated. Moreover, the image energy is compacted into a small proper subset of transform coefficients.

The basis vector (1-D) and the basis image (2-D) provide a meaningful interpretation of TC. This type of interpretation considers the original image to be a weighted sum of basis vectors or basis images. The weights are the transform coefficients, each of which is essentially a correlation measure between the original image and the corresponding basis image. These weights are less correlated than the gray-level values of pixels in the original image. Furthermore, they have a great disparity in variance distribution. Some weights have large variances. They are retained and finely quantized. Some weights have small energy. They are retained and coarsely quantized. A vast majority of weights are insignificant and discarded. In this way, a high coding efficiency is achieved in TC. Because the quantized nonzero coefficients have a very nonuniform probability distribution, they can be encoded by using efficient variable-length codes. In summary, three factors—truncation (discarding a great majority of transform coefficients), adaptive quantization, and variable-length coding—contribute mainly to a high coding efficiency of TC.

Several linear, reversible, unitary transforms have been studied and utilized in TC. They include the discrete KLT (the Hotelling transform), the DFT, the Walsh transform, the Hadamard transform, and the DCT. It is shown that the KLT is the optimum. The transform coefficients of the KLT are uncorrelated. The KLT can compact the most energy in the smallest fraction of transform coefficients. However, the KLT is image dependent. There is no fast algorithm to implement it. This prohibits the KLT from practical use in TC. While the rest of the transforms perform closely, the DCT appears to be the best. Its energy compaction is very close to the optimum KLT and it can be implemented using the FFT. The DCT has been found to be efficient not only for still images coding but also for coding residual images (predictive error) in motion-compensated interframe predictive coding. These features make the DCT the most widely used transform in image and video coding.

There are two ways to truncate transform coefficients: zonal coding and threshold coding. In zonal coding, a zone is predefined based on average statistics. The transform coefficients within the zone are retained, while those outside the zone are discarded. In threshold coding, each transform coefficient is compared with a threshold. Those coefficients larger than the threshold are retained, while those smaller are discarded. Threshold coding is adaptive to local statistics. A two-pass procedure is usually taken. That is, the local statistics are measured or estimated in the first pass. The truncation takes place in the second pass. The addresses of the retained coefficients need to be sent to the receiver as overhead side information.

A one-step adaptive framework of TC has evolved as a result of the tremendous research efforts in image coding. It became a base of the international still image coding standard JPEG. Its fundamental components include the DCT transform, thresholding and adaptive quantization of transform coefficients, zigzag scan, Huffman coding of magnitude of the nonzero DCT coefficients and run-length of zeros in the zigzag scan, the codeword of EOB, and rate buffer feedback control.

Threshold and normalization factor are controlled by rate buffer feedback. Since the threshold decides how many transform coefficients are retained and the normalization

factor is actually the quantization step size, the rate buffer has direct impact on the bit rate of the TC system. Selection of quantization steps takes the energy compaction of the DCT and the characteristics of the HVS into consideration. That is, it uses not only statistical redundancy but also psychovisual redundancy to enhance coding efficiency.

After thresholding, normalization, and roundoff are applied to the DCT transform coefficients in a block, a great majority of transform coefficients are set to zero. Zigzag scan can convert the 2-D array of transform coefficients into a 1-D sequence. The number of consecutive zero-valued coefficients in the 1-D sequence is referred to as run-length of zeros and is used to provide address information of nonzero DCT coefficients. Both magnitude of nonzero coefficients and run-length information need to be coded. The statistical analysis has demonstrated that small magnitude and short run-length are dominant. Therefore, efficient lossless entropy coding methods such as Huffman coding and arithmetic coding (the focus of the next chapter) can be applied to magnitude and run-length.

In a reconstructed sub-image, there are three types of error involved: truncation error (some transform coefficients have been set to zero), quantization error, and transmission error. In a broad sense, the truncation can be viewed as a part of the quantization. That is, these truncated coefficients are quantized to zero. The transmission error in terms of bit reversal will affect the whole reconstructed sub-image. This is because, in the inverse transform (such as the inverse DCT), each transform coefficient makes a contribution.

In reconstructing the original image all the sub-images are organized to form the whole image. Therefore, the independent processing of individual sub-images causes block artifacts. Though they may not severely affect the objective assessment of reconstructed image quality, block artifacts can be annoying, especially in low bit rate image coding. Block overlapping and postfiltering are two effective ways to alleviate block artifacts. In the former, neighboring blocks are purposely overlapped by one pixel. In reconstructing the image, those pixels that have been coded more than once take an average of the multiple decoded values. Extra bits are used. In the latter technique, a low-pass filter is applied along boundaries of blocks. No extra bits are required in the process and the effect of combating block artifacts is better than with the former technique.

The selection of sub-image size is an important issue in the implementation of TC. In general, the large size will remove more interpixel redundancy. But it has been shown that the pixel correlation becomes insignificant when the distance of pixels exceeds 20. On the other hand, large size is not suitable for adaptation to local statistics, while adaptation is required in handling nonstationary images. Large size also makes the effect of transmission error spread more widely. For these reasons, sub-image size should not be large. In motion-compensated predictive interframe coding, motion estimation is normally carried out in sizes of 16×16 or 8×8 . To be compatible, the sub-image size in TC is frequently chosen as 8×8 .

Both predictive coding—say, DPCM, and TC—utilize interpixel correlation and are efficient coding schemes. Compared with TC, DPCM is simpler in computation. It needs less storage and has less processing delay. But it is more sensitive to image-to-image variation. On the other hand, TC provides higher adaptation to statistical variation. TC is capable of removing more interpixel correlation, thus providing higher coding efficiency. Traditionally, people consider that predictive coding is preferred if bit rate is in the range of two to three bites per pixel, while TC is preferred when bit rate is below two to three bits per pixel. However, the situation changes. TC becomes the core technology in image and video coding. Many special VLSI chips are designed and manufactured for reducing computational complexity. The complexity becomes less important. Consequently, predictive coding such as DPCM is only used in some very simple applications.

In the context of interframe coding, 3-D (two spatial dimensions and one temporal dimension) TC has not found wide application in practice due to the complexity in computation and storage. Hybrid transform/waveform coding has proven to be very efficient in interframe coding. There, the motion-compensated predictive coding is used along temporal dimension, while TC is used to code the prediction error in two spatial dimensions.

Exercises

- 4.1 Consider the following eight points in a 3-D coordinate system: $(0,0,0)^T, (1,0,0)^T, (0,1,0)^T, (0,0,1)^T, (0,1,1)^T, (1,0,1)^T, (1,1,0)^T, (1,1,1)^T$. Find the mean vector and covariance matrix using the Equations 4.12 and 4.13.
- 4.2 For $N = 4$, find the basis images of the DFT, $I_{u,v}$ when (a) $u = 0, v = 0$, (b) $u = 1, v = 0$, (c) $u = 2, v = 2$, (d) $u = 3, v = 2$. Use both methods discussed in the text, i.e., the method with basis image and the method with basis vectors.
- 4.3 For $N = 4$, find the basis images of the ordered DHT when (a) $u = 0, v = 2$, (b) $u = 1, v = 3$, (c) $u = 2, v = 3$, (d) $u = 3, v = 3$. Verify your results by comparing them with [Figure 4.5](#).
- 4.4 Repeat the previous problem for the DWT, and verify your results by comparing them with [Figure 4.4](#).
- 4.5 Repeat problem 3 for the DCT and $N = 4$.
- 4.6 When $N = 8$, draw the transform matrix F for the DWT, DHT, the order DHT, DFT, and DCT.
- 4.7 The matrix form of forward and inverse 2-D symmetric image transforms is expressed in texts such as (Jayant and Noll 1984) as $T = FGF^T$, and $G = ITI^T$, which are different from Equations 4.28 and 4.29. Can you explain this discrepancy?
- 4.8 Derive Equation 4.64. (Hint: use the concept of basis vectors and the orthogonality of basis vectors.)
- 4.9 Justify that the normalization factor is the quantization step.
- 4.10 The transform used in TC has two functions: decorrelation and energy compaction. Does decorrelation automatically lead to energy compaction? Comment.
- 4.11 Using your own words, explain the main idea behind TC.
- 4.12 Read the techniques by Chen and Pratt presented in [Section 4.4.2](#). Compare them with JPEG discussed in [Chapter 7](#). Comment on the similarity and dissimilarity between them.
- 4.13 How is the one-pass adaptation to local statistics in the algorithm of (Chen and Pratt) achieved?
- 4.14 Using your own words, explain why the DCT is superior to the DFT in terms of energy compaction.
- 4.15 Why is the sub-image size of 8×8 widely used?

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5

Variable-Length Coding: Information Theory Results (II)

Recall the block diagram of encoders shown in [Figure 2.3](#). There are three stages that take place in an encoder: transformation, quantization, and codeword assignment. Quantization was discussed in [Chapter 2](#). Differential coding and transform coding using two different transformation components were covered in [Chapters 3 and 4](#), respectively. In differential coding it is the difference signal that is quantized and encoded, while in transform coding it is the transformed signal that is quantized and encoded. In this chapter and the next chapter, we discuss several codeword assignment (encoding) techniques. In this chapter we cover two types of variable-length coding: Huffman coding and arithmetic coding.

First, we introduce some fundamental concepts of encoding. After that, the rules that must be obeyed by all optimum and instantaneous codes are discussed. Based on these rules, the Huffman coding algorithm is presented. A modified version of the Huffman coding algorithm is introduced as an efficient way to dramatically reduce codebook memory while keeping almost the same optimality.

The promising arithmetic coding algorithm, which is quite different from Huffman coding, is another focus of the chapter. While Huffman coding is a *block-oriented* coding technique, arithmetic coding is a *stream-oriented* coding technique. With improvements in implementation, arithmetic coding has gained increasing popularity. Both Huffman coding and arithmetic coding are included in the international still image coding standard Joint Photographic (image) Experts Group (JPEG). The adaptive arithmetic coding algorithms is adopted by the international bilevel image coding standard Joint Bi-level Image Experts Group (JBIG). Note that the material presented in this chapter can be viewed as a continuation of the information theory results presented in [Chapter 1](#).

5.1 Some Fundamental Results

Prior to presenting Huffman coding and arithmetic coding, we first provide some fundamental concepts and results as necessary background.

5.1.1 Coding an Information Source

Consider an information source, represented by a *source alphabet* S .

$$S = \{s_1, s_2, \dots, s_m\}, \quad (5.1)$$

where $s_i, i = 1, 2, \dots, m$ are *source symbols*. Note that the terms source symbol and information message are used interchangeably in the literature. In this book, however, we would like

to distinguish them. That is, an information message can be a source symbol or a combination of source symbols. We denote *code alphabet* by A and

$$A = \{a_1, a_2, \dots, a_r\}, \quad (5.2)$$

where $a_j, j = 1, 2, \dots, r$ are *code symbols*. A *message code* is a sequence of code symbols that represents a given information message. In the simplest case, a message consists of only a source symbol. Encoding is then a procedure to assign a *codeword* to the source symbol. Namely,

$$s_i \rightarrow A_i = (a_{i1}, a_{i2}, \dots, a_{ik}), \quad (5.3)$$

where the codeword A_i is a string of k code symbols assigned to the source symbol s_i . The term *message ensemble* is defined as the entire set of messages. A code, also known as an *ensemble code*, is defined as a mapping of all the possible sequences of symbols of S (message ensemble) into the sequences of symbols in A .

Note that in binary coding, the number of code symbols r is equal to 2, since there are only two code symbols available: the binary digits “0” and “1.” Two examples are given below to illustrate the above concepts.

Example 5.1

Consider an English article and the ASCII code. Refer to [Table 5.1](#). In this context, the source alphabet consists of all the English letters in both lower and upper cases and all the punctuation marks. The code alphabet consists of the binary 1 and 0. There are a total of 128 seven-bit binary codewords. From [Table 5.1](#), we see that the codeword assigned to the capital letter A is 1000001. That is, A is a source symbol, while 1000001 is its codeword.

TABLE 5.1

Seven-Bit American Standard Code for Information Interchange (ASCII)

| | | 5 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
|------|---|---|---|-----|-----|----|---|---|---|-----|
| Bits | | 6 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 |
| 1 | 2 | 3 | 4 | 7 | 0 | 0 | 0 | 1 | 1 | 1 |
| 0 | 0 | 0 | 0 | NUL | DLE | SP | 0 | @ | P | ' |
| 1 | 0 | 0 | 0 | SOH | DC1 | ! | 1 | A | Q | a |
| 0 | 1 | 0 | 0 | STX | DC2 | " | 2 | B | R | b |
| 1 | 1 | 0 | 0 | ETX | DC3 | # | 3 | C | S | c |
| 0 | 0 | 1 | 0 | EOT | DC4 | \$ | 4 | D | T | d |
| 1 | 0 | 1 | 0 | ENQ | NAK | % | 5 | E | U | e |
| 0 | 1 | 1 | 0 | ACK | SYN | & | 6 | F | V | f |
| 1 | 1 | 1 | 0 | BEL | ETB | ' | 7 | G | W | w |
| 0 | 0 | 0 | 1 | BS | CAN | (| 8 | H | X | h |
| 1 | 0 | 0 | 1 | HT | EM |) | 9 | I | Y | i |
| 0 | 1 | 0 | 1 | LF | SUB | * | : | J | Z | j |
| 1 | 1 | 0 | 1 | VT | ESC | + | ; | K | [| k |
| 0 | 0 | 1 | 1 | FF | FS | , | < | L | \ | l |
| 1 | 0 | 1 | 1 | CR | GS | - | = | M |] | m |
| 0 | 1 | 1 | 1 | SO | RS | . | > | N | ^ | n |
| 1 | 1 | 1 | 1 | SI | US | / | ? | O | — | o |
| | | | | | | | | | | DEL |

(Continued)

TABLE 5.1 (Continued)

Seven-Bit American Standard Code for Information Interchange (ASCII)

| | | | |
|-----|-----------------------|-----|---------------------------|
| NUL | Null, or all zeros | DC1 | Device control 1 |
| SOH | Start of heading | DC2 | Device control 2 |
| STX | Start of text | DC3 | Device control 3 |
| ETX | End of text | DC4 | Device control 4 |
| EOT | End of transmission | NAK | Negative acknowledgment |
| ENQ | Enquiry | SYN | Synchronous idle |
| ACK | Acknowledge | ETB | End of transmission block |
| BEL | Bell, or alarm | CAN | Cancel |
| BS | Backspace | EM | End of medium |
| HT | Horizontal tabulation | SUB | Substitution |
| LF | Line feed | ESC | Escape |
| VT | Vertical tabulation | FS | File separator |
| FF | Form feed | GS | Group separator |
| CR | Carriage return | RS | Record separator |
| SO | Shift out | US | Unit separator |
| SI | Shift in | SP | Space |
| DLE | Data link escape | DEL | Delete |

TABLE 5.2

A (5,2) Linear Block Code

| Source Symbol | Codeword |
|---------------|-----------|
| S1 (0 0) | 0 0 0 0 0 |
| S2 (0 1) | 1 0 1 0 0 |
| S3 (1 0) | 0 1 1 1 1 |
| S4 (1 1) | 1 1 0 1 1 |

Example 5.2

Table 5.2 lists what is known as the (5,2) code. It is a linear block code. In this example, the source alphabet consists of the four (2^2) source symbols listed in the left column of the table: 00, 01, 10, and 11. The code alphabet consists of the binary 1 and 0. There are four codewords listed in the right column of the table. From the table, we see that the code assigns a five-bit codeword to each source symbol. Specifically, the codeword of the source symbol 00 is 00000. The source symbol 01 is encoded as 10100. 01111 is the codeword assigned to 10. The symbol 11 is mapped to 11011.

5.1.2 Some Desired Characteristics

To be practical in use, codes need to have some desired characteristics (Abramson 1963). Some of the characteristics are addressed in this subsection.

5.1.2.1 Block Code

A code is said to be a block code if it maps each source symbol in S into a fixed codeword in A . Hence, the codes listed in the above two examples are block codes.

5.1.2.2 Uniquely Decodable Code

A code is uniquely decodable if it can be unambiguously decoded. Obviously, a code has to be uniquely decodable if it is to be in use.

Example 5.3

[Table 5.3](#) specifies a code. Obviously, it is not uniquely decodable since if a binary string “00” is received we do not know which of the following two source symbols has been sent out: s_1 or s_3 .

Nonsingular Code

A block code is nonsingular if all the codewords are distinct.

Example 5.4

[Table 5.4](#) gives a nonsingular code since all four codewords are distinct. If a code is not a nonsingular code, i.e., at least two codewords are identical, then the code is not uniquely decodable. Notice that, however, a nonsingular code does not guarantee unique decodability. The code shown in [Table 5.4](#) is such an example in that it is nonsingular while it is not uniquely decodable. It is not uniquely decodable because once the binary string “11” is received, we do not know if the source symbols transmitted are s_1 followed by s_1 or simply s_2 .

The n th Extension of a Block Code

The n th extension of a block code, which maps the source symbol s_i into the codeword A_i , is a block code that maps the sequences of source symbols $s_{i1}s_{i2}\dots s_{in}$ into the sequences of codewords $A_{i1}A_{i2}\dots A_{in}$.

A Necessary and Sufficient Condition of Block Codes’ Unique Decodability

A block code is uniquely decodable if and only if the n th extension of the code is nonsingular for every finite n .

TABLE 5.3

A Not Uniquely Decodable Code

| Source Symbol | Codeword |
|---------------|----------|
| s_1 | 0 0 |
| s_2 | 1 0 |
| s_3 | 0 0 |
| s_4 | 1 1 |

TABLE 5.4

A Nonsingular Code

| Source Symbol | Codeword |
|---------------|----------|
| s_1 | 1 |
| s_2 | 1 1 |
| s_3 | 0 0 |
| s_4 | 0 1 |

TABLE 5.5

The Second Extension of the Nonsingular Block Code Shown in Example 5.4

| Source Symbol | Codeword | Source Symbol | Codeword |
|---------------|----------|---------------|----------|
| $S_1 S_1$ | 1 1 | $S_3 S_1$ | 0 0 1 |
| $S_1 S_2$ | 1 1 1 | $S_3 S_2$ | 0 0 1 1 |
| $S_1 S_3$ | 1 0 0 | $S_3 S_3$ | 0 0 0 0 |
| $S_1 S_4$ | 1 0 1 | $S_3 S_4$ | 0 0 0 1 |
| $S_2 S_1$ | 1 1 1 | $S_4 S_1$ | 0 1 1 |
| $S_2 S_2$ | 1 1 1 1 | $S_4 S_2$ | 0 1 1 1 |
| $S_2 S_3$ | 1 1 0 0 | $S_4 S_3$ | 0 1 0 0 |
| $S_2 S_4$ | 1 1 0 1 | $S_4 S_4$ | 0 1 0 1 |

Example 5.5

The second extension of the nonsingular block code shown in Example 5.4 is listed in [Table 5.5](#). Clearly, this second extension of the code is not a nonsingular code, since the entries $s_1 s_2$ and $s_2 s_1$ are the same. This confirms the nonunique decodability of the nonsingular code in Example 5.4.

5.1.2.3 Instantaneous Codes

5.1.2.3.1 Definition of Instantaneous Codes

A uniquely decodable code is said to be instantaneous if it is possible to decode each codeword in a code symbol sequence without knowing the succeeding codewords.

Example 5.6

[Table 5.6](#) lists three uniquely decodable codes. The first one is in fact a two-bit natural binary code. In decoding we can immediately tell which source symbols are transmitted since each codeword has the same length. In the second code, code symbol “1” functions like a comma. Whenever we see a “1,” we know it is the end of the codeword. The third code is different from the previous two codes in that if we see a “10” string we are not sure if it corresponds to s_2 until we see a succeeding “1.” Specifically, if the next code symbol is “0,” we still cannot tell if it is s_3 since the next one may be “0” (hence, s_4) or “1” (hence, s_3). In this example, the next “1” belongs to the succeeding codeword. Therefore, we see that code 3 is uniquely decodable. It is not instantaneous, however.

Definition of the j th Prefix

Assume a codeword $A_i = a_{i1}a_{i2}\dots a_{ik}$. Then the sequences of code symbols $a_{i1}a_{i2}\dots a_{ij}$ with $1 \leq j \leq k$ is the j th order prefix of the codeword A_i .

TABLE 5.6

Three Uniquely Decodable Codes

| Source Symbol | Code 1 | Code 2 | Code 3 |
|---------------|--------|---------|---------|
| S_1 | 0 0 | 1 | ~1 |
| S_2 | 0 1 | 0 1 | 1 0 |
| S_3 | 1 0 | 0 0 1 | 1 0 0 |
| S_4 | 1 1 | 0 0 0 1 | 1 0 0 0 |

Example 5.7

If a codeword is 11001, it has the following five prefixes: 11001, 1100, 110, 11, 1. The first order prefix is 1, while the fifth-order prefix is 11001.

A Necessary and Sufficient Condition of Being Instantaneous Codes

A code is instantaneous if and only if no codeword is a prefix of some other codeword.

This condition is often referred to as the *prefix condition*. Hence, the instantaneous code is also called the prefix condition code or sometimes simply the prefix code. In many applications, we need a block code that is nonsingular, uniquely decodable, and instantaneous.

5.1.2.4 Compact Code

A uniquely decodable code is said to be compact if its average length is the minimum among all other uniquely decodable codes based on the same source alphabet S and code alphabet A . A compact code is also referred to as a *minimum-redundancy* code, or an *optimum* code.

Note that the average length of a code was defined in [Chapter 1](#) and is restated below.

5.1.3 Discrete Memoryless Sources

This is the simplest model of an information source. In this model, the symbols generated by the source are independent of each other. That is, the source is memoryless or it has a zero-memory.

Consider the information source expressed in Equation 5.1 as a discrete memoryless source. The occurrence probabilities of the source symbols can be denoted by $p(s_1), p(s_2), \dots, p(s_m)$. The lengths of the codewords can be denoted by l_1, l_2, \dots, l_m . The average length of the code is then equal to

$$L_{avg} = \sum_{i=1}^m l_i p(s_i). \quad (5.4)$$

Recall Shannon's first theorem, i.e., the noiseless coding theorem, described in [Chapter 1](#). The average length of the code is bounded below by the entropy of the information source. The entropy of the source S is defined as $H(S)$ and

$$H(S) = - \sum_{i=1}^m p(s_i) \log_2 p(s_i). \quad (5.5)$$

Recall that entropy is the average amount of information contained in a source symbol. In [Chapter 1](#) the efficiency of a code, η , is defined as the ratio between the entropy and the code. That is, $\eta = H(S) / L_{avg}$. The redundancy of the code, ζ , is defined as $\zeta = 1 - \eta$.

5.1.4 Extensions of a Discrete Memoryless Source

Instead of coding each source symbol in a discrete source alphabet, it is often useful to code blocks of symbols. It is, therefore, necessary to define the n th extension of a discrete memoryless source.

5.1.4.1 Definition

Consider the zero-memory source alphabet S defined in Equation 5.1. That is, $S = \{s_1, s_2, \dots, s_m\}$. If n symbols are grouped into a block, then there is a total of m^n blocks. Each block is considered as a new source symbol. These m^n blocks thus form an information source alphabet, called the n th extension of the source S , which is denoted by S^n .

5.1.4.2 Entropy

Let each block be denoted by β_i and

$$\beta_i = (s_{i1}, s_{i2}, \dots, s_{in}). \quad (5.6)$$

Then we have the following relation due to the memoryless assumption.

$$p(\beta_i) = \prod_{j=1}^n p(s_{ij}). \quad (5.7)$$

Hence, the relationship between the entropy of the source S and the entropy of its n th extension is as follows.

$$H(S^n) = n \cdot H(S). \quad (5.8)$$

Example 5.8

Table 5.7 lists a source alphabet. Its second extension is listed in **Table 5.8**. The entropy of the source and its second extension are calculated below.

$$H(S) = -0.6 \cdot \log_2(0.6) - 0.4 \cdot \log_2(0.4) \approx 0.97,$$

$$H(S^2) = -0.36 \cdot \log_2(0.36) - 2 \cdot 0.24 \cdot \log_2(0.24) - 0.16 \cdot \log_2(0.16) \approx 1.94.$$

It is seen that $H(S^2) = 2H(S)$.

TABLE 5.7
A Discrete Memoryless Source Alphabet

| Source Symbol | Occurrence Probability |
|---------------|------------------------|
| S_1 | 0.6 |
| S_2 | 0.4 |

TABLE 5.8
The Second Extension of the Source Alphabet Shown in **Table 5.7**

| Source Symbol | Occurrence Probability |
|---------------|------------------------|
| $S_1 S_1$ | 0.36 |
| $S_2 S_2$ | 0.24 |
| $S_2 S_1$ | 0.24 |
| $S_1 S_2$ | 0.16 |

5.1.4.3 Noiseless Source Coding Theorem

The noiseless source coding theorem, also known as Shannon's first theorem, was presented in [Chapter 1](#), but without a mathematical expression. Here, we provide some mathematical expressions in order to give more insight about the theorem.

For a discrete zero-memory information source S , the noiseless coding theorem can be expressed as

$$H(S) \leq L_{avg} < H(S) + 1, \quad (5.9)$$

that is, there exists a variable-length code whose average length is bounded below by the entropy of the source (that is encoded) and bounded above by the entropy plus 1. Since the n th extension of the source alphabet, S^n , is itself a discrete memoryless source, we can apply the above result to it. That is,

$$H(S^n) \leq L_{avg}^n < H(S^n) + 1, \quad (5.10)$$

where L_{avg}^n is the average codeword length of a variable-length code for the S^n . Since $H(S^n) = nH(S)$ and $L_{avg}^n = nL_{avg}$, we have

$$H(S) \leq L_{avg} < H(S) + \frac{1}{n}. \quad (5.11)$$

Therefore, when coding blocks of n source symbols, the noiseless source coding theory states that for an arbitrary positive number ε , there is a variable-length code that satisfies the following:

$$H(S) \leq L_{avg} < H(S) + \varepsilon \quad (5.12)$$

as n is large enough. That is, the average number of bits used in coding per source symbol is bounded below by the entropy of the source and is bounded above by the sum of the entropy and an arbitrary positive number. To make ε arbitrarily small, i.e., to make the average length of the code arbitrarily close to the entropy, we have to make the block size n large enough. This version of the noiseless coding theorem suggests a way to make the average length of a variable-length code approach the source entropy. It is known, however, that the high coding complexity that occurs when n approaches infinity makes implementation of the code impractical.

5.2 Huffman Codes

Consider the source alphabet defined in [Equation 5.1](#). The method of encoding source symbols according to their probabilities suggested in [Shannon \(1948\)](#), [Fano \(1949\)](#) is not optimum. It approaches the optimum, however, when the block size n approaches infinity. This results in a large storage requirement and high computational complexity.

In many cases, we need a direct encoding method that is optimum and instantaneous (hence, uniquely decodable) for an information source with finite source symbols in source alphabet S . Huffman code is the first such optimum code (Huffman 1952) and is the technique most frequently used at present. It can be used for r -ary encoding as $r > 2$. For the notational brevity, however, we discuss only the Huffman coding used in the binary case presented here.

5.2.1 Required Rules for Optimum Instantaneous Codes

Let us rewrite Equation 5.1 as follows.

$$S = (s_1, s_2, \dots, s_m). \quad (5.13)$$

Without loss of generality, assume the occurrence probabilities of the source symbols are as follows:

$$p(s_1) \geq p(s_2) \geq \dots \geq p(s_{m-1}) \geq p(s_m). \quad (5.14)$$

Since we are seeking the optimum code for S , the lengths of codewords assigned to the source symbols should be

$$l_1 \leq l_2 \leq \dots \leq l_{m-1} \leq l_m. \quad (5.15)$$

Based on the requirements of the optimum and instantaneous code, Huffman derived the following rules (restrictions):

$$1. l_1 \leq l_2 \leq \dots \leq l_{m-1} = l_m. \quad (5.16)$$

Equations 5.14 and 5.16 imply that when the source symbol occurrence probabilities are arranged in a nonincreasing order, the length of the corresponding codewords should be in a nondecreasing order. In other words, the codeword length of a more probable source symbol should not be longer than that of a less probable source symbol. Furthermore, the length of the codewords assigned to the two least probable source symbols should be the same.

2. The codewords of the two least probable source symbols should be the same except for their last bits.
3. Each possible sequence of length $l_m - 1$ bits must be used either as a codeword or must have one of its prefixes used as a codeword.

Rule 1 can be justified as follows. If the first part of the rule, i.e., $l_1 \leq l_2 \leq \dots \leq l_{m-1}$ is violated, say, $l_1 > l_2$, then we can exchange the two codewords to shorten the average length of the code. This means the code is not optimum, which contradicts the assumption that the code is optimum. Hence, it is impossible. That is, the first part of rule 1 has to be the case. Now assume that the second part of the rule is violated, i.e., $l_{m-1} < l_m$. (Note that $l_{m-1} > l_m$ can be shown to be impossible by using the same reasoning we just used to prove the first part of the rule.) Since the code is instantaneous, codeword A_{m-1} is not a prefix of codeword A_m . This implies that the last bit in the codeword A_m is redundant. It can be removed to reduce the average length of the code, implying that the code is not optimum. This contradicts the assumption, thus proving rule 1.

Rule 2 can be justified as follows. As in the above, A_{m-1} and A_m are the codewords of the two least probable source symbols. Assume that they do not have the identical prefix of the order $l_m - 1$. Since the code is optimum and instantaneous, codewords A_{m-1} and A_m cannot have prefixes of any order that are identical to other codewords. This implies that we can drop the last bits of A_{m-1} and A_m to achieve a lower average length. This contradicts the optimum code assumption. It proves that rule 2 has to be the case.

Rule 3 can be justified using a similar strategy to that used above. If a possible sequence of length $l_m - 1$ has not been used as a codeword and any of its prefixes have not been used as codewords, then it can be used in place of the codeword of the m th source symbol, resulting in a reduction of the average length L_{avg} . This is a contradiction to the optimum code assumption and it justifies the rule.

5.2.2 Huffman Coding Algorithm

Based on these three rules, we see that the two least probable source symbols have equal-length codewords. These two codewords are identical except for the last bits, the binary 0 and 1, respectively. Therefore, these two source symbols can be combined to form a single new symbol. Its occurrence probability is the sum of two source symbols, i.e., $p(s_{m-1}) + p(s_m)$. Its codeword is the common prefix of order $l_m - 1$ of the two codewords assigned to s_m and s_{m-1} , respectively. The new set of source symbols thus generated is referred to as the first auxiliary source alphabet, which is one source symbol less than the original source alphabet. In the first auxiliary source alphabet, we can rearrange the source symbols according to a nonincreasing order of their occurrence probabilities. The same procedure can be applied to this newly created source alphabet. A binary 0 and a binary 1 are, respectively, assigned to the last bits of the two least probable source symbols in the alphabet. The second auxiliary source alphabet will again have one source symbol less than the first auxiliary source alphabet. The procedure continues. In some step, the resultant source alphabet will have only two source symbols. At this time, we combine them to form a single source symbol with a probability of 1. The coding is then complete.

Let's go through the following example to illustrate the above Huffman algorithm.

Example 5.9

Consider a source alphabet whose six source symbols and their occurrence probabilities are listed in [Table 5.9](#). [Figure 5.1](#) demonstrates the Huffman coding procedure applied. In the example, among the two least probable source symbols encountered at each step, we assign binary 0 to the top symbol and binary 1 to the bottom symbol.

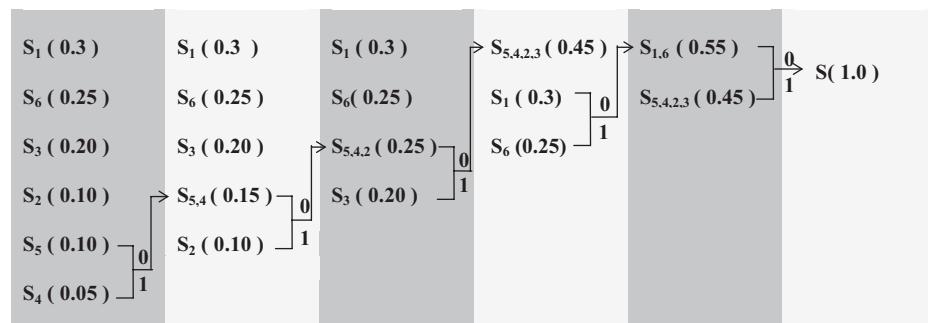


FIGURE 5.1

Huffman coding procedure in Example 5.9.

TABLE 5.9

The Source Alphabet, and Huffman Codes in Example 5.9

| Source Symbol | Occurrence Probability | Codeword Assigned | Length of Codeword |
|---------------|------------------------|-------------------|--------------------|
| S_1 | 0.3 | 00 | 2 |
| S_2 | 0.1 | 101 | 3 |
| S_3 | 0.2 | 11 | 2 |
| S_4 | 0.05 | 1001 | 4 |
| S_5 | 0.1 | 1000 | 4 |
| S_6 | 0.25 | 01 | 2 |

5.2.2.1 Procedures

In summary, the Huffman coding algorithm consists of the following steps.

1. Arrange all source symbols in such a way that their occurrence probabilities are in a nonincreasing order.
2. Combine the two least probable source symbols:
 - a. Form a new source symbol with a probability equal to the sum of the probabilities of the two least probable symbols.
 - b. Assign a binary 0 and a binary 1 to the two least probable symbols.
3. Repeat until the newly created auxiliary source alphabet contains only one source symbol.
4. Start from the source symbol in the last auxiliary source alphabet and trace back to each source symbol in the original source alphabet to find the corresponding codewords.

5.2.2.2 Comments

First, it is noted that the assignment of the binary 0 and 1 to the two least probable source symbols in the original source alphabet and each of the first $(u-1)$ auxiliary source alphabets can be implemented in two different ways. Here, u denotes the total number of the auxiliary source symbols in the procedure. Hence, there is a total of 2^u possible Huffman codes. In Example 5.9, there are five auxiliary source alphabets, hence a total of $2^5 = 32$ different codes. Note that each is optimum: that is, each has the same average length.

Second, in sorting the source symbols, there may be more than one symbol having equal probabilities. This results in multiple arrangements of symbols, hence multiple Huffman codes. While all of these Huffman codes are optimum, they may have some other different properties. For instance, some Huffman codes result in the minimum codeword length variance (Sayood 1996). This property is desired for applications in which a constant bit rate is required.

Third, Huffman coding can be applied to r-ary encoding with $r > 2$. That is, code symbols are r-ary with $r > 2$.

5.2.2.3 Applications

As a systematic procedure to encode a finite discrete memoryless source, the Huffman code has found wide application in image and video coding. Recall that it has been used in differential coding and transform coding. In transform coding, as introduced in [Chapter 4](#), the magnitude of the quantized transform coefficients and the run-length of zeros in the zigzag scan are encoded by using the Huffman code.

5.3 Modified Huffman Codes

5.3.1 Motivation

As a result of Huffman coding, a set of all the codewords, called a codebook, is created. It is an agreement between the transmitter and the receiver. Consider the case where the occurrence probabilities are skewed, i.e., some are large, while some are small. Under these circumstances, the improbable source symbols take a disproportionately large amount of memory space in by the codebook. The size of the codebook will be very large if the number of the improbable source symbols is large. A large size codebook requires a large memory space and increases the computational complexity. A modified Huffman procedure was therefore devised in order to reduce the memory requirement while keeping almost the same optimality (Hankamer 1979).

Example 5.10

Consider a source alphabet consisting of 16 symbols, each being a four-bit binary sequence. That is, $S = \{s_i, i = 1, 2, \dots, 16\}$. The occurrence probabilities are

$$p(s_1) = p(s_2) = 1/4,$$

$$p(s_3) = p(s_4) = \dots = p(s_{16}) = 1/28.$$

The source entropy can be calculated as follows.

$$H(S) = 2 \cdot \left(-\frac{1}{4} \log_2 \frac{1}{4} \right) + 14 \cdot \left(-\frac{1}{28} \log_2 \frac{1}{28} \right) \approx 3.404 \quad \text{bits/symbol.}$$

Applying the Huffman coding algorithm, we find that the codeword lengths associated with the symbols are: $l_1 = l_2 = 2$, $l_3 = 4$, and $l_4 = l_5 = \dots = l_{16} = 5$, where l_i denotes the length of the i th codeword. The average length of Huffman code is

$$L_{avg} = \sum_{i=1}^{16} p(s_i)l_i = 3.464 \quad \text{bits/symbol.}$$

We see that the average length of Huffman code is quite close to the lower entropy bound. It is noted, however, that the required codebook memory, M (defined as the sum of the codeword lengths), is quite large:

$$M = \sum_{i=1}^{16} l_i = 73 \quad \text{bits}$$

This number is obviously larger than the average codeword length multiplied by the number of codewords. This should not come as a surprise since the average here is in the statistical sense instead of in the arithmetic sense. When the total number of improbable symbols increases, the required codebook memory space will increase dramatically, resulting in a great demand on memory space.

5.3.2 Algorithm

Consider a source alphabet S that consists of 2^v binary sequences, each of length v . In other words, each source symbol is a v -bit codeword in the natural binary code. The occurrence probabilities are highly skewed and there is a large number of improbable symbols in S . The modified Huffman coding algorithm is based on the following idea: lumping all the improbable source symbols into a category named ELSE (Weaver 1978). The algorithm is described below.

1. Categorize the source alphabet S into two disjoint groups, S_1 and S_2 , such that

$$S_1 = \left\{ s_i \mid p(s_i) > \frac{1}{2^v} \right\} \quad \text{and} \quad (5.17)$$

$$S_2 = \left\{ s_i \mid p(s_i) \leq \frac{1}{2^v} \right\}. \quad (5.18)$$

2. Establish a source symbol ELSE with its occurrence probability equal to $p(S_2)$.
3. Apply the Huffman coding algorithm to the source alphabet S_3 with $S_3 = S_1 \cup \text{ELSE}$.
4. Convert the codebook of S_3 to that of S as follows.
 - a. Keep the same codewords for those symbols in S_1 .
 - b. Use the codeword assigned to ELSE as a prefix for those symbols in S_2 .

5.3.3 Codebook Memory Requirement

Codebook memory M is the sum of the codeword lengths. The M required by Huffman coding with respect to the original source alphabet S is

$$M = \sum_{i \in S} l_i = \sum_{i \in S_1} l_i + \sum_{i \in S_2} l_i, \quad (5.19)$$

where l_i denotes the length of the i th codeword, as defined previously. In the case of the modified Huffman coding algorithm, the memory required M_{mH} is

$$M_{mH} = \sum_{i \in S_3} l_i = \sum_{i \in S_1} l_i + l_{\text{ELSE}}, \quad (5.20)$$

where l_{ELSE} is the length of the codeword assigned to ELSE. The above equation reveals the big savings in memory requirement when the probability is skewed. The following example is used to illustrate the modified Huffman coding algorithm and the resulting dramatic memory savings.

Example 5.11

In this example, we apply the modified Huffman coding algorithm to the source alphabet presented in Example 5.10. We first lump the 14 symbols having the least occurrence probabilities together to form a new symbol ELSE. The probability of ELSE is the sum of the 14 probabilities. That is,

$$p(\text{ELSE}) = \frac{1}{28} \cdot 14 = \frac{1}{2}$$

Apply Huffman coding to the new source alphabet $S_3 = \{s_1, s_2, \text{ELSE}\}$, as shown in [Figure 5.2](#).

From [Figure 5.2](#), it is seen that the codewords assigned to symbols s_1, s_2 and ELSE are, respectively, 10, 11, and 0. Hence, for every source symbol lumped into ELSE, its codeword is 0 followed by the original four-bit binary sequence. Therefore,

$$M_{mH} = 2 + 2 + 1 = 5 \quad \text{bits},$$

i.e., the required codebook memory is only five bits. Compared with 73 bits required by Huffman coding (refer to Example 5.10), there is a savings of 68 bits in codebook memory space. Similar to the comment made in Example 5.10, the memory savings will be even larger if the probability distribution is skewed more severely and the number of improbable symbols is larger. The average length of the modified Huffman algorithm is

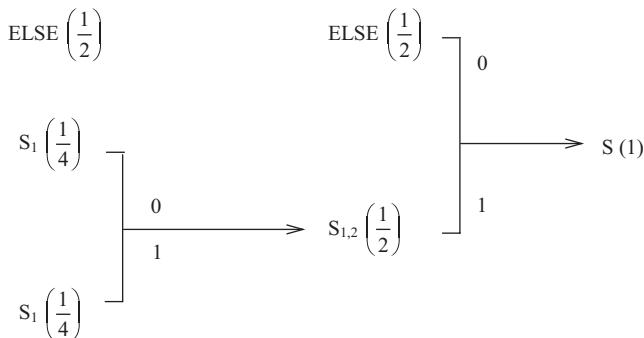
$$L_{avg,mH} = \frac{1}{4} \cdot 2 \cdot 2 + \frac{1}{28} \cdot 5 \cdot 14 = 3.5 \quad \text{bits/symbol}$$

This demonstrates that modified Huffman coding retains almost the same coding efficiency as that achieved by Huffman coding.

5.3.4 Bounds on Average Codeword Length

It has been shown that the average length of the modified Huffman codes satisfies the following condition.

$$H(S) \leq L_{avg} < H(S) + 1 - p \log_2 p, \quad (5.21)$$

**FIGURE 5.2**

The modified Huffman coding procedure in Example 5.11.

where $p = \sum_{s_i \in S_2} p(s_i)$. It is seen that, compared with the noiseless source coding theorem, the upper bound of the code average length is increased by a quantity of $-p\log_2 p$. In Example 5.11, it is seen that the average length of the modified Huffman code is close to that achieved by the Huffman code. Hence, the modified Huffman code is almost optimum.

5.4 Arithmetic Codes

Arithmetic coding, which is quite different from Huffman coding, is gaining increasing popularity. In this section, we will first analyze the limitations of Huffman coding. Then, the principle of arithmetic coding will be introduced. Finally, some implementation issues are discussed briefly.

5.4.1 Limitations of Huffman Coding

As seen in [Section 5.2](#), Huffman coding is a systematic procedure for encoding a source alphabet, with each source symbol having an occurrence probability. Under these circumstances, Huffman coding is optimum in the sense that it produces a minimum coding redundancy. It has been shown that the average codeword length achieved by Huffman coding satisfies the following inequality (Gallagher 1978).

$$H(S) \leq L_{avg} < H(S) + p_{max} + 0.086, \quad (5.22)$$

where $H(S)$ is the entropy of the source alphabet, and p_{max} denotes the maximum occurrence probability in the set of the source symbols. This inequality implies that the upper bound of the average codeword length of Huffman code is determined by the entropy and the maximum occurrence probability of the source symbols being encoded.

In the case where the probability distribution among source symbols is skewed (some probabilities are small, while some are quite large), the upper bound may be large, implying that the coding redundancy may not be small. Imagine the following extreme situation. There are only two source symbols. One has a very small probability, while the other has a very large probability (very close to 1). The entropy of the source alphabet in this case is close to 0 since the uncertainty is very small. Using Huffman coding, however, we need two bits: one for each. That is, the average codeword length is 1, which means that the redundancy is very close to 1. This agrees with Equation 5.22. This inefficiency is due to the fact that Huffman coding always encodes a source symbol with an integer number of bits.

The noiseless coding theorem (reviewed in [Section 5.1](#)) indicates that the average codeword length of a block code can approach the source alphabet entropy when the block size approaches infinity. As the block size approaches infinity, the storage required, the codebook size, and the coding delay will approach infinity, however, and the complexity of the coding will be out of control. Fortunately, it is often the case that when the block size is large enough in practice the average codeword length of a block code has been rather close to the source alphabet entropy.

The fundamental idea behind Huffman coding and Shannon-Fano coding (devised a little earlier than Huffman coding [Bell 1990]) is block coding. That is, some codeword

having an integral number of bits is assigned to a source symbol. A message may be encoded by cascading the relevant codewords. It is the *block-based* approach that is responsible for the limitations of Huffman codes.

Another limitation is that when encoding a message that consists of a sequence of source symbols the *n*th extension Huffman coding needs to enumerate all possible sequences of source symbols having the same length, as discussed in coding the *n*th extended source alphabet. This is not computationally efficient.

Quite different from Huffman coding, arithmetic coding is *stream-based*. It overcomes the drawbacks of Huffman coding. A string of source symbols is encoded as a string of code symbols. It is hence free of the integral-bits-per-source-symbol restriction and is more efficient. Arithmetic coding may reach the theoretical bound to coding efficiency specified in the noiseless source coding theorem for any information source. Below, we introduce the principle of arithmetic coding, from which we can see the stream-based nature of arithmetic coding.

5.4.2 The Principle of Arithmetic Coding

To understand the different natures of Huffman coding and arithmetic coding, let us look at Example 5.12, where we use the same source alphabet and the associated occurrence probabilities used in Example 5.9. In this example, however, a string of source symbols $s_1s_2s_3s_4s_5s_6$ is encoded. Note that we consider the terms *string* and *stream* to be slightly different. By *stream*, we mean a message or possibly several messages, which may correspond to quite a long sequence of source symbols. Moreover, *stream* gives a dynamic “flavor.” Later on, we will see that arithmetic coding is implemented in an incremental manner. Hence, *stream* is a suitable term to use for arithmetic coding. In this example, however, only six source symbols are involved. Hence, we consider the term *string* to be suitable, aiming at distinguishing it from the term *block*.

Example 5.12

The set of six source symbols and their occurrence probabilities are listed in [Table 5.10](#). In this example, the string to be encoded using arithmetic coding is $s_1s_2s_3s_4s_5s_6$. In the following four subsections we will use this example to illustrate the principle of arithmetic coding and decoding.

TABLE 5.10
Source Alphabet and Cumulative Probabilities
in Example 5.12

| Source Symbol | Occurrence Probability | Associated Subintervals | CP |
|---------------|------------------------|-------------------------|------|
| S_1 | 0.3 | (0, 0.3) | 0 |
| S_2 | 0.1 | (0.3, 0.4) | 0.3 |
| S_3 | 0.2 | (0.4, 0.6) | 0.4 |
| S_4 | 0.05 | (0.6, 0.65) | 0.6 |
| S_5 | 0.1 | (0.65, 0.75) | 0.65 |
| S_6 | 0.25 | (0.75, 1.0) | 0.75 |

5.4.2.1 Dividing Interval (0,1) into Subintervals

As pointed out by Elias, it is not necessary to sort out source symbols according to their occurrence probabilities. Therefore, in Part (a) of [Figure 5.3](#) the six symbols are arranged in their natural order from symbols s_1, s_2, \dots , up to s_6 . The real interval between 0 and 1 is divided into six subintervals, each having a length of $p(s_i), i = 1, 2, \dots, 6$. Specifically, the interval denoted by $(0, 1)$ —where 0 is included in (the left end is closed) and 1 is excluded from (the right end is open) the interval—is divided into six subintervals. The first subinterval $(0, 0.3)$ corresponds to s_1 and has a length of $p(s_1)$, i.e., 0.3. Similarly, the subinterval $(0, 0.3)$ is said to be closed on the left and open on the right. The remaining five subintervals are similarly constructed. All six subintervals thus formed are disjoint and their union is equal to the interval $(0, 1)$. This is because the sum of all the probabilities is equal to 1.

We list the sum of the preceding probabilities, known as *cumulative probability* (CP; Langdon 1984), in the right-most column of [Table 5.10](#) as well. Note that the concept

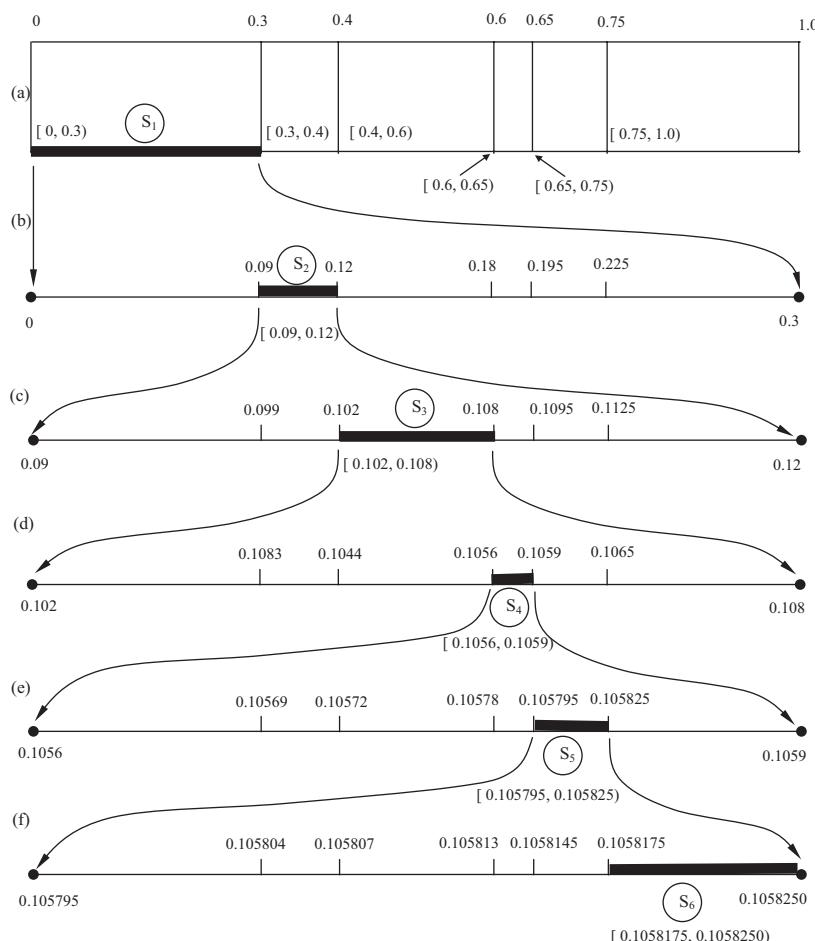


FIGURE 5.3

Arithmetic coding working on the same source alphabet as that in Example 5.9. The encoded symbol string is $S_1 S_2 S_3 S_4 S_5 S_6$.

of CP is slightly different from that of cumulative distribution function (CDF) in probability theory. Recall that in the case of discrete random variables the CDF is defined as follows.

$$CDF(s_i) = \sum_{j=1}^i p(s_j). \quad (5.23)$$

The CP is defined as

$$CP(s_i) = \sum_{j=1}^{i-1} p(s_j), \quad (5.24)$$

where $CP(s_1) = 0$ is defined. Now we see each subinterval has its lower end point located at $CP(s_i)$. The width of each subinterval is equal to the probability of the corresponding source symbol. A subinterval can be completely defined by its lower end point and its width. Alternatively, it is determined by its two end points: the lower and upper end points (sometimes also called the left and right end points).

Now consider encoding the string of source symbols $s_1s_2s_3s_4s_5s_6$ with the arithmetic coding method.

5.4.2.2 Encoding

5.4.2.2.1 Encoding the First Source Symbol

Refer to Part (a) of [Figure 5.3](#). Since the first symbol is s_1 , we pick up its subinterval $(0, 0.3)$. Picking up the subinterval $(0, 0.3)$ means that any real number in the subinterval, i.e., any real number equal to or greater than 0 and smaller than 0.3, can be a pointer to the subinterval, thus representing the source symbol s_1 . This can be justified by considering that all the six subintervals are disjoint.

5.4.2.2.2 Encoding the Second Source Symbol

Refer to Part (b) of [Figure 5.3](#). We use the same procedure as used in Part (a) to divide the interval $(0, 0.3)$ into six subintervals. Since the second symbol to be encoded is s_2 , we pick up its subinterval $(0.09, 0.12)$.

Notice that the subintervals are recursively generated from Part (a) to Part (b). It is known that an interval may be completely specified by its lower end point and width. Hence, the subinterval recursion in the arithmetic coding procedure is equivalent to the following two recursions: end point recursion and width recursion.

From interval $(0, 0.3)$ derived in Part (a) to interval $(0.09, 0.12)$ obtained in Part (b), we can conclude the following lower end point recursion:

$$L_{new} = L_{current} + W_{current} \cdot CP_{new}, \quad (5.25)$$

where L_{new} , $L_{current}$ represent, respectively, the lower end points of the new and current recursions, and the $W_{current}$ and the CP_{new} denote, respectively, the width of the interval in the current recursion and the CP in the new recursion. The width recursion is

$$W_{new} = W_{current} \cdot p(s_i), \quad (5.26)$$

where W_{new} , and $p(s_i)$ are, respectively, the width of the new subinterval and the probability of the source symbol s_i that is being encoded. These two recursions, also called double recursion (Langdon 1984), play a central role in arithmetic coding.

5.4.2.2.3 Encoding the Third Source Symbol

Refer to Part (c) of [Figure 5.3](#). When the third source symbol is encoded, the subinterval generated above in Part (b) is similarly divided into six subintervals. Since the third symbol to encode is s_3 , its subinterval (0.102, 0.108) is picked up.

5.4.2.2.4 Encoding the Fourth, Fifth, and Sixth Source Symbols

Refer to Parts (d), (e), and (f) of [Figure 5.3](#). The subinterval division is carried out according to Equations 5.25 and 5.26. The symbols s_4 , s_5 and s_6 are encoded. The final subinterval generated is (0.1058175, 0.1058250).

That is, the resulting subinterval (0.1058175, 0.1058250) can represent the source symbol string $s_1s_2s_3s_4s_5s_6$. Note that in this example decimal digits instead of binary digits are used. In binary arithmetic coding, the binary digits 0 and 1 are used.

5.4.2.3 Decoding

As seen in this example, for the encoder of arithmetic coding, the input is a source symbol string, and the output is a subinterval. Let us call this the final subinterval or the resultant subinterval. Theoretically, any real numbers in the interval can be the code string for the input symbol string since all subintervals are disjoint. Often, however, the lower end of the final subinterval is used as the code string. Now let us examine how the decoding process is carried out with the lower end of the final subinterval.

Decoding sort of reverses what encoding has done. The decoder knows the encoding procedure and therefore has the information contained in Part (a) of [Figure 5.3](#). It compares the lower end point of the final subinterval 0.1058175 with all the end points in Part (a). It is determined that

$$0 < 0.1058175 < 0.3.$$

That is, the lower end falls into the subinterval associated with the symbol s_1 . Therefore, the symbol s_1 is first decoded.

Once the first symbol is decoded, the decoder may know the partition of subintervals shown in Part (b) of [Figure 5.3](#). It is then determined that

$$0.09 < 0.1058175 < 0.12.$$

That is, the lower end is contained in the subinterval corresponding to the symbol s_2 . As a result, s_2 is the second decoded symbol.

The procedure repeats itself until all six symbols are decoded. That is, based on Part (c) in [Figure 5.3](#), it is found that

$$0.102 < 0.1058175 < 0.108.$$

The symbol s_3 is decoded. Then, the symbols s_4, s_5, s_6 are subsequently decoded because the following inequalities are determined:

$$0.1056 < 0.1058175 < 0.1059$$

$$0.105795 < 0.1058175 < 0.1058250$$

$$0.1058145 < 0.1058175 < 0.1058250$$

Note that a terminal symbol is necessary to inform the decoder to stop decoding.

The above procedure gives us an idea of how decoding works. The decoding process, however, does not need to construct Parts (b), (c), (d), (e), and (f) of [Figure 5.3](#). Instead, the decoder only needs the information contained in Part (a) of [Figure 5.3](#). Decoding can be split into the following three steps: *comparison*, *readjustment* (subtraction), and *scaling* (Langdon 1984).

As described above, through comparison we decode the first symbol s_1 . From the way Part (b) of [Figure 5.3](#) is constructed, we know the decoding of s_2 can be accomplished as follows. We subtract the lower end of the subinterval associated with s_1 in Part (a), that is, 0 in this example from the lower end of the final subinterval 0.1058175, resulting in 0.1058175. Then we divide this number by the width of the subinterval associated with s_1 , i.e., the probability of s_1 , 0.3, resulting in 0.352725. Looking at Part (a) of [Figure 5.3](#), it is found that

$$0.3 < 0.352725 < 0.4$$

That is, the number is within the subinterval corresponding to s_2 . Therefore, the second decoded symbol is s_2 . Note that these three decoding steps exactly “undo” what encoding did.

To decode the third symbol, we subtract the lower end of the subinterval with s_2 , 0.3 from 0.352725, obtaining 0.052725. This number is divided by the probability of s_2 , 0.1, resulting in 0.52725. The comparison of 0.52725 with end points in Part (a) reveals that the third decoded symbol is s_3 .

In decoding the fourth symbol, we first subtract the lower end of the s_3 ’s subinterval in Part (a), 0.4 from 0.52725, getting 0.12725. Dividing 0.12725 by the probability of s_3 , 0.2, results in 0.63625. Referring to Part (a), we decode the fourth symbol as s_4 by comparison.

Subtraction of the lower end of the subinterval of s_4 in Part (a), 0.6, from 0.63625 leads to 0.03625. Division of 0.03625 by the probability of s_4 , 0.05, produces 0.725. The comparison between 0.725 and the end points in Part (a) decodes the fifth symbol as s_5 .

Subtracting 0.725 by the lower end of the subinterval associated with s_5 in Part (a), 0.65, gives 0.075. Dividing 0.075 by the probability of s_5 , 0.1, generates 0.75. The comparison indicates that the sixth decoded symbol is s_6 .

In summary, considering the way in which Parts (b), (c), (d), (e), and (f) of [Figure 5.3](#) are constructed, we see that the three steps discussed in the decoding process—comparison, readjustment, and scaling—exactly “undo” what the encoding procedure has done.

5.4.2.4 Observations

Both encoding and decoding involve only arithmetic operations (addition and multiplication in encoding, subtraction and division in decoding). This explains the name *arithmetic coding*.

We see that an input source symbol string $s_1s_2s_3s_4s_5s_6$, via encoding, corresponds to a subinterval $(0.1058175, 0.1058250)$. Any number in this interval can be used to denote the string of the source symbols.

We also observe that arithmetic coding can be carried out in an *incremental* manner. That is, source symbols are fed into the encoder one by one and the final subinterval is refined continually, i.e., the code string is generated continually. Furthermore, it is done in a manner called *first in first out* (FIFO). That is, the source symbol encoded first is decoded first. This manner is superior to that of *last in first out* (LIFO). This is because FIFO is suitable for adaptation to the statistics of the symbol string.

It is obvious that the width of the final subinterval becomes smaller and smaller when the length of the source symbol string becomes larger and larger. This causes what is known as the precision problem. It is this problem that prohibited arithmetic coding from practical usage for quite a long period of time. Only after this problem was solved in the late 1970s did arithmetic coding become an increasingly important coding technique.

It is necessary to have a termination symbol at the end of an input source symbol string. In this way, an arithmetic coding system is able to know when to terminate decoding.

Compared with Huffman coding, arithmetic coding is quite different. Basically, Huffman coding converts each source symbol into a fixed codeword with an integral number of bits, while arithmetic coding converts a source symbol string to a code symbol string. To encode the same source symbol string, Huffman coding can be implemented in two different ways. One way is shown in Example 5.9. We construct a fixed codeword for each source symbol. Since Huffman coding is instantaneous, we can cascade the corresponding codewords to form the output, a 17-bit code string 00.101.11.1001.1000.01, where, for easy reading, the five periods are used to indicate different codewords. As we see that for the same source symbol string, the final subinterval obtained by using arithmetic coding is $(0.1058175, 0.1058250)$. It is noted that a decimal in binary number system, 0.00011011111111, which is of 15 bits, is equal to the decimal in decimal number system, 0.1058211962, which falls into the final subinterval representing the string $s_1s_2s_3s_4s_5s_6$. This indicates that, for this example, arithmetic coding is more efficient than Huffman coding.

Another way is to form a sixth extension of the source alphabet as discussed in [Section 5.1.4](#): treat each group of six source symbols as a new source symbol, calculate its occurrence probability by multiplying the related six probabilities, then apply the Huffman coding algorithm to the sixth extension of the discrete memoryless source. This is called the sixth extension of Huffman block code (refer to [Section 5.1.2.2](#)). In other words, in order to encode the source string $s_1s_2s_3s_4s_5s_6$, (the sixth extension of) Huffman coding encodes all of the $6^6 = 46656$ codewords in the sixth extension of the source alphabet. This implies a high complexity in implementation and a large codebook. It is therefore not efficient.

Note that we use the decimal fraction in this section. In binary arithmetic coding, we use the binary fraction. In Langdon (1984) both binary source and code alphabets are used in binary arithmetic coding.

Similar to the case of Huffman coding, arithmetic coding is also applicable to r-ary encoding with $r > 2$.

5.4.3 Implementation Issues

As mentioned, the final subinterval resulting from arithmetic encoding of a source symbol stream becomes smaller and smaller as the length of the source symbol string increases. That is, the lower and upper bounds of the final subinterval become closer and closer. This causes a growing precision problem. It is this problem that prohibited arithmetic coding

from practical usage for a long period of time. This problem has been resolved and the finite precision arithmetic is now used in arithmetic coding. This advance is due to the incremental implementation of arithmetic coding.

5.4.3.1 Incremental Implementation

Recall Example 5.12. As source symbols come in one by one, the lower and upper ends of the final subinterval get closer and closer. In [Figure 5.3](#), these lower and upper ends in Example 5.12 are listed. We observe that after the third symbol, s_3 , is encoded, the resultant subinterval is (0.102, 0.108). That is, the two most significant decimal digits are the same and they remain the same in the encoding process. Hence, we can transmit these two digits without affecting the final code string. After the fourth symbol s_4 is encoded, the resultant subinterval is (0.1056, 0.1059). That is, one more digit, 5, can be transmitted. Or we say the cumulative output is now .105. After the sixth symbol is encoded, the final subinterval is (0.1058175, 0.1058250). The cumulative output is 0.1058. Refer to [Table 5.11](#). This important observation reveals that we are able to incrementally transmit output (the code symbols) and receive input (the source symbols that need to be encoded).

5.4.3.2 Finite Precision

With the incremental manner of transmission of encoded digits and reception of input source symbols, it is possible to use finite precision to represent the lower and upper bounds of the resultant subinterval, which gets closer and closer as the length of the source symbol string becomes long.

Instead of floating-point math, integer math is used. The potential problems known as underflow and overflow, however, need to be carefully monitored and controlled (Bell 1990).

5.4.3.3 Other Issues

There are some other problems that need to be handled in implementation of binary arithmetic coding. Two of them are listed below (Langdon 1981).

TABLE 5.11
Final Subintervals and Cumulative Output in
Example 5.12

| Source Symbol | Final Subinterval | | Cumulative Output |
|---------------|-------------------|-----------|-------------------|
| | Lower End | Upper End | |
| S_1 | 0 | 0.3 | 0.10 |
| S_2 | 0.09 | 0.12 | 0.105 |
| S_3 | 0.102 | 0.108 | 0.105 |
| S_4 | 0.1056 | 0.1059 | 0.1058 |
| S_5 | 0.105795 | 0.105825 | |
| S_6 | 0.1058175 | 0.1058250 | |

5.4.3.3.1 Eliminating Multiplication

The multiplication in the recursive division of subintervals is expensive in hardware as well as software. It can be avoided in binary arithmetic coding so as to simplify the implementation of binary arithmetic coding. The idea is to approximate the lower end of the interval by the closest binary fraction 2^{-Q} , where Q is an integer. Consequently, the multiplication by 2^{-Q} becomes a right shift by Q bits. A simpler approximation to eliminate multiplication is used in the Skew Coder (Langdon 1982) and the Q-Coder (Pennebaker 1988).

5.4.3.3.2 Carry-Over Problem

Carry-over takes place in the addition required in the recursion updating the lower end of the resultant subintervals. A carry may *propagate* over q bits. If the q is larger than the number of bits in the fixed-length register utilized in finite precision arithmetic, the carry-over problem occurs. To block the carry-over problem, a technique known as "bit stuffing" is used, in which an additional buffer register is utilized.

For detailed discussion on the various issues involved, readers are referred to Langdon (1981, 1982, 1984), Pennebaker (1988, 1992). Some computer programs of arithmetic coding in C language can be found in Bell (1990), Nelson (1996).

5.4.4 History

The idea of encoding by using CP in some ordering and decoding by comparison of magnitude of binary fraction was introduced in Shannon's celebrated paper (Shannon 1948). The recursive implementation of arithmetic coding was devised by Elias. This unpublished result was first introduced by Abramson as a note in his book on information theory and coding (Abramson 1963). The result was further developed by Jelinek in his book on information theory (Jelinek 1968). The growing precision problem prevented arithmetic coding from practical usage, however. The proposal of using finite precision arithmetic was made independently by Pasco (1976) and Rissanen (1976). Practical arithmetic coding was developed by several independent groups (Rissanen 1979, Rubin 1979, Guazzo 1980). A well-known tutorial paper on arithmetic coding appeared in Langdon (1984). The tremendous efforts made in IBM led to a new form of adaptive binary arithmetic coding known as the Q-coder (Pennebaker 1988). Based on the Q-coder, the activities of the international still image coding standards JPEG andJBIG combined the best features of the various existing arithmetic coders and developed the binary arithmetic coding procedure known as the QM-coder (Pennebaker 1992).

5.4.5 Applications

Arithmetic coding is becoming popular. Note that in text and bilevel image applications there are only two source symbols (black and white), and the occurrence probability is skewed. Therefore, binary arithmetic coding achieves high coding efficiency. It has been successfully applied to bilevel image coding (Langdon 1981) and adopted by the international standards for bilevel image compression JBIG. It has also been adopted by the international still image coding standard JPEG. More in this regard is covered in the next chapter when we introduce JBIG.

5.5 Summary

So far in this chapter, not much has been explicitly discussed regarding the term variable-length codes. It is known that if source symbols in a source alphabet are equally probable, i.e., their occurrence probabilities are the same, then fixed-length codes such as the natural binary code are a reasonable choice. When the occurrence probabilities are, however, unequal, variable-length codes should be used in order to achieve high coding efficiency. This is one of the restrictions on the minimum redundancy codes imposed by Huffman. That is, the length of the codeword assigned to a probable source symbol should not be larger than that associated with a less probable source symbol. If the occurrence probabilities happen to be the integral powers of $1/2$, then choosing the codeword length equal to $-\log_2 p(s_i)$ for a source symbol s_i having the occurrence probability $p(s_i)$ results in minimum redundancy coding. In fact, the average length of the code thus generated is equal to the source entropy.

Huffman devised a systematic procedure to encode a source alphabet consisting of finitely many source symbols, each having an occurrence probability. It is based on some restrictions imposed on the optimum, instantaneous codes. By assigning codewords with variable lengths according to variable probabilities of source symbols, Huffman coding results in minimum redundancy codes, or optimum codes for short. These have found wide applications in image and video coding and have been adopted in the international still image coding standard JPEG and video coding standards H.261, H.263, and MPEG 1, 2.

When some source symbols have small probabilities and their number is large, the size of the codebook of Huffman codes will require a large memory space. The modified Huffman coding technique employs a special symbol to lump all the symbols with small probabilities together. As a result, it can reduce the codebook memory space drastically while retaining almost the same coding efficiency as that achieved by the conventional Huffman coding technique.

On the one hand, Huffman coding is optimum as a block code for a fixed-source alphabet. On the other hand, compared with the source entropy (the lower bound of the average codeword length) it is not efficient when the probabilities of a source alphabet are skewed with the maximum probability being large. This is caused by the restriction that Huffman coding can only assign an integral number of bits to each codeword.

Another limitation of Huffman coding is that it has to enumerate and encode all the possible groups of n source symbols in the n th extension Huffman code, even though there may be only one such group that needs to be encoded.

Arithmetic coding can overcome the limitations of Huffman coding because it is stream-oriented rather than block-oriented. It translates a stream of source symbols into a stream of code symbols. It can work in an incremental manner. That is, the source symbols are fed into the coding system one by one and the code symbols are output continually. In this stream-oriented way, arithmetic coding is more efficient. It can approach the lower coding bounds set by the noiseless source coding theorem for various sources.

The recursive subinterval division (equivalently, the double recursion, the lower end recursion, and width recursion) is the heart of arithmetic coding. Several measures have been taken in the implementation of arithmetic coding. They include the incremental manner, finite precision, and the elimination of multiplication. Due to its merits, binary arithmetic coding has been adopted by the international bilevel image coding standard JBIG and still image coding standard JPEG. It is becoming an increasingly important coding technique.

Exercises

- 5.1 What does the noiseless source coding theorem state (using your own words)? Under what condition does the average code length approach the source entropy? Comment on the method suggested by the noiseless source coding theorem.
- 5.2 What characterizes a block code? Consider another definition of block code in Blahut (1986): A block code breaks the input data stream into blocks of fixed length n and encodes each block into a codeword of fixed length m . Are these two definitions (the one above and the one in [Section 5.1](#), which comes from Abramson [1963]) essentially the same? Explain.
- 5.3 Is a uniquely decodable code necessarily a prefix condition code?
- 5.4 For text encoding, there are only two source symbols for black and white. It is said that Huffman coding is not efficient in this application. But it is known as the optimum code. Is there a contradiction? Explain.
- 5.5 A set of source symbols and their occurrence probabilities is listed in [Table 5.12](#). Apply the Huffman coding algorithm to encode the alphabet.
- 5.6 Find the Huffman code for the source alphabet shown in Example 5.10.
- 5.7 Consider a source alphabet $S = \{s_i, i = 1, 2, \dots, 32\}$ with $p(s_1) = 1/4$, $p(s_i) = 3/124$, $i = 2, 3, \dots, 32$. Determine the source entropy, the average length of Huffman code if applied to the source alphabet. Then apply the modified Huffman coding algorithm. Calculate the average length of the modified Huffman code. Compare the codebook memory required by Huffman code and the modified Huffman code.
- 5.8 A source alphabet consists of the following four source symbols: s_1, s_2, s_3 , and s_4 with their occurrence probability equal to 0.25, 0.375, 0.125, and 0.25, respectively. Applying arithmetic coding as shown in Example 5.12 to the source symbol string $s_2s_1s_3s_4$, determine the lower end of the final subinterval.
- 5.9 For the above problem, show step by step how we can decode the original source string from the lower end of the final subinterval.

TABLE 5.12
Source Alphabet in Problem 5

| Source Symbol | Occurrence Probability | Codeword Assigned |
|---------------|------------------------|-------------------|
| s_1 | 0.20 | |
| s_2 | 0.18 | |
| s_3 | 0.10 | |
| s_4 | 0.10 | |
| s_5 | 0.10 | |
| s_6 | 0.06 | |
| s_7 | 0.06 | |
| s_8 | 0.04 | |
| s_9 | 0.04 | |
| s_{10} | 0.04 | |
| s_{11} | 0.04 | |
| s_{12} | 0.04 | |

- 5.10 In Problem 8, find the codeword of the symbol string $s_2s_1s_3s_4$ by using the fourth extension of Huffman code. Compare the two methods.
- 5.11 Discuss how modern arithmetic coding overcame the growing precision problem.
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6

Run-Length and Dictionary Coding: Information Theory Results (III)

As mentioned at the beginning of [Chapter 5](#), we study some codeword assignment (encoding) techniques in [Chapters 5 and 6](#). In this chapter, we focus on run-length and dictionary-based coding techniques. We first introduce Markov models as a type of dependent source model in contrast to the memoryless source model discussed in [Chapter 5](#). Based on the Markov model, run-length coding (RLC) is suitable for facsimile encoding. Its principle and application to facsimile encoding are discussed, followed by an introduction to dictionary-based coding, which is quite different from Huffman and arithmetic coding techniques covered in [Chapter 5](#). Two types of adaptive dictionary coding techniques, the LZ77 and LZ78 algorithms, are presented. Finally, a brief summary of and a performance comparison between international standard algorithms for lossless still image coding are presented.

Since the Markov source model, run-length, and dictionary-based coding are the core of this chapter, we consider this chapter as a third part of information theory results presented in the book. It is noted that, however, the emphasis is placed on their applications to image and video compression.

6.1 Markov Source Model

In the previous chapter, we discussed the discrete memoryless source model, in which source symbols are assumed to be independent of each other. In other words, the source has zero memory, i.e., the previous status does not affect the present one at all. In reality, however, many sources are dependent in nature. Namely, the source has memory in the sense that the previous status has an influence on the present status. For instance, as mentioned in [Chapter 1](#), there is an interpixel correlation in digital images. That is, pixels in a digital image are not independent of each other. As will be seen in this chapter, there is some dependence between characters in text. For instance, the letter u often follows the letter q in English. Therefore, it is necessary to introduce models that can reflect this type of dependence. A Markov source model is often in this regard.

6.1.1 Discrete Markov Source

Here, as in the previous chapter, we denote a source alphabet by $S = \{s_1, s_2, \dots, s_m\}$, the occurrence probability by p . An l th-order Markov source is characterized by the following equation of conditional probabilities.

$$p(s_j | s_{i1}, s_{i2}, \dots, s_{il}, \dots) = p(s_j | s_{i1}, s_{i2}, \dots, s_{il}), \quad (6.1)$$

where $j, i1, i2, \dots, il, \dots \in \{1, 2, \dots, m\}$, i.e., the symbols $s_j, s_{i1}, s_{i2}, \dots, s_{il}, \dots$ are chosen from the source alphabet S . This equation states that the source symbols are not independent of each other. The occurrence probability of a source symbol is determined by some of its previous symbols. Specifically, the probability of s_j given its history being $s_{i1}, s_{i2}, \dots, s_{il}, \dots$ (also called the transition probability), is determined completely by the immediately previous l symbols s_{i1}, \dots, s_{il} . That is, the knowledge of the entire sequence of previous symbols is equivalent to that of the l symbols immediately preceding the current symbol s_j .

An l th-order Markov source can be described by what is called a *state diagram*. A state is a sequence of $(s_{i1}, s_{i2}, \dots, s_{il})$ with $i1, i2, \dots, il \in \{1, 2, \dots, m\}$. That is, any group of l symbols from the m symbols in the source alphabet S forms a state. When $l = 1$, it is called a first-order Markov source. The state diagrams of the first-order Markov sources, with their source alphabets having two and three symbols, are shown in Figure 6.1a and b, respectively.

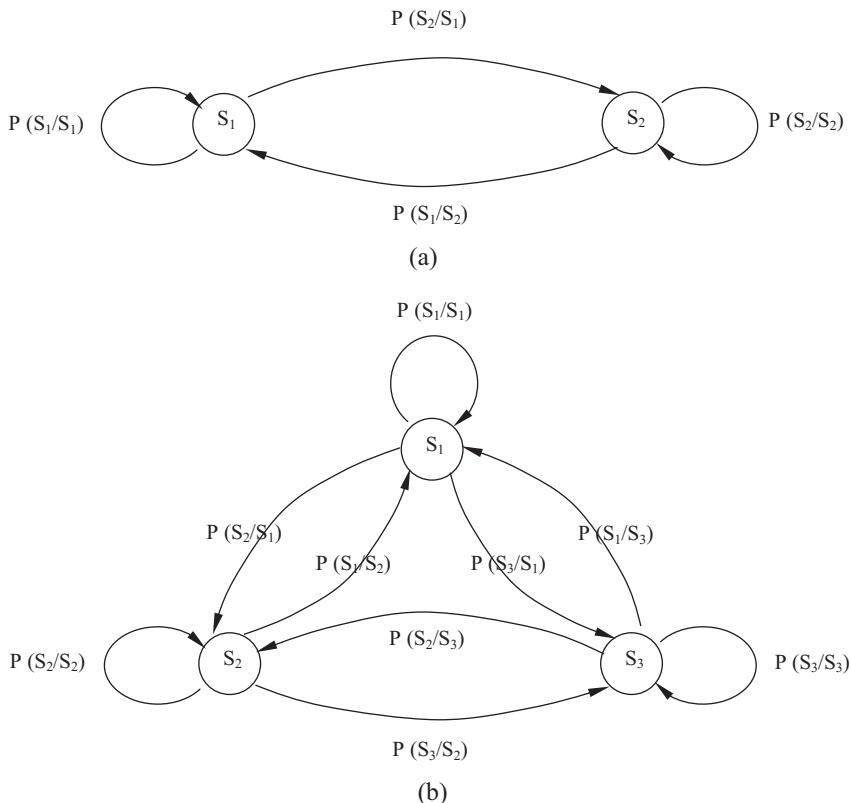


FIGURE 6.1

State diagrams of the first-order Markov sources with their source alphabets having (a) Two symbols and (b) Three symbols.

Obviously, an l th-order Markov source with m symbols in the source alphabet has a total of m^l different states. Therefore, we conclude that a state diagram consists of all the m^l states. In the diagram, all the transition probabilities together with appropriate arrows are used to indicate the state transitions.

The source entropy at a state $(s_{i1}, s_{i2}, \dots, s_{il})$ is defined as

$$H(S|s_{i1}, s_{i2}, \dots, s_{il}) = -\sum_{j=1}^m p(s_j | s_{i1}, s_{i2}, \dots, s_{il}) \log_2 p(s_j | s_{i1}, s_{i2}, \dots, s_{il}), \quad (6.2)$$

The source entropy is defined as the statistical average of the entropy at all the states. That is,

$$H(S) = \sum_{(s_{i1}, s_{i2}, \dots, s_{il}) \in S^l} p(s_{i1}, s_{i2}, \dots, s_{il}) H(S|s_{i1}, s_{i2}, \dots, s_{il}), \quad (6.3)$$

where, as defined in the previous chapter, S^l denotes the l th extension of the source alphabet S . That is, the summation is carried out with respect to all l -tuples taking over the S^l . Extensions of a Markov source are defined below.

6.1.2 Extensions of a Discrete Markov Source

An extension of a Markov source can be defined in a similar way to that of an extension of a memoryless source in the previous chapter. The definition of extensions of a Markov source and the relation between the entropy of the original Markov source and the entropy of the n th extension of the Markov source are presented below without derivation. For the derivation, readers are referred to Abramson (1963).

6.1.2.1 Definition

Consider an l th-order Markov source $S = \{s_1, s_2, \dots, s_m\}$ and a set of conditional probabilities $p(s_j | s_{i1}, s_{i2}, \dots, s_{il})$, where $j, i1, i2, \dots, il \in \{1, 2, \dots, m\}$. Similar to the memoryless source discussed in Chapter 5, if n symbols are grouped into a block, then there is a total of m^n blocks. Each block can be viewed as a new source symbol. Hence, these m^n blocks form a new information source alphabet, called the n th extension of the source S and denoted by S^n . The n th extension of the l th-order Markov source is a k th-order Markov source, where k is the smallest integer greater than or equal to the ratio between l and n . That is,

$$k = \left\lceil \frac{l}{n} \right\rceil, \quad (6.4)$$

where the notation $\lceil a \rceil$ represents the operation of taking the smallest integer greater than or equal to the quantity a .

6.1.2.2 Entropy

Denote, respectively, the entropy of the l th-order Markov source S by $H(S)$, and the entropy of the n th extension of the l th-order Markov source, S^n , by $H(S^n)$. The following relation between the two entropies can be shown.

$$H(S^n) = nH(S) \quad (6.5)$$

6.1.3 Autoregressive Model

The Markov source discussed above represents a kind of dependence between source symbols in terms of the transition probability. Concretely, in determining the transition probability of a present source symbol given all the previous symbols, only the set of finitely many immediately preceding symbols matters. The autoregressive (AR) model is another kind of dependent source model that has been used often in image coding. It is defined below.

$$s_j = \sum_{k=1}^l a_k s_{ik} + x_j, \quad (6.6)$$

where s_j represents the currently observed source symbol, while s_{ik} with $k = 1, 2, \dots, l$ denote the l preceding observed symbols, a_k 's are coefficients, and x_j is the current input to the model. If $l = 1$, the model defined in Equation 6.6 is referred to as the first-order AR model. Clearly, in this case, the current source symbol is a linear function of its preceding symbol.

6.2 Run-Length Coding

The term *run* is used to indicate the repetition of a symbol, while the term *run-length* is used to represent the number of repeated symbols, in other words, the number of consecutive symbols of the same value. Instead of encoding the consecutive symbols, it is obvious that encoding the run-length and the value that these consecutive symbols commonly share may be more efficient. According to an excellent early review on binary image compression (Arps 1979), RLC has been in use since the earliest days of information theory (Shannon 1949, Laemmle 1951).

From the discussion of the Joint Photographic (image) Experts Group (JPEG) coding made in [Chapter 4](#) (with more detail in [Chapter 7](#)), it is seen that most of the DCT coefficients within a block of 8×8 are zero after certain manipulations. The DCT coefficients are zigzag scanned. The nonzero DCT coefficients and their address in the 8×8 block need to be encoded and transmitted to the receiver side. There, the nonzero DCT values are referred to as labels. The position information about the nonzero DCT coefficients is represented by the run-length of zeros between the nonzero DCT coefficients in the zigzag scan. The labels and the run-length of zeros are then Huffman coded.

Many documents such as letters, forms, and drawings can be transmitted using facsimile machines over the general switched telephone network (GSTN). In digital facsimile techniques, these documents are quantized into binary levels: black and white. The resolution of these binary tone images is usually very high. In each scan line, there are many consecutive white and black pixels, i.e., many alternate white runs and black runs. Therefore, it is not surprising to see that RLC has proven to be efficient in binary document transmission. RLC has been adopted in the international standards for facsimile coding: the CCITT Recommendations T.4 and T.6.

RLC using only the horizontal correlation between pixels on the same scan line is referred to as 1-D RLC. It is noted that the first-order Markov source model with two symbols in the source alphabet depicted in [Figure 6.1a](#) can be used to characterize 1-D RLC. To achieve higher coding efficiency, 2-D RLC utilizes both horizontal and vertical correlation between pixels. Both the 1-D and 2-D RLC algorithms are introduced below.

6.2.1 1-D Run-Length Coding

In this technique, each scan line is encoded independently. Each scan line can be considered as a sequence of alternating, independent white runs and black runs. As an agreement between encoder and decoder, the first run in each scan line is assumed to be a white run. If the first actual pixel is black, then the run-length of the first white run is set to be zero. At the end of each scan line, there is a special codeword called end-of-line (EOL). The decoder knows the end of a scan line when it encounters an EOL codeword.

Denote run-length by r , which is integer-valued. All of the possible run-lengths construct a source alphabet R , which is a random variable. That is,

$$R = \{r : r \in 0, 1, 2, \dots\}. \quad (6.7)$$

Measurements on typical binary documents have shown that the maximum compression ratio, ζ_{\max} , which is defined below, is about 25% higher when the white and black runs are encoded separately (Hunter 1980). The average white run-length, \bar{r}_W , can be expressed as

$$\bar{r}_W = \sum_{r=0}^m r \cdot P_W(r), \quad (6.8)$$

where m is the maximum value of the run-length, and $P_W(r)$ denotes the occurrence probability of a white run with length r . The entropy of the white runs, H_W , is

$$H_W = - \sum_{r=0}^m P_W(r) \log_2 P_W(r). \quad (6.9)$$

For the black runs, the average run-length \bar{r}_B and the entropy H_B can be defined similarly. The maximum theoretical compression factor ζ_{\max} is

$$\zeta_{\max} = \frac{\bar{r}_W + \bar{r}_B}{H_W + H_B}. \quad (6.10)$$

Huffman coding is then applied to two source alphabets. According to CCITT Recommendation T.4, A4 size (210×297 mm) documents should be accepted by facsimile machines. In each scan line, there are 1728 pixels. This means that the maximum run-length for both white and black runs is 1728, i.e., $m = 1728$. Two source alphabets of such a large size imply the requirement of two large codebooks, hence the requirement of large storage space. Therefore, some modification was made, resulting in the “modified” Huffman (MH) code.

In the MH code, if the run-length is larger than 63, then the run-length is represented as

$$r = M \times 64 + T \quad \text{as} \quad r > 63, \quad (6.11)$$

where M takes integer values from 1, 2, ..., to 27, and $M \times 64$ is referred to as the makeup run-length; T takes integer values from 0, 1 to 63, and is called the terminating run-length. That is, if $r < 63$, the run-length is represented by a terminating codeword only. Otherwise, if $r > 63$, the run-length is represented by a makeup codeword and a terminating codeword. A portion of the MH code table (Hunter 1980) is shown in [Table 6.1](#). In this way, the requirement of large storage space is alleviated. The idea is similar to that behind MH coding, discussed in [Chapter 5](#).

TABLE 6.1

Modified Huffman Code Table (Hunter 1980)

| Run-Length | White Runs | Black Runs |
|------------------------------|--------------|---------------|
| Terminating Codewords | | |
| 0 | 00110101 | 0000110111 |
| 1 | 000111 | 010 |
| 2 | 0111 | 11 |
| 3 | 1000 | 10 |
| 4 | 1011 | 011 |
| 5 | 1100 | 0011 |
| 6 | 1110 | 0010 |
| 7 | 1111 | 00011 |
| 8 | 10011 | 000101 |
| : | : | : |
| 60 | 01001011 | 000000101100 |
| 61 | 00110010 | 000001011010 |
| 62 | 00110011 | 000001100110 |
| 63 | 00110100 | 000001100111 |
| Make-up Codewords | | |
| 64 | 11011 | 0000001111 |
| 128 | 10010 | 000011001000 |
| 192 | 010111 | 000011001001 |
| 256 | 0110111 | 000001011011 |
| : | : | : |
| 1536 | 010011001 | 0000001011010 |
| 1600 | 010011010 | 0000001011011 |
| 1664 | 011000 | 0000001100100 |
| 1728 | 010011011 | 0000001100101 |
| EOL | 000000000001 | 000000000001 |

Source: Hunter, R. and Robinson, A. H., *Proceedings of the IEEE*, 68, 854–867, 1980.

6.2.2 2-D Run-Length Coding

The 1-D RLC discussed above only utilizes correlation between pixels within a scan line. In order to utilize correlation between pixels in neighboring scan lines to achieve higher coding efficiency, 2-D RLC was developed. In Recommendation T.4, the modified relative element address designate (READ) code, also known as the modified READ (MR) code is adopted.

The MR code operates in a line-by-line manner. In Figure 6.2, two lines are shown. The top line is called the reference line, which has been coded, while the bottom line is referred to as the coding line, which is being coded. There are a group of five changing pixels, a_0, a_1, a_2, b_1, b_2 , in the two lines. Their relative positions decide which of the three coding

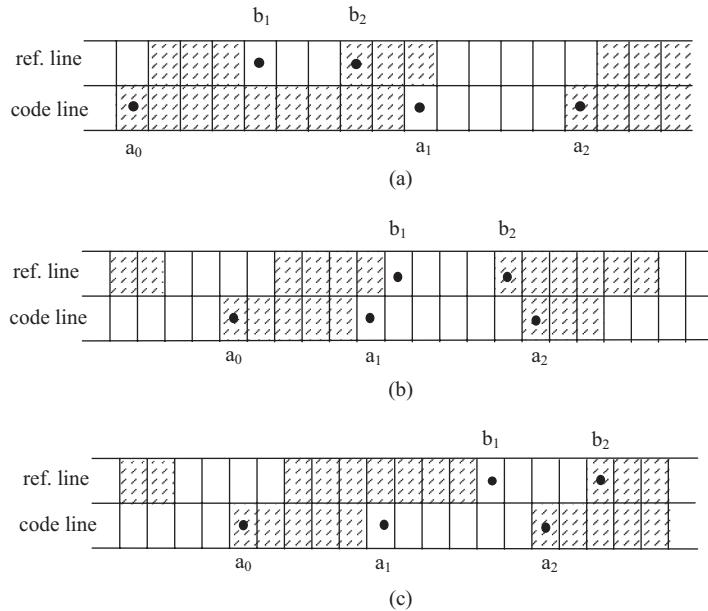


FIGURE 6.2
2-D RLC. (a) Pass mode, (b) Vertical mode, and (c) Horizontal mode.

modes is used. The starting changing pixel a_0 (hence, five changing points) moves from left to right and from top to bottom as 2-D RLC proceeds. The five changing pixels and the three coding modes are defined below.

6.2.2.1 Five Changing Pixels

By a changing pixel, we mean the first pixel encountered in white or black runs when we scan an image line-by-line, from left to right, and from top to bottom. The five changing pixels are defined below.

- a_0 : The reference changing pixel in the coding line. Its position is defined in the previous coding mode, whose meaning will be explained shortly. At the beginning of a coding line, a_0 is an imaginary white changing pixel located before the first actual pixel in the coding line.
- a_1 : The next changing pixel in the coding line. Because of the above-mentioned left-to-right and top-to-bottom scanning order, it is at the right-hand side of a_0 . Since it is a changing pixel, it has an opposite “color” to that of a_0 .
- a_2 : The next changing pixel after a_1 in the coding line. It is to the right of a_1 and has the same color as that of a_0 .
- b_1 : The changing pixel in the reference line that is closest to a_0 from the right and has the same color as a_1 .
- b_2 : The next changing pixel in the reference line after b_1 .

6.2.2.2 Three Coding Modes

Pass Coding Mode: If the changing pixel b_2 is located to the left of the changing pixel a_1 , it means that the run in the reference line starting from b_1 is not adjacent to the run in the coding line starting from a_1 . Note that these two runs have the same color. This is called pass coding mode. A special codeword, “0001,” is sent out from transmitter. The receiver then knows that the run starting from a_0 in the coding line does not end at the pixel below b_2 . This pixel (below b_2 in the coding line) is identified as the reference changing pixel a_0 of the new set of five changing pixels for the next coding mode.

Vertical Coding Mode: If the relative distance along the horizontal direction between the changing pixels a_1 and b_1 is not larger than three pixels, the coding is conducted in vertical coding mode. That is, the position of a_1 is coded with reference to the position of b_1 . Seven different codewords are assigned to seven different cases: the distance between a_1 and b_1 equals $0, \pm 1, \pm 2, \pm 3$, where + means a_1 is to the right of b_1 , while – means a_1 is to the left of b_1 . The a_1 then becomes the reference changing pixel a_0 of the new set of five changing pixels for the next coding mode.

Horizontal Coding Mode: If the relative distance between the changing pixels a_1 and b_1 is larger than three pixels, the coding is conducted in horizontal coding mode. Here, 1-D RLC is applied. Specifically, the transmitter sends out a codeword consisting the following three parts: a flag “001”; a 1-D run-length codeword for the run from a_0 to a_1 ; a 1-D run-length codeword for the run from a_1 to a_2 . The a_2 then becomes the reference changing pixel a_0 of the new set of five changing pixels for the next coding mode.

Table 6.2 contains three coding modes and the corresponding output codewords. There, (a_0a_1) and (a_1a_2) represent 1-D run-length codewords of run-length a_0a_1 and a_1a_2 , respectively.

6.2.3 Effect of Transmission Error and Uncompressed Mode

In this subsection, effect of transmission error in the 1-D and 2-D RLC cases and uncompressed mode are discussed.

TABLE 6.2

2-D RLC Table, $|x_iy_j|$: Distance Between x_i and y_j , $x_iy_j > 0$: x_i Is Right to y_j , $x_iy_j < 0$: x_i Is Left to y_j . (x_iy_j) : Codeword of the Run Denoted by x_iy_j Taken from the Modified Huffman Code

| Mode | Conditions | Output Codeword | Position of New a_0 |
|------------------------|----------------|-----------------------------|----------------------------|
| Pass coding mode | $b_2a_1 < 0$ | 0001 | under b_2 in coding line |
| Vertical coding mode | $a_1b_1 = 0$ | 1 | a_1 |
| | $a_1b_1 = 1$ | 011 | |
| | $a_1b_1 = 2$ | 000011 | |
| | $a_1b_1 = 3$ | 0000011 | |
| | $a_1b_1 = -1$ | 010 | |
| | $a_1b_1 = -2$ | 000010 | |
| | $a_1b_1 = -3$ | 0000010 | |
| Horizontal coding mode | $ a_1b_1 > 3$ | $001 + (a_0a_1) + (a_1a_2)$ | a_2 |

Source: Hunter, R. and Robinson, A. H., *Proceedings of the IEEE*, 68, 854–867, 1980.

6.2.3.1 Error Effect in the 1-D RLC Case

As introduced above, the special codeword EOL is used to indicate the end of each scan line. With the EOL, 1-D RLC encodes each scan line independently. If a transmission error occurs in a scan line, there are two possibilities that the effect caused by the error is limited within the scan line. One possibility is that *resynchronization* is established after a few runs. One example is shown in [Figure 6.3](#). There, the transmission error takes place in the second run from the left. Resynchronization is established in the fifth run in this example. Another possibility lies in the EOL, which forces resynchronization.

In summary, it is seen that the 1-D RLC will not propagate transmission error between scan lines. In other words, a transmission error will be restricted within a scan line. Although error detection and retransmission of data via an automatic repeat request (ARQ) system are supposed to be able to effectively handle the error susceptibility issue, the ARQ technique was not included into Recommendation T.4 due to the computational complexity and extra transmission time required.

Once the number of decoded pixels between two consecutive EOL codewords is not equal to 1728 (for an A4 size document), an error has been identified. Some *error concealment* techniques can be used to reconstruct the scan line (Hunter 1980). For instance, we can repeat the previous line, or replace the damaged line by a white line, or use a correlation technique to recover the line as much as possible.

6.2.3.2 Error Effect in the 2-D RLC Case

From the above discussion, we realize that 2-D RLC is more efficient than 1-D RLC on the one hand. The 2-D RLC is more susceptible to transmission errors than the 1-D RLC on the other hand. To prevent error propagation, there is a parameter used in 2-D RLC, known as the *K-factor*, which specifies the number of scan lines that are 2-D RLC coded.

Recommendation T.4 defined that no more than K-1 consecutive scan lines be 2-D RLC coded after a 1-D RLC coded line. For binary documents scanned at normal resolution, K = 2. For documents scanned at high resolution, K = 4.

According to Arps (1979), there are two different types of algorithms in binary image coding, *raster* algorithms and *area* algorithms. Raster algorithms only operate on data within one or two raster scan lines. They are, hence, mainly 1-D in nature. Area algorithms are truly 2-D in nature. They require that all, or a substantial portion, of the image is in random access memory. From our discussion above, we see that both 1-D and 2-D RLC defined in T.4 belong to the category of raster algorithms. Area algorithms require large memory space and are susceptible to transmission noise.

| Original coded line | 1000 | 011 | 0111 | 0011 | 1110 | 10 | ... |
|-------------------------|------|------|------|------|------|----|-----|
| | 3W | 4B | 2W | 5B | 6W | 3B | |
| an error | | | | | | | |
| Error contaminated line | 1000 | 0010 | 1110 | 011 | 1110 | 10 | ... |
| | 3W | 6B | 6W | 4B | 6W | 3B | |

FIGURE 6.3

Establishment of resynchronization after a few runs.

6.2.3.3 Uncompressed Mode

For some detailed binary document images, both 1-D and 2-D RLC may result in data expansion instead of data compression. Under these circumstances the number of coding bits is larger than the number of bilevel pixels. An uncompressed mode is created as an alternative way to avoid data expansion. Special codewords are assigned for the uncompressed mode.

For the performances of 1-D and 2-D RLC applied to eight CCITT test document images, and issues such as “fill bits” and “minimum scan line time (MSLT),” to only name a few, readers are referred to an excellent tutorial paper (Hunter 1980).

6.3 Digital Facsimile Coding Standards

Facsimile transmission, an important means of communication in modern society, is often used as an example to demonstrate the mutual interaction between widely used applications and standardization activities. Active facsimile applications and the market brought on the necessity for international standardization in order to facilitate interoperability between facsimile machines worldwide. Successful international standardization, in turn, has stimulated wider use of facsimile transmission and, hence, a more demanding market. Facsimile has also been considered as a major application for binary image compression.

So far, facsimile machines are classified in four different groups. Facsimile apparatuses in groups 1 and 2 use analog techniques. They can transmit an A4-size (210×297 mm) document scanned at 3.85 lines/mm in 6 and 3 minutes, respectively, over the GSTN. International standards for these two groups of facsimile apparatus are CCITT (now ITU) Recommendations T.2 and T.3, respectively. Group 3 facsimile machines use digital techniques and, hence, achieve high coding efficiency. They can transmit the A4-size binary document scanned at a resolution of 3.85 lines/mm and sampled at 1728 pixels/line in about 1 minute at a rate of 4800 bits/sec over the GSTN. The corresponding international standard is CCITT Recommendations T.4. Group 4 facsimile apparatuses have the same transmission speed requirement as that for group 3 machines, but the coding technique is different. Specifically, the coding technique used for group 4 machines is based on 2-D RLC, discussed above, but modified to achieve higher coding efficiency. Hence, it is referred to as the modified modified READ coding (MMR). The corresponding standard is CCITT Recommendations T.6. [Table 6.3](#) summarizes the above descriptions.

TABLE 6.3

Facsimile Coding Standards

| Group of Facsimile Apparatuses | Speed Requirement for A4-size Document | Analog or Digital Scheme | CCITT Recommendation | Compression Technique | | |
|--------------------------------|--|--------------------------|----------------------|----------------------------------|------------------|-------------------|
| | | | | Model | Basic Coder | Algorithm Acronym |
| G ₁ | 6 min | Analog | T.2 | — | — | — |
| G ₂ | 3 min | Analog | T.3 | — | — | — |
| G ₃ | 1 min | Digital | T.4 | 1-D RLC 2-D RLC (optional) | Modified Huffman | MH MR |
| G ₄ | 1 min | Digital | T.6 | 2-D RLC | Modified Huffman | MMR |

6.4 Dictionary Coding

Dictionary coding, the focus of this section, is different from Huffman coding and arithmetic coding, discussed in the previous chapter. Both Huffman and arithmetic coding techniques are based on a statistical model, and the occurrence probabilities play a particular important role. Recall that in the Huffman coding the shorter codewords are assigned to more frequently occurring source symbols. In dictionary-based data compression techniques a symbol or a string of symbols generated from a source alphabet is represented by an index to a dictionary constructed from the source alphabet. A dictionary is a list of symbols and strings of symbols. There are many examples of this in our daily lives. For instance, the string “September” is sometimes represented by an index “9,” while a social security number represents a person in the U.S.

Dictionary coding is widely used in text coding. Consider English text coding. The source alphabet includes 26 English letters in both lower and upper cases, numbers, various punctuation marks and the space bar. Huffman or arithmetic coding treats each symbol based on its occurrence probability. That is, the source is modeled as a memoryless source. It is well known, however, that this is not true in many applications. In text coding, *structure* or *context* plays a significant role. As mentioned earlier, it is very likely that the letter *u* appears after the letter *q*. Likewise, it is likely that the word “concerned” will appear after “As far as the weather is.” The strategy of the dictionary coding is to build a dictionary that contains frequently occurring symbols and string of symbols. When a symbol or a string is encountered and it is contained in the dictionary, it is encoded with an index to the dictionary. Otherwise, if not in the dictionary, the symbol or the string of symbols is encoded in a less efficient manner.

6.4.1 Formulation of Dictionary Coding

To facilitate further discussion, we define dictionary coding in a precise manner (Bell 1990). We denote a source alphabet by S . A dictionary consisting of two elements is defined as $D = (P, C)$, where P is a finite set of phrases generated from the S , and C is a coding function mapping P onto a set of codewords.

The set P is said to be complete if any input string can be represented by a series of phrases chosen from the P . The coding function C is said to obey the prefix property if there is no codeword that is a prefix of any other codeword. For practical usage, i.e., for reversible compression of any input text, the phrase set P must be complete and the coding function C must satisfy the prefix property.

6.4.2 Categorization of Dictionary-Based Coding Techniques

The heart of dictionary coding is the formulation of the dictionary. A successfully built dictionary results in data compression; the opposite case may lead to data expansion. According to the ways in which dictionaries are constructed, dictionary coding techniques can be classified as static or adaptive.

6.4.2.1 Static Dictionary Coding

In some particular applications, the knowledge about the source alphabet and the related strings of symbols, also known as phrases, is sufficient for a fixed dictionary to be produced

before the coding process. The dictionary is used at both the transmitting and receiving ends. This is referred to as static dictionary coding. The merit of the static approach is its simplicity. Its drawbacks lie in its relatively lower coding efficiency and less flexibility compared with adaptive dictionary techniques. By less flexibility, we mean that a dictionary built for a specific application is not normally suitable for utilization in other applications.

An example of static algorithms occurs is *digram* coding. In this simple and fast coding technique, the dictionary contains all source symbols and some frequently used pairs of symbols. In encoding, two symbols are checked at once to see if they are in the dictionary. If so, they are replaced by the index of the two symbols in the dictionary, and the next pair of symbols is encoded in the next step. If not, then the index of the first symbol is used to encode the first symbol. The second symbol is combined with the third symbol to form a new pair, which is encoded in the next step.

The diagram can be straightforwardly extended to *n-gram*. In the extension, the size of the dictionary increases and so does its coding efficiency.

6.4.2.2 Adaptive Dictionary Coding

As opposed to the static approach, with the adaptive approach a completely defined dictionary does not exist prior to the encoding process and the dictionary is not fixed. At the beginning of coding, only an initial dictionary exists. It adapts itself to the input during the coding process. All the adaptive dictionary coding algorithms can be traced back to two different original works by Ziv and Lempel (1977, 1978). The algorithms based on Ziv and Lempel (1977) are referred to as the LZ77 algorithms, while those based on Ziv and Lempel (1978) are referred to as the LZ78 algorithms. Prior to introducing the two landmark works, we will discuss the parsing strategy.

6.4.3 Parsing Strategy

Once we have a dictionary, we need to examine the input text and find a string of symbols that matches an item in the dictionary. Then the index of the item to the dictionary is encoded. This process of segmenting the input text into disjoint strings (whose union equals the input text) for coding is referred to as *parsing*. Obviously, the way to segment the input text into strings is not unique.

In terms of the highest coding efficiency, optimal parsing is essentially a shortest-path problem (Bell 1990). In practice, however, a method called *greedy* parsing is used most often. In fact, it is used in all the LZ77 and LZ78 algorithms (Nelson 1995). With greedy parsing, the encoder searches for the longest string of symbols in the input that matches an item in the dictionary at each coding step. Greedy parsing may not be optimal, but it is simple in implementation.

Example 6.1

Consider a dictionary, D , whose phrase set $P = \{a, b, ab, ba, bb, aab, bbb\}$. The codewords assigned to these strings are $C(a) = 10$, $C(b) = 011$, $C(ab) = 010$, $C(ba) = 0101$, $C(bb) = 01$, $C(aab) = 11$, and $C(bbb) = 0110$. Now the input text is *abbaab*.

Using greedy parsing, we then encode the text as $C(ab).C(ba).C(ab)$, which is a 10-bit string: 010.0101.010. In the above representations, the periods are used to indicate the division of segments in the parsing. This, however, is not an optimum solution. Obviously, the following parsing will be more efficient, i.e., $C(a).C(bb).C(aab)$, which is a six-bit string: 10.01.11.

6.4.4 Sliding Window (LZ77) Algorithms

As mentioned earlier, LZ77 algorithms are a group of adaptive dictionary coding algorithms rooted in the pioneering work in Ziv and Lempel (1977). Since they are adaptive, there is no complete and fixed dictionary before coding. Instead, the dictionary changes as the input text changes.

6.4.4.1 Introduction

In the LZ77 algorithms (Bell 1990, Nelson 1995), the dictionary used is actually a portion of the input text, which has been recently encoded. The text that needs to be encoded is compared with the strings of symbols in the dictionary. The longest matched string in the dictionary is characterized by a *pointer* (sometimes called a *token*), which is represented by a triple of data items. Note that this triple functions as an index to the dictionary, as mentioned above. In this way, a variable-length string of symbols is mapped to a fixed-length pointer.

There is a sliding window in the LZ77 algorithms. The window consists of two parts: a search buffer and a look-ahead buffer. The search buffer contains the portion of the text stream that has recently been encoded, which, as mentioned, is the dictionary; while the look-ahead buffer contains the text to be encoded next. The window slides through the input text stream from beginning to end during the entire encoding process. This explains the term *sliding window*. The size of the search buffer is much larger than that of the look-ahead buffer. This is expected because what is contained in the search buffer is in fact the adaptive dictionary. The sliding window is usually on the order of a few thousand symbols, whereas the look-ahead buffer is on the order of several tens to one hundred symbols.

6.4.4.2 Encoding and Decoding

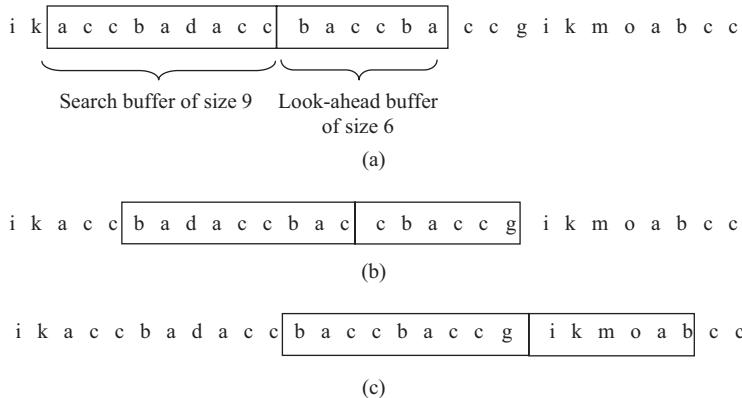
Below we present more detail about the sliding window dictionary coding technique, i.e., the LZ77 approach, via a simple illustrative example.

Example 6.2

[Figure 6.4](#) shows a sliding window. The input text stream is
 ikaccbadaccbaccbaccgikmoabcc

In Part (a) of the figure, a search buffer of nine symbols and a look-ahead buffer of six symbols are shown. All the symbols in the search buffer, *accbadacc*, have just been encoded. All the symbols in the look-ahead buffer, *baccba*, are to be encoded. (It is understood that the symbols before the search buffer have been encoded and the symbols after the look-ahead buffer are to be encoded.) The strings of symbols, *ik* and *ccgikmoabcc*, are not covered by the sliding window at the moment.

At the moment, or in other words, in the first step of encoding, the symbol (symbols) to be encoded begins (begin) with the symbol *b*. The pointer starts searching for the symbol *b* from the last symbol in the search buffer, *c*, which is immediately to the left of the first symbol *b* in the look-ahead buffer. It finds a match at the sixth position from *b*. It further determines that the longest string of the match is *ba*. That is, the maximum matching length is two. The pointer is then represented by a triple, $\langle i, j, k \rangle$. The first item, “*i*,” represents the distance between the first symbol in the look-ahead buffer and the position of the pointer (the position of the first symbol of the matched string). This distance is called *offset*. In this step, the offset is six. The second item in the triple, “*j*,” indicates the length of the matched string. Here, the length of the matched string *ba* is two. The third item, “*k*,” is the codeword assigned to the symbol immediately following

**FIGURE 6.4**

An encoding example using LZ77. (a) Triple: <6, 2, C(c)>, (b) Triple: <4, 5, C(g)>, and (c) Triple: <0, 0, C(i)>.

the matched string in the look-ahead buffer. In this step, the third item is $C(c)$, where C is used to represent a function to map symbol(s) to a codeword, as defined in [Section 6.4.1](#). That is, the resulting triple after the first step is: <6, 2, $C(c)$ >.

The reason to include the third item “*k*” into the triple is as follows. In the case where there is no match in the search buffer, both “*i*” and “*j*” will be zero. The third item at this moment is the codeword of the first symbol in the look-ahead buffer itself. This means that even in the case where we cannot find a match string, the sliding window still works. In the third step of the encoding process described below, we will see that the resulting triple is: <0, 0, $C(i)$ >. The decoder hence understands that there is no matching, and the single symbol *i* is decoded.

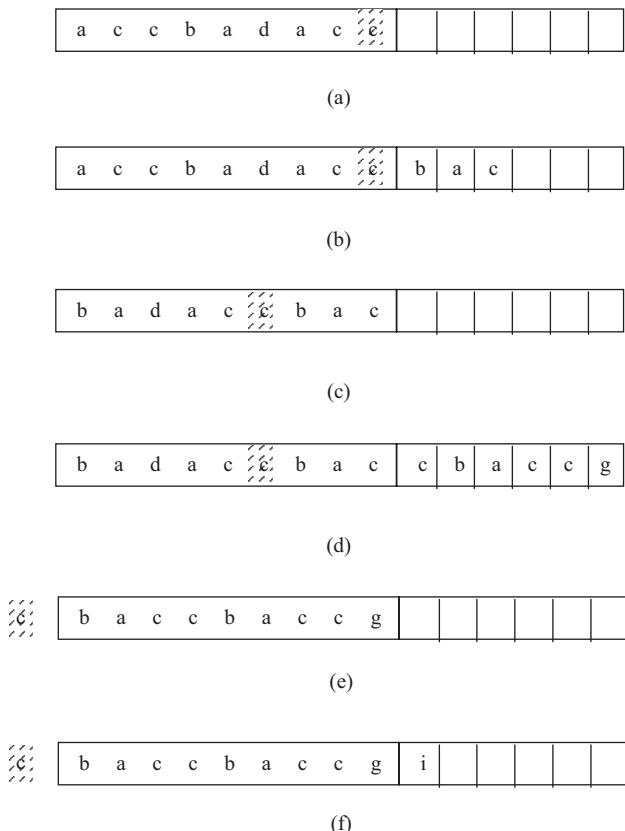
The second step of the encoding is illustrated in Part (b) of [Figure 6.4](#). The sliding window has been shifted to the right by three positions. The first symbol to be encoded now is *c*, which is the left-most symbol in the look-ahead buffer. The search pointer moves towards the left from the symbol *c*. It first finds a match in the first position with a length of one. It then finds another match in the fourth position from the first symbol in the look-ahead buffer. Interestingly, the maximum matching can exceed the boundary between the search buffer and the look-ahead buffer and can enter the look-ahead buffer. Why this is possible will be seen shortly, when we discuss the decoding process. In this manner, it is found that the maximum length of matching is five. The last match is found at the fifth position. The length of the matched string is, however, only one. Since greedy parsing is used, the match with a length five is chosen. That is, the offset is four and the maximum match length is five. Consequently, the triple resulting from the second step is <4, 5, $C(g)$ >.

The sliding window is then shifted to the right by six positions. The third step of the encoding is depicted in Part (c). Obviously, there is no matching of *i* in the search buffer. The resulting triple is hence <0, 0, $C(i)$ >.

The encoding process can continue in this way. The possible cases we may encounter in the encoding, however, are described in the three steps. Hence, we end our discussion of the encoding process and discuss the decoding process. Compared with the encoding, the decoding is simpler because there is no need for matching, which involves many comparisons between the symbols in the look-ahead buffer and the symbols in the search buffer. The decoding process is illustrated in [Figure 6.5](#).

In the three steps, the resulting triples are: <6, 2, $C(c)$ >, <4, 5, $C(g)$ >, and <0, 0, $C(i)$ >. Now let us see how the decoder works. That is, how the decoder recovers the string *baccbaccgi* from these three triples.

In Part (a) of [Figure 6.5](#), the search buffer is the same as that in Part (a) of [Figure 6.4](#). That is, the string *accbadacc* stored in the search window is what was just decoded.

**FIGURE 6.5**

A decoding example using LZ77. (a) Search buffer at the beginning, (b) After decoding $<6, 2, C(c)>$, (c) Shifting the sliding window, (d) After decoding $<4, 5, C(g)>$, (e) Shifting the sliding window, and (f) After decoding $<0, 0, C(i)>$.

Once the first triple $<6, 2, C(c)>$ is received, the decoder will move the decoding pointer from the first position in the look-ahead buffer to the left by six positions. That is, the pointer will point to the symbol b . The decoder then copies the two symbols starting from b , i.e., ba , into the look-ahead buffer. The symbol c will be copied right to ba . This is shown in part (b) of Figure 6.5. The window is then shifted to the right by three positions, as shown in Part (c) of Figure 6.5.

After the second triple $<4, 5, C(g)>$ is received, the decoder moves the decoding pointer from the first position of the look-ahead buffer to the left by four positions. The pointer points the symbol c . The decoder then copies five successive symbols starting from the symbol c pointed by the pointer. We see that at the beginning of this copying process there are only four symbols available for copying. Once the first symbol is copied, however, all five symbols are available. After copying, the symbol g is added to the end of the five copied symbols in the look-ahead buffer. The results are shown in Part (c) of Figure 6.5. Part (d) then shows the window shifting to the right by six positions.

After receiving the triple $<0, 0, C(i)>$, the decoder knows that there is no matching and a single symbol i is encoded. Hence, the decoder adds the symbol i following the symbol g . This is shown in Part (f) of Figure 6.5.

In Figure 6.5, for each part, the last previously encoded symbol c prior to the receiving of the three triples is shaded. From Part (f), we see that the string added after the symbol c due to the three triples is $baccbaccgi$. This agrees with the sequence mentioned at

the beginning of our discussion about the decoding process. We thus conclude that the decoding process has correctly decoded the encoded sequence from the last-encoded symbol and the received triples.

6.4.4.3 Summary of the LZ77 Approach

The sliding window consists of two parts: the search buffer and the look-ahead buffer. The most recently encoded portion of the input text stream is contained in the search buffer, while the portion of the text that needs to be encoded immediately is in the look-ahead buffer. The first symbol in the look-ahead buffer, located to the right of the boundary between the two buffers, is the symbol or the beginning of a string of symbols to be encoded at the moment. Let us call it the symbol s . The size of the search buffer is usually much larger than that of the look-ahead buffer.

In encoding, the search pointer moves to the left, away from the symbol s , to find a match of the symbol s in the search buffer. Once a match is found, the encoding process will further determine the length of the matched string. When there are multiple matches, the match that produces the longest matched string is chosen. The match is denoted by a triple $\langle i, j, k \rangle$. The first item in the triple, “ i ,” is the offset, which is the distance between the pointer pointing to the symbol giving the maximum match and the symbol s . The second item, “ j ,” is the length of the matched string. The third item, “ k ,” is the codeword of the symbol following the matched string in the look-ahead buffer. The sliding window is then shifted to the right by $j+1$ positions before the next coding step takes place.

When there is no matching in the search buffer, the triple is represented by $\langle 0, 0, C(s) \rangle$, where $C(s)$ is the codeword assigned to the symbol s . The sliding window is then shifted to the right by one position.

The sliding window is shifted along the input text stream during the encoding process. The symbol s moves from the beginning symbol to the ending symbol of the input text stream.

At the very beginning, the content of the search buffer can be arbitrarily selected. For instance, the symbols in the search buffer may all be the space symbol.

Let us denote the size of the search buffer by SB , the size of the look-ahead buffer by L , and the size of the source alphabet by A . Assume that the natural binary code is used. Then we see that the LZ77 approach encodes variable-length strings of symbols with fixed-length codewords. Specifically, the offset “ i ” is of coding length $\lceil \log_2(SB) \rceil$, the length of matched string “ j ” is of coding length $\lceil \log_2(SB+L) \rceil$, and the codeword “ k ” is of coding length $\lceil \log_2(A) \rceil$, where the sign $\lceil a \rceil$ denotes the smallest integer larger than a .

The length of the matched string is equal to $\lceil \log_2(SB+L) \rceil$ because the search for the maximum matching can enter into the look-ahead buffer as shown in Example 6.2.

The decoding process is simpler than the encoding process since there is no comparison involved in the decoding.

The most recently encoded symbols in the search buffer serve as the dictionary used in the LZ77 approach. The merit of doing so is that the dictionary is adapted to the input text well. The limitation of the approach is that if the distance between the repeated patterns in the input text stream is larger than the size of the search buffer, then the approach cannot utilize the structure to compress the text. A vivid example can be found in Sayood (1996).

A window with a moderate size, say, $SB + L \leq 8192$, can compress a variety of texts well. Several reasons have been analyzed in Bell (1990).

Many variations have been made to improve coding efficiency of the LZ77 approach. The LZ77 produces a triple in each encoding step, i.e., the offset (position of the matched string),

the length of the matched string, and the codeword of the symbol following the matched string. The transmission of the third item in each coding step is not efficient. This is true especially at the beginning of coding. A variant of the LZ77, referred to as the LZSS algorithm (Bell 1986), improves this inefficiency.

6.4.5 LZ78 Algorithms

6.4.5.1 Introduction

As mentioned above, the LZ77 algorithms use a sliding window of fixed size, and both the search buffer and the look-ahead buffer have a fixed size. This means that if the distance between two repeated patterns is larger than the size of the search buffer, the LZ77 algorithms cannot work efficiently. The fixed size of the both buffers implies that the matched string cannot be longer than the sum of the sizes of the two buffers, meaning another limitation on coding efficiency. Increasing the sizes of the search buffer and the look-ahead buffer seemingly will resolve the problems. A close look, however, reveals that it also leads to increases in the number of bits required to encode the offset and matched string length as well as an increase in processing complexity.

The LZ78 algorithms (Ziv and Lempel 1978, Bell 1990, Nelson 1995) eliminate the use of the sliding window. Instead, these algorithms use the encoded text as a dictionary that, potentially, does not have a fixed size. Each time a pointer (token) is issued, the encoded string is included in the dictionary. Theoretically the LZ78 algorithms reach optimal performance as the encoded text stream approaches infinity. In practice, however, as mentioned above with respect to the LZ77, a very large dictionary will affect coding efficiency negatively. Therefore, once a preset limit to the dictionary size has been reached, either the dictionary is fixed for the future (if the coding efficiency is good), or it is reset to zero, i.e., it must be restarted.

Instead of the triples used in the LZ77, only pairs are used in the LZ78. Specifically, only the position of the pointer to the matched string and the symbol following the matched string need to be encoded. The length of the matched string does not need to be encoded since both the encoder and the decoder have the exactly the same dictionary, i.e., the decoder knows the length of the matched string.

6.4.5.2 Encoding and Decoding

Like the discussion of the LZ77 algorithms, we will go through an example to describe the LZ78 algorithms.

Example 6.3

Consider the text stream: *baccbacacbcabccbbacc*. Table 6.4 shows the coding process. We see that for the first three symbols there is no match between the individual input symbols and the entries in the dictionary. Therefore, the doubles are, respectively, $\langle 0, C(b) \rangle$, $\langle 0, C(a) \rangle$ and $\langle 0, C(c) \rangle$, where 0 means no match, and $C(b)$, $C(a)$, and $C(c)$ represent the codewords of b , a , and c , respectively. After symbols b , a , c , comes c , which finds a match in the dictionary (the third entry). Therefore, the next symbol b is combined to be considered. Since the string cb did not appear before, it is encoded as a double and it is appended as a new entry into the dictionary. The first item in the double is the index of the matched entry c , 3, the second item is the index/codeword of the symbol following the match b , 1. That is, the double is $\langle 3, 1 \rangle$. The following input symbol is a , which appeared in the dictionary. Hence, the next symbol c is taken into consideration.

TABLE 6.4

An Encoding Example Using the LZ78 Algorithm

| Index | Doubles | Encoded Symbols |
|-------|-------------|-----------------|
| 1 | < 0, C(b) > | b |
| 2 | < 0, C(a) > | a |
| 3 | < 0, C(c) > | c |
| 4 | < 3, 1 > | cb |
| 5 | < 2, 3 > | ac |
| 6 | < 3, 2 > | ca |
| 7 | < 4, 3 > | cbc |
| 8 | < 2, 1 > | ab |
| 9 | < 3, 3 > | cc |
| 10 | < 1, 1 > | bb |
| 11 | < 5, 3 > | acc |

Since the string *ac* is not an entry of the dictionary, it is encoded with a double. The first item in the double is the index of symbol *a*, 2, the second item is the index of symbol *c*, 3, i.e., <2, 3>. The encoding proceeds in this way. Take a look at [Table 6.4](#). In general, as the encoding proceeds, the entries in the dictionary become longer and longer. First, entries with single symbols come out, but later, more and more entries with two symbols show up. After that more and more entries with three symbols appear. This means that coding efficiency is increasing.

Now consider the decoding process. Since the decoder knows the rule applied in the encoding, it can reconstruct the dictionary and decode the input text stream from the received doubles. When the first double <0, C(b)> is received, the decoder knows that there is no match. Hence, the first entry in the dictionary is *b*. So is the first decoded symbol. From the second double <0, C(a)>, symbol *a* is known as the second entry in the dictionary as well as the second decoded symbol. Similarly, the next entry in the dictionary and the next decoded symbol are known as *c*. When the following double <3, 1> is received. The decoder knows from two items, 3 and 1, that the next two symbols are the third and the first entries in the dictionary. This indicates that the symbols *c* and *b* are decoded, and the string *cb* becomes the fourth entry in the dictionary.

We omit the next two doubles and take a look at the double <4, 3>, which is associated with index 7 in [Table 6.4](#). Since the first item in the double is 4, it means that the maximum matched string is *cb*, which is associated with index 4 in [Table 6.4](#). The second item in the double, 3, implies that the symbol following the match is the third entry *c*. Therefore, the decoder decodes a string *cbc*. Also, the string *cbc* becomes the seventh entry in the reconstructed dictionary. In this way, the decoder can reconstruct the exact same dictionary as that established by the encoder and decode the input text stream from the received doubles.

6.4.5.3 LZW Algorithm

Both the LZ77 and LZ78 approaches, when published in 1977 and 1978, respectively, were theory-oriented. The effective and practical improvement over the LZ78 in Welch (1984) brought much attention to the LZ dictionary coding techniques. The resulting algorithm is referred to the LZW algorithm (Bell 1990, Nelson 1995). It removed the second item in the double (the index of the symbol following the longest matched string) and, hence, it enhanced coding efficiency. In other words, the LZW only sends the indexes of the dictionary to the decoder. For the purpose, the LZW first forms an initial dictionary, which

consists of all the individual source symbols contained in the source alphabet. Then, the encoder examines the input symbol. Since the input symbol matches to an entry in the dictionary, its succeeding symbol is cascaded to form a string. The cascaded string does not find a match in the initial dictionary. Hence, the index of the matched symbol is encoded and the enlarged string (the matched symbol followed by the cascaded symbol) is listed as a new entry in the dictionary. The encoding process continues in this manner.

For the encoding and decoding processes, let us go through an example to see how the LZW algorithm can encode only the indexes and the decoder can still decode the input text string.

Example 6.4

Consider the following input text stream: *accbadaccbacccacc*. We see that the source alphabet is $S = \{a, b, c, d\}$. The top portion of [Table 6.5](#) (with indexes 1,2,3,4) gives a possible initial dictionary used in the LZW. When the first symbol *a* is input, the encoder finds that it has a match in the dictionary. Therefore, the next symbol *c* is taken to form a string *ac*. Because the string *ac* is not in the dictionary, it is listed as a new entry in the dictionary and is given an index, 5. The index of the matched symbol *a*, 1, is encoded. When the second symbol, *c*, is input, the encoder takes the following symbol *c* into consideration because there is a match to the second input symbol *c* in the dictionary. Since the string *cc* does not match any existing entry, it becomes a new entry in the dictionary with an index, 6. The index of the matched symbol (the second input symbol), *c*, is encoded. Now consider the third input symbol *c*, which appeared in the dictionary. Hence, the following symbol *b* is cascaded to form a string *cb*. Since the string *cb* is not in the dictionary, it becomes a new entry in the dictionary and is given an index, 7. The index of matched symbol *c*, 3, is encoded. The process proceeds in this fashion. Take a look at entry 11 in the dictionary shown in [Table 6.5](#). The input symbol at this point is *a*. Since it has a match in the previous entries, its next symbol *c* is considered. Since the string *ac* appeared in entry 5, the succeeding symbol *c* is combined. Now the new enlarged string becomes *acc* and it does not have a match in the previous entries. It is thus added to the dictionary. And a new index, 11, is given to the string *acc*. The index of the matched string *ac*, 5, is encoded and transmitted. The final sequence of encoded indexes is 1, 3, 3, 2, 1, 4, 5, 7, 11, 8. Like the LZ78, the entries in the dictionary become

TABLE 6.5

An Example of the Dictionary Coding Using the LZW Algorithm

| Index | Entry | Input Symbols | Encoded Index |
|-------|-------|---------------|---------------|
| 1 | a | | |
| 2 | b | | |
| 3 | c | | |
| 4 | d | | |
| 5 | ac | a | 1 |
| 6 | cc | c | 3 |
| 7 | cb | c | 3 |
| 8 | ba | b | 2 |
| 9 | ad | a | 1 |
| 10 | da | d | 4 |
| 11 | acc | a, c | 5 |
| 12 | cba | c, b | 7 |
| 13 | accb | a, c, c | 11 |
| 14 | bac | b, a, | 8 |
| 15 | cc... | c, c, ... | |

longer and longer in the LZW algorithm. This implies high coding efficiency since long strings can be represented by indexes.

Now let us take a look at the decoding process to see how the decoder can decode the input text stream from the received index. Initially, the decoder has the same dictionary (the top four rows in [Table 6.5](#)) as that in the encoder. Once the first index 1 comes, the decoder decodes a symbol *a*. The second index is 3, which indicates that the next symbol is *c*. From the rule applied in encoding, the decoder knows further that a new entry *ac* has been added to the dictionary with an index 5. The next index is 3. It is known that the next symbol is also *c*. It is also known that the string *cc* has been added into the dictionary as the sixth entry. In this way, the decoder reconstructs the dictionary and decodes the input text stream.

6.4.5.4 Summary

The LZW algorithm, as a representative of the LZ78 approach, is summarized below.

The initial dictionary contains the indexes for all the individual source symbols. At the beginning of encoding, when a symbol is input, since it has a match in the initial dictionary, the next symbol is cascaded to form a two-symbol string. Since the two-symbol string cannot find a match in the initial dictionary, the index of the first symbol is encoded and transmitted, and the two-symbol string is added to the dictionary with a new, incremented index. The next encoding step starts with the second symbol among the two symbols.

In the middle, the encoding process starts with the last symbol of the latest added dictionary entry. Since it has a match in the previous entries, its succeeding symbol is cascaded after the symbol to form a string. If this string appeared before in the dictionary (i.e., the string finds a match), the next symbol is cascaded as well. This process continues until such an enlarged string cannot find a match in the dictionary. At this moment, the index of the last matched string (the longest match) is encoded and transmitted, and the enlarged and unmatched string is added into the dictionary as a new entry with a new, incremented index.

Decoding is a process of transforming the index string back to the corresponding symbol string. In order to do so, however, the dictionary must be reconstructed exactly the same as that established in the encoding process. That is, the initial dictionary is constructed first in the same way as that in the encoding. When decoding the index string, the decoder reconstructs the same dictionary as that in the encoder according to the rule used in the encoding.

Specifically, at the beginning of the decoding, after receiving an index, a corresponding single symbol can be decoded. Via the next-received index, another symbol can be decoded. From the rule used in the encoding, the decoder knows that the two symbols should be cascaded to form a new entry added into the dictionary with an incremented index. The next step in the decoding will start from the second symbol among the two symbols.

Now consider the middle of the decoding process. The presently received index is used to decode a corresponding string of input symbols according to the reconstructed dictionary at the moment. (Note that this string is said to be with the present index). It is known from the encoding rule that the symbols in the string associated with the next index should be considered. (Note that this string is said to be with the next index). That is, the first symbol in the string with the next index should be appended to the last symbol in the string with the present index. The resultant combination, i.e., the string with the present index followed by the first symbol in the string with the next index, cannot find a match to an entry in the dictionary. Therefore, the combination should be added to the dictionary with an incremented index. At this moment, the next index becomes the new present

index, and the index following the next index becomes the new next index. The decoding process then proceeds in the same fashion in a new decoding step.

Compared with the LZ78 algorithm, the LZW algorithm eliminates the necessity of having the second item in the double, an index/codeword of the symbol following a matched string. That is, the encoder only needs to encode and transmit the first item in the double. This greatly enhances the coding efficiency and reduces the complexity of the LZ algorithm.

6.4.5.5 Applications

The CCITT Recommendation V.42 bis is a data compression standard used in modems that connect computers with remote users via the GSTN. In the compressed mode, the LZW algorithm is recommended for data compression.

In image compression, the LZW finds its application as well. Specifically, it is utilized in the graphic interchange format (GIF) which was created to encode graphical images. GIF is now also used to encode natural images, though it is not very efficient in this regard. For more information, readers are referred to Sayood (1996). The LZW algorithm is also used in the Unix Compress command.

6.5 International Standards for Lossless Still Image Compression

In the previous chapter, we studied Huffman and arithmetic coding techniques. We also briefly discussed the international standard for bilevel image compression, known as the Joint Bilevel Image Experts Group (JBIG). In this chapter, so far, we have discussed another two coding techniques: the run-length and dictionary coding techniques. We also introduced the international standards for facsimile compression, in which the techniques known as the MH, MR, and MMR were recommended. All of these techniques involve lossless compression. In the next chapter, the international still image coding standard JPEG will be introduced. As we will see, the JPEG has four different modes. They can be divided into two compression categories: lossy and lossless. Hence, we can talk about the lossless JPEG. Before leaving this chapter, however, we briefly discuss, compare, and summarize various techniques used in the international standards for lossless still image compression. For more detail, readers are referred to an excellent survey paper (Arps 1994).

6.5.1 Lossless Bilevel Still Image Compression

6.5.1.1 Algorithms

As mentioned previously, there are four different international standard algorithms falling into this category.

MH coding: This algorithm is defined in CCITT Recommendation T.4 for facsimile coding. It uses the 1-D RLC technique followed by the “modified” Huffman coding technique.

MR coding: Defined in CCITT Recommendation T.4 for facsimile coding. It uses the 2-D RLC technique followed by the MH coding technique.

MMR coding: Defined in CCITT Recommendation T.6. It is based on MR, but is modified to maximize compression.

JBIG coding: Defined in CCITT Recommendation T.82. It uses an adaptive 2-D coding model, followed by an adaptive arithmetic coding technique.

6.5.1.2 Performance Comparison

The JBIG test image set was used to compare the performance of the international algorithms. The set contains scanned business documents with different densities, graphic images, digital halftones, and mixed (document and halftone) images.

Note that digital halftones, also named (digital) halftone images, are generated by using only binary devices. Some small black units are imposed on a white background. The units may assume different shapes: a circle, a square, and so on. The denser the black units in a spot of an image, the darker the spot appears. The digital halftoning method has been used for printing gray-level images in newspapers and books. Digital halftoning through character overstriking, used to generate digital images in the early days for the experimental work associated with courses on digital image processing, is described in Gonzalez (1992).

The following two observations on the performance comparison were made after the application of the several techniques to the JBIG test image set.

For bilevel images excluding digital halftones, the compression ratio achieved by these techniques ranges from 3 to 100. The compression ratio increases monotonically in the order of the following standard algorithms: MH, MR, MMR, JBIG.

For digital halftones, MH, MR, and MMR result in data expansion, while JBIG achieves compression ratios in the range of 5 to 20. This demonstrates that among the techniques, JBIG is the only one suitable for the compression of digital halftones.

6.5.2 Lossless Multilevel Still Image Compression

6.5.2.1 Algorithms

There are two international standards for multilevel still image compression:

JBIG coding: Defined in CCITT Recommendation T. 82. It uses an adaptive arithmetic coding technique. To encode multilevel images, the JBIG decomposes multilevel images into bit-planes, then compresses these bit-planes using its bilevel image-compression technique. To further enhance compression ratio, it uses Gary coding to represent pixel amplitudes instead of weighted binary coding.

JPEG coding: Defined in CCITT Recommendation T. 81. For lossless coding, it uses the differential coding technique. The predictive error is encoded using either Huffman coding or adaptive arithmetic coding techniques.

6.5.2.2 Performance Comparison

A set of color test images from the JPEG standards committee was used for performance comparison. The luminance component (Y) is of resolution 720×576 pixels, while the chrominance components (U and V) are of 360×576 pixels. The compression ratios calculated are the combined results for all the three components. The following observations have been reported.

When quantized in eight bits/pixel, the compression ratios vary much less for multilevel images than for bilevel images, and are roughly equal to 2.

When quantized with five bits/pixel down to two bits/pixel, compared with the lossless JPEG, the JBIG achieves an increasingly higher compression ratio, up to a maximum of 29%.

When quantized with six bits/pixel, JBIG and lossless JPEG achieve similar compression ratios.

When quantized with seven bits/pixel to eight bits/pixel, the lossless JPEG achieves a 2.4%–2.6% higher compression ratio than JBIG.

6.6 Summary

Both Huffman coding and arithmetic coding, discussed in the previous chapter, are referred to as variable-length coding techniques, since the lengths of codewords assigned to different entries in a source alphabet are different. In general, a codeword of a shorter length is assigned to an entry with higher occurrence probabilities. They are also classified as fixed-length-to-variable-length coding techniques (Arps 1979), since the entries in a source alphabet have the same fixed length. RLC and dictionary coding, the focus of this chapter, are opposite, and are referred to as variable-length-to-fixed-length coding techniques. This is because the runs in the RLC and the string in the dictionary coding are variable and are encoded with codewords of the same fixed length.

Based on RLC, the international standard algorithms for facsimile coding, MH, MR, and MMR have worked successfully except for dealing with digital halftones. That is, these algorithms result in data expansion when applied to digital halftones. The JBIG, based on an adaptive arithmetic coding technique, not only achieves a higher coding efficiency than MH, MR, and MMR for facsimile coding, but also compresses the digital halftones effectively.

Note that 1-D RLC utilizes the correlation between pixels within a scan line, whereas 2-D RLC utilizes the correlation between pixels within a few scan lines. As a result, 2-D RLC can obtain higher coding efficiency than 1-D RLC on the one hand. On the other hand, 2-D RLC is more susceptible to transmission errors than 1-D RLC.

In text compression, the dictionary-based techniques have proven to be efficient. All the adaptive dictionary-based algorithms can be classified into two groups. One is based on a pioneering work by Ziv and Lempel in 1977, and another is based on their pioneering work in 1978. They are called the LZ77 and LZ78 algorithms, respectively. With the LZ77 algorithms, a fixed-size window slides through the input text stream. The sliding window consists of two parts: the search buffer and the look-ahead buffer. The search buffer contains the most recently encoded portion of the input text, while the look-ahead buffer contains the portion of the input text to be encoded immediately. For the symbols to be encoded, the LZ77 algorithms search for the longest match in the search buffer. The information about the match—the distance between the matched string in the search buffer and that in the look-ahead buffer, the length of the matched string, and the codeword of the symbol following the matched string in the look-ahead buffer—are encoded. Many improvements have been made in the LZ77 algorithms.

The performance of the LZ77 algorithms is limited by the sizes of the search buffer and the look-ahead buffer. With a finite size for the search buffer, the LZ77 algorithms will not work well in the case where repeated patterns are apart from each other by a distance longer than the size of the search buffer. With a finite size for the sliding window, the LZ77 algorithms will not work well in the case where matching strings are longer than the window. In order to be efficient, however, these sizes cannot be very large.

In order to overcome the problem, the LZ78 algorithms work in a different way. They do not use the sliding window at all. Instead of using the most recently encoded portion of the input text as a dictionary, the LZ78 algorithms use the index of the longest matched string as an entry of the dictionary. That is, each matched string cascaded with its immediate next symbol is compared with the existing entries of the dictionary. If this combination (a new string) does not find a match in the dictionary constructed at the moment, the combination will be included as an entry in the dictionary. Otherwise, the next symbol in the input text will be appended to the combination and the enlarged new combination will

be checked with the dictionary. The process continues until the new combination cannot find a match in the dictionary. Among various variants of the LZ78 algorithms, the LZW algorithm is perhaps the most important one. It only needs to encode the indexes of the longest matched strings to the dictionary. It can be shown that the decoder can decode the input text stream from the given index stream. In doing so, the same dictionary as that established in the encoder needs to be reconstructed at the decoder, and this can be implemented since the same rule used in the encoding is known in the decoder.

The size of the dictionary cannot be infinitely large because, as mentioned above, the coding efficiency will not be high. The common practice of the LZ78 algorithms is to keep the dictionary fixed once a certain size has been reached and the performance of the encoding is satisfactory. Otherwise, the dictionary will be set to empty and will be reconstructed from scratch.

Considering the fact that there are several international standards concerning still image coding (for both bilevel and multilevel images), a brief summary and a performance comparison are presented at the end of this chapter. At the beginning of this chapter, a description of the discrete Markov source and its n th extensions are provided. The Markov source and the AR model serve as important models for the dependent information sources.

Exercises

- 6.1 Draw the state diagram of a second-order Markov source with two symbols in the source alphabet. That is, $S = \{s_1, s_2\}$. It is assumed that the conditional probabilities are

$$p(s_1 | s_1s_1) = p(s_2 | s_2s_2) = 0.7,$$

$$p(s_2 | s_1s_1) = p(s_1 | s_2s_2) = 0.3, \text{ and}$$

$$p(s_1 | s_1s_2) = p(s_1 | s_2s_1) = p(s_2 | s_1s_2) = p(s_2 | s_2s_1) = 0.5$$

- 6.2 What are the definitions of raster algorithm and area algorithm in binary image coding? Which category does 1-D RLC belong to? Which category does 2-D RLC belong to?
- 6.3 What effect does a transmission error have on 1-D RLC and 2-D RLC, respectively? What is the function of the codeword EOL?
- 6.4 Make a convincing argument that the MH algorithm reduces the requirement of large storage space.
- 6.5 Which three different modes does 2-D RLC have? How do you view the vertical mode?
- 6.6 Using your own words, describe the encoding and decoding processes of the LZ77 algorithms. Go through Example 6.2.
- 6.7 Using your own words, describe the encoding and decoding processes of the LZW algorithm. Go through Example 6.3.
- 6.8 Read the reference paper (Arps 1994), which is an excellent survey on the international standards for lossless still image compression. Pay particular attention to all the figures and to [Table 6.1](#).

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7

Some Material Related to Multimedia Engineering

Prior to going to [Part II](#), which covers the subject of still image compression, in this [Chapter 7](#), the last chapter of [Part I](#), some important and relevant material will be addressed briefly. The chapter mainly discusses digital watermarking but also touches on reversible data hiding (RDH) and information forensics. Although these subjects do not belong to image and video compression directly, they are closely related to image and video compression and do belong to multimedia engineering.

7.1 Digital Watermarking

By the late 1990s, digital watermarking had been an active research area for signal processing and communication for years. Instead of conventional analog communications for speech, music, and movies, the corresponding digital communications have become more and more popular nowadays. However, it is clear that the digital version of signals can easily be copied as compared with the analog version of the signal in the communication. Therefore, how to protect signal and communication in the digital world had become an important issue. The digital watermarking scheme had been an important technology in this regard. That is, the existence of a digital watermarking signal can be utilized as an indication to protect the ownership.

7.1.1 Where to Embed Digital Watermark

Many research works have been conducted and reported in this field. For instance, where the watermark signal should be embedded has been an important issue for digital watermarking. Some researchers had proposed to embed the watermark signal into the high-frequency portion of a given host signal considering the watermark in the high-frequency portion may be less perceived by the human eyes. Some other researchers had proposed to embed the watermark signal into the middle-frequency portion of a given host signal.

Later, in 1997, a well-known research paper was published by Cox et al. (1997) that has been cited 8037 times currently, according to Google. In this paper, the watermark signal has been proposed to be embedded into the low-frequency portion of a given host signal in some selected and transformed domain. This technology has largely boosted digital watermarking technology. Furthermore, a survey paper was published by Cox and Miller (2002), in which it was shown that the concept of electronic watermarking could be traced back to a patent filed in 1954.

Note that there is only one randomly selected bit stream that has been utilized as the watermark signal. This watermark signal has then been embedded into the host signal, say a digital image, in this type of watermarking scheme. From this point of view, the embedded signal is binary, i.e., with or without the embedded watermarking signal in the carrier.

Shortly after the watermarking scheme was reported in Cox et al. (1997), a software known as StirMark was proposed in Petitcolas et al. (1998) and available in the public domain. This has proposed a dramatic challenge to digital watermarking technology. Although quite a few challenges have been solved by now, still some tough issues remain to be solved.

Later, it was found that the watermarking signal can also be embedded into the DC component of a given medium signal, say, digital image. It is shown that a thus-generated watermarked image is very much similar to the original image (Huang et al. 2000). This will be discussed in detail later in [Section 7.1.3](#).

7.1.2 Watermark Signal with One Random Binary Sequence

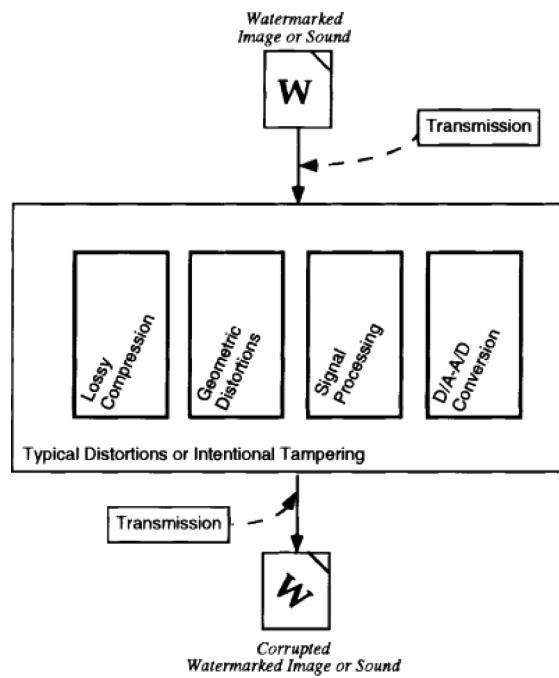
As mentioned above, a significant and successful watermarking scheme was proposed and conducted by Cox et al. (1997), which was published in IEEE Transactions on Image Processing. There, a watermark could be constructed as an independently and identically distributed (i.i.d.) Gaussian random vector, and is imperceptibly inserted in a spread-spectrum-like fashion into the perceptually most significant spectral components of the data set. The insertion of a watermark signal into the framework should make the watermark robust to some signal processing operations, e.g., lossy compression, filtering, digital-analog and analog-digital conversion, and requantization. Besides, it is expected to be able to resist some commonly utilized geometric transformations (such as cropping, scaling, translation, and rotation) provided that the original image is available and that it can be successfully registered against the transformed watermarked image. In these cases, the watermark detector can unambiguously identify the owner. Furthermore, the use of Gaussian noise ensures strong resilience to multiple-document or collisional attacks. Experimental results have been provided to support these claims, along with an exposition of pending open problems.

Note that [Figure 7.1](#) has been shown in Cox et al. (1997). In this figure, a watermarked image or sound may have been transmitted through lossy compression, or geometric distortion, or signal processing, or D/A-A/D conversion. Hence, some typical distortions or intentional tampering may take place here. Thus, transmitted image or sound may have gone through these commonly encountered corruptions. Watermarking signals are expected to remain.

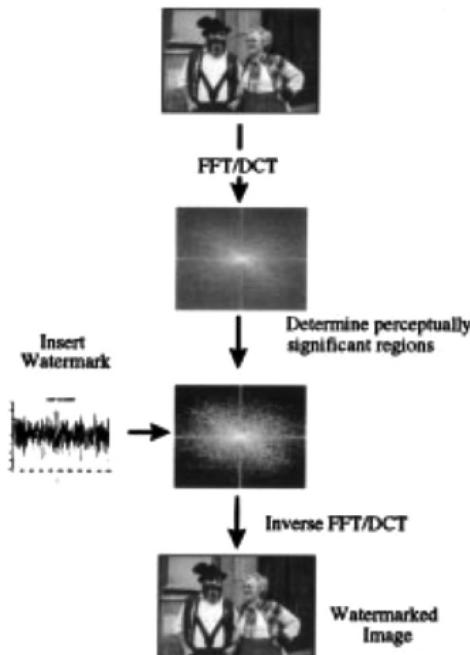
In [Figure 7.2](#), it is shown how the watermark is inserted into a host image. Specifically, a given host image is first transformed by either the fast Fourier transform (FFT) or the discrete cosine transform (DCT). Then the watermark signal is inserted into the FFT or DCT transform accordingly. The watermarked image can be derived after applying the inverse FFT or DCT transform.

As demonstrated in Cox et al. (1997), shown in [Figure 7.3](#) is one way to examine if a given image has a digital watermark signal or not. First, a given test image and an original image are going through the DCT operation, and the difference between these two images is then obtained. This difference is compared with the original watermark, then the similarity obtained is utilized so as to determine whether the given test image has been watermarked or not. Similarly, instead of the DCT, the FFT can be also be used.

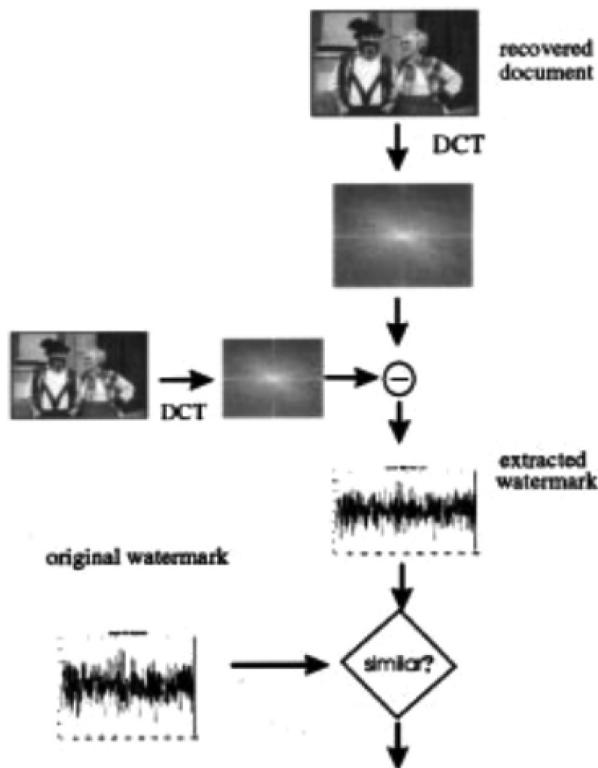
Here the watermarking procedure is briefly described with a digital document, say, image as an example. Considering a sequence of image pixel values which can be shown as $V = v_1, v_2, \dots, v_n$; while a watermark signal is represented as $X = x_1, x_2, \dots, x_n$. Hence, the sequence of image pixels after the watermark signal is embedded can be represented as $V' = v'_1, v'_2, \dots, v'_n$. This watermarked image is denoted as D' . Note that one or more attackers

**FIGURE 7.1**

Common processing operations that a media document could undergo. (From Cox, I.J. et al., *IEEE T. Image Process.*, 6, 1997.)

**FIGURE 7.2**

Stages of watermark insertion process. (From Cox, I.J. et al., *IEEE T. Image Process.*, 6, 1997.)

**FIGURE 7.3**

Encoding and decoding of the watermark string. (From Cox, I.J. et al., *IEEE T. Image Process.*, 6, 1997.)

may further alter D' , resulting in D^* . The corresponding corrupted watermark is defined as X^* .

Furthermore, it is noted that the following two equations are utilized in the algorithm. The first one is shown below.

$$v'_i = v_i (1 + \alpha x_i) \quad (7.1)$$

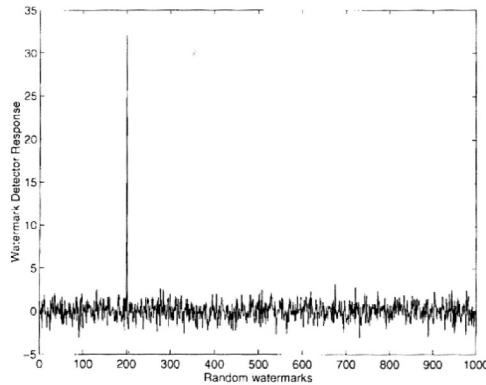
Note that $V = v_1, \dots, v_n$, which has been shown above.

Another relevant quantity, which is often utilized to measure the similarity between the extracted watermark signal and the original watermark signal, is shown below.

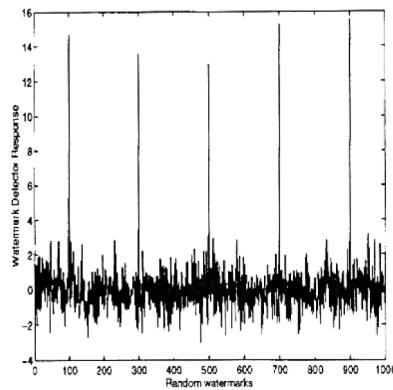
$$\text{Sim}(X, X^*) = X^* X / (X^* X^*) \quad (7.2)$$

Some successful works have been demonstrated in Cox et al. (1997). Two figures that have been demonstrated in Cox et al. (1997) are shown below. The left figure has shown that among 1000 randomly generated watermarks only one watermark has demonstrated the much higher response than the remaining 999 images. From the right image, it is observed that five images have shown high response, meaning that there are five watermarked images ([Figures 7.4](#) and [7.5](#)).

In summary, the novel watermarking works (Cox et al. 1997) described above have made substantial contribution to this subject.

**FIGURE 7.4**

Watermark detector response to 1000 randomly generated watermarks. Only one watermark matches that presented. (From Cox, I.J. et al., *IEEE T. Image Process.*, 6, 1997.)

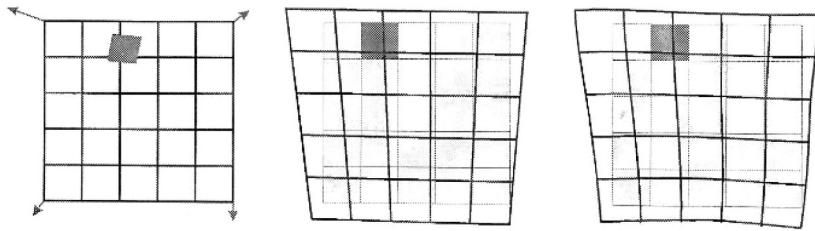
**FIGURE 7.5**

Watermark detector response to 1000 random generated watermarks. Each of the five watermarks is clearly indicated. (From Cox, I.J. et al., *IEEE T. Image Process.*, 6, 1997.)

7.1.3 Challenge Faced by Digital Watermarking

While the digital watermarking technology had been moved ahead as shown above, a critical challenge had been shown quickly. That is, Petitcolas et al. (1998) demonstrated a severe challenge faced by the watermarking schemes. They established a so-called StirMark scheme, which can make some slight geographical changes to a given test image so that it will be rather difficult for the embedded digital watermark signal to be identified and then utilized.

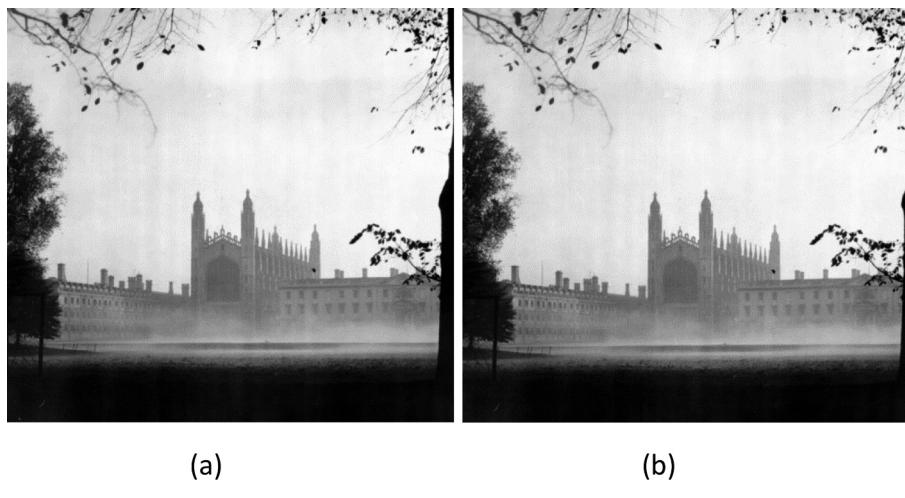
Let's see [Figure 7.6](#), which was shown in Petitcolas et al. (1998). On the left side there is a given test image. In the middle image, a slightly distorted image is shown, while in the right image, another different modification, called randomization, has been applied. As mentioned (Petitcolas et al. 1998), the size of an image shape's change has been extended in order to show clearly the minor geographical modification. The key point here is that the two kinds of manipulated images (in the middle and on the right side) would have

**FIGURE 7.6**

We exaggerate here the distortion applied by StirMark to still pictures. The first drawing corresponds to the original pictures; the others show the picture after StirMark has been applied—Without and with bending and randomization. (From Petitcolas, F.A.P. et al., Attacks on copyright marking systems (StirMark), in *International Workshop on Information Hiding*, Springer, Berlin, Germany, 1998.)

the watermark signal to be embedded into somehow different positions. Consequently, recovering the original watermark signal will become difficult. In particular, in the right-most case, where only the small and randomized modification has been applied to the watermarked image, it is rather difficult for people to extract the embedded watermark signal anymore.

Another example is demonstrated in Figure 7.7 (Petitcolas et al. 1998). The left image is a watermarked image while the right image is a geographically slightly modified watermarked image. Indeed, it is hard for human eyes to see the difference between the two. However, the watermark embedded into the left image is very hard to be identified from the right image with the human eyes.

**FIGURE 7.7**

Kings' College Chapel. (From Petitcolas, F. A. P. et al., Attacks on copyright marking systems (StirMark), in *International Workshop on Information Hiding*, Springer, Berlin, Germany, 1998.) (a) The watermarked image and (b) StirMark was applied, and then the watermark presence was tested. The similarity between the original watermark and the extracted watermark was only 3.74, which is rather lower than the 21.08 that can be obtained by working on the original watermarked image in (a). This indicates that the identifying watermarked image failed after StirMark was utilized.

7.1.4 Watermark Embedded into the DC Component

As mentioned in 7.1.1, here we discuss why a watermark signal should be embedded into the DC components of, say, a digital image. Although many papers in the literature have agreed that watermarks should be embedded in perceptually significant components, the DC components have been explicitly excluded from watermark embedding for a while. In Huang et al. (2000), a new embedding strategy for watermarking has been proposed based on a quantitative analysis on the magnitudes of the DCT components of host images. It was argued that more robustness can be achieved if watermarks are embedded in DC components since DC components have much larger perceptual capacity than any AC components do. Based on this idea, an adaptive watermarking algorithm has been proposed. There, the features of texture masking and luminance masking of the human visual system are incorporated into watermarking. The experimental results have demonstrated that the invisible watermarks embedded with the proposed watermark algorithm are very robust.

In Figure 7.8, the magnitude of the DCT obtained from three commonly utilized images in digital image processing—Lena, Baboon and Pepper—versus the corresponding spatial frequency are demonstrated. Note that the so-called spatial frequency means the sequence of the DCT coefficients follow zigzag sequencing. First, it is observed that the magnitude of the DC components is much larger than that of any AC components in general. Obviously, Figure 8 has demonstrated a huge discrepancy in terms of magnitude between the DC component and any the AC components.

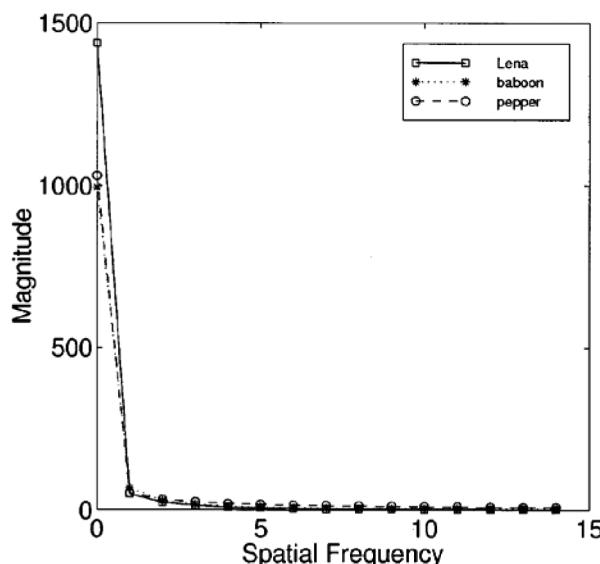
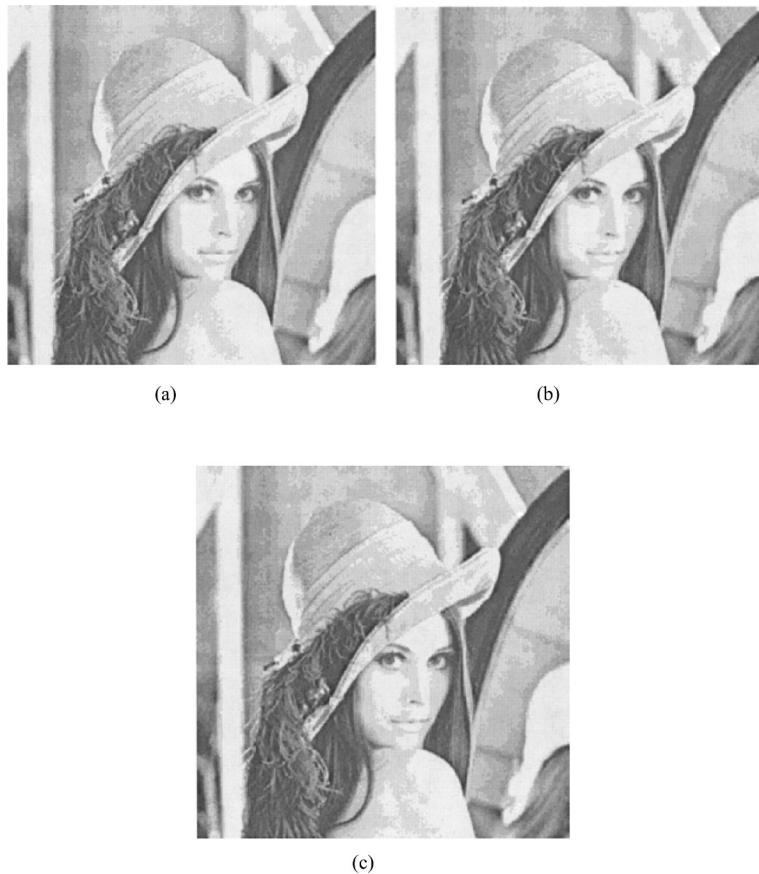


FIGURE 7.8

Magnitudes of DCT components at different spatial frequencies from 0 to 14. (From Huang, J. et al., *IEEE T. Circuits Syst. Vid.*, 10, 974–979, 2000.)

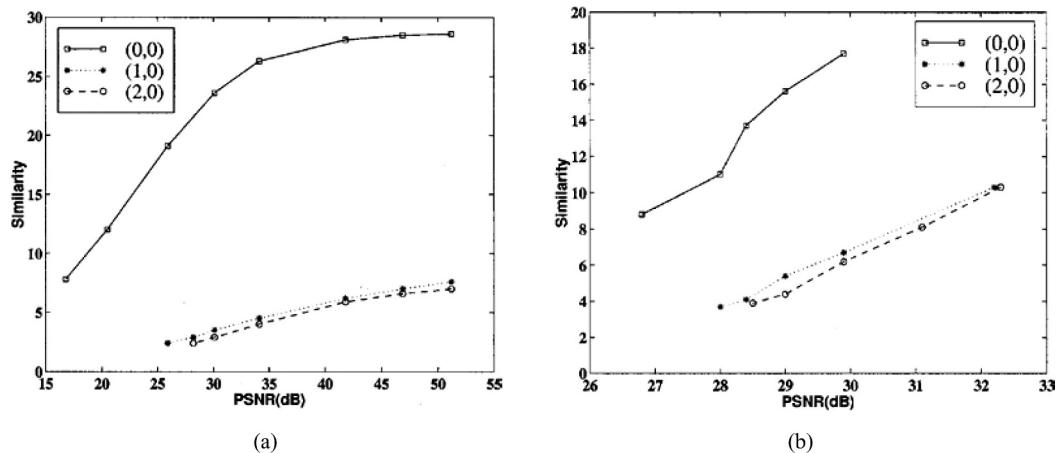
**FIGURE 7.9**

Comparison of invisibility when embedding watermarks in DC and AC components. (a) Original "Lena" image, (b) Watermarked image using DC components, and (c) Watermarked image using AC components. (From Huang, J. et al., *IEEE T. Circuits Syst. Vid.*, 10, 974–979, 2000.)

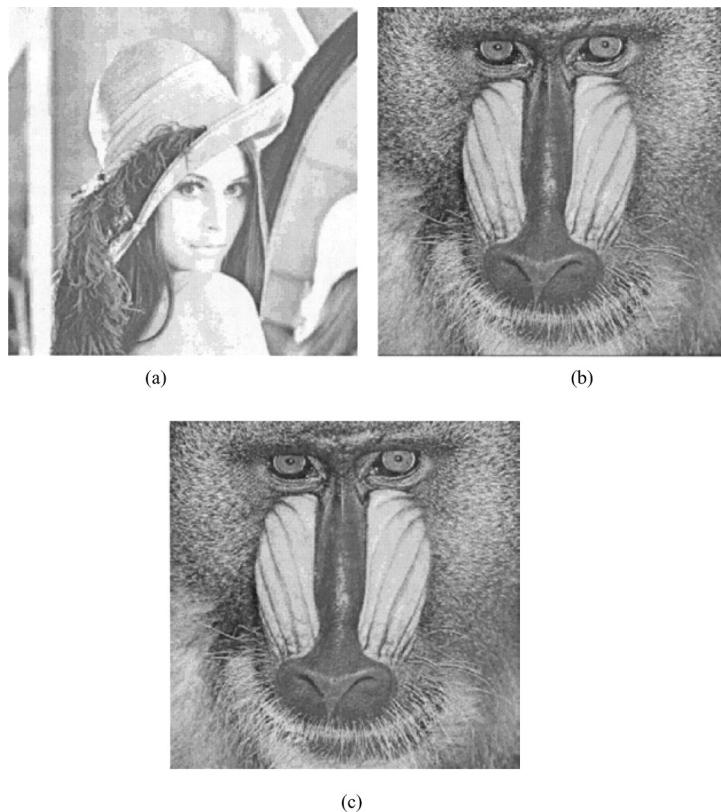
[Figure 7.9](#) shows the original Lena image, the watermarked Lena image with some data embedded into the DC components, and the watermarked Lena image with data hidden into the AC components. It becomes clear that the last two images have the same amount of data embedded into DC components and into the AC components. Obviously, the quality of the Lena image shown in (b) is very much similar to that shown (c). The reason is that the amount of data hidden in (b) is not larger. This indicates that embedding watermarking signal into the DC component can maintain the high quality of the watermarked image as long as we do not embed much data into the DC component.

Furthermore, it is shown in [Figure 7.10](#) that the watermarked Lena image with data hidden into DC components has higher similarity than the watermarked Lena image with data hidden into the AC components in both of the following two cases: (1) robustness against Gaussian noise and (2) robustness against JPEG compression.

In [Figure 7.11a](#), a watermarked Lena image is shown. An original Baboon image is shown in [Figure 7.11b](#). A watermarked Baboon image is shown in [Figure 7.11c](#).

**FIGURE 7.10**

Comparison of robustness when embedding watermarks in DC and AC components. (a) Robustness against Gaussian noise and (b) Robustness against JPEG compression. (From Huang, J. et al., *IEEE T. Circuits Syst. Vid.*, 10, 974–979, 2000.)

**FIGURE 7.11**

Demonstration of invisibility. (a) Watermarked "Lena" image, the original image is in Figure 9(a), (b) Original "Baboon" image, and (c) Watermarked "Baboon" image. In both (a) and (c), the proposed watermarking algorithm is applied. All images are of 256×256 . (From Huang, J. et al., *IEEE T. Circuits Syst. Vid.*, 10, 974–979, 2000.)

7.1.5 Digital Watermark with Multiple Information Bits and Error Correction Coding

So far all of the watermarking schemes that have been discussed in the prior sections have one thing in common. That is, only one fixed piece of information has been embedded as a watermark into, say, digital images or voice messages. In reality, instead of only one fixed piece of information, multiple different pieces of information may be needed as a watermark signal that needs to be embedded into image, video, and speech. Furthermore, the interleaving technology has been applied in order to further make thus embedded watermark signal to be more secure. Some works in this regard have been reported, e.g., (Huang and Shi 2002, Kang et al. 2003, 2010, 2011).

7.1.6 Conclusion

Digital watermarking schemes have been useful in our modern life. Although it is possible that digital watermarking schemes may be broken by some attacker, digital watermarking will be able to play an important role in our daily lives. A good example is shown below. It was reported that in the 2008 Olympic competitions held in Beijing, China all of the news agencies utilized watermarking technologies when they sent news from Beijing to their host countries and areas. On the one hand, every lock used in our daily life may possibly be broken. As the lock is strong, however, to break it may take a long period of time and more efforts. On the other hand, the different locks with different security levels can be selected for different scenarios. Therefore, locks are still widely utilized in the world in our daily life. The conclusion we can make here is that, for different scenarios, some different watermarking schemes need to be carefully selected and utilized.

7.2 Reversible Data Hiding

In the past two decades, another technology, RDH, also referred to as lossless or invertible data hiding, has gradually become a very active research area in the field of data hiding. RDH is another kind of data-hiding scheme, which is different from the digital watermarking we introduced in [Section 7.1](#). The main difference is shown below. That is, once the embedded data have been extracted from the carrier signal, say, a digital image or an oral speech, the so-called RDH scheme requests the carrier signal, here a digital image or an oral speech, be recovered back to its original version of the image or oral speech without any change. Obviously, the RDH is rather different from the watermarking we just discussed. In certain scenarios, the reversibility may be needed and hence requested.

In a recent comprehensive survey paper (Shi et al. 2016) on RDH, the RDH has been considered and separated into six different categories. They are (1) RDH into image-spatial domain; (2) RDH into image-compressed domain (e.g., JPEG); (3) RDH suitable for image semi-fragile authentication; (4) RDH with image quality measurement different from the widely utilized one (e.g., peak signal noise ratio [PSNR]); (5) RDH into encrypted images, which is expected to have wide application in the cloud computation; and (6) RDH into video and audio. Each of all of these six different kinds of RDH has been introduced and summarized, and the future research is also discussed.

7.3 Information Forensics

As we have entered into the modern digital world, we do need to study so as to get to know information forensics. By forensics, one example can be given as follows. That is, given an image or a speech signal we want to know if the image or the speech signal has been compressed or not, and if it has been compressed then to what degree. For example, has it been compressed only once or more than once, with what type of compression parameters, and so on. If an image has been modified somehow, we may want to know where the modification has taken place and to what degree the image has been modified. All of these are critically important to our modern society. Therefore, it is expected that the research work in this direction will face severe challenges.

Some efforts have been made to solve some issues in information forensics. As said earlier, we knew that digital watermarking has been studied and research efforts have been made. Many problems have been solved, while some tough issues remain. One example is the so-called StirMark scheme. Up to this point, carefully designed watermarking schemes can handle the schemes listed in StirMark as long as the attack is not that tough. On the other hand, the current watermarking schemes in general still could not handle all of the attacks listed in StirMark completely, especially the attack known as randomization.

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Part II

Still Image Compression



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8

Still Image Coding Standard—JPEG

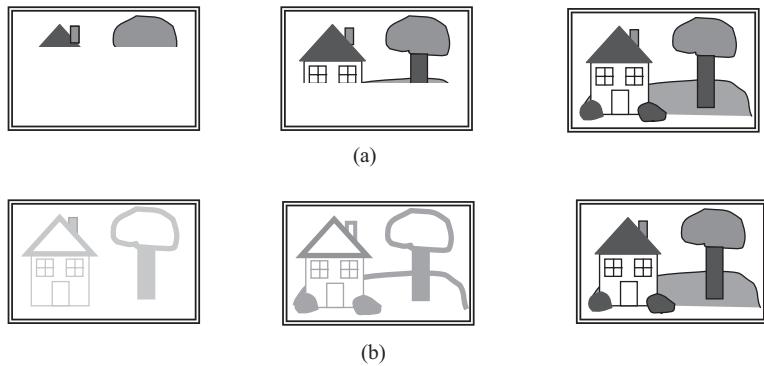
In this chapter, the JPEG standard is introduced. This standard allows for lossy and lossless encoding of still images, and four distinct modes of operation are supported: sequential DCT-based mode, progressive DCT-based mode, lossless mode, and hierarchical mode.

8.1 Introduction

Still image coding is an important application of data compression. When an analog image or picture is digitized, each pixel is represented by a fixed number of bits, which correspond to a certain number of gray levels. In this uncompressed format, the digitized image requires a large number of bits to be stored or transmitted. As a result, compression becomes necessary due to the limited communication bandwidth or storage size. Since the mid-1980s, the ITU and ISO have been working together to develop a joint international standard for the compression of still images. Officially, JPEG (Mitchell 1992) is the ISO/IEC international standard 10918-1, digital compression and coding of continuous-tone still images, or the ITU-T recommendation T.81. JPEG became an international standard in 1992. The JPEG standard allows for both lossy and lossless encoding of still images. The algorithm for lossy coding is a DCT-based coding scheme. This is the baseline of JPEG and is sufficient for many applications. However, to meet the needs of applications that cannot tolerate loss, e.g., compression of medical images, a lossless coding scheme is also provided and is based on a predictive coding scheme. From the algorithmic point of view, JPEG includes four distinct modes of operation: sequential DCT-based mode, progressive DCT-based mode, lossless mode, and hierarchical mode. In the following sections, an overview of these modes is provided. Further technical details can be found in the books by Pennebaker and Mitchell (1992) and Symes (1998).

In the sequential DCT-based mode, an image is first partitioned into blocks of 8×8 pixels. The blocks are processed from left to right and top to bottom. The 8×8 two-dimensional Forward DCT is applied to each block and the 8×8 DCT coefficients are quantized. Finally, the quantized DCT coefficients are entropy encoded and output as part of the compressed image data.

In the progressive DCT-based mode, the process of block partitioning and forward DCT transform is the same as in the sequential DCT-based mode. However, in the progressive mode, the quantized DCT coefficients are first stored in a buffer before the encoding is performed. The DCT coefficients in the buffer are then encoded by a multiple scanning process. In each scan, the quantized DCT coefficients are partially encoded by either spectral selection or successive approximation. In the method of spectral selection, the quantized DCT coefficients are divided into multiple spectral bands according to a zigzag

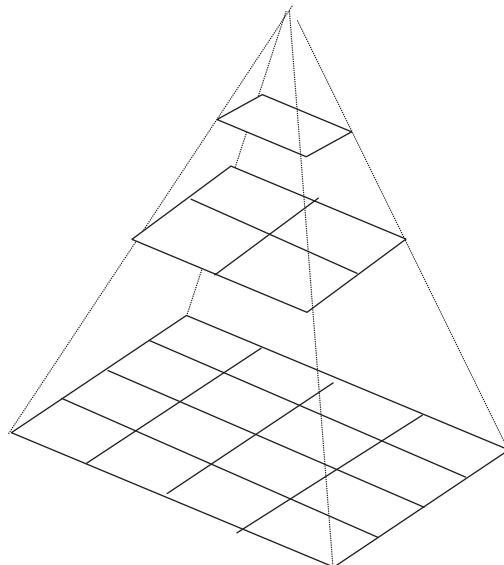
**FIGURE 8.1**

(a) Sequential coding and (b) Progressive coding.

order. In each scan, a specified band is encoded. In the method of successive approximation, a specified number of most significant bits of the quantized coefficients are first encoded and the least significant bits are then encoded in subsequent scans.

The difference between sequential coding and progressive coding is shown in [Figure 8.1](#). In the sequential coding an image is encoded part-by-part according to the scanning order while in the progressive coding the image is encoded by multi-scanning process and in each scan the full image is encoded to a certain quality level.

As mentioned earlier, lossless coding is achieved by a predictive coding scheme. In this scheme, three neighboring pixels are used to predict the current pixel to be coded. The prediction difference is entropy-coded using either Huffman or arithmetic coding. Since the prediction is not quantized, the coding is lossless.

**FIGURE 8.2**

Hierarchical multi-resolution encoding.

Finally, in the hierarchical mode, an image is first spatially down-sampled to a multi-layered pyramid, resulting in a sequence of frames as shown in [Figure 8.2](#). This sequence of frames is encoded by a predictive coding scheme. Except for the first frame, the predictive coding process is applied to the differential frames, i.e., the differences between the frame to be coded and the predictive reference frame. It is important to note that the reference frame is equivalent to the previous frame that would be reconstructed in the decoder. The coding method for the difference frame may use the DCT-based coding method, the lossless coding method, or the DCT-based processes with a final lossless process. Down-sampling and up-sampling filters are used in the hierarchical mode. The hierarchical coding mode provides a progressive presentation similar to progressive DCT-based mode but is also useful in the applications that have multi-resolution requirements. The hierarchical coding mode also provides the capability of progressive coding to a final lossless stage.

8.2 Sequential DCT-Based Encoding Algorithm

The sequential DCT-based coding algorithm is the baseline algorithm of the JPEG coding standard. The block diagram of encoding process is shown in [Figure 8.3](#). As shown in [Figure 8.4](#), the digitized image data is first partitioned into blocks of 8×8 pixels. The two-dimensional forward DCT is applied to each 8×8 block. The two-dimensional forward and inverse DCT of 8×8 block are defined as follows.

FDCT:

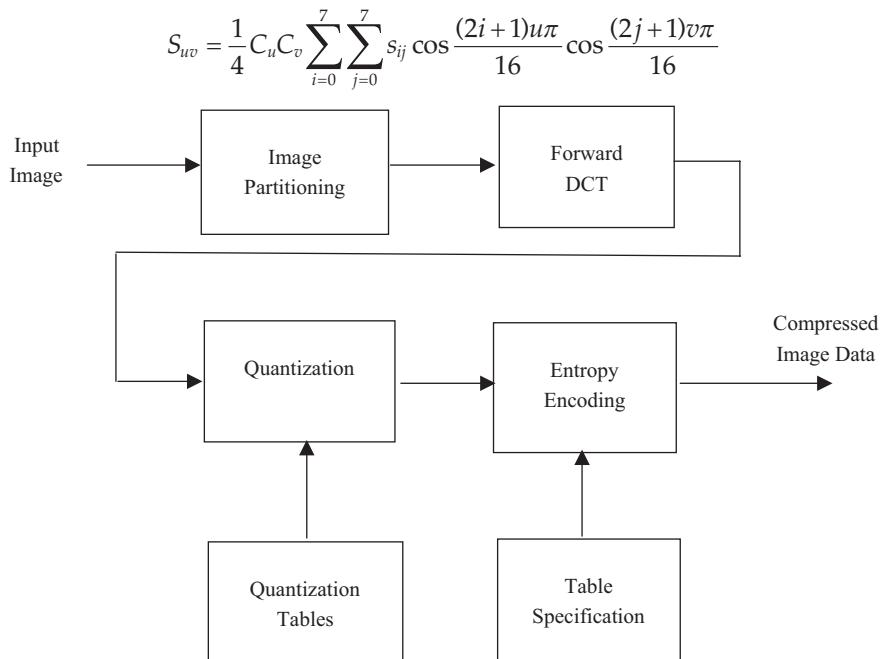
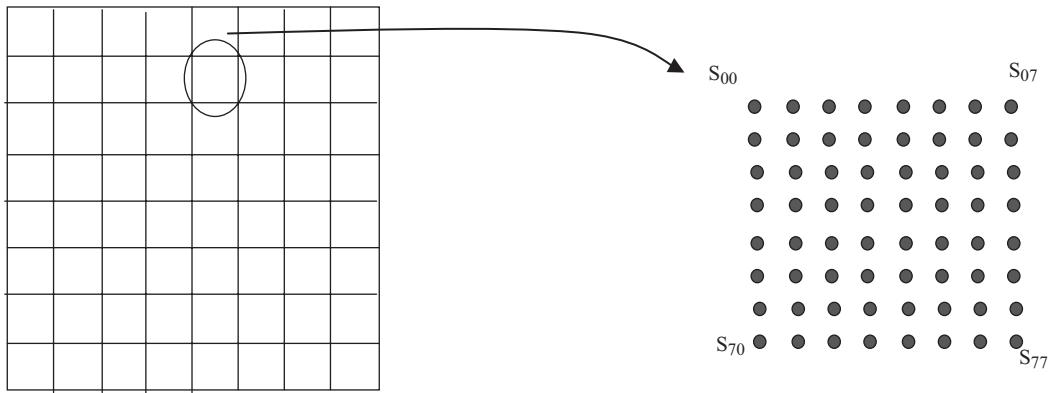


FIGURE 8.3

Block diagram of sequential DCT-based encoding process.

**FIGURE 8.4**Partitioning to 8×8 blocks.

IDCT:

$$s_{ij} = \frac{1}{4} \sum_{u=0}^7 \sum_{v=0}^7 C_u C_v S_{uv} \cos \frac{(2i+1)u\pi}{16} \cos \frac{(2j+1)v\pi}{16}$$

$$C_u C_v = \begin{cases} \frac{1}{\sqrt{2}} & \text{for } u, v = 0 \\ 1 & \text{otherwise} \end{cases} \quad (8.1)$$

where s_{ij} is the value of the pixel at position (i, j) in the block and S_{uv} is the transformed (u, v) DCT coefficient.

After the forward DCT, quantization of the transformed DCT coefficients is performed. Each of the 64 DCT coefficients is quantized by a uniform quantizer:

$$S_{quv} = \text{round}\left(\frac{S_{uv}}{Q_{uv}}\right) \quad (8.2)$$

where the S_{quv} is quantized value of the DCT coefficient, S_{uv} and Q_{uv} is the quantization step obtained from the quantization table. There are four quantization tables that may be used by the encoder, but there is no default quantization table specified by the standard. Two particular quantization tables are shown in [Table 8.1](#).

At the decoder, the dequantization is performed as follows:

$$R_{quv} = S_{quv} \times Q_{uv} \quad (8.3)$$

where R_{quv} is the value of the dequantized DCT coefficient. After quantization, the DC coefficient, S_{q00} , is treated separately from the other 63 AC coefficients. The DC coefficients are encoded by a predictive coding scheme. The encoded value is the difference (*DIFF*) between the quantized DC coefficient of the current block (S_{q00}) and that of the previous block of the same component (*PRED*):

TABLE 8.1

Two Examples of Quantization Tables Used by JPEG

| | | | | | | | | | | | | | | | |
|------------------------------|----|----|----|-----|-----|-----|-----|--------------------------------|----|----|----|----|----|----|----|
| 16 | 11 | 10 | 16 | 24 | 40 | 51 | 61 | 17 | 18 | 24 | 47 | 99 | 99 | 99 | 99 |
| 12 | 12 | 14 | 19 | 26 | 58 | 60 | 55 | 18 | 21 | 26 | 66 | 99 | 99 | 99 | 99 |
| 14 | 13 | 16 | 24 | 40 | 57 | 69 | 56 | 24 | 26 | 56 | 99 | 99 | 99 | 99 | 99 |
| 14 | 17 | 22 | 29 | 51 | 87 | 80 | 62 | 47 | 66 | 99 | 99 | 99 | 99 | 99 | 99 |
| 18 | 22 | 37 | 56 | 68 | 109 | 103 | 77 | 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 24 | 35 | 55 | 64 | 81 | 104 | 113 | 92 | 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 49 | 64 | 78 | 87 | 103 | 121 | 120 | 101 | 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 72 | 92 | 95 | 98 | 112 | 100 | 103 | 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| Luminance quantization table | | | | | | | | Chrominance quantization table | | | | | | | |

$$DIFF = S_{q00} - PRED \quad (8.4)$$

The value of *DIFF* is entropy-coded with Huffman tables. More specifically, the two's complement of the possible *DIFF* magnitudes is grouped into 12 categories, "SSSS." The Huffman codes for these 12 difference categories and additional bits are shown in [Table 8.2](#).

For each non-zero category, additional bits are added to the codeword to uniquely identify which difference within the category actually occurred. The number of additional bits is defined by "SSSS" and the additional bits are appended to the least significant bit of the Huffman code (most significant bit first) according the following rule. If the difference value is positive, the "SSSS" low-order bits of *DIFF* are appended; if the difference value is negative, then the "SSSS" low-order bits of *DIFF*-1 are appended. As an example, the Huffman tables used for coding the luminance and chrominance DC coefficients are shown in [Table 8.3](#) and [8.4](#), respectively. These two tables have been developed from the average statistics of a large set of images with eight-bit precision.

In contrast to the coding of DC coefficients, the quantized AC coefficients are arranged to a zigzag order before being entropy coded. This scan order is shown in [Figure 8.5](#).

According to the zigzag scanning order, the quantized coefficients can be represented as:

$$ZZ(0) = S_{q00}, ZZ(1) = S_{q01}, ZZ(2) = S_{q10}, \dots, ZZ(63) = S_{q77}. \quad (8.5)$$

TABLE 8.2

Huffman Coding of DC Coefficients

| SSSS | DIFF Values | Additional Bits |
|------|------------------------------------|--------------------------------------|
| 0 | 0 | - |
| 1 | -1, 1 | 0, 1 |
| 2 | -3, -2, 2, 3 | 00, 01, 10, 11 |
| 3 | -7, ..., -4, 4, ..., 7 | 000, ..., 011, 100, ..., 111 |
| 4 | -15, ..., -8, 8, ..., 15 | 0000, ..., 0111, 1000, ..., 1111 |
| 5 | -31, ..., -16, 16, ..., 31 | 00000, ..., 01111, 10000, ..., 11111 |
| 6 | -63, ..., -32, 32, ..., 63 | |
| 7 | -127, ..., -64, 64, ..., 127 | |
| 8 | -255, ..., -128, 128, ..., 255 | |
| 9 | -511, ..., -256, 256, ..., 511 | |
| 10 | -1023, ..., -512, 512, ..., 1023 | |
| 11 | -2047, ..., -1024, 1024, ..., 2047 | |

TABLE 8.3

Huffman Table for Luminance DC Coefficient Differences

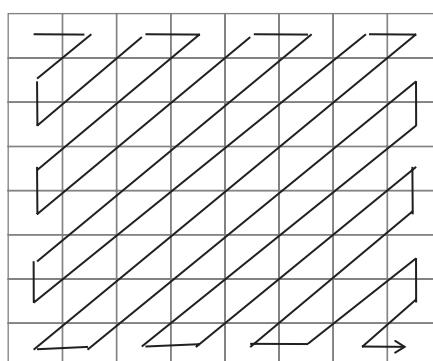
| Category | Code Length | Code Word |
|----------|-------------|-----------|
| 0 | 2 | 00 |
| 1 | 3 | 010 |
| 2 | 3 | 011 |
| 3 | 3 | 100 |
| 4 | 3 | 101 |
| 5 | 3 | 110 |
| 6 | 4 | 1110 |
| 7 | 5 | 11110 |
| 8 | 6 | 111110 |
| 9 | 7 | 1111110 |
| 10 | 8 | 11111110 |
| 11 | 9 | 111111110 |

TABLE 8.4

Huffman Table for Chrominance DC Coefficient Differences

| Category | Code Length | Code Word |
|----------|-------------|-------------|
| 0 | 2 | 00 |
| 1 | 2 | 01 |
| 2 | 2 | 10 |
| 3 | 3 | 110 |
| 4 | 4 | 1110 |
| 5 | 5 | 11110 |
| 6 | 6 | 111110 |
| 7 | 7 | 1111110 |
| 8 | 8 | 11111110 |
| 9 | 9 | 111111110 |
| 10 | 10 | 1111111110 |
| 11 | 11 | 11111111110 |

DC

**FIGURE 8.5**

Zigzag scanning order of DCT coefficients.

Since many of the quantized AC coefficients become zero, they can be very efficiently encoded by exploiting the run of zeros. The run-length of zeros are identified by the non-zero coefficients. An eight-bit code “RRRRSSSS” is used to represent the non-zero coefficient. The four least significant bits, “SSSS,” define a category for the value of the next non-zero coefficient in the zigzag sequence, which ends the zero-run. The four most significant bits, “RRRR,” define the run-length of zeros in the zigzag sequence or the position of the non-zero coefficient in the zigzag sequence. The composite value, RRRRSSSS, is shown in [Figure 8.6](#). The value “RRRRSSSS” = “11110000” is defined as ZRL, “RRRR”=“1111” represents a run-length of 16 zeros and “SSSS”=“0000” represents a zero-amplitude. Therefore, ZRL is used to represent a run length of 16 zero coefficients followed by a zero-amplitude coefficient, it is not an *abbreviation*. In the case of a run-length of zero coefficients that exceeds 15, multiple symbols will be used. A special value “RRRRSSSS” = “00000000” is used to code the end-of-block (EOB). An EOB occurs when the remaining coefficients in the block are zero. The entries marked “N/A” are undefined.

The composite value, RRRRSSSS, is then Huffman coded. SSSS is actually the number to indicate “category” in the Huffman code table. The coefficient values for each category are shown in [Table 8.5](#).

Each Huffman code is followed by additional bits that specify the sign and exact amplitude of the coefficients. As with the DC code tables, the AC code tables have also been developed

| | | SSSS | | | | |
|------|----|------|---|---|------------------|----|
| | | 0 | 1 | 2 | 9 | 10 |
| RRRR | 0 | EOB | | | | |
| | . | N/A | | | | |
| | . | N/A | | | | |
| | 15 | N/A | | | | |
| | | ZRL | | | | |
| | | | | | Composite values | |
| | | | | | | |

FIGURE 8.6

Two-dimensional value array for Huffman coding.

TABLE 8.5
Huffman Coding for AC Coefficients

| Category (SSSS) | AC Coefficient Range |
|-----------------|-------------------------------|
| 1 | -1,1 |
| 2 | -3,-2,2,3 |
| 3 | -7,...,-4,4,...,7 |
| 4 | -15,...,-8,8,...,15 |
| 5 | -31,...,-16,16,...,31 |
| 6 | -63,...,-32,32,...,63 |
| 7 | -127,...,-64,...,64,...,127 |
| 8 | -255,...,-128,128,...,255 |
| 9 | -511,...,-256,256,...,511 |
| 10 | -1023,...,-512,512,...,1023 |
| 11 | -2047,...,-1024,1024,...,2047 |

from the average statistics of a large set of images with eight-bit precision. Each composite value is represented by a Huffman code in the AC code table. The format for the additional bits is the same as in the coding of DC coefficients. The value of SSSS gives the number of additional bits required to specify the sign and precise amplitude of the coefficient. The additional bits are either the low-order SSSS bits of ZZ(k) when ZZ(k) is positive or the low-order SSSS bits of ZZ(k)-1 when ZZ(k) is negative. Here, ZZ(k) is the kth coefficient in the zigzag scanning order of coefficients being coded. The Huffman tables for AC coefficients can be found in Annex K of the JPEG standard (Mitchell 1992) and are not listed here due to space limitations.

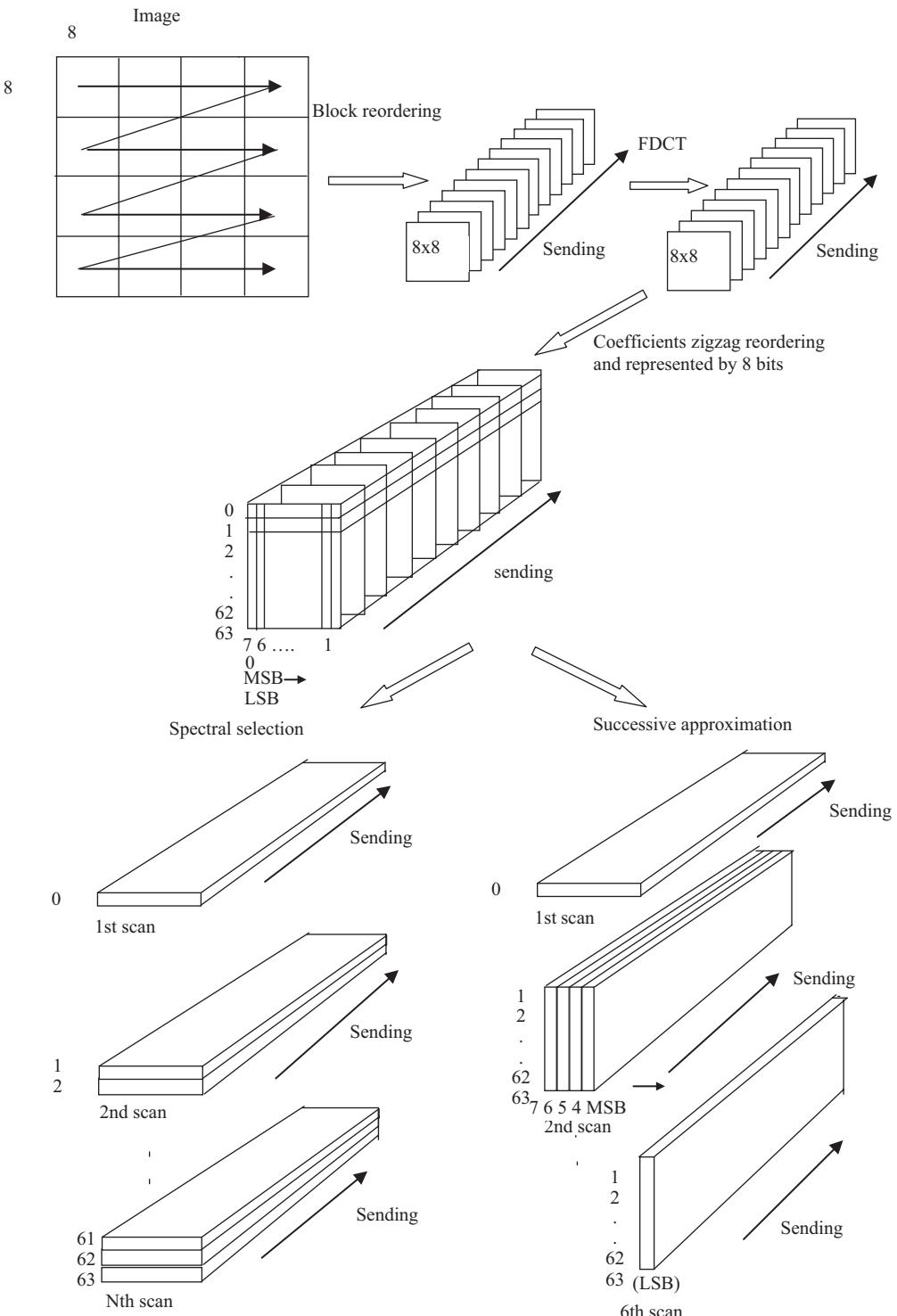
As described above, Huffman coding is used as the means of entropy coding. However, an adaptive arithmetic coding procedure can also be used. As with the Huffman coding technique, the binary arithmetic coding technique is also lossless. It is possible to transcode between two systems without either the FDCT or IDCT processes. Since this transcoding is a lossless process, it does not affect the picture quality of the reconstructed image. The arithmetic encoder encodes a series of binary symbols—zeros or ones—where each symbol represents the possible result of a binary decision. The binary decisions include the choice between positive and negative signs, a magnitude being zero or non-zero, or a particular bit in a sequence of binary digits being zero or one. There are four steps in the arithmetic coding: initializing the statistical area, initializing the encoder, terminating the code string, and adding restart markers.

8.3 Progressive DCT-Based Encoding Algorithm

In progressive DCT-based coding, the input image is first partitioned to blocks of 8×8 pixels. The two-dimensional 8×8 DCT is then applied to each block. The transformed DCT-coefficient data are then encoded with multiple scans. At each scan, a portion of the transformed DCT coefficient data is encoded. This partial encoded data can be reconstructed to obtain a full image size with lower picture quality. The coded data of each additional scan will enhance the reconstructed image quality until the full quality has been achieved at the completion of all scans. Two methods have been used in JPEG standard to perform the DCT-based progressive coding. These include spectral selection and successive approximation.

In the method of spectral selection, the transformed DCT coefficients are first re-ordered as zigzag sequence and then divided into several bands. A frequency band is defined in the scan header by specifying the starting and ending indices in the zigzag sequence. The band containing DC coefficient is encoded at the first scan. In the following scan, it is not necessary for the coding procedure to follow the zigzag ordering. In the method of the successive approximation, the DCT coefficients are first reduced in precision by the point transform. The point transform of the DCT coefficients is an arithmetic-shift-right by a specified number of bits, or divided by a power of 2 (near zero, there is slight difference in truncation of precision between arithmetic shift and divide by 2, see annex K10 of Mitchell [1992]). This specified number is the successive approximation of bit position. To encode using successive approximations, the significant bits of DCT coefficient are encoded in the first scan, and each successive scan that follows progressively improves the precision of the coefficients by one bit. This continues until full precision is reached.

The principles of spectral selection and successive approximation are shown in [Figure 8.7](#). For both methods, the quantized coefficients are coded with either Huffman or arithmetic codes at each scan. In spectral selection and the first scan of successive approximation for an

**FIGURE 8.7**

Progressive coding with spectral selection and successive approximation.

image, the AC coefficient coding model is similar to that used by in the sequential DCT-based coding mode. However, the Huffman code tables are extended to include coding of runs of end-of-bands (EOBs). For distinguishing the end-of-band and end-of-block, a number, n , which is used to indicate the range of run length, is added to the end-of-band (EOBn). The EOBn code sequence is defined as follows. Each EOBn is followed by an extension field, which has the minimum number of bits required to specify the run length. The end-of-band run structure allows efficient coding of blocks, which have only zero coefficients. For example, an EOB run of length 5 means that the current block and the next four blocks have an end-of-band with no intervening non-zero coefficients. The Huffman coding structure of the subsequent scans of successive approximation for a given image is similar to the coding structure of the first scan of that image. Each non-zero quantized coefficient is described by a composite eight-bit run length-magnitude value of the form: RRRRSSSS. The four most significant bits, RRRR, indicate the number of zero coefficients between the current coefficient and the previously coded coefficient. The four least significant bits, SSSS, gives the magnitude category of the non-zero coefficient. The run length-magnitude composite value is Huffman coded. Each Huffman code is followed by additional bits: one bit is used to code the sign of the non-zero coefficient and another one bit is used to code the correction, where "0" means no correction and "1" means add one to the decoded magnitude of the coefficient. Although this technique has been described using Huffman coding, it should be noted that arithmetic encoding can also be used in its place.

8.4 Lossless Coding Mode

In the lossless coding mode, the coding method is spatial-based coding instead of DCT-based coding. However, the coding method is extended from the method for coding the DC coefficients in the sequential DCT-based coding mode. Each pixel is coded with a predictive coding method, where the predicted value is obtained from one of three one-dimensional or one of four two-dimensional predictors, which are shown in [Figure 8.8](#).

In [Figure 8.8](#), the pixel to be coded is denoted by x , and the three causal neighbors are denoted by a , b , and c . The predictive value of x , P_x , is obtained from three neighbors, a , b , and c , in one of seven ways as listed in [Table 8.6](#).

In [Table 8.6](#), the selection value 0 is only used for differential coding in hierarchical coding mode. Selections 1, 2, and 3 are one-dimensional predictions and 4, 5, 6, and 7 are two-dimensional predictions. Each prediction is performed with full integer precision, and without clamping of either underflow or overflow beyond the input bounds. In order

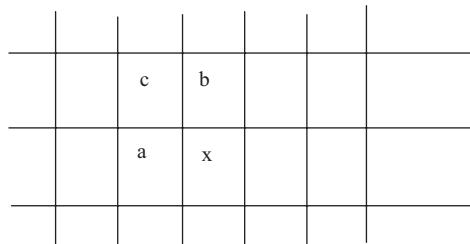


FIGURE 8.8

Spatial relation between the pixel to be coded and three decoded neighbors.

TABLE 8.6

Predictors for Lossless Coding

| Selection-value | Prediction |
|-----------------|-----------------------------------|
| 0 | No prediction (Hierarchical mode) |
| 1 | $P_x = a$ |
| 2 | $P_x = b$ |
| 3 | $P_x = c$ |
| 4 | $P_x = a+b-c$ |
| 5 | $P_x = a + ((b-c)/2)^a$ |
| 6 | $P_x = b + ((a-c)/2)^a$ |
| 7 | $P_x = (a+b)/2$ |

^a Shift right arithmetic operation

to achieve lossless coding, the prediction differences are coded with either Huffman coding or arithmetic coding. The prediction difference values can be from 0 to 2^{16} for eight-bit pixels. The Huffman tables developed for coding DC coefficients in the sequential DCT-based coding mode are used with one additional entry to code the prediction differences. For arithmetic coding, the statistical model defined for the DC coefficients in sequential DCT-based coding mode is generalized to a two-dimensional form in which differences are conditioned on the pixel to the left and the line above.

8.5 Hierarchical Coding Mode

The hierarchical coding mode provides a progressive coding similar to the progressive DCT-based coding mode, but it offers more functionality. This functionality addresses applications with multi-resolution requirements. In hierarchical coding mode, an input image frame is first decomposed to a sequence of frames, such as the pyramid shown in [Figure 8.2](#). Each frame is obtained through a down-sampling process, i.e., low-pass filtering followed by sub-sampling. The first frame (the lowest resolution) is encoded as a non-differential frame. The following frames are encoded as differential frames, where the differential is with respect to the previously coded frame. Note that an up-sampled version that would be reconstructed in the decoder is used. The first frame can be encoded by the methods of sequential DCT-based coding, spectral selection method of progressive coding, or lossless coding with either Huffman code or arithmetic code. However, within an image, the differential frames are either coded by the DCT-based coding method, the lossless coding method, or the DCT-based process with a final lossless coding. All frames within the image must use the same entropy coding, either Huffman or arithmetic, with the exception that non-differential frame coded with the baseline coding may occur in the same image with frames coded with arithmetic coding methods. The differential frames are coded with the same method used for the non-differential frame except the final frame. The final differential frame for each image may use differential lossless coding method. In the hierarchical coding mode, the resolution changes of frames may occur. These resolution changes occur if down-sampling filters are used to reduce the spatial resolution of some or all frames of an image. When the resolution of a reference frame does not match the resolution of the frame to be coded, an up-sampling filter is used to increase the resolution of reference frame. The block diagram of coding a differential frame is shown in [Figure 8.9](#).

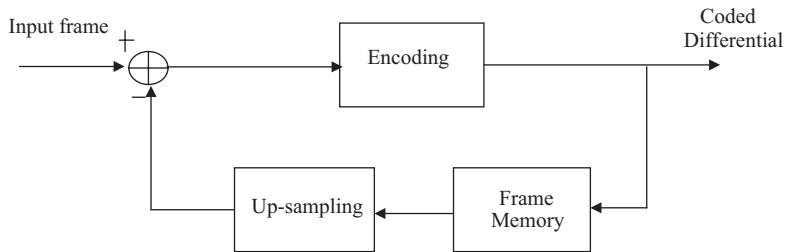


FIGURE 8.9
Coding of differential frame in hierarchical coding.

The up-sampling filter increases the spatial resolution by a factor of two in both horizontal and vertical directions by using bi-linear interpolation of two neighboring pixels. The up-sampling with bi-linear interpolation is consistent with the down-sampling filter that is used for the generation of down-sampled frames. It should be noted that the hierarchical coding mode allows one to improve the quality of the reconstructed frames at a given spatial resolution.

8.6 Summary

In this chapter, the still image coding standard, JPEG, has been introduced. The JPEG coding standard includes four coding modes, sequential DCT-based coding mode, progressive DCT-based coding mode, lossless coding mode, and hierarchical coding mode. The DCT-based coding method is probably the one that most are familiar with; however, the lossless coding modes in JPEG that use a spatial domain predictive coding process have many interesting applications as well. For each coding mode, the entropy coding can be implemented with either Huffman coding or arithmetic coding. JPEG has been widely adopted for many applications.

Exercises

- 8.1 What is the difference between sequential coding and progressive coding in JPEG? Conduct a project to encode an image with sequence coding and progressive coding, respectively.
- 8.2 Use JPEG lossless mode to code several images and explain why different bit rates are obtained.
- 8.3 Generate a Huffman code table using a set of images with eight-bit precision (approx. 2 ~ 3) using the method presented in Annex C of the JPEG specification. This set of images is called the training set. Use this table to code an image within the training set and an image, which is not in the training set, and explain the results.

- 8.4 Design a three-layer progressive JPEG coder using (a) spectral selection and (b) progressive approximation (0.3 bit/pixel at the first layer, 0.2 bits/pixel at the second layer and 0.1 bits/pixel at the third layer).
- 8.5 B1 image (255:262, 255:262)



B1 pixel value:

| | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|
| 144 | 163 | 194 | 210 | 195 | 151 | 136 | 191 |
| 170 | 194 | 209 | 200 | 162 | 136 | 178 | 226 |
| 185 | 200 | 205 | 183 | 152 | 159 | 207 | 218 |
| 186 | 201 | 188 | 167 | 172 | 197 | 200 | 176 |
| 204 | 194 | 166 | 171 | 203 | 199 | 162 | 167 |
| 208 | 167 | 163 | 203 | 212 | 164 | 155 | 215 |
| 180 | 148 | 186 | 219 | 181 | 141 | 191 | 234 |
| 141 | 170 | 217 | 198 | 146 | 166 | 231 | 194 |

References

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- Pennebaker, W. B. and J. L. Mitchell, *JPEG: Still Image Data Compression Standard*, New York: Van Nostrand Reinhold, 1992.
- Symes, P. *Video Compression: Fundamental Compression Techniques and an Overview of the JPEG and MPEG Compression Systems*, New York: McGraw-Hill, 1998.



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9

Wavelet Transform for Image Coding: JPEG2000

Since the middle of the 1980s, a number of signal processing applications have emerged using wavelet theory. Among those applications, the most widespread developments have occurred in the area of data compression. Wavelet techniques have demonstrated the ability to provide not only high coding efficiency, but also spatial and quality scalability features. In this chapter, we focus on the utility of the wavelet transform for image data compression applications.

We first introduce wavelet transform theory by starting with the short-time Fourier transform (STFT). Discrete wavelet transform (DWT) is then presented. Finally, the lifting scheme, known as the second-generation wavelet transform, is described.

We then discuss the basic concept of image wavelet transform coding with an emphasis on embedded image wavelet transform coding algorithms, which is the base of JPEG2000.

Finally, JPEG2000, the newest still image coding standard, is described in this chapter with emphasis on its functionality and current status.

9.1 A Review of Wavelet Transform

9.1.1 Definition and Comparison with Short-Time Fourier Transform

The wavelet transform, as a specialized research field, started over more than two decades ago (Grossman and Morlet 1984). It is known that the wavelet transform is rather different from the Fourier transform. The former is suitable for studying transitional property of signals, while the latter is not suitable for studying signals in the time-frequency space. The so-called STFT was designed to overcome the drawback of the Fourier transform. To better understand the theory of wavelets, we first give a very short review of the STFT since there are some similarities between the STFT and the wavelet transform. As we know, the STFT uses sinusoidal waves as its orthogonal basis and is defined as:

$$F(\omega, \tau) = \int_{-\infty}^{+\infty} f(t)w(t-\tau)e^{-j\omega t}dt \quad (9.1)$$

where $w(t)$ is a time-domain windowing function, the simplest of which is a rectangular window that has a unit value over a time interval and has zero elsewhere. The value τ is the starting position of the window. Thus, the STFT maps a function $f(t)$ into a two-dimensional plane (ω, τ) , where ω stands for frequency and τ for time moment. The STFT is also referred to as Gabor transform (Cohen 1989). Similar to the STFT, the wavelet transform also maps a time or spatial function into a two-dimensional function of a and τ ,

where a denotes dilation and τ for translation in time. The wavelet transform is defined as follows. Let $f(t)$ be any square integral function, i.e., it satisfies:

$$\int_{-\infty}^{+\infty} |f(t)|^2 dt < \infty \quad (9.2)$$

The continuous-time wavelet transform of $f(t)$ with respect to a wavelet $\psi(t)$ is defined as:

$$W(a, \tau) = \int_{-\infty}^{+\infty} f(t) \frac{1}{\sqrt{|a|}} \psi^* \left(\frac{t-\tau}{a} \right) dt \quad (9.3)$$

where a and τ are real variables and $*$ denotes complex conjugation. The wavelet, denoted by $\psi_{a\tau}(t)$, is expressed as:

$$\psi_{a\tau}(t) = |a|^{-1/2} \psi \left(\frac{t-\tau}{a} \right) \quad (9.4)$$

Equation 9.4 represents a set of functions that are generated from a single function, $\psi(t)$, by dilations and translations. The variable τ represents the time shift and the variable a corresponds to the amount of time scaling or dilation. If $a > 1$, there is an expansion of $\psi(t)$, while if $0 < a < 1$, there is a contraction of $\psi(t)$. For negative values of a , the wavelet experiences a time reversal in combination with a dilation. The function, $\psi(t)$, is referred to as the *mother* wavelet and it must satisfy two conditions:

The function integrates to zero:

$$\int_{-\infty}^{+\infty} \psi(t) dt = 0 \quad (9.5)$$

The function is square integral, or has finite energy:

$$\int_{-\infty}^{+\infty} \psi(t)^2 dt < \infty \quad (9.6)$$

The continuous-time wavelet transform can now be rewritten as:

$$W(a, \tau) = \int_{-\infty}^{+\infty} f(t) \psi_{a\tau}^*(t) dt \quad (9.7)$$

In the following, we give two well-known examples of $\psi(t)$ and their Fourier transform. The first example is the Morlet (Modulated Gaussian) wavelet (Daubechies 1992),

$$\begin{aligned} \psi(t) &= e^{-\frac{1}{2}t^2} e^{j\omega_0 t} \\ \Psi(\omega) &= \sqrt{2\pi} e^{-\frac{(\omega-\omega_0)^2}{2}} \end{aligned} \quad (9.8)$$

and the second example is the Haar wavelet:

$$\psi(t) = \begin{cases} 1 & 0 \leq t \leq 1/2 \\ -1 & 1/2 \leq t \leq 1 \\ 0 & otherwise \end{cases} \quad (9.9)$$

$$\Psi(\omega) = j e^{-j\frac{\omega}{2}} \frac{\sin^2(\omega/4)}{\omega/4}$$

From these definitions and examples, we can find that the wavelets have zero DC value. This is clear from Equation 9.5. In order to have good time localization, the wavelets are usually bandpass signals and they decay rapidly towards zero with time. We can also find several other important properties of the wavelet transform and several differences between the STFT and the wavelet transform.

The STFT uses a sinusoidal wave as its basis function. These basis functions keep the same frequency over the entire time interval. In contrast, the wavelet transform uses a particular wavelet as its basis function. Hence, wavelets vary in both position and frequency over the time interval. Examples of two basis functions for the sinusoidal wave and wavelet are shown in Figure 9.1a and b, respectively, where the vertical axes stand for magnitude and the horizontal axes for time.

The STFT uses a single analysis window. In contrast, the wavelet transform uses a short time window at high frequencies and a long time window at low frequencies. This is referred to as constant Q-factor filtering or relative constant bandwidth frequency analysis. A comparison of constant bandwidth analysis of the STFT and relative-constant bandwidth wavelet transform is shown in Figure 9.2a and b, respectively.

This feature can be further explained with the concept of a time-frequency plane, which is shown in Figure 9.3. It is known from the Heisenberg inequality (Rioul 1991) that the product of time resolution and frequency resolution has been lower bounded as follows.

$$\Delta t \cdot \Delta f \geq 1/(4\pi)$$

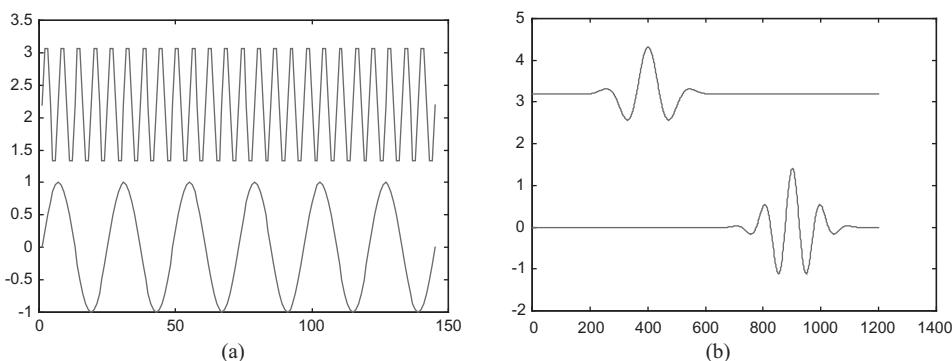
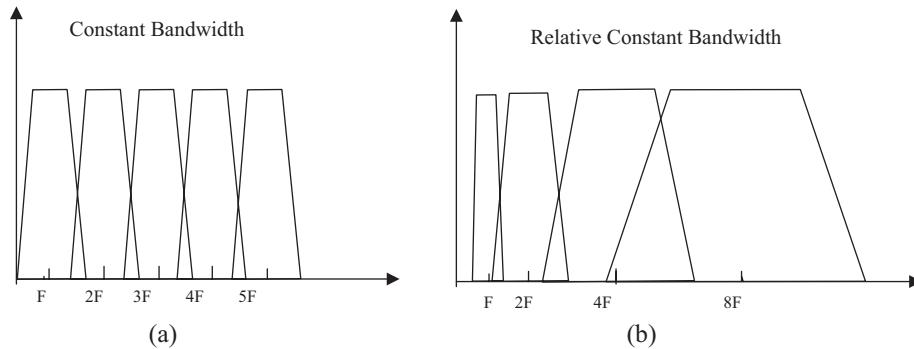
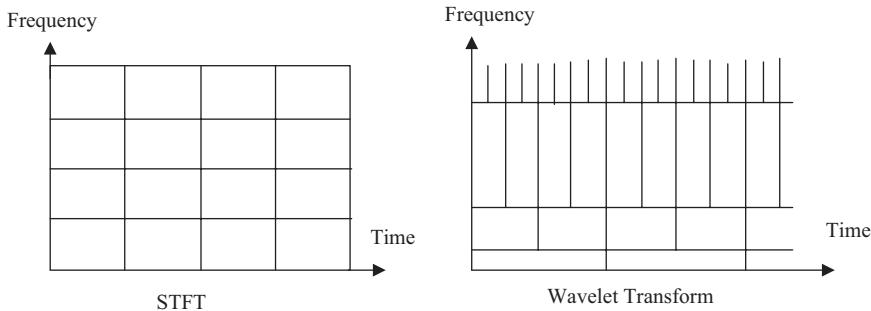


FIGURE 9.1

Wave versus wavelet: (a) Two sinusoidal waves and (b) two wavelets, where vertical axes stand for magnitude and horizontal axes for time. (Castleman, K.R., *Digital Image Processing*, Prentice Hall, Upper Saddle River, NJ, 1996.)

**FIGURE 9.2**

(a) Constant bandwidth analysis (for Fourier transform) and (b) relative constant bandwidth analysis (for Wavelet transform). (From Rioul, O. and Vetterli, M., *IEEE Signal Process. Mag.*, 8, 14–38, 1991.)

**FIGURE 9.3**

Comparison of the STFT and the wavelet transform in the time-frequency plane. (From Rioul, O. and Vetterli, M., *IEEE Signal Process. Mag.*, 8, 14–38, 1991.)

That is, these two resolutions cannot be arbitrarily small. As shown in Figure 9.3, the window size of the STFT in the time domain is always chosen to be constant. The corresponding frequency bandwidth is also constant. In the wavelet transform, the window size in time domain varies with the frequency. A longer time window is used for lower frequency and shorter time window is used for higher frequency. This property is very important for image data compression. For image data, the concept of time-frequency plane becomes spatial-frequency plane. The spatial resolution of a digital image is measured with pixels, as described in Chapter 15. To overcome the limitations of DCT-based coding, the wavelet transform allows the spatial resolution and frequency bandwidth to vary in the spatial-frequency plane. With this variation, better bit allocation for active and smooth areas can be achieved.

The continuous-time wavelet transform can be considered as a correlation. For fixed a , it is clear from Equation 9.3 that $W(a, \tau)$ is the cross-correlation of functions $f(t)$ with related wavelet conjugate dilated to scale factor a at time lag τ . This is an important property of the wavelet transform for multi-resolution analysis (MRA) of image data. Since the convolution can be seen as a filtering operation, the integral wavelet transform can be seen as a bank of linear filters acting upon $f(t)$. This implies that the image data can be decomposed by a bank of filters defined by the wavelet transform.

The continuous-time wavelet transform can be seen as an operator. First, it has the property of linearity. If we rewrite $W(a, \tau)$ as $W_{a\tau}[f(t)]$, then we have

$$W_{a\tau}[\alpha f(t) + \beta g(t)] = \alpha W_{a\tau}[f(t)] + \beta W_{a\tau}[g(t)] \quad (9.10)$$

where α and β are constant scalars. Second, it has the property of translation

$$W_{a\tau}[f(t - \lambda)] = W(a, \tau - \lambda) \quad (9.11)$$

where λ is a time lag.

Finally, it has the property of scaling

$$W_{a\tau}[f(t/\alpha)] = W(a/\alpha, \tau/\alpha) \quad (9.12)$$

9.1.2 Discrete Wavelet Transform

In the continuous-time wavelet transform, the function $f(t)$ is transformed to a function $W(a, \tau)$ using the wavelet $\psi(t)$ as a basis function. Recall that the two variables a and τ are the dilation and translation, respectively. Now let us find a means of obtaining the inverse transform, i.e., given $W(a, \tau)$, find $f(t)$. If we know how to get the inverse transform, we can then represent any arbitrary function $f(t)$ as a summation of wavelets such as in the Fourier transform and discrete cosine transform (DCT) that provide a set of coefficients for reconstructing the original function using sine and cosine as the basis functions. In fact, this is possible if the mother wavelet satisfies the admissibility condition:

$$C = \int_{-\infty}^{+\infty} \frac{|\Psi(\omega)|^2}{|\omega|} d\omega \quad (9.13)$$

where C is a finite constant and $\Psi(\omega)$ is the Fourier transform of the mother wavelet function $\psi(t)$. Then, the inverse wavelet transform is:

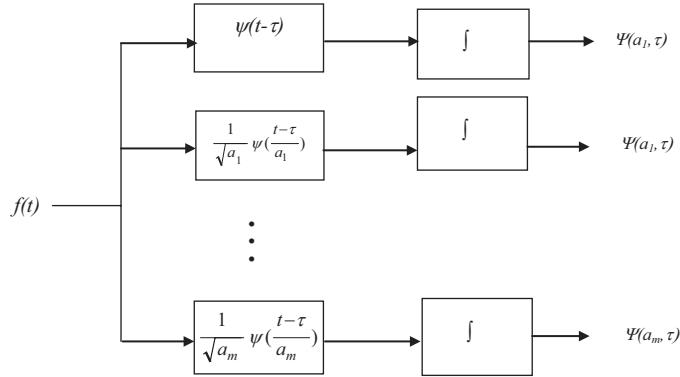
$$f(t) = \frac{1}{C} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \frac{1}{|a|^2} W(a, \tau) \psi_{a\tau}(t) da d\tau \quad (9.14)$$

The above results can be extended for two-dimensional signals. If $f(x, y)$ is a two-dimensional function, its continuous-time wavelet transform is defined as:

$$W(a, \tau_x, \tau_y) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} f(x, y) \psi_{a\tau_x\tau_y}^*(x, y) dx dy \quad (9.15)$$

where τ_x and τ_y specify the transform in two dimensions. The inverse two-dimensional continuous-time wavelet transform is then defined as:

$$f(x, y) = \frac{1}{C} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \frac{1}{|a|^3} W(a, \tau_x, \tau_y) \psi_{a\tau_x\tau_y}(x, y) da d\tau_x d\tau_y \quad (9.16)$$

**FIGURE 9.4**

The wavelet transform implemented with a bank of filters.

where the C is defined as in (9.13) and $\psi(x, y)$ is a two-dimensional wavelet

$$\psi_{at_x t_y}(x, y) = \frac{1}{|a|} \psi\left(\frac{x - \tau_x}{a}, \frac{y - \tau_y}{a}\right) \quad (9.17)$$

For image coding, the wavelet transform is used to decompose the image data into wavelets. As indicated in the third property of the wavelet transform, the wavelet transform can be viewed as the cross-correlation of the function $f(t)$ and the wavelets $\psi_{at}(t)$. Therefore, the wavelet transform is equivalent to finding the output of a bank of bandpass filters specified by the wavelets of $\psi_{at}(t)$ as shown in Figure 9.4. This process decomposes the input signal into several sub-bands. Since each sub-band can be further partitioned, the filter bank implementation of the wavelet transform can be used for MRA. Intuitively, when the analysis is viewed as a filter bank, the time resolution must increase with the central frequency of the analysis filters. This can be exactly obtained by the scaling property of the wavelet transform, where the center frequencies of the bandpass filters increase as the bandwidth become wider. Again, the bandwidth becomes wider by reducing the dilation parameter a . It should be noted that such an MRA is consistent with the constant Q-factor property of the wavelet transform. Furthermore, the resolution limitation of the STFT does not exist in the wavelet transform since the time-frequency resolutions in the wavelet transform vary, as shown in Figure 9.2b.

For digital image compression, it is preferred to represent $f(t)$ as a discrete superposition sum rather than an integral. With this move to the discrete space, the dilation parameter a in Equation 9.10 takes the values $a = 2^k$ and the translation parameter τ takes the values $\tau = 2^k l$, where both k and l are integers. From Equation 9.4, the discrete version of $\psi_{at}(t)$ becomes:

$$\psi_{kl}(t) = 2^{-\frac{k}{2}} \psi(2^{-k} t - l) \quad (9.18)$$

Its corresponding wavelet transform can be rewritten as:

$$W(k, l) = \int_{-\infty}^{+\infty} f(t) \psi_{kl}^*(t) dt \quad (9.19)$$

and the inverse transform becomes:

$$f(t) = \sum_{k=-\infty}^{+\infty} \sum_{l=-\infty}^{+\infty} d(k, l) 2^{-\frac{k}{2}} \psi(2^{-k} t - l) \quad (9.20)$$

The values of the wavelet transform at those a and τ are represented by $d(k, l)$:

$$d(k, l) = W(k, l)/C \quad (9.21)$$

The $d(k, l)$ coefficients are referred to as the DWT of the function $f(t)$ (Daubechies 1992, Vetterli and Kovacevic 1995). It is noted that the discretization so far is only applied to the parameters a and τ , $d(k, l)$ is still a continuous-time function. If the discretization is further applied to the time domain by letting $t = mT$, where m is an integer and T is the sampling interval (without loss of generality, we assume $T = 1$), then the discrete-time wavelet transform is defined as:

$$W_a(k, l) = \sum_{m=-\infty}^{+\infty} f(m) \psi_{kl}^*(m) \quad (9.22)$$

Of course, the sampling interval has to be chosen according to the Nyquist sampling theorem so that no information has been lost in the process of sampling. The inverse discrete-time wavelet transform is then

$$f(m) = \sum_{k=-\infty}^{+\infty} \sum_{l=-\infty}^{+\infty} d(k, l) 2^{-\frac{k}{2}} \psi(2^{-k} m - l) \quad (9.23)$$

9.1.3 Lifting Scheme

An alternative implementation of the DWT has been proposed recently, known as the *lifting scheme* (Sweldens 1995, Daubechies and Sweldens 1998). The implementation of the lifting scheme is very efficient and similar to the fast Fourier transform (FFT) implementation for Fourier transform. In this subsection, we will first introduce how the lifting scheme works. Then, we will comment on its features, merits, and application in JPEG2000.

9.1.3.1 Three Steps in Forward Wavelet Transform

Similar to the DWT, the lifting scheme is conducted from one resolution level to the next lower resolution level iteratively. To facilitate representation, let us consider here only the case of one-dimensional (1-D) data sequence. Two-dimensional data extension should be understandable straightforwardly afterwards. One iteration of lifting scheme is described as follows. Denote the 1-D data sequence by X_i , and $X_i = \{x_j\}$. After the iteration of lifting scheme, the date sequence X_i becomes two data sequences X_{i+1} and Y_{i+1} , say, the former is the low-pass component and the latter is the high-pass component. The lifting scheme iterative consists of the following three steps.

Splitting (often referred to as **lazy wavelet transform**):

The data sequence X_i is split into two parts: X_{i+1} and Y_{i+1} .

Prediction (often referred to as **dual lifting**):

In this step, the data sequence Y_{i+1} is predicted with the data sequence X_{i+1} , and then Y_{i+1} is replaced by the prediction error.

$$Y_{i+1} \leftarrow Y_{i+1} - P(X_{i+1})$$

Updated (often referred to as **primary lifting**):

In this step, the data sequence X_{i+1} is updated with the data sequence Y_{i+1} , and then X_{i+1} is replaced as follows.

After this iteration, a new iteration will apply the same three steps to X_{i+1} generate X_{i+2} and Y_{i+2} .

$$X_{i+1} \leftarrow X_{i+1} + U(Y_{i+1})$$

It is observed that the 1-D DWT via lifting scheme is now very simple and efficient if the prediction and update operators are simple. In the example that follows, we can see this is the case.

9.1.3.2 Inverse Transform

The inverse wavelet transform via lifting scheme is exactly the reverse process of the above forward transform in the sense that plus and minus are reverses, splitting and merging are reversed, and the order of the three steps is reversed. The corresponding three steps in inverse transform are shown below.

Inverse update

$$X_{i+1} \leftarrow X_{i+1} - U(Y_{i+1})$$

Inverse prediction

$$Y_{i+1} \leftarrow Y_{i+1} + P(X_{i+1})$$

Merging

The data sequence X_i is formed by union of X_{i+1} and Y_{i+1} .

9.1.3.3 Lifting Version of CDF (2,2)

In this subsection, a specific lifting scheme is introduced, which essentially implements the well-known CDF(2,2) wavelet transform, named after its three inventors: Cohen, Daubechies, and Feauveau.

The dataset $X_i = \{x_j\}$ is split into two parts: even data samples and odd data samples. This is similar to the FFT technique.

That is,

$$s_j \leftarrow x_{2j}$$

$$d_j \leftarrow x_{2j+1}$$

Note that we use the notations $\{s_j\}$ and $\{d_j\}$ to denote the even and odd data sequence of $\{x_j\}$ in order to avoid confusion in notation of subscripts.

Prediction:

Predict the odd data samples with the even data samples as follows.

$$d_j \leftarrow d_j - \frac{1}{2}(s_j + s_{j+1})$$

Update:

Update the even data samples with the odd data samples to preserve the mean of data samples.

$$s_j \leftarrow s_j + \frac{1}{4}(d_{j-1} + d_j)$$

It is observed that both prediction and update are linear in this example.

9.1.3.4 A Numerical Example

Here, we present a simple numerical example for illustration purpose. In this example, we only consider a four-point data sequence, i.e.,

$$X_i = \{1, 2, 3, 4\}$$

After splitting, we have

$$\{s_j\} = \{2, 4\} \quad \text{and} \quad \{d_j\} = \{1, 3\}$$

After prediction, we have

$$d_1 = d_1 - \frac{1}{2}(s_1 + s_2) = -2 \quad \text{and} \quad d_2 = d_2 - \frac{1}{2}(s_2 + s_3) = 1$$

Note that we do not have s_3 and hence treat $s_3 = 0$.

After update, we have

$$s_1 = s_1 + \frac{1}{4}(d_0 + d_1) = 1.5 \quad \text{and} \quad s_2 = s_2 + \frac{1}{4}(d_1 + d_2) = 3.75$$

Note that we do not have d_0 and hence treat $d_0 = 0$. Hence, after CDF (2,2) via lifting scheme we have $X_{i+1} = \{1.5, 3.75\}$ and $Y_{i+1} = \{-2, 1\}$. The former is the low-pass frequency part of the data sequence $X_i = \{1, 2, 3, 4\}$, and the latter is its high-pass frequency part of X_i .

For inverse transform, after inverse update, we have

$$s_1 = s_1 - \frac{1}{4}(d_0 + d_1) = 2 \quad \text{and} \quad s_2 = s_2 - \frac{1}{4}(d_1 + d_2) = 4$$

After inverse prediction, we have

$$d_1 = d_1 + \frac{1}{2}(s_1 + s_2) = 1 \quad \text{and} \quad d_2 = d_2 + \frac{1}{2}(s_2 + s_3) = 3$$

Hence, inverse transform via lifting scheme produce the original sequence $X_i = \{1, 2, 3, 4\}$.

9.1.3.5 (5,3) Integer Wavelet Transform

An additional advantage that lifting scheme possesses has something to do with integer wavelet transform (IWT). That is, both the forward IWT and the inverse IWT can easily be conducted. Here, we present the integer version of CDF (2,2), which is referred to as (5,3) IWT, in this subsection. Note that the (5,3) IWT transform is adopted in JPEG2000 (Rabbani 2001).

Forward (5,3) IWT

Splitting: $s_j \leftarrow x_{2j}$ and $d_j \leftarrow x_{2j+1}$

Dual lifting (Prediction):

$$d_j \leftarrow d_j - \left[\frac{1}{2}(s_j + s_{j+1}) + \frac{1}{2} \right]$$

Primary lifting (Update):

$$s_j \leftarrow s_j + \left[\frac{1}{4}(d_{j-1} + d_j) + \frac{1}{2} \right]$$

where the notation $[z]$ indicates the largest integer not larger than z .

Inverse (5,3) IWT

Inverse primary lifting:

$$s_j \leftarrow s_j - \left[\frac{1}{4}(d_{j-1} + d_j) + \frac{1}{2} \right]$$

Inverse dual lifting:

$$d_j \leftarrow d_j + \left[\frac{1}{2}(s_j + s_{j+1}) + \frac{1}{2} \right]$$

Merging:

$$x_{2j} \leftarrow s_j \quad \text{and} \quad x_{2j+1} \leftarrow d_j$$

9.1.3.6 A Demonstration Example of (5,3) IWT

Here we work on the same 1-D data sequence as used in the example shown in [Section 9.1.3.4](#). That is,

$$X_i = \{1, 2, 3, 4\}$$

After splitting, we have

$$\{s_j\} = \{2, 4\} \quad \text{and} \quad \{d_j\} = \{1, 3\}$$

After dual lifting, we have

$$d_1 = d_1 - \left[\frac{1}{2}(s_1 + s_2) + \frac{1}{2} \right] = -2 \quad \text{and} \quad d_2 = d_2 - \left[\frac{1}{2}(s_2 + s_3) + \frac{1}{2} \right] = 1$$

After primary lifting, we have

$$s_1 = s_1 + \left\lceil \frac{1}{4}(d_0 + d_1) + \frac{1}{2} \right\rceil = 2 \quad \text{and} \quad s_2 = s_2 + \left\lceil \frac{1}{4}(d_1 + d_2) + \frac{1}{2} \right\rceil = 4$$

Because we do not have s_3 and d_0 , we treat $s_3 = 0$ and $d_0 = 0$. We then see that after (5,3) IWT with lifting scheme we have $X_{i+1} = \{2, 4\}$ and $Y_{i+1} = \{-2, 1\}$. The former is the low-pass frequency part of the data sequence $X_i = \{1, 2, 3, 4\}$, and the latter is its high-pass frequency part of X_i . It is observed that both parts are integers.

Now we show that the inverse (5,3) IWT gives back exactly the same original data sequence $X_i = \{1, 2, 3, 4\}$ as follows.

For inverse transform, after inverse primary lifting, we have

$$s_1 = s_1 - \left\lceil \frac{1}{4}(d_0 + d_1) + \frac{1}{2} \right\rceil = 2 \quad \text{and} \quad s_2 = s_2 - \left\lceil \frac{1}{4}(d_1 + d_2) + \frac{1}{2} \right\rceil = 4$$

After inverse dual lifting, we have

$$d_1 = d_1 + \left\lceil \frac{1}{2}(s_1 + s_2) + \frac{1}{2} \right\rceil = 1 \quad \text{and} \quad d_2 = d_2 + \left\lceil \frac{1}{2}(s_2 + s_3) + \frac{1}{2} \right\rceil = 3$$

After merging, we have $X_i = \{1, 2, 3, 4\}$.

9.1.3.7 Summary

In this section, we summarize the advantages possessed by lifting scheme. Because of these merits, lifting scheme has been adopted by JPEG2000 (Rabbani 2001).

1. Lifting scheme provides a different way to illustrate wavelet transform. It is noted that most of wavelet transform theory starts from Fourier transform theory. Lifting scheme, however, does provide one way to view wavelet transform without using Fourier transform.
2. Lifting scheme is simple and hence efficient in implementation.
3. In addition, lifting scheme can reduce memory requirement significantly. It can provide so-called in-place computation of wavelet coefficients. That is, it can overwrite the memory used to store input data with wavelet coefficients. This bears similarity to the FFT.
4. Lifting scheme lends itself easily to IWT computation.

9.2 Digital Wavelet Transform for Image Compression

9.2.1 Basic Concept of Image Wavelet Transform Coding

From the previous section, we have learned that the wavelet transform has several features that are different from traditional transforms. It is noted from [Figure 9.2](#) that each transform coefficient in the STFT represents a constant interval of time regardless of which

band the coefficient belongs to, whereas for the wavelet transform, the coefficients at the coarse level represent a larger time interval but a narrower band of frequencies. This feature of the wavelet transform is very important for image coding. In traditional image transform coding, which make use of the Fourier transform or DCT, one difficult problem is to choose the block size or window width so that statistics computed within that block provide good models of the image signal behavior. The choice of the block size has to be compromised so that it can handle both active and smooth areas. In the active areas, the image data is more localized in the spatial domain, while in the smooth areas, the image data is more localized in the frequency domain. With traditional transform coding, it is very hard to reach a good compromise. The main contribution of wavelet transform theory is that it provides an elegant framework in which both statistical behaviors of image data can be analyzed with equal importance. This is because wavelets can provide a signal representation in which some of the coefficients represent long data lags corresponding to a narrow band or low-frequency range, and some of the coefficients represent short data lags corresponding to a wideband or high-frequency range. Therefore, it is possible to obtain a good trade-off between spatial and frequency domain with the wavelet representation of image data.

To use the wavelet transform for image coding applications, an encoding process is needed, which includes three major steps: image data decomposition, quantization of the transformed coefficients, and coding of the quantized transformed coefficients. A simplified block diagram of this process is shown in [Figure 9.5](#). The image decomposition is usually a lossless process, which converts the image data from the spatial domain to frequency domain, where the transformed coefficients are decorrelated. The information loss happens in the quantization step and the compression is achieved in the coding step. To begin the decomposition, the image data is first partitioned into four subbands labeled as LL_1 , HL_1 , LH_1 , and HH_1 , as shown in [Figure 9.6a](#). Each coefficient represents a spatial area corresponding to the one-quarter of the original image size. The low frequencies represent a bandwidth corresponding to $0 < |\omega| < \pi/2$, while the high frequencies represent the band $\pi/2 < |\omega| < \pi$. To obtain the next level of decomposition, the LL_1 subband is further decomposed into the next level of four subbands, as shown in [Figure 9.6b](#). The low frequencies of the second-level decomposition correspond to $0 < |\omega| < \pi/4$, while the high frequencies at the second level correspond to $\pi/4 < |\omega| < \pi/2$. This decomposition can be continued to as many levels as needed. The filters used to compute the DWT are generally the symmetric quadrature mirror filters (QMF), which is described in Woods (1991). A QMF-pyramid subband decomposition is illustrated in [Figure 9.6b](#).

During quantization, each subband is quantized differently depending on its importance, which is usually based on its energy or variance (Jayant and Noll 1984). To reach the predetermined bit rate or compression ratio, the coarse quantizers or large quantization steps would be used to quantize the low-energy subbands while the finer

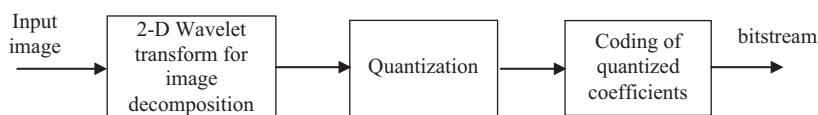
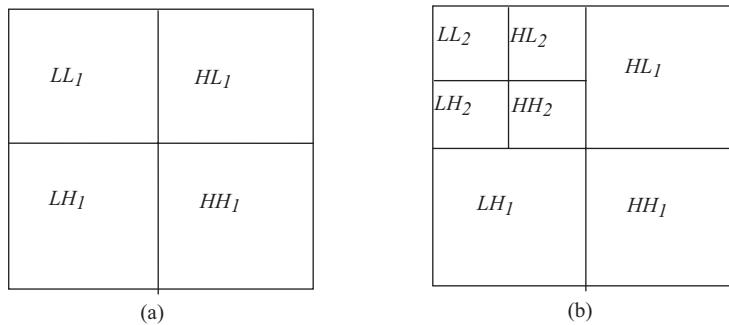


FIGURE 9.5

Block diagram of the image coding with the wavelet transform coding.

**FIGURE 9.6**

Two-dimensional wavelet transform, (a) first level decomposition and (b) second level decomposition (L denotes low band, H denotes high band, and the subscript denotes number of level, for example LL_1 denotes the LL band at level 1).

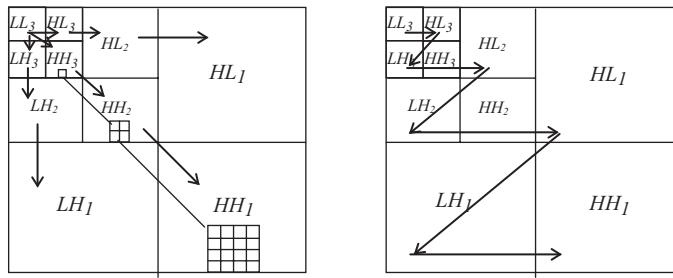
quantizers or small quantization steps would be used to quantize the large-energy subbands. This results in fewer bits allocated to those low-energy subbands and more bits for large-energy subbands.

9.2.2 Embedded Image Wavelet Transform Coding Algorithms

In this section, the wavelet transform-based image coding methods that form the basic framework of JPEG2000 are discussed. We first comment on the drawbacks of early wavelet transform-based image coding methods. Then, we introduce the concept of modern wavelet transform-based image coding methods, i.e., embedded image wavelet transform coding algorithm, in particular, the embedded image coding using zero trees of wavelet coefficients (embedded zerotree wavelet, EZW).

9.2.2.1 Early Wavelet Image Coding Algorithms and Their Drawbacks

As with other transform coding schemes, most wavelet coefficients in the high-frequency bands have very low energy. After quantization, many of these high-frequency wavelet coefficients are quantized to zero. Based on the statistical property of the quantized wavelet coefficients, Huffman coding tables can be designed. Generally, most of the energy in an image is contained in the low-frequency bands. The data structure of the wavelet-transformed coefficients is suitable to exploit this statistical property. Consider a multi-level decomposition of an image with the DWT, where the lowest levels of decomposition would correspond to the highest-frequency subbands and the finest spatial resolution and the highest level of decomposition would correspond to the lowest-frequency subband and the coarsest spatial resolution. Arranging the subbands from lowest to highest frequency, we expect a decrease in energy. Also, we expect that if the wavelet-transformed coefficients at a particular level have lower energy, then coefficients at the lower levels or high-frequency subbands, which correspond to the same spatial location, would have smaller energy. Another feature of the wavelet coefficient data structure is spatial self-similarity across subbands, which is shown in Figure 9.7. The early wavelet image coding methods (Antonini et al. 1992, Vetterli 1984, Woods 1986) utilizing the above features of wavelet transform are referred to as early or conventional wavelet image coding methods.

**FIGURE 9.7**

(a) Parent-children dependencies of subbands, the arrow points from the subband of the parents to the subband of children. The top left is the lowest-frequency band and (b) The scanning order of the subbands for encoding a significance map. (From Shapiro, J., *IEEE Trans. Signal Process.*, 3445–3462, 1993.)

The drawbacks of these conventional wavelet image coding methods are discussed in Usevitch (2001):

- Quantizer can only be optimal as coding rate larger than 1 bit per pixel (bpp)
- Optimal bit allocation changes as overall bit rate changes, requiring coding process repeated entirely for each new target bit rate desired
- Difficult to code an input to give an exact target bit rate (or predefined output size)

9.2.2.2 Modern Wavelet Image Coding

Embedded image coding is the basic concept of modern wavelet image coding algorithm. By embedding code, it means that the code arranges its bits in the order of their importance. In other words, the bits corresponding to a lower bit rate coding will be arranged in the beginning portion of the embedded code. Because the embedded codes have all lower-rate codes arranged at the beginning portion of the bit stream, the embedded codes can be truncated to fit a targeted bit rate by simply truncating the bit stream accordingly. Embedded wavelet image coding began with the EZW algorithm by Shapiro in the early 1990s (Shapiro 1993). This revolutionary breakthrough marks the beginning of the modern wavelet image-coding age. The typical algorithms including the EZW, set partitioning in hierarchical trees (SPIHT) by Said and Pearlman (1996), and embedded block coding with optimized truncation of the embedded bit streams (EBCOT) (Taubman 2000). Consequently, the modern wavelet coding has been adopted by JPEG2000 for still image coding. A given image can be coded once and it can then be truncated easily and optimally according to any given bit rate.

Several algorithms have been developed to exploit this and the previously mentioned properties for image coding. Among them, one of the first was EZW, proposed by Shapiro (1993). Another algorithm is the so-called SPIHT developed by Said and Pearlman (1996). This algorithm also produces an embedded bitstream. The advantage of the embedded coding schemes allows an encoding process to terminate at any point so that a target bit rate or distortion metric can be met exactly. Intuitively, for a given bit rate or distortion requirement, a non-embedded code should be more efficient than an embedded code since it has no constraints imposed by embedding requirements. However, embedded wavelet transform coding algorithms are the best currently. The additional constraints do

not seem to have a deleterious effect. In the following, we introduce the two embedded coding algorithms—the zerotree coding and the SPIHT coding—with an emphasis on the former.

9.2.2.3 Embedded Zerotree Wavelet Coding

As with DCT-based coding, an important aspect of wavelet-based coding is to code the positions of those coefficients that will be transmitted as nonzero values. After quantization, the probability of the zero symbol must be extremely high for the very low bit rate case. It is well-known that the most of energy of an image is contained in the low-low (LL) subband at the highest scale level and the distribution of wavelet coefficients of high-frequency subbands follows a generalized Laplacian density. That is, it has a high peak around zero and long tail towards two sides, which means a large number of coefficients having zero and small magnitude and yet still some small number of coefficients with large magnitudes. The statistics just mentioned imply that a large portion of the bit budget will then be spent on encoding the significance map, or the binary decision map that indicates whether a transformed coefficient has a zero or non-zero quantized value. Therefore, the ability to efficiently encode the significance map becomes a key issue for coding images at very low bit rates. A new data structure, the zerotree, has been proposed for this purpose (Shapiro 1993). To describe zerotree, we first must define insignificance. A wavelet coefficient is insignificant with respect to a given threshold value if the absolute value of this coefficient is smaller than this threshold. From the nature of the wavelet transform we can assume that every wavelet transform coefficient at a given scale can be strongly related to a set of coefficients at the next finer scale of similar orientation. More specifically, we can further assume that if a wavelet coefficient at a coarse scale is insignificant with respect to the preset threshold, then all wavelet coefficients at finer scales are likely to be insignificant with respect to this threshold. Therefore, we can build a tree with these parent-child relationships, such that coefficients at a coarse scale are called parents, and all coefficients corresponding to the same spatial location at the next finer scale of similar orientation are called children. Furthermore, for a parent, the set of all coefficients at all finer scales of similar orientation corresponding to the same spatial location are called descendants. For a QMF-pyramid decomposition the parent-children dependencies are shown in [Figure 9.7a](#). For a multi-scale wavelet transform, the scan of the coefficients begins at the lowest-frequency subband and then takes the order of LL, HL, LH, and HH from the coarser scale to the next finer scale as shown in [Figure 9.7b](#).

The zerotree is defined such that if a coefficient itself and all of its descendants are insignificant with respect to a threshold, then this coefficient is considered as an element of a zerotree. An element of a zerotree is considered as a zerotree root if this element is not the descendant of a previous zerotree root with respect to the same threshold value. The significance map can then be efficiently represented by a string with three symbols: zerotree root, isolated zero, and significant. The isolated zero means that the coefficient is insignificant, but it has some significant descendant. At the finest scale, only two symbols are needed since all coefficients have no children, so the symbol for zerotree root is not used. The symbol string is then entropy-encoded. Zerotree coding efficiently reduces the cost for encoding the significance map by using self-similarity of the coefficients at different scales. Additionally, it is different from the traditional run-length coding that is used in DCT-based coding schemes. Each symbol in a zerotree is a single terminating symbol, which can be applied to all depth of the zerotree, similar to the end-of-block (EOB) symbol in the JPEG and MPEG video coding standards. The difference between the zerotree and EOB

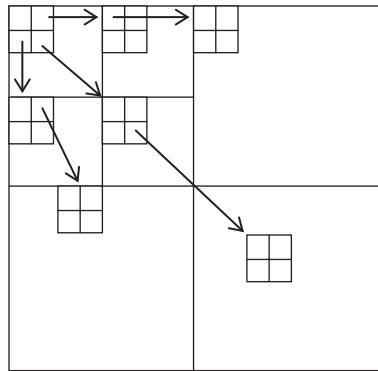
is that the zerotree represents the insignificance information at a given orientation across different scale layers. Therefore, the zerotree can efficiently exploit the self-similarity of the coefficients at the different scales corresponding to the same spatial location. The EOB only represents the insignificance information over the spatial area at the same scale. In summary, the zerotree-coding scheme tries to reduce the number of bits to encode the significance map, which is used to encode the insignificant coefficients. Therefore, more bits can be allocated to encode the important significant coefficients. It should be emphasized that this zerotree coding scheme of wavelet coefficients is an embedded coder, which means that an encoder can terminate the encoding at any point according to a given target bit rate or target distortion metric. Similarly, a decoder that receives this embedded stream can terminate at any point to reconstruct an image that has been scaled in quality.

In summary, the statistics of wavelet transform coefficients indicate that how to code coefficients' magnitude and position is a key issue in wavelet image coding. The EZW coding has proposed to code the positions of the zero coefficients using wavelet transform's self-similarity characteristics instead of coding positions of significant coefficients directly. This is referred to as significance map coding using zero-trees (Usevitch 2001). In addition to this key point, the EZW has developed a successive approximation quantization, which generates a large number of zero coefficients and leads to embedded coding (Usevitch 2001). In either Shapiro (1993) or Usevitch (2001), there is one example of 8×8 image with three-level wavelet transform. In the examples, step by step, the EZW coding scheme is implemented. Readers are encouraged to go through the examples to get first-hand experience about the EZW algorithm, to see how the two mentioned key techniques enhance the coding efficiency and how embedded coding is realized. At the end of this chapter, there is one problem in Exercises that is similar to these two examples.

9.2.2.4 Set Partitioning in Hierarchical Trees Coding

Another embedded wavelet coding method is the SPIHT-based algorithm (Said and Pearlman 1996). This algorithm includes two major core techniques: the set partitioning sorting algorithm and the spatial orientation tree. The set partitioning sorting algorithm is the algorithm that hierarchically divides coefficients into significant and insignificant from the most significant bit to the least significant bit by decreasing the threshold value at each hierarchical step for constructing a significance map. At each threshold value, the coding process consists of two passes—the sorting pass and the refinement pass—except for the first threshold that has only the sorting pass. Let $c(i, j)$ represent the wavelet transformed coefficients and m is an integer. The sorting pass involves selecting the coefficients such that $2^m \leq |c(i, j)| \leq 2^{m+1}$, with m being decreased at each pass. This process divides the coefficients into subsets and then tests each of these subsets for significant coefficients. The significance map constructed in the procedure is tree-encoded. The significant information is stored in three ordered lists: list of insignificant pixels (LIP), list of significant pixels (LSP), and list of insignificant sets (LIS). At the end of each sorting pass, the LSP contains the coordinates of all significant coefficients with respect to the threshold at that step. The entries in the LIS can be one of two types: type A represents all its descendants, and type B represents all its descendants from its grandchildren onward. The refinement pass involves transmitting the m -th most significant bit of all the coefficients with respect to the threshold, 2^{m+1} .

The idea of a spatial orientation tree is based on the following observation. Normally, among the transformed coefficients most of the energy is concentrated in the low frequencies. For the wavelet transform, when we move from the highest to the lowest levels of

**FIGURE 9.8**

Relationship between pixels in the spatial orientation tree.

the subband pyramid, the energy usually decreases. It is also observed that there exists strong spatial self-similarity between subbands in the same spatial location such as in the zerotree case. Therefore, a spatial orientation tree structure has been proposed for the SPIHT algorithm. The spatial orientation tree naturally defines the spatial relationship on the hierarchical pyramid as shown in [Figure 9.8](#).

During the coding, the wavelet-transformed coefficients are first organized into spatial orientation trees as in [Figure 9.8](#). In the spatial orientation tree, each pixel (i, j) from the former set of subbands is seen as a root for the pixels $(2i, 2j)$, $(2i+1, 2j)$, $(2i, 2j+1)$, and $(2i+1, 2j+1)$ in the subbands of the current scale. For a given n -level decomposition, this structure is used to link pixels of the adjacent subbands from level n until to level 1. In the highest-level n , the pixels in the low-pass subband are linked to the pixels in the three high-pass subbands at the same level. In the subsequent levels, all the pixels of a subband are involved in the tree-forming process. Each pixel is linked to the pixels of the adjacent subband at the next lower level. The tree stops at the lowest level.

The implementation of the SPIHT algorithm consists of four steps: initialization, sorting pass, refinement pass, and quantization scale update. In the initialization step, we find an integer $m = \lfloor \log_2(\max_{(i,j)}\{|c(i, j)|\}) \rfloor$. Here $\lfloor \cdot \rfloor$ represent an operation of obtaining the largest integer less than $|c(i, j)|$. The value of m is used for testing the significance of coefficients and constructing the significance map. The LIP is set as an empty list. The LIS is initialized to contain all the coefficients in the low-pass subbands that have descendants. These coefficients can be used as roots of spatial trees. All these coefficients are assigned to be of type A. The LIP is initialized to contain all the coefficients in the low-pass subbands.

In the sorting pass, each entry of the LIP is tested for significance with respect to the threshold value 2^m . The significance map is transmitted in the following way. If it is significant, a “1” is transmitted, a sign bit of the coefficient is transmitted, and the coefficient coordinates are moved to the LSP. Otherwise, a “0” is transmitted. Then, each entry of the LIS is tested for finding the significant descendants. If there are none, a “0” is transmitted. If the entry has at least one significant descendent, then a “1” is transmitted and each of the immediate descendants are tested for significance. The significance map for the immediate descendants is transmitted in such a way that if it is significant, a “1” plus a sign bit are transmitted and the coefficient coordinates are appended to the LSP. If it is not significant, a “0” is transmitted and the coefficient coordinates are appended to the LIP. If the coefficient has more descendants, then it is moved to the end of the LIS as an entry of

type B. If an entry in the LIS is of type B, then its descendants are tested for significance. If at least one of them is significant, then this entry is removed from the list, and its immediate descendants are appended to the end of the list of type A. For the refinement pass, the m -th most significant bit of the magnitude of each entry of the LSP is transmitted except those in the current sorting pass. For the quantization scale update step, m is decreased by 1 and the procedure is repeated from the sorting pass.

9.3 Wavelet Transform for JPEG-2000

9.3.1 Introduction of JPEG2000

Most image coding standards have exploited the DCT as their core technology for image decomposition for a while. However, this has been changing. The wavelet transform has been adopted by MPEG-4 for still image coding [mpeg4]. Also, JPEG-2000 has used the wavelet transform as its core technology for the next generation of the still image coding standard [jpeg2000 vm]. This is because the wavelet transform can provide not only excellent coding efficiency, but also good spatial and quality scalable functionality. JPEG-2000 is a new type of image compression system under development by Joint Photographic Experts Group for still image coding. This standard is intended to meet a need for image compression with great flexibility and efficient interchangeability. JPEG-2000 is also intended to offer unprecedented access into the image while still in compressed domain. Thus, images can be accessed, manipulated, edited, transmitted, and stored in a compressed form.

9.3.1.1 Requirements of JPEG-2000

As a new coding standard, the detailed requirements of JPEG-2000 include:

Low bit-rate compression performance: JPEG-2000 is required to offer excellent coding performance at bit-rates lower than 0.25 bit/pixel for highly detailed gray-level images since the current JPEG (10918-1) cannot provide satisfactory results at this range of bit-rates. This is the primary feature of JPEG-2000.

Lossless and lossy compression: it is desired to provide lossless compression naturally in the course of progressive decoding. This feature is especially important for medical image coding where the loss is not always allowed. Also, other applications such as high-quality image archival systems and network applications desire to have functionality of lossless reconstruction.

Large images: currently, the JPEG image compression algorithm does not allow for images greater than 64K by 64K without tiling.

Single decomposition architecture: the current JPEG standard has 44 modes, many of them for specific applications and not used by the majority of JPEG decoders. It is desired to have a single decomposition architecture that can encompass the interchange between applications.

Transmission in noisy environments: it is desirable to consider error robustness while designing the coding algorithm. This is important for the application of wireless communication. The current JPEG has provision for restart intervals, but image quality suffers dramatically when bit errors are encountered.

Computer-generated imagery: the current JPEG is optimized for natural imagery and does not perform well on computer-generated imagery or computer graphics.

Compound documents: the new coding standard is desired to be capable of compressing both continuous-tone and bi-level images. The coding scheme can compress and decompress images from 1-bit to 16-bit for each color component. The current JPEG standard does not work well for bi-level images.

Progressive transmission by pixel accuracy and resolution: progressive transmission that allows images to be transmitted with increasing pixel accuracy or spatial resolution is important for many applications. The image can be reconstructed with different resolutions and pixel accuracy as needed for different target devices such as in applications on the World Wide Web and image archiving.

Real-time encoding and decoding: for real-time applications, the coding scheme should be capable of compressing and decompressing with a single sequential pass. Of course, the optimal performance cannot be guaranteed in this case.

Fixed-rate, fixed-size, and limited workspace memory: the requirement of fixed bit rate allows decoder to run in real-time through channels with limited bandwidth. The limited memory space is required by the hardware implementation of decoding.

There are also some other requirements such as backwards compatibility with JPEG, open architecture for optimizing the system for different image types and applications, interface with MPEG-4, and so on. All these requirements have been seriously considered during the development of JPEG-2000. It is no doubt that the basic requirements on the coding performance at very low bit rate for still image coding have been achieved by using the wavelet-based coding as the core technology instead of DCT-based coding as used in JPEG.

9.3.1.2 Parts of JPEG-2000

JPEG-2000 consists of several parts. Some parts have become International Standards (IS), while some are still in the development stage. We first present in this subsection some completed parts and then introduce some parts that are still in their evolution stages.

Part 1 of JPEG-2000 is entitled JPEG-2000 Image Coding System: Core Coding System. This is the counterpart of the JPEG baseline system and was issued as an IS in December 2000. It is royalty-free.

Part 2 is entitled JPEG-2000 Image Coding Systems: Extension. It involves more advanced technologies and higher computational complexity and provides enhanced performance, compared with those in Part 1.

Part 3 is Motion JPEG-2000 (MJP2). It encodes motion pictures frame by frame using JPEG-2000 technologies. As a result, it offers random access to any frame in the motion pictures and is much less complicated than MPEG coding schemes. It has been adopted by Hollywood as a format for digital cinema. It is also used for digital cameras.

Part 4 is Conformance Testing.

Part 5 is about Reference Software for Part 1. Two available implementations are as follows (Rabbani 2001). One is a C implementation by the Image Power and

University of British Columbia (Adams 2000) the other is a Java implementation by the JJ2000 group JJ2000.

Part 6 is Compound Image File Format for document scanning and fax applications (Rabbani 2001).

While these six parts became ISs before 2004, some parts are still in the working stage. For instance, Part 8, Secure JPEG2000, abbreviated as JPSEC, had its IS published in April 2007. Part 11 is about Wireless JPEG-2000 (JPWL) and is close to the completion of IS. JPEG2000 is still going on with some new issues and new parts at this writing.

9.3.2 Verification Model of JPEG2000

As in other standards such as MPEG-2 and MPEG-4, the verification model (VM) plays an important role during the development of standards. This is because the VM or test model (TM) for MPEG-2 is a platform for verifying and testing the new techniques before they are adopted by the standards. The VM is updated by completing a set of core experiments for one meeting to another. Experience has shown that the decoding part of the final version of VM is very close to the final standard. Therefore, in order to give an overview of the related wavelet transform parts of the JPEG-2000, we start to introduce the newest version of JPEG-2000 VM [jpeg2000 vm]. The VM of JPEG-2000 describes the encoding process, decoding process, and bitstream syntax, which eventually completely defines the functionality of the existing JPEG-2000 compression system.

The newest version of JPEG2000 VM, currently VM 4.0, was revised on April 22, 1999. In this VM, the final convergence has not been reached, but several candidates have been introduced. These techniques include a DCT-based coding mode, which is currently the baseline JPEG, and a wavelet-based coding mode. In the wavelet-based coding mode, several algorithms have been proposed: overlapped spatial segmented wavelet transform (SSWT), non-overlapped SSWT, and the embedded block coding with optimized truncation (EBCOT). Among these techniques, and according to the consensus, the EBCOT had been included into the final JPEG2000 standard.

The basic idea of EBCOT is the combination of block coding with wavelet transform. First the image is decomposed into subbands using the wavelet transform. The wavelet transform is not restricted to any particular decomposition. However, the Mallat wavelet provides the best compression performance on average for natural images; therefore, the current bitstream syntax is restricted to the standard Mallat wavelet transform in VM 4.0. After decomposition, each subband is divided into 64×64 blocks except at image boundaries where some blocks may have smaller sizes. Every block is then coded independently. For each block, a separate bitstream is generated without utilizing any information from other blocks. The key techniques used for coding include embedded quad-tree algorithm and fractional bit-plane coding.

The idea of embedded quad-tree algorithm is that it uses a single bit to represent whether or not each leading bit-plane contains any significant samples. The quad-tree is formed in the following way. The subband is partitioned into a basic block. The basic block size is 64×64 . Each basic block is further partitioned into 16×16 sub-blocks, as shown in [Figure 9.9](#). Let $\sigma(B_i^k)$ denote the significance of sub-block, B_i^k is the k -th sub-block as shown in [Figure 9.9](#), in j -th bit plane of i -th block. If one or more samples in the sub-block have the magnitude greater than 2^j , then $\sigma(B_i^k)=1$; otherwise, $\sigma(B_i^k)=0$. For each bit-plane, the information concerning the significant sub-blocks is first encoded. All other sub-blocks can then be by-passed in the remaining coding procedure for that

| | | | |
|------------|------------|------------|------------|
| B_i^1 | B_i^2 | B_i^3 | B_i^4 |
| B_i^5 | B_i^6 | B_i^7 | B_i^8 |
| B_i^9 | B_i^{10} | B_i^{11} | B_i^{12} |
| B_i^{13} | B_i^{14} | B_i^{15} | B_i^{16} |

FIGURE 9.9

Example of sub-block partitioning for a block of 64×64 .

bit-plane. To specify the exact coding sequence, we define a two-level quad-tree for the block size of 64×64 and sub-block size of 16×16 . The level-1 quads, $Q_i^1[k]$, consist of four sub-blocks, B_i^1 , B_i^2 , B_i^3 and B_i^4 from Figure 9.9. In the same way, we define level-2 quads, $Q_i^2[k]$, to be 2×2 groupings of level-1 quads. Let $\sigma^j(Q_i^l[k])$ denote the significance of the level-1 quad, $Q_i^l[k]$, in j -th bit plane. If at least one member sub-block is significant in the j -th bit plane, then $\sigma^j(Q_i^l[k]) = 1$; otherwise, $\sigma^j(Q_i^l[k]) = 0$. At each bit-plane, the quad-tree coder visits the level-2 quad first, followed by level-1 quads. When visiting a particular quad, $Q_i^L[k]$ ($L = 1$ or 2 , it is the number of level), the coder sends the significance of each of the four child quads, $\sigma^j(Q_i^L[k])$, or sub-blocks, $\sigma^j(B_i^k)$, as appropriate, except if the significance value can be deduced from the decoder. Under following three cases, the significance may be deduced by the decoder: (1) the relevant quad or sub-block was significant in the previous bit-plane, (2) the entire sub-block is insignificant, or (3) this is the last child or sub-block visited in $Q_i^L[k]$ and all previous quads or sub-blocks are insignificant.

The idea of bit-plane coding is to code the most significant bit first for all samples in the sub-blocks with entropy coding and to send the resulting bits. Then, the next most significant bit will be coded and sent; this process will be continued until all bit planes have been coded and sent. This kind of bitstream structure can be used for robust transmission. If the bitstream is truncated due to transmission error or some other reason, then some or all of the samples in the block may lose one or more least significant bits. This will be equivalent to having used a coarser quantizer for the relevant samples and we can still obtain a reduced quality reconstructed image. The idea of fractional bit-plane coding is to code each bit-plane with four passes: forward significance propagation pass, backward significance propagation pass, magnitude refinement pass, and normalization pass. For the technical detail of fractional bit-plane coding, the interested readers can refer to the VM of JPEG-2000 [jpeg2000 vm] (Skodras 2001).

Finally, we briefly describe the optimization issue of EBCOT. The encoding optimization algorithm is not a part of the standard, since the decoder does not need to know how the encoder generates the bitstream. From the viewpoint of the standard, the only requirement from the decoder to the encoder is that the bitstream must be compliant with the syntax of the standard. However, from the other side, the bitstream syntax could always be defined to favor certain coding algorithms for generating optimized bitstreams. The optimization algorithm described here is justified only if the distortion measure adopted for the code blocks is additive. That is, the final distortion, D , of the whole reconstructed image should satisfy

$$D = \sum D_i^{Ti} \quad (9.24)$$

where D_i is the distortion for block B_i and T_i is the truncation point for B_i . Let R be the total number of bits for coding all blocks of the image for a set of truncation point T_i , then

$$R = \sum R_i^{T_i} \quad (9.25)$$

where $R_i^{T_i}$ are the bits for coding block B_i . The optimization process wishes to find the suitable set of T_i values, which minimizes D subject to the constraint $R \leq R_{max}$. R_{max} is the maximum number of bits assigned for coding the image. The solution is obtained by the method of Lagrange multipliers:

$$L = \sum (R_i^{T_i} - \lambda D_i^{T_i}) \quad (9.26)$$

where the value λ must be adjusted until the rate obtained by the truncation points, which minimize the value of L , satisfy $R = R_{max}$. From equation 9.26, we have a separate trivial optimization problem for each individual block. Specially, for each block, B_i , we find the truncation point, T_i , which minimizes the value $(R_i^{T_i} - \lambda D_i^{T_i})$. This can be achieved by finding the slope turning point of rate distortion curves. In the VM, the set of truncation points and the slopes of rate distortion curves are computed immediately after each block is coded, and we only store enough information to later determine the truncation points that correspond to the slope turning points of rate distortion curves. This information is generally much smaller than the bitstream itself, which is stored for the block. Also, the search for the optimal λ is extremely fast and occupies a negligible proportion of the overall computation time.

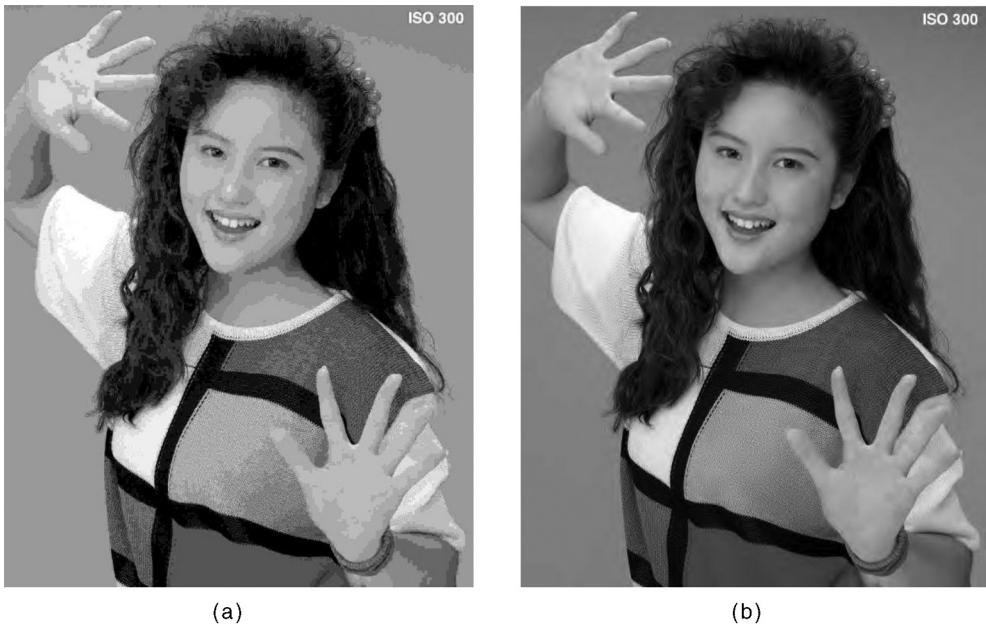


FIGURE 9.10

Performance comparison between the JPEG-compressed and JPEG-2000-compressed Woman image at 0.1 bpp.
 (a) JPEG compressed with PSNR 23.91 dB and (b) JPEG-2000 compressed with PSNR 25.50 dB.

9.3.3 An Example of Performance Comparison between JPEG and JPEG2000

Before ending this chapter, we present an example to compare the performance of JPEG and JPEG2000 in low-bit-rate compression. We apply both JPEG and JPEG-2000 algorithms to one of the JPEG2000 test images, named Woman or N1A, with 0.1 bpp. At this rather low bit rate, the advantage of JPEG-2000 over JPEG is rather obvious. At the 0.1 bpp, the PSNR of the JPEG-2000-compressed Woman image is 25.50 dB, while the JPEG-compressed Woman image is 23.91 dB. From the human visual system point of view, the superior visual quality of the JPEG-2000 compressed image is rather obvious because it can be clearly observed that there is severe distortion called false-countering (as discussed in [Section 1.2.2.2](#)) in the JPEG-compressed Woman image ([Figure 9.10](#)).

9.4 Summary

In this chapter, image coding using wavelet transform has been introduced. First, an overview of wavelet theory was given, and second, the principles of image coding using wavelet transform have been presented. Additionally, two particular embedded image-coding algorithms have been explained, namely the embedded zerotree and SPIHTs. Finally, the new standard for still image coding, JPEG-2000, which adopts the wavelet transform as its core technique, has been described.

Exercises

9.1 For a given function, the Mexican hat wavelet,

$$f(t) = \begin{cases} 1, & \text{for } |t| \leq 1, \\ 0, & \text{otherwise} \end{cases}$$

use formula (9.3) and (9.4) to derive a closed-form expression for the continuous wavelet transform, $\psi_{ab}(t)$.

9.2 Consider the dilation equation

$$\varphi(t) = \sqrt{2} \sum_k h(k) \varphi(2t - k)$$

How does $\varphi(t)$ change if $h(k)$ is shifted? Specifically, let

$$g(k) = h(n - l)$$

$$u(t) = \sqrt{2} \sum_k g(k) u(2t - k)$$

How does $u(t)$ related to $\varphi(t)$?

- 9.3 Let $\varphi_a(t)$ and $\varphi_b(t)$ be two scaling functions generated by the two scaling filters $h_a(k)$ and $h_b(k)$. Show that the convolution $\varphi_a(t)^* \varphi_b(t)$ satisfies a dilation equation with $h_a(k)^* h_b(k)/\sqrt{2}$.
- 9.4 In the applications of denoising and image enhancement, how can the wavelet transform improve the results?
- 9.5 For a given function

$$f(t) = \begin{cases} 0 & t < 0 \\ t & 0 \leq t < 1 \\ 1 & t \geq 1 \end{cases}$$

Show that the wavelet transform of $f(t)$ will be

$$W(a, b) = \text{sgn} \frac{2f\left(b + \frac{a}{2}\right) - f(b) - f(b+a)}{\sqrt{|a|}}$$

where $\text{sgn}(x)$ is the signum function defined as

$$\text{sgn}(x) = \begin{cases} -1 & t < 0 \\ 1 & t > 0 \\ 0 & t = 0 \end{cases}$$

- 9.6 Given an 8×8 block of pixels from the central portion (255:262, 255:262) of Barbara image, whose 8×8 pixel values are shown below.

| | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|
| 144 | 163 | 194 | 210 | 195 | 151 | 136 | 191 |
| 170 | 194 | 209 | 200 | 162 | 136 | 178 | 226 |
| 185 | 200 | 205 | 183 | 152 | 159 | 207 | 218 |
| 186 | 201 | 188 | 167 | 172 | 197 | 200 | 176 |
| 204 | 194 | 166 | 171 | 203 | 199 | 162 | 167 |
| 208 | 167 | 163 | 203 | 212 | 164 | 155 | 215 |
| 180 | 148 | 186 | 219 | 181 | 141 | 191 | 234 |
| 141 | 170 | 217 | 198 | 146 | 166 | 231 | 194 |

- a. Apply three-level 9/7, or 5/3, or Haar wavelet transform, to this 8×8 block image. (If you have difficulty on this, the result of 5/3 is listed below. If you can apply 9/7 or Haar, it would be nicer.)

3-level Integer 5/3 DWT:

| | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|
| 144 | 45 | 26 | -49 | -6 | 15 | -15 | 55 |
| 56 | -63 | -15 | 1 | 8 | 3 | -21 | 7 |
| 9 | -16 | 56 | 111 | 9 | -14 | 18 | 6 |
| -32 | -2 | 62 | 61 | -30 | 32 | -41 | 32 |
| 5 | 11 | -15 | 6 | 5 | 4 | -16 | 15 |
| -9 | 2 | -5 | 10 | 7 | -8 | 13 | -32 |
| 16 | -13 | 20 | -14 | -6 | 4 | -5 | 36 |
| -39 | 33 | -34 | 26 | 26 | -19 | 22 | -80 |

- b. Then, following the examples shown in Shapiro (1993) or the example shown in Usevitch (2001), apply the EZW method to this 8×8 wavelet coefficient array completely. It means that you come up with a set of four different types of symbols (positive significant coefficient, negative significant coefficient, zero-tree root, and isolated zero), which represent this 8×8 three-level wavelet coefficient 2-D array. Provide your coding results in terms of the four types of symbols in tables.
 - c. Comment on the efficiency and the nature of the embedding code of the EZW.
-

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10

Non-standardized Still Image Coding

In this chapter, we introduce three non-standard image coding techniques: vector quantization (VQ) (Nasrabadi and King 1988), fractal coding (Barnsley and Hurd 1993, Fisher 1994, Jacquin 1993), and model-based coding (Li et al. 1994).

10.1 Introduction

The VQ, fractal coding, and model-based coding techniques have not been adopted by any image coding standard. However, due to their unique features these techniques may find some special applications. VQ is an effective technique for performing data compression. Theoretically, VQ is always better than scalar quantization because it fully exploits the correlation between components within the vector. The optimal coding performance will be obtained when the dimension of vector approaches to infinity, and then the correlation between all components is exploited for compression. Another very attractive feature of image VQ is that its decoding procedure is very simple since it only consists of table look-ups. However, there are two major problems with image VQ techniques. The first is that the complexity of VQ exponentially increases with the increasing dimensionality of vectors. Therefore, for VQ it is important to solve the problem of how to design a practical coding system that can provide a reasonable performance under a given complexity constraint. The second major problem of image VQ is the need of a codebook that causes several problems in practical application such as generating a universal codebook for a large number of images, scaling the codebook to fit the bit rate requirement, and so on. Recently, the lattice VQ schemes have been proposed to address these problems (Li et al. 1997).

Fractal theory has a long history. Fractal-based techniques have been used in several areas of digital image processing, such as image segmentation, image synthesis, and computer graphics, but only in recent years has it been extended to the applications of image compression (Jacquin 1993). A fractal is a geometric form, which has the unique feature of having extremely high visual self-similar irregular details while containing very low information content. Several methods for image compression have been developed based on different characteristics of fractals. One method is based on iterated function systems (IFS) proposed in Barnsley and Jacquin (1988). This method uses the self-similar and self-affine property of fractals. Such a system consists of sets of transformations including translation, rotation, and scaling. In the encoder side of the fractal image coding system, a set of fractals is generated from the input image. These fractals can be used to reconstruct the image at the decoder side. Since these fractals are represented by very compact fractal transformations, they require a very small amount of data to be expressed and stored as formulas. Therefore, the information needed be transmitted is very small. The second fractal image coding method is based on the fractal dimension (Lu 1993, Jang and Rajala 1990). Fractal dimension is a good representation of roughness of image surfaces. In this method,

the image is first segmented using the fractal dimension and then the resulted uniform segments can be efficiently coded using the properties of the human visual system (HVS). Another fractal image coding scheme is based on fractal geometry, which is used to measure the length of a curve with a yardstick (Walach and Karnin 1989). The details of these coding methods will be discussed in [Section 10.4](#).

The basic idea of model-based coding is to reconstruct an image with a set of model parameters. The model parameters are then encoded and transmitted to the decoder. At the decoder, the decoded model parameters are used to reconstruct the image with the same model used at the encoder. Therefore, the key techniques in the model-based coding are image modeling, image analysis, and image synthesis.

10.2 Vector Quantization

10.2.1 Basic Principle of Vector Quantization

An N -level vector quantizer, Q , is a mapping from a K -dimensional vector set $\{V\}$, into a finite codebook, $W = \{w_1, w_2, \dots, w_N\}$:

$$Q: V \rightarrow W \quad (10.1)$$

In other words, it assigns an input vector, v , to a representative vector (codeword), w from a codebook, W . The vector quantizer, Q , is completely described by the codebook, $W = \{w_1, w_2, \dots, w_N\}$, together with the disjoint partition, $R = \{r_1, r_2, \dots, r_N\}$, where

$$r_i = \{v: Q(v) = w_i\} \quad (10.2)$$

and w and v are K -dimensional vectors. The partition should identically minimize the quantization error (Gersho 1982). A block diagram of the various steps involved in image VQ is depicted in [Figure 10.1](#).

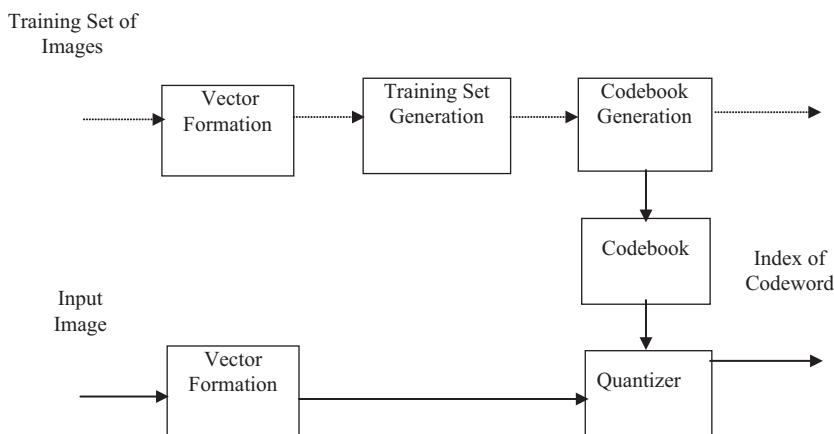


FIGURE 10.1

Principle of image VQ. The dashed lines correspond to the training set generation, codebook generation, and transmission (if it is necessary).

The first step of image VQ is the image formation. The image data is first partitioned into a set of vectors. A large number of vectors from various images are then used to form a training set. The training set is used to generate a codebook, normally using an iterative clustering algorithm. The quantization or coding step involves searching, for each input vector, the closest codeword in the codebook. Then the corresponding index of the selected codeword is coded and transmitted to the decoder. At the decoder, the index is decoded and converted to the corresponding vector with the same codebook as at the encoder by look-up table. Thus, the design decisions in implementing image VQ include (1) vector formation, (2) training set generation, (3) codebook generation, and (4) quantization.

10.2.1.1 Vector Formation

The first step of VQ is vector formation, that is, the decomposition of the images into a set of vectors. Many different decompositions have been proposed; examples include the intensity values of a spatially contiguous block of pixels (Gersho and Ramamuthi 1982, Baker and Gray 1983), these same intensity values but now normalized by the mean and variance of the block (Murakami et al. 1982), the transformed coefficients of the block pixels (Li and Zhang 1995), and the adaptive linear predictive coding coefficients for a block of pixels (Sun and Goldberg 1984). Basically, the approaches of vector formation can be classified into two categories: direct spatial or temporal and feature extraction. Direct spatial or temporal is a simple approach to forming vectors from the intensity values of a spatial or temporal contiguous block of pixels in an image or an image sequence. A number of image vector quantization schemes have been investigated with this method. The other kind of method is feature extraction. An image feature is a distinguishing primitive characteristic. Some features are natural in the sense that such features are defined by the visual appearance of an image, while the other so-called artificial features result from specific manipulations or measurements of images or image sequences. In vector formation, it is well known that the image data in the spatial domain can be converted to a different domain so that subsequent quantization and joint entropy encoding can be more efficient. For this purpose, some features of image data, such as transformed coefficients, block means, can be extracted and vector quantized. The practical significance of feature extraction is that it can result in the reduction of vector size, and consequently, reduce the complexity of the coding procedure.

10.2.1.2 Training Set Generation

An optimal vector quantizer should ideally match the statistics of the input vector source. However, if the statistics of an input vector source are unknown, a training set representative of the expected input vector source can be used to design the vector quantizer. If the expected vector source has a large variance, then a large training set is needed. To alleviate the implementation complexity caused by a large training set, the input vector source can be divided into the subsets. For example, in Gersho (1982) the single input source is divided into "edge" and "shade" vectors, and then the separate training sets are used to generate the separate codebooks, respectively. Those separate codebooks are then concatenated into a final codebook. In other methods, small local input sources corresponding to portions of the image are used as the training sets, so the codebook can better match the local statistics. However, the codebook needs to be updated to track the changes in local statistics of the input sources. This may increase the complexity and reduce the coding efficiency. Practically, in most coding systems a set of typical images is selected as the training set and used to generate the codebook. The coding performance can then be insured for the images with the training set or those not in the training set but with statistics similar to those in the training set.

10.2.1.3 Codebook Generation

The key step of conventional image VQ is the development of a good codebook. The optimal codebook, using the mean squared error (MSE) criterion, must satisfy two necessary conditions (Gersho 1982). First, the input vector source is partitioned into a pre-decided number of regions with the minimum distance rule. The number of regions is decided by the requirement of the bit rate, or compression ratio and coding performance. Second, the codeword or the representative vector of this region is the mean value, or the statistical center, of the vectors within the region. Under these two conditions, a generalized Lloyd clustering algorithm proposed by Linde, Buzo, and Gray (the so-called LBG algorithm [Linde et al. 1980]) has been extensively used to generate the codebook. The clustering algorithm is an iterative process, minimizing a performance index calculated from the distances between the sample vectors and their cluster centers. The LBG clustering algorithm can only generate a codebook with a local optimum, which depends on the initial cluster seeds. Two basic procedures have been used to obtain the initial codebook or cluster seeds. In the first approach, the starting point involves finding a small codebook with only two codewords and then recursively splitting the codebook until the required number of codewords is obtained. This approach is referred to as binary splitting. The second starts with initial seeds for the required number of codewords, these seeds being generated by pre-processing the training sets. To address the problem of local optimum, Equitz (1989) proposed a new clustering algorithm, the pairwise nearest neighbor (PNN) algorithm. The PNN algorithm begins with a separate cluster for each vector in the training set and merges together two clusters at a time until the desired codebook size is obtained. At the beginning of the clustering process, each cluster contains only one vector. At the following process, the two closest vectors in the training set are merged to their statistical mean value, in such a way that the error incurred by replacing these two vectors with a single codeword is minimized. The PNN algorithm significantly reduces computation complexity without sacrificing performance. This algorithm can also be used as an initial codebook generation for LBG algorithm.

10.2.1.4 Quantization

Quantization in the context of a VQ involves selecting a codeword in the codebook for each input vector. The optimal quantization, in turn, implies that for each input vector, v , the closest codeword, w_k , is found as shown in [Figure 10.2](#). The measure criterion could be MSE, absolute error, or other distortion measures.

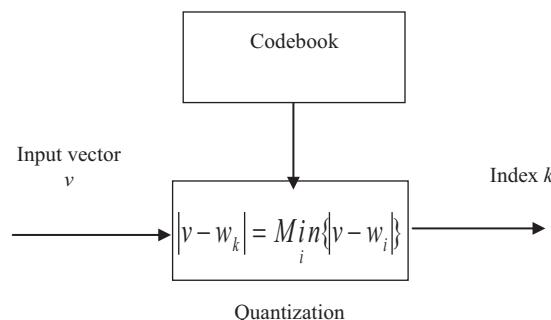
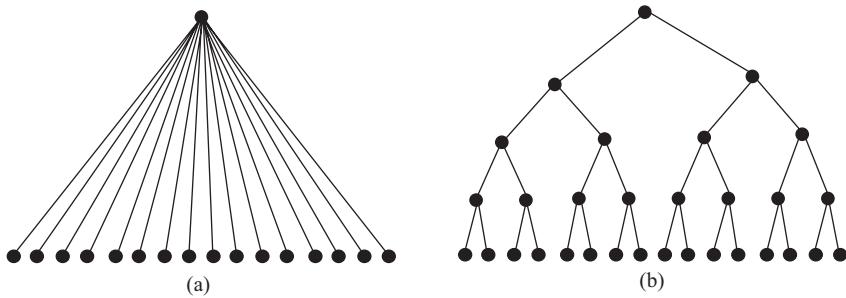


FIGURE 10.2
Principle of VQ.

**FIGURE 10.3**

(a) Full search quantization and (b) Binary tree search quantization.

A full-search quantization is an exhaustive search process over the entire codebook for finding the closest codeword as shown in Figure 10.3a. It is optimal for the given codebook, but the computation is more expensive. An alternative approach is a tree-search quantization, where the search is carried out based on a hierarchical partition. A binary-tree search is shown in Figure 10.3b. Tree search is much faster than full search, but it is clear that the tree search is sub-optimal for the given codebook and requires more memory for the codebook.

10.2.2 Several Image Coding Schemes with Vector Quantization

In this section, we are going to present several image coding schemes using VQ, which include residual VQ, classified VQ, transform domain VQ, predictive VQ, and block truncation coding (BTC), which can be seen as a binary VQ.

10.2.2.1 Residual VQ

In the conventional image VQ, the vectors are formed by spatially partitioning the image data into blocks of 8×8 or 4×4 pixels. In the original spatial domain, the statistics of vectors may be widely spread in the multidimensional vector space. This causes the difficulty for generating the codebook with a finite size and limits the coding performance. Residual VQ is proposed to alleviate this problem. In residual VQ, the mean of the block is extracted and coded separately. The vectors are formed by subtracting the block mean from the original pixel values. This scheme can be further modified by considering the variance of the blocks. The original blocks are converted to the vectors with zero mean and unit standard deviation with the following conversion formula (Murakami et al. 1982):

$$m_i = \frac{1}{K} \sum_{j=0}^{K-1} s_j \quad (10.3)$$

$$x_j = \frac{(s_j - m_i)}{\sigma_i} \quad (10.4)$$

$$\sigma_i = \left[\frac{1}{K} \sum_{j=0}^{K-1} (s_j - m_i)^2 \right]^{\frac{1}{2}} \quad (10.5)$$

where m_i is the mean value of i -th block, σ_i is the variance of i -th block, s_j is the pixel value of pixel j ($j = 0, \dots, K-1$) in the i -th block, K is the total number of pixels in the block, and x_j is the normalized value of pixel j . The new vector X_i is now formed by x_j ($j = 0, 1, \dots, k-1$):

$$X_i = [x_0, x_1, \dots, x_K]_i \quad (10.6)$$

With the above normalization, the probability function $P(X)$ of input vector X is approximately similar for image data from different scenes. Therefore, it is easy to generate a codebook for the new vector set. The problem of this method is that the mean and variance values of blocks have to be coded separately. This increases the overhead and limits the coding efficiency. Several methods have been proposed to improve the coding efficiency. One of these methods is to use predictive coding to code the block mean values. The mean value of the current block can be predicted by the one of previously coded neighbors. In such a way, the coding efficiency increases as the use of inter-block correlation.

10.2.2.2 Classified VQ

In image VQ, the codebook is usually generated using training set under constraint of minimizing the MSE. This implies that the codeword is the statistical mean of the region. During the quantization, each input vector is replaced by its closest codeword. Therefore, the coded images usually suffer from edge distortion at very low bit rates since edges are smoothed by the operation of averaging with the small sized codebook. To overcome this problem, we can classify the training vector set into edge vectors and shade vectors (Gersho 1982). Two separate codebooks can then be generated with the two types of training sets, respectively. Each input vector can be coded by the appropriate codeword in the codebook. However, the edge vectors can be further classified into many types according to their location and angular orientation. The classified VQ can be extended into a system, which contains many sub-codebooks, where each represents a type of edges. However, this would increase the complexity of the system and would be hard to be implemented in practical applications.

10.2.2.3 Transform Domain VQ

The VQ can be performed in the transform domain. A spatial block of 4×4 or 8×8 pixels is first transformed to the 4×4 or 8×8 transformed coefficients. There are several ways to form vectors with transformed coefficients. In the first method, a number of high-order coefficients can be discarded since most of the energy is usually contained in the low-order coefficients for most of the blocks. This reduces the VQ computational complexity at the expense of a small increase of distortion. However, for some active blocks, the edge information is contained in the high frequencies, or high-order coefficients. It will cause serious subjective distortion by discarding high frequencies. In the second method, the transformed coefficients are divided into several bands and each band is used to form its corresponding vector set. This method is equivalent to the classified VQ in the spatial domain. An adaptive scheme is then developed by using two kinds of vector formation methods. The first method is used for the blocks containing the moderate intensity variation and the second method is used for the blocks with high spatial activities. However, the complexity increases as more codebooks are needed in such kind of adaptive coding system.

10.2.2.4 Predictive VQ

The vectors are usually formed by the spatially consecutive blocks. The consecutive vectors are then highly statistically dependent. Therefore, better coding performance can be achieved if the correlation between vectors is exploited. Several predictive VQ schemes have been proposed to address this problem. One kind of predictive VQ is finite-state VQ (Foster et al. 1985). The finite-state VQ is similar to a trellis coder (Stewart et al. 1982). In finite-state VQ, the codebook consists of a set of sub-codebooks. A state variable is then used to specify which sub-codebook should be selected for coding the input vector. The information about state variable must be inferred from the received sequence of state symbols and initial state such as in a trellis coder. Therefore, there is no side information or overhead that needs to be transmitted to the decoder. The new encoder state is a function of the previous encoder state and the selected sub-codebook. This permits the decoder to track the encoder state if the initial condition is known. The finite-state VQ needs additional memory to store the previous state, but it takes advantage of correlation between successive input vectors by choosing the appropriate codebook for the given past history. It should be noted that the minimum distortion selection rule of conventional VQ is not necessarily optimum for finite-state VQ for a given decoder since a low distortion codeword may lead to a bad state and hence to poor long-term behavior. Therefore, the key design issue of finite-state VQ is to find a good next-state function.

Another predictive VQ was proposed in Hang and Woods (1985). In this system, the input vector is formed in such a way that the current pixel is as the first element of the vector and the previous inputs as the remaining elements in the vector. The system is like a mapping or recursive filter that is used to predict the next pixel. The mapping is implemented by a vector quantizer look-up table and provides the predictive errors.

10.2.2.5 Block Truncation Coding

In the block truncation code (BTC) (Delp and Mitchell 1979), an image is first divided into 4×4 blocks. Each block is then coded individually. The pixels in each block are first converted into two level signals by using the first two moments of the block:

$$\begin{aligned} a &= m + \sigma \sqrt{\frac{N-q}{q}} \\ b &= m - \sigma \sqrt{\frac{q}{N-q}} \end{aligned} \tag{10.7}$$

where m is the mean value of the block, σ is the standard deviation of the block, N is the number of total pixels in the block, and q is the number of pixels that are greater in value than m . Therefore, each block can be described by the values of block mean, variance, and a binary-bit plane that indicates whether the pixels have the values above or below the block mean. The binary-bit plane can be seen as a binary vector quantizer. If the mean and variance of the block are quantized to eight bits, then two bits/pixel is achieved for the blocks of 4×4 pixels. The conventional BTC scheme can be modified to increase the coding efficiency. For example, the block mean can be coded by DPCM coder that exploits the inter-block correlation. The bit plane can be coded with an entropy coder on the patterns (Udpikar and Raina 1987).

10.2.3 Lattice VQ for Image Coding

In the conventional image VQ schemes, there are several issues, which cause some difficulties for the practical applications of image VQ. The first problem is the limitation of vector dimension. It is indicated that the coding performance of VQ increases as vector dimension while the coding complexity exponentially increases at the same time as the increasing vector dimension. Therefore, in practice only a small size of vector dimension is possible under the complexity constraint. Another important issue in VQ is the need for a codebook. Much research effort has gone into finding out how to generate a codebook. However, in practical applications, there is another problem of how to scale the codebook for various rate-distortion requirements. The codebook generated by LBG-like algorithms with a training set is usually only suitable for a specified bit rate and it does not have the flexibility of codebook scalability. For example, a codebook generated for an image with small resolution may not be suitable for the images with high resolution. Even for the same spatial resolution, different bit rates would require different codebooks. Additionally, the VQ needs a table to specify the codebook and consequently, the complexity of storing and searching the table is too high to have a very large table. This further limits the coding performance of image VQ. These problems become major obstacles of image VQ for implementation. Recently, an algorithm of lattice VQ has been proposed to address these problems (Li et al. 1997). Lattice VQ does not have the problems described here. The codebook for lattice VQ is simply a collection of lattice points uniformly distributed over the vector space. Scalability can be achieved by scaling the cell size associated with every lattice point just like in the scalar quantizer by scaling the quantization step. The basic concept of lattice can be found in Conway and Sloane (1991). A Typical Lattice VQ scheme is shown in Figure 10.4. There are two steps involved in the image lattice VQ. The first step is to find the closest lattice point for the input vector. The second step is to label the lattice point, i.e., mapping a lattice point to an index. Since lattice VQ does need a codebook, the index assignment is based on lattice labeling algorithm instead of look-up table such as in the conventional VQ. Therefore, the key issue of lattice VQ is to develop an efficient lattice-labeling algorithm. With this algorithm the closest lattice point and its corresponding index within a finite boundary can be obtained by calculation at the encoder for each input vector.

At the decoder, the index is converted to the lattice point by the same labeling algorithm. The vector is then reconstructed with the lattice point. The efficiency of a labeling

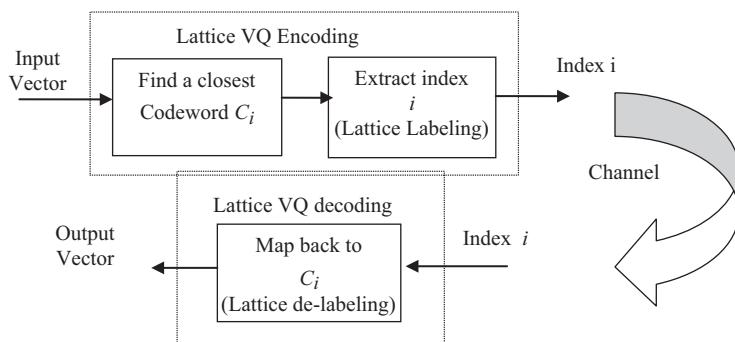


FIGURE 10.4

Block diagram of lattice VQ.

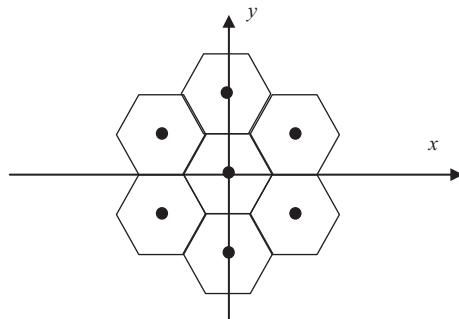


FIGURE 10.5
Labeling a two-dimensional lattice.

algorithm for lattice VQ is measured by how many bits needed to represent the indices of the lattice points within a finite boundary. We use a two-dimensional lattice to explain the lattice labeling efficiency. A two-dimensional lattice is shown in Figure 10.5.

In Figure 10.5, there are seven lattice points. One method to label these seven 2-D lattice points is to use their coordinates (x, y) to label each point. If we label x and y separately, we need two bits to label three values of x and three bits to label a possible five values of y , for a total of five bits. It is clear that three bits are sufficient to label seven lattice points. Therefore, different labeling algorithms may have different labeling efficiency. Several algorithms have been developed for multi-dimensional lattice labeling. In Conway and Sloane (1983), the labeling method assigns an index to every lattice point within a Voronoi boundary where the shape of the boundary is the same as the shape of Voronoi cells. Apparently, for different dimensions, the boundaries have different shapes. In the algorithm proposed in Laroia and Favardin (1993), the same method is used to assign an index to each lattice point. Since the boundaries are defined by the labeling algorithm, this algorithm might not achieve a 100% labeling efficiency for a prespecified boundary such as a pyramid boundary. The algorithm proposed in Fischer (1986) can assign an index to every lattice point within a prespecified pyramid boundary and achieves a 100% labeling efficiency, but this algorithm can only be used for the Z^n lattice. In the recent proposed algorithm (Wang 1998), the technical breakthrough has been obtained. In this algorithm, a labeling method has been developed for Construction-A and Construction-B lattices (Conway and Sloane 1983), which are very useful for VQ with proper vector dimension such as 16 and achieve 100% efficiency. Additionally, these algorithms are used for labeling lattice points with dimension 16 and provide the minimum distortion. These algorithms are developed based on the relations between lattices and linear block codes. Construction-A and Construction-B are the two simplest ways to construct a lattice from a binary linear block code $C = (n, k, d)$, where n , k , and d are the length, the dimension, and the minimum distance of the code, respectively.

A construct-A lattice is defined as:

$$\Lambda_n = C + 2Z^n \quad (10.8)$$

where Z^n is the n -dimensional cubic lattice and C is a binary linear block code. There are two steps involved for labeling a Construction-A lattice. First is to order the lattice points according to the binary linear block code C , and then to order the lattice points associated with a particular non-zero binary codeword. For the lattice points associated with

a non-zero binary codeword, two sub-lattices are considered separately. One sub-lattice consists of all the dimensions that have “0” component in the binary codeword and the other consists of all the dimensions that have “1” component in the binary codeword. The first sub-lattice is considered as a $2\mathbb{Z}$ lattice while the second is considered as a translated $2\mathbb{Z}$ lattice. Therefore, the labeling problem is reduced to label the \mathbb{Z} lattice at the final stage.

A Construction-B lattice is defined as:

$$\Lambda_n = C + 2D_n \quad (10.9)$$

where D_n is an n-dimensional Construction-A lattice with the definition as:

$$D_n = (n, n-1, 2) + 2\mathbb{Z}^n \quad (10.10)$$

and C is a binary doubly even linear block code. When n is equal to 16, the binary even linear block code associated with Λ_{16} is $C = (16, 5, 8)$. The method for labeling a Construction-B lattice is similar to the method for labeling a Construction-A lattice with two minor differences. The first difference is that for any vector $y = c+2x$, $x \in \mathbb{Z}^n$, if y is a Construction-A lattice point; and $x \in D_n$, if y is a Construction-B lattice point. The second difference is that C is a binary doubly even linear block code for Construction-B lattices while it is not necessarily doubly even for Construction-A lattices. In the implementation of these lattice point labeling algorithm, the encoding and decoding functions for lattice VQ have been developed in Li et al. (1997). For a given input vector, an index representing the closest lattice point will be found by the encoding function and for an input index, the reconstructed vector will be generated by the decoding function. In summary, the idea of lattice VQ for image coding is an important achievement for eliminating the need of codebook for image VQ. The development of efficient algorithms for lattice point labeling makes lattice VQ feasible for image coding.

10.3 Fractal Image Coding

10.3.1 Mathematical Foundation

A fractal is a geometric form whose irregular details can be represented by some objects with different scale and angle, which can be described by a set of transformations such as affine transformations. Additionally, the objects used to represent the image irregular details have some form of self-similarity and these objects can be used to represent an image in a simple recursive way. An example of fractals is the Von Koch curve as shown in [Figure 10.6](#). The fractals can be used to generate an image. The fractal image coding that is based on IFS is the inverse process of image generation with fractals; therefore, the key technology of fractal image coding is the generation of fractals with an *IFS*.

To explain what an *IFS* is, we start from the contractive affine transformation. A two-dimensional affine transformation A is defined as follows:

$$A \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} e \\ f \end{bmatrix} \quad (10.11)$$

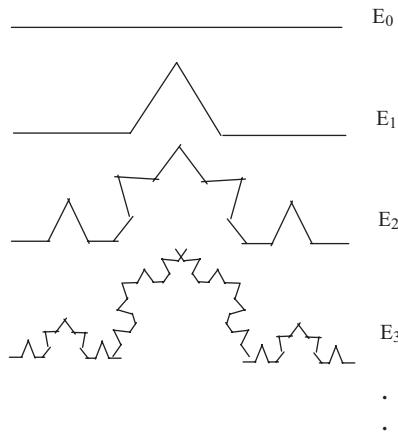


FIGURE 10.6
Construction of the Von Koch curve.

This is a transformation that consists of a linear transformation followed by a shift or translation and maps points in the Euclidean plane into new points in another Euclidean plane. We define that a transformation is contractive if the distance of two points P_1 and P_2 in the new plane is smaller than their distance in the original plane, i.e.,

$$d(A(P_1), A(P_2)) < s d(P_1, P_2) \quad (10.12)$$

where s is a constant and $0 < s < 1$. The contractive transformations have the property that when the contractive transformations are repeatedly applied to the points in a plane, these points will converge to a fixed point. An IFS is defined as a collection of contractive affine transformations. A well-known example of the IFS contains the four following transformations:

$$A_i \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} e \\ f \end{bmatrix} \quad i = 1, 2, 3, 4 \quad (10.13)$$

This is the *IFS* of a fern leaf, which parameters are shown in [Table 10.1](#).

The transformation A_1 is used to generate the stalk, the transformation A_2 is used to generate right leaf, the transformation A_3 is used to generate left leaf, and the transformation A_4 is used to generate the main fern. A fundamental theorem of fractal geometry is that each *IFS* defines a unique fractal image. This image is referred to as the attractor of the *IFS*. In other words, an image corresponds to the attractor of an *IFS*.

TABLE 10.1
The Parameters of the *IFS* of a Fern Leaf

| | a | b | c | d | e | f |
|-------|-------|-------|-------|------|---|-----|
| A_1 | 0 | 0 | 0 | 0.16 | 0 | 0.2 |
| A_2 | 0.2 | -0.26 | 0.23 | 0.22 | 0 | 0.2 |
| A_3 | -0.15 | 0.28 | 0.26 | 0.24 | 0 | 0.2 |
| A_4 | 0.85 | 0.04 | -0.04 | 0.85 | 0 | 0.2 |

Now let us explain how to generate the image using the *IFS*. Let us suppose that an *IFS* contains N affine transformations, A_1, A_2, \dots, A_N , and each transformation has an associated probability, p_1, p_2, \dots, p_N , respectively. Suppose that this is a complete set and the sum of the probability equals to 1, i.e.,

$$p_1 + p_2 + \dots + p_N = 1 \text{ and } p_i > 0 \text{ for } i = 0, 1, \dots, N. \quad (10.14)$$

The procedure of generating an attractor is as follows. For any given point (x_0, y_0) in a Euclidean plane, one transformation in the *IFS* according to its probability is selected and applied to this point to generate a new point (x_1, y_1) . Then another transformation is selected according to its probability and applied to the point (x_1, y_1) to obtain a new point (x_2, y_2) . This process is repeated over and over again to obtain a long sequence of points: $(x_0, y_0), (x_1, y_1), \dots, (x_n, y_n), \dots$. According to the theory of *IFSs*, these points will be converged to an image that is the attractor of the given *IFS*. The above-described procedure is shown in the flowchart of [Figure 10.7](#). With the above algorithm and the parameters in the [Table 10.1](#), initially the point can be anywhere within the large square, but after several iterations it will converge onto the fern. The 2-D affine transformations are extended to 3-D transformations, which can be used to create fractal surfaces with the *IFSs*. This fractal surface can be considered as the gray level or brightness of a 2-D image.

10.3.2 IFS-Based Fractal Image Coding

As it is described in the last section, an *IFS* can be used to generate a unique image, which is referred to as an attractor of the *IFS*. In other words, an image is the attractor of an *IFS*, and this image can be simply represented by the parameters of the *IFS*. Therefore, if we can use an inverse procedure to generate a set of transformations, i.e.,

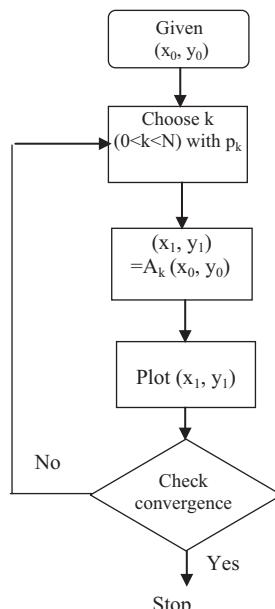


FIGURE 10.7

Flowchart of generating an image with an *IFS*.

an IFS, from an image, then these transformations or the IFS can be used to represent the approximation of the image. The image coding system can use the parameters of the transformations in the IFS instead of the original image data for storage or transmission. Since the IFS contains only very limited data such as transformation parameters, this image coding method may result in a very high compression ratio. For example, the fern image is represented by 24 integers or 192 bits (if each integer is represented by eight bits). This number is much smaller than the number needed to represent the fern image in the way of pixel by pixel. Now the key issue of the IFS-based fractal image coding is to generate the IFS for the given input image. Three methods have been proposed to obtain the IFS (Lu 1993). One is the direct method that directly finds a set of contractive affine transformations from the image based on the self-similarity of the image. The second method is to partition an image into the smaller objects whose IFSs are known. These IFSs are used to form a library. The encoding procedure is to look for an IFS from the library for each small object. The third method is called partitioned IFS (PIFS). In this method, the image is first divided into the smaller blocks and then the IFS for each block is found by mapping a larger block into a small block.

In the first direct approach, the image is first partitioned into non-overlapped blocks in such a way that each block is similar to the whole image and a transformation can map the whole image to the block. The transformation for each individual block may be different. The combination of these transformations can be taken as the IFS of the given image. Then, much less data is required to represent the IFS or the transformations than to transmit or store the given image in the pixel-by-pixel way. For the second approach, the key issue is how to partition the given image into objects whose IFSs are known. The image processing techniques such as color separation, edge detection, spectrum analysis, and texture-variation analysis can be used for the image partitioning. However, for natural images or arbitrary images, it may be impossible or very difficult to find an IFS whose attractor perfectly covers the original image. Therefore, for most natural images the PIFS method has been proposed (Lu 1993). In this method, the transformations do not map the whole image into a small block. For encoding an image, the whole image is first partitioned into a number of larger blocks that are referred to as domain blocks. The domain blocks can be overlapped. Then, the image is partitioned into a number of smaller blocks that are called range blocks. The range blocks do not overlap and the sum of total range blocks cover whole image. In the third step, a set of contractive transformations is chosen. Each range block is mapped into a domain block with a searching method and a matching criterion. The combination of the transformations is used to form a PIFS. The parameters of PIFS are transmitted to the decoder. It is noted that no domain blocks are transmitted. The decoding starts with a flat background. The iterated process is then applied with the set of transformations. The reconstructed image is then obtained after the process converges. From the above discussion, it is found that there are three main design issues involved in the block fractal image coding system. First are partitioning techniques, which include the range block partitioning and domain block partitioning. As mentioned earlier, the domain block is larger than the range block. Dividing the image into square blocks is the simplest partitioning approach. The second issue is the choice of distortion measure and searching method. The common distortion measure in the block fractal image coding is the root-mean-square (RMS) error. The closest matching between range block and transformed domain block is found by the RMS distortion measure. The third is the selection of a set of contractive transformations defined consistently with a partition.

It is noted that the PIFS-based fractal image coding has several similar features with image VQ. Both coding schemes are block-based coding schemes and need a codebook

for encoding. For PIFS-based fractal image coding the domain blocks can be seen as forming a virtual codebook. One difference is that the fractal image coding does not need to transmit the codebook data (domain blocks) to the decoder while VQ needs. The second difference is the block size. For VQ block size for code vector and input vector is the same while in PIFS fractal coding the size of the domain block is different from the size of the range blocks. Another difference is that in fractal image coding the image itself serves as the codebook, while this is not true for VQ image coding.

10.3.3 Other Fractal Image Coding Methods

In addition to the IFS-based fractal image coding, there are several other fractal image coding methods. One is the segmentation-based coding scheme using fractal dimension. In this method, the image is segmented into regions based on the properties of the human HVS. The image is segmented into the regions, each of these regions is homogeneous in the sense of having similar features in visual perception. This is different from the traditional image segmentation techniques that try to segment an image into regions of constant intensity. For complicated image, good representation of an image needs a large number of small segmentations. However, in order to obtain high compression ratio, the number of segmentations is limited. The trade-off between image quality and bit rate has to be considered. A parameter, fractal dimension, is used as a measure to control the trade-off. Fractal dimension is a characteristic of a fractal. It is related to a metric property such as the length of a curve and the area of a surface. The fractal dimension can provide a good measure of perceptual roughness of the curve and surface. For example, if we use many segments of straight lines to approximate a curve, with increasing the length of straight line the perceptual rougher curves are represented.

10.4 Model-Based Coding

10.4.1 Basic Concept

In the model-based coding, an image model that can be 2-D model for still images or 3-D model for video sequence is first constructed. At the encoder, the model is used to analyze the input image. The model parameters are then transmitted to the decoder. At the decoder the reconstructed image is synthesized by the model parameters with the same image model used at the encoder. This basic idea of model-based coding is shown in [Figure 10.8](#). Therefore, the basic techniques in the model-based coding are the image modeling, image analysis, and image synthesis techniques. Both image analysis and synthesis are based on the image model. The image modeling techniques used for image coding can normally be divided into two classes: structure modeling and motion modeling. The motion modeling is usually used for video sequences and moving pictures, while the structure modeling is usually used for still image coding. The structure model is used for reconstruction of 2-D or 3-D scene model.

10.4.2 Image Modeling

The geometric model is usually used for image structure description. The geometric model can be classified into surface-based description and volume-based description.

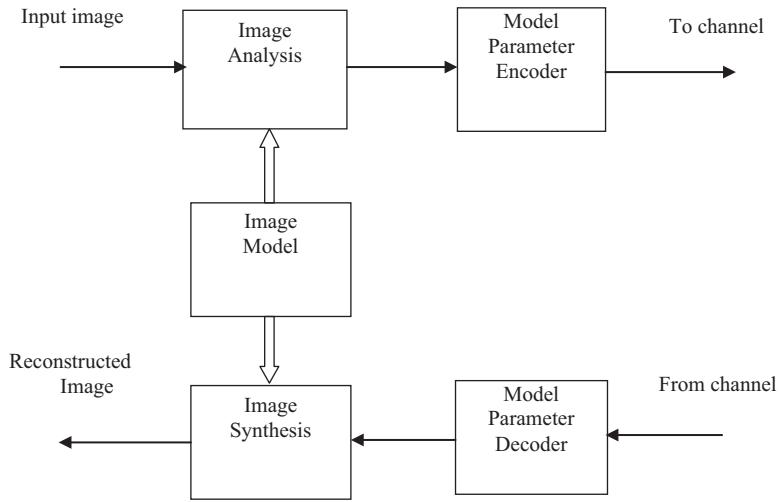


FIGURE 10.8
Basic principle of model-based coding.

The major advantage of surface description is that such description is easily converted into surface representation that can be encoded and transmitted. In these models, the surface is approximated by planar polygonal patches such as triangle patches. The surface shape is represented by a set of points that represent the vertices of these triangle meshes. The size of these triangle patches can be adjusted according to the surface complexity. In other words, for more complicated areas, more triangle meshes are needed to approximate the surface, while for smoothing area, the mesh sizes can be larger or fewer vertices of the triangle meshes are needed to represent the surface. The volume-based description is a natural approach for modeling most solid world objects. Most existing research work on volume-based description focuses on the parametric volume description. The volume-based description is, of course, used for 3-D objects or video sequences.

However, model-based coding is successfully applicable only to certain kinds of images since it is very hard to find general image models suitable for most natural scenes. The few successful examples of image models include the human face, head, and body. These models are developed for analysis and synthesis of moving images. The face animation has been adopted by the MPEG-4 visual coding. The body animation is under consideration for the version 2 of MPEG-4 visual coding.

10.5 Summary

In this chapter, three kinds of image coding techniques, VQ, fractal image coding, and model-based coding, which are not used in the current standards, have been presented. All three techniques have several important features such as very high compression ratio for certain kinds of images and very simple decoding procedure (special for VQ). However, due to some limitations these techniques have not been adopted by industry standards. It should be noted that recently the facial model, face animation technique, has been adopted by MPEG-4 visual standard [mpeg4 visual].

Exercises

- 10.1 In the modified residual VQ described in (10.5), with 4×4 block and eight bits for each pixel of original image, if we use eight bits for coding block mean and block variance. We want to obtain the final bit rate is two bits/pixel, what codebook size must we use for coding residual, assuming that we use fixed-length coding to code vector indices?
- 10.2 In the BTC described in (9.7), what is the bit rate for a block size of 4×4 if the mean and variance are both encoded with eight bits? Do you have any suggestions for reducing the bit rate without seriously affecting the reconstruction quality? Is the codebook generated with the LBG algorithm local optimum? List the several important factors that will affect the quality of codebook generation.
- 10.3 In image coding using VQ, what kind of problems will be caused by using codebook in the practical applications (hint: changing bit rate).
- 10.4 What is the most important improvement of the lattice VQ over traditional VQ in the practical application? What is the key issue for lattice VQ for image coding application?
- 10.5 Write a subroutine to generate a fern leaf (using C).

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Part III

Motion Estimation and Compensation



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11

Motion Analysis and Motion Compensation

Up to this point, what we discussed in the previous chapters were basic techniques in image coding, specifically, techniques utilized in still image coding. From here on, we are going to address the issue of video sequence compression. To fulfill the task, we will first define the concepts of image and video sequences. Then, we address the issue of interframe correlation between successive frames. Two techniques in exploitation of interframe correlation, frame replenishment, and motion-compensated coding will then be discussed. The rest of the chapter covers the concepts of motion analysis and motion compensation in general.

11.1 Image Sequences

In this section, the concept of various image sequences is defined in a theoretical and systematic manner. The relationship between image sequences and video sequences is also discussed.

It is well known that, in the 1960s, the advent of the semiconductor computer and the space program swiftly brought the field of digital image processing into public focus. Since then, the field has experienced rapid growth and has entered every aspect of modern technology. Since the early 1980s, digital image sequence processing has been an attractive research area (Huang 1981a, 1983). This is not surprising, because an image sequence, as a collection of images, may provide more information than a single image frame. The increased computational complexity and memory space associated with image sequence processing are becoming more affordable due to more advanced, achievable computational capability. With the tremendous advancements continuously made in VLSI computer and information processing, image and video sequences are evermore indispensable elements of modern life. While the pace and the future of this development cannot be predicted, one thing is certain: this process is going to drastically change all aspects of our world in the next several decades.

As far as image sequence processing is concerned, it is noted that in addition to temporal image sequences, stereo image pair and stereo image sequences also obtained attention in the middle of the 1980s (Waxman and Duncan 1986). The concepts of temporal and spatial image sequences and the imaging space (which may be considered as a next higher-level unification of temporal and spatial image sequences) may be illustrated as follows.

Consider a sensor located in a specific position in the three-dimensional (3-D) world space. It generates images about the scene, one after another. As time goes by, the images form a sequence. The set of these images can be represented with a brightness function $g(x, y, t)$, where x and y are coordinates on the image planes. This is referred to as a *temporal image sequence*. This is the basic outline about the brightness function $g(x, y, t)$ dealt with by researchers in both the computer vision (e.g., Horn and Schunck 1980) and signal processing fields (e.g., Pratt 1979).

Now consider a generalization of the above basic outline. A sensor, as a solid article, can be translated (in three free dimensions) and rotated (in two free dimensions). It is noted that here the rotation of a sensor about its optical axis is not counted, since the images generated will remain unchanged when this type of rotation takes place. So, we can obtain a variety of images when a sensor is translated to different coordinates and rotated to different angles in the 3-D world space. Equivalently, we can imagine that there is an infinite number of sensors in the 3-D world space that occupy all possible spatial coordinates and assume all possible orientations at each coordinate; i.e., they are located on all possible positions. At one specific moment, all of these images form a set, which can be referred to as a *spatial image sequence*. When time varies, these sets of images form a much larger set of images, called an *imaging space*.

Clearly, it is impossible to describe such a set of images by using the previously mentioned $g(x, y, t)$. Instead, it should be described by a more general brightness function,

$$g(x, y, t, \bar{s}), \quad (11.1)$$

where \bar{s} indicates the sensor's position in the 3-D world space, i.e., the coordinates of the sensor center and the orientation of the optical axis of the sensor. Hence, \bar{s} is a 5-D vector. That is,

$$\bar{s} = (\tilde{x}, \tilde{y}, \tilde{z}, \beta, \gamma), \quad (11.2)$$

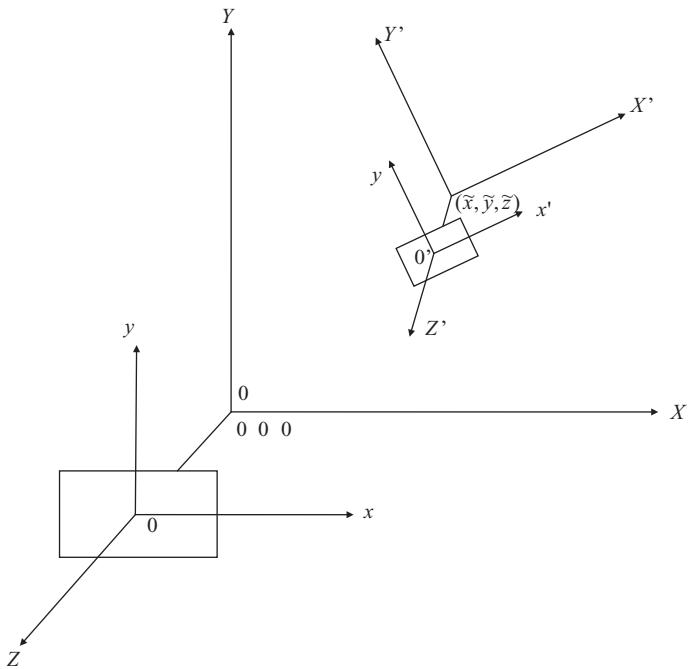
where \tilde{x} , \tilde{y} , and \tilde{z} represent the coordinates of the optical center of the sensor in the 3-D world space, and β and γ represent the orientation of the optical axis of the sensor in the 3-D world space. More specifically, each sensor in the 3-D world space may be considered associated with a 3-D Cartesian coordinate system such that its optical center is located on the origin and its optical axis is aligned with the OZ axis. In the 3-D world space, we choose a 3-D Cartesian coordinate system as the reference coordinate system. Hence, a sensor with its Cartesian coordinate system coincident with the reference coordinate system has its position in the 3-D world space denoted by $\bar{s} = (0, 0, 0, 0, 0)$. An arbitrary sensor position denoted by $\bar{s} = (\tilde{x}, \tilde{y}, \tilde{z}, \beta, \gamma)$ can be described as follows. The sensor's associated Cartesian coordinate system is first shifted from the reference coordinate system in the 3-D world space with its origin settled at $(\tilde{x}, \tilde{y}, \tilde{z})$ in the reference coordinate system. Then, it is rotated with the rotation angles β and γ being the same as Euler angles (Shu and Shi 1991, Shi et al. 1994). [Figure 11.1](#) shows the reference coordinate system and an arbitrary Cartesian coordinate system (indicating an arbitrary sensor position). There, oxy and $o'x'y'$ represent, respectively, the related image planes.

Assume now a world point P in the 3-D space that is projected onto the image plane as a pixel with the coordinates x_p and y_p . Then, x_p and y_p are also dependent on t and \bar{s} . That is, the coordinates of the pixel can be denoted by $x_p = x_p(t, \bar{s})$ and $y_p = y_p(t, \bar{s})$. So generally speaking, we have

$$g = g(x_p(t, \bar{s}), y_p(t, \bar{s}), t, \bar{s}) \quad (11.3)$$

As far as temporal image sequences are concerned, let us take a look at the framework of Pratt (1979) and Horn and Schunck (1980). There, $g = g(x_p(t), y_p(t), t)$ is actually a special case of Equation (11.3), i.e.,

$$g = g(x_p(t, \bar{s} = \text{constant vector}), y_p(t, \bar{s} = \text{constant vector}), t, \bar{s} = \text{constant vector})$$

**FIGURE 11.1**

Two sensors' position $\bar{s} = (0,0,0,0,0)$ and $\tilde{s} = (\tilde{x},\tilde{y},\tilde{z},\beta,\gamma)$.

In other words, the variation of \bar{s} is restricted to be zero, i.e., $\Delta \bar{s} = 0$. This means the sensor is fixed in a certain position in the 3-D world space.

Obviously, an alternative is to define the imaging space as a set of all temporal image sequences, i.e., those taken by sensors located at all possible positions in the 3-D world space. Stereo image sequences can thus be viewed as a proper subset of the imaging space, just like a stereo pair of images can be considered as a proper subset of a spatial image sequence.

In summary, the imaging space is a collection of all possible forms assumed by the general brightness function $g(x, y, t, \bar{s})$. Each picture, taken by a sensor located on a particular position at a specific moment, is merely a special cross-section of this imaging space. Both temporal and spatial image sequences are special proper subsets of the imaging space. They are in the middle level, between the imaging space and the individual images. This hierarchical structure is depicted in Figure 11.2.

Before we conclude this section, we should discuss the relationship between image sequences and video sequences. It is noted that the term *video* is used very often nowadays in addition to the terms *image frames* and *image sequence*. It is necessary to pause for a while to discuss the relationship between these terms. Image frames and image sequence have been defined clearly above with the introduction of the concept of the imaging space. Video can mean an individual video frame or video sequences. It refers, however, to those frames and sequences that are associated with the visible frequency band in the electromagnetic spectrum. For image frames and image sequences, there is no such restriction. For instance, infrared image frames and sequences correspond to a band outside the visible band in the spectrum. From this point of view, the scope of image frames and sequences

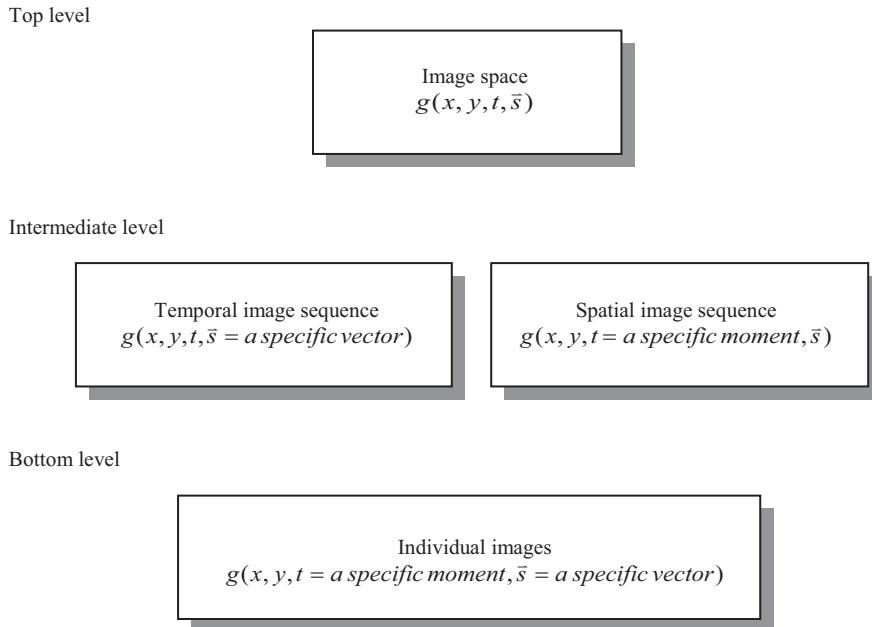


FIGURE 11.2
A hierarchical structure.

is wider than that of video frames and sequences. When the visible band is concerned, the terms *image frame and sequence* are interchangeable with that *video frame and sequence*.

Another point we would like to bring to readers' attention is as follows. Though video is referred to as visual information, which includes both a single frame and frame sequences, in practice it is often used to mean sequences exclusively. Such an example can be found in a book entitled *Digital Video Processing* by Tekalp (1995).

In this book, we use *image compression* to indicate still image compression, and *video compression* to indicate video sequence compression. Readers should keep in mind, however, that first, video can mean a single frame or sequences of frames; second, the scope of image is wider than that of video, and video is more pertinent to multimedia engineering.

11.2 Interframe Correlation

As far as video compression is concerned, all the techniques discussed in the previous chapters are applicable. By this we mean two classes of techniques. The first class, which is also the most straightforward way to handle video compression, is to code each frame separately. That is, individual frames are coded independently on each other. For instance, using a JPEG compression algorithm to code each frame in a video sequence results in *motion JPEG* (Westwater and Furht 1997). In the second class, methods utilized for still image coding can be generalized for video compression. For instance, discrete cosine transform (DCT) coding can be generalized and applied to video coding by extending 2-D DCT to 3-D DCT. That is, instead of 2-D DCT, say, 8 x 8, applied to a single image frame,

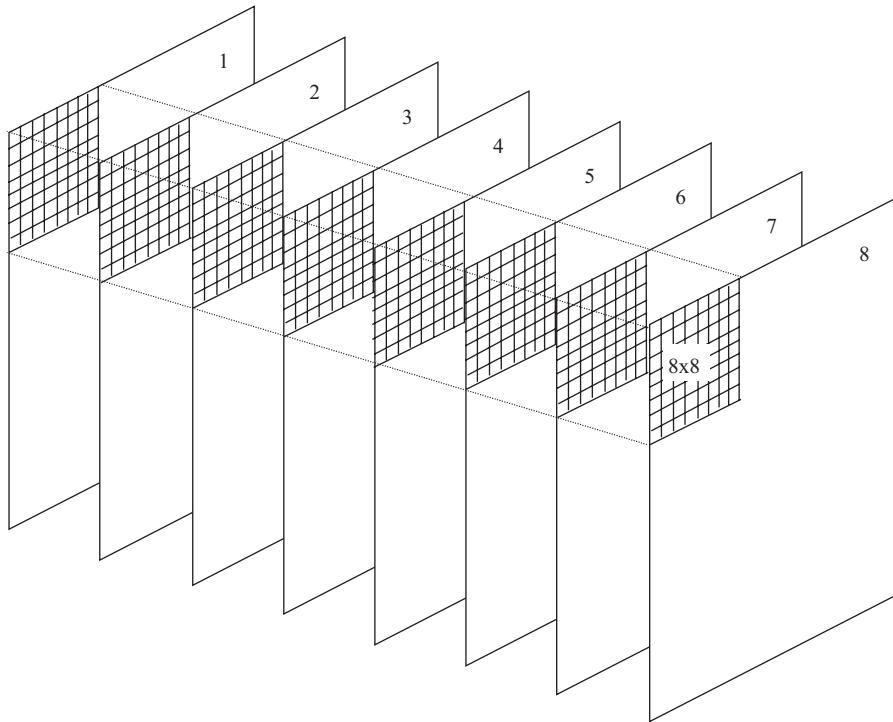
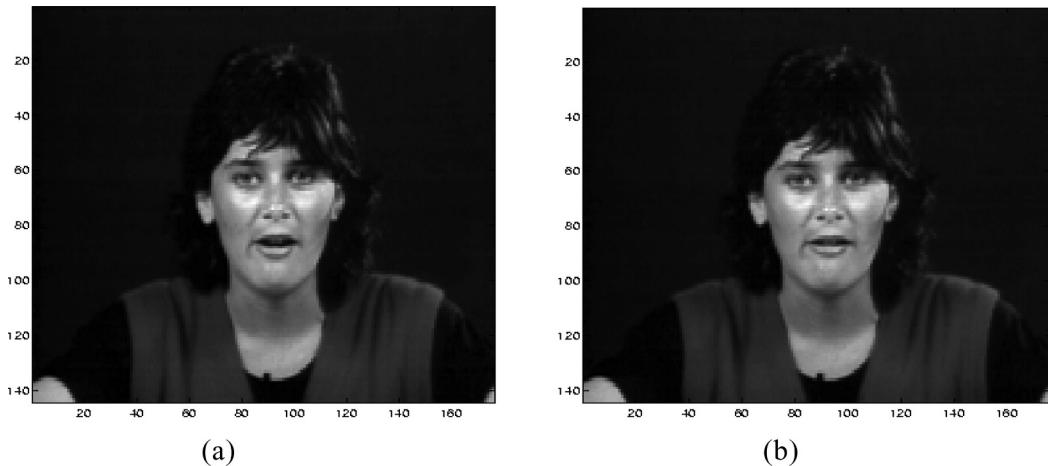


FIGURE 11.3
3-D DCT of $8 \times 8 \times 8$.

we can apply 3-D DCT, say, $8 \times 8 \times 8$, to a video sequence. Refer to Figure 11.3. That is, eight blocks of 8×8 each located, respectively, at the same position in one of the eight successive frames from a video sequence are coded together with the 3-D DCT. It was reported that this 3-D DCT technique is quite efficient (Lim 1990, Westwater and Furht 1997). In addition, the DPCM technique and the hybrid technique can be generalized and applied to video compression in a similar fashion (Jain 1989, Lim 1990). It is noted that in the second class of techniques several successive frames are grouped and coded together, while in the first class each frame is coded independently.

Video compression has its own characteristics, however, that make it quite different from still image compression. The major difference lies in the exploitation of interframe correlation that exists between successive frames in video sequences in addition to the intraframe correlation that exists within each frame. As mentioned in Chapter 1, the interframe correlation is also referred to as *temporal redundancy*, while the intraframe correlation is referred to as *spatial redundancy*. In order to achieve coding efficiency, we need to remove these redundancies for video compression. To do so, we must first understand these redundancies.

Consider a video sequence taken in a videophone service. There, the camera is static most of the time. A typical scene is a head-and-shoulder view of a person imposed on a background. In this type of video sequence, the background is usually static. Only the speaker is experiencing motion, which is not severe. Therefore, there is a strong similarity between successive frames, that is, a strong adjacent-frame correlation. In other words, there is a strong interframe correlation. It was reported in Mounts (1969) that when using

**FIGURE 11.4**

Two frames of the Miss America sequence (a) Frame 24 and (b) Frame 25.

videophone-like signals with moderate motion in the scene, on average, less than one-tenth of the elements change between frames by an amount that exceeds one percent of the peak signal. Here, a one-percent change is regarded as significant. Our experiment on the first 40 frames of the “Miss America” sequence supports this observation. Two successive frames of the sequence, frames 24 and 25, are shown in [Figure 11.4](#).

Now, consider a video sequence generated in a television broadcast. It is well known that television signals are generated with a scene scanned in a particular manner in order to maintain a steady picture for a human being to view regardless of whether there is a scenery change or not. That is, even if there is no change from one frame to the next, the scene is still scanned constantly. Hence there is a great deal of frame-to-frame correlation (Haskell et al. 1972b, Netravali and Robbins 1979). In TV broadcasts, the camera is most likely not static, and it may be panned, tilted, and zoomed. Furthermore, more movement is involved in the scene. As long as the TV frames are taken densely enough, then most of the time we think the changes between successive frames are due mainly to the apparent motion of the objects in the scene, that takes place during the frame intervals. This implies that there is also a high correlation between sequential frames. In other words, there is an interframe redundancy (interpixel redundancy between pixels in successive frames). There is more correlation between television picture elements along the frame-to-frame temporal dimension than there is between adjacent elements in a single frame along the spatial dimension. That is, there is generally more interframe correlation than intraframe correlation. Taking advantage of the interframe correlation, i.e., eliminating or decreasing the uncertainty of successive frames, leads to video data compression. This is analog to the case of still image coding with the DPCM technique, where we can predict part of an image by knowing the other part. Now the knowledge of the previous frames can remove the uncertainty of the next frame. In both cases, knowledge of the past removes the uncertainty of the future, leaving less actual information to be transmitted (Kretzmer 1952). In [Chapter 16](#), we will see that the words “past” and “future” used here are not necessary. They can be changed, respectively, to “some frames” and “some other frames” in advanced video coding techniques such as MPEG. There, a frame might be predicted from both its previous frames and its future frames.

At this point, it becomes clear that the second class of techniques (mentioned at the beginning of this section), which generalizes techniques originally developed for still image coding and applies them to video coding, exploits interframe correlation. For instance, in the case of the 3-D DCT technique, a strong temporal correlation causes an energy compaction within the low temporal frequency region. The 3-D DCT technique drops transform coefficients associated with high temporal frequency, thus achieving data compression.

The two techniques specifically developed to exploit interframe redundancy, i.e., frame replenishment and motion-compensated coding, are introduced below. The former is the early work, while the latter is the more popular recent work.

11.3 Frame Replenishment

As mentioned in [Chapter 3](#), frame-to-frame redundancy has long been recognized in TV signal compression. The first few experiments of a frame sequence coder exploiting interframe redundancy may be traced back to the 1960s (Seyler 1962, 1965, Mounts 1969). In Mounts (1969) the first real demonstration was presented and was termed *conditional replenishment*. This frame-replenishment technique can be briefly described as follows. Each pixel in a frame is classified into *changing* or *unchanging* areas depending on whether or not the intensity difference between its present value and its previous one (the intensity value at the same position on the previous frame) exceeds a threshold. If the difference does exceed the threshold, i.e., a *significant* change has been identified, the address and intensity of this pixel are coded and stored in a buffer and then transmitted to the receiver to replenish intensity. For those unchanging pixels, nothing is coded and transmitted. Their previous intensities are repeated in the receiver. It is noted that the buffer is utilized to make the information presented to the transmission channel occur at a smooth bit rate. The threshold is to make the average replenishment rate match the channel capacity.

Since the replenishment technique only encodes those pixels whose intensity value has changed significantly between successive frames, its coding efficiency is much higher than the coding techniques, which encode every pixel of every frame, say, the DPCM technique applied to each single frame. In other words, utilizing interframe correlation, the replenishment technique achieves a lower bit rate, while keeping the equivalent reconstructed image quality.

Much effort had been made to further improve this type of simple replenishment algorithm. As mentioned in the discussion of 3-D DPCM in [Chapter 3](#), for instance, it was soon realized that intensity values of pixels in a changing area need not be transmitted independently on one another. Instead, using both spatial and temporal neighbors' intensity values to predict the intensity value of a changing pixel leads to a *frame-difference* predictive coding technique. There, the differential signal is coded instead of the original intensity values, thus achieving a lower bit rate. For more detail, readers are referred to [Section 3.5.2](#). Another example of the improvements is that measures have been taken to distinguish the intensity difference caused by noise from those associated with changing to avoid the dirty window effect, whose meaning is given in the next paragraph. For more detailed information on these improvements over the simple frame-replenishment technique, readers are referred to two excellent reviews (Haskell et al. 1972b, 1979).

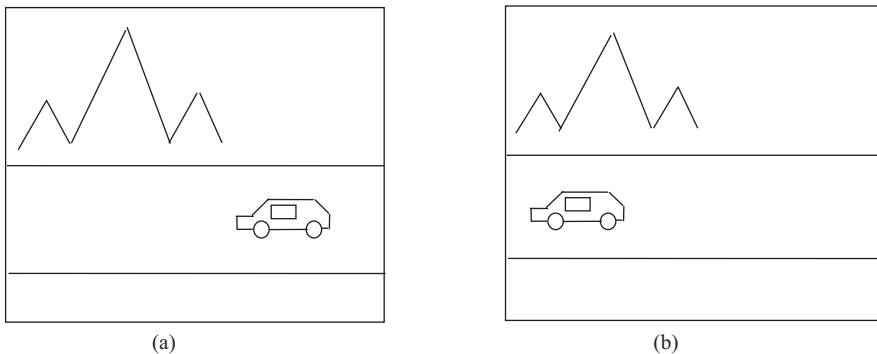


FIGURE 11.5
Dirty window effect.

The main drawback associated with the frame-replenishment technique is that it is difficult to handle frame sequences containing more rapid changes. When there are more rapid changes, the number of pixels whose intensity values need to be updated increases. In order to maintain the transmission bit-rate in a steady and proper level, the threshold has to be raised, thus causing many slow changes that cannot show up in the receiver. This poorer reconstruction in the receiver is somewhat analogous to viewing a scene through a dirty window. This is referred to as the dirty window effect. The result of one experiment on the dirty window effect is displayed in [Figure 11.5](#). From frame 22 to frame 25 of the "Miss America" sequence, there are 2166 pixels (less than 10% of the total pixels) that change their gray-level values by more than 1% of the peak signal. When we only update the gray-level values for 25% (randomly chosen) of these changing pixels, we can clearly see the dirty window effect. When rapid scene changes exceed a certain level, buffer saturation will result, causing picture breakup (Mounts 1969). Motion-compensated coding, which is discussed below, has been proved to be able to provide better performance than the replenishment technique in situations with rapid changes.

11.4 Motion-Compensated Coding

In addition to the frame-difference predictive coding technique (a variant of the frame-replenishment technique discussed above), another technique—displacement-based predictive coding—was developed at almost the same time (Rocca 1969, Haskell and Limb 1972a). In this technique, a motion model is assumed. That is, the changes between successive frames are considered due to the translation of moving objects in the image planes. Displacement vectors of objects are first estimated. Differential signals between the intensity value of the picture elements in the moving areas and that of their counterpart in the

**FIGURE 11.6**

Two consecutive frames of a video sequence (a) t_{n-1} and (b) t_n .

previous frame, which are translated by the estimated displacement, are encoded. This approach, which takes motion into account to compress video sequences, is referred to as motion-compensated predictive coding. It was found to be much more efficient than the frame-difference prediction technique.

To understand the above statement, let us take a look at the diagram shown in Figure 11.6. Assume a car translating from the right side to the left side in the image planes in a uniform speed during the time interval between the two consecutive image frames. Other than this, there are no movements or changes in the frames. Under this circumstance, if we know the displacement vector of the car on the image planes during the time interval between two consecutive frames, we can then predict the position of the car in the latter frame from its position in the former frame. One may think that if the translation vector is estimated well, then so is the prediction of the car position. This is true. In reality, however, estimation errors occurring in determination of the motion vector, which may be caused by various noises existing in the frames, may cause the predicted position of the car in the latter frame to differ from the actual position of the car in the latter frame.

This translational model is a very simple one; it cannot accommodate motions other than translation, say, rotation and camera zooming. Occlusion and disocclusion of objects make the situation even more complicated since in the occlusion case some portions of the images may disappear, while in the disocclusion case some newly exposed areas may appear. Therefore, the prediction error is almost inevitable. In order to have good-quality frames in the receiver, we can find the prediction error by subtracting the predicted version of the latter frame from the actual version of latter frame. If we encode both the displacement vectors and the prediction error, and transmit these data to the receiver, we may be able to obtain high-quality reconstructed images in the receiver. This is because in the receiving end, using the displacement vectors transmitted from the transmitter and the reconstructed former frame, we can predict the latter frame. Adding the transmitted prediction error to the predicted frame, we may reconstruct the latter frame with satisfactory quality. Furthermore, if manipulating the procedure properly, we are able to achieve data compression.

The displacement vectors are referred to as side or overhead information to indicate their auxiliary nature. It is noted that motion estimation drastically increases the computational complexity of the coding algorithm. In other words, higher coding efficiency is obtained in motion-compensated coding, but with a higher computational burden. As we pointed out in Section 10.1, this is both technically feasible and economically desired

since the cost of digital signal processing decreases much faster than that of transmission (Dubois et al. 1981).

Motion-compensated video compression has been a major development in coding since then. For more information, readers should refer to several excellent survey papers (Musmann et al. 1985, Zhang et al. 1995, Kunt 1995).

The common practice of motion-compensated coding in video compression can be split into the following three stages. First is the *motion analysis* stage, in which displacement vectors for either every pixel or a set of pixels in image planes from sequential images are estimated. Second, the present frame is predicted by using estimated motion vectors and the previous frame. The prediction error is then calculated. This stage is called *prediction and differentiation*. The third stage is *encoding*. The prediction error (difference between the present and the predicted present frames) and the motion vectors are encoded. Through an appropriate manipulation, the total amount of data for both the motion vectors and prediction error is expected to be much less than the raw data existing in the image frames, thus resulting in data compression. A block diagram of motion-compensated coding is shown in [Figure 11.7](#).

Before leaving this section, we compare the frame-replenishment technique with the motion-compensated coding technique. Qualitatively speaking, we see from the above discussion that the replenishment technique is also a kind of predictive coding in nature. This is particularly true if we consider the frame-difference predictive technique used in frame replenishment. There, it uses a pixel's intensity value in the previous frame as an estimator of its intensity value in the present frame. Now let's take a look at motion-compensated coding. Consider a pixel on the present frame. Through motion analysis, the motion-compensated technique finds its counterpart in the previous frame. That is, a pixel in the previous frame is identified such that it is supposed to translate to the position on the present frame of the pixel under consideration during the time interval between successive frames. This counterpart's intensity value is used as an estimator of that of the pixel under consideration. Therefore, we can see the model used for motion-compensated coding is much more advanced than that used for frame replenishment, so it achieves much higher coding efficiency. A motion-compensated coding technique that utilized the first pel-recursive algorithm for motion estimation (Netravali and Robbins 1979) was reported

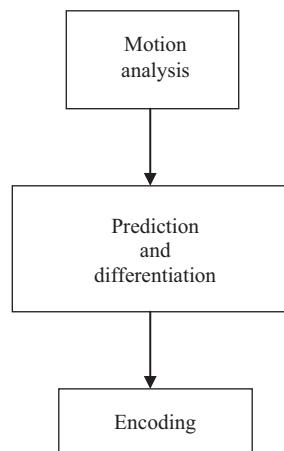


FIGURE 11.7

Block diagram of motion-compensated coding.

to achieve a bit rate 22%–50% lower than that obtained by simple frame-difference prediction, a version of frame replenishment.

The more advanced model utilized in motion-compensated coding, on the other hand, leads to higher computational complexity. Consequently, both the coding efficiency and the computational complexity in motion-compensated coding are higher than that in frame replenishment.

11.5 Motion Analysis

As discussed above, we usually conduct motion analysis in video sequence compression. There, 2-D displacement vectors of a pixel or a group of pixels on image planes are estimated from given image frames. Motion analysis can be viewed from a much broader point of view. It is well-known that the vision systems of both human beings and animals observe the outside world to ascertain motion and to navigate themselves in the 3-D world space. Two groups of scientists study vision. Scientists in the first group, including psychophysicists, physicians, and neurophysiologists, study human and animal vision. Their goal is to understand biological vision systems—their operation, features, and limitations. Computer scientists and electrical engineers form the second group. As pointed out in Aggarwal and Nandhakumar (1988), their ultimate goal is to develop computer vision systems with the ability to navigate, recognize and track objects, and estimate their speed and direction. Each group benefits from the research results of the other group. The knowledge and results of research in psychophysics, physiology, and neurophysiology have influenced the design of computer vision systems. Simultaneously, the research results achieved in computer vision have provided a framework in modeling biological vision systems and have helped in remedying faults in biological vision systems. This process will continue to advance research in both groups, hence benefiting human beings.

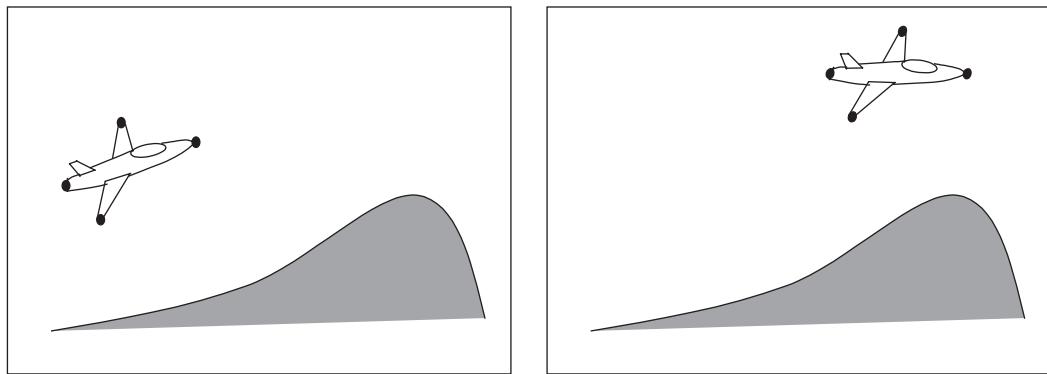
11.5.1 Biological Vision Perspective

In the field of biological vision, most scientists consider motion perception as a two-step process, even though there is no ample biological evidence to support this view (Singh 1991). The two steps are measurement and interpretation. The first step measures the 2-D motion projected on the imaging surfaces. The second step interprets the 2-D motion to induce the 3-D motion and structure on the scene.

11.5.2 Computer Vision Perspective

In the field of computer vision, motion analysis from image sequences is traditionally split into two steps. In the first step, intermediate variables are derived. By *intermediate variables*, we mean 2-D motion parameters in image planes. In the second step, 3-D motion variables, say, speed, displacement, position, and direction, are determined.

Depending on the different intermediate results, all approaches to motion analysis can be basically classified into two categories: feature correspondence and optical flow. In the former category, a few distinct features are first extracted from image frames. For instance, consider an image sequence containing an aircraft. Two consecutive frames are shown in Figure 11.8. The head and tail of the aircraft, and the tips of its wings, may be chosen as

**FIGURE 11.8**

Feature exaction and correspondence from two consecutive frames in a temporal image sequence.

features. The correspondence of these features on successive image frames needs to be established. In the second step, 3-D motion can then be analyzed from the extracted features and their correspondence in successive frames. In the latter category of approaches, the intermediate variables are optical flow. An optical flow vector is defined as a velocity vector of a pixel on an image frame. An optical flow field is referred to as the collection of the velocity vectors of all the pixels on the frame. In the first step, optical flow vectors are determined from image sequences as the intermediate variables. In the second step, 3-D motion is estimated from optical flow. It is noted that optical flow vectors are closely related to displacement vectors in that a velocity vector multiplying by the time interval between two consecutive frames results in the corresponding displacement vector. Optical flow and its determination will be discussed in detail in [Chapter 13](#).

It is noted that there is a so-called direct method in motion analysis. Contrary to the above optical flow approach, instead of determining 2-D motion variables (i.e., the intermediate variables), prior to 3-D motion estimation, the direct method attempts to estimate 3-D motion without explicitly solving for the intermediate variables. In Huang and Tsai (1981b) the equation characterizing displacement vectors in the 2-D image plane and the equation characterizing motion parameters in 3-D world space are combined so that the motion parameters in 3-D world space can be directly derived. This method has been utilized to recover structure (object surfaces) in 3-D world space as well (Negahdaripour and Horn 1987, Horn and Weldon 1988, Shu and Shi 1993). The direct method has certain limitations. That is, if the geometry of object surfaces is not known in advance, then the method fails.

The feature correspondence approach is sometimes referred to as the discrete approach, while the optical flow approach is sometimes referred to as the continuous approach. This is because the correspondence approach concerns only a set of relatively sparse but highly discriminatory 2-D features on image planes. The optical flow approach is concerned with a dense field of motion vectors.

It has been found that both feature extraction and correspondence establishment are not trivial tasks. Occlusion and disocclusion, which, respectively, cause some features to disappear and some features to reappear, make feature correspondence even more difficult. The development of robust techniques to solve the correspondence problem is an active research area and is still in its infancy. So far, only partial solutions suitable for simplistic situations have been developed (Aggarwal and Nandhakumar 1988). Hence, the feature

correspondence approach is rarely used in video compression. Because of this, we will not discuss this approach any further.

Motion analysis (sometimes referred to as motion estimation or motion interpretation) from image sequences is necessary in automated navigation. It has played a central role in the field of computer vision since the late 1970s and early 1980s. A great number of papers presented at the International Conference on Computer Vision cover this and related topics. Many workshops, symposiums, and special sessions are organized around this subject (Thompson 1989).

11.5.3 Signal Processing Perspective

In the field of signal processing, motion analysis is mainly considered in the context of bandwidth reduction and/or data compression in the transmission of visual signals. Therefore, instead of the motion in 3-D world space, only the 2-D motion in the image plane is concerned.

Because of the real-time nature in visual transmission, the motion model cannot be very complicated. So far, the 2-D translational model is most frequently assumed in the field. In the 2-D translational model it is assumed that the change between a frame and its previous one is due to the motion of objects in the frame plane during the time interval between two consecutive frames. In many cases, as long as frames are taken densely enough, this assumption is valid. By *motion analysis* we mean the estimation of translational motion—either the displacement vectors or velocity vectors. With this kind of motion analysis, one can apply the motion-compensated coding discussed above, making coding more efficient.

Basically, there are three techniques in 2-D motion analysis: correlation, recursive, and differential techniques. Philosophically speaking, the first two techniques belong to the same group: region matching.

Refer to [Figure 11.6](#), where the moving car is the object under investigation. By *motion analysis*, we mean finding the displacement vector, i.e., a vector representing the relative positions of the car in the two consecutive frames. With region matching, one may consider the car (or a portion of the car) as a region of interest and seek the best matching between the two regions in the two frames: specifically, the region in the present frame and the region in the previous frame. For identifying the best matching, two techniques, the correlation and recursive methods, work differently in methodology. The correlation technique finds the best matching by searching the maximum correlation between the two regions in a predefined search range, while the recursive technique estimates the best matching by recursively minimizing a nonlinear measure of the dissimilarity between the two regions.

A couple of comments are in order. First, it is noted that the most frequently used technique in motion analysis is called block matching, which is a type of the correlation technique. There, a video frame is divided into non-overlapped rectangular blocks with each block having the same size, usually 16 by 16. Each block thus generated is assumed to move as one, i.e., all pixels in a block share the same displacement vector. For each block, we find its best matching in the previous frame with correlation. That is, the block in the previous frame, which gives the maximum correlation, is identified. The relative position of these two best-matched blocks produces a displacement vector. This block-matching technique is simple and very efficient, and will be discussed in detail in [Chapter 12](#). Second, as multimedia finds more and more applications, the regions occupied by arbitrary-shaped objects (no longer always rectangular blocks) become increasingly important in content-based video retrieval and manipulation. Motion analysis in this case is discussed in [Chapter 18](#).

Third, although the recursive technique is categorized as a region-matching technique, it may be used for finding displacement vectors for individual pixels. In fact, the recursive technique was originally developed for determining displacement vectors of pixels and, hence, it is called pel-recursive. This technique is discussed in [Chapter 12](#). Fourth, both correlation and recursive techniques can be utilized for determining optical flow vectors. Optical flow is discussed in [Chapter 13](#).

The third technique in 2-D motion analysis is the differential technique. This is one of the main techniques utilized in determining optical flow vectors. It is named after the term of differential because it uses the partial differentiation of an intensity function with respect to the spatial coordinates x and y , as well as the temporal coordinate t . This technique is also discussed in [Chapter 13](#).

11.6 Motion Compensation for Image Sequence Processing

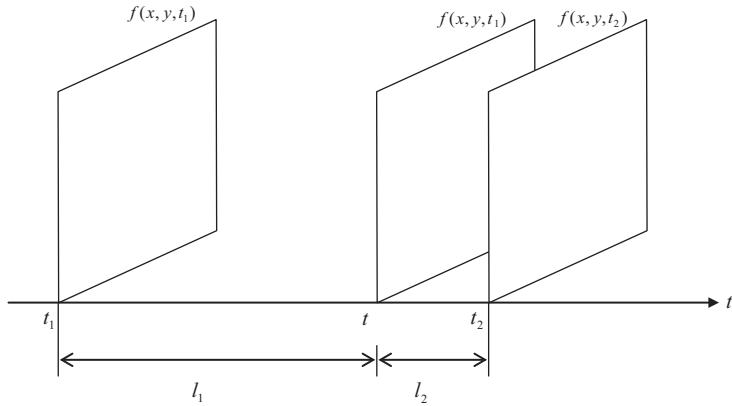
Motion analysis has long been considered a key issue in image sequence processing (Huang 1981a, Shi 1998). Obviously, in an area like automated navigation, motion analysis plays a central role. From the discussion in this chapter, we see that motion analysis also plays a key role in video data compression. Specifically, we have discussed the concept of motion-compensated video coding in [Section 11.4](#). In this section we would like to consider motion compensation for image sequence processing, in general. Let us first consider motion-compensated interpolation. Then, we will discuss motion-compensated enhancement, restoration, and down-conversion.

11.6.1 Motion-Compensated Interpolation

Interpolation is a simple yet efficient and important method in image and video compression. In image compression, we may only transmit, say, every other row. We then try to interpolate these missing rows from the other half transmitted rows in the receiver. In this way, we compress the data to half. Since the interpolation is carried out within a frame, it is referred to as *spatial* interpolation. In video compression, for instance, in videophone service, instead of transmitting 30 frames per second, we may choose a lower frame rate, say, 10 frames per second. In the receiver, we may try to interpolate the dropped frames from the transmitted frames. This strategy immediately drops the transmitted data to one third. Another example is the conversion of a motion picture into a National Television System Commission (NTSC) TV signal. There, every first frame in the motion picture is repeated three times and the next frame twice, thus converting a 24-frame-per-second motion picture to a 60-field-per-second NTSC signal. This is commonly referred to as 3:2 pulldown. In these two examples concerning video, interpolation is along the temporal dimension, which is referred to as *temporal* interpolation.

For basic concepts of zero-order interpolation, bilinear interpolation, and polynomial interpolation, readers are referred to signal processing texts, for instance (Lim 1990). In temporal interpolation, the zero-order interpolation means creation of a frame by copying its nearest frame along the time dimension. The conversion of a 24-frame-per-second motion picture to a 60-field-per-second NTSC signal can be classified into this type of interpolation. Weighted linear interpolation can be illustrated with [Figure 11.9](#).

There, the weights are determined according to the lengths of time intervals, which is similar to the bilinear interpolation widely used in spatial interpolation, except that here

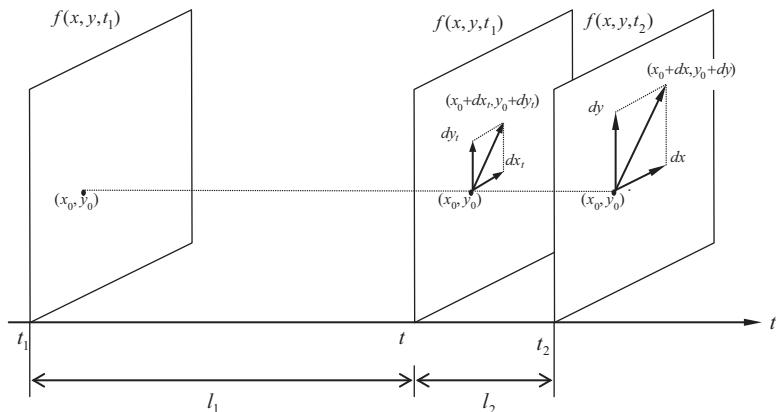
**FIGURE 11.9**

Weighted linear interpolation.

only one index (along the time axes) is used, while two indexes (along two spatial axes) are used in spatial bilinear interpolation. That is,

$$f(x, y, t) = \frac{l_2}{l_1 + l_2} f(x, y, t_1) + \frac{l_1}{l_1 + l_2} f(x, y, t_2) \quad (11.4)$$

If there are one or multiple moving objects existing in successive frames, however, the weighted linear interpolation will blur the interpolated frames. Taking motion into account in the interpolation results in motion-compensated interpolation. In Figure 11.10, we still use three frames shown in Figure 11.9 to illustrate the concept of motion-compensated interpolation. First, motion between two given frames is estimated. That is, the displacement vectors for each pixel are determined. Second, we choose a frame that is nearer to the frame we want to interpolate. Third, the displacement vectors determined in the first step are proportionally converted to the frame to be created. Each pixel in this frame is

**FIGURE 11.10**

Motion-compensated interpolation.

projected via the determined motion trajectory to the frame chosen in step 2. In the process of motion-compensated interpolation, spatial interpolation in the frame chosen in step 2 usually is needed.

11.6.2 Motion-Compensated Enhancement

It is well-known that when an image is corrupted by additive white Gaussian noise (AWGN) or burst noise, linear low-pass filtering such as simple averaging or nonlinear low-pass filtering such as a median filter performs well in removing the noise. When an image sequence is concerned, we may apply such types of filtering along the temporal dimension to remove noise. This is called temporal filtering. These types of low-pass filtering may blur images, an effect that may become quite serious when motion exists in image planes. The enhancement, which takes motion into account, is referred to as motion-compensated enhancement, and it was found very efficient in temporal filtering (Huang and Hsu 1981c).

To facilitate the discussion, we consider simple averaging as a means for noise filtering in what follows. It is understood that other filtering techniques are possible, and that everything discussed here is applicable there. Instead of simply averaging n successive image frames in a video sequence, motion-compensated temporal filtering will first analyze the motion existing in these frames. That is, we estimate the motion of pixels in successive frames first. Then averaging will be conducted only on those pixels along the same motion trajectory. In Figure 11.11, three successive frames are shown and denoted by $f(x, y, t_1)$, $f(x, y, t_2)$ and $f(x, y, t_3)$, respectively. Assume that three pixels, denoted by (x_1, y_1) , (x_2, y_2) and (x_3, y_3) , respectively, are identified to be perspective projections of the same object point

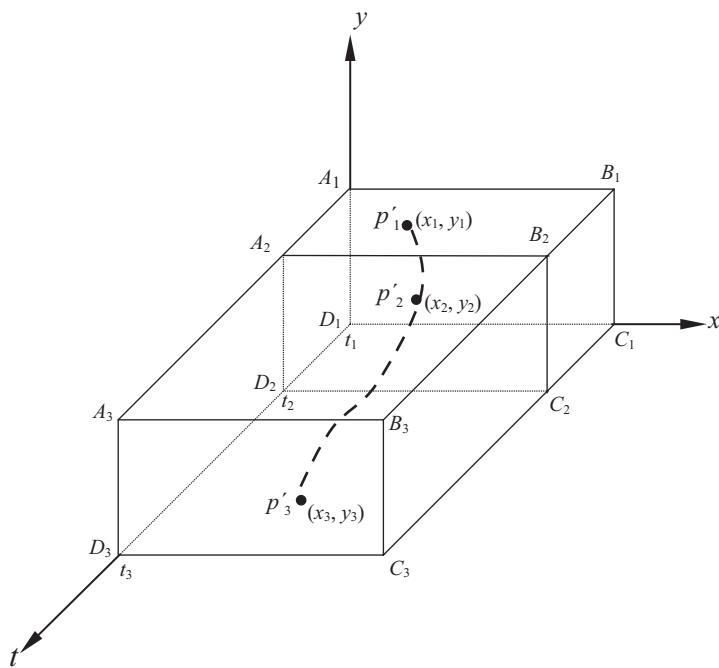


FIGURE 11.11

Motion-compensated temporal filtering.

in the 3-D world space on the three frames. The averaging is then applied to these three pixels. It is noted that the number of successive frames, n , may not necessarily have to be three. Motion analysis can be any one of several techniques discussed in [Section 11.5](#). Motion-compensated temporal filtering is not necessarily implemented pixelwise; it can also be objectwise or regionwise.

11.6.3 Motion-Compensated Restoration

Extensive attention has been paid to the restoration of full-length feature films. There, typical artifacts are due to dirt and sparkle. Early work in the detection of these artifacts ignored motion information completely. Late motion estimation has been utilized to detect these artifacts based on the assumption that the artifacts occur occasionally along the temporal dimension. Once the artifacts have been found, motion-compensated temporal filtering and/or interpolation will be used to remove the artifacts. One successful algorithm for the detection and removal of anomalies in digitized animation film can be found in Tom et al. (1998).

11.6.4 Motion-Compensated Down-Conversion

Here, we present one more example in which motion compensation finds application in digital video processing.

It is believed that there will be a need to down-convert a high-definition television (HDTV) image sequence for display onto an NTSC monitor during the upcoming transition to digital television broadcast. The most straightforward approach is to fully decode the image sequence first, then apply a prefiltering and sub-sampling process to each field of the interlaced sequence. This is referred to as a full-resolution decoder (FRD). The merit of this approach is the high quality achieved, while the drawback is a high cost in terms of the large amount of memory required to store the reference frames. To reduce the required memory space, another approach is considered. In this approach, the down-conversion is conducted within the decoding loop and is referred to as a low-resolution decoder (LRD). It can significantly reduce the required memory and still achieve a reasonably good picture quality.

The prediction drift is a major type of artifact existing in the down-conversion. It is defined as the successive blurring of forward-predicted frames with a group of pictures. It is caused mainly by non-ideal interpolation of sub-pixel intensities and the loss of high-frequency data within the block. An optimal set of filters to perform low-resolution motion compensation has been derived to effectively minimize the drift. For details on an algorithm in the down-conversion utilizing an optimal motion compensation scheme, readers are referred to Vetro and Sun (1998).

11.7 Summary

After Part 2, still image compression, we shift our attention to video compression. Prior to Part 4, where we discuss various video compression algorithms and standards; however, we first address the issue of motion analysis and motion compensation in this chapter that starts Part 3, motion estimation and compensation. This is because video compression has

its own characteristics, which are different from that of still image compression. The main difference lies in interframe correlation.

In this chapter, the concept of various image sequences is discussed in a broad scope. In doing so, a single image, temporal image sequences, and spatial image sequences are all unified under the concept of imaging space. The redundancy between pixels in successive frames is analyzed for both video conferencing and TV broadcast cases. In these applications, there is more interframe correlation than intraframe correlation in general. Therefore, the utilization of interframe correlation becomes a key issue in video compression.

There are two major techniques in exploitation of interframe correlation: frame replenishment and motion compensation. In the conditional replenishment technique, only those pixels' gray-level values, whose variation from their counterparts in the previous frame exceeds a threshold, are encoded and transmitted to the receiver. These pixels are called changing pixels. For those other than the changing pixels, their gray values are just repeated in the receiver. This simplest frame-replenishment technique achieves higher coding efficiency than coding each pixel in each frame due to utilization of interframe redundancy. In the more advanced frame-replenishment techniques, say, frame-difference predictive coding technique, both temporal and spatial neighboring pixels' gray values are used to predict that of a changing pixel. Instead of the intensity values of the changing pixels, the prediction error is encoded and transmitted. Because the variance of the prediction error is smaller than that of the intensity values, this more advanced frame-replenishment technique is more efficient than the conditional replenishment technique.

The main drawback of the frame-replenishment techniques is associated with rapid motion and/or intensity variation occurring on the image planes. Under these circumstances, frame replenishment will suffer from dirty window effect, and even buffer saturation.

In motion-compensated coding, the motion of pixels is first analyzed. Based on the previous frame and the estimated motion, the current frame is predicted. The prediction error together with motion vectors are encoded and transmitted to the receiver. Due to more accurate prediction based on motion model, motion-compensated coding achieves higher coding efficiency compared with frame replenishment. This is conceivable because frame replenishment basically uses the intensity value of a pixel in the previous frame to predict that of the pixel in the same location in the present frame, while the prediction in motion-compensated coding uses motion trajectory. This implies that higher coding efficiency is obtained in motion compensation at the cost of higher computational complexity. This is technically feasible and economically desired since the cost of digital signal processing decreases much faster than that of transmission.

Because of the real-time requirement in video coding, only simple 2-D translational model is used. There are mainly three types of motion analysis techniques used in motion-compensated coding. They are block matching, pel-recursion, and optical flow. By far, the block matching is used most frequently. These three techniques are discussed in detail in the following three chapters.

Motion compensation is also widely utilized in other tasks of digital video sequence processing. Examples include motion-compensated interpolation, motion-compensated enhancement, motion-compensated restoration, and motion-compensated down-conversion.

Exercises

- 11.1 Explain the analogy between a stereo image sequence versus the imaging space, and a stereo image pair versus the spatial image sequence, to which the stereo image pair belongs.
- 11.2 Explain why the imaging space can be considered as a unification of image frames, spatial image sequences, and temporal image sequences.
- 11.3 Give the definitions of the following concepts: image, image sequence, and video. Discuss the relation between them.
- 11.4 What feature causes video compression to be quite different from still image compression?
- 11.5 Describe the conditional replenishment technique. Why can it achieve higher coding efficiency in video coding than those techniques encoding each pixel in each frame?
- 11.6 Describe the frame-difference predictive coding technique. You may want to refer to [Section 3.5.2](#).
- 11.7 What is the main drawback of frame replenishment?
- 11.8 Both the frame-difference predictive coding and motion-compensated coding are predictive coding in nature.
 - a. What is the main difference between the two?
 - b. Explain why motion-compensated coding is usually more efficient.
 - c. What is the price paid for higher coding efficiency with motion-compensated coding?
- 11.9 Motion analysis is an important task encountered in both computer vision and video coding. What is the major different requirement for motion analysis in these two fields?
- 11.10 Work on the first 40 frames of a video sequence other than the “Miss America.” Determine, on an average basis, what percentages of the total pixels change their gray-level values by more than 1% of the peak signal between two consecutive frames.
- 11.11 Similar to the experiment associated with [Figure 11.5](#), do your own experiment to observe the dirty window effect. That is, work on two successive frames of a video sequence chosen by yourself, and only update a part of those changing pixels.
- 11.12 Take two frames from the “Miss America” sequence or from other sequence with your own choice, between which a relatively large motion is involved.
 - a. Using the weighted linear interpolation defined in Equation 11.4, create an interpolated frame, which is located in the 1/3 of the time interval from the second frame (i.e., $I_2 = \frac{1}{3}(I_1 + I_2)$ according to [Figure 11.9](#)).
 - b. Using motion-compensated interpolation, create an interpolated frame at the same position along the temporal dimension.
 - c. Compare the two interpolated frames and make your comments.

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12

Block Matching

As mentioned in the previous chapter, displacement vector measurement and its usage in motion compensation in interframe coding for a TV signal can be traced back to the 1970s. Netravali and Robbins (1979) developed a pel-recursive technique, which estimates the displacement vector for each pixel recursively from its neighboring pixels using an optimization method. Limb and Murphy (1975), Rocca and Zanoletti (1972), Cafforio and Rocca (1976), and Brofferio and Rocca (1977), developed techniques for estimation of displacement vectors of a block of pixels. In the latter approach, an image is first segmented into areas with each having an approximately uniform translation. Then, the motion vector is estimated for each area. The segmentation and motion estimation associated with these arbitrarily shaped blocks are very difficult. When there are multiple moving areas in images, the situation becomes more challenging. In addition to motion vectors, the shape information of these areas needs to be coded. Hence, when moving areas have various complicated shapes, both computational complexity and coding load will increase remarkably.

In contrast, the block-matching technique, which is the focus of this chapter, is simple, straightforward, and yet very efficient. It has been by far the most popularly utilized motion-estimation technique in video coding. In fact, it has been adopted by all the international video coding standards: ISO MPEG-1 and MPEG-2, and ITU H.261, H.263, and H.264. These standards will be introduced in detail in [Chapters 16 through 20](#), respectively.

It is interesting to note that nowadays, with the tremendous advancements in multimedia engineering, object-based and/or content-based manipulation of audiovisual information is very demanding, particularly in audiovisual data storage, retrieval, and distribution. The applications include digital library, video on demand, audiovisual database, and so on. Therefore, the coding of arbitrarily shaped objects has regained great research attention these days. It has been included in the MPEG-4 activities (Iscas 1997) and will be discussed in [Chapter 18](#).

In this chapter, various aspects of block matching are addressed. They include the concept and algorithm, matching criteria, searching strategies, limitations, and new improvements.

12.1 Non-overlapped, Equally Spaced, Fixed-Size, Small Rectangular Block Matching

To avoid the kind of difficulties encountered in motion estimation and motion compensation with arbitrarily shaped blocks, the block-matching technique was proposed by Jain and Jain (1981) based on the following simple motion model.

An image is partitioned into a set of nonoverlapped, equally spaced, fixed size, small rectangular blocks; and the translation motion within each block is assumed to be uniform. Although this simple model considers translation motion only, other types of motions, such as rotation and zooming of large objects, may be closely approximated by the piecewise translation of these small blocks provided that these blocks are small enough. This observation, originally made by Jain and Jain, has been confirmed again and again since then.

Displacement vectors for these blocks are estimated by finding their best-matched counterparts in the previous frame. In this manner, motion estimation is significantly easier than that for arbitrarily shaped blocks. Since the motion of each block is described by only one displacement vector, the side information on motion vectors decreases. Furthermore, the rectangular shape information is known to both the encoder and the decoder, and hence does not need to be encoded, which saves both computation load and side information.

The block size needs to be chosen properly. In general, the smaller the block size, the more accurate the approximation is. It is apparent, however, that the smaller block size leads to more motion vectors to be estimated and encoded, which means an increase in both computation and side information. As a compromise, a size of 16×16 is considered to be a good choice. (This has been specified in international video coding standards such as H.261, H.263, MPEG-1, and MPEG-2). Note that for finer estimation sometimes a block size of 8×8 is used.

Figure 12.1 is utilized to illustrate the block-matching technique. In **Figure 12.1a** an image frame at moment t_n is segmented into non-overlapped $p \times q$ rectangular blocks. As mentioned above, in common practice, square blocks of $p = q = 16$ are used most often. Consider one of the blocks centered at (x, y) . It is assumed that the block is

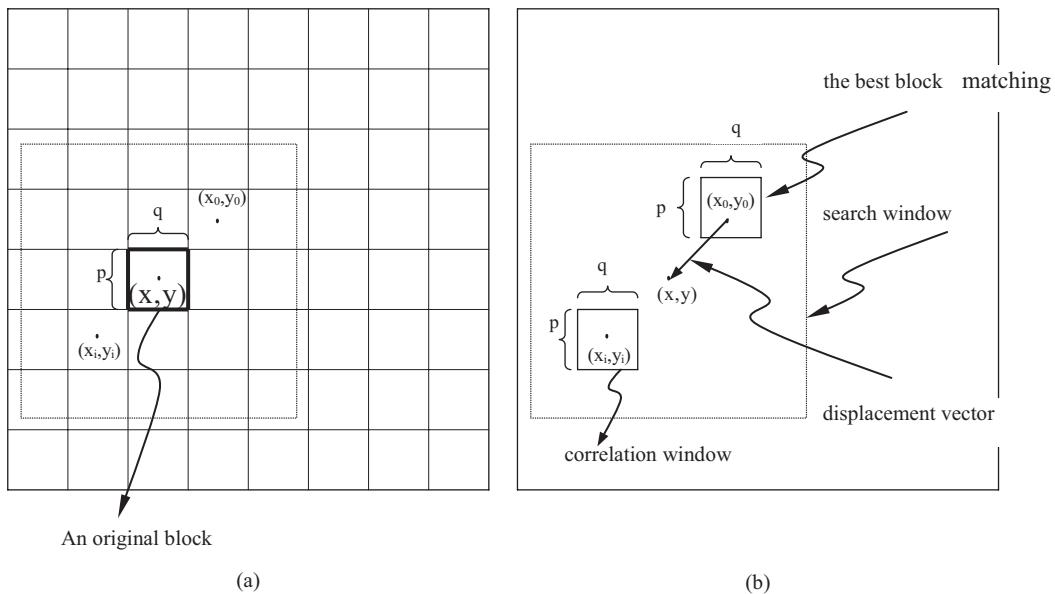


FIGURE 12.1
Block matching (a) t_n frame and (b) t_{n-1} frame.

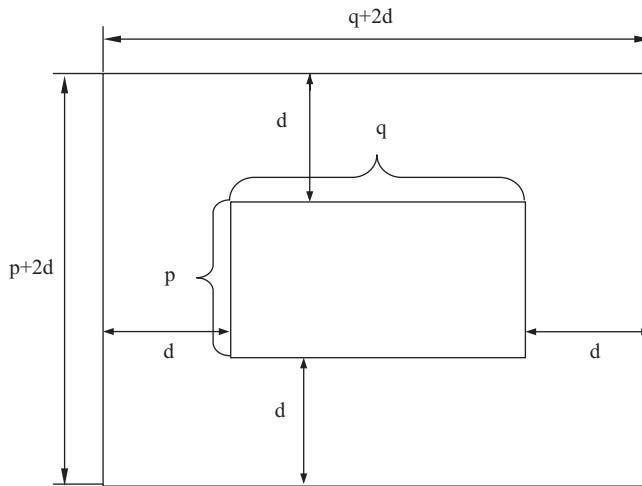


FIGURE 12.2
Search window and correlation window.

translated as a whole. Consequently, only one displacement vector needs to be estimated for this block. [Figure 12.1b](#) shows the previous frame: the frame at moment t_{n-1} . In order to estimate the displacement vector, a rectangular search window is opened in the frame t_{n-1} and centered at the pixel (x, y) . Consider a pixel in the search window: a rectangular correlation window of the same size $p \times q$ is opened with the pixel located in its center. A certain type of similarity measure (correlation) is calculated. After this matching process has been completed for all candidate pixels in the search window, the correlation window corresponding to the largest similarity becomes the best match of the block under consideration in frame t_n . The relative position between these two blocks (the block and its best match) gives the displacement vector. This is shown in [Figure 12.1b](#).

The size of the search window is determined by the size of the correlation window and the maximum possible displacement along four directions: upwards, downwards, rightwards, and leftwards. In [Figure 12.2](#) these four quantities are assumed to be the same and are denoted by d . Note that d is estimated from *a priori* knowledge about the translation motion, which includes the largest possible motion speed and the temporal interval between two consecutive frames, i.e., $t_n - t_{n-1}$.

12.2 Matching Criteria

Block matching belongs to image matching and can be viewed from a wider perspective. In many image processing tasks, we need to examine two images or two portions of images on a pixel-by-pixel basis. These two images or two image regions can be selected from a spatial image sequence, i.e., from two frames taken at the same time with two different sensors aiming at the same object, or from a temporal image sequence, i.e., from two

frames taken at two different moments by the same sensor. The purpose of the examination is to determine the similarity between the two images or two portions of images. Examples of this type of application include image registration (Pratt 1974) and template matching (Jain 1989). The former deals with spatial registration of images, while the latter extracts and/or recognizes an object in an image by matching the object template and a certain area of the image.

The similarity measure, or correlation measure, is a key element in the matching process. The basic correlation measure between two images t_n and t_{n-1} , $C(s, t)$, is defined as follows (Anuta 1969).

$$C(s, t) = \frac{\sum_{j=1}^p \sum_{k=1}^q f_n(j, k) f_{n-1}(j+s, k+t)}{\sqrt{\sum_{j=1}^p \sum_{k=1}^q f_n(j, k)^2} \sqrt{\sum_{j=1}^p \sum_{k=1}^q f_{n-1}(j+s, k+t)^2}}. \quad (12.1)$$

This is also referred to as a normalized two-dimensional cross-correlation function (Musmann et al. 1985).

Instead of finding the maximum similarity, or correlation, an equivalent yet more computationally efficient way of block matching is to find the minimum dissimilarity, or matching error. The dissimilarity (sometimes referred to as the error, distortion, or distance) between two images t_n and t_{n-1} , $D(s, t)$ is defined as follows.

$$D(s, t) = \frac{1}{lm} \sum_{j=1}^p \sum_{k=1}^q M(f_n(j, k), f_{n-1}(j+s, k+t)), \quad (12.2)$$

where $M(u, v)$ is a metric that measures the dissimilarity between the two arguments u and v . The $D(s, t)$ is also referred to as the matching criterion or the D values.

In the literature there are several types of matching criteria, among which the mean-square error (MSE) (Jain and Jain 1981) and mean absolute difference (MAD) (Koga et al. 1981) are used most often. It is noted that the sum of squared difference (SSD) (Anandan 1987) or the sum of squared error (SSE) (Chan 1990) is essentially the same as MSE. The MAD is sometimes referred to as the mean absolute error (MAE) in the literature (Nogaki 1992).

In the MSE matching criterion, the dissimilarity metric $M(u, v)$ is defined as

$$M(u, v) = (u - v)^2. \quad (12.3)$$

In the MAD,

$$M(u, v) = |u - v|. \quad (12.4)$$

Obviously, both criteria are simpler than the normalized two-dimensional cross-correlation measure defined in Equation 12.1.

Before proceeding to the next section, a comment on the selection of the dissimilarity measure is due. A study based on experimental works reported that the matching criterion does not significantly affect the search (Srinivasan and Rao 1984). The MAD is hence preferred due to its simplicity in implementation (Musmann et al. 1985).

12.3 Searching Procedures

Searching strategy is another important issue to deal with in block matching. Several searching strategies are discussed below.

12.3.1 Full Search

[Figure 12.2](#) shows a search window, a correlation window, and their sizes. In searching for the best matching, the correlation window is moved to each candidate position within the search window. That is, there are a total $(2d + 1) \times (2d + 1)$ positions that need to be examined. The minimum dissimilarity gives the best matching. Apparently, this full-search procedure is brute force in nature. While the full search delivers good accuracy in searching for the best matching (thus, good accuracy in motion estimation), a large amount of computation is involved.

In order to lower computational complexity, several fast searching procedures have been developed. They are introduced below.

12.3.2 2-D Logarithm Search

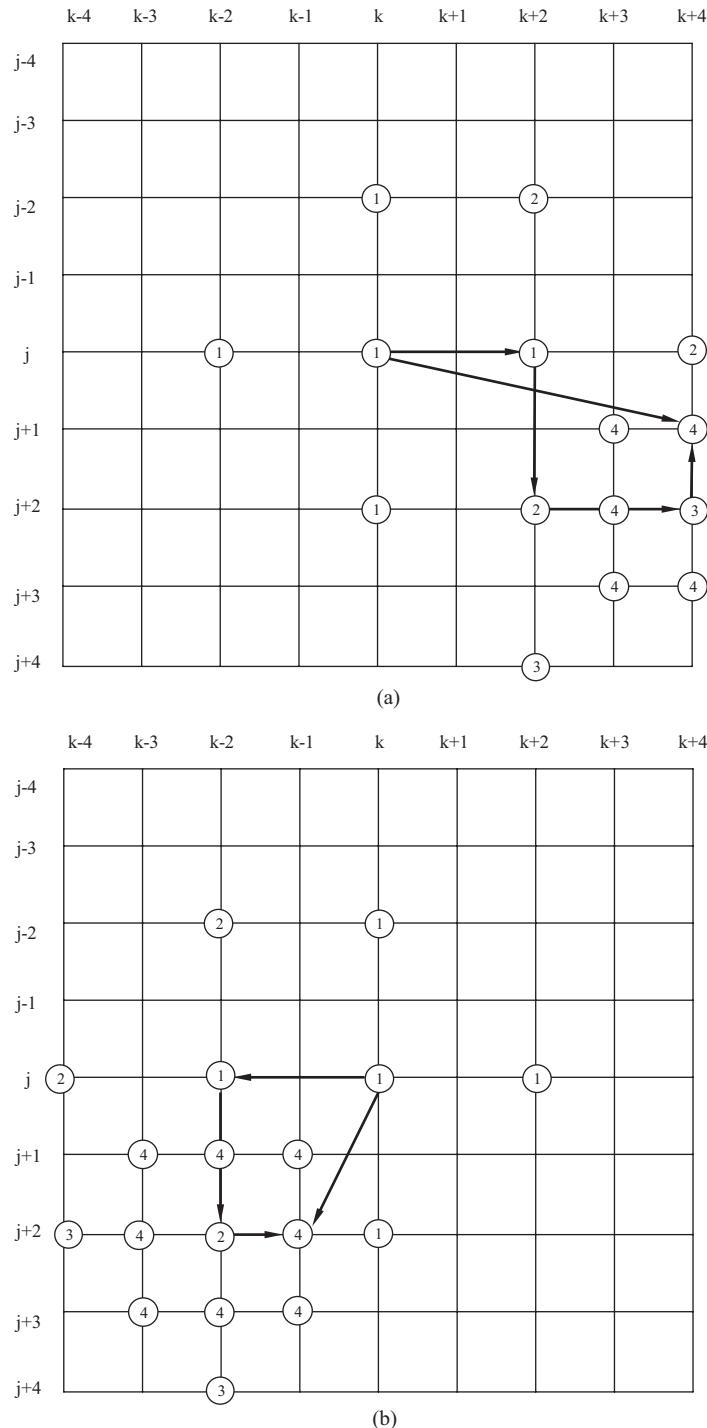
Jain and Jain developed a 2-D logarithmic searching procedure in [Jain and Jain \(1981\)](#). Based on a 1-D logarithm search procedure ([Knuth 1973](#)), the 2-D procedure successively reduces the search area, thus reducing the computational burden. The first step computes the matching criterion for five points in the search window. These five points are as follows: the central point of the search window and the four points surrounding it, with each being a midpoint between the central point and one of the four boundaries of the window. Among these five points, the one corresponding to the minimum dissimilarity is picked as the winner. In the next step, surrounding this winner, another set of five points are selected in a similar fashion to that in the first step, with the distances between the five points remaining unchanged. The exception takes place when either a central point of a set of five points or a boundary point of the search window gives a minimum D value. In these circumstances, the distances between the five points need to be reduced. The procedure continues until the final step, in which a set of candidate points are located in a 3×3 2-D grid. [Figure 12.3](#) demonstrates two cases of the procedure. [Figure 12.3a](#) shows that the minimum D value takes place on a boundary, while [Figure 12.3b](#) the minimum D value in the central position.

A convergence proof of the procedure is presented in [Jain and Jain \(1981\)](#), under the assumption that the dissimilarity monotonically increases as the search point moves away from the point corresponding to the minimum dissimilarity.

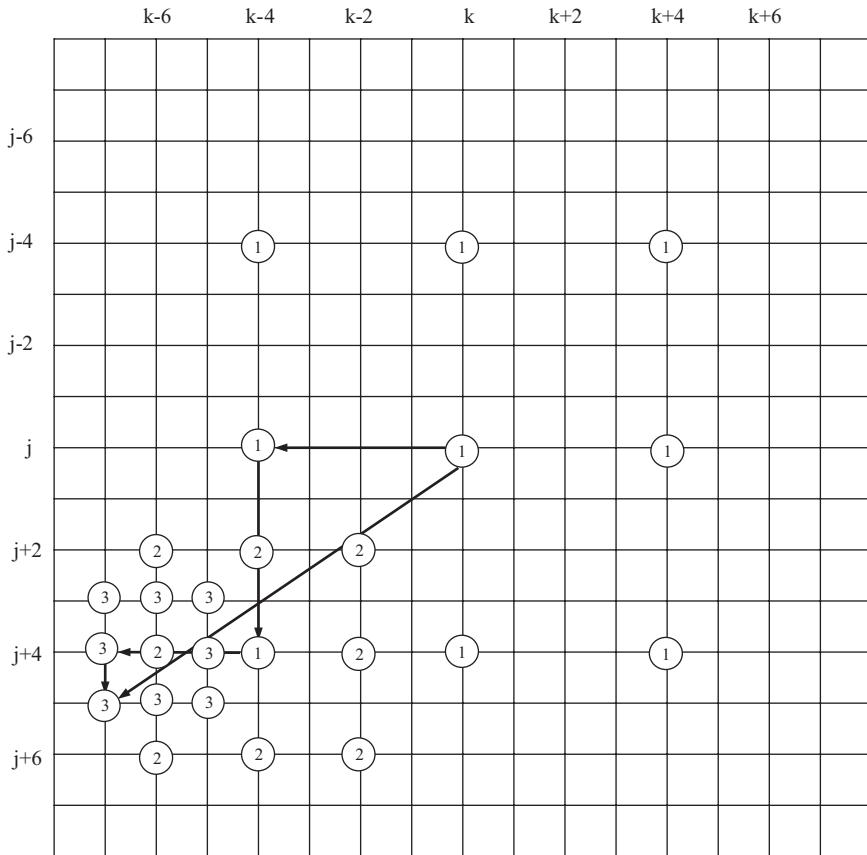
12.3.3 Coarse-Fine Three-Step Search

Another important work on the block-matching technique was completed at almost the same time by Koga, Linuma, Hirano, Iijima, and Ishiguro. A coarse-fine three-step procedure was developed for fast searching ([Koga et al. 1981](#)).

The three-step search is very similar to the 2-D logarithm search. There are, however, three main differences between the two procedures. First, each step in the three-step search compares a set of nine points that form a 3×3 2-D grid structure. Second, the distances between the points in the 3×3 2-D grid structure in the three-step search decrease

**FIGURE 12.3**

(a) 2-D logarithm search procedure: Points at $(j, k+2)$, $(j+2, k+2)$, $(j+2, k+4)$, and $(j+1, k+4)$ are found to give the minimum dissimilarity in steps 1, 2, 3, and 4, respectively and (b) 2-D logarithm search procedure: Points at $(j, k-2)$, $(j+2, k-2)$, and $(j+2, k-1)$ are found to give the minimum dissimilarity in steps 1, 2, 3, and 4, respectively.

**FIGURE 12.4**

Three-step search procedure: Points $(j+4, k-4)$, $(j+4, k-6)$, and $(j+5, k-7)$ give the minimum dissimilarity in steps 1, 2, and 3, respectively.

monotonically in steps 2 and 3. Third, a total of only three steps are carried out. Obviously, these three items are different from the 2-D logarithm search described in [Section 12.3.2](#).

An illustrative example of the three-step search is shown in [Figure 12.4](#).

12.3.4 Conjugate Direction Search

The conjugate direction search is another fast-search algorithm, developed by Srinivasan and Rao. In principle, the procedure consists of two parts. In the first part, it finds the minimum dissimilarity along the horizontal direction with the vertical coordinate fixed at an initial position. In the second part, it finds the minimum D value along the vertical direction with the horizontal coordinate fixed in the position determined in the first part. Starting with the vertical direction followed by the horizontal direction is, of course, functionally equivalent. It was reported that this search procedure works quite efficiently (Srinivasan and Rao 1984).

[Figure 12.5](#) illustrates the principle of the conjugate direction search. In this example, each step involves a comparison between three testing points. If a point assumes the minimum D value compared with both of its two immediate neighbors (in one direction),

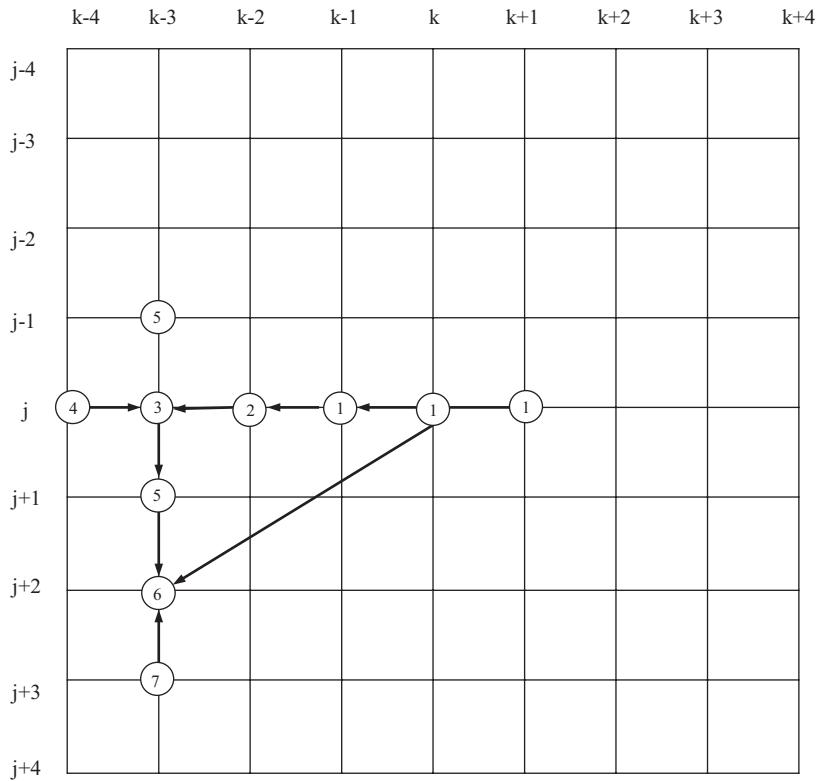
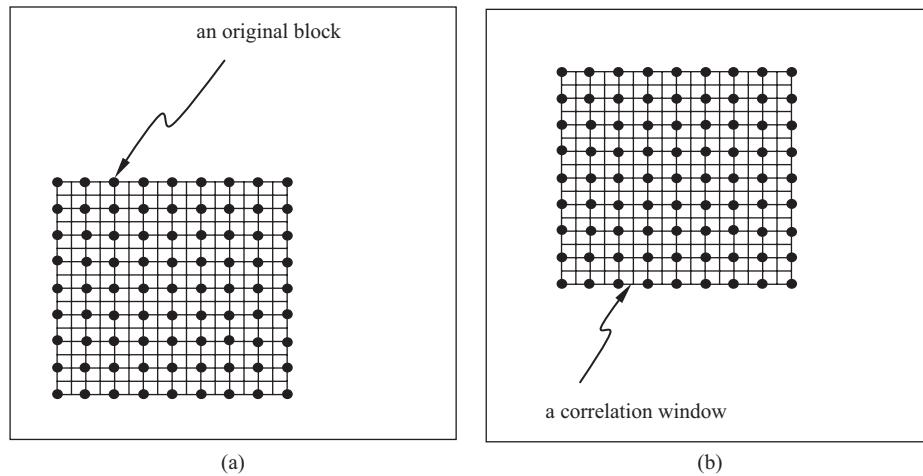


FIGURE 12.5
Conjugate direction search.

then it is considered to be the best matching along this direction, and the search along another direction is started. Specifically, the procedure starts to compare the D values for three points $(j, k-1)$, (j, k) , and $(j, k+1)$. If the D value of point $(j, k-1)$ appears to be the minimum among the three, then points $(j, k-2)$, $(j, k-1)$, and (j, k) are examined. The procedure continues, finding point $(j, k-3)$ as the best matching along the horizontal direction since its D value is smaller than that of points $(j, k-4)$ and $(j, k-2)$. The procedure is then conducted along the vertical direction. In this example the best matching is finally found at point $(j+2, k-3)$.

12.3.5 Subsampling in the Correlation Window

In the evaluation of the matching criterion, either MAD or MSE, all pixels within a correlation window at the t_{n-1} frame and an original block at the t_n frame are involved in the computation. Note that the correlation window and the original block are the same size (refer to Figure 12.1). In order to further reduce the computational effort, a subsampling inside the window and the block is performed (Bierling 1988). Aliasing effects can be avoided by using low-pass filtering. For instance, only every second pixel, both horizontally and vertically, inside the window and the block, is taken into account for the evaluation of the matching criterion. Obviously, by using this subsampling technique, the computational burden is reduced by a factor of 4. Since 3/4 of the pixels within the window and the block are not involved in the matching computation, however, the use of such a subsampling

**FIGURE 12.6**

An example of 2×2 subsampling in the original block and correlation window for fast search (a) An original block of 16×16 in frame at t_n and (b) A correlation window of 16×16 in frame at t .

procedure may affect the accuracy of the estimated motion vectors, especially in the case of small size blocks. Therefore, the subsampling technique is recommended only for those cases with a large enough block size so that the matching accuracy will not be seriously affected. Figure 12.6 shows an example of 2×2 subsampling applied to both an original block of 16×16 at the t_n frame and a correlation window of the same size at the t_{n-1} frame.

12.3.6 Multiresolution Block Matching

It is well known that multiresolution structure, also known as pyramid structure, is a very powerful computational configuration for various image processing tasks. To save computation in block matching, it is natural to resort to the pyramid structure. In fact, the multiresolution technique has been regarded as one of the most efficient methods in block matching (Tzovaras et al. 1994). In a named top-down multiresolution technique, a typical Gaussian pyramid is formed first.

Before diving into further description, let us pause here to give those readers who have not been exposed to the Gaussian pyramid a short introduction to the concept of Gaussian pyramid. For those who know the concept, this paragraph can be skipped. Briefly speaking, a Gaussian pyramid can be understood as a set of images with different resolutions related to an original image in a certain way. The original image has the highest resolution and is considered as the lowest level, sometimes called the bottom level, in the set. From the bottom level to the top level, the resolution decreases monotonically. Specifically, between two consecutive levels, the upper level is half as large as the lower level in both horizontal and vertical directions. The upper level is generated by applying a low-pass filter (which has a group of weights) to the lower level, followed by a 2×2 subsampling. That is, each pixel in the upper level is a weighted average of some pixels in the lower level. In general, this iterative procedure of generating a level in the set is equivalent to convolving a specific weight function with the original image at the bottom level followed by an appropriate subsampling. Under certain conditions, these weight functions can closely approximate the Gaussian probability density function, which is why the pyramid is named after Gauss. (For a detailed discussion, readers are referred to [Burt and Adelson 1983, Burt 1984]). A diagram of a Gaussian pyramid structure is depicted in Figure 12.7.

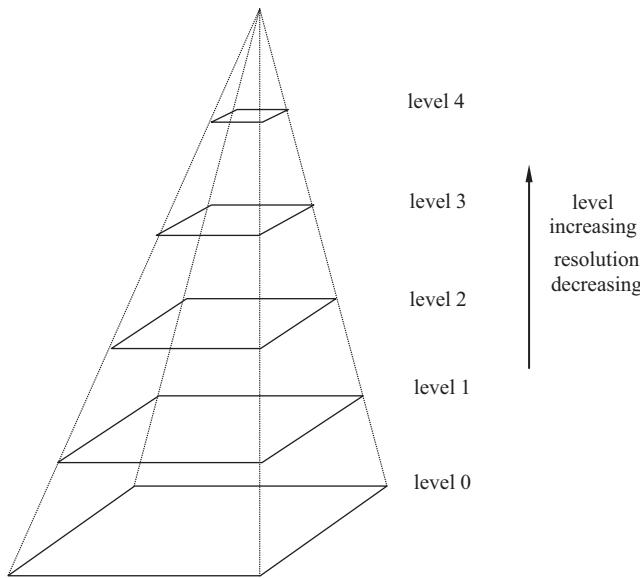


FIGURE 12.7
A Gaussian pyramid structure.

Note that the Gaussian pyramid depicted in [Figure 12.7](#) resembles a so-called quad-tree structure in which each node has four children nodes. In the simplest quad-tree pyramid, each pixel in an upper level is assigned an average value of its corresponding four pixels in the next lower level.

Now let's return to our discussion on the top-down multiresolution technique. After a Gaussian pyramid has been constructed, motion search ranges are allocated among the different pyramid levels. Block matching is initiated at the lowest resolution level to obtain an initial estimation of motion vectors. These computed motion vectors are then propagated to the next higher resolution level, where they are corrected, and then propagated to the next level. This procedure continues until the highest resolution level is reached. As a result, a large amount of computation can be saved. In Tzovaras et al. (1994) it was shown that a two-level Gaussian pyramid outperforms a three-level pyramid. Compared with full-search block matching, the top-down multiresolution block search saves up to 67% computation without seriously affecting the quality of the reconstructed images.

In conclusion, it has been demonstrated that multiresolution is indeed an efficient computational structure in block matching. This once again confirms the high computational efficiency of the multiresolution structure.

12.3.7 Thresholding Multiresolution Block Matching

With the multiresolution technique discussed above, the computed motion vectors at any intermediate pyramid level are projected to the next higher resolution level. In reality, some computed motion vectors at the lower resolution level may be inaccurate and have to be further refined, while others may be relatively accurate and able to provide satisfactory motion compensation for the corresponding block. From a computation saving point of view, for the latter class it may not be worth propagating the motion vectors to the next higher resolution level for further processing.

Motivated by the above observation, a new multiresolution block-matching method with a thresholding technique was developed (Shi and Xia 1997). With the thresholding technique, it prevents those blocks, whose estimated motion vectors provide satisfactory motion compensation, from further processing, thus saving a lot of computation. In what follows, this technique is presented in detail so as to provide readers with an insight to both multiresolution block-matching and thresholding multiresolution block-matching techniques.

12.3.7.1 Algorithm

Let $f_n(x, y)$ be the frame of an image sequence at current moment n . First, two Gaussian pyramids are formed, pyramids n and $n-1$, from image frames $f_n(x, y)$ and $f_{n-1}(x, y)$, respectively. Let the levels of the pyramids be denoted by l , $l = 0, 1, \dots, L$, where 0 is the lowest resolution level (top level), L is the full-resolution level (bottom level), and $L+1$ is the total number of layers in the pyramids. (Note that this way to number levels of the pyramid structure [Shi and Xia 1997] is different from the way depicted in Figure 12.7.) If (i, j) are the coordinates of the upper left corner of a block at level l of pyramid n , the block is referred to as block $(i, j)_n^l$. The horizontal and vertical dimensions of a block at level l are denoted by b_x^l and b_y^l , respectively. Like the variable block size method (refer to Method 1 in Tzovaras et al. [1994]), the size of the block in this work varies with the pyramid levels. That is, if the size of a block at level l is $b_x^l \times b_y^l$, then the size of the block at level $l-1$ becomes $2b_x^l \times 2b_y^l$. The variable block size method is used because it gives more efficient motion estimation than the fixed-block-size method. Here, the matching criterion used for motion estimation is the MAD because it does not require multiplication and gives similar performance as the MSE does. The MAD between block $(i, j)_n^l$ of the current frame and block $(i + v_x, j + v_y)_{n-1}^{l-1}$ of the previous frame at level l can be calculated as

$$MAD_{(i,j)_n^l}(v_x^l, v_y^l) = \frac{1}{b_x^l \times b_y^l} \sum_{k=0}^{b_x^l-1} \sum_{m=0}^{b_y^l-1} |f_n^l(i+k, j+m) - f_{n-1}^l(i+k+v_x^l, j+m+v_y^l)| \quad (12.5)$$

where $V^l = (v_x^l, v_y^l)$ is one of the candidates of the motion vector of block $(i, j)_n^l$ and v_x^l, v_y^l are the two components of the motion vector along the x and y directions, respectively.

A block diagram of the algorithm is shown in Figure 12.8. The threshold in terms of MAD needs to be determined in advance according to the accuracy requirement of the motion estimation. How to determine the threshold is discussed below in Part B of this subsection. Gaussian pyramids are formed for two consecutive frames of an image sequence from which motion estimation is desired. Block matching is then performed at the top level with the full-search scheme. The estimated motion vectors are checked to see if they provide satisfactory motion compensation. If the accuracy requirement is met, then the motion vectors will be directly transformed to the bottom level of the pyramid. Otherwise, the motion vectors will be propagated to the next higher resolution level for further refinement. This thresholding process is discussed below in Part C of this subsection. The algorithm continues in this fashion until either the threshold has been satisfied or the bottom level has been reached. The skipping of some intermediate-level computation provides for computational saving. Experimental work with quite different motion complexities demonstrates that the proposed algorithm reduces the processing time from 14% to 20%, while maintaining almost the same quality in the reconstructed image compared with the fastest existing multiresolution block-matching algorithm (Tzovaras et al. 1994).

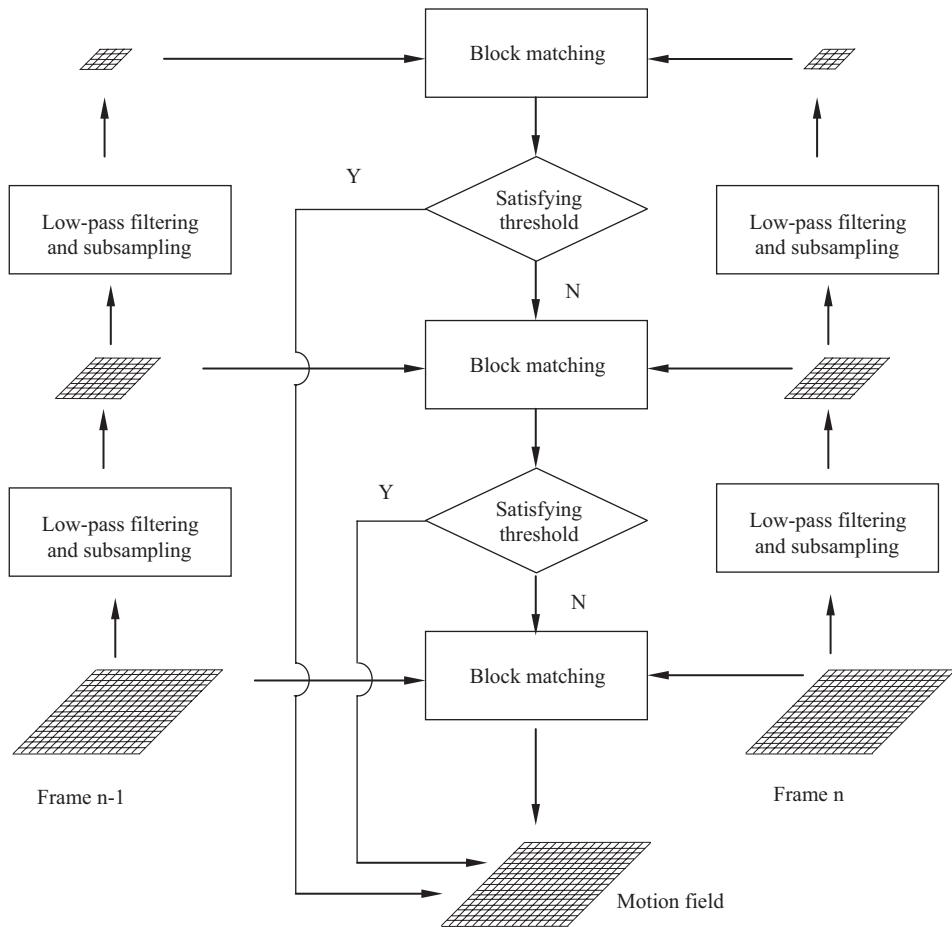


FIGURE 12.8
Block diagram for a three-level threshold multiresolution block matching.

12.3.7.2 Threshold Determination

The MAD accuracy criterion is used in this work for the sake of saving computation. The threshold value has a direct impact on the performance of the proposed algorithm. A small threshold value can improve the reconstructed image quality at the expense of increased computational effort. On the other hand, a large threshold value can reduce the computational complexity, but the quality of the reconstructed image may be degraded. One possible way to determine a threshold value, which is used in many experiments in Shi et al. (1998), is as follows.

The peak signal-to-noise ratio (PSNR) is commonly used as a measure of the quality of the reconstructed image. As introduced in Chapter 1, it is defined as

$$PSNR = 10 \log_{10} \frac{255^2}{MSE}. \quad (12.6)$$

From the given required PSNR, one can find out the necessary MSE value. A square root of this MSE value can be chosen as a threshold value, which is applied to the first

two images from the sequence. If the resulting PSNR and required processing time are satisfactory, it is then used for the rest of the sequence. Otherwise, the threshold can be slightly adjusted accordingly and applied to the second and third images to check the PSNR and processing time. It was reported that this adjusted threshold value has been good enough, and that there is no need for further adjustment in numerous experiments. As shown in [Table 12.1](#), the threshold values used for the "Miss America," "Train," and "Football" sequences (note that three sequences have quite different motion complexities) are 2, 3, and 4, respectively. They are all determined in this fashion and give satisfactory performance, as shown in the three rows marked "New Method (TH = 2)," "New Method (TH = 3)," and "New Method (TH = 4)," respectively, in [Table 12.2](#). That is, the PSNR experiences only about 0.1 dB loss and the processing time decreases drastically.

TABLE 12.1

Parameters Used in Experiments.

| <i>Parameters at Level</i> | Low-Resolution Level | Full-Resolution Level |
|----------------------------|-----------------------------|------------------------------|
| "Miss America" | | |
| Search Range | 3×3 | 1×1 |
| Block Size | 4×4 | 8×8 |
| Thresholding Value | 2 | None (Not applicable) |
| "Train" | | |
| Search Range | 4×4 | 1×1 |
| Block Size | 4×4 | 8×8 |
| Thresholding Value | 3 | None (Not applicable) |
| "Football" | | |
| Search Range | 4×4 | 1×1 |
| Block Size | 4×4 | 8×8 |
| Thresholding Value | 4 | None (Not applicable) |

TABLE 12.2

Experimental Results (I)

| | PSNR (dB) | Error Image Entropy (Bits/Pixel) | Vector Entropy (Bits/Vector) | Block Stopped at Top Level/ Total Block | Processing Times (No. of Additions, 10^6) |
|--------------------------------|----------------------|---|---|--|---|
| "Miss America" Sequence | | | | | |
| Method 1 (Tzovaras 1994) | 38.91 | 3.311 | 6.02 | 0/1280 | 10.02 |
| New Method (TH = 2) | 38.79 | 3.319 | 5.65 | 679/1280 | 8.02 |
| New Method (TH = 3) | 38.43 | 3.340 | 5.45 | 487/1280 | 6.17 |
| "Train" Sequence | | | | | |
| Method 1 (Tzovaras 1994) | 27.37 | 4.692 | 6.04 | 0/2560 | 22.58 |
| New Method (TH = 3) | 27.27 | 4.788 | 5.65 | 1333/2560 | 18.68 |
| "Football" Sequence | | | | | |
| Method 1 (Tzovaras 1994) | 24.26 | 5.379 | 7.68 | 0/3840 | 30.06 |
| New Method (TH = 4) | 24.18 | 5.483 | 7.58 | 1464/3840 | 25.90 |
| New Method (TH = 3) | 24.21 | 5.483 | 7.57 | 1128/3840 | 27.10 |

In the experiments, the threshold value of 3, i.e., the average value of 2, 3, and 4, was also tried. Refer to the three rows marked “New Method (TH = 3)” in [Table 12.2](#). It is noted that this average threshold value 3 has already given satisfactory performance for all three sequences. Specifically, for the “Miss America” sequence, since the criterion increases from 2 to 3, the PSNR loss increases from 0.12 dB to 0.48 dB, and the reduction in processing time increases from 20% to 38%. For the “Football” sequence, since the criterion decreases from 4 to 3, the PSNR loss decreases from 0.08 dB to 0.05 dB, and the reduction in processing time decreases from 14% to 9%. Obviously, for the “Train” sequence, the criterion and the performance remain the same. One can therefore conclude that the threshold determination may not require much computation at all.

12.3.7.3 Thresholding

Motion vectors estimated at each pyramid level will be checked to see if they provide satisfactory motion compensation. Assume $V^l(i, j) = (v_x^l, v_y^l)$ is the estimated motion vector for block $(i, j)_n^l$ at level l of pyramid n . For thresholding, $V^l(i, j)$ should be directly projected to the bottom level L . The corresponding motion vector for the same block at the bottom level of pyramid n will be $V^L(2^{(L-l)}i, 2^{(L-l)}j)$, and is given as

$$V^L(2^{(L-l)}i, 2^{(L-l)}j) = 2^{(L-l)}V^l(i, j). \quad (12.7)$$

The MAD between the block at the bottom pyramid level of the current frame and its counterpart in the previous frame can be determined according to [Equation 12.5](#), where the motion vector is $V^L = V^L(2^{(L-l)}i, 2^{(L-l)}j)$.

This computed MAD value can be compared with the predefined threshold. If this MAD value is less than the threshold, the computed motion vector $V^L(2^{(L-l)}i, 2^{(L-l)}j)$ will be assigned to block $(2^{(L-l)}i, 2^{(L-l)}j)_n^L$ at level L in the current frame and motion estimation for this block will be stopped. If not, the estimated motion vector $V^l(i, j)$ at level l will be propagated to level $l+1$ for further refinement. [Figure 12.9](#) gives an illustration of the above thresholding process.

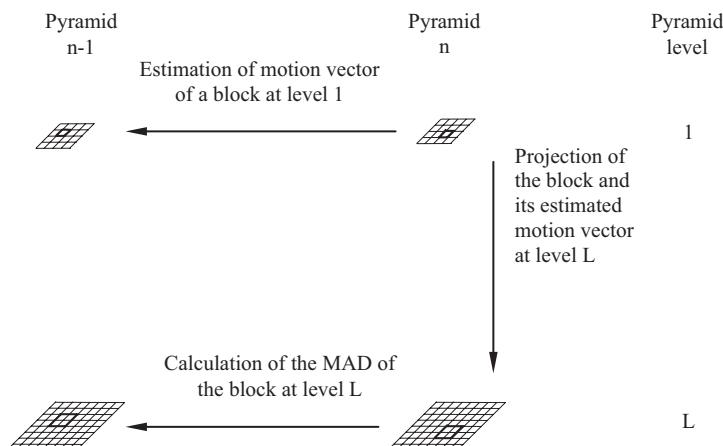


FIGURE 12.9
The thresholding process.

12.3.7.4 Experiments

To verify the effectiveness of the proposed algorithm, extensive experiments have been conducted. The performance of the new algorithm is evaluated and compared with that of Method 1, one of the most efficient multiresolution block-matching methods (Tzovaras et al. 1994), in terms of PSNR, error image entropy, motion vector entropy, the number of blocks stopped at the top level versus the total number of blocks, and processing time. The number of blocks stopped at the top level is the number of blocks withheld from further processing, while the total number of blocks is the number of blocks existing at the top level. It is noted that the total number of blocks is the same for each level in the pyramid. The processing time is the sum of the total number of additions involved in the evaluation of the MAD and the thresholding operation.

In the experiments, two-level pyramids are used since they give better performance for motion-estimation purposes (Tzovaras et al. 1994). The algorithms are tested on three video sequences with different motion complexities, i.e., the "Miss America," "Train," and "Football." The "Miss America" sequence has a speaker imposed on a static background and contains less motion. The "Train" sequence has more detail and contains a fast-moving object (train). The 20th frame of the sequence is shown in Figure 12.10. The "Football" sequence contains the most complicated motion compared with the other two sequences. The 20th frame is shown in Figure 12.11. Table 12.1 is the list of implementing parameters used in the experiments. Tables 12.2 and 12.3 give the performance of the proposed algorithm compared with Method 1. In all three cases, the motion estimation has a half-pixel accuracy, the meaning of which will be explained in the next section. All performance measures listed there are averaged for the first 25 frames of the testing sequences.

Each frame of the "Miss America" sequence is of 360×288 pixels. For convenience, only the central portion, 320×256 pixels, is processed. With the operational parameters listed in Table 12.1 (with a criterion value of 2), 38% of the total blocks at the top level satisfy the predefined criterion and are not propagated to the bottom level. The processing time needed by the proposed algorithm is 20% less than Method 1, while the PSNR, the error



FIGURE 12.10
The 20th frame of the "Train" sequence.



FIGURE 12.11
The 20th frame of the “Football” sequence.

TABLE 12.3
Experimental Results (II)

| | Percentage of Total Blocks Stopped at Top Level | Percentage of Saved Processing Time Compared with Method 1 in (Tzovaras 1994) |
|-------------------------------------|---|---|
| “Miss America” sequence (TH = 2) | 38% | 20% |
| “Train” sequence (TH = 3) | 52% | 17% |
| “Football” sequence (TH = 4) | 38% | 14% |

image entropy, and the vector entropy are almost the same. Compared with Method 1, an extra amount of computation (around 0.16×10^6 additions) is conducted on the thresholding operation, but a large computational savings (around 2.16×10^6 additions) is achieved through withholding from further processing those blocks whose MAD values at the full-resolution level are less than the predefined accuracy criterion.

The frames of the “Train” sequence are 720×288 pixels, and only the central portion, 640×256 pixels, is processed. With the operational parameters listed in Table 12.1 (with a criterion value of 3), about 52% of the total blocks are stopped at the top level. The processing time is reduced by about 17% by the new algorithm, compared with Method 1. The PSNR, the error image entropy, and the vector entropy are almost the same.

The frames of the “Football” sequence are 720×480 pixels, and only the central portion, 640×384 pixels, is processed. With the operational parameters listed in [Table 12.1](#) (with a criterion value of 4), about 38% of the total blocks are stopped at the top level. The processing time is about 14% less than that required by Method 1, while the PSNR, the error image entropy, and the vector entropy are almost the same.

As discussed, the experiments with a single accuracy criterion of 3 also produce similarly good performance for the three different image sequences.

In summary, it is clear that with the three different testing sequences, the thresholding multiresolution block-matching algorithm works faster than the fastest existing top-down multiresolution block-matching algorithm while achieving almost the same quality of the reconstructed image.

12.4 Matching Accuracy

Apparently, the two components of the displacement vectors obtained using the technique described above are an integer multiple of pixels. This is referred to as one-pixel accuracy. If a higher accuracy is desired, i.e., the components of the displacement vectors may be a non-integer multiple of pixels, then spatial interpolation is required. Not only will more computation be involved, but also will more bits be required to represent motion vectors. The gain is more accurate motion estimation, hence less prediction error. In practice, half-pixel and quarter-pixel accuracy are two widely utilized accuracies other than one-pixel accuracy.

12.5 Limitations with Block-Matching Techniques

Although very simple, straightforward, and efficient, hence, utilized most widely in video coding, the block-matching motion-compensation technique has its drawbacks. First, it has an unreliable motion vector field with respect to the true motion in 3-D world space, in particular, it has unsatisfactory motion estimation and compensation along moving boundaries. Second, it causes block artifacts. Third, it needs to handle side information. That is, it needs to encode and transmit motion vectors as an overhead to the receiving end, thus making it difficult to use smaller block size to achieve higher accuracy in motion estimation.

All these drawbacks are due to its simple model: Each block is assumed to experience a uniform translation, and the motion vectors of partitioned blocks are estimated independently of each other.

Unreliable motion estimation, particularly along moving boundaries, causes more prediction error, hence reduced coding efficiency.

The block artifacts do not cause severe perceptual degradation to the human visual system (HVS) when the available coding bit rate is adequately high. This is because, with a high bit rate, a sufficient amount of the motion-compensated prediction error can be transmitted to the receiving end, hence improving the subjective visual effect to such an extent

**FIGURE 12.12**

The 21st reconstructed frame of the "Miss America" sequence by using a codec following H.263.

that the block artifacts do not appear to be annoying. However, when the available bit rate is low, particularly lower than 64 kilobits per second (kbps), the artifacts become visually unpleasant. In [Figure 12.12](#), a reconstructed frame of the "Miss America" sequence at a low bit rate is shown. Obviously, block artifacts are very annoying, especially where mouth and hair are. The sequence was coded and decoded by using a codec following ITU-T Recommendations H.263, an international standard in which block matching is utilized for motion estimation.

The assumption that motion within each block is uniform requires a small block size such as 16×16 and 8×8 . A small block size leads to a large number of motion vectors, however, resulting in a large overhead of side information. A study in Chan (1990) indicates that 8×8 block matching performs much better than 16×16 in terms of decoded image quality due to better motion estimation and compensation. The bits used for encoding motion vectors, however, increase significantly (about four times), which may be prohibitive for very-low-bit-rate coding since the total bit rate needed for both prediction error and motion vectors may exceed the available bit rate. It is noted that when coding bit rate is quite low, say, on the order of 20 kbps, the *side* information becomes compatible with the *main* information (prediction error) (Lin et al. 1997).

Tremendous research efforts have been made to overcome the limitations of block-matching techniques. Some improvements have been achieved and are discussed next. It should be kept in mind, however, that so far block matching is still by far the most popular and efficient motion-estimation and -compensation technique utilized for video coding, and it has been adopted by various international coding standards. In other words, block matching is the most appropriate in the framework of first-generation video coding (Dufaux and Moscheni 1995).

12.6 New Improvements

12.6.1 Hierarchical Block Matching

Bierling developed the hierarchical search in Bierling (1988) based on the following two observations. On the one hand, for a relatively large displacement, accurate block matching requires a relatively large block size. This is conceivable if one considers its opposite case: a large displacement with a small correlation window. Under this circumstance, the search range is large. Therefore, the probability of finding multiple matching is high, resulting in unreliable motion estimation. On the other hand, a large block size may violate the assumption that all pixels in the block share the same displacement vector. Hence, a relatively small block size is required in order to meet the assumption. These observations shed light on the problem of using a fixed block size, which may lead to unreliable motion estimation.

To satisfy these two contradicting requirements simultaneously, in a hierarchical search procedure, a set of different sizes of blocks and correlation windows is utilized. To facilitate the discussion, consider a three-level hierarchical block-matching algorithm, in which three block-matching procedures are conducted, each with its own parameters. Block matching is first conducted with respect to the largest size of blocks and correlation windows. Using the estimated displacement vector as an initial vector at the second level, a new search is carried out with respect to the second largest size of blocks and correlation windows. The third search procedure is carried out similarly based on the results of the second search. An example with three correlation windows is illustrated in [Figure 12.13](#). It is noted that the resultant displacement vector is the sum of the three displacement vectors determined by three searches.

The parameters in these three levels are listed in [Table 12.4](#). The algorithm is described below with an explanation of the various parameters in [Table 12.4](#). Prior to each block matching, a separate low-pass filter is applied to the whole image in order to achieve reliable block matching. The low-pass filtering used is simply a local averaging. That is, the gray value of every pixel is replaced by the mean value of the gray values of all pixels within a square area centered at the pixel to which the mean value is assigned.

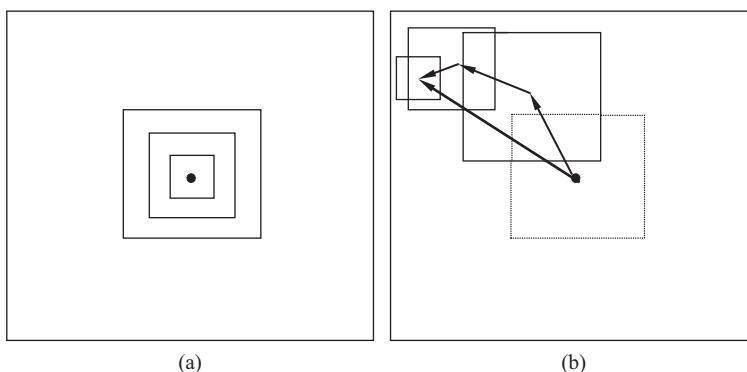


FIGURE 12.13
Hierarchical block matching (a) frame t_i and (b) frame t_{i-1} .

TABLE 12.4

Parameters Used in a Three-Level Hierarchical Block Matching

| Hierarchical Level | Maximum Displacement | Correlation Window Size | Step Size | LPF Window Size | Subsampling |
|--------------------|----------------------|-------------------------|-----------|-----------------|--------------|
| 1 | ± 7 pel | 64×64 | 8 | 5×5 | 4×4 |
| 2 | ± 3 pel | 28×28 | 4 | 5×5 | 4×4 |
| 3 | ± 1 pel | 12×12 | 2 | 3×3 | 2×2 |

Source: Bierling, M., Displacement estimation by hierarchical blockmatching, *Proceedings of Visual Communications and Image Processing*, SPIE, Cambridge, MA, vol. 1001, pp. 942–951, 1988.

In calculating the matching criterion D value, a subsampling is applied to the original block and the correlation window in order to save computation, which was discussed in [Section 12.3.5](#).

In the first level, for every eighth pixel horizontally and vertically (a step size of 8×8), block matching is conducted with the maximum displacement being ± 7 pixels, a correlation window size of 64×64 , and a subsampling factor of 4×4 . A 5×5 averaging low-pass filtering is applied prior to first-level block matching. Second-level block matching is conducted with respect to every fourth pixel horizontally and vertically (a step size of 4×4). Note that for a pixel whose displacement vector estimate has not been determined in first-level block matching, an average of the four nearest neighboring estimates will be taken as its estimate. All the parameters for the second level are listed in [Table 12.4](#). One thing that needs to be emphasized is that in block matching at this level the search window should be displaced by the estimated displacement vector obtained in the first level. Third-level block matching is dealt with accordingly for every second pixel horizontally and vertically (a step size of 2×2). The different parameters are listed in [Table 12.4](#).

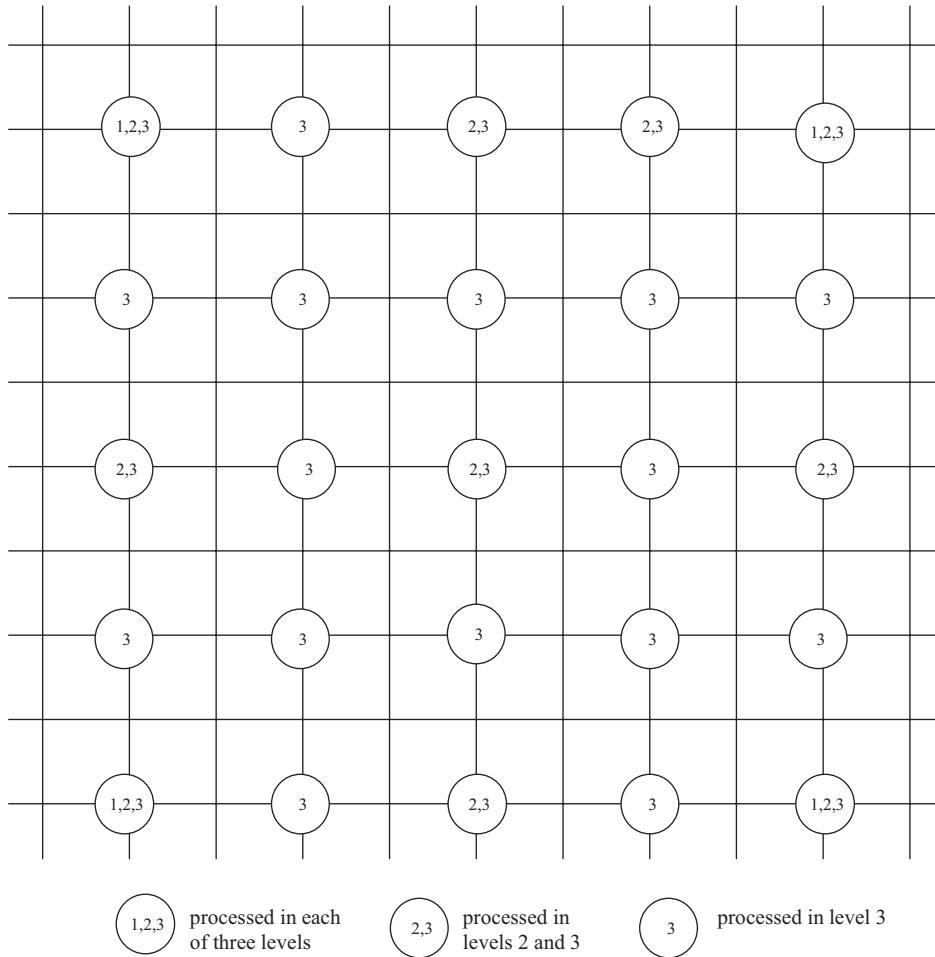
In each of the three levels, the three-step search discussed in [Section 12.3.3](#) is utilized.

Experimental work has demonstrated a more reliable motion estimation due to the usage of a set of different sizes for both the original block and the correlation window. The first level with a large window size and a large displacement range determines a major portion of the displacement vector reliably. The successive levels with smaller window sizes and smaller displacement ranges are capable of adaptively estimating motion vectors more locally.

[Figure 12.14](#) shows a portion of an image with pixels processed in the three levels, respectively. It is noted that it is possible to apply one more interpolation after these three levels so that a motion vector field of full resolution is available. Such a full-resolution motion vector field is useful in such applications as motion-compensated interpolation in the context of videophony. There, in order to maintain a low bit rate, some frames are skipped for transmission. At the receiving end, these skipped frames need to be interpolated. As discussed in [Chapter 10](#), motion-compensated interpolation is able to produce better frame quality than that achievable by using weighted linear interpolation.

12.6.2 Multigrid Block Matching

Multigrid theory was developed originally in mathematics (Hackbusch and Trottenberg 1982). It is a useful computational structure in image processing besides the multiresolution

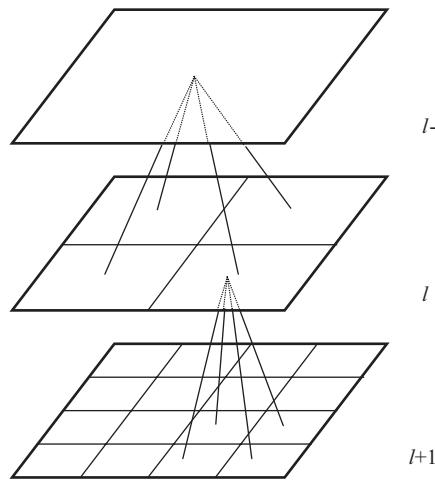
**FIGURE 12.14**

A portion of an image with pixels processed in the three levels respectively.

one described in [Section 12.3.6](#). A diagram with three different levels used to illustrate a multigrid structure is shown in [Figure 12.15](#). Although it is also a hierarchical structure, each level within the hierarchy is of the same resolution. A few algorithms based on multigrid structure have been developed in order to improve the block-matching technique. Two advanced methods are introduced below.

12.6.2.1 Thresholding Multigrid Block Matching

Realizing that the simple block-based motion model (assuming a uniform motion within a fixed size block) in the block-matching technique causes several drawbacks, Chan, Yu, and Constantinides proposed a variable-size block-matching technique. The main idea is using a split-and-merge strategy with a multigrid structure in order to segment an image

**FIGURE 12.15**

An illustration of a three-level hierarchical structure.

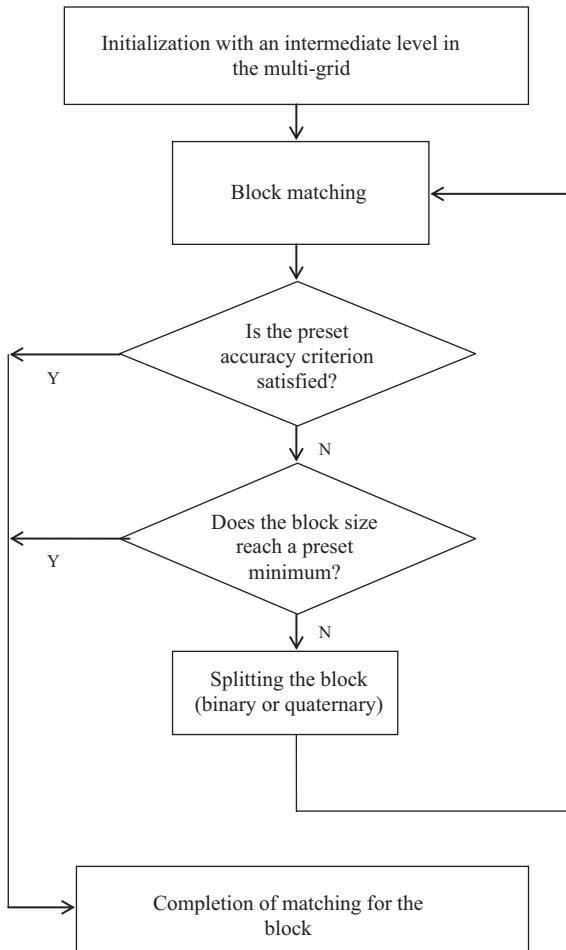
into a set of variable size blocks, each of which has an approximately uniform motion. A binary tree (also known as bin-tree) structure is used to record the relationship between these blocks with different sizes.

Specifically, an image frame is initially split into a set of square blocks by cutting the image alternately horizontally and vertically. With respect to each block thus generated, a block matching is performed in conjunction with its previous frame. Then the matching accuracy in terms of the sum squared error (SSE) is compared with a preset threshold. If it is smaller than or equal to the threshold, the block remains unchanged in the whole process and the estimated motion vector is final. Otherwise, the block will be split into two blocks, and a new run of block matching is conducted for each of these two children blocks. The process continues until either the estimated vector satisfies a preset accuracy requirement or the block size has reached a predefined minimum. At this point, a merge process is proposed by Chan et al: Neighboring blocks under the same intermediate nodes in the bin-tree are checked to see if they can be merged, i.e., if the merged block can be approximated by a block in the reconstructed previous frame with adequate accuracy. It is noted that the merge operation may be optional depending on the specific application.

A block diagram of the multigrid block matching is shown in [Figure 12.16](#). Note that it is similar to that shown in [Figure 12.8](#) for the thresholding multiresolution block matching discussed in [Section 12.3.6](#). This observation reflects the similarities between multigrid and multiresolution structures: both are hierarchical in nature and the split and merge can be easily performed.

An example of an image decomposition and its corresponding bin-tree are shown in [Figure 12.17](#).

It was reported in Chan (1990) that, with respect to a picture of a computer mouse and a coin, the proposed variable size block matching achieves up to 6 dB improvement in SNR and about 30% reduction in required bits compared with fixed-size (16×16) block matching. For several typical videoconferencing sequences, the proposed algorithm constantly

**FIGURE 12.16**

A block diagram of multigrid block matching.

performs better than the fixed-size block-matching technique in terms of improved SNR of reconstructed frames with the same bit rate.

A similar algorithm was reported in Xia et al. (1996), where a quad-tree based segmentation is used. The thresholding technique is similar to that used in Shi and Xia (1997), and the emphasis is placed on the reduction of computational complexity. It was found that for head-shoulder type of videophony sequences the thresholding multigrid block-matching algorithm (Xia and Shi 1996) performs better than the thresholding multiresolution block-matching algorithm (Shi and Xia 1997). For video sequences that contain more complicated details and motion, however, the performance comparison turns out to be reversed.

A few remarks can be made as a conclusion for the thresholding technique. Although it needs to encode and transmit the bin-tree or quad-tree as a portion of side information, and it has to resolve the preset threshold issue, overall, the proposed algorithms achieve

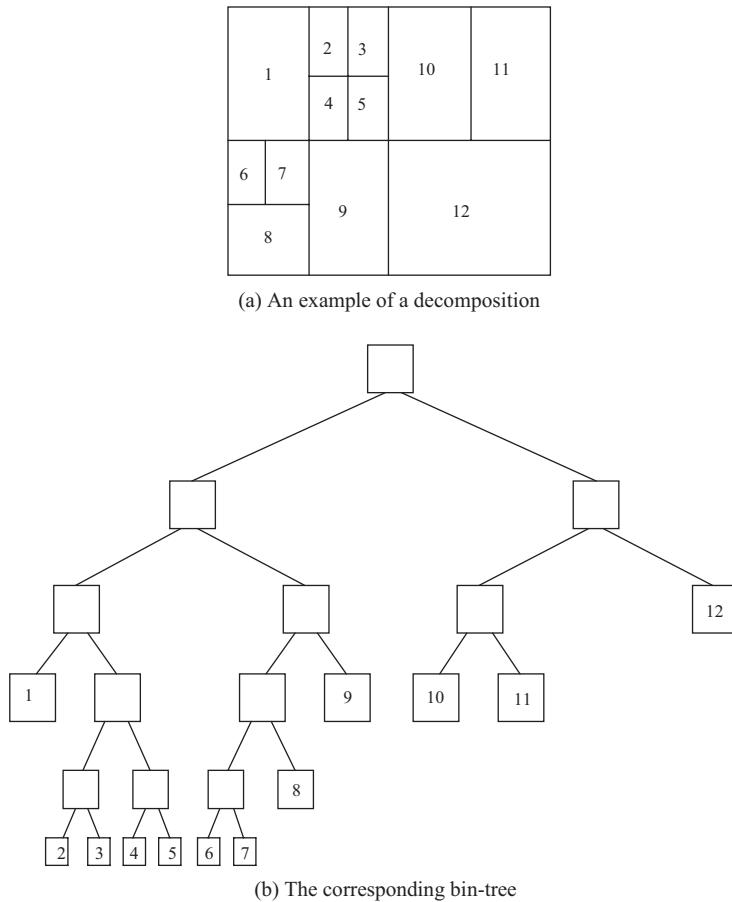


FIGURE 12.17
Thresholding multigrid block matching.

better performance compared with fixed-size block matching. With the flexibility provided through the variable-size methodology, the proposed approach is capable of making the motion model of the uniform motion within each block more accurate than fixed-size block matching can do.

12.6.2.2 Optimal Multigrid Block Matching

As pointed out in [Chapter 10](#), the ultimate goal of motion estimation and motion compensation in the context of video coding is to provide a high code efficiency in real-time. In other words, accurate true motion estimation is not the final goal, although accurate motion estimation is certainly desired. This point was presented in Bierling (1988) as well. There, the different requirements with respect to motion-compensated coding and motion-compensated interpolation were discussed. While the former requires motion vector estimation leading to minimum prediction error and at the same time a low amount of motion vector information, the latter requires accurate estimation of true vectors and a high resolution of the motion vector field.

This point was very much emphasized in Dufaux and Moscheni (1995). There, Dufaux and Moscheni clearly stated that in the context of video coding, estimation of true motion in 3-D world space is not the ultimate goal. Instead, motion estimation should be able to provide good temporal prediction and at the same time require low overhead information. In a word, the total amount of information that needs to be encoded should be minimized. Based on this observation, a multigrid block-matching technique with an advanced entropy criterion was proposed.

Since it belongs to the category of thresholding multigrid block matching, it shares many similarities with that in Chan (1990) and Xia (1996). It also bears some resemblance to thresholding multiresolution block matching (Shi and Xia 1997). What really distinguishes this approach from other algorithms is its segmentation decision rule. Instead of a preset threshold, the algorithm works with an adaptive entropy criterion, which aims at controlling the segmentation in order to achieve an optimal solution in such a way that the total bits needed for representing both the prediction error and motion overhead is minimized. The decision of splitting a block is made only when the extra motion overhead involved in the splitting is lower than the gain obtained from less prediction error due to more accurate motion estimation. Not only it is optimal in the sense of bit saving, but it also eliminates the need for setting a threshold.

The number of bits needed for encoding motion information can be estimated in a straightforward manner. As far as the prediction error is concerned, the number of bits required can be represented by a total entropy of the prediction error, which can be estimated by using an analytical expression presented in Dufaux and Kunt (1992), Dufaux (1994), and Moscheni et al. (1993). Note that the coding cost for quad-tree segmentation information is negligible compared with that used for encoding prediction error and motion vectors and, hence, is omitted in determining the criterion.

In addition to this entropy criterion, a more advanced procedure is adopted in the algorithm for down-projecting the motion vectors between two consecutive grids in the coarse-to-fine iterative refinement process.

Both qualitative and quantitative assessments in experiments demonstrate its good performance. It was reported that, when the PSNR is fixed, the bit rate saving for the sequence "Flower Garden" is from 10% to 20%, for "Mobile Calendar" from 6% to 12%, and for "Table Tennis" up to 8%. This can be translated into a gain in the PSNR ranging from 0.5 to 1.5 dB. Subjectively, the visual quality is improved greatly. In particular, moving edges become much sharper. Figures 12.18 through 12.20 show a frame from "Flower Garden," "Mobile Calendar," and "Table Tennis" sequences, respectively.

12.6.3 Predictive Motion Field Segmentation

As pointed at the beginning of [Section 12.5](#), the block-based model, which assumes constant motion within each block, leads to unreliable motion estimation and compensation. This block effect becomes more obvious and severe for motion discontinuous areas in image frames. This is because there are two or more regions in a block in the areas, each having a different motion. Using one motion vector to represent and compensate for the whole block results in significant prediction error increase.

Orchard proposed a predictive motion field segmentation technique to improve motion estimation and compensation along boundaries of moving objects in Orchard (1993). The significant improvement in the accuracy of the motion-compensated frame was achieved through relaxing the restrictive block-based model along moving boundaries. That is, for those blocks involving moving boundaries, the motion field assumes pixel resolution instead of block resolution.

**FIGURE 12.18**

The 20th frame of the “Flower garden” sequence.

**FIGURE 12.19**

The 20th frame of the “Mobile and Calendar” sequence.

**FIGURE 12.20**

The 20th frame of the “Table tennis” sequence.

Two key issues have to be resolved in order to realize the idea. One is the segmentation issue. It is known that the segmentation information is needed at the receiving end for motion compensation. This gives rise to a large increase in side information. To maintain almost the same amount of coding cost as the conventional block-matching technique, the motion field segmentation was proposed to be conducted based on previously decoded frames. This scheme is based on the following observation: The shape of a moving object does not change from frame to frame.

This segmentation is similar to the pel-recursive technique (which will be discussed in detail in the next chapter) in the sense that both techniques operate *backwards*: based on previously decoded frames. The segmentation is different from the pel-recursive method in that it only uses previously decoded frames to predict the shape of discontinuity in the motion field, not the whole motion field itself. Motion vectors are still estimated using the current frame at the encoder. Consequently, this scheme is capable of achieving high accuracy in motion estimation, and at the same time it does not cause a large increase in side information due to the motion field segmentation.

Another key issue is how to achieve a reconstructed motion field with pixel resolution along moving boundaries. In order to avoid extra motion vectors that need to be encoded and transmitted, the motion vectors applied to these segmented regions in the areas of motion discontinuity are selected from a set of neighboring motion vectors. As a result, the proposed technique is capable of reconstructing discontinuities in the motion field at pixel resolution while maintaining the same amount of motion vectors as the conventional block-matching technique.

A number of algorithms using this type of motion field segmentation technique have been developed and their performance has been tested and evaluated on some real video

sequences (Orchard 1993). Two of the 40-frame test sequences used were the “Table Tennis” and the “Football.” The former contains fast ball motion and camera zooming, while the latter contains small objects with relatively moderate amounts of motion and camera panning. Several proposed algorithms were compared with conventional block matching in terms of average pixel prediction error energy and bits per frame required for coding prediction error. For the average pixel prediction error energy, the proposed algorithms achieve a significant reduction, ranging from -0.7 dB to -2.8 dB with respect to the “Table Tennis” sequence, and from -1.3 dB to -4.8 dB with the “Football” sequence. For bits per frame required for coding prediction error, a reduction of 20%–30% was reported.

12.6.4 Overlapped Block Matching

All the techniques discussed so far in this section aim at more reliable motion estimation. As a result, they also alleviate annoying block artifacts to a certain extent. In this subsection we discuss a group of techniques, termed overlapped block matching, developed to alleviate or eliminate block artifacts (Nogaki 1992, Auyeung 1992).

The idea is to relax the restriction of a nonoverlapped block partition imposed in the block-based model in block matching. After the nonoverlapped, fixed-size, small rectangular block partition has been made, each block is enlarged along all four directions from the center of the block. Refer to Figure 12.21. Both motion-estimation (block-matching) and motion-compensated prediction are conducted in the same manner as that in block matching except for the inclusion of a window function. That is, a 2-D window function is utilized in order to maintain an appropriate quantitative level along the overlapped portion. The window function decays towards the boundaries. In Nogaki (1992) a sine-shaped window function was used.

Next, we use the algorithm proposed by Nogaki and Ohta as an example to specifically illustrate this type of technique. Consider one of the enlarged, overlapped original

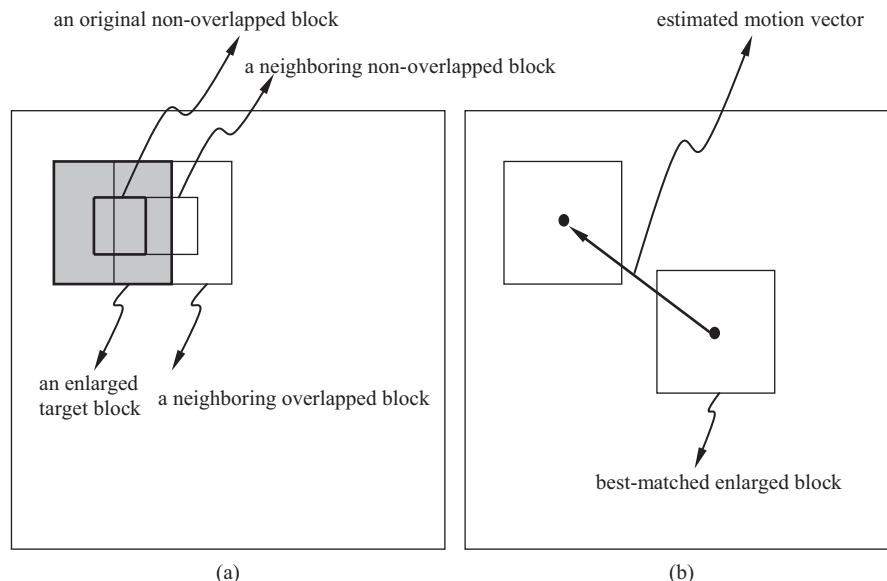


FIGURE 12.21
Overlapped block matching (a) frame at t_n and (b) frame at t_{n-1} .

(also known as target) blocks, $T(x, y)$, with a dimension of $l \times l$. Assume that a vector v_i is one of the candidate displacement vectors under consideration. The predicted version of the target block with v_i is denoted by $P_{v_i}(x, y)$. Thus, the prediction error with v_i , $E_{v_i}(x, y)$ can be calculated according to the following equation

$$E_{v_i}(x, y) = P_{v_i}(x, y) - T(x, y). \quad (12.8)$$

The window function $W(x, y)$ is applied at this stage as follows, resulting in a window-operated prediction error with v_i , WE_{v_i} .

$$WE_{v_i}(x, y) = E_{v_i}(x, y) \times W(x, y). \quad (12.9)$$

Assume that the *MAD* is used as the matching criterion. It can then be determined as usual by using the window-operated prediction error $WE_{v_i}(x, y)$. That is,

$$MAD = \frac{1}{l^2} \sum_{x=1}^l \sum_{y=1}^l |WE_{v_i}(x, y)|. \quad (12.10)$$

The best matching, which corresponds to the minimum *MAD*, produces the displacement vector v .

In motion-compensated prediction, the predicted version of the enlarged target block, $P_v(x, y)$ is derived from the frame at t_{i-1} by using estimated vector v . The same window function $W(x, y)$ is used to generate the final window-operated predicted version of the target block. That is,

$$WP_v(x, y) = P_v(x, y) \times W(x, y). \quad (12.11)$$

It was reported in Nogaki (1992) that the luminance signal of an HDTV sequence was used in computer simulation. A block size of 16×16 was used for conventional block matching, while a block size of 32×32 was employed for the proposed overlapped block matching. The maximum displacement range d was taken as $d = 15$, i.e., from -15 to $+15$ in the both horizontal and vertical directions. The simulation indicated a reduction in the power of prediction error by about 19%. Subjectively, it was observed that the blocking edges originally existing in the prediction error signal with conventional block matching were largely removed with the proposed overlapped block-matching technique.

12.7 Summary

By far, block matching is used more frequently than any other motion-estimation techniques in motion-compensated coding. By partitioning a frame into nonoverlapped, equally spaced, fixed-size, small rectangular blocks and assuming that all the pixels in a block experience the same translational motion, block matching avoids the difficulty encountered in motion estimation of arbitrarily shaped blocks. Consequently, block matching is much simpler and involves less side information compared with motion estimation with arbitrarily shaped blocks.

Although this simple model considers translation motion only, other types of motions, such as rotation and zooming of large objects, may be closely approximated by the piecewise translation of these small blocks provided that these blocks are small enough. This important observation, originally made by Jain and Jain, has been confirmed again and again since then.

Various issues related to block matching such as selection of block sizes, matching criteria, search strategies, matching accuracy, its limitations, and improvements are discussed in this chapter. Specifically, a block size of 16×16 is used most often. For more accurate motion estimation, the size of 8×8 is used sometimes. In the latter case, more accurate motion estimation is obtained at the cost of more side information and higher computational complexity.

There are several different types of matching criteria that can be used in block matching. Since it was shown that the different criteria do not cause significant difference in block matching, the *MAD* is hence preferred due to its simplicity in implementation.

On the one hand, full-search procedure delivers good accuracy in searching for the best matching. On the other hand, it requires a large amount of computation. In order to lower computational complexity, several fast-searching procedures were developed, including 2-D logarithm search, coarse-fine three-step search, and conjugate direction search, to name a few.

Besides these suboptimum search procedures, there are some other measures developed to lower computation. One of them is subsampling in the original blocks and the correlation windows. By the subsampling, the computational burden in block matching can be reduced drastically, while the accuracy of the estimated motion vectors may be affected. Therefore, the subsampling procedure is only recommended for the case with a large block size.

Naturally, multiresolution structure, a powerful computational configuration in image processing, lends itself well to fast search in block matching. It significantly reduces computation involved in block matching. Thresholding multiresolution block matching further saves computation.

In terms of matching accuracy, several common choices are one-pixel, half-pixel, and quarter-pixel accuracies. Spatial interpolation is usually required for half-pixel and quarter-pixel accuracies. That is, a higher accuracy is achieved with more computation.

The main limitations with block-matching techniques are unreliable motion vector field and block artifacts. Both are caused by the simple model: Each block is assumed to experience a uniform translation. Extensive efforts have been made to improve these drawbacks. Several techniques that have made improvement over the conventional block-matching technique are discussed in this chapter.

In the hierarchical block-matching technique, a set of different sizes for both the original block and the correlation window are used. The first level in the hierarchy with a large window size and a large displacement range determines a major portion of the displacement vector reliably. The successive levels with smaller window sizes and smaller displacement ranges are capable of adaptively estimating motion vectors more locally.

The multigrid block-matching technique uses multigrid structure, another powerful computational structure in image processing, to provide a variable-size block matching. With a split-and-merge strategy, the thresholding multigrid block-matching technique segments an image into a set of variable size block, each of which experiences an approximately uniform motion. A tree structure (bintree or quadtree) is used to record the relationship between these variable size blocks. With the flexibility provided through the variable-size methodology, the thresholding block-matching technique is capable of making the motion model of the uniform motion within each block more accurate than the fixed-size block matching can do.

As pointed out in [Chapter 10](#), the ultimate goal of motion compensation in video coding is to achieve a high coding efficiency. In other words, accurate true motion estimation is not the final goal. From this point of view, in the above-mentioned multigrid block matching, the decision of splitting a block is made only when the bits used to encode extra motion vectors involved in the splitting are less than the bits saved from encoding reduced prediction error due to more accurate estimation. To this end, an adaptive entropy criterion is proposed and used in the optimal multigrid block-matching technique. Not only it is optimal in the sense of bit saving, but it also eliminates the need for setting a threshold.

Apparently, the block-based model encounters more severe problems along moving boundaries. To solve the problem, the predictive motion field segmentation technique makes the blocks involving moving boundaries have the motion field with pixel resolution instead of block resolution. In order to save shape overhead, segmentation is carried out backwards, i.e., based on previously decoded frames. In order to avoid a large increase of side information associated with extra motion vectors, the motion vectors applied to these segmented regions along moving boundaries are selected from a set of neighboring motion vectors. As a result, the technique is capable of reconstructing discontinuities in the motion field at pixel resolution while maintaining the same amount of motion vectors as the conventional block-matching technique.

The last improvement over the conventional block matching discussed in this chapter is overlapped block matching. In contrast to dealing with blocks independently of each other, the overlapped block-matching technique enlarges blocks so as to make them overlapped. A window function is then constructed and used in both motion estimation and motion compensation. Because it relaxes the restriction of a nonoverlapped block partition imposed by the conventional block matching, it achieves better performance than the conventional block matching.

Exercises

- 12.1 Refer to [Figure 12.2](#), it is said that there is a total of $(2d+1) \times (2d+1)$ positions that need to be examined in block matching with full search if one-pixel accuracy is required. How many positions are there that need to be examined in block matching with full search if half-pixel and quarter-pixel accuracies are required?
- 12.2 What are the two effects that the subsampling in the original block and the correlation block may bring out?
- 12.3 Read Burt and Adelson (1983) or Burt (1984) and explain why the pyramid is named after Gauss.
- 12.4 Read Burt and Adelson (1983) or Burt (1984), and explain why a pyramid structure is considered as a powerful computational configuration. Specifically, in multi-resolutional block matching, how and to what extent does it save computation dramatically compared with the conventional block-matching technique? You may want to refer to [Section 12.3.7](#).
- 12.5 How is the threshold determined in the thresholding multidimensional block-matching technique (refer to [Section 12.3.7](#))? It is said that the square root of the MSE value, derived from the given PSNR according to Equation 12.6, is used as an initial threshold value. Justify the necessity of the square root operation.

- 12.6 Refer to [Section 12.6.1](#) or paper (Bierling 1988). State the different requirements in the applications of motion-compensated interpolation and motion-compensated coding. Discuss where a full resolution of translational motion vector field may be used?
- 12.7 Read the paper (Dufaux 1995) and explain the main feature of the optimal multigrid block matching. State how the adaptive entropy criterion is established. Implement the algorithm and compare its performance with that presented in Chan (1990).
- 12.8 Learn the predictive motion field segmentation technique (Orchard 1993). Explain how the algorithms avoid a large increase in overhead due to motion field segmentation.
- 12.9 Implement the overlapped block-matching algorithm introduced in Nogaki (1992). Compare its performance with that of the conventional block-matching technique.

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13

Pel-Recursive Technique

As discussed in [Chapter 11](#), the pel-recursive technique is one of the three major approaches to 2-D displacement estimation in image planes for the signal processing community. Conceptually speaking, it is one type of region-matching technique. In contrast to block matching (which was discussed in the previous chapter), it *recursively* estimates displacement vectors for *each pixel* in an image frame. The displacement vector of a pixel is estimated by recursively minimizing a nonlinear function of the dissimilarity between two certain regions located in two consecutive frames. Note that *region* means a group of pixels, but it could be as small as a single pixel. Also note that the terms *pel* and *pixel* have the same meaning. Both terms are used frequently in the field of signal and image processing.

This chapter is organized as follows. A general description of the recursive technique is provided in [Section 13.1](#). Some fundamental techniques in optimization are covered in [Section 13.2](#). [Section 13.3](#) describes the Netravali and Robbins algorithm, the pioneering work in this category. Several other typical pel-recursive algorithms are introduced in [Section 13.4](#). In [Section 13.5](#), a performance comparison between these algorithms is made.

13.1 Problem Formulation

In 1979, Netravali and Robbins published the first pel-recursive algorithm to estimate displacement vectors for motion compensated interframe image coding. In Netravali and Robbins (1979), a quantity, called the displaced frame difference (DFD), was defined as follows.

$$DFD(x, y; d_x, d_y) = f_n(x, y) - f_{n-1}(x - d_x, y - d_y) \quad (13.1)$$

where the subscript n and $n-1$ indicate two moments associated with two successive frames based on which motion vectors are to be estimated; x, y are coordinates in image planes, d_x, d_y are the two components of the displacement vector, \bar{d} , along the horizontal and vertical directions in the image planes, respectively. $DFD(x, y; d_x, d_y)$ can also be expressed as $DFD(x, y; \bar{d})$. Whenever it does not cause confusion, it can be written as DFD for the sake of brevity. Obviously, if there is no error in the estimation, i.e., the estimated displacement vector is exactly equal to the true motion vector, then DFD will be zero.

A nonlinear function of the DFD was then proposed as a dissimilarity measure in Netravali and Robbins (1979), which is a square function of DFD , i.e., DFD^2 .

Netravali and Robbins thus converted displacement estimation into a minimization problem. That is, each pixel corresponds to a pair of integers (x, y) , denoting its spatial position in the image plane. Therefore, the DFD is a function of \bar{d} . The estimated displacement vector $\bar{d} = (d_x, d_y)^T$, where $(.)^T$ denotes the transposition of the argument vector or matrix, can be determined by minimizing the DFD^2 . This is a typical nonlinear

programming problem, on which a large body of research has been reported in the literature. In the next section, several techniques that rely on a method, called descent method, in optimization are introduced. The Netravali and Robbins algorithm can be applied to a pixel once or iteratively applied several times for displacement estimation. Then the algorithm moves to the next pixel. The estimated displacement vector of a pixel can be used as an initial estimate for the next pixel. This recursion can be carried out horizontally, vertically, or temporally. By *temporally*, we mean that the estimated displacement vector can be passed to the pixel of the same spatial position within image planes in a temporally neighboring frame. Figure 13.1 illustrates these three different types of recursion.

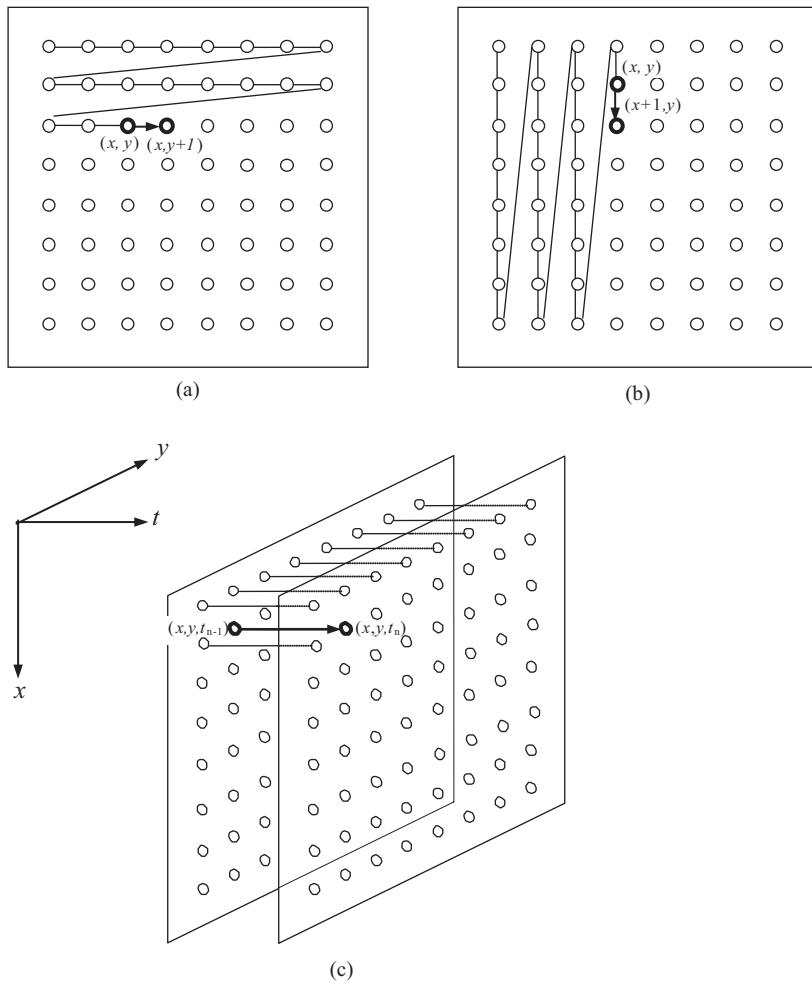


FIGURE 13.1
Three types of recursions (a) Horizontal, (b) Vertical, and (c) Temporal.

13.2 Descent Methods

Consider a nonlinear real-valued function z of a vector variable \bar{x} ,

$$z = f(\bar{x}) \quad (13.2)$$

with $\bar{x} \in R^n$, where R^n represents the set of all n -tuples of real numbers. The question we face now is how to find such a vector denoted by \bar{x}^* that the function z is minimized. This is classified as an unconstrained nonlinear programming problem.

13.2.1 First-Order Necessary Conditions

According to the optimization theory, if $f(\bar{x})$ has continuous first-order partial derivatives, then the first-order necessary conditions that \bar{x}^* has to satisfy are

$$\nabla f(\bar{x}^*) = 0 \quad (13.3)$$

where ∇ denotes the gradient operation with respect to \bar{x} evaluated at \bar{x}^* . Note that whenever there is only one vector variable in the function z to which the gradient operator is applied, the sign ∇ would remain without a subscript, as in Equation 13.3. Otherwise, i.e., if there is more than one vector variable in the function, we will explicitly write out the variable, to which the gradient operator is applied, as a subscript of the sign ∇ . In the component form, Equation 13.4 can be expressed as

$$\left\{ \begin{array}{l} \frac{\partial f(\bar{x})}{\partial x_1} = 0 \\ \frac{\partial f(\bar{x})}{\partial x_2} = 0 \\ \vdots \\ \frac{\partial f(\bar{x})}{\partial x_n} = 0 \end{array} \right. \quad (13.4)$$

13.2.2 Second-Order Sufficient Conditions

If $f(\bar{x})$ has second-order continuous derivatives, then the second-order sufficient conditions for $f(\bar{x}^*)$ to reach the minimum are known as:

$$\nabla f(\bar{x}^*) = 0 \quad (13.5)$$

and

$$H(\bar{x}^*) > 0 \quad (13.6)$$

where H denotes the Hessian matrix and is defined as follows.

$$H(\bar{x}) = \begin{bmatrix} \frac{\partial^2 f(\bar{x})}{\partial x_1^2} & \frac{\partial^2 f(\bar{x})}{\partial x_1 \partial x_2} & \cdots & \frac{\partial^2 f(\bar{x})}{\partial x_1 \partial x_n} \\ \frac{\partial^2 f(\bar{x})}{\partial x_2 \partial x_1} & \frac{\partial^2 f(\bar{x})}{\partial x_2^2} & \cdots & \frac{\partial^2 f(\bar{x})}{\partial x_2 \partial x_n} \\ \vdots & \vdots & \vdots & \vdots \\ \frac{\partial^2 f(\bar{x})}{\partial x_n \partial x_1} & \frac{\partial^2 f(\bar{x})}{\partial x_n \partial x_2} & \cdots & \frac{\partial^2 f(\bar{x})}{\partial x_n^2} \end{bmatrix} \quad (13.7)$$

We can thus see that the Hessian matrix consists of all the second-order partial derivatives of f with respect to the components of \bar{x} . Equation 13.6 means that the Hessian matrix H is positive definite.

13.2.3 Underlying Strategy

Our aim is to derive an iterative procedure for the minimization. That is, we want to find a sequence

$$\bar{x}_0, \bar{x}_1, \bar{x}_2, \dots, \bar{x}_n, \dots \quad (13.8)$$

such that

$$f(\bar{x}_0) > f(\bar{x}_1) > f(\bar{x}_2) > \dots > f(\bar{x}_n) > \dots \quad (13.9)$$

and the sequence converges to the minimum of $f(\bar{x})$, $f(\bar{x}^*)$.

A fundamental underlying strategy for almost all the descent algorithms (Luenberger 1984) is described next. We start with an initial point in the space; we determine a direction to move according to a certain rule; then we move along the direction to a relative minimum of the function z . This minimum point becomes the initial point for the next iteration.

This strategy can be better visualized using a two-dimensional example, shown in [Figure 13.2](#). There, $\bar{x} = (x_1, x_2)^T$. Several closed curves are referred to as *contour curves* or *level curves*. That is, each of the curves represents

$$f(x_1, x_2) = c \quad (13.10)$$

with c being a constant.

Assume that at the k th iteration, we have a guess: \bar{x}^k . For the $k+1$ th iteration, we need to

1. Find a search direction, pointed by a vector $\vec{\omega}^k$;
2. Determine an optimal step size α^k with $\alpha^k > 0$

such that the next guess \bar{x}^{k+1} is

$$\bar{x}^{k+1} = \bar{x}^k + \alpha^k \vec{\omega}^k \quad (13.11)$$

and \bar{x}^{k+1} satisfies $f(\bar{x}^k) > f(\bar{x}^{k+1})$.

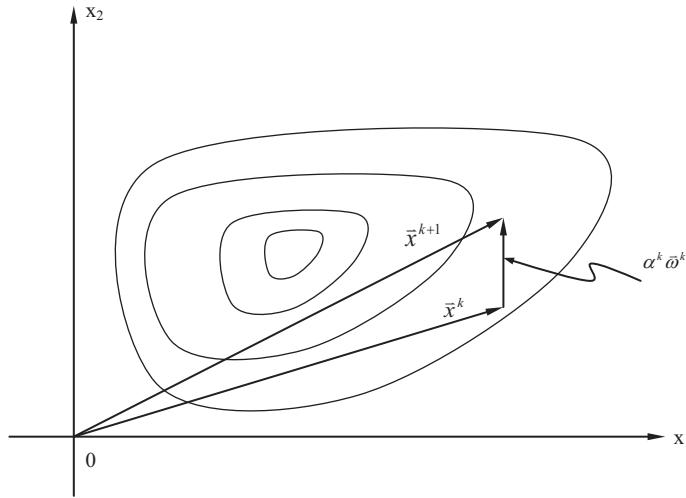


FIGURE 13.2
Descent method.

In Equation 13.11, \bar{x}^k can be viewed as a prediction vector for \bar{x}^{k+1} , while $\alpha^k \bar{\omega}^k$ an update vector, \bar{v}^k . Hence, using the Taylor series expansion, we can have

$$f(\bar{x}^{k+1}) = f(\bar{x}^k) + \langle \nabla f(\bar{x}^k), \alpha^k \bar{\omega}^k \rangle + \varepsilon \quad (13.12)$$

where $\langle \bar{s}, \bar{t} \rangle$ denotes the inner product between vectors \bar{s} and \bar{t} , and ε represents the higher-order terms in the expansion. Consider that the increment of $\alpha^k \bar{\omega}^k$ is small enough and, thus, ε can be ignored. From Equation 13.10, it is obvious that in order to have $f(\bar{x}^{k+1}) < f(\bar{x}^k)$ we must have $\langle \nabla f(\bar{x}^k), \alpha^k \bar{\omega}^k \rangle < 0$. That is,

$$f(\bar{x}^{k+1}) < f(\bar{x}^k) \Rightarrow \langle \nabla f(\bar{x}^k), \alpha^k \bar{\omega}^k \rangle < 0 \quad (13.13)$$

Choosing a different update vector, i.e., the product of the $\bar{\omega}^k$ vector and the step size α^k results in a different algorithm in implementing descent method.

In the same category of the descent method, a variety of techniques have been developed. The reader may refer to Luenberger (1984) or the many other existing books on optimization. Two commonly used techniques of the descent method are discussed below. One is called the steepest descent method, in which the search direction represented by the $\bar{\omega}$ vector is chosen to be opposite to that of the gradient vector, and a real parameter of the step size α^k is used; the other is the Newton-Raphson method, in which the update vector in estimation, determined jointly by the search direction and the step size, is related to the Hessian matrix, defined in Equation 13.7. These two techniques are further discussed in [Sections 13.2.5](#) and [13.2.6](#), respectively.

13.2.4 Convergence Speed

Speed of convergence is an important issue in discussing the descent method. It is utilized to evaluate the performance of different algorithms.

13.2.4.1 Order of Convergence

Assume a sequence of vectors $\{\bar{x}^k\}$, with $k = 0, 1, \dots, \infty$, converges to a minimum denoted by \bar{x}^* . We say that the convergence is of order p if the following formula holds (Luenberger 1984):

$$0 \leq \overline{\lim}_{k \rightarrow \infty} \frac{|\bar{x}^{k+1} - \bar{x}^*|}{|\bar{x}^k - \bar{x}^*|^p} < \infty \quad (13.14)$$

where p is positive, $\overline{\lim}$ denotes the limit superior, and $|.|$ indicates the magnitude or norm of a vector argument. For the two latter notions, more descriptions follow.

The concept of the limit superior is based on the concept of supremum. Hence, let us first discuss the supremum. Consider a set of real numbers, denoted by Q , that is bounded above. Then there must exist a smallest real number o such that for all the real numbers in the set Q , i.e., $q \in Q$, we have $q \leq o$. This real number o is referred to as the least upper bound or the supremum of the set Q , and it is denoted by

$$\sup\{q : q \in Q\} \text{ or } \sup_{q \in Q}(q) \quad (13.15)$$

Now, turn to a real bounded above sequence r^k , $k = 0, 1, \dots, \infty$. If $s^k = \sup\{r^j : j \geq k\}$, then the sequence $\{s^k\}$ converges to a real number s^* . This real number s^* is referred to as the limit superior of the sequence $\{r^k\}$, and is denoted by

$$\overline{\lim}_{k \rightarrow \infty}(r^k) \quad (13.16)$$

The magnitude or norm of a vector \bar{x} , denoted by $|\bar{x}|$, is defined as

$$|\bar{x}| = \langle \bar{x}, \bar{x} \rangle \quad (13.17)$$

where $\langle \bar{s}, \bar{t} \rangle$ is the inner product between the vector \bar{s} and \bar{t} . Throughout this discussion, when we say *vector*, we mean column vector. (Row vectors can be handled accordingly.) The inner product is therefore defined as

$$\langle \bar{s}, \bar{t} \rangle = \bar{s} \bar{t}^T \quad (13.18)$$

with the superscript T indicating the transposition operator.

With the definitions of the limit superior and the magnitude of a vector introduced, we are now in a position to easily understand the concept of the order of convergence defined in Equation 13.14. Since the sequences generated by the descent algorithms behave quite well in general (Luenberger 1984), the limit superior is rarely necessary. Hence, roughly speaking, instead of the limit superior, the limit may be used in considering the speed of convergence.

13.2.4.2 Linear Convergence

Among the various orders of convergence, the order of unity is of importance and is referred to as linear convergence. Its definition is as follows. If a sequence $\{\bar{x}^k\}$, $k = 0, 1, \dots, \infty$, converges to \bar{x}^* with

$$\lim_{k \rightarrow \infty} \frac{|\bar{x}^{k+1} - \bar{x}^*|}{|\bar{x}^k - \bar{x}^*|} = \gamma < 1 \quad (13.19)$$

then we say that this sequence converges linearly with a convergence ratio γ . The linear convergence is also referred to as geometric convergence because a linear convergent sequence with convergence ration γ converges to its limit at least as fast as the geometric sequences $c\gamma^k$, with c being a constant.

13.2.5 Steepest Descent Method

The steepest descent method, often referred to as the gradient method, is the oldest and simplest one among various techniques in the descent method. As Luenberger pointed out in his book (Luenberger 1984), it remains to be the fundamental method in the category for the following two reasons. First, owing to its simplicity, it is usually the first method attempted for solving a new problem. This observation is very true. As we shall see soon, when handling the displacement estimation as a nonlinear programming problem in the pel-recursive technique, the first algorithm developed by Netravali and Robbins is essentially the steepest descent method. Second, owing to the existence of a satisfactory analysis for the steepest descent method, it continues to serve as a reference for comparing and evaluating various newly developed and more advanced methods.

13.2.5.1 Formulae

In the steepest descent method, $\bar{\omega}^k$ is chosen as

$$\bar{\omega}^k = -\nabla f(\bar{x}^k) \quad (13.20)$$

resulting in

$$f(\bar{x}^{k+1}) = f(\bar{x}^k) - \alpha^k \nabla f(\bar{x}^k) \quad (13.21)$$

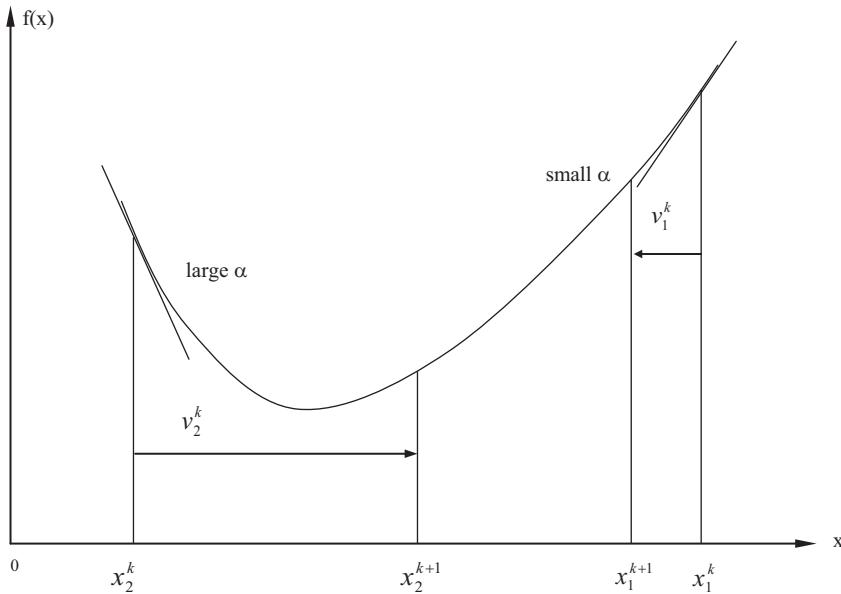
where the step size α^k is a real parameter, and, with our rule mentioned before, the sign ∇ here denotes a gradient operator with respect to \bar{x}^k . Since the gradient vector points to the direction along which the function $f(\bar{x})$ has greatest increases, it is naturally expected that the selection of the negative direction of the gradient as the search direction will lead to the steepest descent of $f(\bar{x})$. This is where the term *steepest descent* originated.

13.2.5.2 Convergence Speed

It can be shown that if the sequence $\{\bar{x}\}$ is bounded above, then the steepest descent method will converge to the minimum. Furthermore, it can be shown that the steepest descent method is linear convergent.

13.2.5.3 Selection of Step Size

It is worth noting that the selection of the step size α^k has significant influence on the algorithm's performance. In general, if it is small, it produces an accurate estimate of \bar{x}^* . But a smaller step size means it will take longer for the algorithm to reach the minimum.

**FIGURE 13.3**

An illustration of effect of selection of step size on minimization performance. Too small α requires more steps to reach x^* . Too large α may cause overshooting.

Although a larger step size will make algorithm converge faster, it may lead to an estimate with large error. This situation can be demonstrated in Figure 13.3. There, for the sake of an easy graphical illustration, \bar{x} is assumed to be one-dimensional. Two cases of too small (with subscript 1) and too large (with subscript 2) step sizes are shown for comparison.

13.2.6 Newton-Raphson's Method

The Newton-Raphson method is the next most popular method among various descent methods.

13.2.6.1 Formulae

Consider \bar{x}^k at the k th iteration. The $k+1$ th guess, \bar{x}^{k+1} , is the sum of \bar{x}^k and \bar{v}^k ,

$$\bar{x}^{k+1} = \bar{x}^k + \bar{v}^k \quad (13.22)$$

where \bar{v}^k is an update vector as shown in Figure 13.4. Now, expand the \bar{x}^{k+1} into the Taylor series explicitly containing the second-order term.

$$f(\bar{x}^{k+1}) = f(\bar{x}^k) + \langle \nabla f, \bar{v} \rangle + \frac{1}{2} \langle H(\bar{x}^k) \bar{v}, \bar{v} \rangle + \varphi, \quad (13.23)$$

where φ denotes the higher order terms, ∇ gradient, and H the Hessian matrix. If \bar{v} is small enough, we can ignore the φ . According to the first-order necessary conditions for \bar{x}^{k+1} to be the minimum, discussed in Section 13.2.1, we have

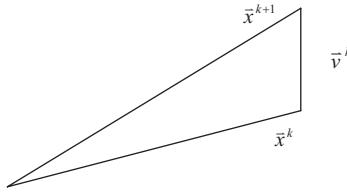


FIGURE 13.4
Derivation of Newton-Raphson's method.

$$\nabla_{\bar{v}} f(\bar{x}^k + \bar{v}) = \nabla f(\bar{x}^k) + H(\bar{x}^k)\bar{v} = 0, \quad (13.24)$$

where $\nabla_{\bar{v}}$ denotes the gradient operator with respect to \bar{v} . This leads to

$$\bar{v} = -H^{-1}(\bar{x}^k)\nabla f(\bar{x}^k) \quad (13.25)$$

The Newton-Raphson method is thus derived below.

$$f(\bar{x}^{k+1}) = f(\bar{x}^k) - H^{-1}(\bar{x}^k)\nabla f(\bar{x}^k) \quad (13.26)$$

Another loose and intuitive way to view the Newton-Raphson method is that its format is similar to the steepest descent method, except that the step size α^k is now chosen as $H^{-1}(\bar{x}^k)$, the inverse of the Hessian matrix evaluated at \bar{x}^k .

The idea behind the Newton-Raphson method is that the function being minimized is approximated locally by a quadratic function and this quadratic function is then minimized. It is noted that any function will behave like a quadratic function when it is close to the minimum. Hence, the closer to the minimum, the more efficient the Newton-Raphson method. This is the exact opposite of the steepest descent method, which works more efficiently at the beginning and less efficiently when close to the minimum. The price paid with the Newton-Raphson method is the extra calculation involved in evaluating the inverse of the Hessian matrix at \bar{x}^k .

13.2.6.2 Convergence Speed

Assume that the second-order sufficient conditions discussed in Section 13.2.2 are satisfied. Furthermore, assume that the initial point \bar{x}^0 is sufficiently close to the minimum \bar{x}^* . Then it can be shown that the Newton-Raphson method converges with an order of at least two. This indicates that the Newton-Raphson method converges faster than the steepest descent method.

13.2.6.3 Generalization and Improvements

In Luenberger (1984), a general class of algorithms is defined as

$$\bar{x}^{k+1} = \bar{x}^k - \alpha^k G \nabla f(\bar{x}^k) \quad (13.27)$$

where G denotes an $n \times n$ matrix and α^k a positive parameter. Both the steepest descent method and the Newton-Raphson method fall into this framework. It is clear that if G is an $n \times n$ identical matrix I , this general form reduces to the steepest descent method. If $G = H$ and $\alpha = 1$ then this is the Newton-Raphson method.

Although it descends rapidly near the solution, the Newton-Raphson method may not descend for points far away from the minimum because the quadratic approximation may not be valid there. The introduction of the α^k , which minimizes f , can guarantee the descent of f at the general points. Another improvement is to set $G = [\zeta^k I + H(\bar{x}^k)]^{-1}$ with $\zeta \geq 0$. Obviously, this is a combination of the steepest descent method and the Newton-Raphson method. The two extreme ends are the steepest method (very large ζ^k) and the Newton-Raphson method ($\zeta^k = 0$). For most cases, the selection of the parameter ζ^k aims at making the G matrix positive definite.

13.2.7 Other Methods

There are other gradient methods such as the Fletcher-Reeves method (also known as the conjugate gradient method) and the Fletcher-Powell-Davidon method (also known as the variable metric method). Reader may refer to (Luenberger 1984) or other optimization texts.

13.3 Netravali-Robbins' Pel-Recursive Algorithm

Having had an introduction to some basic nonlinear programming theory, we now turn to the pel-recursive technique in displacement estimation from the perspective of the descent methods. Let us take a look at the first pel-recursive algorithm, the Netravali-Robbins pel-recursive algorithm. It actually estimates displacement vectors using the steepest descent method to minimize the squared DFD. That is,

$$\bar{d}^{k+1} = \bar{d}^k - \frac{1}{2} \alpha \nabla_{\bar{d}} DFD^2(x, y, \bar{d}^k) \quad (13.28)$$

where $\nabla_{\bar{d}} DFD^2(x, y, \bar{d}^k)$ denotes the gradient of DFD^2 with respect to \bar{d} evaluated at \bar{d}^k , the displacement vector at the k th iteration, and α is positive. This equation can be further written as

$$\bar{d}^{k+1} = \bar{d}^k - \alpha DFD(x, y, \bar{d}^k) \nabla_{\bar{d}} DFD(x, y, \bar{d}^k) \quad (13.29)$$

Owing to Equation 13.1, the above equation leads to

$$\bar{d}^{k+1} = \bar{d}^k - \alpha DFD(x, y, \bar{d}^k) \nabla_{x,y} f_{n-1}(x - d_x, y - d_y) \quad (13.30)$$

where $\nabla_{x,y}$ means a gradient operator with respect to x and y . In Netravali and Robbins (1979) a constant of 1/1024 is assigned to α , i.e., 1/1024.

13.3.1 Inclusion of a Neighborhood Area

In order to make displacement estimation more robust, Netravali and Robbins considered an area for evaluating the DFD^2 in calculating the update term. More precisely, they assume

the displacement vector is constant within a small neighborhood Ω of the pixel for which the displacement is being estimated. That is,

$$\bar{d}^{k+1} = \bar{d}^k - \frac{1}{2} \alpha \nabla_{\bar{d}} \sum_{i,x,y_i \in \Omega} w_i DFD^2(x, y_i; \bar{d}^k) \quad (13.31)$$

where i represents an index for the i th pixel (x, y) within Ω , and w_i is the weight for the i th pixel in Ω . All the weights satisfy the following two constraints.

$$w_i \geq 0 \quad (13.32)$$

$$\sum_{i \in \Omega} w_i = 1 \quad (13.33)$$

This inclusion of a neighborhood area also explains why pel-recursive technique is classified into the category of region-matching techniques as we discussed at the beginning of this chapter.

13.3.2 Interpolation

It is noted that interpolation will be necessary when displacement vectors' components d_x and d_y are not integer number of pixels. A bilinear interpolation technique is used in Netravali and Robbins (1979). For the bilinear interpolation, readers may refer to [Chapter 10](#).

13.3.3 Simplification

To make the proposed algorithm more efficient in computation, Netravali and Robbins also proposed simplified versions of the displacement estimation and interpolation algorithms in their paper.

One simplified version of the Netravali and Robbins algorithm is as follows:

$$\bar{d}^{k+1} = \bar{d}^k - \alpha \operatorname{sign}\left\{ DFD(x, \bar{d}^k) \right\} \operatorname{sign}\left\{ \nabla_{x,y} f_{n-1}(x - d_x, y - d_y) \right\} \quad (13.34)$$

where $\operatorname{sign}\{s\} = 0, 1, -1$ depending on $s = 0, s > 0, s < 0$, respectively, while the sign of a vector quantity is the vector of signs of its components. In this version, the update vectors can only assume an angle that is an integer multiple of 45 degrees. As shown in Netravali and Robbins (1979), this version is effective.

13.3.4 Performance

The performance of the Netravali and Robbins algorithm has been evaluated using computer simulation (Netravali and Robbins 1979). Two video sequences with different amounts and different types of motion are tested. In either case, the proposed pel-recursive algorithm displays superior performance over the replenishment algorithm (Mounts 1969, Haskell 1979), which was discussed briefly in [Chapter 10](#). The Netravali and Robbins algorithm achieves a bit rate that is 22% to 50% lower than that required by the replenishment technique with the simple frame difference prediction.

13.4 Other Pel-Recursive Algorithms

The progress and success of the Netravali and Robbins algorithm stimulated great research interest in pel-recursive techniques. Many new algorithms have been developed. Some of them are discussed in this section.

13.4.1 Bergmann's Algorithm (1982)

Bergmann modified Netravali and Robbins' algorithm by using the Newton-Raphson method (Bergmann 1982). In doing so, the following difference between the fundamental framework of the descent methods discussed in [Section 13.2](#) and the minimization problem in displacement estimation discussed in [Section 13.3](#) needs to be noticed. That is, the object function $f(\bar{x})$ discussed in [Section 13.2](#) now becomes $DFD^2(x, y, \bar{d})$. The Hessian matrix H , consisting of the second-order partial derivatives of the $f(\bar{x})$ with respect to the components of \bar{x} , now become the second-order derivatives of DFD^2 with respect to d_x and d_y . Since the vector \bar{d} is a 2-D column vector now, the H matrix is a 2×2 matrix. That is,

$$H = \begin{bmatrix} \frac{\partial^2 DFD^2(x, y, \bar{d})}{\partial^2 d_x} & \frac{\partial^2 DFD^2(x, y, \bar{d})}{\partial d_x \partial d_y} \\ \frac{\partial^2 DFD^2(x, y, \bar{d})}{\partial d_y \partial d_x} & \frac{\partial^2 DFD^2(x, y, \bar{d})}{\partial^2 d_y} \end{bmatrix} \quad (13.35)$$

As expected, the Bergmann algorithm (1982) converges to the minimum faster than the steepest descent method since the Newton-Raphson method converges with an order of at least two.

13.4.2 Bergmann's Algorithm (1984)

Based on Burkhard and Moll's algorithm (1979), Bergmann developed an algorithm that is similar to the Newton-Raphson algorithm. The primary difference is that an average of two second-order derivatives is used to replace those in the Hessian matrix. In this sense, it can be considered as a variation of the Newton-Raphson algorithm.

13.4.3 Cafforio and Rocca's Algorithm

Based on their early work, Cafforio and Rocca proposed an algorithm in 1983 that is essentially the steepest descent method. That is, the step size α is defined as follows (Cafforio and Rocca 1983):

$$\alpha = \frac{1}{|\nabla f_{n-1}(x - d_x, y - d_y)|^2 + \eta^2} \quad (13.36)$$

with $\eta^2 = 100$. The addition of η^2 is intended to avoid the problem that would have occurred in a uniform region where the gradients are very small.

13.4.4 Walker and Rao's algorithm

Walker and Rao developed an algorithm based on the steepest descent method (Walker and Rao 1984, Tekalp 1995), and also with a variable step size. That is,

$$\alpha = \frac{1}{2|\nabla f_{n-1}(x - d_x, y - d_y)|^2} \quad (13.37)$$

where

$$\begin{aligned} |\nabla f_{n-1}(x - d_x, y - d_y)|^2 &= \\ \left(\frac{\partial f_{n-1}(x - d_x, y - d_y)}{\partial d_x} \right)^2 + \left(\frac{\partial f_{n-1}(x - d_x, y - d_y)}{\partial d_y} \right)^2 & \end{aligned} \quad (13.38)$$

It is observed that this step size is variable instead of being a constant. Furthermore, this variable step size is reverse proportional to the norm square of the gradient of $f_{n-1}(x - d_x, y - d_y)$ with respect to x, y . That means this type of step size will be small in the edge or rough area, and will be large in the relatively smooth area. These features are desirable.

Although it is quite similar to the Cafforio and Rocca algorithm, the Walker and Rao algorithm differs in the following two aspects. First, the α is selected differently. Second, implementation of the algorithm is different. For instance, instead of putting an η^2 in the denominator of α , the Walker and Rao algorithm uses a logic.

As a result of using the variable step size α , the convergence rate is improved substantially. This implies fast implementation and accurate displacement estimation. It was reported that usually one to three iterations are able to achieve quite satisfactory results in most cases.

Another contribution is that the Walker and Rao algorithm eliminates the need to transmit explicit address information so as to bring out higher coding efficiency.

13.5 Performance Comparison

A comprehensive survey of various algorithms using the pel-recursive technique can be found in a paper by Musmann et al. (1985). There, two performance features are compared among the algorithms. One is the convergence rate and hence the accuracy of displacement estimation. The other is the stability range. By *stability range*, we mean a range starting from which an algorithm can converge to the minimum of DFD^2 , or the true displacement vector.

Compared with the Netravali and Robbins algorithm, those improved algorithms discussed in the previous section do not use a constant step size, thus providing better adaptation to local image statistics. Consequently, they achieve a better convergence rate and more accurate displacement estimation. According to Bergmann (1984) and

Musmann et al. (1985), Bergmann's algorithm (1984) performs best among these various algorithms in terms of convergence rate and accuracy.

According to Musmann et al. (1985), the Newton-Raphson algorithm has a relatively smaller stability range than the other algorithms. This agrees with our discussion in [Section 13.2.2](#). That is, the performance of the Newton-Raphson method improves when it works in the area close to the minimum. The choice of the initial guess, however, is relatively more restricted.

13.6 Summary

The pel-recursive technique is one of three major approaches to displacement estimation for motion compensation. It recursively estimates displacement vectors in a pixel-by-pixel fashion. There are three types of recursion: horizontal, vertical, and temporal. Displacement estimation is carried out by minimizing the square of the DFD. Therefore, the steepest descent method and the Newton-Raphson method, the two most fundamental methods in optimization, naturally find their application in pel-recursive techniques. The pioneering Netravali and Robbins algorithm and several other algorithms such as Bergmann's (1982), Cafforio and Rocca's, Walker and Rao's, and Bergmann's (1984) are discussed in this chapter. They can be classified into one of two categories: The steepest-descent-based algorithms or the Newton-Raphson-based algorithms. [Table 13.1](#) contains a classification of these algorithms.

Note that the DFD can be evaluated within a neighborhood of the pixel for which a displacement vector is being estimated. The displacement vector is assumed constant within this neighborhood. This makes the displacement estimation more robust against various noises.

Compared with the replenishment technique with simple frame difference prediction (the first real interframe coding algorithm), the Netravali and Robbins algorithm (the first pel-recursive technique) achieves much higher coding efficiency. Specifically, a 22% to 50% saving in bit rate has been reported for some computer simulations. Several new pel-recursive algorithms have made further improvements in terms of the convergence rate and the estimation accuracy owing to the replacement of the fixed step size utilized in the Netravali and Robbins algorithms, which make these algorithms more adaptive to the local statistics in image frames.

TABLE 13.1
Classification of Several Pel-Recursive Algorithms

| Algorithms | Category I Steepest-Descent-Based | Category II Newton-Raphson-Based |
|-----------------------|--------------------------------------|-------------------------------------|
| Netravali and Robbins | Steepest-descent | |
| Bergmann (1982) | | Newton-Raphson |
| Walker and Rao | Variation of Steepest-descent | |
| Cafforio and Rocca | Variation of Steepest-descent | |
| Bergmann (1984) | | Variation of Newton-Raphson |

Exercises

- 13.1 What is the definition of the DFD? Justify Equation 12.1?
 - 13.2 Why does the inclusion of a neighborhood area make the pel-recursive algorithm more robust against noise?
 - 13.3 Compare the performance of the steepest descent method with that of the Newton-Raphson method.
 - 13.4 Explain the function of η^2 in the Cafforio and Rocca algorithm.
 - 13.5 What is the advantage you expect to have from the Walker and Rao algorithm?
 - 13.6 What is the difference between the Bergmann algorithm (1982) and the Bergmann algorithm (1984)?
 - 13.7 Why does the Newton-Raphson method have a smaller stability range?
-

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14

Optical Flow

As mentioned in [Chapter 11](#), optical flow is one of three major techniques that can be used to estimate displacement vectors from successive image frames. As opposed to the other two displacement estimation techniques discussed in [Chapters 12 and 13](#), block matching and pel-recursive method, however, the optical-flow technique was developed primarily for 3-D motion estimation in the computer vision community. Although it provides a relatively more accurate displacement estimation than the other two techniques, as we shall see in this and the next chapter, optical flow has not yet found wide applications for motion-compensated video coding. This is mainly due to the fact that there is a large number of motion vectors (one vector per pixel) involved, hence, the more side information that needs to be encoded and transmitted. As emphasized in [Chapter 11](#), we should not forget the ultimate goal in motion-compensated video coding: to encode video data with a *total* bit rate as low as possible, while maintaining a satisfactory quality of reconstructed video frames at the receiving end. If the extra bits required for encoding a large amount of optical-flow vectors counterbalance the bits saved in encoding the prediction error (owing to more accurate motion estimation), then the usage of optical flow in motion-compensated coding is not worthwhile. Besides, more computation is required in optical-flow determination. These factors have prevented optical flow from being practically utilized in motion-compensated video coding. With the continued advance in technologies, however, we believe this problem may be resolved in the near future. In fact, an initial, successful attempt has been made (Shi et al. 1998).

On the other hand, in theory, the optical-flow technique is of great importance in understanding the fundamental issues in 2-D motion determination, such as the aperture problem, the conservation and neighborhood constraints, and the distinction and relationship between 2-D motion and 2-D apparent motion.

In this chapter we will focus on the optical-flow technique. In [Section 14.1](#), as stated above, some fundamental issues associated with optical flow are addressed. [Section 14.2](#) discusses the differential method. The correlation method is covered in [Section 14.3](#). In [Section 14.4](#), a multiple-attributes approach is presented. Some performance comparisons between various techniques are included in [Sections 14.3 and 14.4](#). A summary is given in [Section 14.5](#).

14.1 Fundamentals

Optical flow is referred to as the 2-D distribution of apparent velocities of movement of intensity patterns in an image plane (Horn and Schunck 1981). In other words, an optical-flow field consists of a dense velocity field with one velocity vector for each pixel in the image plane. If we know the time interval between two consecutive images, which is

usually the case, then velocity vectors and displacement vectors can be converted from one to another. In this sense, optical flow is one of the techniques used for displacement estimation.

14.1.1 2-D Motion and Optical Flow

In the above definition, it is noted that the word *apparent* is used and nothing about 3-D motion in the scene is stated. The implication behind this observation is discussed in this subsection. We start with the definition of 2-D motion. 2-D motion is referred to as motion in a 2-D image plane caused by 3-D motion in the scene. That is, 2-D motion is the projection (commonly perspective projection) of 3-D motion in the scene onto the 2-D image plane. This can be illustrated by using a very simple example, shown in [Figure 14.1](#). There the world coordinate system $O\text{-}XYZ$ and the camera coordinate systems $o\text{-}xyz$ are aligned. The point C is the optical center of the camera. A point A_1 moves to A_2 , while its perspective projection moves correspondingly from a_1 to a_2 . We then see that a 2-D motion (from a_1 to a_2) in the image plane is invoked by a 3-D motion (from A_1 to A_2) in 3-D space. By a 2-D motion field, or sometimes image flow, we mean a dense 2-D motion field: One velocity vector for each pixel in the image plane.

Optical flow, according to its definition, is caused by movement of intensity patterns in an image plane. Therefore 2-D motion (field) and optical flow (field) are generally different. To support this conclusion, let us consider the following two examples. One is given by Horn and Schunck (1981). Imagine a uniform sphere rotating with a constant speed in the scene. Assume the luminance and all other conditions do not change at all when pictures are taken. Then, there is no change in brightness patterns in the images. According to the definition of optical flow, the optical flow is zero, whereas the 2-D motion field is obviously not zero. At the other extreme, consider a stationary scene; all objects in the 3-D world space are still. If illuminance changes when pictures are taken in such a way that there is movement of intensity patterns in image planes, optical flow may be nonzero. This confirms a statement made by Singh: the scene does not have to be in motion relative to the image for the optical-flow field to be nonzero (Singh 1991). It can be shown that the 2-D

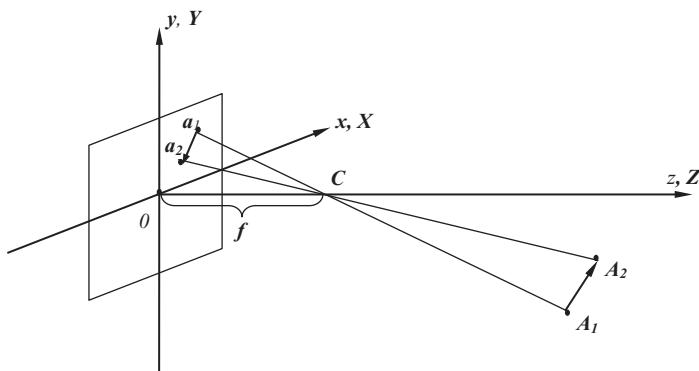


FIGURE 14.1
2-D motion versus 3-D motion.

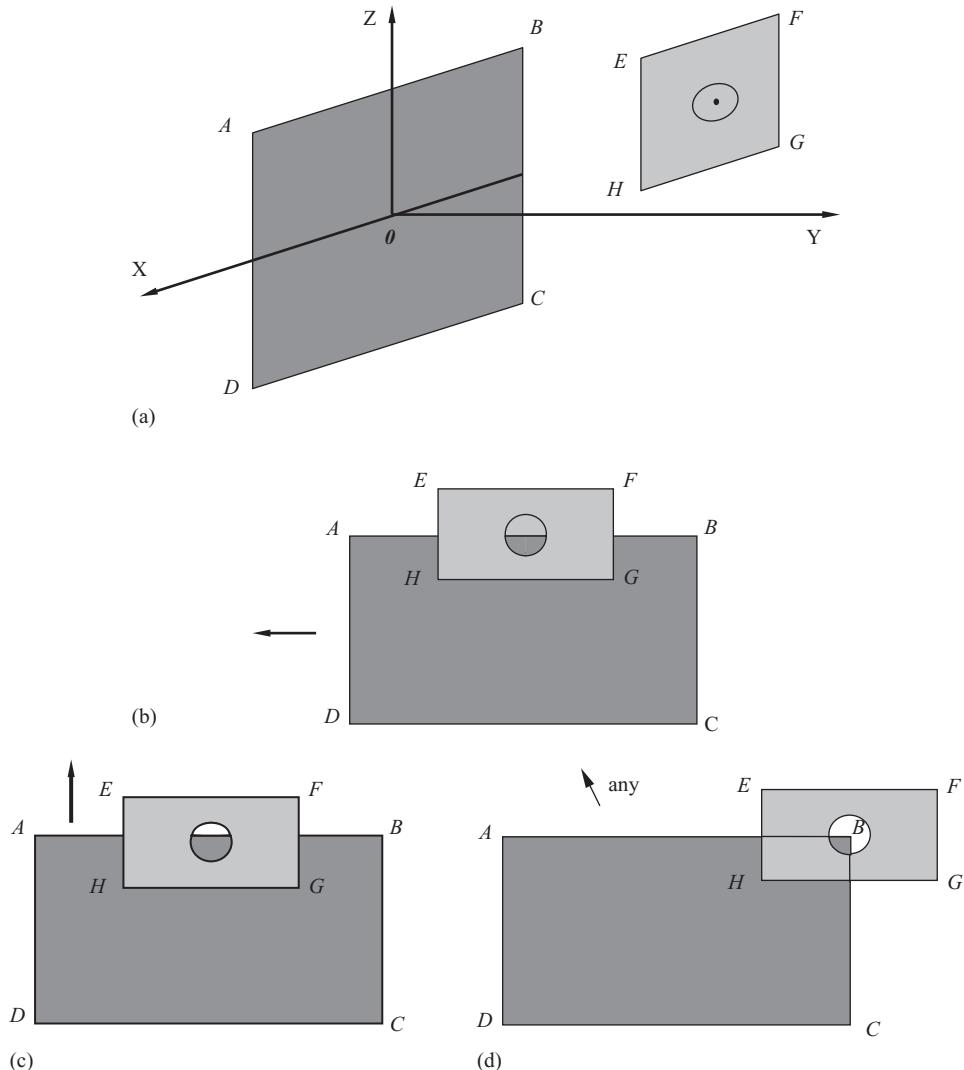
motion field and the optical-flow field are equal under certain conditions. Understanding the difference between the two quantities and the conditions under which they are equal is important.

This understanding can provide us with some sort of guide to evaluate the reliability of estimating 3-D motion from optical flow. This is because, in practice, time-varying image sequences are the only ones what we have at hand. The task in computer vision is to interpret 3-D motion from time-varying sequences. Therefore, we can only work with optical flow in estimating 3-D motion. Since the main focus of this book is on image and video coding, we do not cover these equality conditions here. Interested readers may refer to Singh (1991). In motion-compensated video coding, it is likewise true that the image frames and video data are only what we have at hand. We also, therefore, have to work with optical flow. Our attention is thus turned to optical-flow determination and its usage in video data compression.

14.1.2 Aperture Problem

Aperture problem is an important issue, originating in optics. Since it is inherent in the local estimation of optical flow, we address this issue in this subsection. In optics, apertures are openings in flat screens (Bracewell 1995). Therefore, apertures can have various shapes, such as circular, semicircular, and rectangular. Examples of apertures include a thin slit or array of slits in a screen. A circular aperture, a round hole made on the shutter of a window, was used by Newton to study the composition of sunlight. It is also well known that the circular aperture is of special interest in studying the diffraction pattern (Sears et al. 1986).

Roughly speaking, the aperture problem in motion analysis refers to the problem that occurs when viewing motion via an aperture, i.e., a small opening in a flat screen. In Marr (1982), it is stated that when a straight moving edge is observed through an aperture only the component of motion orthogonal to the edge can be measured. Let us examine some simple examples depicted in Figure 14.2. In Figure 14.2a, a large rectangular ABCD is located in the XOZ plane. A rectangular screen EFGH with a circular aperture is perpendicular to the OY axis. Figure 14.2b and c show, respectively, what is observed through the aperture when the rectangular ABCD is moving along the positive X and Z directions with a uniform speed. Since the circular opening is small and the line AB is very long, no motion will be observed in (b). Obviously, in (c) the upward movement can be observed clearly. In Figure 14.2d, the upright corner of the rectangle ABCD, angle B, appears. At this time the translation along any direction in the XOZ plane can be observed clearly. The phenomena observed in this example demonstrate that it is sometimes impossible to estimate motion of a pixel by only observing a small neighborhood surrounding it. The only motion that can be estimated from observing a small neighborhood is the motion orthogonal to the underlying moving contour. In Figure 14.2b, there is no motion orthogonal to the moving contour AB; the motion is aligned with the moving contour AB, which cannot be observed through the aperture. Therefore, no motion can be observed through the aperture. In Figure 14.2c, the observed motion is upward, which is perpendicular to the horizontal moving contour AB. In Figure 14.2d, any translation in the XOZ plane can be decomposed into horizontal and vertical components. Either of these two components is orthogonal to one of the two moving contours: AB or BC.

**FIGURE 14.2**

(a) Aperture problem: A large rectangle $ABCD$ is located in the XOZ plane. A rectangular screen $EFGH$ with a circular aperture is perpendicular to the OY axis, (b) Aperture problem: No motion can be observed through the circular aperture when the rectangular $ABCD$ is moving along the positive X direction, (c) Aperture problem: The motion can be observed through the circular aperture when the $ABCD$ is moving along the positive Z direction, and (d) Aperture problem: The translation of $ABCD$ along any direction in the XOZ plane can be observed through the circular aperture when the upright corner of the rectangle $ABCD$, angle B , appears in the aperture.

A more accurate statement on the aperture problem needs a definition of the so-called normal optical flow. The normal optical flow refers to the component of optical flow along the direction pointed by the local intensity gradient. Now, we can make a more accurate statement: the only motion in an image plane that can be determined is the normal optical flow.

In general, the aperture problem becomes severe in image regions where strong intensity gradients exist, such as at the edges. In image regions with strong higher-order intensity

variations, such as corners or textured areas, the true motion can be estimated. Singh provides a more elegant discussion on the aperture problem, in which he argues that the aperture problem should be considered as a continuous problem (it always exists, but in varying degrees of acuteness) instead of a binary problem (either it exists or it doesn't) (Singh 1991).

14.1.3 Ill-Posed Problem

Motion estimation from image sequences, including optical-flow estimation, belongs to the category of inverse problems. This is because we want to infer motion from given 2-D images, which is the perspective projection of 3-D motion. According to Hadamard (Bertero et al. 1988), a mathematical problem is well-posed if it possesses the following three characteristics:

1. Existence. That is, the solution exists.
2. Uniqueness. That is, the solution is unique.
3. Continuity. That is, when the error in the data tends toward zero, then the induced error in the solution tends toward zero as well.

Inverse problems usually are not well-posed in that the solution may not exist. In the example discussed in [Section 14.1.1](#), i.e., a uniform sphere rotated with illuminance fixed, the solution to motion estimation does not exist since no motion can be inferred from given images. The aperture problem discussed in [Section 14.1.2](#) is the case in which the solution to the motion may not be unique. Let us take a look at [Figure 14.2b](#). From the given picture, one cannot tell whether the straight-line AB is static or is moving horizontally. If it is moving horizontally, one cannot tell the moving speed. In other words, infinitely many solutions exist for the case. In optical-flow determination, we will see that computations are noise sensitive. That is, even a small error in the data can produce an extremely large error in the solution. Hence, we see that the motion estimation from image sequences suffers from all the three aspects just mentioned: nonexistence, nonuniqueness, and discontinuity. The last term is also referred to as the instability of the solution.

It is pointed out in Bertero et al. (1988) that all the low-level processing (also known as early vision) in computational vision are inverse problems and are often ill-posed. Examples in the low-level processing include motion recovery, computation of optical flow, edge detection, structure from stereo, structure from motion, structure from texture, shape from shading, and so on. Fortunately, the problem with early vision is mildly ill-posed in general. By *mildly*, we mean that a reduction of errors in the data can significantly improve the solution.

Since the early 1960s, the demand for accurate approximates and stable solutions in areas such as optics, radioastronomy, microscopy, and medical imaging has stimulated great research efforts in inverse problems, resulting in a unified theory: the regularization theory of ill-posed problems (Tikhonov and Arsenin 1977). In the discussion of optical-flow methods, we shall see that some regularization techniques have been posed and have improved accuracy in flow determination. More advanced algorithms continue to come.

14.1.4 Classification of Optical-Flow Techniques

Optical flow in image sequences provides important information regarding both motion and structure, and it is useful in such diverse fields as robot vision, autonomous navigation,

and video coding. Although this subject has been studied for more than a decade, reducing the error in the flow estimation remains a difficult problem. A comprehensive review and a comparison of the accuracy of various optical-flow techniques have recently been made (Barron et al. 1994). So far, most of the techniques in the optical-flow computations use one of the following basic approaches:

1. Gradient-based (Horn and Schunck 1981, Lucas and Kanade 1981, Nagel 1986, Uras et al. 1988, Szeliski et al. 1995, Black and Anandan 1996)
2. Correlation-based (Anandan 1989, Singh 1992, Pan et al. 1998)
3. Spatiotemporal energy-based (Adelson and Bergen 1985, Heeger 1988, Bigun et al. 1991)
4. Phase-based (Waxman et al. 1988, Fleet and Jepson 1990)

Besides these deterministic approaches, there is the stochastic approach to optical-flow computation (Konrad and Dubois 1992). In this chapter, we focus our discussion of optical flow on the gradient-based and correlation-based techniques because of their frequent applications in practice and fundamental importance in theory. We also discuss multiple attributes techniques in optical-flow determination. The other two approaches will be briefly touched when we discuss new techniques in motion estimation in the next chapter.

14.2 Gradient-Based Approach

It is noted that before the methods of optical-flow determination were actually developed, optical flow had been discussed and exploited for motion and structure recovery from image sequences in computer vision for years. That is, the optical-flow field was assumed to be available in the study of motion recovery. The first type of methods in optical-flow determination is referred to as gradient-based techniques. This is because the spatial and temporal partial derivatives of intensity function are utilized in these techniques. In this section, we shall present the Horn and Schunck algorithm. It is regarded as the most prominent representative of this category. After the basic concepts are presented, some other methods in this category are briefly discussed.

14.2.1 Horn and Schunck's Method

We shall begin with a very general framework (Shi et al. 1994) to derive a brightness time-invariance equation. We then introduce Horn and Schunck's method.

14.2.1.1 Brightness Invariance Equation

As stated in [Chapter 10](#), the imaging space can be represented by

$$f(x, y, t, \bar{s}) \quad (14.1)$$

where \bar{s} indicates the sensor's position in 3-D world space, i.e., the coordinates of the sensor center and the orientation of the optical axis of the sensor. The \bar{s} is a 5-D vector. That is

$\bar{s} = (\tilde{x}, \tilde{y}, \tilde{z}, \beta, \gamma)$ where \tilde{x} , \tilde{y} , and \tilde{z} represent the coordinate of the optical center of the sensor in the 3-D world space, and β and γ represent the orientation of the optical axis of the sensor in the 3-D world space; the Euler angles are pan and tilt, respectively.

With this very general notion, each picture, which is taken by a sensor located on a particular position at a specific moment, is merely a special cross-section of this imaging space. Both temporal and spatial image sequences become a proper subset of the imaging space.

Assume now a world point P in 3-D space that is perspectively projected onto the image plane as a pixel with the coordinates x_p and y_p . Then, x_p and y_p are also dependent on t and \bar{s} . That is,

$$f = f(x_p(t, \bar{s}), y_p(t, \bar{s}), t, \bar{s}) \quad (14.2)$$

If the optical radiation of the world point P is invariant with respect to the time interval from t_1 to t_2 , we then have:

$$f(x_p(t_1, \bar{s}_1), y_p(t_1, \bar{s}_1), t_1, \bar{s}_1) = f(x_p(t_2, \bar{s}_1), y_p(t_2, \bar{s}_1), t_2, \bar{s}_1) \quad (14.3)$$

This is the brightness time-invariance equation.

At a specific moment t_1 , if the optical radiation of P is isotropical we then get

$$f(x_p(t_1, \bar{s}_1), y_p(t_1, \bar{s}_1), t_1, \bar{s}_1) = f(x_p(t_1, \bar{s}_2), y_p(t_1, \bar{s}_2), t_1, \bar{s}_2) \quad (14.4)$$

This is the brightness space-invariance equation.

If both conditions are satisfied, we get the brightness time-and-space-invariance equation, i.e.,

$$f(x_p(t_1, \bar{s}_1), y_p(t_1, \bar{s}_1), t_1, \bar{s}_1) = f(x_p(t_2, \bar{s}_2), y_p(t_2, \bar{s}_2), t_2, \bar{s}_2) \quad (14.5)$$

Consider two brightness functions $f(x(t, \bar{s}), y(t, \bar{s}), t, \bar{s})$, and $f(x(t + \Delta t, \bar{s} + \Delta \bar{s}), y(t + \Delta t, \bar{s} + \Delta \bar{s}), t + \Delta t, \bar{s} + \Delta \bar{s})$ in which the variation in time, Δt , and the variation in the spatial position of the sensor, $\Delta \bar{s}$, are very small. Due to the time-and-space-invariance of brightness, we can get

$$f(x(t, \bar{s}), y(t, \bar{s}), t, \bar{s}) = f(x(t + \Delta t, \bar{s} + \Delta \bar{s}), y(t + \Delta t, \bar{s} + \Delta \bar{s}), t + \Delta t, \bar{s} + \Delta \bar{s}) \quad (14.6)$$

The expansion of the right-hand side of the above equation in the Taylor series at (t, \bar{s}) , and the use of Equation 14.5 lead to

$$\left(\frac{\partial f}{\partial x} u + \frac{\partial f}{\partial y} v + \frac{\partial f}{\partial t} \right) \Delta t + \left(\frac{\partial f}{\partial x} u^{\bar{s}} + \frac{\partial f}{\partial y} v^{\bar{s}} + \frac{\partial f}{\partial \bar{s}} \right) \Delta \bar{s} + \varepsilon = 0 \quad (14.7)$$

where $u = \frac{\Delta \partial x}{\partial t}$, $v = \frac{\Delta \partial y}{\partial t}$, $u^{\bar{s}} = \frac{\Delta \partial x}{\partial \bar{s}}$, $v^{\bar{s}} = \frac{\Delta \partial y}{\partial \bar{s}}$.

If $\Delta\bar{s} = 0$, i.e., the sensor, is static in a fixed spatial position (in other words, both the coordinate of the optical center of the sensor and its optical axis direction remain unchanged), dividing both sides of the equation by Δt and evaluating the limit as $\Delta t \rightarrow 0$ degenerate Equation 14.7 into

$$\frac{\partial f}{\partial x} u + \frac{\partial f}{\partial y} v + \frac{\partial f}{\partial t} = 0 \quad (14.8)$$

If $\Delta t = 0$, its both sides are divided by $\Delta\bar{s}$ and $\Delta\bar{s} \rightarrow 0$ is examined, Equation 14.7 then reduces to:

$$\frac{\partial f}{\partial x} u^{\bar{s}} + \frac{\partial f}{\partial y} v^{\bar{s}} + \frac{\partial f}{\partial \bar{s}} = 0 \quad (14.9)$$

When $\Delta t = 0$, i.e., at a specific time moment, the images generated with sensors at different spatial positions can be viewed as a spatial sequence of images. Equation 14.9 is, then, the equation for the spatial sequence of images.

For the sake of brevity, we shall focus on the gradient-based approach to optical-flow determination with respect to temporal image sequences. That is, in the rest of this section we shall address only Equation 14.8. It is noted that the derivation can be extended to spatial image sequences. The optical-flow technique for spatial image sequences is useful in stereo image data compression. It plays an important role in motion and structure recovery. Interested readers are referred to Shi et al. (1994), Shu and Shi (1993).

14.2.1.2 Smoothness Constraint

A careful examination of Equation 14.8 reveals that we have two unknowns: u and v , i.e., the horizontal and vertical components of an optical-flow vector at a three-tuple (x, y, t) , but only one equation to relate them. This once again demonstrates the ill-posed nature of optical-flow determination. This also indicates that there is no way to compute optical flow by considering a single point of the brightness pattern moving independently. As stated in [Section 14.1.3](#), some regularization measure—here an extra constraint—must be taken to overcome the difficulty.

A most popularly used constraint was proposed by Horn and Schunck and is referred to as the smoothness constraint. As the name implies, it constrains flow vectors to vary from one to another smoothly. Clearly, this is true for points in the brightness pattern most of the time, particularly for points belonging to the same object. It may be violated, however, along moving boundaries. Mathematically, the smoothness constraint is imposed in optical-flow determination by minimizing the square of the magnitude of the gradient of the optical-flow vectors:

$$\left(\frac{\partial u}{\partial x} \right)^2 + \left(\frac{\partial u}{\partial y} \right)^2 + \left(\frac{\partial v}{\partial x} \right)^2 + \left(\frac{\partial v}{\partial y} \right)^2 \quad (14.10)$$

It can be easily verified that the smoother the flow vector field, the smaller these quantities. Actually, the square of the magnitude of the gradient of intensity function with respect to the spatial coordinates, summed over a whole image or an image region, has been used as a smoothness measure of the image or the image region in the digital image processing literature (Gonzalez and Woods 1992).

14.2.1.3 Minimization

Optical-flow determination can then be converted into a minimization problem.

The square of the left-hand side of Equation 14.8, which can be derived from the brightness time-invariance equation, represents one type of error. It may be caused by quantization noise or other noises and can be written as

$$\varepsilon_b^2 = \left(\frac{\partial f}{\partial x} u + \frac{\partial f}{\partial y} v + \frac{\partial f}{\partial t} \right)^2 \quad (14.11)$$

The smoothness measure expressed in Equation 14.10 denotes another type of error, which is

$$\varepsilon_s^2 = \left(\frac{\partial u}{\partial x} \right)^2 + \left(\frac{\partial u}{\partial y} \right)^2 + \left(\frac{\partial v}{\partial x} \right)^2 + \left(\frac{\partial v}{\partial y} \right)^2 \quad (14.12)$$

The total error to be minimized is

$$\begin{aligned} \varepsilon^2 &= \sum_x \sum_y \varepsilon_b^2 + \alpha^2 \varepsilon_s^2 \\ &= \sum_x \sum_y \left(\frac{\partial f}{\partial x} u + \frac{\partial f}{\partial y} v + \frac{\partial f}{\partial t} \right)^2 + \alpha^2 \left[\left(\frac{\partial u}{\partial x} \right)^2 + \left(\frac{\partial u}{\partial y} \right)^2 + \left(\frac{\partial v}{\partial x} \right)^2 + \left(\frac{\partial v}{\partial y} \right)^2 \right] \end{aligned} \quad (14.13)$$

where α is a weight between these two types of errors. The optical-flow quantities u and v can be found by minimizing the total error. Using the calculus of variation, Horn and Schunck derived the following pair of equations for two unknowns, u and v , at each pixel in the image.

$$\begin{cases} f_x^2 u + f_x f_y v = \alpha^2 \nabla^2 u - f_x f_t \\ f_x f_y u + f_y^2 v = \alpha^2 \nabla^2 v - f_y f_t \end{cases} \quad (14.14)$$

where $f_x = \frac{\partial f}{\partial x}$, $f_y = \frac{\partial f}{\partial y}$, $f_t = \frac{\partial f}{\partial t}$; ∇^2 denotes the Laplacian operator. The Laplacian operators of u and v are defined below.

$$\begin{aligned} \nabla^2 u &= \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \\ \nabla^2 v &= \frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \end{aligned} \quad (14.15)$$

14.2.1.4 Iterative Algorithm

Instead of using classical algebraic method to solve the pair of equations for u and v , Horn and Schunck adopted the Gaussian Seidel (Ralston and Rabinowitz 1978) method to have the following iterative procedure:

$$\begin{aligned} u^{k+1} &= \bar{u}^k - \frac{f_x[f_x\bar{u}^k + f_y\bar{v}^k + f_t]}{\alpha^2 + f_x^2 + f_y^2} \\ v^{k+1} &= \bar{v}^k - \frac{f_y[f_x\bar{u}^k + f_y\bar{v}^k + f_t]}{\alpha^2 + f_x^2 + f_y^2} \end{aligned} \quad (14.16)$$

where the superscripts k and $k + 1$ are indexes of iteration; and \bar{u}, \bar{v} are the local averages of u and v , respectively.

Horn and Schunck define \bar{u}, \bar{v} as follows:

$$\begin{aligned} \bar{u} &= \frac{1}{6}\{u(x, y+1) + u(x, y-1) + u(x+1, y) + u(x-1, y)\} \\ &\quad + \frac{1}{12}\{u(x-1, y-1) + u(x-1, y+1) + u(x+1, y-1) + u(x+1, y+1)\} \\ \bar{v} &= \frac{1}{6}\{v(x, y+1) + v(x, y-1) + v(x+1, y) + v(x-1, y)\} \\ &\quad + \frac{1}{12}\{v(x-1, y-1) + v(x-1, y+1) + v(x+1, y-1) + v(x+1, y+1)\} \end{aligned} \quad (14.17)$$

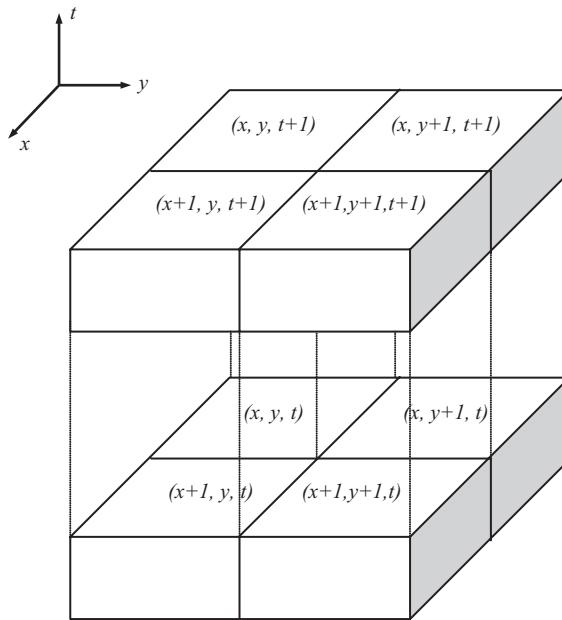
The estimation of the partial derivatives of intensity function and the Laplacian of flow vectors need to be addressed. Horn and Schunck considered a $2 \times 2 \times 2$ spatiotemporal neighborhood, shown in [Figure 14.3](#), for estimation of partial derivatives f_x, f_y and f_t . Note that replacing the first-order differentiation by the first-order difference is a common practice in managing digital images. The arithmetic average can remove the noise effect, thus making the obtained first-order differences less sensitive to various noises.

The Laplacian of u and v are approximated by

$$\begin{aligned} \nabla^2 u &= \bar{u}(x, y) - u(x, y) \\ \nabla^2 v &= \bar{v}(x, y) - v(x, y) \end{aligned} \quad (14.18)$$

Equivalently, the Laplacian of u and v , $\nabla^2(u)$ and $\nabla^2(v)$, can be obtained by applying a 3×3 window operator, shown in [Figure 14.4](#), to each point in the u and v planes, respectively.

Similar to the pel-recursive technique discussed in the previous chapter, there are two different ways to iterate. One way is to iterate at a pixel until a solution is steady. Another way is to iterate only once for each pixel. In the latter case, a good initial flow vector is required and is usually derived from the previous pixel.

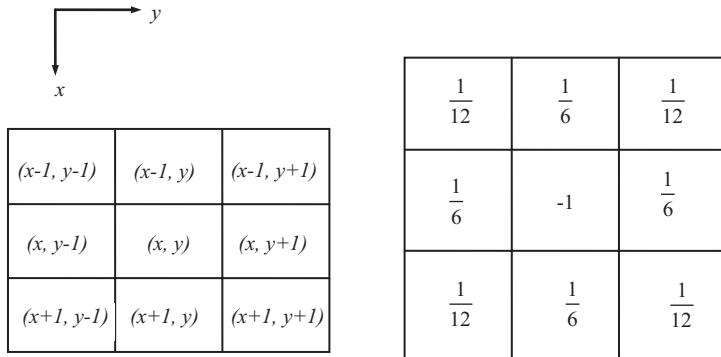


$$\begin{aligned}
 f_x &= \frac{1}{4} \{ [f(x+1, y, t) - f(x, y, t)] + [f(x+1, y, t+1) - f(x, y, t+1)] \\
 &\quad + [f(x+1, y+1, t) - f(x, y, t)] + [f(x+1, y+1, t+1) - f(x, y+1, t+1)] \} \\
 f_y &= \frac{1}{4} \{ [f(x, y+1, t) - f(x, y, t)] + [f(x+1, y+1, t) - f(x+1, y, t)] \\
 &\quad + [f(x, y+1, t+1) - f(x, y, t+1)] + [f(x+1, y+1, t+1) - f(x+1, y, t+1)] \} \\
 f_t &= \frac{1}{4} \{ [f(x, y, t+1) - f(x, y, t)] + [f(x+1, y, t+1) - f(x+1, y, t)] \\
 &\quad + [f(x, y+1, t+1) - f(x, y+1, t)] + [f(x+1, y+1, t+1) - f(x+1, y+1, t)] \}
 \end{aligned}$$

FIGURE 14.3
Estimation of f_x , f_y and f_t .

14.2.2 Modified Horn and Schunck Method

Observing that the first-order difference is used to approximate the first-order differentiation in Horn and Schunck's original algorithm, and regarding this as a relatively crude form and a source of error, Barron et al. (1994) developed a modified version of the Horn and Schunck method.



$$\begin{aligned}\nabla^2 u &\approx \frac{1}{6} [u(x-1, y) + u(x, y-1) + u(x, y+1) + u(x+1, y)] \\ &\quad + \frac{1}{12} [u(x-1, y-1) + u(x-1, y+1) + u(x+1, y-1) + u(x+1, y+1)] \\ &\quad - u(x, y) \\ \nabla^2 v &\approx \frac{1}{6} [v(x-1, y) + v(x, y-1) + v(x, y+1) + v(x+1, y)] \\ &\quad + \frac{1}{12} [v(x-1, y-1) + v(x-1, y+1) + v(x+1, y-1) + v(x+1, y+1)] \\ &\quad - v(x, y)\end{aligned}$$

FIGURE 14.4

A 3×3 window operation for estimation of the Laplacian of flow vector.

It features a spatiotemporal presmoothing and a more advanced approximation of differentiation. Specifically, it uses a Gaussian filter as a spatiotemporal prefilter. By the term *Gaussian filter*, we mean a low-pass filter with a mask shaped similar to that of the Gaussian probability density function. This is similar to what was utilized in the formulation of the Gaussian pyramid, which was discussed in [Chapter 11](#). The term *spatiotemporal* means that the Gaussian filter is used for low-pass filtering in both spatial and temporal domains.

With respect to the more advanced approximation of differentiation, a four-point central difference operator is used, which has a mask, shown in [Figure 14.5](#).

As we shall see later in this chapter, this modified Horn and Schunck algorithm has achieved better performance than the original one owing to the two above-mentioned measures. This success indicates that a reduction of noise in image (data) leads to a significant reduction of noise in optical flow (solution). This example supports the statement we mentioned earlier that the ill-posed problem in low level computational vision is mildly ill-posed.

| | | | | |
|-----------------|----------------|---|-----------------|----------------|
| $-\frac{1}{12}$ | $\frac{8}{12}$ | 0 | $-\frac{8}{12}$ | $\frac{1}{12}$ |
|-----------------|----------------|---|-----------------|----------------|

FIGURE 14.5

Four-point central difference operator mask.

14.2.3 Lucas and Kanade's Method

Lucas and Kanade assume a flow vector is constant within a small neighborhood of a pixel, denoted by Ω . Then they form a weighted object function as follows.

$$\sum_{(x,y) \in \Omega} w^2(x,y) \left[\frac{\partial f(x,y,t)}{\partial x} u + \frac{\partial f(x,y,t)}{\partial v} v + \frac{\partial f(x,y,t)}{\partial t} \right]^2 \quad (14.19)$$

where $w(x, y)$ is a window function, which gives more weight to the central portion than the surrounding portion of the neighborhood Ω .

The flow determination thus becomes a problem of a least square fit of the brightness invariance constraint. We observe that the smoothness constraint has been implied in Equation 14.19, where the flow vector is assumed to be constant within Ω .

14.2.4 Nagel's Method

Nagel first used the second-order derivatives in optical-flow determination in the very early days (Nagel 1983). Since the brightness function $f(x, y, t, \bar{s})$ is a real-valued function of multiple variables (or a vector of variables), the Hessian matrix, discussed in [Chapter 12](#), is used for the second-order derivatives.

An oriented-smoothness constraint was developed by Nagel that prohibits imposition of the smoothness constraint across edges, as illustrated in [Figure 14.6](#). In the figure, an edge AB separates two different moving regions: region 1 and region 2. The smoothness constraint is imposed in these regions separately. That is, no smoothness constraint is imposed across the edge. Obviously, it would be a disaster if we smoothed the flow vectors across the edge. As a result, this reasonable treatment effectively improves the accuracy of optical-flow estimation (Nagel 1989).

14.2.5 Uras, Girosi, Verri, and Torre's Method

The Uras, Girosi, Verri, and Torre method is another method that uses second-order derivatives. Based on a local procedure, it performs quite well (Uras et al. 1988).

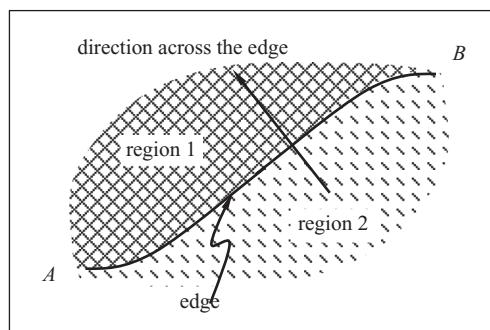


FIGURE 14.6
Oriented-smoothness constraint.

14.3 Correlation-Based Approach

The correlation-based approach to optical-flow determination is similar to block matching, covered in [Chapter 11](#). As may be recalled, the conventional block-matching technique partitions an image into nonoverlapped, fixed-size, rectangle blocks. Then, for each block, the best matching in the previous image frame is found. In doing so, a search window is opened in the previous frame according to some *priori* knowledge: the time interval between the two frames and the maximum possible moving velocity of objects in frames. Centered on each of the candidate pixels in the search window, a rectangle correlation window of the same size as the original block is opened. The best-matched block in the search window is chosen such that either the similarity measure is maximized or the dissimilarity measure is minimized. The relative spatial position between these two blocks (the original block in the current frame and the best-matched one in the previous frame) gives a translational motion vector to the original block. In the correlation-based approach to optical-flow computation, the mechanism is very similar to that in the conventional block matching. The only difference is that for each pixel in an image, we open a rectangle correlation window centered on this pixel for which an optical-flow vector needs to be determined. It is for this correlation window that we find the best match in the search window in its temporal neighboring image frame. This is shown in [Figure 14.7](#). A comparison between [Figures 14.7](#) and [11.1](#) can convince us about the above observation. In this section, we first briefly discuss Anandan's method, which is a pioneer work in this category. Then Singh's method is described. His unified view of optical-flow computation is introduced. We then present a correlation-feedback method by Pan, Shi, and Shu, which uses the feedback technique in flow calculation.

14.3.1 Anandan's Method

As mentioned in [Chapter 11](#), the sum of squared difference (SSD) is used as a dissimilarity measure in Anandan (1987). It is essentially a simplified version of the well-known mean

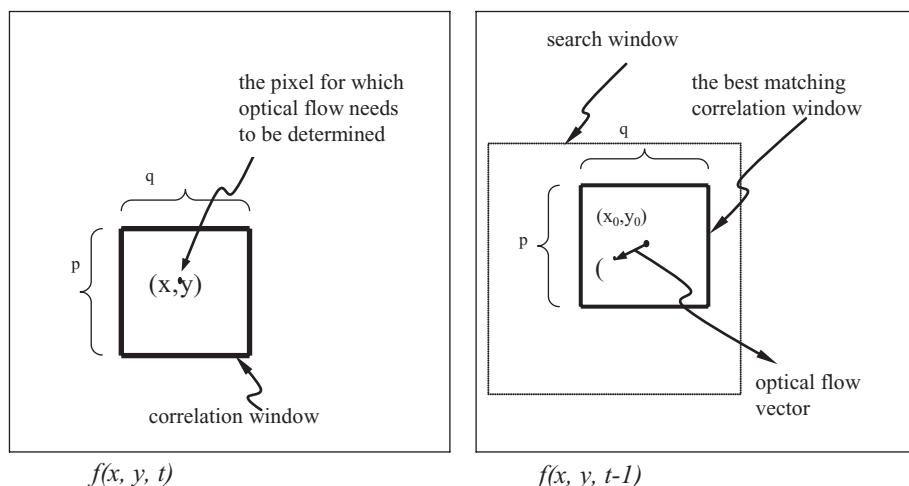


FIGURE 14.7

Correlation-based approach to optical-flow determination.

square error (MSE). Due to its simplicity, it is used in the methods developed by Singh (1992) and Pan et al. (1998).

In Anandan's method (1989), a pyramid structure is formed, and it can be used for an efficient coarse-fine search. This is very similar to the multiresolution block-matching techniques discussed in [Chapter 12](#). In the higher levels (with lower resolution) of the pyramid, a full search can be performed without a substantial increase in computation. The estimated velocity (or displacement) vector can be propagated to the lower levels (with higher resolution) for further refinement. As a result, a relatively large motion vector can be estimated with a certain degree of accuracy.

Instead of the Gaussian pyramid discussed in [Chapter 12](#), however, a Laplacian pyramid is used here. To understand the Laplacian pyramid, let us take a look at [Figure 14.8a](#). There, two consecutive levels are shown in a Gaussian pyramid structure: level k , denoted by $f^k(x, y)$, and level $k+1$, $f^{k+1}(x, y)$. Part (b) of the figure shows how level $k+1$ can be derived from level k in the Gaussian pyramid. That is, as stated in [Chapter 12](#), level $k+1$ in the Gaussian pyramid can be obtained through low-pass filtering applied to level k , followed by subsampling. In part (c), level $k+1$ is first interpolated, thus producing an estimate of level k , $\hat{f}^k(x, y)$. The difference between the original level k and the interpolated estimate of level k generates an error at level k , denoted by $e^k(x, y)$. If there are no quantization errors involved, then level k , $f^k(x, y)$ can be recovered completely from the interpolated estimate of level k , $\hat{f}^k(x, y)$, and the error at level k , $e^k(x, y)$. That is,

$$f^k(x, y) = \hat{f}^k(x, y) + e^k(x, y) \quad (14.20)$$

With quantization errors, however, the recovery of level k , $f^k(x, y)$ is not error free. It can be shown that coding $\hat{f}^k(x, y)$ and $e^k(x, y)$ is more efficient than directly coding $f^k(x, y)$.

A set of images $e^k(x, y)$, $k = 0, 1, \dots, k-1$ and $f^k(x, y)$ forms a Laplacian pyramid. Part (d) in [Figure 14.8](#) displays a Laplacian pyramid with $k = 5$. It can be shown that Laplacian pyramids provide an efficient way for image coding (Burt and Adelson 1983). A more detailed description of Gaussian and Laplacian pyramids can be found in Burt (1984), Lim (1990).

14.3.2 Singh's Method

Singh presented a unified point of view on optical-flow computation in Singh (1991, 1992). He classified the information available in image sequences for optical-flow determination into two categories: conservation information and neighborhood information. Conservation information is the information assumed to be conserved from one image frame to the next in flow estimation. Intensity is an example of conservation information, which is used most frequently in flow computation. Clearly, the brightness invariance constraint in the Horn and Schunck method is another way to state this type of conservation. Some functions of intensity may be used as conservation information as well. In fact, Singh uses the Laplacian of intensity as conservation information for computational simplicity. More examples can be found later in [Section 14.4](#). Other information, different from intensity, such as color, can be used as conservation information. Neighborhood information is the information available in the neighborhood of the pixel from which optical flow is estimated.

These two different types of information correspond to two steps in flow estimation. In the first step, conservation information is extracted, resulting in an initial estimate of flow vector. In the second step, this initial estimate is propagated into a neighborhood area

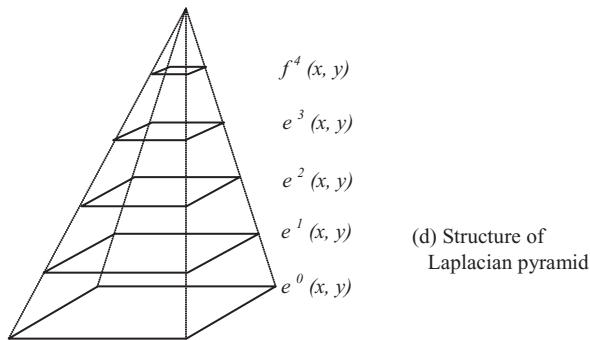
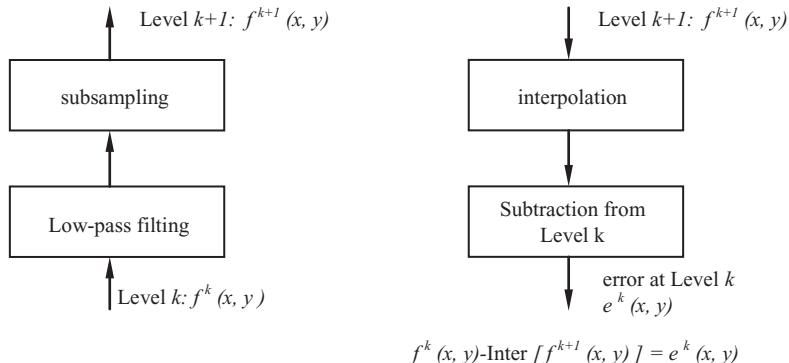
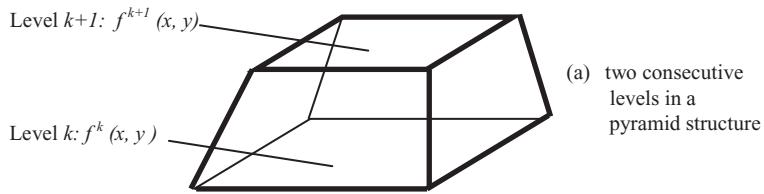


FIGURE 14.8
Laplacian pyramid (Level k in a Gaussian Pyramid).

and is iteratively updated. Obviously, in the Horn and Schunck method, the smoothness constraint is essentially one type of neighborhood information. Iteratively, estimates of flow vectors are refined with neighborhood information so that flow estimators from areas having sufficient intensity variation, such as the intensity corners as shown Figure 14.2d and areas with strong texture, can be propagated into areas with relatively small intensity variation or uniform intensity distribution.

With this unified point of view on optical-flow estimation, Singh treated flow computation as parameter estimation. By applying estimation theory to flow computation, he developed an estimation-theoretical method to determine optical flow. It is a correlation-based method and consists of the above-mentioned two steps.

14.3.2.1 Conservation Information

In the first step, for each pixel (x, y) in the current frame $f_n(x, y)$, a correlation window of $(2l + 1) \times (2l + 1)$ is opened, centered on the pixel. A search window of $(2N + 1) \times (2N + 1)$ is opened in the previous frame $f_{n-1}(x, y)$ centered on (x, y) . An error distribution of those $(2N + 1) \times (2N + 1)$ samples are calculated by using SSD as follows:

$$E_c(u, v) = \sum_{s=-l}^l \sum_{t=-l}^l [f_n(x+s, y+t) - f_{n-1}(x-u+s, y-v+t)]^2 \quad -N \leq u, v \leq N \quad (14.21)$$

A response-distribution for these $(2N + 1) \times (2N + 1)$ samples is then calculated.

$$R_c(u, v) = e^{-\beta E_c(u, v)} \quad (14.22)$$

where β is a parameter, whose function and selection will be described in [Section 14.3.3.1](#).

According to the weighted-least-square estimation, the optical flow can be estimated in this step as follows:

$$\begin{aligned} u_c &= \frac{\sum_u \sum_v R_c(u, v) u}{\sum_u \sum_v R_c(u, v)} \\ v_c &= \frac{\sum_u \sum_v R_c(u, v) v}{\sum_u \sum_v R_c(u, v)} \end{aligned} \quad (14.23)$$

Assuming errors are additive and zero-mean random noise, we can also find the covariance matrix associated with the above estimate:

$$S_c = \left(\begin{array}{cc} \frac{\sum_u \sum_v R_c(u, v) (u - u_c)^2}{\sum_u \sum_v R_c(u, v)} & \frac{\sum_u \sum_v R_c(u, v) (u - u_c)(v - v_c)}{\sum_u \sum_v R_c(u, v)} \\ \frac{\sum_u \sum_v R_c(u, v) (u - u_c)(v - v_c)}{\sum_u \sum_v R_c(u, v)} & \frac{\sum_u \sum_v R_c(u, v) (v - v_c)^2}{\sum_u \sum_v R_c(u, v)} \end{array} \right) \quad (14.24)$$

14.3.2.2 Neighborhood Information

After step 1, all initial estimates are available. In step 2, they need to be refined according to neighborhood information. For each pixel, the method considers a $(2w + 1) \times (2w + 1)$ neighborhood centered on it. The optical flow of the center pixel is updated from the estimates in the neighborhood. A set of Gaussian coefficients is used in the method such that the closer the neighbor pixel to the center pixel, the more influence the neighbor pixel has on the flow vector of the center pixel. The weighted-least-square based estimate in this step is

$$\bar{u} = \frac{\sum_u \sum_v R_n(u, v) u}{\sum_u \sum_v R_n(u, v)} \quad (14.25)$$

$$\bar{v} = \frac{\sum_u \sum_v R_n(u, v) v}{\sum_u \sum_v R_n(u, v)}$$

and the associated covariance matrix is

$$S_c = \begin{pmatrix} \frac{\sum_i R_n(u_i, v_i)(u_i - \bar{u})^2}{\sum_i R_n(u_i, v_i)} & \frac{\sum_i R_n(u_i, v_i)(u_i - \bar{u})(v_i - \bar{v})}{\sum_i R_n(u_i, v_i)} \\ \frac{\sum_i R_n(u_i, v_i)(u_i - \bar{u})(v_i - \bar{v})}{\sum_i R_n(u_i, v_i)} & \frac{\sum_i R_n(u_i, v_i)(v_i - \bar{v})^2}{\sum_i R_n(u_i, v_i)} \end{pmatrix} \quad (14.26)$$

where $1 \leq i \leq (2w+1)^2$.

In implementation, Singh uses a 3×3 neighborhood (i.e., $w = 1$) centered on the pixel under consideration. The weights are depicted in [Figure 14.9](#).

14.3.2.3 Minimization and Iterative Algorithm

According to estimation theory (Beck and Arnold 1977), two covariance matrices, expressed in Equations 14.24 and 14.26, respectively, are related to the confidence measure. That is, the reciprocals of the eigenvalues of the covariance matrix reveal confidence of the

| | | |
|--|--------------------------------------|--|
| (0.25×0.25) $\frac{1}{16}$ | (0.5×0.25) $\frac{1}{8}$ | (0.25×0.25) $\frac{1}{16}$ |
| (0.5×0.25) $\frac{1}{8}$ | (0.5×0.5) $\frac{1}{4}$ | (0.5×0.25) $\frac{1}{8}$ |
| (0.25×0.25) $\frac{1}{16}$ | (0.5×0.25) $\frac{1}{8}$ | (0.25×0.25) $\frac{1}{16}$ |

FIGURE 14.9
3 \times 3 Gaussian mask.

estimate along the direction represented by the corresponding eigenvectors. Moreover, conservation error and neighborhood error can be represented as the following two quadratic terms, respectively.

$$(U - U_c)^T S_c^{-1} (U - U_c) \quad (14.27)$$

$$(U - \bar{U})^T S_n^{-1} (U - \bar{U}) \quad (14.28)$$

where $\bar{U} = (\bar{u}, \bar{v})$, $U_c = (u_c, v_c)$, $U = (u, v)$

$$\begin{array}{ccc} (0.25 \times 0.25) & (0.5 \times 0.25) & (0.25 \times 0.25) \\ \frac{1}{16} & \frac{1}{8} & \frac{1}{16} \\ \hline (0.5 \times 0.25) & (0.5 \times 0.5) & (0.5 \times 0.25) \\ \frac{1}{8} & \frac{1}{4} & \frac{1}{8} \\ \hline (0.25 \times 0.25) & (0.5 \times 0.25) & (0.25 \times 0.25) \\ \frac{1}{16} & \frac{1}{8} & \frac{1}{16} \end{array}$$

The minimization of the sum of these two errors over the image area leads to an optimal estimate of optical flow. That is, find (u, v) such that the following error is minimized.

$$\sum_x \sum_y [(U - U_c)^T S_c^{-1} (U - U_c) + (U - \bar{U})^T S_n^{-1} (U - \bar{U})] \quad (14.29)$$

An iterative procedure according to the Gauss-Siedel algorithm (Ralston and Rabinowitz 1978) is used by Singh:

$$\begin{aligned} U^{k+1} &= [S_c^{-1} + S_n^{-1}]^{-1} [S_c^{-1} U_c + S_n^{-1} \bar{U}^k] \\ U^0 &= U_c \end{aligned} \quad (14.30)$$

Note that U_c , S_c are calculated once and remain unchanged in all the iterations. On the contrary, \bar{U} and S_n vary with each iteration. This agrees with the description of the method in [Section 14.3.2.2](#).

14.3.3 Pan, Shi, and Shu's Method

Applying feedback (a powerful technique widely used in automatic control and many other fields) to a correlation-based algorithm, Pan, Shi, and Shu developed a correlation-feedback method to compute optical flow. The method is iterative in nature. In each iteration, the estimated optical flow and its several variations are fed back. For each of the varied optical-flow vectors, the corresponding sum of squared displaced frame difference (DFD), which was discussed in [Chapter 12](#), and often involves bilinear interpolation, is calculated. This useful information is then utilized in a revised version of a correlation-based algorithm (Singh 1992). They choose to work with this algorithm because it has several merits, and its estimation-theoretical computation framework lends itself to the application of the feedback technique.

As expected, the repeated usage of two given images via the feedback iterative procedure improves the accuracy of optical flow considerably. Several experiments on real image sequences in the laboratory and some synthetic image sequences demonstrate that the correlation-feedback algorithm performs better than some standard gradient- and correlation-based algorithms in terms of accuracy.

14.3.3.1 Proposed Framework

The block diagram of the proposed framework is shown in [Figure 14.10](#) and described next.

14.3.3.1.1 Initialization

Although any flow algorithms can be used to generate an initial optical-flow field $\bar{u}^0 = (u^0, v^0)$ (even a non-zero initial flow field without applying any flow algorithm may work, but slowly), the Horn and Schunck algorithm (1981), discussed in [Section 14.2.1](#) (usually 5 to 10 iterations) is used to provide an appropriate starting point after preprocessing (involving low-pass filtering), since the algorithm is fast and the problem caused by the smoothness constraint is not serious in the first 10 to 20 iterations. The modified Horn and Schunck method, discussed in [Section 14.2.2](#) may also be used for the initialization.

14.3.3.1.2 Observer

The DFD at the k th iteration is observed as $f_n(\bar{x}) - f_{n-1}(\bar{x} - \bar{u}^k)$, where f_n and f_{n-1} denote two consecutive digital images, $\bar{x} = (x, y)$ denotes the spatial coordinates of the pixel under consideration, and $\bar{u}^k = (u^k, v^k)$ denotes the optical flow of this pixel estimated at the k th iteration. (Note that the vector representation of the spatial coordinates in image planes is used quite often in the literature, owing to its brevity in notation.) Demanding fractional pixel accuracy usually requires interpolation. In Pan et al.'s work, the bilinear interpolation is adopted. The bilinearly interpolated image is denoted by \hat{f}_{n-1} .

14.3.3.1.3 Correlation

Once the bilinearly interpolated image is available, a correlation measure needs to be selected to search for the best match of a given pixel in $f_n(\bar{x})$ in a search area in the

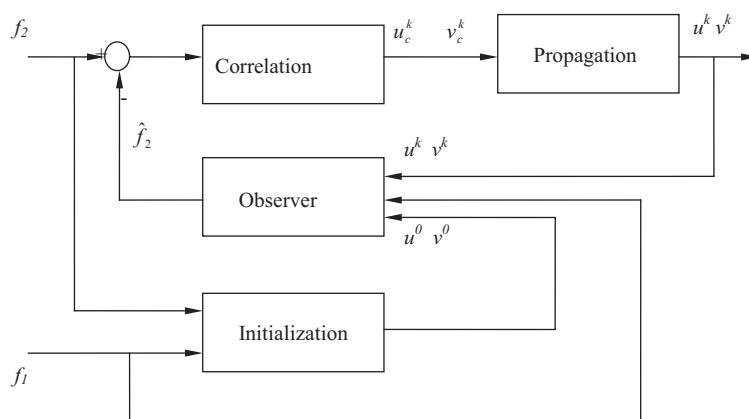


FIGURE 14.10

Block diagram of correlation feedback technique.

interpolated image. In their work, the SSD is used. For each pixel in f_n , a correlation window W_c of size $(2l + 1) \times (2l + 1)$ is formed, centered on the pixel.

The search window in the proposed approach is quite different from that used in the correlation-based approach, say, in Singh (1992). Let u be a quantity chosen from the following five quantities:

$$u \in \left\{ u^k - \frac{1}{2}u^k, u^k - \frac{1}{4}u^k, u^k, u^k + \frac{1}{4}u^k, u^k + \frac{1}{2}u^k \right\} \quad (14.31)$$

Let v be a quantity chosen from the following five quantities:

$$v \in \left\{ v^k - \frac{1}{2}v^k, v^k - \frac{1}{4}v^k, v^k, v^k + \frac{1}{4}v^k, v^k + \frac{1}{2}v^k \right\} \quad (14.32)$$

Hence, there are 25 (i.e., 5×5) possible combinations for (u, v) . (It is noted that the restriction of the non-zero initial flow field mentioned above in part A comes from here). Note that other choices of variations around (u^k, v^k) are possible. Each of them corresponds to a pixel, $(x-u, y-v)$, in the bilinearly interpolated image plane. A correlation window is formed and centered in this pixel. The 25 samples of error distribution around (u^k, v^k) can be computed by using the SSD. That is,

$$E(u, v) = \sum_{s=-l}^l \sum_{t=-l}^l (f_n(x+s, y+t) - \hat{f}_{n-1}(x-u+s, y-v+t))^2 \quad (14.33)$$

The 25 samples of response distribution can be computed as follows:

$$R_c(u, v) = e^{-\beta E(u, v)} \quad (14.34)$$

where β is chosen so as to make the maximum R_c among the 25 samples of response distribution be a number close to unity. The choice of an exponential function for converting the error distribution into the response distribution is based primarily on the following consideration: the exponential function is well behaved when the error approaches zero and all the response distribution values are positive. The choice of β mentioned above is motivated by the following observation: in this way, the R_c values, which are the weights used in Equation 14.35, will be more effective. That is, the computation in Equation 14.35 will be more sensitive to the variation of the error distribution defined in Equation 14.33.

The optical-flow vector derived at this correlation stage is then calculated as follows, according to the weighted-least-squares estimation (Singh 1992).

$$u^k(x, y) = \frac{\sum_u \sum_v R_c(u, v)u}{\sum_u \sum_v R_c(u, v)}, \quad v^k(x, y) = \frac{\sum_u \sum_v R_c(u, v)v}{\sum_u \sum_v R_c(u, v)} \quad (14.35)$$

14.3.3.1.4 Propagation

Except in the vicinity of motion boundaries, the motion vectors associated with neighboring pixels are expected to be similar. Therefore, this constraint can be used to regularize the motion field. That is,

$$u^{k+1}(x, y) = \sum_{i=-w}^w \sum_{j=-w}^w w_1(i, j) u_c^k(x+i, y+j), v^{k+1}(x, y) = \sum_{i=-w}^w \sum_{j=-w}^w w_1(i, j) v_c^k(x+i, y+j) \quad (14.36)$$

where $w_1(i, j)$ is a weighting function. The Gaussian mask shown in Figure 14.9 is chosen as the weighting function $w_1(i, j)$ used in our experiments. By using this mask, the velocity of various pixels in a pixel's neighborhood will be weighted according to their distance from the pixel: the larger the distance the smaller the weight. The mask smooths the optical-flow field as well.

14.3.3.1.5 Convergence

Under the assumption of the symmetric response distribution with a single maximum value assumed by the ground-truth optical flow, the convergence of the correlation-feedback technique is justified in Pan et al. (1995).

14.3.3.2 Implementation and Experiments

14.3.3.2.1 Implementation

In order to make the algorithm more robust against noise, three consecutive images in an image sequence, denoted by f_1 , f_2 , and f_3 , respectively, are used to implement their algorithm instead of the two images in the above principle discussion. This implementation was proposed in Singh (1992). Assume the time interval between f_1 and f_2 is the same as that between f_2 and f_3 . Also assume the apparent 2-D motion is uniform during these two intervals along the motion trajectories. From images f_1 and f_2 , (u^o, v^o) can be computed. From (u^k, v^k) , the optical flow estimated during the k th iteration, and f_1 and f_2 , the response distribution, $R_c^+(u^k, v^k)$, can be calculated as

$$R_c^+(u^k, v^k) = \exp \left\{ -\beta \sum_{s=-l}^l \sum_{t=-l}^l [f_2(x+s, y+t) - \hat{f}_1(x-u^k+s, y-v^k+t)]^2 \right\} \quad (14.37)$$

Similarly, from images f_3 and f_2 , $(-u^k, -v^k)$ can be calculated. Then $R_c^-(-u^k, -v^k)$ can be calculated as

$$R_c^-(-u^k, -v^k) = \exp \left\{ -\beta \sum_{s=-l}^l \sum_{t=-l}^l [f_2(x+s, y+t) - \hat{f}_3(x+u^k+s, y+v^k+t)]^2 \right\} \quad (14.38)$$

The response distribution $R_c(u^k, v^k)$ can then be determined as the sum of $R_c^+(u^k, v^k)$ and $R_c^-(-u^k, -v^k)$. The size of the correlation window and the weighting function is chosen to be 3×3 , i.e., $l = 1$, $w = 1$. In each search window, β is chosen so as to make the larger one among R_c^+ and R_c^- a number close to unity. In the observer stage, the bilinear interpolation is used, which is shown to be faster and better than the B-spline in Pan et al.'s many experiments.

14.3.3.2.2 Experiment I

[Figure 14.11](#) shows the three successive image frames f_1, f_2 and f_3 about a square post. They were taken by a CCD video camera and a DATACUBE real-time image-processing system supported by a Sun workstation. The square post is moving horizontally, perpendicular to the optical axis of the camera, in a uniform speed of 2.747 pixels per frame. To remove various noises to a certain extent and to speed up processing, these three 256×256 images are low-pass filtered and then subsampled prior to optical-flow estimation. That is, the intensities of every 16 pixels in a block of 4×4 are averaged and the average value is assigned to represent this block. Note that the choice of other low-pass filters is also possible. In this way, these three images are compressed into three 64×64 images. The “ground-truth” 2-D motion velocity vector is hence known as $u^g = -0.6868; v^g = 0$.

In order to compare the performance of the correlation-feedback approach with that of the gradient-based and correlation-based approaches, Horn and Schunck’s algorithm is chosen to represent the gradient-based approach and Singh’s framework to represent the correlation-based approach. [Table 14.1](#) shows the results of the comparison. There, l, w , and N indicate the sizes of the correlation window, weighting function, and search window, respectively. The program that implements Singh’s algorithm is provided by the authors of Barron et al. (1994). In the correlation-feedback algorithm, 10 iterations of Horn and Schunck’s algorithm with $\alpha = 5$ are used in the initialization. (Recall that the α is a regularization parameter used in Horn and Schunck [1981]). Only the central 40×40 flow vector array is used to compute u_{error} , which is the root mean square (RMS) error in the vector magnitudes between the ground-truth and estimated optical-flow vectors. It is noted that the relative error in Experiment I is greater than 10%. This is because the denominator in the formula calculating the RMS error is too small due to the static background and, hence, many zero ground-truth 2-D motion velocity vectors in this experiment. Relatively speaking, the correlation-feedback algorithm performs best in determining optical flow for a texture post in translation. The correct optical-flow field and those calculated by using three different algorithms are shown in [Figure 14.12](#).

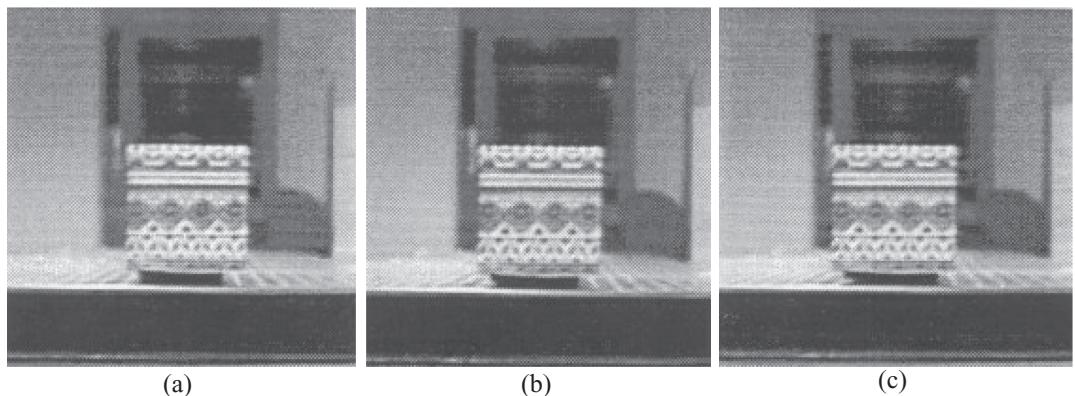
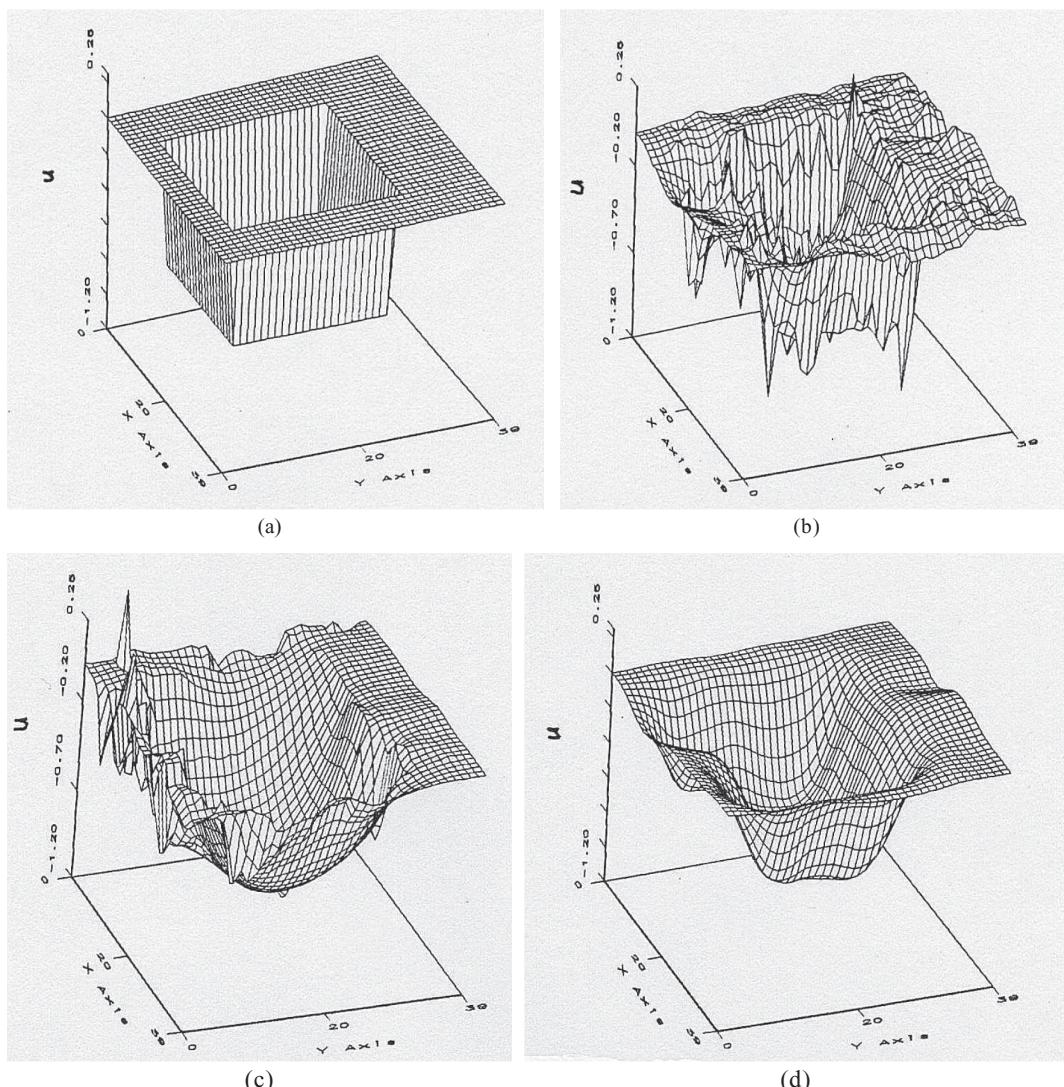


FIGURE 14.11
(a) Texture square, (b) Texture square, and (c) Texture square.

TABLE 14.1

Comparison in Experiment I

| Techniques | Gradient-Based Approach | Correlation-Based Approach | Correlation-Feedback Approach |
|--------------------|-------------------------------------|---|---|
| Conditions | Iteration no. = 128 $\alpha = 5$ | Iteration no. = 25 $l = 2, w = 2, N = 4$ | Iteration no. = 10 $l = 1, w = 1, N = 5$ |
| u_{error} | 56.37% | 80.97% | 44.56% |

**FIGURE 14.12**

(a) Correct optical-flow field, (b) Optical-flow field calculated by the gradient-based approach, (c) Optical-flow field calculated by the correlation-based approach, and (d) Optical-flow field calculated by the correlation-feedback approach.

14.3.3.2.3 Experiment II

The images in [Figure 14.13](#) were obtained by rotating a CCD camera with respect to the center of a ball. The rotating velocity is 2.5° per frame. Similarly, three 256×256 images are compressed into three 64×64 images by using the averaging and sub-sampling discussed above. Only the central 40×40 optical vector arrays are used to compute u_{error} . [Table 14.2](#) reports the results for this experiment. There, u_{error} , l , w , and N have the same meaning as that discussed in Experiment I. It is obvious that our correlation-feedback algorithm performs best in determining optical flow for this rotating ball case.

14.3.3.2.4 Experiment III

In order to compare the correlation-feedback algorithm with other existing techniques in a more objective, quantitative manner, Pan et al. cite some results reported in Barron et al. (1994), which were obtained by applying some typical optical-flow techniques to some image sequences chosen with deliberation. In the meantime, they report the results obtained by applying their feedback technique to the identical image sequences with the same accuracy measurement as used in Barron et al. (1994).

Three image sequences used in Barron et al. (1994) were utilized here. They are named “Translating Tree,” “Diverging Tree,” and “Yosemite.” The first two simulate translational camera motion with respect to a textured planar surface (see [Figure 14.14](#)), and are sometimes referred to as “Tree 2-D” sequence. Therefore, there are no occlusions and no motion discontinuities in these two sequences. In the “Translating Tree” sequence, the camera moves normally to its line of sight, with velocities between 1.73 and 2.26 pixels/frame parallel to the x-axis in the image plane. In the “Diverging Tree” sequence, the camera moves along its line of sight. The focus of expansion is at the center of the image. The speeds

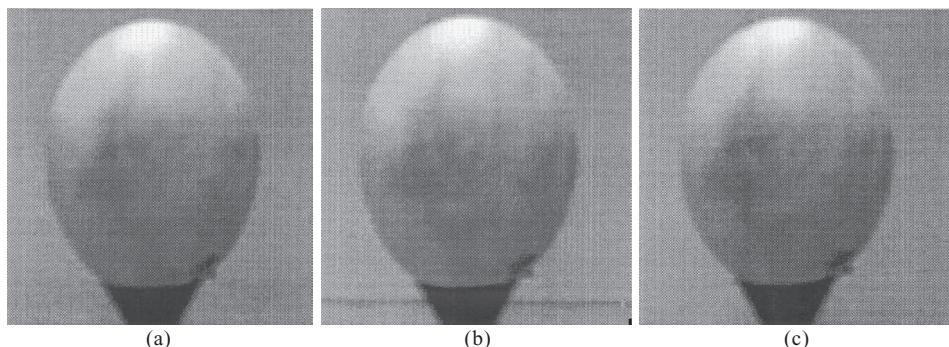


FIGURE 14.13

(a) Ball, (b) Ball, and (c) Ball.

TABLE 14.2

Comparison in Experiment II

| Techniques | Gradient-Based Approach | Correlation-Based Approach | Correlation-Feedback Approach |
|--------------------|--|--|--|
| Conditions | <i>Iteration no. = 128</i> $\alpha = 5$ | <i>Iteration no. = 25</i> $l = 2, w = 2, N = 4$ | <i>Iteration no. = 10</i> $l = 1, w = 1, N = 5$ |
| u_{error} | 65.67% | 55.29% | 49.80% |

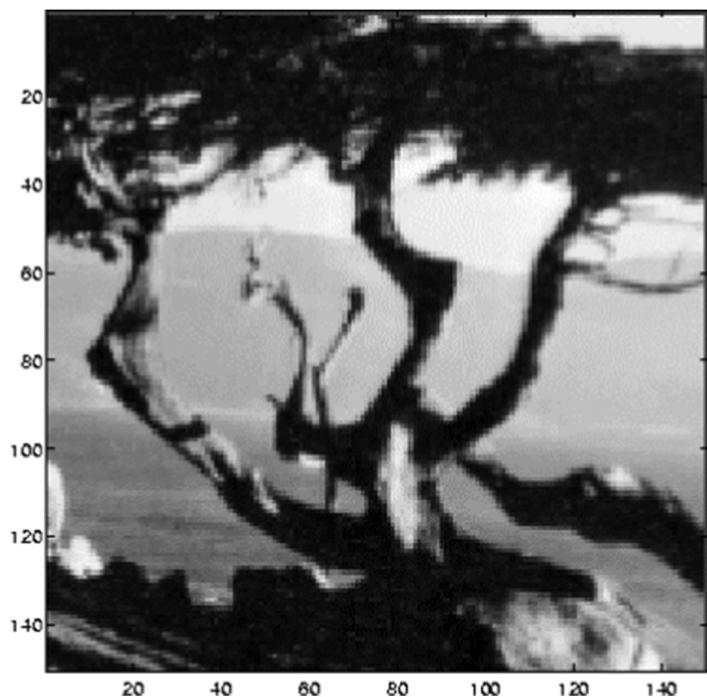


FIGURE 14.14
A frame of the “Tree 2-D” sequence.

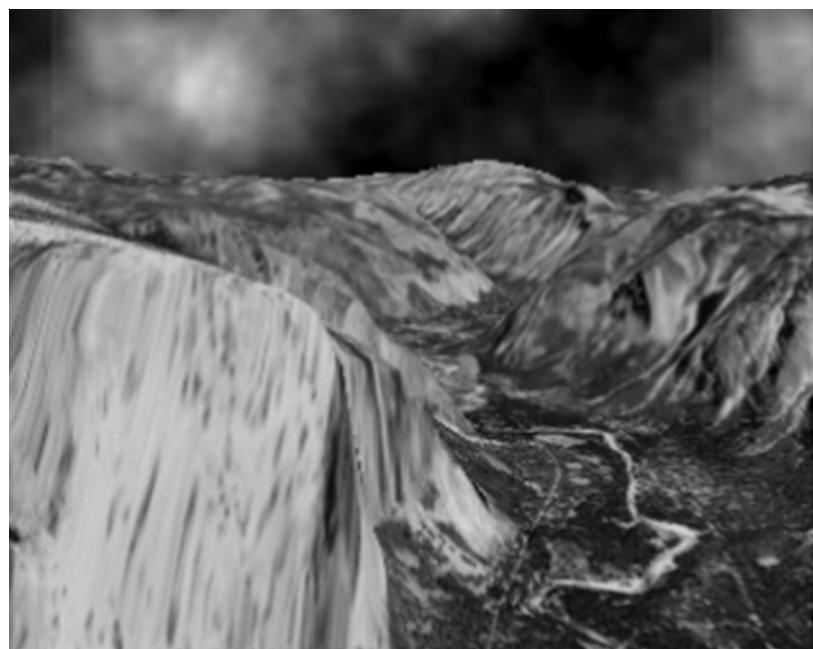


FIGURE 14.15
A frame of the “Yosemite” sequence.

vary from 1.29 pixels/frame on left side to 1.86 pixels/frame on the right. The “Yosemite” sequence is a more complex test case (see [Figure 14.15](#)). The motion in the upper right is mainly divergent. The clouds translate to the right with a speed of 1 pixel/frame, while velocities in the lower left are about 4 pixels/frame. This sequence is challenging because of the range of velocities and the occluding edges between the mountains and at the horizon. There is severe aliasing in the lower portion of the images, causing most methods to produce poorer velocity measurements. Note that this synthetic sequence is for quantitative study purposes since its ground-truth flow field is known and is, otherwise, far less complex than many real-world outdoor sequences processed in the literature.

The angular measure of the error used in Barron et al. (1994) is utilized here, as well. Let image velocity $\bar{u} = (u, v)$ be represented as 3-D direction vectors,

$$\bar{V} \equiv \frac{1}{\sqrt{u^2 + v^2 + 1}} (u, v, 1) \quad (14.39)$$

The angular error between the correct image velocity \bar{V} and an estimate \bar{V}_e is $\psi_e = \text{acos}(\bar{V}_c \cdot \bar{V}_e)$. It is obvious that the smaller the angular error ψ_e , the more accurate the estimation of the optical-flow field will be. Despite the fact that the confidence measurement can be used in the correlation-feedback algorithm as well, Pan et al. did not consider the usage of the confidence measurement in their work. Therefore, only the results with 100% density in [Tables 4.6, 4.7](#), and [4.10](#) in Barron et al., (1994) were used in [Tables 14.3](#) through [14.5](#), respectively.

TABLE 14.3

Summary of the “Translating Tree” 2-D Velocity Results

| Techniques | Average Error | Standard Deviation | Density |
|--------------------------------------|---------------|--------------------|---------|
| Horn and Schunck (original) | 38.72 | 27.67 | 100% |
| Horn and Schunck (modified) | 2.02 | 2.27 | 100% |
| Uras et al. (unthresholded) | 0.62 | 0.52 | 100% |
| Nagel | 2.44 | 3.06 | 100% |
| Anandan | 4.54 | 3.10 | 100% |
| Singh (step 1, $l = 2, w = 2$) | 1.64 | 2.44 | 100% |
| Singh (step 2, $l = 2, w = 2$) | 1.25 | 3.29 | 100% |
| Pan, Shi, and Shu ($l = 1, w = 1$) | 1.07 | 0.48 | 100% |

TABLE 14.4

Summary of the “Diverging Tree” 2-D Velocity Results

| Techniques | Average Error | Standard Deviation | Density |
|--------------------------------------|---------------|--------------------|---------|
| Horn and Schunck (original) | 12.02 | 11.72 | 100% |
| Horn and Schunck (modified) | 2.55 | 3.67 | 100% |
| Uras et al. (unthresholded) | 4.64 | 3.48 | 100% |
| Nagel | 2.94 | 3.23 | 100% |
| Anandan (frames 19 and 21) | 7.64 | 4.96 | 100% |
| Singh (step 1, $l = 2, w = 2$) | 17.66 | 14.25 | 100% |
| Singh (step 2, $l = 2, w = 2$) | 8.60 | 5.60 | 100% |
| Pan, Shi, and Shu ($l = 1, w = 1$) | 5.12 | 2.16 | 100% |

TABLE 14.5

Summary of the “Yosemite” 2-D Velocity Results

| Techniques | Average Error | Standard Deviation | Density |
|--------------------------------------|---------------|--------------------|---------|
| Horn and Schunck (original) | 32.43 | 30.28 | 100% |
| Horn and Schunck (modified) | 11.26 | 16.41 | 100% |
| Uras et al. (unthresholded) | 10.44 | 15.00 | 100% |
| Nagel | 11.71 | 10.59 | 100% |
| Anandan (frames 19 and 21) | 15.84 | 13.46 | 100% |
| Singh (step 1, $l = 2, w = 2$) | 18.24 | 17.02 | 100% |
| Singh (step 2, $l = 2, w = 2$) | 13.16 | 12.07 | 100% |
| Pan, Shi, and Shu ($l = 1, w = 1$) | 7.93 | 6.72 | 100% |

Prior to computation of the optical-flow field, the “Yosemite” and “Tree 2-D” test sequences were compressed by a factor of 16 and 4, respectively, using the averaging and sub-sampling method discussed earlier.

As mentioned in Barron et al. (1994) the optical-flow field for the “Yosemite” sequence is complex, and Table 14.5 indicates that the correlation-feedback algorithm evidently performs best. In Black and Anandan (1996), a robust method was developed and applied to a cloudless Yosemite sequence. It is noted that the performance of flow determination algorithms will be improved if the sky is removed from consideration (Barron et al. 1994, Black and Anandan 1996). Still, it is clear that the algorithm in Black and Anandan (1996) achieved very good performance in terms of accuracy. In order to make a comparison with their algorithm, the correlation-feedback algorithm was applied to the same cloudless Yosemite sequence. The results were reported in Table 14.6, from which it can be observed that the results obtained by Pan et al. are slightly better. Tables 14.3 and 14.4 indicate that the feedback technique also performs very well in translating and diverging texture post cases.

14.3.3.2.5 Experiment IV

Here, the correlation-feedback algorithm is applied to a real sequence named *Hamburg Taxi*, which is used as a testing sequence in Barron et al. (1994). There are four moving objects in the scene: a moving pedestrian in the upper left portion, a turning car in the middle, a car moving towards right at the left side, and a car moving towards the left at the right side. A frame of the sequence and the needle diagram of flow vectors estimated by using 10 iterations of the correlation-feedback algorithm (with 10 iterations of Horn and Schunck’s algorithm for initialization) are shown in Figures 14.16 and 14.17, respectively. The needle diagram is printed in the same fashion as those shown in Barron et al. (1994). It is noted that the moving pedestrian in the upper left portion cannot be shown because of the scale used in the needle diagram. The other three moving vehicles in the sequence are shown very clearly. The noise level is low. Compared with those diagrams reported in Barron et al. (1994), the correlation-feedback algorithm achieves very good results.

TABLE 14.6

Summary of the Cloudless “Yosemite” 2-D Velocity Results

| Techniques | Average Error | Standard Deviation | Density |
|--------------------------------------|---------------|--------------------|---------|
| Robust formulation | 4.46 | 4.21 | 100% |
| Pan, Shi, and Shu ($l = 1, w = 1$) | 3.79 | 3.44 | 100% |



FIGURE 14.16
Hamburg taxi.

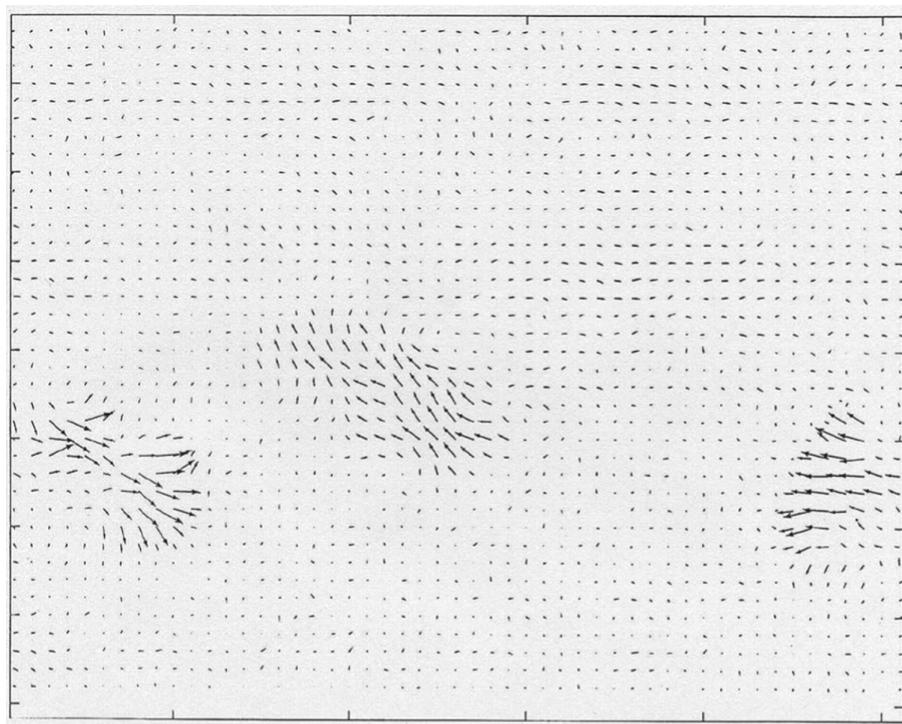
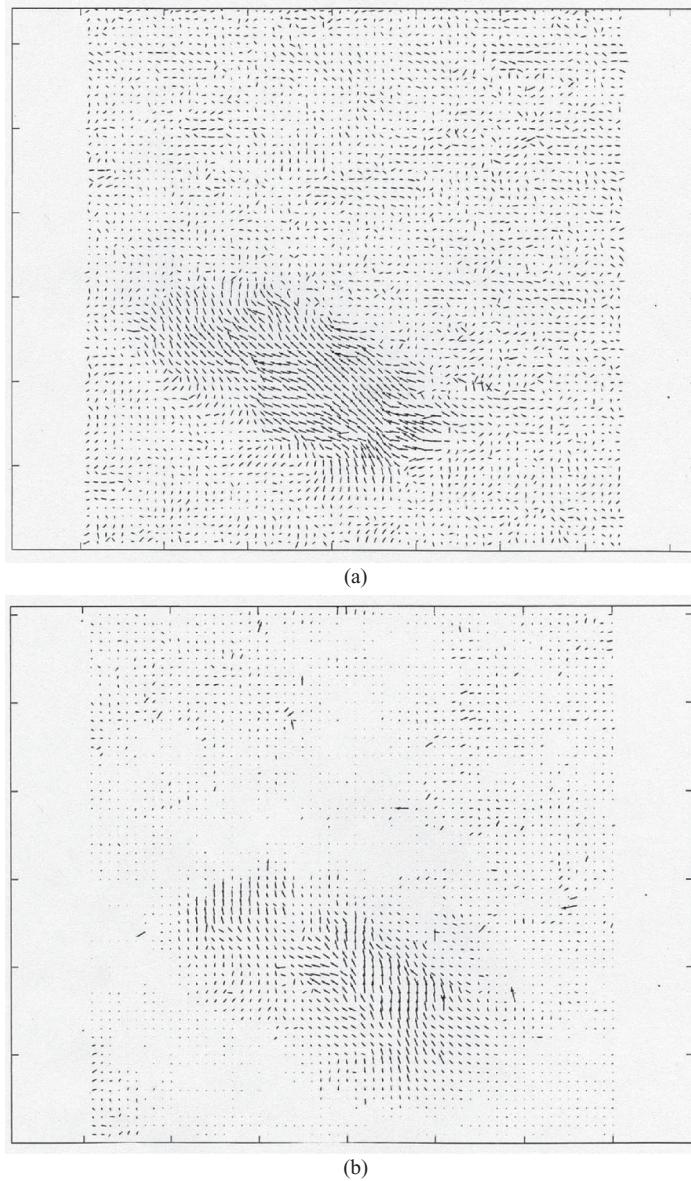
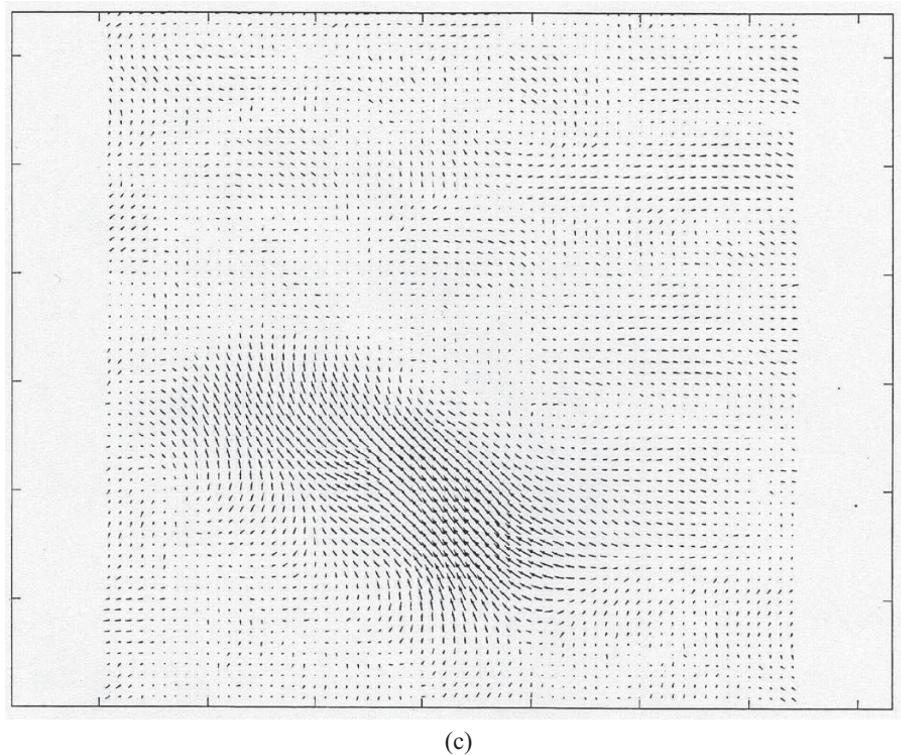


FIGURE 14.17
Needle diagram of flow field of Hamburg taxi sequence obtained by using the correlation-feedback algorithm.

For a comparison on a local basis, the portion of the needle diagram associated with the area surrounding the turning car (a sample of the velocity fields), obtained by 50 iterations of the correlation-feedback algorithm with five iterations of Horn and Schunck's algorithm as initialization, is provided in [Figure 14.18c](#). Its counterparts obtained by applying Horn and Schunck's (50 iterations) and Singh's (50 iterations) algorithms are displayed in [Figure 14.18a](#) and [b](#), respectively. It is observed that the correlation-feedback algorithm achieves the best results among the three algorithms.

**FIGURE 14.18**

A portion of the needle diagram obtained by using (a) Horn and Schunk's algorithm, (b) Singh's algorithm, and
(Continued)

**FIGURE 14.18 (Continued)**

A portion of the needle diagram obtained by using (c) the correlation-feedback algorithm.

14.3.3.3 Discussion and Conclusion

Though it uses a revised version of a correlation-based algorithm (Singh 1992), the correlation-feedback technique is quite different from the correlation-based algorithm (Singh 1992) in the following four aspects. First, different optimization criteria: the algorithm does not use the iterative minimization procedure used in Singh (1992). Instead, some variations of the estimated optical-flow vectors are generated and fed back. The associated bilinearly interpolated DFD for each variation is calculated and utilized. In essence, the feedback approach utilizes two given images repeatedly, while the Singh method uses two given images only once (u_c and v_c derived from the two given images are only calculated once). The best local matching between the displaced image, generated via feedback of the estimated optical flow, and the given image is actually used as the ultimate criterion for improving optical-flow accuracy in the iterative process. Second, the search window in the algorithm is an adaptive “rubber” window, having a variable size depending on (u^k, v^k) . In the correlation-based approaches (Singh 1992), the search window has a fixed size. Third, the algorithm uses a bilinear interpolation technique in the observation stage and provides the correlation stage with a virtually continuous image field for more accurate motion vector computation, while that in Singh (1992) does not. Fourth, different performances are achieved when image intensity is a linear function of image coordinates. In fact, in the vicinity of a pixel, the intensity can usually be considered as such a linear function. Except if the optical-flow vectors happen to have only an integer multiple of pixels as their components, an analysis in Pan (1994) shows that the correlation-based approach

(Singh 1992) will not converge to the apparent 2-D motion vectors and will easily have error much greater than 10%. In Pan (1994) it is also shown that the linear intensity function guarantees the assumption of the symmetric response distribution with a single maximum value assumed by the ground-truth optical flow. As discussed in [Section 14.3.3.1](#), under this assumption the convergence of the correlation-feedback technique is justified.

Numerous experiments have demonstrated the correlation-feedback algorithm's convergence and accuracy, and usually it is more accurate than some standard gradient- and correlation-based approaches. In the complicated optical-flow cases, specifically in the case of the "Yosemite" image sequence (regarded as the most challenging quantitative test image sequence in Barron et al. [1994]), it performs better than all other techniques.

14.4 Multiple Attributes for Conservation Information

As stated at the beginning of this chapter, there are many algorithms in optical-flow computation reported in the literature. Many more new algorithms continue to be developed. In [Sections 14.2](#) and [14.3](#), we introduced some typical algorithms using gradient- and correlation-based approaches. We will not explore various algorithms any further here. It is hoped that the fundamental concepts and algorithms introduced above have provided a solid base for readers to study more advanced techniques.

We would like to discuss optical flow from another point of view, however: Multiple image attributes versus a single image attribute. All of the methods we have discussed so far use only one kind of image attributes as conservation information in flow determination. Most methods use intensity. Singh's method uses the Laplacian of intensity, which is calculated by using the difference of the Gaussian operation (Burt 1984). It was reported by Weng, Ahuja, and Huang that using a single attribute as conservation information may result in ambiguity in matching two perspective views, while multiple attributes, which are motion insensitive, may reduce ambiguity remarkably, resulting in better matching (Weng et al. 1992). An example is shown in [Figure 14.19](#) to illustrate this argument. In this section, Weng et al.'s method is discussed first. Then we introduce Xia and Shi's method, which uses multiple attributes in a framework based on weighted-least-square estimation and feedback techniques.

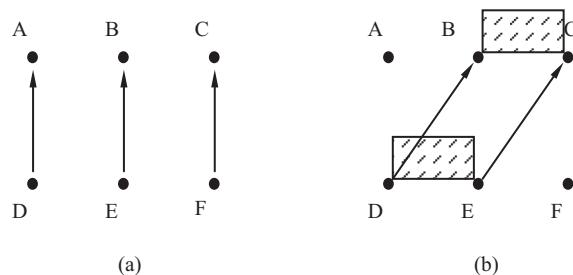


FIGURE 14.19

Multiple attributes vs. single attribute. (a) With intensity information only, points D, E, and F tend to match to points A, B, and C, respectively and (b) With intensity, edge and corner information points D and E tend to match points B and C, respectively.

14.4.1 Weng, Ahuja, and Huang's Method

Weng, Ahuja, and Huang proposed a quite different approach to image-point matching (Weng et al. 1992). Note that the image matching amounts to flow-field computation since it calculates a displacement field for each point in image planes, which is essentially a flow field if the time interval between two image frames is known.

Based on an analysis indicating that using image intensity as a single attribute is not enough in accurate image matching, Weng, Ahuja, and Huang utilize multiple attributes associated with images in estimation of the dense displacement field. These image attributes are motion insensitive, i.e., they generally sustain only small change under motion assumed to be locally rigid. The image attributes used are image intensity, edgeness, and cornerness. For each image attribute, the algorithm forms a residual function, reflecting the inaccuracy of the estimated matching. The matching is then determined via an iterative procedure to minimize the weighted sum of these residual functions. In handling neighborhood information, a more advanced smoothness constraint is used to take care of moving discontinuities. The method considers uniform regions and the occlusion issue as well.

In addition to using multiple image attributes, the method is pointwise processing. There is no need for calculation of correlation within two correlation windows, which saves computation dramatically. However, the method also has some drawbacks. First, the edgeness and cornerness involve calculation of the spatial gradient, which is noise sensitive. Second, in solving for minimization, the method resorts to numerical differentiation again: the estimated displacement vectors are updated based on the partial derivatives of the noisy attribute images. In a word, the computational framework heavily relies on numerical differentiation, which is considered to be impractical for accurate computation (Barron et al. 1994).

On the other hand, the Pan, Shi, and Shu method, discussed in [Section 14.3.3](#) in the category of correlation-based approaches, seems to have some complementary features. It is correlation-based. It uses intensity as a single attribute. In these two aspects, the Pan et al.'s method is inferior to the method by Weng, Ahuja, and Huang. The feedback technique and the weighted least square computation framework used in the Pan et al. method are superior, however, compared with the method by Weng et al. Motivated by the above observations, an efficient, multiattribute feedback method was developed by Xia and Shi (Xia and Shi 1995, Xia 1996) and is discussed in the next subsection. It is expected that more insight of the Weng, Ahuja, and Huang method will become clear in the discussion as well.

14.4.2 Xia and Shi's Method

This method uses multiple attributes that are motion insensitive. The following five attributes are used: image intensity, horizontal edgeness, vertical edgeness, contrast, and entropy. The first three are used in Weng et al. (1992) as well, and can be considered as structural attributes, while the last two, which are not used in Weng et al. (1992), can be considered as textural attributes according to Haralick (1979).

Instead of the computational framework presented in Weng et al. (1992), which, as discussed above, may be not practical for accurate computation, the method uses the computational framework of Pan (1994), Pan et al. (1998). That is, the weighted-least-squared estimation technique used in Singh (1992) and the feedback technique used in Pan (1994), Pan et al. (1998) are utilized here. Unlike in Weng et al. (1992), subpixel accuracy is considered and a confidence measure is generated in the method.

The Xia and Shi method is also different from those algorithms presented in Singh (1992), Pan et al. (1995, 1998). First, there is no correlation in the method, while both (Singh 1992, Pan et al. 1995, 1998) are correlation-based. Specifically, the method is a point-wise processing. Second, the method uses multiple attributes, while both (Singh 1992, Pan et al. 1995, 1998) use image intensity as a single attribute.

In summary, the Xia and Shi method to compute optical flow is motivated by several existing algorithms mentioned above. It does, however, differ from each of them significantly.

14.4.2.1 Multiple Image Attributes

As mentioned before, there are five image attributes in the Xia and Shi method. They are defined below.

14.4.2.1.1 Image Intensity

The intensity at a pixel (x, y) in an image $f_n(x, y)$, denoted by $A_i(x, y)$, i.e., $A_i(x, y) = f_n(x, y)$.

14.4.2.1.2 Horizontal Edgeness

The horizontal edgeness at a pixel (x, y) , denoted by $A_h(x, y)$, is defined as

$$A_h(x, y) = \frac{\partial f(x, y)}{\partial y} \quad (14.40)$$

i.e., the partial derivative of $f(x, y)$ with respect to y , the second component of the gradient of intensity function at the pixel.

14.4.2.1.3 Vertical Edgeness

The vertical edgeness at a pixel (x, y) , denoted by $A_v(x, y)$, is defined as

$$A_v(x, y) = \frac{\partial f(x, y)}{\partial x} \quad (14.41)$$

i.e., the first component of the gradient of intensity function at the pixel. Note that the partial derivatives in Equations 14.40 and 14.41 are computed by applying a Sobel operator (Gonzalez and Woods 1992) in a 3×3 neighborhood of the pixel.

14.4.2.1.4 Contrast

The local contrast at a pixel (x, y) , denoted by $A_c(x, y)$, is defined as

$$A_c(x, y) = \sum_{i,j \in S} (i - j)^2 C_{i,j} \quad (14.42)$$

where S is a set of all the distinct gray levels within a 3×3 window centered at pixel (x, y) . $C_{i,j}$ specifies a relative frequency with which two neighboring pixels separated horizontally by a distance 1 occur in the 3×3 window, one with gray level i and the other with gray level j .

14.4.2.1.5 Entropy

The local entropy at a point (x, y) , denoted by $A_e(x, y)$, is given by

$$A_e(x, y) = - \sum_{i \in S} p_i \log p_i \quad (14.43)$$

where S was defined above, and p_i is the probability of occurrence of the gray level i in the 3×3 window.

Since the intensity is assumed to be invariant to motion, so are the horizontal edgeness, vertical edgeness, contrast, and entropy.

As mentioned above, the intensity and edgeness are used as attributes in Weng et al.'s algorithm as well. Compared with the negative and positive cornerness used in Weng et al.'s algorithm, the local contrast and entropy need no differentiation and therefore are less sensitive to various noises in original images. In addition, these two attributes are inexpensive in terms of computation. They reflect the textural information about the local neighborhood of the pixel for which flow vector is to be estimated.

14.4.2.2 Conservation Stage

In the Xia et al. algorithm, this stage is similar to that in the Pan et al. algorithm. That is, for a flow vector estimated at the k th iteration, denoted by (u^k, v^k) , we find its 25 variations, (u, v) , according to

$$\begin{aligned} u &\in \left\{ u^k - \frac{u^k}{2}, u^k - \frac{u^k}{4}, u^k, u^k + \frac{u^k}{4}, u^k + \frac{u^k}{2} \right\} \\ v &\in \left\{ v^k - \frac{v^k}{2}, v^k - \frac{v^k}{4}, v^k, v^k + \frac{v^k}{4}, v^k + \frac{v^k}{2} \right\} \end{aligned} \quad (14.44)$$

For each of these 25 variations, the matching error is computed as

$$E(u, v) = r_{A_i}^2(x, y, u, v) + r_{A_h}^2(x, y, u, v) + r_{A_v}^2(x, y, u, v) + r_{A_c}^2(x, y, u, v) + r_{A_e}^2(x, y, u, v) \quad (14.45)$$

where r_{A_i} , r_{A_h} , r_{A_v} , r_{A_c} , r_{A_e} denote the residual function with respect to the five attributes, respectively.

The residual function of intensity is defined as

$$r_{A_i}(x, y, u, v) = A_{i_n}(x, y) - A_{i_{n-1}}(x-u, y-v) = f_n(x, y) - f_{n-1}(x-u, y-v) \quad (14.46)$$

where $f_n(x, y)$ and $f_{n-1}(x, y)$ are defined as before, i.e., the intensity function at t_n and t_{n-1} , respectively; A_{i_n} , $A_{i_{n-1}}$ denote the intensity attributes on f_n and f_{n-1} , respectively.

It is observed that the residual error of intensity is essentially the DFD discussed in [Chapter 12](#). The rest of the residual functions are defined similarly. When subpixel accuracy is required, spatial interpolation in the attribute images generally is necessary. Thus, the flow vector estimation is now converted to a minimization problem. That is, find u and v at pixel (x, y) such that the matching error defined in Equation 14.45 is minimized. The weighted least square method (Singh 1992, Pan et al. 1998) is then used. That is,

$$R(u, v) = e^{-\beta E(u, v)} \quad (14.47)$$

$$u_c^{k+1} = \frac{\sum_u \sum_v R(u, v) u}{\sum_u \sum_v R(u, v)}, \quad v_c^{k+1} = \frac{\sum_u \sum_v R(u, v) v}{\sum_u \sum_v R(u, v)} \quad (14.48)$$

Since the weighted least square method has been discussed in detail in [Sections 14.3.2](#) and [14.3.3](#), we will not go into more detail here.

14.4.2.3 Propagation Stage

Similar to what was proposed in the Pan et al. algorithm, in this stage Xia et al. form a window W of size $(2w + 1) \times (2w + 1)$ centered at the pixel (x, y) in the image $f_n(x, y)$. The flow estimate at the pixel (x, y) in this stage, denoted by (u^{k+1}, v^{k+1}) , is calculated as a weighted sum of the flow vectors of the pixels within the window W .

$$\begin{aligned} u^{k+1} &= \sum_{s=-w}^w \sum_{t=-w}^w w_1[f_n(x, y), f_n(x+s, y+t)] \cdot u_c^{k+1}(x+s, y+t) \\ v^{k+1} &= \sum_{s=-w}^w \sum_{t=-w}^w w_1[f_n(x, y), f_n(x+s, y+t)] \cdot v_c^{k+1}(x+s, y+t) \end{aligned} \quad (14.49)$$

where $w_1[\cdot, \cdot]$ is a weight function. For each point in the window W , a weight is assigned according to the weight function. Let $(x+s, y+t)$ denote a pixel within the window W , then the weight of the pixel $(x+s, y+t)$ is given by

$$w_1[f_n(x, y), f_n(x+s, y+t)] = \frac{c}{\varepsilon + |f_n(x, y) - f_n(x+s, y+t)|} \quad (14.50)$$

where ε is a small positive number to prevent the denominator from vanishing, c is a normalization constant that makes the summation of all the weights in the W equal 1.

From the above equation, we see that the weight is determined based on the intensity difference between the pixel under consideration and its neighboring pixel. The larger the difference in the intensity, the more likely the two points belong to different regions. Therefore, the weight will be small in this case. On the other hand, the flow vector in the same region will be similar since the corresponding weight is large. Thus, the weighting function implicitly takes flow discontinuity into account and is more advanced than that in Singh (1992), Pan (1994), Pan et al. (1998).

14.4.2.4 Outline of Algorithm

The following summarizes the procedures of the algorithm.

1. Perform a low-pass prefiltering on two input images to remove various noises.
2. Generate attribute images: intensity, horizontal edgeness, vertical edgeness, local contrast, and local entropy. Those attributes are computed at each grid point of both images.

3. Set the initial flow vectors to zero. Set the maximum iteration number and/or estimation accuracy.
4. For each pixel under consideration, generate flow variations according to Equation 14.44. Compute matching error for each flow variation according to Equation 14.45 and transform them to the corresponding response distribution R using Equation 14.47. Compute the flow estimation u^c, v^c using Equation 14.48.
5. Form a $(2w + 1) \times (2w + 1)$ neighborhood window W centered at the pixel. Compute the weight for each pixel within the window W using Equation 14.50. Update the flow vector using Equation 14.49.
6. Decrease the preset iteration number. If the iteration number is zero, the algorithm returns with the resultant optical-flow field. Otherwise, go to the next step.
7. If the change in flow vector over two successive iterations is less than the pre-defined threshold, the algorithm returns with the estimated optical-flow field. Otherwise, go to step 4.

14.4.2.5 Experimental Results

In order to compare the method with other methods existing in the literature, similar to what has been done in Pan et al. (1998) (discussed above in [Section 14.3.3](#)), the method was applied to three test sequences used in Barron et al. (1994): the “Translating Tree” sequence, the “Diverging Tree” sequence, and the “Yosemite” sequence. The same accuracy criterion is used as that in Barron et al. (1994). Only those results reported in Barron et al. (1994) with 100% density are listed in [Tables 14.7](#) through [14.9](#) for a fair and easy comparison. Weng et al.’s algorithm was implemented by Xia et al. and the results were reported in Xia and Shi (1995).

14.4.2.6 Discussion and Conclusion

The above experimental results demonstrate that the Xia and Shi method outperforms both Pan, Shi, and Shu’s method and Weng, Ahuja, and Huang’s method in terms of accuracy of optical flow determined. Computationally speaking, Xia and Shi’s method is less expensive than Pan et al.’s, since there is no correlation involved and the correlation is known to be computationally expensive.

TABLE 14.7

Summary of the “Translating Tree” 2D Velocity Results

| Techniques | Average Error | Standard Deviation | Density |
|--------------------------------------|---------------|--------------------|---------|
| Horn and Schunck (original) | 38.72 | 27.67 | 100% |
| Horn and Schunck (modified) | 2.02 | 2.27 | 100% |
| Uras et al. (unthresholded) | 0.62 | 0.52 | 100% |
| Nagel | 2.44 | 3.06 | 100% |
| Anandan | 4.54 | 3.10 | 100% |
| Singh (step 1, $n = 2, w = 2$) | 1.64 | 2.44 | 100% |
| Singh (step 2, $n = 2, w = 2$) | 1.25 | 3.29 | 100% |
| Pan, Shi, and Shu ($n = 1, w = 1$) | 1.07 | 0.48 | 100% |
| Weng, Ahuja, and Huang | 1.81 | 2.03 | 100% |
| Xia and Shi | 0.55 | 0.52 | 100% |

TABLE 14.8

Summary of the “Diverging Tree” 2D Velocity Results

| Techniques | Average Error | Standard Deviation | Density |
|--|---------------|--------------------|---------|
| Horn and Schunck (original) | 32.43 | 30.28 | 100% |
| Horn and Schunck (modified) | 11.26 | 16.41 | 100% |
| Uras et al. (unthresholded) | 10.44 | 15.00 | 100% |
| Nagel | 11.71 | 10.59 | 100% |
| Anandan | 15.84 | 13.46 | 100% |
| Singh (step 1, $n = 2, w = 2, N = 4$) | 18.24 | 17.02 | 100% |
| Singh (step 2, $n = 2, w = 2, N = 4$) | 13.16 | 12.07 | 100% |
| Pan, Shi, and Shu ($n = 1, w = 1$) | 7.93 | 6.72 | 100% |
| Weng, Ahuja, and Huang | 8.41 | 8.22 | 100% |
| Xia and Shi | 7.54 | 6.61 | 100% |

TABLE 14.9

Summary of the “Yosemite” 2D Velocity Results

| Techniques | Average Error | Standard Deviation | Density |
|--|---------------|--------------------|---------|
| Horn and Schunck (original) | 12.02 | 11.72 | 100% |
| Horn and Schunck (modified) | 2.55 | 3.67 | 100% |
| Uras et al. (unthresholded) | 4.64 | 3.48 | 100% |
| Nagel | 2.94 | 3.23 | 100% |
| Anandan (frame 19 and 21) | 7.64 | 4.96 | 100% |
| Singh (step 1, $n = 2, w = 2, N = 4$) | 17.66 | 14.25 | 100% |
| Singh (step 2, $n = 2, w = 2, N = 4$) | 8.60 | 5.60 | 100% |
| Pan, Shi, and Shu ($n = 1, w = 1$) | 5.12 | 2.16 | 100% |
| Weng, Ahuja, and Huang | 8.01 | 9.71 | 100% |
| Xia and Shi | 4.04 | 3.82 | 100% |

14.5 Summary

The optical-flow field is a dense 2-D distribution of apparent velocities of movement of intensity patterns in image planes, while the 2-D motion field can be understood as the perspective projection of 3-D motion in the scene onto image planes. They are different. Only under certain circumstances are they equal to each other. In practice, however, they are closely related in that image sequences are usually the only data we have in motion analysis. Hence, we can only deal with the optical flow in motion analysis, instead of the 2-D motion field. The aperture problem in motion analysis refers to the problem that occurs when viewing motion via an aperture. Specifically, the only motion we can observe from local measurement is the motion component orthogonal to the underlying moving contour. That is another way to manifest the ill-posed nature of optical-flow computation. In general, motion analysis from image sequences is an inverse problem, which is ill-posed. Fortunately, low-level computational vision problems are only mildly ill-posed. Hence, lowering the noise in image data leads to a possible significant reduction of errors in flow determination.

Numerous flow determination algorithms have appeared over the course of more than one decade. Most of the techniques take one of the following approaches: the gradient-based approach, the correlation-based approach, the energy-based approach, and the phase-based approach. In addition to these deterministic approaches, there is also a stochastic approach. A unification point of view of optical-flow computation is presented in [Section 14.3](#). That is, for any algorithm in optical-flow computation, there are two types of information that need to be extracted—conservation information and neighborhood information.

Several techniques are introduced for the gradient-based approach, particularly the Horn and Schunck algorithm, which is a pioneer work in flow determination. There, the brightness invariant equation is used to extract conservation information; the smoothness constraint is used to extract neighborhood information. The modified Horn and Schunck algorithm shows significant error reduction in flow determination, owing to a reduction of noise in image data, which confirms the mildly ill-posed nature of optical-flow computation.

Several techniques are discussed for the correlation-based approach. The Singh algorithm is given emphasis due to its estimation-theoretical framework. The Pan, Shi, and Shu algorithm, which applies the feedback technique to the correlation method, demonstrates an accuracy enhancement in flow estimation.

[Section 14.4](#) addresses the usage of multiple image attributes versus that of a single image attribute in the flow-determination technique. It is found that the usage of multiple motion-insensitive attributes can help reduce the ambiguity in motion analysis. The application of multiple image attributes to conservation information turns out to be promising for flow computation.

Some experimental works were presented in [Sections 14.3](#) and [14.4](#). With Barron et al.'s recent comprehensive survey of various existing optical-flow algorithms, we can have a quantitative assessment on various optical-flow techniques.

Optical flow finds application in areas such as computer vision, image interpolation, temporal filtering, and video coding. In computational vision, raising the accuracy of optical-flow estimation is important. In video coding, however, lowering the bit rate for both prediction error and motion overhead while keeping certain qualities of reconstructed frames is the ultimate goal. Properly handling the large number of velocity vectors is a key issue in this regard. It is noted that the optical-flow-based motion estimation for video compression has been applied for many years. However, the high bit overhead and computational complexity prevent it from practical usage in video coding. With the continued advance in technologies, however, we believe this problem may be resolved in the near future. In fact, an initial, successful attempt has been made and reported in Shi et al. (1998). There, based on a study that demonstrates that flow vectors are highly correlated and can be modeled by a first-order autoregressive (AR) model, the DCT is applied to flow vectors. An adaptive threshold technique is developed to match optical-flow motion prediction and minimize the residual errors. Consequently, this optical-flow-based motion-compensated video-coding algorithm achieves good performance for very-low-bit-rate video coding. It obtains a bit rate compatible with that obtained by an H.263 standard algorithm, which uses block matching for motion estimation. (Note that the video coding standard H.263 is covered in [Chapter 19](#).) Furthermore, the reconstructed video frames by using this flow-based algorithm are free of annoying blocking artifacts. This effect is demonstrated in [Figure 14.20](#). Note that [Figure 14.20b](#) has appeared in [Figure 12.12](#), where the same picture is displayed in a larger size and the blocking artifacts are hence clearer.

**FIGURE 14.20**

(a) The 21st original frame of the “Miss America” sequence, (b) the reconstructed 21st frame with H.263, and (c) the reconstructed 21st frame with the proposed technique.

Exercises

- 14.1 What is an optical-flow field? What is a 2-D motion field? What is the difference between the two? How are they related to each other?
- 14.2 What is an aperture problem? Give two of your own examples.
- 14.3 What is the ill-posed problem? Why do we consider motion analysis from image sequences an ill-posed problem?
- 14.4 Is the relationship between the optical flow in an image plane and the velocities of objects in the 3-D world space necessarily obvious? Justify your answer.
- 14.5 What does the smoothness constraint imply? Why is it required?
- 14.6 How are the derivatives of intensity function and the Laplacian of flow components estimated in the Horn and Schunck method?
- 14.7 What are the differences between the Horn and Schunck original method and the modified Horn and Schunck method? What do you observe from these differences?
- 14.8 What is the difference between the smoothness constraint proposed by Horn and Schunck and the oriented smoothness constraint proposed by Nagel? Provide comments.
- 14.9 In your own words, describe the Singh method. What is the weighted-least-square estimation technique?
- 14.10 In your own words, describe conservation information and neighborhood information. Using this perspective, take a new look at the Horn and Schunck algorithm.
- 14.11 How is the feedback technique applied in the Pan et al. algorithm?
- 14.12 In your own words, tell the difference between the Singh method and the Pan et al. method.
- 14.13 Give two of your own examples to show that multiple image attributes are able to reduce ambiguity in image matching.
- 14.14 How does the Xia et al. method differ from the Weng et al. method?
- 14.15 How does the Xia et al. method differ from the Pan et al. method?

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15

Further Discussion and Summary on 2-D Motion Estimation

Konrad

Since [Chapter 10](#), we have been devoting our discussion to motion analysis and motion-compensated coding. Following a general description in [Chapter 10](#), three major techniques—block matching, pel-recursion, and optical flow—are covered in [Chapters 11 through 13](#), respectively.

In this chapter, before concluding this subject, we provide further discussion and a summary. A general characterization for 2-D motion estimation, thus for all three techniques, is given in [Section 15.1](#). In [Section 15.2](#), different classifications of various methods for 2-D motion analysis are given in a wider scope. [Section 15.3](#) is concerned with a performance comparison among the three major techniques. More advanced techniques and new trends in motion analysis and motion compensation are introduced in [Section 14.4](#).

15.1 General Characterization

A few common features characterizing all three major techniques are discussed in this section.

15.1.1 Aperture Problem

The aperture problem, discussed in [Chapter 13](#), describes phenomena that occur when observing motion through a small opening in a flat screen. That is, one can only observe normal velocity. It is essentially a form of ill-posed problem since it is concerned with existence and uniqueness issues, as illustrated in [Figure 13.2a](#) and [b](#). This problem is inherent with the optical-flow technique.

We note, however, that the aperture problem also exists in block-matching and pel-recursive techniques. Consider an area in an image plane having strong intensity gradients. According to our discussion in [Chapter 13](#), the aperture problem does exist in this area no matter what type of technique is applied to determine local motion. That is, motion perpendicular to the gradient cannot be determined as long as only a local measure is utilized. It is noted that, in fact, the steepest descent method of the pel-recursive technique only updates the estimate along the gradient direction (Tekalp 1995).

15.1.2 Ill-Posed Inverse Problem

In [Chapter 13](#), when we discuss the optical-flow technique, a few fundamental issues are raised. It is stated that optical-flow computation from image sequences is an inverse problem, which is usually ill-posed. Specifically, there are three problems: nonexistence,

nonuniqueness, and instability. That is, the solution may not exist; if it exists, it may not be unique; or the solution may not be stable in the sense that a small perturbation in the image data may cause a huge error in the solution.

Now we can extend our discussion to both block matching and pel-recursion. This is because both block-matching and pel-recursive techniques are intended for determining 2-D motion from image sequences, and are therefore inverse problems.

15.1.3 Conservation Information and Neighborhood Information

Because of the ill-posed nature of 2-D motion estimation, a unified point of view regarding various optical-flow algorithms is also applicable for block-matching and pel-recursive techniques. That is, all three major techniques involve extracting conservation information and extracting neighborhood information.

Take a look at the block-matching technique. There, conservation information is a distribution of some sort of features (usually intensity or functions of intensity) within blocks. Neighborhood information manifests itself in that all pixels within a block share the same displacement. If the latter constraint is not imposed, block matching cannot work. One example is the following extreme case. Consider a block size of 1×1 , i.e., a block containing only a single pixel. It is well-known that there is no way to estimate the motion of a pixel whose movement is independent of all its neighbors (Horn 1981).

With the pel-recursive technique, say, the steepest descent method, conservation information is the intensity of the pixel for which the displacement vector is to be estimated. Neighborhood information manifests itself as recursively propagating displacement estimates to neighboring pixels (spatially or temporally) as initial estimates.

In [Section 12.3](#), it is pointed out that Netravali and Robbins suggested an alternative, called “inclusion of a neighborhood area.” That is, in order to make displacement estimation more robust, they consider a small neighborhood Ω of the pixel for evaluating the square of the displaced frame difference (DFD) in calculating the update term. They assume a constant displacement vector within the area. The algorithm thus becomes

$$\bar{d}^{k+1} = \bar{d}^k - \frac{1}{2} \alpha \nabla_{\bar{d}} \sum_{i,x,y \in \Omega} w_i DFD^2(x, y; \bar{d}^k), \quad (15.1)$$

where i represents an index for the i th pixel (x, y) within Ω and w_i is the weight for the i th pixel in Ω . All the weights satisfy certain conditions; i.e., they are nonnegative, and their sum equals 1. Obviously, in this more advanced algorithm, the conservation information is the intensity distribution within the neighborhood of the pixel, the neighborhood information is imposed more explicitly, and it is stronger than that in the steepest descent method.

15.1.4 Occlusion and Disocclusion

The problems of occlusion and disocclusion make motion estimation more difficult and hence more challenging. Here we give a brief description about these and other related concepts.

Let us consider [Figure 15.1](#). There, the rectangle ABCD represents an object in an image taken at the moment of t_{n-1} , $f(x, y, t_{n-1})$. The rectangle EFGH denotes the same object, which has been translated, in the image taken at t_n moment, $f(x, y, t_n)$. In the image $f(x, y, t_n)$, the area BFDH is occluded by the object that newly moves in. On the other hand, in $f(x, y, t_n)$, the area of AECC resurfaces and is referred to as a newly visible area, or a newly exposed area.

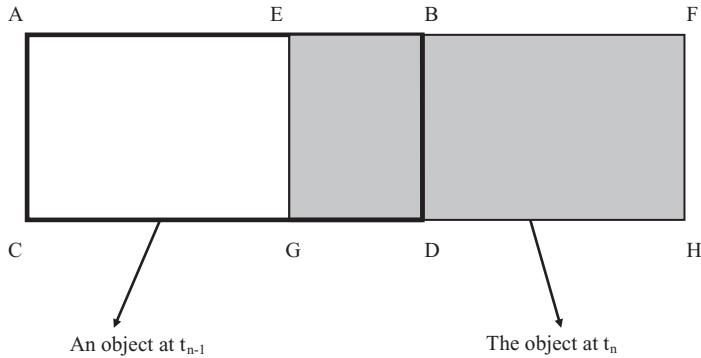


FIGURE 15.1
Occlusion and disocclusion.

Clearly, when occlusion and disocclusion occur, all three major techniques discussed in this part will encounter a fatal problem, since conservation information may be lost, making motion estimation fail in the newly exposed areas. If image frames are taken densely enough along the temporal dimension, however, occlusion and disocclusion may not cause serious problems, since the failure in motion estimation may be restricted to some limited areas. An extra bit rate paid for the corresponding increase in encoding prediction error is another way to resolve the problem. If high quality and low bit rate are both desired, then some special measures have to be taken.

One of the techniques suitable for handling the situation is Kalman filtering, which is known as the best, by almost any reasonable criterion, working in the Gaussian white noise case (Brown and Hwang 1992). If we consider the system that estimates the 2-D motion to be contaminated by the Gaussian white noise, we can use Kalman filtering to increase the accuracy of motion estimation, particularly along motion discontinuities. It is powerful in doing incremental, dynamic, and real-time estimation.

In estimating 3-D motion, the Kalman filtering was applied in Matthies et al. (1989) and Pan and Shi (1994a). Kalman filters were also utilized in optical-flow computation (Singh 1991, Pan et al. 1994b). In using the Kalman filter technique, the question of how to handle the newly exposed areas was raised in Matthies et al. (1989). In Pan and Shi (1994a), one way to handle this issue was proposed, and some experimental work demonstrated its effectiveness.

15.1.5 Rigid and Nonrigid Motion

There are two types of motion: rigid motion and nonrigid motion. Rigid motion refers to motion of rigid objects. It is known that our human vision system is capable of perceiving 2-D projections of 3-D moving rigid bodies as 2-D moving rigid bodies. Most cases in computer vision are concerned with rigid motion. Perhaps this is due to the fact that most applications in computer vision fall into this category. On the other hand, rigid motion is easier to handle than nonrigid motion. This can be seen in the following discussion.

Consider a point P in 3-D world space with the coordinates (X, Y, Z) , which can be represented by a column vector \bar{v} :

$$\bar{v} = (X, Y, Z)^T. \quad (15.2)$$

Rigid motion involves rotation and translation, and has six free-motion parameters. Let R denote the rotation matrix and T the translational vector. The coordinates of point P in the 3-D world after the rigid motion are denoted by \bar{v}' . Then we have

$$\bar{v}' = R\bar{v} + T. \quad (15.3)$$

Nonrigid motion is more complicated. It involves deformation in addition to rotation and translation, and thus cannot be characterized by the above equation. According to the Helmholtz theory (Sommerfeld 1950), the counterpart of the above equation becomes

$$\bar{v}' = R\bar{v} + T + D\bar{v} \quad (15.4)$$

where D is a deformation matrix. Note that R , T , and D are pixel dependent. Handling nonrigid motion, hence, is very complicated.

In videophony and videoconferencing applications, a typical scene might be a head-and-shoulder view of a person imposed on a background. The facial expression is nonrigid in nature. Model-based facial coding has been studied extensively (Aizawa and Harashima 1989, Li et al. 1993, Aizawa and Huang 1995). There, a 3-D wireframe model is used for handling rigid head motion. In Li et al. (1993), the facial nonrigid motion is analyzed as a weighted linear combination of a set of *action units*, instead of determining $D\bar{v}$ directly. Since the number of action units is limited, the computation becomes less expensive. In Aizawa and Harashima (1989), the portions in the human face with rich expression, such as lips, are *cut* and then transmitted out. At the receiving end, the portions are *pasted* back in the face.

Among the three types of techniques, block matching may be used to manage rigid motion, while pel-recursive and optical flow may be used to handle either rigid or nonrigid motion.

15.2 Different Classifications

There are various methods in motion estimation. They can be classified in many different ways. We discuss some of the classifications in this section.

15.2.1 Deterministic Methods vs. Stochastic Methods

Most algorithms are deterministic in nature. To see this, let us take a look at the most prominent algorithm for each of the three major 2-D motion estimation techniques. That is, the Jain and Jain algorithm for the block-matching technique (Jain 1981), the Netravali and Robbins algorithm for the pel-recursive technique (Netravali and Robbins 1979), and the Horn and Schuck algorithm for the optical-flow technique (Horn 1981). All are deterministic methods. There are also stochastic methods in 2-D motion estimation, such as the Konrad and Dubois algorithm (Konrad and Dubois 1992), which estimates 2-D motion using the maximum *a posteriori* probability (MAP).

15.2.2 Spatial Domain Methods vs. Frequency Domain Methods

While most techniques in 2-D motion analysis are spatial domain methods, there are also frequency domain methods (Kughlin and Hines 1975, Heeger 1988, Porat and Friedlander

1990, Girod 1993, Kojima 1993, Koc 1998). In Heeger (1988), a method to determine optical flow in the frequency domain, which is based on spatiotemporal filters, was developed. The basic idea and principle of the method is introduced in this subsection. A very new and effective frequency method for 2-D motion analysis (Koc 1998) is presented in [Section 15.4](#), where we discuss new trends in 2-D motion estimation.

15.2.2.1 Optical-Flow Determination Using Gabor Energy Filters

The frequency domain method of optical-flow computation developed by Heeger is suitable for highly textured image sequences. First let us take a look at how motion can be detected in the frequency domain.

15.2.2.1.1 Motion in the Spatiotemporal Frequency Domain

We initiate our discussion with a one-dimensional case. The spatial frequency of a (translationally) moving sinusoidal signal, ω_x , is defined as cycles per distance (usually cycles per pixel), while temporal frequency, ω_t , is defined as cycles per time unit (usually cycles per frame). Hence, the velocity of (translational) motion, defined as distance per time unit (usually pixels per frame), can be related to the spatial and temporal frequencies as follows.

$$v = \omega_t / \omega_x \quad (15.5)$$

A 1-D moving signal with a velocity v may have multiple spatial frequency components. Each spatial frequency component ω_{xi} , $i=1,2,\dots$ has a corresponding temporal frequency component ω_{ti} such that

$$\omega_{ti} = v\omega_{xi}. \quad (15.6)$$

This relation is shown in [Figure 15.2](#). Thus, we see that in the spatiotemporal frequency domain, velocity is the slope of a straight line relating temporal and spatial frequencies.

For 2-D moving signals, we denote spatial frequencies by ω_x and ω_y , and velocity vector by $\vec{v} = (v_x, v_y)$. The above 1-D result can be extended in a straightforward manner as follows:

$$\omega_t = v_x \omega_x + v_y \omega_y. \quad (15.7)$$

The interpretation of Equation (15.7) is that a 2-D translating texture pattern occupies a plane in the spatiotemporal frequency domain.

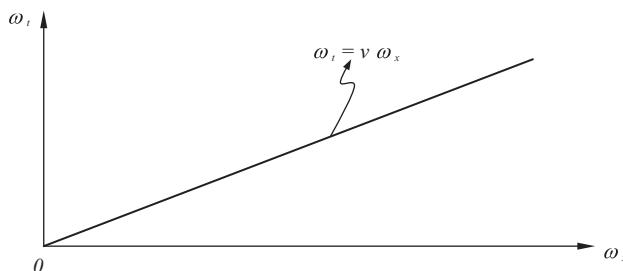


FIGURE 15.2

Velocity in 1-D spatiotemporal frequency domain.

15.2.2.1.2 Gabor Energy Filters

As Adelson and Berger pointed out, the translational motion of image patterns is characterized by orientation in the spatiotemporal domain (Adelson and Bergen 1985). This can be seen from [Figure 15.3](#). Therefore, motion can be detected by using spatiotemporally oriented filters. One of this type of filter, suggested by Heeger, is the Gabor filter.

A 1-D sine phase Gabor filter is defined as follows:

$$g(t) = \frac{1}{\sqrt{2\pi}\sigma} \sin(2\pi\omega t) \exp\left\{-\frac{t^2}{2\sigma^2}\right\}. \quad (15.8)$$

Obviously, this is a product of a sine function and a Gaussian probability density function. In the frequency domain, this is the convolution between a pair of impulses located in ω and $-\omega$, and the Fourier transform of the Gaussian, which is itself again a Gaussian function. Hence, the Gabor function is localized in a pair of Gaussian windows in the frequency domain. This means that the Gabor filter is able to selectively pick up some frequency components.

A 3-D sine Gabor function is

$$g(x, y, t) = \frac{1}{\sqrt{2\pi}^{\frac{3}{2}}\sigma_x\sigma_y\sigma_t} \cdot \exp\left\{-\frac{1}{2}\left(\frac{x^2}{\sigma_x^2} + \frac{y^2}{\sigma_y^2} + \frac{t^2}{\sigma_t^2}\right)\right\} \cdot \sin[2\pi(\omega_{x_0}x + \omega_{y_0}y + \omega_{t_0}t)] \quad (15.9)$$

where σ_x , σ_y , and σ_t are, respectively, the spreads of the Gaussian window along the spatiotemporal dimensions; and ω_{x_0} , ω_{y_0} , and ω_{t_0} are, respectively, the central spatiotemporal frequencies. The actual Gabor energy filter used by Heeger is the sum of a sine-phase filter

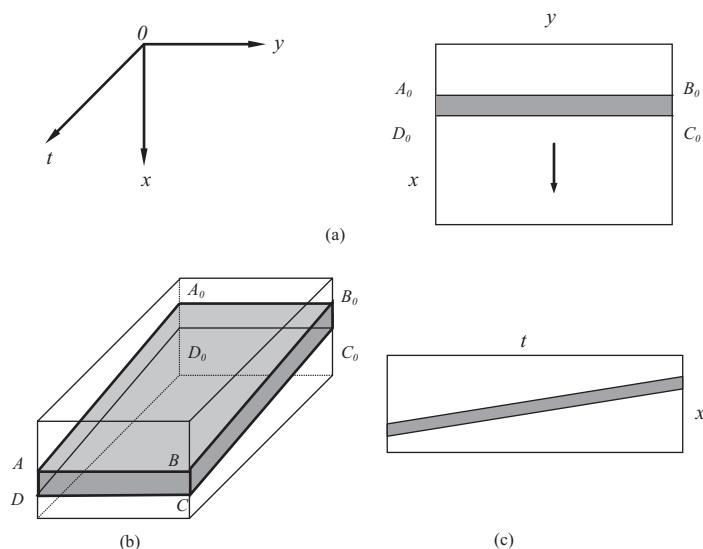


FIGURE 15.3

Orientation in spatiotemporal domain. (a) A horizontal bar translating downwards, (b) A spatiotemporal cube, and (c) A slice of the cube perpendicular to \$y\$ axis. The orientation of the slant edges represents the motion.

(which is defined above), and a cosine-phase filter (which shares the same spreads and central frequencies as that in the sine-phase filter, and replaces sine by cosine in Equation 15.9). Its frequency response, therefore, is as follows.

$$\begin{aligned} G(\omega_x, \omega_y, \omega_t) = & \frac{1}{4} \exp \left\{ -4\pi^2 \left[\sigma_x^2 (\omega_x - \omega_{x_0})^2 + \sigma_y^2 (\omega_y - \omega_{y_0})^2 \right. \right. \\ & \left. \left. + \sigma_t^2 (\omega_t - \omega_{t_0})^2 \right] \right\} + \frac{1}{4} \exp \left\{ -4\pi^2 \left[\sigma_x^2 (\omega_x + \omega_{x_0})^2 \right. \right. \\ & \left. \left. + \sigma_y^2 (\omega_y + \omega_{y_0})^2 + \sigma_t^2 (\omega_t + \omega_{t_0})^2 \right] \right\} \end{aligned} \quad (15.10)$$

This indicates that the Gabor filter is motion-sensitive in that it responds largely to motion that has more power distributed near the central frequencies in the spatiotemporal frequency domain, while it responds poorly to motion that has little power near the central frequencies.

15.2.2.1.3 Flow Extraction with Motion Energy

Using a vivid example, Heeger explains in his paper why one such filter is not sufficient in detection of motion. Multiple Gabor filters must be used. In fact, a set of twelve Gabor filters are utilized in Heeger's algorithm. The twelve Gabor filters in the set have one thing in common:

$$\omega_0 = \sqrt{\omega_{x0}^2 + \omega_{y0}^2}. \quad (15.11)$$

In other words, the twelve filters are tuned to the same spatial frequency band but to different spatial orientation and temporal frequencies.

Briefly speaking, optical flow is determined as follows. Denote the measured motion energy by $n_i, i=1, 2, \dots, 12$. Here i indicates one of the twelve Gabor filters. The summation of all n_i is denoted by

$$\bar{n} = \sum_{i=1}^{12} n_i. \quad (15.12)$$

Denote the predicted motion energy by $P_i(v_x, v_y)$, and the sum of predicted motion energy by

$$\bar{P} = \sum_{i=1}^{12} P_i(v_x, v_y). \quad (15.13)$$

Similar to what many algorithms do, optical-flow determination is then converted to a minimization problem. That is, optical flow should be able to minimize error between the measured and predicted motion energies:

$$J(v_x, v_y) = \sum_{i=1}^{12} \left[n_i - \bar{n} \frac{P_i(v_x, v_y)}{\bar{P}} \right]^2. \quad (15.14)$$

Similarly, many readily available numerical methods can be used for solving this minimization problem.

15.2.3 Region-Based Approaches vs. Gradient-Based Approaches

As stated in [Chapter 10](#), methodologically speaking, there are generally two approaches to 2-D motion analysis for video coding: region-based and gradient-based. Now that we have gone through three major techniques, we can see this classification more clearly.

The region-based approach can be characterized as follows. For a region in an image frame, we find its best match in another image frame. The relative spatial position between these two regions produces a displacement vector. The best matching is found by minimizing a dissimilarity measure between the two regions, which is defined as

$$\sum_{(x,y) \in R} \sum M[f(x,y,t), f(x-dx, y-dy, t-\Delta t)], \quad (15.15)$$

where R denotes a spatial region, on which the displacement vector $(d_x, d_y)^T$ estimate is based; $M[\alpha, \beta]$ denotes a dissimilarity measure between two arguments α and β ; Δt is the time interval between two consecutive frames.

Block matching certainly belongs to the region-based approach. By region, we mean a rectangle block. For an original block in a (current) frame, block matching searches for its best match in another (previous) frame among candidates. Several dissimilarity measures are utilized, among which the mean absolute difference (MAD) is used most often.

Although it uses the spatial gradient of intensity function, the pel-recursive method with inclusion of a neighborhood area assumes the same displacement vector within a neighborhood region. A weighted sum of the squared DFD within the region is used as a dissimilarity measure. By using numerical methods such as various descent methods, the pel-recursive method iteratively minimizes the dissimilarity measure, thus delivering displacement vectors. The pel-recursive technique is therefore in the category of region-based approaches.

In optical-flow computation, the two most frequently used techniques discussed in [Chapter 13](#) are the gradient method and the correlation method. Clearly, the correlation method is region-based. In fact, as we pointed out in [Chapter 13](#), it is very similar to block matching.

As far as the gradient-based approach is concerned, we start its characterization with the brightness invariant equation, covered in [Chapter 13](#). That is, we assume that brightness is conserved during the time interval between two consecutive image frames.

$$f(x, y, t) = f(x - d_x, y - d_y, t - \Delta t). \quad (15.16)$$

By expanding the right-hand side of the above equation into the Taylor series, applying the above equation, and some mathematical manipulation, we can derive the following equation.

$$f_x u + f_y v + f_t = 0, \quad (15.17)$$

where f_x, f_y, f_t are partial derivatives of intensity function with respect to x, y , and t , respectively; and u and v are two components of pixel velocity. This equation contains gradients of intensity function with respect to spatial and temporal variables and links two components of the displacement vector. The square of the left-hand side in the above equation is an error that needs to be minimized. Through the minimization, we can estimate displacement vectors.

TABLE 15.1

Region-Based vs. Gradient-Based Approaches

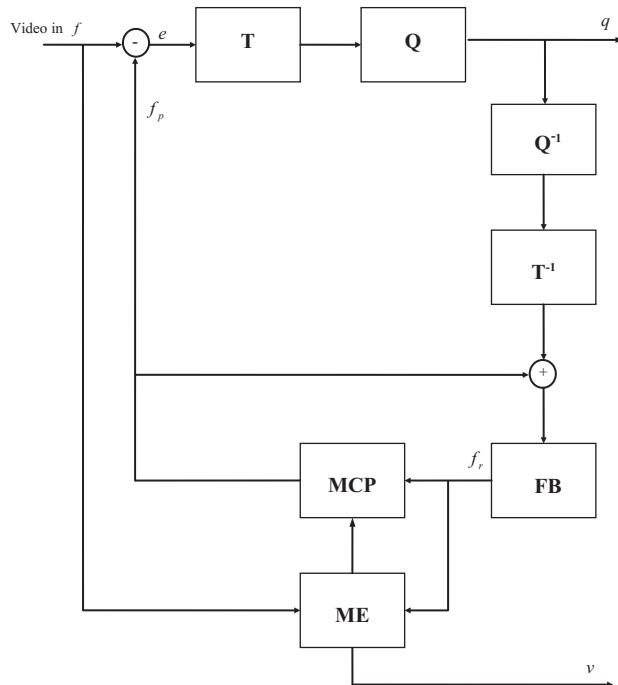
| | Block Matching | Pel-Recursive | Optical Flow | |
|---------------------------|----------------|---------------|-----------------------|--------------------------|
| | | | Gradient-Based Method | Correlation-Based Method |
| Regional-based approaches | ✓ | ✓ | | ✓ |
| Gradient-based approaches | | | ✓ | |

Clearly, the gradient method in optical-flow determination, discussed in [Chapter 13](#), falls into the above framework. There, an extra constraint is imposed and included into the error represented in Equation 15.17.

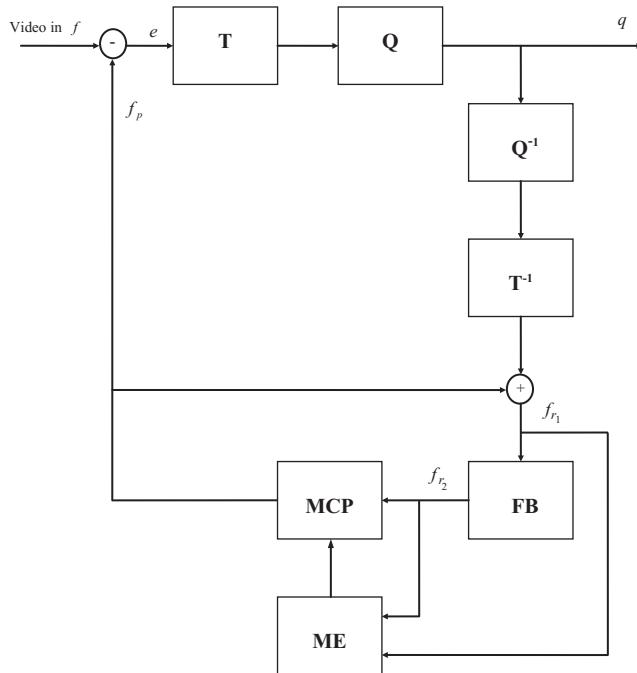
The following table summarizes what we discussed in this subsection ([Table 15.1](#)).

15.2.4 Forward vs. Backward Motion Estimation

Motion-compensated predictive video coding may be done in two different ways: forward and backward (Boroczky 1991). These ways are depicted in [Figures 15.4](#) and [15.5](#), respectively. With the forward manner, motion estimation is carried out by using the

**FIGURE 15.4**

Forward motion estimation and compensation, T: transformer, Q: quantizer, FB: frame buffer, MCP: motion-compensated predictor, ME: motion estimator, e: prediction error, f: input video frame, f_p : predicted video frame, f_r : reconstructed video frame, q: quantized transform coefficients, v: motion vector.

**FIGURE 15.5**

Backward motion estimation and compensation, T: transformer, Q: quantizer, FB: frame buffer, MCP: motion-compensated predictor, ME: motion estimator, e : prediction error, f : input video frame, f_p : predicted video frame, f_{r1} : reconstructed video frame, f_{r2} : reconstructed previous video frame, q : quantized transform coefficients.

original input video frame and the reconstructed previous input video frame. With the backward manner, motion estimation is implemented with two successive reconstructed input video frames.

The former provides relatively higher accuracy in motion estimation and hence more efficient motion compensation than the latter, owing to the fact that the original input video frames are utilized. However, the latter does not need to transmit motion vectors to the receiving end as an overhead, while the former does.

Block matching is used in almost all the international video coding standards, such as H.261, H.263, and MPEG 1 and MPEG 2 (which are covered in the next part of this book), as forward motion estimation. The pel-recursive technique is used as backward motion estimation. In this way, the pel-recursive technique avoids encoding a large amount of motion vectors. On the other hand, it provides relatively less accurate motion estimation than block matching. Optical flow is usually used as forward motion estimation in motion-compensated video coding. Therefore, as expected, it achieves higher motion estimation accuracy on the one hand and it needs to handle a large amount of motion vectors as overhead on the other hand. These will be discussed in the next section.

It is noted that one of the new improvements in the block-matching technique is described in [Section 11.6.3](#). It is called the predictive motion field segmentation technique (Orchard 1993), and it is motivated by backward motion estimation. There, segmentation is conducted *backwards*, i.e., based on previously decoded frames. The purpose of this is to save overhead for shape information of motion discontinuities.

15.3 Performance Comparison between Three Major Approaches

15.3.1 Three Representatives

A performance comparison between the three major approaches—block matching, pel-recursion, and optical flow—was provided in a review paper by Dufaux and Moscheni (1995). Experimental work was carried out as follows. The conventional full-search block matching is chosen as a representative for the block-matching approach, while the Netravali and Robbins algorithm and the modified Horn and Schunck algorithm are chosen to represent the pel-recursion and optical-flow approaches, respectively.

15.3.2 Algorithm Parameters

In full-search block matching, the block size is chosen as 16×16 pixels, the maximum displacement is ± 15 pixels, and the accuracy is half pixels. In the Netravali and Robbins pel-recursion, $\varepsilon = 1/1024$, the update term is averaged in an area of 5×5 pixels and clipped to a maximum of $1/16$ pixels per frame, and the algorithm iterates one iteration per pixel. In the modified Horn and Schunck algorithm, the weight α^2 is set to 100, and 100 iterations of the Gauss and Seidel procedure are carried out.

15.3.3 Experimental Results and Observations

The three test video sequences are the “Mobile and Calendar,” “Flower Garden,” and “Table Tennis.” Both subjective criterion (in terms of needle diagrams showing displacement vectors) and objective criteria (in terms of DFD error energy) are applied to access the quality of motion estimation.

It turns out that the pel-recursive algorithm gives the worst accuracy in motion estimation. In particular, it cannot follow the fast and large motions. Both block-matching and optical-flow algorithms give better motion estimation.

It is noted that we must be cautious in drawing conclusions from these tests. This is because different algorithms in the same category and the same algorithm under different implementation conditions will provide quite different performances. In the above experiments, the full-search block matching with half-pixel accuracy is one of the better block-matching techniques. On the contrary, there are many improved pel-recursive and optical-flow algorithms, which outperform the chosen representatives in the reported experiments.

The experiments do, however, provide an insight about the three major approaches. Pel-recursive algorithms are seldom used in video coding now, mainly due to their inaccurate motion estimation, although they do not require transmitting motion vectors to the receiving end. Although they can provide relatively accurate motion estimation, optical-flow algorithms require a large amount of overhead for handling dense motion vectors. This prevents the optical-flow techniques from wide and practical usage in video coding. Block matching is simple, yet very efficient for motion estimation. It provides quite accurate and reliable motion estimation for most practical video sequences in spite of its simple piecewise translational model. At the same time, it does not require much overhead. Therefore, for first-generation video coding, block matching is considered to be the most suitable among the three approaches.

15.4 New Trends

In Chapters 11 through 13, many new, effective improvements within the three major approaches were discussed. These techniques include multiresolution block matching, (locally adaptive) multigrid block matching, overlapped block matching, thresholding techniques, (predictive) motion field segmentation, feedback, and multiple attributes in optical-flow computation, subpixel accuracy, and so on. Some improvements will be discussed in Part IV, where various international video coding standards such as H.263 and MPEG 2 and 4 are introduced.

As pointed out in Orchard (1998), today our understanding of motion analysis and video compression is still based on an ad-hoc framework, in general. What today's standards have achieved is not near the ideally possible performance. Therefore, more efforts are continuously made in this field, seeking much more simple, practical, and efficient algorithms.

As an example of such developments, we conclude this chapter by presenting a novel method for 2-D motion estimation: the DCT-based motion estimation (Koc 1998).

15.4.1 DCT-Based Motion Estimation

As pointed out in Section 15.2.2, as opposed to the conventional 2-D motion estimation techniques, this method is carried out in the frequency domain. It is also different from the Gabor energy filter method by Heeger, discussed in Section 15.2.2.1. Without introducing Gabor filters, this method is directly DCT-based. The fundamental concepts and techniques of this method are discussed below.

15.4.1.1 DCT and DST Pseudophases

The underlying idea behind this method is to estimate 2-D translational motion by determining the DCT and DST (discrete sine transform) *pseudophases*. Let us use the simpler 1-D case to illustrate this concept. Once it is established, it can be easily extended to the 2-D case.

Consider a 1-D signal sequence $\{f(n), n \in (0, 1, \dots, N-1)\}$ of length N . Its translated version is denoted by $\{g(n), n \in (0, 1, \dots, N-1)\}$. The translation is defined as follows.

$$g(n) = \begin{cases} f(n-d), & \text{if } (n-d) \in (0, 1, \dots, N-1) \\ 0, & \text{otherwise} \end{cases} \quad (15.18)$$

In the above equation, d is the amount of the translation and it needs to be estimated. Let us define the following several functions before introducing the pseudophases. The DCT and the DST of the second kind of $g(n)$, $G^C(k)$ and $G^S(k)$, are defined as follows.

$$G^C(k) = \frac{2}{N} C(k) \sum_{n=0}^{N-1} g(n) \cos \left[\frac{k\pi}{N} (n+0.5) \right] \quad k \in \{0, 1, \dots, N-1\} \quad (15.19)$$

$$G^S(k) = \frac{2}{N} C(k) \sum_{n=0}^{N-1} g(n) \sin \left[\frac{k\pi}{N} (n+0.5) \right] \quad k \in \{1, \dots, N\} \quad (15.20)$$

The DCT and DST of the first kind of $f(n)$, $F^C(k)$ and $F^S(k)$, are defined as

$$F^C(k) = \frac{2}{N} C(k) \sum_{n=0}^{N-1} f(n) \cos \left[\frac{k\pi}{N} n \right] \quad k \in \{0, 1, \dots, N-1\} \quad (15.21)$$

$$F^S(k) = \frac{2}{N} C(k) \sum_{n=0}^{N-1} f(n) \sin \left[\frac{k\pi}{N} n \right] \quad k \in \{1, \dots, N\} \quad (15.22)$$

In the above equations, $C(k)$ is defined as

$$C(k) = \begin{cases} \frac{1}{\sqrt{2}} & \text{for } n = 0 \text{ or } N \\ 1 & \text{otherwise} \end{cases} \quad (15.23)$$

Now we are in a position to introduce the following equation, which relates the translational amount d to the DCT and DST of the original sequence and its translated version, defined above. That is,

$$\begin{bmatrix} G^C(k) \\ G^S(k) \end{bmatrix} = \begin{bmatrix} F^C(k) & -F^S(k) \\ F^C(k) & F^C(k) \end{bmatrix} \begin{bmatrix} D^C(k) \\ D^S(k) \end{bmatrix}, \quad (15.24)$$

where $D^C(k)$ and $D^S(k)$ are referred to as the pseudophases and defined as follows:

$$D^C(k) \stackrel{\Delta}{=} \cos \left[\frac{k\pi}{N} \left(d + \frac{1}{2} \right) \right] \quad (15.25)$$

$$D^S(k) \stackrel{\Delta}{=} \sin \left[\frac{k\pi}{N} \left(d + \frac{1}{2} \right) \right]$$

Equation (15.24) can be solved for the amount of translation d , thus motion estimation. This becomes clearer when we rewrite the equation in a matrix-vector format. Denote the 2×2 matrix in Equation (15.24) by $\mathbf{F}(k)$, the 2×1 column vector at the left-hand side of the equation by $\bar{G}(k)$, and the 2×1 column vector at the right-hand side by $\bar{D}(k)$. It is easy to verify that the matrix $\mathbf{F}(k)$ is orthogonal by observing the following.

$$\lambda \mathbf{F}^T(k) \mathbf{F}(k) = \mathbf{I} \quad (15.26)$$

where \mathbf{I} is a 2×2 identity matrix, the constant λ is

$$\lambda = \frac{1}{[\mathbf{F}^C(k)]^2 + [\mathbf{F}^S(k)]^2}. \quad (15.27)$$

We then derive the matrix-vector format of Equation 15.24 as follows:

$$\vec{D}(k) = \lambda \mathbf{F}^T(k) \bar{G}(k) \quad k \in \{1, \dots, N-1\} \quad (15.28)$$

15.4.1.2 Sinusoidal Orthogonal Principle

It was shown above that the pseudophases, which contain the translation information, can be determined in the DCT and DST frequency domain. But how the amount of the translation can be found has not been mentioned. Here, the algorithm uses the sinusoidal principle to pick up this information. That is, the inverse DST of the second kind of scaled pseudophase, $C(k)D^S(k)$, is found to equal an algebraic sum of the following two discrete impulses according to the sinusoidal orthogonal principle:

$$\begin{aligned} ISDT \{C(k)D^S(k)\} \frac{2}{N} \sum_{k=1}^N C^2(k)D^S(k) \sin \left[\frac{k\pi}{N} \left(n + \frac{1}{2} \right) \right] \\ = \delta(d-n) - \delta(d+n+1) \end{aligned} \quad (15.29)$$

Since the inverse DST is limited to $n \in \{0, 1, \dots, N-1\}$, the only peak value among this set of N values indicates the amount of the translation d . Furthermore, the direction of the translation (positive or negative) can be determined from the polarity (positive or negative) of the peak value.

The block diagram of the algorithm is shown in Figure 15.6. This technique can be extended to the 2-D case in a straightforward manner. Interested readers should refer to Koc (1998).

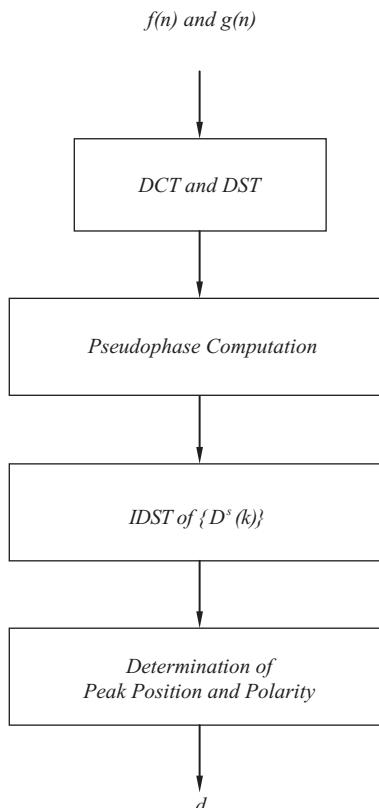


FIGURE 15.6

Block diagram of DCT-based motion estimation (1-D case).

15.4.1.3 Performance Comparison

The algorithm was applied to several typical testing video sequences, such as the "Miss America" and "Flower Garden" sequences, and an "Infrared Car" sequence. The results were compared with the conventional full-search block-matching technique and several fast-search block-matching techniques such as the 2-D logarithm search, three-step search, search with subsampling in the original block and the correlation windows.

Prior to applying the algorithm, one of the following preprocessing procedures is implemented: frame differentiation or edge extraction. It was reported that for the "Flower Garden" and "Infrared Car" sequences, the DCT-based algorithm achieves a higher coding efficiency than all three fast search block-matching methods, while for the Miss America sequence it obtains a lower efficiency. It was also reported that it performs well even in a noisy situation.

A lower computational complexity, $O(M^2)$ for an $M \times M$ search range, is one of the major advantages possessed by the DCT-based motion estimation algorithm compared with conventional full-search block matching, $O(M^2 \cdot N^2)$ for an $M \times M$ search range and an $N \times N$ block size.

With DCT-based motion estimation, a fully DCT-based motion-compensated coder structure becomes possible, which is expected to achieve a higher throughput and a lower system complexity.

15.5 Summary

In this chapter, which concludes the motion analysis and compensation portion of the book, we first generalize the discussion of the aperture problem, the ill-posed nature, and the conservation-and-neighborhood-information unified point of view, previously made with respect to the optical-flow technique in [Chapter 13](#), to cover block-matching and pel-recursive techniques. Then, the occlusion and disocclusion, and rigidity and nonrigidity, are discussed with respect to the three techniques. The difficulty of nonrigid motion estimation is analyzed. Its relevance in visual communications is addressed.

Different classifications of various methods in the three major 2-D motion estimation techniques—block matching, pel-recursion, and optical flow—are presented. Besides the frequently utilized deterministic methods, spatial domain methods, region-based methods, and forward motion estimation, their counterparts—stochastic methods, frequency domain methods, gradient methods, and backward motion estimation—are introduced. In particular, two frequency domain methods are presented with some detail. They are the method using the Gabor energy filter and the DCT-based method.

A performance comparison between the three techniques is also introduced in this chapter, based on which observations are drawn. A main point is that block matching is at present the most suitable technique for 2-D motion estimation among the three techniques.

Exercises

- 15.1 What is the difference between the rigid motion and nonrigid motion? In facial encoding, what is the nonrigid motion? How is the nonrigid motion handled?
- 15.2 How is 2-D motion estimation carried out in the frequency domain? What are the underlying ideas behind the Heeger method, and the Koc and Liu method?
- 15.3 Why is one Gabor energy filter not sufficient in motion estimation? Draw the power spectrum of a 2-D sine-phase Gabor function.
- 15.4 Show the correspondence of a positive (negative) peak value in the inverse DST of the second kind of DST pseudophase to a positive (negative) translation in the 1-D spatial domain.
- 15.5 How does neighborhood information manifest itself in the pel-recursive technique?
- 15.6 Using your own words and some diagrams, state that the translational motion of an image pattern is characterized by orientation in the spatiotemporal domain.

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Part IV

Video Compression



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16

Fundamentals of Digital Video Coding

In this chapter, we introduce the fundamentals of digital video coding, which include digital video representation, rate distortion theory, and digital video formats. Also, we give a brief overview of image and video coding standards, which will be discussed in the subsequent chapters.

16.1 Digital Video Representation

As we discussed in previous chapters, a digital image is obtained by quantizing a continuous image both spatially and in amplitude. Digitization of the spatial coordinates is called image sampling, while digitization of the amplitude is called gray-level quantization. Suppose that a continuous image is denoted by $g(x, y)$, where the amplitude or value of g at the point (x, y) is the intensity or brightness of an image at that point. The transformation of a continuous image to a digital image can then be expressed as

$$f(m, n) = Q[g(x_0 + m\Delta x, y_0 + n\Delta y)] \quad (16.1)$$

where Q is a quantization operator, x_0 and y_0 are the origin of image plane, m and n are the discrete values $0, 1, 2, \dots$, and Δx and Δy are the sampling intervals in the horizontal and vertical directions, respectively. If the sampling process is extended to a third temporal direction (or the original signal in the temporal direction is a discrete format), a sequence, $f(m, n, t)$, is obtained as introduced in [Chapter 10](#),

$$f(m, n, t) = Q[g(x_0 + m\Delta x, y_0 + n\Delta y, t_0 + t\Delta t)] \quad (16.2)$$

where t is the values $0, 1, 2, \dots$ and Δt is the time interval.

Each point of the image or each basic element of the image is called a pixel or pel. Each individual image is called a frame. According to the sampling theory, the original continuous signal can be recovered exactly from its samples if the sampling frequency is higher than two times the bandwidth of the original signal (Oppenheim and Schafer 1989). The frames are normally presented at a regular time interval so that the eye can perceive fluid motion. For example, the National Television Systems Committee (NTSC) specified a temporal sampling rate of 30 frames per second and interlace of 2 to 1. Therefore, as a result of this spatio-temporal sampling, the digital signals exhibit high spatial and temporal correlation, just as the analog signals did before video data compression. In the following, we will discuss the theoretical basis of video digitization. An important notion is the strong dependence between values of neighboring pixels within the same frame and between the

frames themselves; this can be regarded as statistical redundancy of the image sequence. In the following section, we will explain how this statistical redundancy is exploited to achieve compression of the digitized image sequence.

16.2 Information Theory Results: Rate Distortion Function of Video Signal

The principal goal in the design of a video coding system is to reduce the transmission rate requirements of the video source subject to some picture quality constraint. There are only two ways to accomplish this goal: reduction of the statistical redundancy and psychophysical redundancy of the video source. The video source is normally very highly correlated, both spatially and temporally; that is, strong dependence can be regarded as statistical redundancy of the data source. If the video source to be coded in a transmission system is viewed by a human observer, the perceptual limitations of human vision can be used to reduce transmission requirements. Human observers are subject to perceptual limitations in amplitude, spatial resolution, and temporal acuity. By proper design of the coding system, it is possible to discard information without affecting perception, or at least, with only minimal degradation. In summary, we can use two factors—the statistical structure of the data source and the fidelity requirements of the end user—which make the compression possible. The performance of the video compression algorithm depends on several factors. First, and also a basic one, is the amount of redundancy contained in the video data source. In other words, if the original source contains a large amount of information, or high complexity, then more bits are needed to represent the compressed data. Second, if a lossy coding technique is used, by which some amount of loss is permitted in the reconstructed video data, then the performance of the coding technique depends on the compression algorithm and distortion measurements. In lossy coding, different distortion measurements will perceive the loss in different ways, giving different subjective results. The development of a distortion measure that can provide consistent numerical and subjective results is a very difficult task. Moreover, the majority of the video compression applications do not require lossless coding, i.e., it is not required that the reconstructed and original images be identical or reversible.

This intuitive explanation of how redundancy and lossy coding methods can be used to reduce source data is made more precise by Shannon's rate distortion theory (Berger 1971), which addresses the problem of how to characterize both the source and the distortion measure. Let us consider the model of a typical visual communication system depicted in [Figure 16.1](#). The source video data is fed to the encoder system, which consists of two parts: source coding and channel coding. The function of the source coding is to remove the redundancy in both the spatial and temporal domain, whereas the function of channel coding is to insert the controlled redundancy, which is used to protect the transmitted data from the interference of channel noise. It should be noted that according to Shannon (1948) certain conditions allow the source and channel coding operations to be separated without any loss of optimality, such as when the sources are ergodic. However, Shannon did not indicate the complexity constraint on the coder involved. In practical systems that are limited by the complexity, this separation may not be possible (Viterbi and Omura 1979). There is still some work on the joint optimization of the source and channel coding (Modestino et al. 1981, Sayood and Borkenhagen 1991). Coming back to rate-distortion theory, the problem addressed here is the minimization of the channel capacity requirement, while maintaining the average distortion at or below an acceptable level.

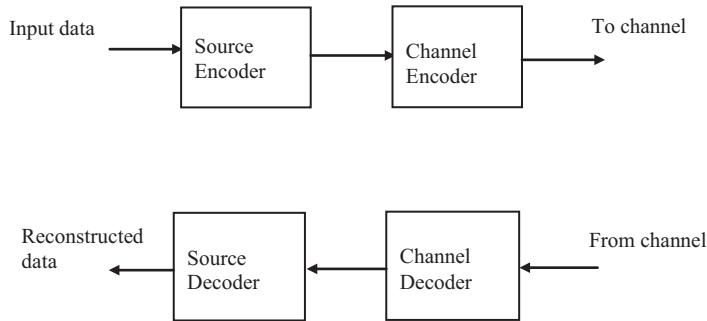


FIGURE 16.1
A typical visual communication system.

The rate distortion function $R(D)$ is the minimum average rate (bits/element), and hence minimum channel capacity, required for a given average distortion level D . To make this more quantitative, we suppose that the source is a sequence of pixels, and these values are encoded by successive blocks of length N . Each block of pixels is then described by one of a denumerable set of messages, $\{X_i\}$, with probability function, $P(X_i)$. For a given input source, $\{X_i\}$, and output, $\{Y_j\}$, the decoder system can be described mathematically by the conditional probability, $Q(Y_j/X_i)$. Therefore, the probability of the output message is,

$$T(Y_j) = \sum_i P(X_i)Q(Y_j/X_i) \quad (16.3)$$

The information transmitted is called the average mutual information between Y and X and is defined for a block of length N as follows:

$$I_N(X, Y) = \sum_i \sum_j P(X_i)Q(Y_j/X_i) \log_2 \frac{Q(Y_j/X_i)}{T(Y_j)} \quad (16.4)$$

In the case of error-free encoding, $Y = X$ and then

$$Q(Y_j/X_i) = \begin{cases} 1, & j = i, \\ 0, & j \neq i \end{cases} \quad \text{and} \quad T(Y_j) = T(Y_i) \quad (16.5)$$

In this case, Equation 16.4 becomes

$$I_N(X, Y) = \sum_i \sum_j P(X_i) \log_2 P(X_i) = H_N(X) \quad (16.6)$$

which is the N th-order entropy of the data source. This can also be seen as the information contained in the data source under the assumption that no correlation exists between blocks and all the correlation between elements of each N length block is considered. Therefore, it requires at least $H_N(X)$ bits to code the data source without any information loss. In other words, the optimal error-free encoder requires $H_N(X)$ bits for the given data

source. In the most general case, noise in the communication channel will result in error at least some of the time, causing $Y \neq X$. As a result,

$$I_N(X, Y) = H_N(X) - H_N(X/Y) \quad (16.7)$$

where $H_N(X/Y)$ is the entropy of the source data at the condition of decoder output Y . Since the entropy is a positive quantity, the source entropy is the upper bound to the mutual information; i.e.,

$$I_N(X, Y) \leq H_N(X) \quad (16.8)$$

Let $d(X, Y)$ be the average distortion between X and Y . Then, the average distortion per pixel is defined as

$$D(Q) = \frac{1}{N} E\{d(X, Y)\} = \frac{1}{N} \sum_i \sum_j d(X_i, Y_j) P(X_i) Q(X_i/Y_j) \quad (16.9)$$

The set of all conditional probability assignments, $Q(Y/X)$, that yield average distortion less than or equal to D^* , can be written as:

$$\{Q: D(Q) \leq D^*\} \quad (16.10)$$

The N -block rate distortion function is then defined as the minimum of the average mutual information, $I_N(X, Y)$, per pixel:

$$R_N(D^*) = \min_{Q: D(Q) \leq D^*} \frac{1}{N} I_N(X, Y) \quad (16.11)$$

The limiting value of the N -block rate distortion function is simply called the rate distortion function,

$$R(D^*) = \lim_{N \rightarrow \infty} R_N(D^*) \quad (16.12)$$

It should be clear from the above discussion that Shannon's rate distortion function is a lower bound on the transmission rate required to achieve an average distortion D when the block size is infinite. In other words, when the block size is approaching infinity, the correlation between all elements within the block is considered as the information contained in the data source. Therefore, the rate obtained is the lowest rate or lower bound. Under these conditions, the rate at which a data source produces information, subject to a requirement of perfect reconstruction, is called the entropy of the data source, i.e., the information contained in the data source. It follows that the rate distortion function is a generalization of the concept of entropy. Indeed, if the distortion measure is a perfect reproduction, it is assigned zero distortion. Then, $R(0)$ is equal to the source entropy $H(X)$. Shannon's coding theorem states that one can design a coding system with rate only negligibly greater than $R(D)$, which achieves the average distortion D . As D increases, $R(D)$ decreases monotonically and usually becomes zero at some finite value of distortion. The rate distortion function $R(D)$ specifies the minimum achievable transmission rate required

to transmit a data with average distortion level D . The main value of this function in a practical application is that it potentially gives a measure for judging the performance of a coding system. However, this potential value has not been completely realized for video transmission. There are two reasons for this. First of all, there currently do not exist tractable and faithful mathematical models for an image source. The rate distortion function for Gaussian sources under the squared-error distortion criterion can be found, but it is not a good model for images. The second reason is that a suitable distortion measure, D , which matches the subjective evaluation of image quality, has not been totally solved. Some results have been investigated for this task such as just noticeable distortion (JND). The issue of subjective and objective assessment of image quality has been discussed in [Chapter 1](#). In spite of these drawbacks, the rate distortion theorem is still a mathematical basis for comparing the performance of different coding systems.

16.3 Digital Video Formats

16.3.1 Digital Video Color Systems

In practical applications, most video signals are color signals. Various color systems have been discussed in [Chapter 1](#). A color signal can be seen as a summation of light intensities of three primary wavelength bands. In this section, we are going to introduce several extensively used color systems in the video industry. There are two primary color spaces used to represent digital video signal: red, green, and blue (*RGB*) and *YCbCr*. The difference between *RGB* and *YCbCr* is that *RGB* represents color as red, green, and blue, while *YCbCr* represents color as brightness and two-color difference signals. In *YCbCr*, the *Y* is the brightness (luma), *Cb* is blue minus luma (*B-Y*) and *Cr* is red minus luma (*R-Y*). We usually use *YCC* as a short way of saying *YCrCb*. The standard *RGB* color space is referred to as *sRGB*, which is an *RGB* color space created cooperatively by Hewlett-Packard and Microsoft Corporation. It has been endorsed by many industry players. It is also well accepted by Open Source software such as the GIMP, and is used in proprietary and open graphics file formats such as PNG. The *sYCC* is simply *YCC* created from *sRGB* (IEC 61966-2-1 [1999]). The *YCbCr* color representation is used for most video coding standards in compliance with the ITU-R BT.601 (International Telecommunications 1987), BT.709 (International Telecommunications 1990), CIF, and SIF formats. ITU-R BT.601 is an ITU-R standard for component digital video. It was designed to provide a common digital standard for interoperability between the three analog video/TV systems (NTSC, PAL, and SECAM). ITU-R BT.601 enables their signals to be converted to digital and then easily converted back again to any of the three formats for distribution. In 1990, BT.709 was introduced for high-definition television (HDTV) with specifications for 1125 and 1250 lines. In 2000, BT.709-4 added 1080 lines to conform to the DTV standard. Conversion between the *YC_bC_r* and *RGB* formats can be accomplished with the transformations in [Chapter 1](#).

Different color spaces cover different range of colors. The term “gamut” is used to represent a set of possible colors within a color system. Currently, most video displays are *sRGB* gamut-limited displays, while the still image systems widely use the displays with *sYCC* color space. Recently, various kinds of extended-gamut displays are emerging and used for displaying still images. Users are always enjoying wide-gamut displays. In video signals there are many unused regions that could store wide-gamut colors. Therefore,

recently a new color space standard, IEC 61966-2-4, has been proposed for video displays (IEC 61966-2-4). In IEC 61966-2-4, the extended-gamut color space for video applications—*xvYCC* color space—has been proposed. The *xvYCC* is compatible with currently used video signals. It uses the same definition for inside of the sRGB gamut and there is no change necessary for conventional contents. However, it adds an unambiguous definition to the currently undefined or out-of-sRGB gamut regions. The *xvYCC* has 100% coverage while sRGB has only 55%, which can be seen in Figures 16.2 and 16.3 (Katoh 2005).

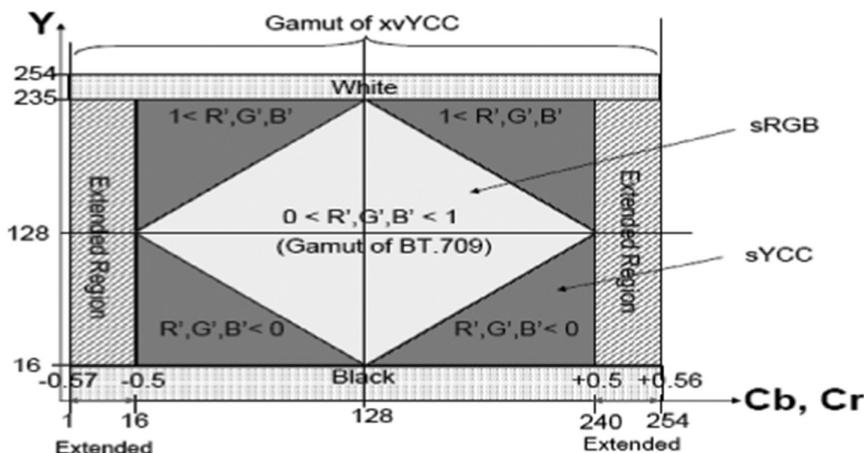


FIGURE 16.2

Two-dimensional view of xvYCC. (From Katoh, N. and Simpuku, Y., *Katoh attachment of proposal for MPEG Hong Kong Meeting*, IEC 61966-2-4 The extended-gamut color space for video application – xvYCC color space, by Color Rendering Community, Sony Corporation, 2005.)

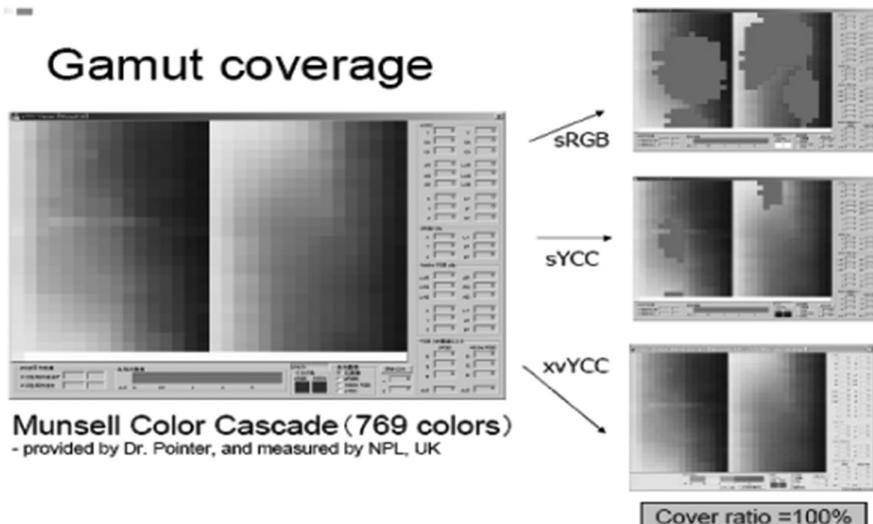


FIGURE 16.3

Gamut coverage of sRGB, sYCC, and xvYCC color spaces. (From Katoh, N. and Simpuku, Y., *Katoh attachment of proposal for MPEG Hong Kong Meeting*, IEC 61966-2-4 The extended-gamut color space for video application – xvYCC color space, by Color Rendering Community, Sony Corporation, 2005.)

16.3.2 Progressive and Interlaced Video Signals

Currently, most video signals that are generated by a TV camera are interlaced. These video signals are represented at 30 frames per second for an NTSC system. Each frame consists of two fields, the top field and bottom field, which are 1/60 of a second apart. In the display of an interlaced frame, the top field is scanned first and the bottom field is scanned next. The top and bottom fields are composed of alternating lines of the interlaced frame. Progressive video does not consist of fields, only frames. In an NTSC system, these frames are spaced 1/30 seconds apart. In contrast to interlaced video, every line within the frame is successively scanned. An example of progressive and interlaced video is shown in [Figure 16.4](#).

16.3.3 Video Formats Used by Video Industry

ITU-R: According to ITU-R 601 (ITU-R was CCIR previously), a color video source has three components: a luminance component (Y) and two-color difference or chrominance components (C_b and C_r , or U and V in some documents). The CCIR format has two options: one for the NTSC TV system and another for the PAL TV system. Both are interlaced. The NTSC format uses 525 lines per frame at 30 frames per second. The luminance frames of this format have 720×480 active pixels. The chrominance frames have two kinds of formats; one has 360×480 active pixels and is referred as the 4:2:2 format, while the other has 360×240 active pixels and is referred as the 4:2:0 format. The PAL format uses 625 lines per frame at 25 frames per second. Its luminance frame has 720×576 active pixels per frame and the chrominance frame has 360×576 active pixels per frame for the 4:2:2 format and 360×288 pixels per frame for the 4:2:0 format, both at 25 frames per second.

The a:b:c notation for sampling ratios, as found in the ITU-R BT601 (ITU-R BT601) specifications, has the following meaning:

4:2:2 means 2:1 horizontal downsampling and no vertical downsampling. (Think 4 Y samples for every 2 C_b and 2 C_r samples in a scanline.)

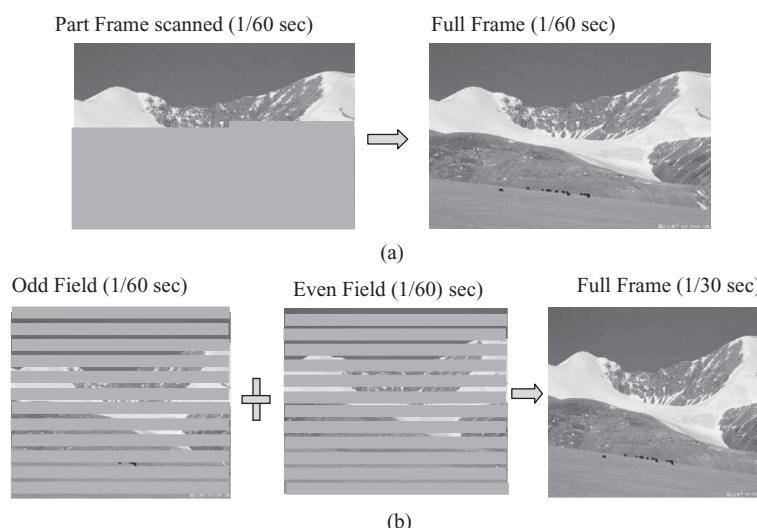


FIGURE 16.4

An example of progressive video and interlaced video. (a) An example of progressive video and (b) An example of interlaced video.

4:2:0 means 2:1 horizontal and 2:1 vertical downsampling. (Think 4 Y samples for every Cb and Cr samples in a scanline.)

Source input format (SIF): SIF has luminance resolution of 360×240 pixels per frame at 30 frames per second or 360×288 pixels per frame at 25 frames per second. For both cases, the resolution of the chrominance components is half of the luminance resolution in both horizontal and vertical dimensions. SIF can easily be obtained from a CCIR format using an appropriate anti-aliasing filter followed by subsampling.

Common intermediate format (CIF): CIF is a non-interlaced format. Its luminance resolution has 352×288 pixels per frame at 30 frame per second and the chrominance has half the luminance resolution in both vertical and horizontal dimensions. Since its line value, 288, represents half the active lines in the PAL television signal, and its picture rate, 30 frames/second, is the same as the NTSC television signal, it is a CIF for both PAL or PAL-like systems and NTSC systems. In the NTSC systems, only a line number conversion is needed, while in the PAL or PAL-like systems only a picture rate conversion is needed. For low-bit-rate applications, the quarter-SIF (QSIF) or quarter-CIF (QCIF) formats may be used since these formats have only a quarter number of pixels of SIF and CIF formats, respectively.

ATSC digital television (DTV) format: The concept of DTV consists of standard-definition television (SDTV) and HDTV. Recently, in the USA, the Federal Communication Commission (FCC) has approved the ATSC-recommended DTV standard (ATSC 1995). The DTV format is not included in the standard due to the divergent opinions of TV and computer manufacturers. Rather, it has been agreed that the picture format will be decided by the future market. The ATSC-recommended DTV formats including two kinds of formats: SDTV and HDTV. The ATSC DTV standard includes the following 18 formats:

For HDTV: 1920×1080 pixels at 23.976/24 Hz progressive scan, 29.97/30 Hz interlaced scan, and 59.94/60 Hz progressive scan; 1280×720 pixels at 24, 30, and 60 Hz progressive scan.

For SDTV: 704×480 pixels with 4:3 aspect ratio at 23.976/24 Hz, 29.97/30 Hz, 59.94/60 Hz progressive scan, 30 Hz interlaced scan; 704×480 pixels with 16:9 aspect ratio at 23.976/24 Hz, 29.97/30 Hz, 59.94/60 Hz progressive scan, 30 Hz interlaced scan; and 640×480 with 4:3 aspect ratio at 23.976/24 Hz, 29.97/30 Hz, 59.94/60 Hz progressive scan, 30 Hz interlaced scan.

It is noted that all HDTV formats use square pixels and only part of SDTV formats use square pixels. The number of pixels per line vs. the number of lines per frame is known as the aspect ratio.

Ultra HD: 4K UHD is a resolution of 3840×2160 pixels (8.3 megapixels, aspect ratio 16:9) and is one of the two resolutions of ultra-high-definition television (UHDTV) targeted towards consumer television, the other being 8K UHD, which is 7680×4320 lines (33.2 megapixels). 4K UHD has twice the horizontal and vertical resolution of the 1080p HDTV format, with four times as many pixels overall. Likewise, 4K UHD has three times the horizontal and vertical resolution of the 720p format, with nine times as many pixels overall (ITU 2012).

8K UHD is the current highest UHDTV resolution in DTV and digital cinematography. 8K refers to the horizontal resolution of 7,680 pixels, forming the total image dimensions of (7680×4320) . It is otherwise known as 4320p (Silva 2014) ([Figure 16.5](#)).



FIGURE 16.5

Resolution comparison. (https://en.wikipedia.org/wiki/8K_resolution.)

16.4 Current Status of Digital Video/Image Coding Standards

The fast growth of digital transmission services has generated a great deal of interest in the digital transmission of video signals. Since some digitized video source signals require very high bit rates, ranging from more than 100 Mbps for broadcast-quality video to more than 1 Gbps for HDTV signals, video compression algorithms that reduce the bit rates to an affordable level on practical communication channels are required. Digital video coding techniques have been investigated over several decades. There are two factors that make video compression possible: the statistical structure of the data in the video source and the psychophysical redundancy of human vision. Video compression algorithms can remove the spatial and temporal correlation that is normally present in the video source. In addition, human observers are subject to perceptual limitations in amplitude, spatial resolution, and temporal acuity. By proper design of the coding system it is possible to discard information without affecting perceived image quality, or at least, with only minimal degradation.

Several traditional techniques have been developed for image and video data compression. Recently, with advances in data compression and VLSI techniques, the data compression techniques have been extensively applied to video signal compression. Video compression techniques have been under development for over 20 years and have recently emerged as the core enabling technology for a new generation of DTV (both SDTV and HDTV) and multimedia applications. Digital video systems currently being implemented (or under active consideration) include terrestrial broadcasting of digital HDTV in the US (ATSC 1995), satellite Direct Broadcasting System (DBS) (Isnardi 1993), computer multimedia (ADA 1993), and video via packet networks (Verbiest and Pinnoo 1989). In response to the needs of these emerging markets for digital video, several national and worldwide standards activities have been started over the last few years. These organizations include International Standards Organization (ISO), International Telecommunication Union

(ITU, formally known as International Telegraph and Telephone Consultative Committee [CCITT]), Joint Photographic Experts Group (JPEG), and Moving Picture Experts Group (MPEG), as shown in [Table 16.1](#). The related standards include JPEG standards, MPEG-1,2,4, HEVC/H.265 standards, and H.261 and H.263 video teleconferencing coding standards, as shown in [Table 16.2](#). It should be noted that the JPEG standards are usually used for still image coding, but they can also be used to code video. Although the coding efficiency would be lowered, they have shown to be useful in some applications, e.g., studio editing systems. Though they are not video coding standards and were discussed in [Chapters 8 and 9](#), respectively, we include them here for completeness of all international image and video coding standards. Also, in this new edition, we add two more items; one is Alliance for Open Media (AOMedia) Video 1 (AV1) [av1] and another is versatile video

TABLE 16.1

List of Some Organizations for Standardization

| Organization | Full name of organization |
|--------------|---|
| ITU | International Telecommunication Union |
| JPEG | Joint Photographic Experts Group |
| MPEG | Moving Picture Experts Group |
| ISO | International Standards Organization |
| IEC | International Electrotechnical Commission |

TABLE 16.2

Video/Image Coding Standards

| Name | Completion Time | Major Features |
|-------------------------------|-------------------|---|
| JPEG | 1992 | For still image coding, DCT-based |
| JPEG-2000 | 2000 | For still image coding, DWT-based |
| H.261 | 1990 | For videoconferencing, 64Kbps–1.92 Mbps |
| MPEG-1 | 1991 | For CD-ROM, 1.5 Mbps |
| MPEG-2 (H.262) | 1994 | For DTV/DVD, 2–15 Mbps; for ATSC HDTV, 19.2 Mbps; most extensively used |
| H.263 | 1995 | For very-low-bit-rate coding, below 64Kbps |
| MPEG-4 Part 2 | 1999 | For multimedia, content-based coding, its simple profile and advanced simple profile is applied to Mobile Video and streaming |
| H.264/AVC (MPEG-4 Part 10) | 2005 | For many applications with significant improved coding performance over MPEG-2 and MPEG-4 part 2 |
| VC-1 | 2005 | For many applications, coding performance close to H.264 |
| RealVideo | 1997 | For many applications, coding performance similar to MPEG-4 part 2 |
| MPEG-7 | 2000 | Content description and indexing |
| MPEG-21 | 2002 | Multimedia framework |
| HEVC/H.265 | 2013 | A successor of H.264/AVC with significant coding performance improvement, it supports resolutions up to 8192×4320 , including 8K UHD |
| AV1 | 2015 | An open, royalty-free video codec designed for video transmissions over the Internet |
| VVC | Under development | The video coding standard beyond HEVC, it is developed by JVET and targets HDR, SDR, and 360° videos |

coding (VVC) [vvc], and both are in the stage of development. The AV1 targets open source and royalty-free video coding format and VVC is a new video coding standard beyond HEVC/H.265 (2015).

JPEG Standard: Since the mid-1980s, the ITU and ISO have been working together to develop a joint international standard for the compression of still images. Officially, JPEG (ISO/IEC IS 11544 1992) [jpeg] is the ISO/IEC international standard 10918-1, "Digital compression and coding of continuous-tone still images," or the ITU-T recommendation T.81. JPEG became an international standard in 1992. JPEG is a DCT-based coding algorithm. It continues to work on future enhancements, which may adopt wavelet-based algorithms.

JPEG-2000: JPEG-2000 [jpeg2000] is a new type of image coding system under development by JPEG for still image coding. JPEG-2000 is considering using the wavelet transform as its core technique. This is because the wavelet transform can provide not only excellent coding efficiency, but also wonderful spatial and quality scalable functionality. This standard is intended to meet a need for image compression with great flexibility and efficient interchangeability. It is also intended to offer unprecedented access into the image while still in compressed domain. Thus, an image can be accessed, manipulated, edited, transmitted, and stored in a compressed form.

MPEG-1: In 1988, ISO established MPEG to develop standards for the coded representation of moving pictures and associated audio information for digital storage applications. MPEG completed the first phase of its work in 1991. It is known as MPEG-1 (ISO/IEC JTC1 IS 11172 1992) or ISO standard 11172, "Coding of moving picture and associated audio." The target application for this specification is digital storage media at bit-rates up to about 1.5 Mbps.

MPEG-2: MPEG started its second phase of work, MPEG-2 (ISO/IEC JTC1 IS 13818 1994), in 1990. MPEG-2 is an extension of MPEG-1 that allows for greater input-format flexibility, higher data rate for SDTV or HDTV applications, and better error resilience. This work resulted in the ISO standard 13818 or ITU-T Recommendation H.262, "Generic coding of moving pictures and associated audio."

MPEG-4: Part 2 (ISO/IEC JTC1 FDIS 14496-2 1998). MPEG-4 Part 2 Visual standard has been approved in 1999. The MPEG-4 Part 2 Visual supports object-based coding technology and is intended to provide enabling technology for a variety of functionalities and multi-media applications:

- universal accessibility and robustness in error prone environments
- high interactive functionality
- coding of natural and synthetic data or both
- compression efficiency

H.261: H.261 [h261] was adopted in 1990 and the final revision was approved in 1993 by the ITU-T. It is designed for video teleconferencing and utilizes a DCT-based motion-compensation scheme. The target bit rates are from 64 Kbps to 1,920 Kbps.

H.263, H.263 Version 2 (H.263+), H.263++, and H.26L: The H.263 [h263] video coding standard is specifically designed for very-low-bit-rate applications such as video conferencing. Its technical content was completed in late 1995 and the standard was approved in early 1996. It is based on the H.261 standard with several added

features: unrestricted motion vectors, syntax-based arithmetic coding, advanced prediction, and PB-frames. The H.263 version 2 video coding standard, also known as "H.263+," was approved in January of 1998 by the ITU-T. H.263+ includes a number of new optional features based on the H.263. These new optional features are added in order to provide improved coding efficiency, a flexible video format, scalability, and backward-compatible supplemental enhancement information. H.263++ is the extension of H.263+ and is currently scheduled to be completed in the year 2000. H.26L is a long-term project that is looking for more efficient video coding algorithms. Finally, the activity of H.26L ended because the joint video coding team (JVT) of MPEG and ITU-T VCEG developed a new video coding standard H.264, which has greatly improved the coding efficiency over MPEG-2 and H.263.

MPEG-4 Part 10 Advanced Video Coding or H.264/AVC: In 2005, the JVT of MPEG and ITU-T VCEG developed video coding standard (ITU-T Rec. H.264 2005). Because many new tools have been used, H.264/AVC has achieved higher coding efficiency, which is almost twice better than MPEG-2. The detailed information will be introduced in [Chapter 20](#).

High-Efficiency Video Coding (HEVC) or H.265: HEVC, also known as H.265 and MPEG-H Part 2, was also been developed by the JVT in 2013 [H265]. It is a new video compression standard and one of several potential successors to the widely used AVC (H.264 or MPEG-4 Part 10). In comparison to H.264/AVC, HEVC offers about double the data compression ratio at the same level of video quality, or substantially improved video quality at the same bit rate. It supports resolutions up to 8192×4320 , including 8K UHD. The detailed information will be described in [Chapter 21](#).

VC-1: VC-1 is a video codec developed by Microsoft and late has been standardized by the Society of Motion Picture and Television Engineers (SMPTE). It is implemented by Microsoft as Windows Media Video (WMV) 9. Its coding performance is close to the H.264/AVC.

RealVideo: RealVideo is a video codec developed by RealNetWorks. It was first released in 1997 and its version 10 was released in 2006. RealVideo is supported on many platforms, including Windows, Mac, Linux, Solaris, and several mobile phones. Its coding performance is close to MPEG-4 Part 2.

AOMedia Video 1 (AV1): the target of AV1 video codec is to provide an open, royalty-free video coding format designed for video transmissions over the Internet. The AV1 codec is developed by the organization of AOMedia, a consortium of firms from the semiconductor industry, video on demand providers, and web browser developers. AOMedia was founded in 2015.

VVC: VVC is the video coding standard beyond HEVC. It is being developed by the Joint Video Experts Team (JVET) of MPEG and ITU. It will target the applications for HDR, SDR, and 360° videos.

The above organizations and standards are summarized in [Tables 16.1](#) and [16.2](#), respectively.

It should be noted that MPEG-7 (MPEG-7 Overview v.8 2002) and MPEG-21 (MPEG-21 Overview v.5 2002) in [Table 16.2](#) are not coding standards; MPEG-7 is a multimedia content description standard, which can be used for fast indexing and searching for

multimedia content; and the MPEG-21 is a multimedia framework, which aims at defining an open framework for multimedia applications. The VC-1 is an SMPTE standard and RealVideo is not an international standard, but it is extensively supported by many platforms.

It is also interesting to note that in terms of video compression methods, there is a growing convergence towards motion-compensated, interframe DCT algorithms represented by the video coding standards. However, wavelet-based coding techniques have found recent success in the compression of still image coding in both the JPEG-2000 and MPEG-4 standards. This is because it has unique features in terms of high coding efficiency and excellent spatial and quality scalability. The wavelet transform has not successfully been applied to video coding due to several difficulties. First, it is not clear how the temporal redundancy can be removed in this domain. Motion compensation is an effective technique for DCT-based video coding scheme; however, it is not so effective for wavelet-based video coding. This is because the wavelet transform uses large block size or full frame, but motion compensation is usually performed on a limited block size. This mismatch would reduce the inter-frame coding efficiency. Many engineers and researchers are working on these problems.

Among these standards, MPEG-2 has had a great impact on the consumer electronics industry since the digital video disk (DVD) and DTV have adopted it as core technology. However, recently developed new coding standards are attracting use in many applications. H.264/AVC has achieved higher coding efficiency, which is almost twice better than MPEG-2. The HEVC/H.265 has reached another milestone on coding efficiency; it is almost twice better than H.264/AVC.

16.5 Summary

In this chapter, the several fundamental issues of digital video coding have been presented. These include the representation and rate distortion function of digital video signals and the various video formats, which are widely used by the video industry. Finally, existing and emerging video coding standards have been briefly introduced.

Exercises

- 16.1 Suppose that we have a one-dimensional digital array (it can be extended to a two-dimensional array that may be an image), $f(i)=X_i$, ($i=0, 1, 2, \dots$). We use the first-order linear predictor to predict the current component value with the previous component, such as $X'_i=\alpha X_{i-1} + \beta$, where α and β are two parameters for this linear predictor. If we want to minimize the mean squared error of the prediction $E\{(X_i - X'_i)^2\}$, what α and β must we choose? Assume that $E\{X_i\}=m$, $E\{X_i^2\}=\sigma^2$ and $E\{X_i | X_{i-1}\}=\rho$, (for $i=0, 1, 2, \dots$), where m , σ , and ρ are constant.

- 16.2 To get a 128×128 or 256×256 digital image, write a program to use two 3×3 operators (Sobel operator) such as:

$$\begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \end{bmatrix}$$

to filter the image, separately. Discuss the resulting image. What will be the result if both of the operators are used?

- 16.3 The conversion of a 2-D array is defined as:

$$y(m, n) = \sum_{k=-\infty}^{+\infty} \sum_{l=-\infty}^{+\infty} x(k, l)h(m-k, n-l)$$

and

$$\bar{x} = \begin{bmatrix} 1 & 4 & 1 \\ 2 & 5 & 3 \end{bmatrix} \quad \bar{h} = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

Calculate the convolution $y(m, n)$. If $h(m, n)$ is changed to

$$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 4 & -1 \\ 0 & -1 & 0 \end{bmatrix},$$

recalculate $y(m, n)$.

- 16.4 The entropy of an image source is defined as

$$H = - \sum_{k=1}^M p_k \log_2 p_k,$$

under assumption that each pixel is an independent random variable. If the image is a binary image, i.e. $M = 2$, and the probability $p_1 + p_2 = 1$. If we define $p_1 = p$, then $p_2 = 1-p$, ($0 \leq p \leq 1$). The entropy can be rewritten as

$$H = -p \log_2 p - (1-p) \log_2 (1-p).$$

Find several digital binary images and compute their entropies. If one image has an almost equal number of zeros and ones and the other has a different number of zeros and ones, which image has larger entropy? Prove that the entropy of a binary source is maximum if the numbers of zeros and ones are equal.

- 16.5 A transformation defined as $y = f(x)$ is applied to a 256×256 digital image, where x is the original pixel value and y is the transformed pixel value. Obtain new images for (a) f is a linear function, (b) f is logarithm, and (c) f is a square function; compare the results; and indicate subjective differences of the resulting images. Repeat the experiments for different images and draw conclusions about possible use of this procedure in image processing applications.

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17

Digital Video Coding Standards—MPEG-1/2 Video

In this chapter, we introduce the ISO/IEC digital video coding standards, MPEG-1 [mpeg1] and MPEG-2 [mpeg2], which are extensively used in the video industry for television broadcast, visual communications, and multimedia applications.

17.1 Introduction

As we know, MPEG has successfully developed two standards, MPEG-1 and MPEG-2. The MPEG-1 video standard was completed in 1991 with the development of the ISO/IEC specification 11172 (ISO/IEC 11172 [1992]), which is the standard for coding of moving pictures and associated audio for digital storage media at up to about 1.5 Mbps. To support a wide range of application profiles, the user can specify a set of input parameters including flexible picture size and frame rate. MPEG-1 was developed for multimedia CD-ROM applications. Important features provided by MPEG-1 include frame-based random access of video, fast-forward/fast-reverse searches through compressed bit streams, reverse playback of video, and editability of the compressed bit stream. MPEG-2 is formally referred to as ISO/IEC specification 13818 (ISO/IEC 13818 [1995]), which is the second phase of MPEG video coding solution for applications not originally covered by the MPEG-1 standard. Specifically, MPEG-2 was developed to provide video quality not lower than NTSC/PAL and up to HDTV quality. The MPEG-2 standard was completed in 1994. Its target bit rates for NTSC/PAL are about 2–15 Mbps, and it is optimized at about 4 Mbps. The bit rates used for HDTV signals are about 19 Mbps. In general, MPEG-2 can be seen as a superset of the MPEG-1 coding standard and is backward compatible to MPEG-1 standard. In other words, every MPEG-2-compatible decoder is able to decode a compliant MPEG-1 bitstream.

In this chapter, we will briefly introduce the standard itself. Since many books and publications exist for the explanation of the standards (Haskell et al. 1997, Mitchell 1997), we will pay more attention to the utility of the standard, how the standard is used, and some interesting research topics that have emerged. In other words, the standards provide the knowledge for how to design the decoders that are able to successfully decode the compliant MPEG bitstreams. But the standards do not specify the means of generating these bitstreams. For instance, given some bit rate, how can one generate a bitstream that provides the best picture quality? To answer this, one needs to understand the encoding process, which is an informative part of standard (referred to as the test model), but it is very important for the content and service providers. In this chapter, the issues related to the encoding process are described. The main contents include the following topics: pre-processing, motion compensation, rate control, statistically multiplexing multiple programs, and optimal mode decision. Some of the sections contain the authors' own research results. These research results are useful in providing examples for the readers to understand how the standard is used.

17.2 Features of MPEG-1/2 Video Coding

It should be noted that MPEG-2 video coding has the feature of being backward compatible with MPEG-1. It turns out that most of the decoders in the market are MPEG-2-compliant decoders. For simplicity, we will start to introduce the technical detail of MPEG-1 and then describe the enhanced features of MPEG-2, which MPEG-1 does not have.

17.2.1 MPEG-1 Features

17.2.1.1 Introduction

The algorithms employed by MPEG-1 do not provide a lossless coding scheme. However, the standard can support a variety of input formats and be applied to a wide range of applications. As we know, the main purpose of MPEG-1 video is to code moving image sequences or video signals. To achieve a high compression ratio, both intra-frame redundancy and inter-frame redundancy should be exploited. This implies that it would not be efficient to code the video signal with an intra-frame-coding scheme, such as JPEG. On the other hand, to satisfy the requirement of random access, we have to use intra-frame coding from time to time. Therefore, the MPEG-1 video algorithm is mainly based on discrete cosine transform (DCT) coding and inter-frame motion compensation. The DCT coding is used to remove the intra-frame redundancy and the motion compensation is used to remove the inter-frame redundancy. With regard to input picture format, MPEG-1 allows progressive pictures only, but offers great flexibility in the size, up to 4095×4095 pixels. However, the coder itself is optimized to the extensively used video SIF picture format. The SIF is a simple derivative of the ITU-R 601 video format for digital television applications. According to ITU-R 601, a color video source has three components, a luminance component (Y) and two chrominance components (Cb and Cr), which are in the 4:2:0 sub-sampling format. Note that the 4:2:0 and 4:2:2 color formats were described in [Chapter 15](#).

17.2.1.2 Layered Structure Based on Group of Pictures

The MPEG coding algorithm uses a full-motion-compensated DCT and DPCM hybrid coding algorithm. In MPEG coding, the video sequence is first divided into groups of pictures or frames (GOP) as shown in [Figure 17.1](#). Each GOP may include three types of pictures or frames: Intra-coded (I) picture or frame, Predictive-coded (P) picture or frame, and Bi-directionally predictive-coded (B) picture or frame. I-pictures are coded by intra-frame techniques only, with no need for previous information. In other words, I-pictures are self-sufficient. They are used as anchors for forward and/or backward prediction. P-pictures are coded using one-directional motion-compensated prediction from a previous anchor frame, which could be either I or P-picture. The distance between two nearest I-frames is denoted by N , which is the size of GOP. The distance between two nearest anchor frames is denoted by M . Parameter N and M both are user-selectable parameters, which are selected during the encoding. Larger numbers of N and M will increase the coding performance but cause error propagation or drift. Usually, N is chosen from 12 to 15 and M from 1 to 3. If M is selected to be 1, this means no B-picture will be used. Lastly, B-pictures can be coded using predictions from either past or future anchor frames (I or P),

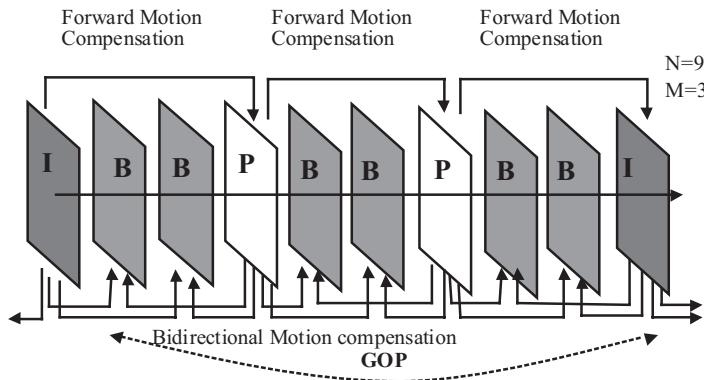


FIGURE 17.1
A GOP of video sequence in display order.

or both. Regardless of the type of frame, each frame may be divided into slices; each slice consists of several macroblocks (MBs). There is no rule to decide the slice size. A slice could contain all MBs in a row of a frame or all MBs of a frame. Smaller slice size is favorable for the purpose of error resilience but will decrease coding performance due to higher overhead. A MB contains a 16×16 Y component and spatially corresponding 8×8 Cb and Cr components. A MB has four luminance blocks and two chrominance blocks (for 4:2:0 sampling format) and the MB is also the basic unit of adaptive quantization and motion compensation. Each block contains 8×8 pixels over which the DCT operation is performed.

In order to exploit the temporal redundancy in the video sequence, the motion vector for each MB is estimated from two original luminance pictures using a block-matching algorithm. The criterion for the best match between the current MB and a MB in the anchor frame is the minimum mean absolute error. Once the motion vector for each MB is estimated, pixel values for the target MB can be predicted from the previously decoded frame. All MBs in I-frame are coded in intra mode with no motion compensation. MBs in P and B-frames can be coded in several modes. Among the modes are intra-coded and inter-coded with motion compensation. This decision is made by mode selection. Most encoders depend on the values of predicted differences to make this decision. Within each slice, the values of motion vectors and DC values of each MB are coded using DPCM. The detailed specifications of this coding can be found in the document proposed by the MPEG video committee [mpeg2]. The structure of MPEG implies that if an error occurs within I frames of data; it will be propagated through all frames in the GOP. Similarly, an error in a P-frame will affect the related P and B frames, while B-frame errors will be isolated.

17.2.1.3 Encoder Structure

The typical MPEG-1 video encoder structure is shown in Figures 17.2 and 17.3. It should be noted that when B-picture is used as shown in Figure 17.1, two frame memories are needed for bi-directionally prediction. Since the encoding order is different from the display order, the input sequence has to be reordered for encoding. For example, if we choose the GOP size (N) to be 12 and the distance between two nearest anchor frames (M) to be 3, the display order and encoding order are shown as in Table 17.1.

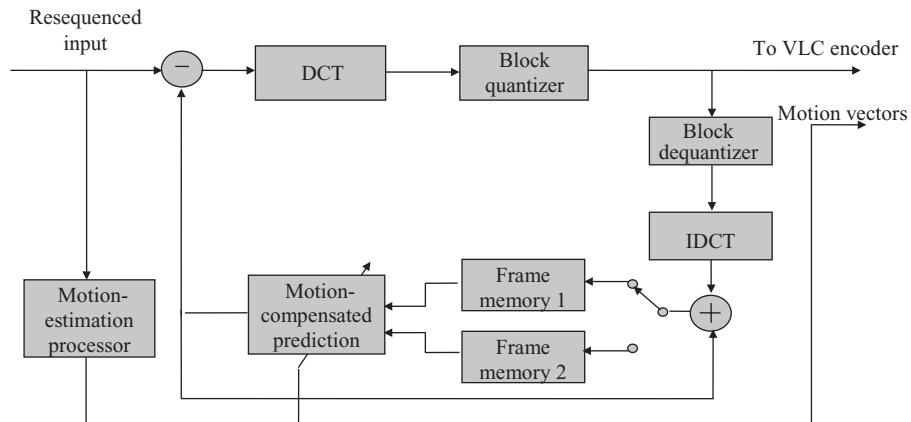


FIGURE 17.2
Typical MPEG-1 encoder structure.



FIGURE 17.3
Half-pixel locations in motion compensation.

TABLE 17.1
Display Order and Encoding Order

| Display Order | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|----------------|---|---|---|---|---|---|---|---|---|---|----|----|----|
| Encoding order | 0 | 3 | 1 | 2 | 6 | 4 | 5 | 9 | 7 | 8 | 12 | 10 | 11 |
| Coding type | I | P | B | B | P | B | B | P | B | B | I | B | B |

It should be noted that in the encoding order or in the bitstream the first frame in a GOP is always an I-picture. In the display order the first frame can be either I-picture or the first B-picture of the consecutive series of B-pictures that immediately precedes the first I-picture, and the last picture in a GOP is an anchor picture, either I or P-picture. The first GOP always starts with an I-picture and as consequence this GOP will have less B-pictures than the other GOPs.

The MPEG-1 video compression technique uses motion compensation to remove the inter-frame redundancy. The concept of motion compensation is based on the estimation of motion between video frames. The fundamental model that is used assumes that a translational motion can approximate the motion of a block. If all elements in a video scene are approximately spatially displaced, the motion between frames can be described by a limited number of motion parameters. In other words, the motion can be described by motion vectors for translatory motion of pixels. Since the spatial correlation between adjacent pixels is usually very high, it is not necessary to transmit motion information for each coded image pixel. This would be too expensive and the coder would never be able to reach a high compression ratio. The MPEG video uses the MB structure for motion

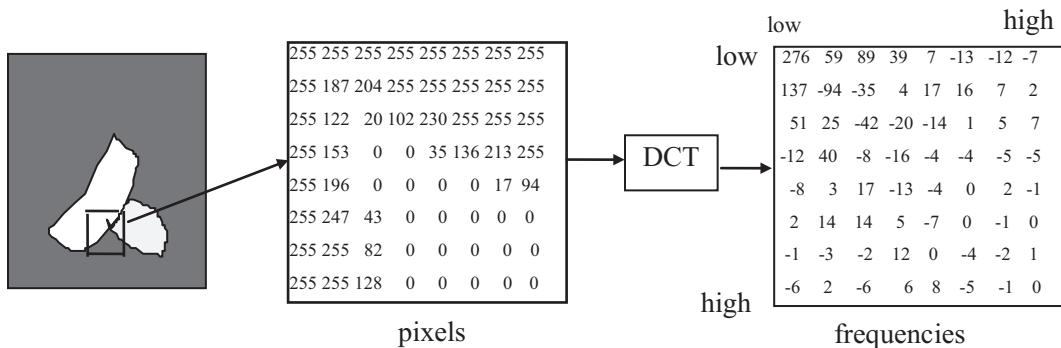


FIGURE 17.4
Example of 8×8 DCT.

compensation, i.e., for each 16×16 MB only one or sometimes two motion vectors are transmitted. The motion vectors for any block are found within a search window that can be up to 512 pixels in each direction. Also, the matching can be done at half-pixel accuracy, where the half-pixel values are computed by averaging the full-pixel values.

For inter-frame coding, the prediction differences or error images are coded and transmitted with motion information. A two-dimensional DCT is used for coding both the intra-frame pixels and predictive error pixels. The image to be coded is first partitioned into 8×8 blocks. Each 8×8 -pixel block is then subject to an 8×8 DCT, resulting in a frequency domain representation of the block as shown in the [Figure 17.4](#).

The goal of the transformation is to decorrelate the block data so that the resulting transform coefficients can be coded more efficiently. The transform coefficients are then quantized. During the process of quantization, a weighted quantization matrix is used. The function of the quantization matrix is to quantize high frequencies with coarser quantization steps that will suppress high frequencies with no subjective degradation, thus taking advantage of human visual perception characteristics. The bits saved for coding high frequencies are used for lower frequencies to obtain better subjectively coded images. There are two quantizer weighting matrices in Test Model 5 (TM5) (MPEG-2 Test model 5 [1993]), an intra quantizer weighting matrix and a non-intra quantizer weighting matrix; the latter is flatter since the energy of coefficients in inter-frame coding is more uniformly distributed than in intra-frame coding.

In intra MBs, the DC value, dc , is an 11-bit value before quantization and it will be quantized to 8, 9, or 10 bits according to the setting of parameter. Thus, the quantized DC value, QDC , is calculated as:

$$QDC(8\text{bit}) = dc//8, QDC(9\text{bit}) = dc//4, \text{ or } QDC(10\text{bit}) = dc//2 \quad (17.1)$$

where symbol//means integer division with rounding to the nearest integer and the half integer values are rounded away for zero unless otherwise specified. The AC coefficients, $ac(i, j)$, are first quantized by individual quantization factors to the value of $ac\sim(i, j)$:

$$ac\sim(i, j) = (16*ac(i, j))//W_1(i, j) \quad (17.2)$$

where $W_1(i, j)$ is the element at the (i, j) position in the intra quantizer weighting matrix shown in [Figure 17.5](#).

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| 8 | 16 | 19 | 22 | 26 | 27 | 29 | 34 |
| 16 | 16 | 22 | 24 | 27 | 29 | 34 | 37 |
| 19 | 22 | 26 | 27 | 29 | 34 | 34 | 38 |
| 22 | 22 | 26 | 27 | 29 | 34 | 37 | 40 |
| 22 | 26 | 27 | 29 | 32 | 35 | 40 | 48 |
| 26 | 27 | 29 | 32 | 35 | 40 | 48 | 58 |
| 26 | 27 | 29 | 34 | 38 | 46 | 56 | 69 |
| 27 | 29 | 35 | 38 | 46 | 56 | 69 | 83 |

(a)

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |
| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |
| 19 | 20 | 21 | 22 | 23 | 24 | 26 | 27 |
| 20 | 21 | 22 | 23 | 25 | 26 | 27 | 28 |
| 21 | 22 | 23 | 24 | 26 | 27 | 28 | 30 |
| 22 | 23 | 24 | 26 | 27 | 28 | 30 | 31 |
| 23 | 24 | 25 | 27 | 28 | 30 | 31 | 33 |

(b)

FIGURE 17.5
Quantizer matrices for (a) Intra and (b) Non-intra coding

The quantized level $QAC(i, j)$ is given by

$$QAC(i, j) = [ac\sim(i, j) + \text{sign}(ac\sim(i, j))^*((p^*mquant)/q)]/(2*mquant) \quad (17.3)$$

where $mquant$ is the quantizer scale or step that is derived for each MB by rate control algorithm, and $p = 3$ and $q = 4$ in TM5 (MPEG-2 Test model 5 [1993]). For non intra MBs,

$$ac\sim(i, j) = (16^*ac(i, j))//W_N(i, j) \quad (17.4)$$

where $W_N(i, j)$ is non intra quantizer weighting matrix in Figure 17.5 and

$$QAC(i, j) = ac\sim(i, j)/(2^*mquant) \quad (17.5)$$

An example of encoding an intra block is shown in Figure 17.6.

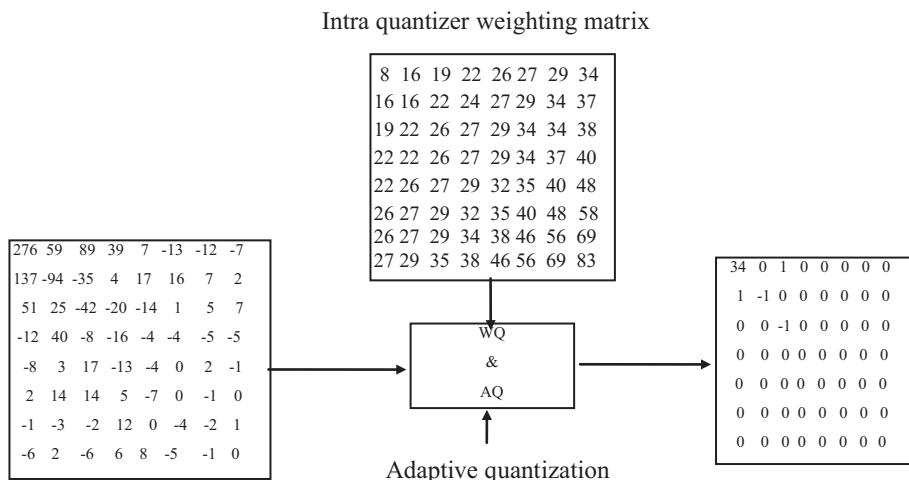
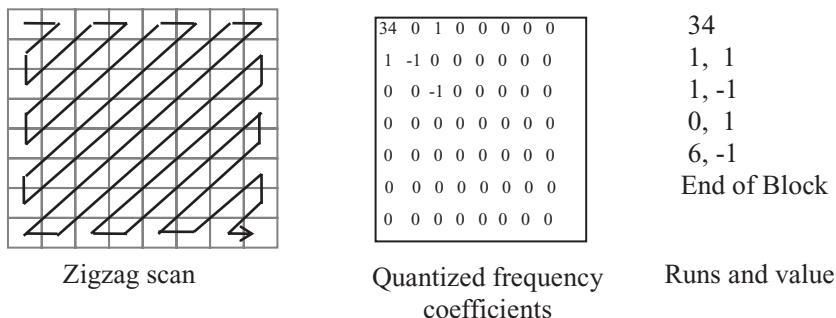


FIGURE 17.6
An example of coding an intra block.

**FIGURE 17.7**

Zigzag scans to get pairs of zero-runs and value.

The coefficients are processed in zigzag order since the most energy is usually concentrated in the lower-order coefficients. The zigzag ordering of elements in an 8×8 matrix allows for a more efficient run-length coder. This is illustrated in [Figure 17.7](#).

With the zigzag order, the run length coder converts the quantized frequency coefficients to pairs of zero runs and non-zero coefficients:

34 0 1 0 -1 1 0 0 0 0 0 0 -1 0 0 0 0 ...

After parsing, we obtain the pairs of zero runs and values:

34 | 0 1 | 0 -1 | 1 | 0 0 0 0 0 -1 | 0 0 0 0 ...

These pairs of runs and values are then coded by a Huffman type entropy coder. For example, the above run/value pairs are:

| Run/Value | VLC (Variable length code) |
|--------------|----------------------------|
| 34 | |
| 1, 1 | 0110 |
| 1, -1 | 0111 |
| 0, 1 | 110 |
| 6, -1 | 0001011 |
| End of Block | 10 |

The VLC tables are obtained by statistically optimizing a large number of training video sequences and are included in the MPEG-2 specification. The same idea is applied to code the DC values, motion vectors, and other information. Therefore, the MPEG video standard contains a number of VLC tables.

17.2.1.4 Structure of the Compressed Bitstream

After coding, all the information is converted to binary bits. The MPEG video bitstream consists of several well-defined layers with headers and data fields. These layers include sequence, GOP, picture, slice, MB, and block. The important syntax elements contained in

each layer can be summarized in [Table 17.2](#). The typical structure of the MPEG-1 video-compressed bitstream is shown in the [Figure 17.8](#). The syntax elements contained in the headers and the number of bits defined for each element can be found in the standard.

For picture layer, a frame of picture is first partitioned into MBs (16×16 for luminance and 8×8 for chrominance in the 4:2:0 color representation). The compressed bitstream structure at this layer is shown in Figure 17.9. It is important to note that most elements in the syntax are coded by variable-length code. The tables of these variable-run-length codes are obtained through the simulation of a large number of training video sequences.

TABLE 17.2
Summary of Important Syntax of Each Layer

| Name of Layer | Important Syntax Elements |
|---------------|--|
| Sequence | Picture size and frame rate |
| | Bit rate and buffering requirement |
| | Programmable coding parameters |
| GOP | Random access unit |
| | Time code |
| Picture | Timing information (buffer fullness, temporal reference) |
| | Coding type (I, P, or B) |
| Slice | Intra-frame addressing information |
| | Coding re-initialization (error resilience) |
| MB | Basic coding structure |
| | Coding mode |
| | Motion vectors |
| | Quantization |
| Block | DCT coefficients |

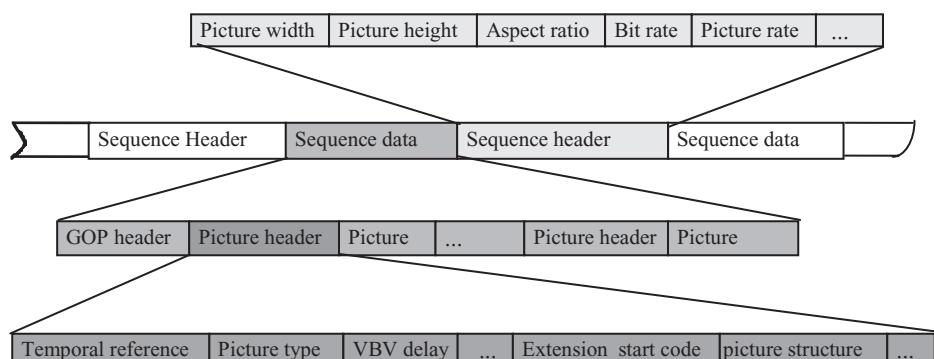


FIGURE 17.8
Description of layered structure of compressed bitstream.

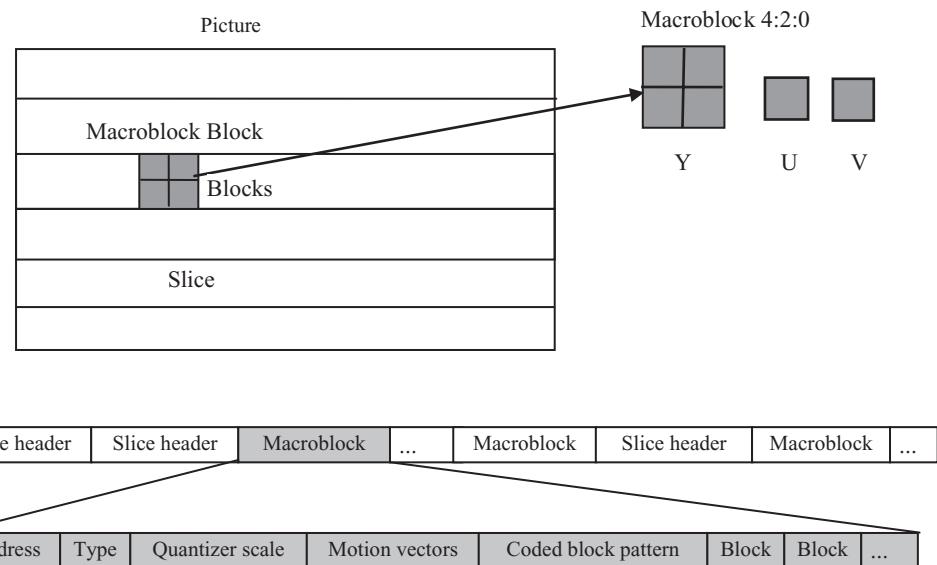


FIGURE 17.9
Picture layer data structure.

17.2.1.5 Decoding Process

The decoding process is an inverse procedure of encoding. The block diagram of a typical decoder is shown in [Figure 17.10](#).

The variable-length decoder (VLD) first decodes the coded data or video bitstream. This process yields the quantized DCT coefficients and motion-vector data for each MB. The coefficients are inversely scanned and de-quantized. The decoded DCT coefficients are then inverse-transformed to obtain the spatial-domain pixels. If the MB was intra-coded, these pixels represent the reconstructed values, without any further processing. However, if the MB is inter-coded, then motion compensation is performed to add the prediction from the corresponding reference frame or frames.

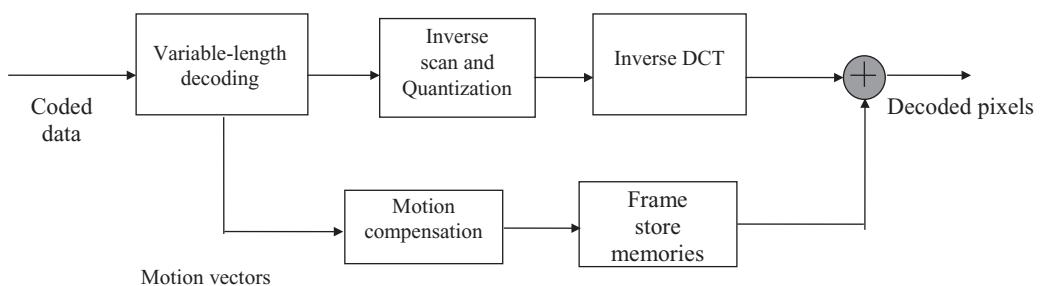


FIGURE 17.10
Simplified MPEG video decoder.

17.2.2 MPEG-2 Enhancements

The basic coding structure of MPEG-2 video is the same as that of MPEG-1 video, that is, intra-frame and inter-frame DCT with I-, P-, and B-pictures. The most important features of MPEG-2 video coding include:

- Field/frame prediction modes for supporting the interlaced video input
- Field/frame DCT coding syntax
- Downloadable quantization matrix and alternative scan order
- Scalability extension

The above enhancement items are all coding performance improvements that are related to the support of interlaced material. There are also several non-compression enhancements, which include:

- Syntax to facilitate 3:2 pull-down in the decoder
- Pan and scan codes with 1/16-pixel resolution
- Display flags indicating chromaticity, subcarrier amplitude, and phase (for NTSC/PAL/SECAM source material)

In the following, each of these enhancements is introduced.

17.2.2.1 Field/Frame-Prediction Mode

In MPEG-1 video, we always code each picture as a frame structure, whether the original material is progressive or interlaced. If the original sequence is interlaced, each frame consists of two fields: top field and bottom field as shown in [Figure 17.11](#). We still can use frame-based prediction if we consider that the two fields as a frame such as shown in [Figure 17.11](#).

In [Figure 17.11](#), three frames are coded as I, B, and P –frames and each frame consists of two fields. The P-frame is predicted with the I-frame with one motion vector. The B-frame can be predicted only with I-frame (forward prediction), only with P-frame (backward prediction), or from both I and P-picture (bi-directional prediction); the forward and backward prediction needs only one motion vector and the bi-directional prediction needs two motion vectors.

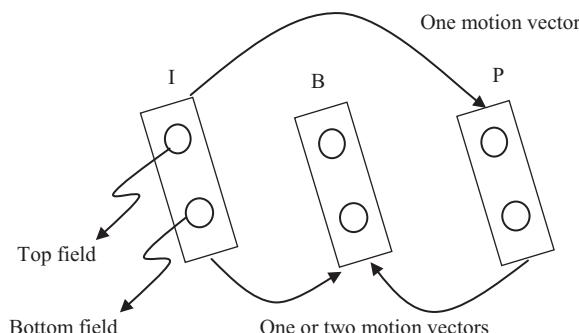


FIGURE 17.11

Frame-based prediction of MPEG-1 video coding.

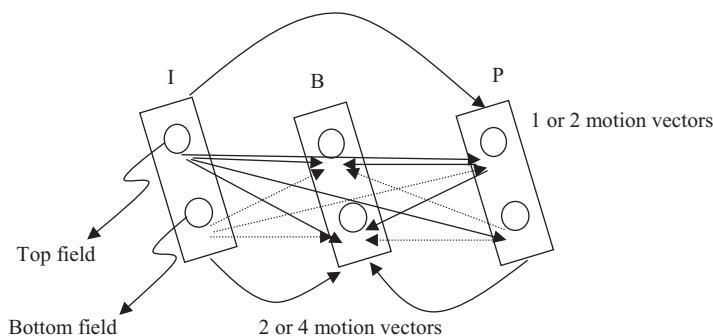


FIGURE 17.12
Field-based prediction of enhanced option of MPEG-2 video coding.

MPEG-2 video provides an enhanced prediction mode to support interlaced material, which uses the adaptive field/frame selection, based on the best-match criteria. Each frame consists of two fields: top field and bottom field. Each field can be predicted from either field of the previous anchor frame. The possible prediction modes are shown in [Figure 17.12](#).

In a field-based prediction, the top field of the current frame can be either predicted from the top field or the bottom field of an anchor frame as shown in [Figure 17.12](#). The solid arrow represents the prediction from the top field and the dashed arrow represents the prediction from the bottom field. The same is also true for bottom field of the current frame. If the current frame is a P-frame, there could be up to two motion vectors used to make the prediction (one for top field and one for bottom field); if the current frame is a B-frame, there could be up to four motion vectors (each field could be bi-directional prediction, which needs two motion vectors). At the MB level of MPEG-2, several coding modes are added to support these new field-based predictions. Additionally, there is another new prediction mode supported by the MPEG-2 syntax. This is the special prediction mode, referred to as dual-prime prediction. The basic idea of dual-prime prediction is to code a set of field motion vectors with a scaling to a near or far field, plus a transmitted delta vector. Due to the correlation of adjacent pixels, the dual-prime coding of field vectors can save the number of bits used for field motion vectors. The dual prime prediction is shown in the [Figure 17.13](#). In [Figure 17.13](#), one field motion vector and the delta motion vector are transmitted, the motion vectors for other field are derived from the above two vectors.

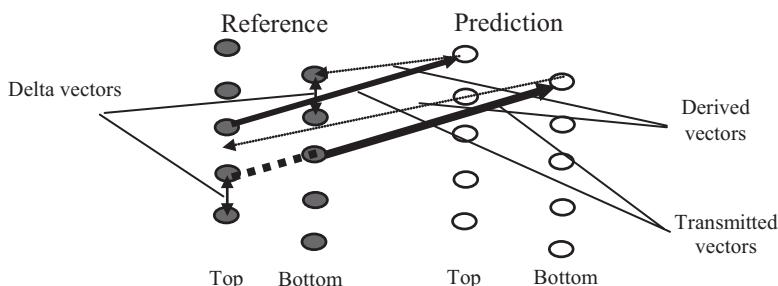


FIGURE 17.13
Dual prime prediction in MPEG-2 video coding.

It should be noted that only the P-picture is allowed to use dual prime prediction. In other words, if the dual prime prediction is used in the encoder, there will be no B-pictures. The reason for this restriction is to limit the required memory bandwidth for a real system implementation.

17.2.2.2 Field/Frame DCT Coding Syntax

Another important feature to support interlaced material is to allow adaptive selection of the field/frame DCT coding as shown in [Figure 17.14](#).

In [Figure 17.14](#), the middle is a luminance MB of 16×16 pixels, the black rectangular represents the eight pixels in the top field, and the white rectangular represents the eight pixels in the bottom field. The left is the field DCT in which each 8×8 block contains only the pixels from the same field. The right is the frame DCT in which each 8×8 block contains the pixels from both top field and bottom field.

At the MB level for interlaced video, the field-type DCT may be selected when the video scene contains less detail and experiences large motion. Since the difference between adjacent fields may be large when there is large motion between fields, it may be more efficient to group the fields together, rather than the frames. In this way, the possibility that there exists more correlation among the fields can be exploited. Ultimately, this can provide much more efficient coding since the block data is represented with fewer coefficients, especially if there is not much detail contained in the scene.

17.2.2.3 Downloadable Quantization Matrix and Alternative Scan Order

The new feature in MPEG-2 regarding the quantization matrix is that it can be downloaded for every frame. This may be helpful if the input video characteristics are very dynamic. In general, the quantizer matrices are different for intra coding and non-intra coding. With 4:2:0 format, only two matrices are used, one for the intra blocks and another for the non-intra blocks. With 4:2:2 or 4:4:4 formats four matrices are used; both an intra and a non-intra matrix are used for the luminance and chrominance blocks. If the matrix load flags are not set, the decoder will use default matrices. The formats 4:2:0, 4:2:2 are defined in [Chapter 15](#). In the 4:4:4 format, the luminance and two chrominance pictures have the same picture size.

In the picture layer, there is a flag that can be set for an alternative scan of DCT blocks, instead of using the zigzag scan discussed earlier. Depending on the spectral

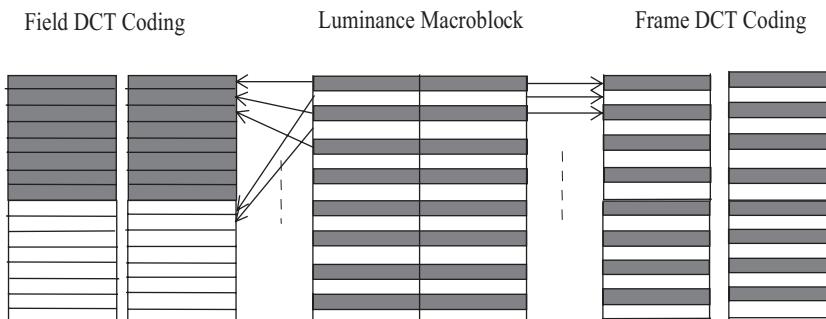
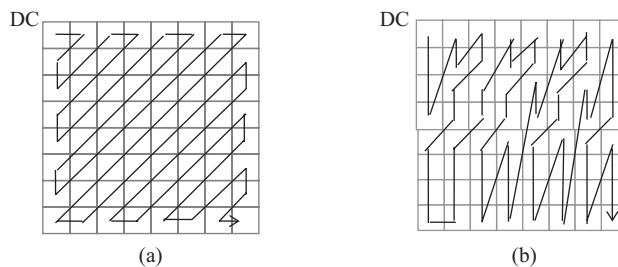


FIGURE 17.14

Frame and field DCT for interlaced video.

**FIGURE 17.15**

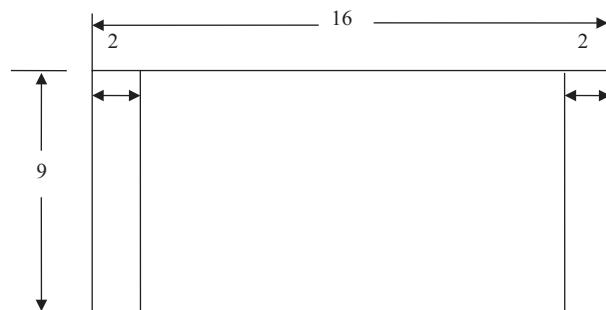
Two zigzag scan methods for MPEG-2 video coding (a) Normal scan order and (b) Alternative scan order.

distribution, the alternative scan can yield run lengths that better exploit the multitude of zero coefficients. The zigzag scan and alternative scan are shown in the following (Figure 17.15):

The normal zigzag scan is used for MPEG-1 and as an option for MPEG-2. The alternative scan is not supported by MPEG-1 and is an option for MPEG-2. For frame-type DCT of interlaced video, more energy may exist at the bottom part of the block, so the run length coding may be better off with the alternative scan.

17.2.2.4 Pan and Scan

In MPEG-2, there are several parameters defined in the sequence display extension and picture display extension for panning a displaying a rectangle around a reconstructed frame. These parameters include display-horizontal-size and display-vertical-size in the sequence display extension, and frame-center-horizontal-offset and frame-center-vertical-offset in the picture display extension. The function of these parameters can be found in the MPEG-2 system specification. A typical example to use pan-scan parameters is the conversion of 16:9 frame to 4:3 frame. The 4:3 region is defined by display-horizontal-size and display-vertical-size and the 16:9 frame is defined by horizontal-size and vertical-size. If we choose the display-horizontal-size to be four pixels less than the horizontal-size, and keep the display-vertical-size the same as the vertical-size, then we can obtain a 4:3 pictures on the display. Figure 17.16 shows the conversion of 16:9 to the 4:3 frame using pan-scan parameter, but there is no center offset involved in this example.

**FIGURE 17.16**

An example of Pan-Scan.

17.2.2.5 Concealment Motion Vector

The concealment motion vector (CMV) is a new tool supported by MPEG-2. This tool is useful in concealing errors in the noisy channel environment where the transmitted data may be lost or corrupted. The basic idea of CMV is that the motion vectors are sent for the intra-coded MB. These motion vectors are referred to as CMV, which should be used in MBs immediately below the one in which the CMV occurs. The details are described in the [Section 17.5.3.2](#).

17.2.2.6 Scalability

MPEG-2 video has several scalable modes, which includes Spatial scalability, Temporal scalability, SNR scalability, and Data partitioning. These scalability tools allow a subset of any bitstream to be decoded into meaningful imagery. Moreover, scalability is a useful tool for error resilience on prioritized transmission media. The drawback of scalability is that some coding efficiency is lost due to extra overhead. Here, we briefly introduce the basic notions of the above scalability features.

Spatial scalability allows multi-resolution coding, which is suitable for video service inter-networking applications. In spatial scalability, a single video source is split into a base layer (lower spatial resolution) and enhancement layers (higher spatial resolution). For example, an ITU-R 601 video can be down-sampled to SIF format with spatial filtering, which can serve as the base layer video. The base layer or low-resolution video can be coded with MPEG-1 or MPEG-2, and the higher resolution layer must be coded by MPEG-2 supported syntax. For the up-sampled lower layer, an additional prediction mode is available in the MPEG-2 encoder. This is a flexible technique in terms of bit-rate ratios, and the enhancement layer can be used in high-quality service. The problem with spatial scalability is that there exists some bit-rate penalty due to overhead and there is also a moderate increase in complexity. A block diagram that illustrates encoding with spatial scalability is shown in [Figure 17.17](#). In [Figure 17.17](#), the output of decoding and spatial upsampling block provides an additional choice of prediction for the MPEG-2-compatible coder, but not the only choice of prediction. The prediction can be obtained from HDTV input itself also depending on the prediction select criterion such as the minimum prediction difference.

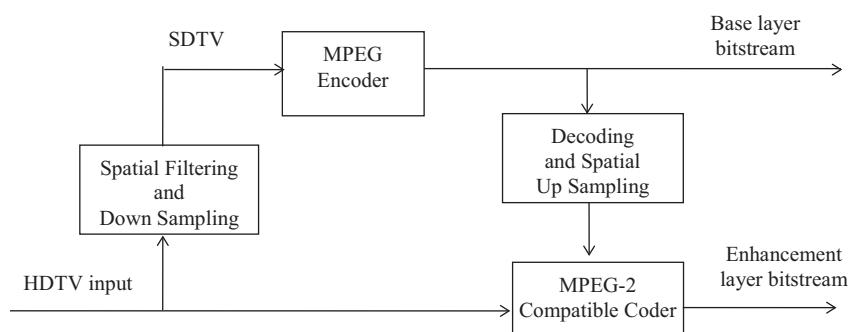


FIGURE 17.17

Block diagram of spatial scalability encoder.

It should be noted that the spatial scalability coding allows the base layer to be coded independently from the enhancement layer. In other words, the base layer or lower layer bitstream is generated without regard for the enhancement layer and can be decoded independently. The enhancement layer bitstream is additional information, which can be seen as the prediction error based on the base layer data. This implies that the enhancement layer is useless without the base. However, this type of structure can find a lot of applications such as error concealment, which will be discussed in [Section 17.5](#).

Temporal scalability is a scalable coding technique in the temporal domain. An example of a two-layer temporal scalable coder is shown in [Figure 17.18](#). The example uses temporal scalability to decompose the progressive image sequence to two interlaced image sequences, and then one is coded as the base layer and one as the enhancement layer. Of course, the decomposition could be different. For the enhancement layer, there is a choice of making predictions. One choice for prediction is available between one base layer prediction and a temporal prediction from the enhancement layer itself. It should be noted that the spatial resolution of two layers is the same and the combined temporal rate of two layers is the full temporal rate of the source. Again, it should be noted that the decoding output of base layer bitstream by the MPEG decoder provides an additional choice of prediction but not the only choice of predictions.

The SNR scalability provides a mechanism for transmitting two-layer service with the same spatial resolution but different quality levels. The low layer is coded at a coarse quantization step at 3–5 Mbps to provide NTSC/PAL/SECAM-quality video for low-capacity channels. In the enhancement layer, the difference between original and coarse quantized signals is then coded with a finer quantizer to generate an enhancement bitstream for high-quality video applications.

The above three scalability schemes all generate at least two bitstreams, one for the base-layer and another for the enhancement layer; the lower layer bitstream can be independently decoded to provide low spatial resolution, low quality, or low frame rate video, respectively. There is another scalability scheme, data partitioning, in which the base layer bitstream cannot be independently decoded. In data partitioning, a single video source is split into a high-priority portion, which can be better protected, and low priority portion, which is less important with regard to the reconstructed video quality. The priority breakpoint in the syntax specifies which syntax elements are coded as low priority (for example, the higher-order DCT coefficients in the inter-coded blocks).

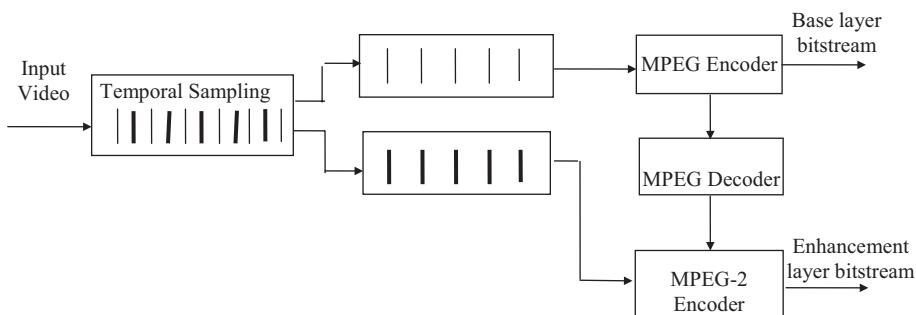


FIGURE 17.18

Block diagram of temporal scalability encoder.

17.3 MPEG-2 Video Encoding

17.3.1 Introduction

MPEG video compression is a generic standard that is essential for the growth of the digital video industry, as mentioned previously. Although the MPEG video coding standard recommended a general coding methodology and syntax for the creation of a legitimate MPEG bitstream, there are many areas of research left open regarding how to generate high-quality MPEG bitstreams. This allows the designers of an MPEG encoder great flexibility in developing and implementing their own MPEG-specific algorithms, leading to product differentiation on the marketplace. In order to design a performance-optimized MPEG-2 encoder system, several major areas of research have to be considered. These include image pre-processing, motion estimation, coding mode decisions, and rate control. Algorithms for all of these areas in an encoder should aim to minimize subjective distortion for a prescribed bit rate and operating delay constraint. The pre-processing includes the noise reduction and the removal of redundant fields, which are contained in the detelecine material. The telecine material is used for the movie industry, which contains 24 progressive frames/second. The TV signal is 30 frames/second. The detelecine process converts the 24 frames/second film signal to the 30 frames/second TV signal. This is also referred to as 3:2 pull-down process. Since the 30-frames/second detelecine material only contains 24 frames/second of unique pictures, the encoder has to detect and remove the redundant fields to obtain better coding performance. The procession of noise reduction can reduce the bits wasted for coding random noise. Motion compensation is used to remove the temporal redundancy in the video signals. The motion vectors between the anchor picture and the current picture are obtained with motion-estimation algorithms. Except for I-pictures, each MB can be inter-or intra-coded, which is determined by the mode decision. The investigation of motion estimation algorithms is an important research topic since different motion estimation schemes may result in different coding efficiency. Rate control is always applied for non-variable bit rate (non-VBR) coding. The purpose of rate control is to properly assign the bits for each MB under the constraints of total bit rate budget and buffer size. This is also an important topic since the optimized bit assignment scheme will result in better coding performance and better subjective reconstruct quality at a given bit rate. In this section, areas of pre-processing and motion estimation are covered. The topics of rate control and optimum mode decision are discussed in later sections.

17.3.2 Pre-processing

For low-bit-rate video coding, pre-processing is sometimes applied to the video signals before coding in order to increase the coding efficiency. Usually the pre-processing implies a filtering of the video signals that are corrupted by random and burst noise for various reasons, such as imperfections of the scanner, transmission, or recording medium. Noise reduction not only improves the visual quality but also increases the performance of video coding. Noise reduction can be achieved by filtering each frame independently. There are a variety of spatial filters that have been developed for image noise filtering and restoration that can be used for noise-reduction tasks (Cano and Benard 1983, Katsaggelos 1991). On the other hand, it is also possible to filter the video sequence temporally along the motion trajectories using motion compensation (Sezan 1991). However, it was shown that among the recursive stationary methods the motion-compensated spatio-temporal filtering performed better than spatial- or motion-compensated temporal filtering alone (Ozkan 1993).

Another important pre-processing is detelecine processing. Since movie material is originally shot at 24 progressive frames/second, standard conversion to television at 30 frames/second is made by a 3:2 pull-down process, which periodically inserts repeated field, giving 30 frames/second telecine source material. Since the 30 frames/second detelecine material only contains 24 frames/second of unique pictures, it is necessary to detect and remove the redundant fields before or during encoding. Rather than directly encoding the 30 frames/second detelecine material, one can remove the redundant fields first and then encode 24 frames/second of unique material, thereby realizing higher coding quality at the same bit rate. The decoder can simply reconstruct the redundant fields before presenting them. Examples of telecine and detelecine process are shown in [Figure 17.19](#).

Television broadcast programmers frequently switch between telecine material and natural 30 frames/second material, such as when splicing to and from various sources of movies, ordinary television programs, and commercials. An MPEG-2 encoder should be able to cope with these transitions and consistently produce decent pictures. During movie segments, the encoder should realize the gains from coding at the lower frame rate after detelecine. Ideally, the process of source transition from the lower 24 frames/second rate to the higher 30 frames/second rate should not cause any quality drop of every encoded frame. The quality of encoded frames should maintain the same as the case where the detelecine process is ignored and all material, regardless of source type, is coded at 30 frames/second.

17.3.3 Motion Estimation and Motion Compensation

In principle, for coding video signals if the motion trajectory of each pixel could be measured, then only the initial or anchor reference frame and the motion vector information need to be coded. In such a way, the inter-frame redundancy will be removed. To reproduce the pictures, one can simply propagate each pixel along its motion trajectory. Since there is also a cost for transmitting motion vector information, in practice, one can only measure the motion vectors of a group of pixels, which will share the cost for transmission of the motion information. Of course, at the same time the pixels in the same group are assumed to have the same motion information. This is not always true since the pixels in the block may move in different directions, or some of them belong to the background. Therefore, both motion vectors and the prediction difference have to be transmitted. Usually, the block matching

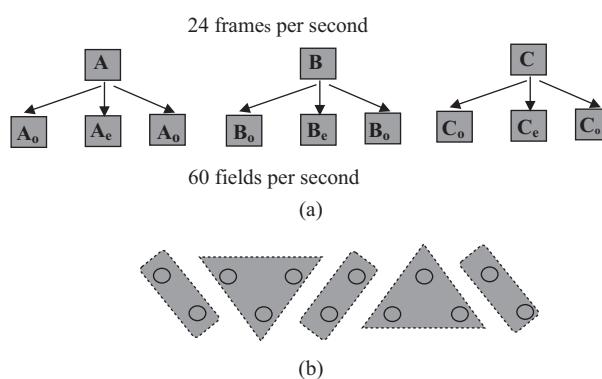


FIGURE 17.19

Examples of telecine and detelecine process (a) Example of telecine process and (b) Example of detelecine process.

can be considered as the most practical method for motion estimation due to less hardware complexity. In the block-matching method, the image frame is divided into fixed-size small rectangular blocks such as 16×16 or 16×8 in MPEG video coding. Each block is assumed to undergo a linear translation and the displacement vector of each block and the predictive errors are coded and transmitted. The related issues for motion estimation and compensation include motion-vector-searching algorithm, searching range, matching criteria, and coding method. Although the matching criteria and searching algorithms have been discussed in [Chapter 11](#), we still briefly introduce them here for the sake of completeness.

17.3.3.1 Matching Criterion

The matching of the blocks can be determined according the various criteria including the maximum cross-correlation, the minimum mean square error (*MSE*), the minimum mean absolute difference (*MAD*) and maximum matching pixel count (*MPC*). For *MSE* and *MAD*, the best matching block is reached if the *MSE* or *MAD* is minimized at that location. In practice, we use *MAD* instead of *MSE* as matching criterion due to its computational simplicity. The minimum *MSE* criterion is not commonly used in hardware implementations because it is difficult to realize the square operation. However, the performance of the *MAD* criterion deteriorates as the search area becomes larger due to the presence of several local minima. In the maximum *MPC* criterion, each pixel is the block is classified as either a matching pixel or a mismatching pixel according to if the difference is smaller than a preset threshold. The best matching is then determined by the maximum number of the matching pixels. However, the *MPC* criterion requires a threshold comparator and a counter.

17.3.3.2 Searching Algorithm

Finding the best-matching block requires optimizing the matching criterion over all possible candidate displacement vectors at each pixel. The so-called full-search, logarithmic search and hierarchical searching algorithms can accomplish this.

17.3.3.2.1 Full Search

The full-search algorithm evaluates the matching criterion for all possible values within the predefined searching window. If the search window is restricted to a $[-p, p]$ square, for each motion vector there are $(2p + 1)^2$ search locations. For a block size of $M \times N$ pixels, at each search location we compare $N \times M$ pixels. If we know the matching criterion and how many operations needed for each comparison then we can calculate the computation complexity of full-search algorithm. Full search is computationally expensive but guarantees finding the global optimal matching within a defined searching range.

17.3.3.2.2 Logarithmic Search

Actually, the expected accuracy of motion estimation algorithms varies according to the applications. In motion-compensated video coding, all one seeks is a matching block in terms of some metric, even if the match does not correlate well with the actual projected motion. Therefore, in most cases, search strategies faster than full searches are used, although they lead to suboptimal solutions. These faster search algorithms evaluate the criterion function only at a predetermined subset of the candidate motion vector locations instead of all possible locations. One of these faster search algorithms is the logarithmic search. Its more popular form is referred to as the three-step search. We explain the three-step search algorithm with the help of [Figure 17.20](#) where only the search frame is depicted. Search locations

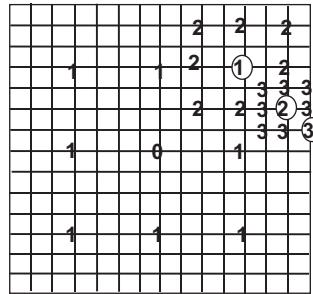


FIGURE 17.20
Three-step search.

corresponding to each of the steps in the three-step search procedure is labeled as 1, 2, and 3. In the first step, starting from pixel 0, we compute MAD for the nine search locations labeled 1. The spacing between these search locations here is 4. Assume that MAD is minimum for the search location (4,4), which is circled 1. In the second step, using the criterion function is evaluated at eight locations around the circled 1, which are labeled 2. The spacing between locations is now two pixels. Assume now the minimum MAD is at the location (6,2), which is also circled. Thus, the new search origin is the circled 2, which is located at (6,2). For the third step, the spacing is set to 1 now and the eight locations labeled 3 are searched. The search procedure is terminated at this point and the output of motion vector is (7,1). Additional steps may be incorporated in to the procedure if we wish to obtain sub-pixel accuracy in the motion estimations. Then the search frame needs to be interpolated to evaluate the criterion function at subpixel locations.

17.3.3.2.3 Hierarchical Motion Estimation

Hierarchical representations of images in the form of a Laplacian pyramid or wavelet transform are also quite often used with block matching method for improved motion estimation. The basic idea of hierarchical block matching is to perform motion estimation at each level successively, starting with the lowest resolution level. The lower resolution levels serve to determine a rough estimate of the motion information using relatively larger blocks. The estimate of the motion vector at a lower resolution level is then passed onto the next higher resolution level as an initial estimate. The higher resolution levels are used to fine-tune the motion vector estimate. At higher resolution levels, relatively smaller window sizes can be used since we start with a good initial estimate. The hierarchical motion estimate can significantly reduce the implementation complexity since its search method is very efficient. However, such a method requires increased storage due to the need to keep pictures at different resolutions. Furthermore, this scheme may yield inaccurate motion vectors for regions containing small objects. Since the search starts at the lowest resolution of the hierarchy, regions containing small objects may be eliminated and thus fail to be tracked. On the other hand, the creation of low-resolution pictures provides some immunity of noise. The following table provides some experimental results. The experimental results performed by one of the authors have shown that comparing with full-search the two-layer hierarchical motion estimation reduces the search complexity of factor 10 at the price of degrading reconstruction quality from about 0.2 dB to 0.6 dB for frame mode coding, from 0.26 dB to 0.38 dB for field mode coding and only 0.16 dB to 0.37 dB for frame/field adaptive coding, for different video sequences in the case of a fixed bit rate of 4 Mbps. In the case of variable bit rate (VBR) coding, the similar results can be observed from the rate distortion curves.

In the above discussion, we have restricted the motion vector estimation to integer pixel grids or pixel-accuracy. Actually, the motion vectors can be estimated with fractional or sub-pixel accuracy. In MPEG-2 video coding the half-pixel accuracy motion estimation can be used. Half-pixel accuracy can easily be achieved by interpolating the current and reference pictures by a factor of two and then using any of the motion estimation methods described previously.

17.3.3.3 Advanced Motion Estimation

Progress has recently been made in several aspects of motion estimation, which are described as follows.

17.3.3.3.1 Motion Estimation Using a Reduced Set of Image Data

The methods to reduce search complexity with sub-sampling and pyramid processing are well known and around in the literature (Sun 1994). However, the reduction by lowering the precision of each sample does not appear to have been extensively studied. Some experimental results have shown that the performance degradation of the hierarchical motion estimation algorithm is not serious when each layer up to four-layer pyramid is limited to 6-bits/sample. At 4–5 bits/sample the performance is degraded 0.2 dB over full precision.

17.3.3.3.2 Overlapped Motion Estimation (Katto et al. 1994)

A limitation of block matching is that it generates a significant proportion of motion vectors that do not represent the true motion present in the scene. One possible reason is that the motion vectors are estimated without reference to any picture data outside of the non-overlapping blocks. This problem has been addressed by overlapped motion estimation. In case of the overlapped motion compensation, motion-compensated regions translated by the motion vectors are overlapped with each other. Then a window function is used to determine the weighting factors for each vector. This technique has been adopted into the H.263 video coding standard. Some improvements have been clearly identified for low-bit-rate coding.

17.3.3.3.3 Frequency Domain Motion Estimation

An alternative to spatial-domain block matching methods is to estimate motion vector in frequency domain through calculating the cross-correlation (Young and Kingsbury 1993). Most international standards such as MPEG, H.263, and the proposed HDTV standard use the DCT and block-based motion estimation as the essential elements to achieve spatial and temporal compression, respectively. The new motion estimation approach is proposed in the DCT-domain (Koc 1998). This method of motion estimation has certain merits over conventional methods. It has very low computational complexity and is robust even in a noise environment. Moreover, the motion-compensation loop in the encoder is much simplified due to replacing the IDCT in the loop (Koc 1998).

17.3.3.3.4 Generalized Block Matching

In generalized block matching, the encoded frame is divided into triangular, rectangular, or arbitrary quadrilateral patches. We then search for the best matching triangular or quadrilateral in the search frame under a given spatial transformation. The choice of

patch shape and the spatial transform are related. For example, triangular patches offer sufficient degree of freedom with affine transformation, which has only six independent parameters. The bilinear transform has eight free parameters. Hence it is suitable for use with rectangular or quadrilateral patches. The generalized block matching is usually only adaptively used for those blocks where standard block-matching is not satisfactory for avoiding imposed computational load.

17.4 Rate Control

17.4.1 Introduction of Rate Control

The purpose of rate control is to optimize the perceived picture quality and to achieve a given constant average bit rate by controlling the allocation of the bits. From the view point of rate control, the encoding can be classified into VBR coding and constant bit rate (CBR) coding. The VBR coding can provide a constant picture quality with variable coding bit rate, while the CBR coding will provide a CBR with a non-uniform picture quality. Rate control and buffer regulation is an important issue for both VBR and CBR applications. In the case of VBR encoding, the rate controller attempts to achieve optimum quality for a given target rate. In the case of CBR encoding and real-time application, the rate control scheme has to satisfy the low-latency and video buffering verifier (VBV) buffer constraints. The VBV is a hypothetical decoder, which is conceptually connected to the output of an encoder (Appendix C of [mpeg2]). The bitstream generated by the encoder is placed to the VBV buffer at the CBR that is being used. The rate control has to assure that the VBV will not overflow and underflow. In addition, the rate control scheme has to be applicable to a wide variety of sequences and bit rates. At the GOP level, the total numbers of available bits are allocated among the various picture types, taking into account the constraints of the decoder buffer, so that the perceived quality is balanced. Within each picture, the available bits are allocated among the MBs to maximize the visual quality and to achieve the desired target of encoded bits for the whole picture.

17.4.2 Rate Control of Test Model 5 for MPEG-2

As we described before, the standard only defines the syntax for decoding. The test model is an example of encoder, which may not be optimal; however, it can provide a compliant compressed bitstream. Also, the test model served as a reference during the development of the standard. The TM5 rate control algorithm consists of three steps to adapting the MB quantization parameter for controlling the bit rate.

17.4.2.1 Step 1: Target Bit Allocation

The target bit allocation is the first step of rate control. Before coding a picture, we need to estimate the number of bits available for coding this picture. The estimation is based on several factors. These include the picture type, buffer fullness, and picture complexity. The estimation of picture complexity is based on the number of bits and quantization

parameter used for coding the same-type previous picture in the GOP. The initial complexity values are given according to the type of picture:

$$\begin{aligned} X_i &= 160 * \text{bit-rate}/115 \\ X_p &= 60 * \text{bit-rate}/115 \\ X_b &= 42 * \text{bit-rate}/115 \end{aligned} \quad (17.6)$$

where the subscript i , p , and b stand for picture types I, P, and B (this will be applied to the formulas in this section). After a picture of a certain type (I , P , or B) is encoded, the respective “global complexity measure” (X_i , X_p , and X_b) is updated as:

$$X_i = S_i Q_i, X_p = S_p Q_p, \text{ and } X_b = S_b Q_b \quad (17.7)$$

where S_i , S_p , S_b are the number of bits generated by encoding this picture and Q_i , Q_p , Q_b are the average quantization parameter computed the actual quantization values used during the encoding of the all the MBs including the skipped MBs. This estimation is very intuitive since if the picture is more complicated, more bits are needed to encode it. The quantization parameter (step or interval) is used to normalize this measure because the number of bits generated by encoder is inversely proportional to the quantization step. The quantization step can also be considered as a measure of coded picture quality. The target number of bits for the next picture in the GOP (T_i , T_p , and T_b) is computed as follows:

$$\begin{aligned} T_i &= \max\left\{\frac{R}{1 + \frac{N_p X_p}{X_i K_p} + \frac{N_b X_b}{X_i K_b}}, \text{bit-rate} / (8 * \text{picture-rate})\right\} \\ T_p &= \max\left\{\frac{R}{N_p + \frac{N_b K_p X_b}{X_b K_p}}, \text{bit-rate} / (8 * \text{picture-rate})\right\} \\ T_b &= \max\left\{\frac{R}{N_b + \frac{N_p K_b X_p}{X_p K_b}}, \text{bit-rate} / (8 * \text{picture-rate})\right\} \end{aligned} \quad (17.8)$$

where K_p and K_b are “universal” constants dependent on the quantization matrices. For the matrices of TM5, $K_p = 1.0$ and $K_b = 1.4$. The R is the remaining number of bits assigned to the GOP and after coding the picture this number is updated by subtracting the bit used for the picture. N_p and N_b is the number of P-pictures and B-pictures remaining in the current GOP in the encoding order. The problem of this target bit assignment algorithm is that it does not handle scene changes efficiently.

17.4.2.2 Step 2: Rate Control

Within a picture the bits used for each MB are determined by the rate control algorithm. Then, a quantizer step is derived from the number of bits available for the MB to be coded. The following is an example of rate control for P-picture.

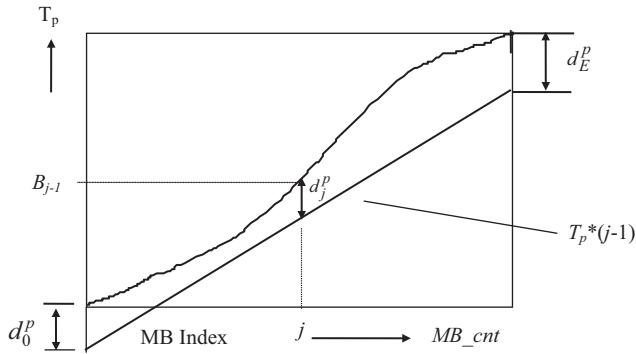


FIGURE 17.21
Rate control for P-picture.

In Figure 17.21, d_0^p is initial virtual buffer fullness, the T_p is the target bits for P picture. B_j is the number of bits generated by encoding all MBs in the picture up to and including j -th MB. MB_cnt is the number of MBs in the picture. Before encoding the j -th MB the virtual buffer fullness is adjusted during the encoding according to the following equation for P-picture:

$$d_j^p = d_0^p + B_{j-1} - \frac{T_p(j-1)}{MB_cnt} \quad (17.9)$$

Then, the quantization step is computed with the equation:

$$Q_j^p = \frac{d_j^p}{r} \quad (17.10)$$

where the “reaction parameter” r is given by $r = 2 * bit-rate/picture-rate$ and d_j^p is the fullness of the appropriate virtual buffer. This procedure is shown in Figure 17.21. The fullness of the virtual buffer for the last MB is used for encoding the next picture of the same type as the initial fullness.

This example can be extended to the general case for all I-, P-, and B-pictures. Before encoding the j -th MB, we compute the fullness of the appropriate virtual buffer:

$$\begin{aligned} d_j^i &= d_0^i + B_{j-1} - \frac{T_i(j-1)}{MB_cnt} \\ \text{or } d_j^p &= d_0^p + B_{j-1} - \frac{T_p(j-1)}{MB_cnt} \\ \text{or } d_j^b &= d_0^b + B_{j-1} - \frac{T_b(j-1)}{MB_cnt} \end{aligned} \quad (17.11)$$

Depending on the picture type, where d_0^i, d_0^p, d_0^b are initial fullness of the virtual buffers and d_j^i, d_j^p, d_j^b are the fullness of virtual buffer at j -th MB—one for each picture type. From the

number of bits of the virtual buffer fullness we compute the quantization step Q_j for MB j according to the buffer fullness:

$$Q_j = \frac{d_j * 31}{r} \quad (17.12)$$

The initial values of the virtual buffer fullness are:

$$\begin{aligned} d_0^i &= 10 \cdot r / 31 \\ d_0^p &= K_p \cdot d_0^i \\ d_0^b &= K_b \cdot d_0^i \end{aligned} \quad (17.13)$$

K_p and K_b are constants, which are defined in (17.8).

17.4.2.3 Step 3: Adaptive Quantization

Adaptive quantization is the last step of the TM5 rate control. It is noted that for active areas or busy areas, the human eyes are not so sensitive to the quantization noise, while the smooth areas are more sensitive to the quantization noise as discussed in [Chapter 1](#). Based on this observation, we modulate the quantization step obtained from the previous step in such a way to increase quantization step for active areas and reduce the quantization step for the smooth areas. In other words, we use more bits in the smooth areas and fewer bits for the active areas. The experiment results have shown that the subjective quality is higher with adaptive quantization step than without this step. The procedure of adaptive quantization in TM5 is as follows. First, the spatial activity measure for the j-th MB is calculated from the four luminance frame-organized subblocks and the four luminance field-organized blocks using the intra pixel values:

$$act_j = 1 + \underset{sblk=1,8}{\text{Min}}(\text{var_sblk}) \quad (17.14)$$

where var_sblk is the variance of each spatial 8×8 block, whose value is calculated as

$$\text{var_sblk} = \frac{1}{64} \sum_{k=1}^{64} (P_k - P_{mean})^2 \quad (17.15)$$

and P_k is the pixel value in the original 8×8 block and P_{mean} is the mean value of the block, which is calculated as

$$P_{mean} = \frac{1}{64} \sum_{k=1}^{64} P_k \quad (17.16)$$

The normalized activity factor N_{act_j} is:

$$N_{act_j} = \frac{2 \cdot act_j + avg_act}{act_j + 2 \cdot avg_act} \quad (17.17)$$

where avg_act is the average value of act_j , the last picture to be encoded. Therefore, this value will not give good results when a scene change occurs. On the first picture,

this parameter takes the value of 400. Finally, we can obtain the modulated quantization step for j-th MB:

$$mquant_j = Q_j \cdot N_act_j \quad (17.18)$$

where Q_j is the reference quantization step value obtained in the last step. The final value of $mquant_j$ is clipped to the range of [1,31] and is used and coded as described in the MPEG standard.

As we indicated before, the TM5 rate control provides only a reference model. It is not optimized in many aspects. Therefore, there is still a lot of room for improving the rate control algorithm, such as to provide more precise estimation of average activity by pre-processing. In the following section, we will investigate the optimization problem for mode decision combined with rate control, which can provide a significant quality improvement as shown by experimental results.

17.5 Optimum Mode Decision

17.5.1 Problem Formation

This section addresses the problem of determining the optimal MPEG [mpeg2] coding strategy in terms of the selection of MB coding modes and quantizer scales. In the Test Model (MPEG-2 Test model 5 [1993]), the rate control operates independently from the coding mode selection for each MB. The coding mode is decided based only upon the energy of predictive residues. Actually, the two processes, coding mode decision and rate control, are intimately related to each other and should be determined jointly in order to achieve optimal coding performance. A constrained optimization problem can be formulated based on the rate-distortion characteristics, or $R(D)$ curves, for all the MBs that compose the picture being coded. Distortion for the entire picture is assumed to be decomposable and expressible as a function of individual MB distortions, with this being the objective function to minimize. The determination of the optimal solution is complicated by the MPEG differential encoding of motion vectors and dc coefficients, which introduce dependencies that carry over from MB to MB for a duration equal to the slice length. As an approximation, a near-optimum greedy algorithm can be developed. Once the upper bound in performance is calculated, it can be used to assess how well practical sub-optimum methods perform.

Prior related works dealing with dependent quantization for MPEG include the works done by Ramchandran et al. (1994) and Lee and Dickerson (1994). Those works treated the problem of bit allocation where there is temporal dependency in coding complexity across I, P, and B frames. While these techniques represent the most proper bit allocation strategies across frames from a theoretical viewpoint, no practical real-time MPEG encoding system will use even those proposed simplified techniques because they require an unwieldy number of pre-analysis encoding passes over the window of dependent frames (one MPEG GOP). To overcome these computational burdens, more pragmatic solutions that can realistically be implemented have been considered by Sun et al. (1997). In this work, the major emphasis is not on the problem of bit allocation among I, P, and B frames; rather, the authors choose to utilize the frame-level allocation method provided by the

Test Model (MPEG-2 Test model 5 [1993]). In this way, frame-level coding complexities are estimated from past frames without any forward pre-analysis knowledge of future frames. This type of analysis forms the most reasonable set of assumptions for a practical real-time encoding system. Another method that extends the basic Test Model idea to alter frame budgets heuristically in the case of scene changes, use of dynamic GOP size, and temporal masking effects can be found in Wang (1995). These techniques also offer very effective and practical solutions for implementation. Given the chosen method for frame-level bit budget allocation, the focus of this section is to jointly optimizing MB coding modes and quantizers within each frame.

There exist many choices for the MB coding mode under the MPEG-2 standard for P and B pictures, including intra mode, no motion compensation mode, frame/field/dual-prime motion compensation inter mode, forward/backward/average inter mode, and field/frame DCT mode. In the standard Test Model reference (MPEG-2 Test model 5 [1993]), the coding mode for each MB is selected by comparing the energy of predictive residuals. For example, the intra/inter decision is determined by a comparison of the variance of the MB pixels against the variance of the predictive residuals; the inter prediction mode is selected to be the inter mode that has the least predictive residual MSE. The coding mode selected by Test Model criteria does not result in the optimal coding performance.

In attempting to achieve optimal coding performance, it is important to realize that coding modes should be determined jointly with rate control because the best coding mode depends upon the operating point for rate. In deciding which of the various coding modes is best, one should consider what the operating point is for distortion, and also consider the tradeoff between spending bits for coding the prediction residuals and bits for coding motion vectors.

The number of bits used for coding the MB is the sum of bits used for coding motion vectors and bits used for coding residuals:

$$R_{MB} = R_{mv} + R_{residual} \quad (17.19)$$

For example, in Figure 17.22, consider the decision between (a) frame-mode forward prediction and (b) field-mode bi-directional prediction. Mode (b) will almost always produce a prediction that has lower MSE than mode (a). However, mode (a) requires coding of fewer motion vectors than mode (b). Which mode is best? The answer depends on the operating point for distortion. When coding at a very coarse quant-scale, (a) can perform

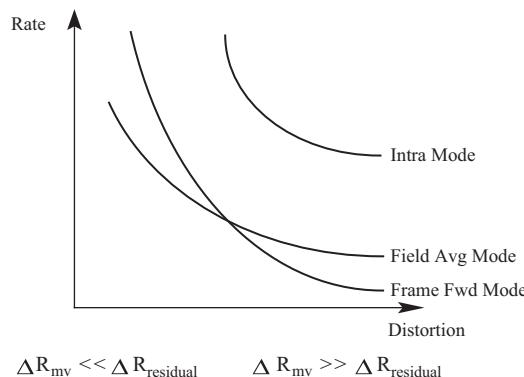


FIGURE 17.22

R(D) curves for different MB coding modes.

better than (b) because the difference in bits required for coding motion vectors between the two modes may be much greater than the difference in bits required for coding residuals between the two modes. However, when coding at a fine quant-scale, (b) can perform better than (a) because (b) provides a better prediction and the bits required for motion vectors would become negligible compared to bits for coding residuals.

Coding mode decisions and rate control can be determined jointly and optimally starting from the basics of constrained optimization using $R(D)$ curves. This optimal solution would be an a-posterior solution that assumes complete knowledge of $R(D)$. We investigate an optimal solution for objective functions of the form:

$$D_{PICT} = \sum_{i=1}^{NMB} D_{MBi} \quad (17.20)$$

which states that the distortion for the picture, D_{PICT} , can be measured as an accumulation of individual MB distortions, D_{MBi} , for all NMB number of MBs in the picture. We minimize this objective function subject to having individual MB distortions being uniform over the picture:

$$D_1 = D_2 = \dots = D_{NMB} \quad (17.21)$$

and having the bits generated from coding each MB, R_{MBi} , sum to a target bit allocation for the entire picture, R_{PICT} :

$$\sum_{i=1}^{NMB} R_{MBi} = R_{PICT} \quad (17.22)$$

The choice for the MB distortion measure, D_{MBi} , can be mean-square-error (MSE) computed over the pixels in the MB, or it can be a measure that reflects subjective distortion more accurately, such as luminance and frequency weighted MSE. Other choices for D_{MBi} may be the quantizer scale used for coding the MB, or better yet, the quantizer scale weighted by an activity masking factor. In this paper, we select distortion for each MB i to be spatial-masking-activity-weighted quantizer scale:

$$DMB_i = qscalei / N_acti \quad (17.23)$$

where $N_acti \in [0.5, 2.0]$ is the normalized spatial masking activity quantizer weighting factor, as defined in the Test Model (MPEG-2 Test model 5 [1993]):

$$N_acti = \frac{2 * act_i + avg_act}{act_i + 2 * avg_act} \quad (17.24)$$

where act_i is the minimum luma block spatial variance for MB i and avg_act is the average value of act_i over the last picture to be coded. N_acti reflects the relative amount of quantization error that can be tolerated for MB i as compared to the rest of the MBs that compose the picture. N_acti depends strongly on whether the MB belongs to a smooth, edge, or textured region of the picture. Hence, the MB distortion metric is space variant and depends on the context of the local picture characteristics surrounding each MB. We assume that maintaining the same D_{MBi} for all MBs, or selecting the quantizer scales directly proportional to N_acti in such a manner, corresponds to maintaining uniform subjective quality throughout

the picture. Masking-activity-weighted quantizer scale is a somewhat coarse measure for image quality, but it reflects subjective image quality better than MSE or PSNR, and it is a practical metric to compute that lends itself to an additive form for distortion.

It is important to note that the resulting distortion measure for the picture D_{PICT} is really only meaningful as a relative comparison figure for the same identical picture (thus having the same masking activities) quantized different ways. It is not useful in comparing between two different images. $PSNR$ is only useful in this sense too, though with poorer subjective accuracy.

In the following, a procedure for obtaining the optimal coding performance with the joint optimization of coding mode selection and rate control is discussed. Since this method would be too complex to implement, a practical sub-optimal heuristic algorithm is presented. Some simulation results and comparisons between the different algorithms—Test Model algorithm, Near-Optimum algorithm and the practical Sub-Optimum algorithm are also provided to assist the reader in understanding the differences in performance.

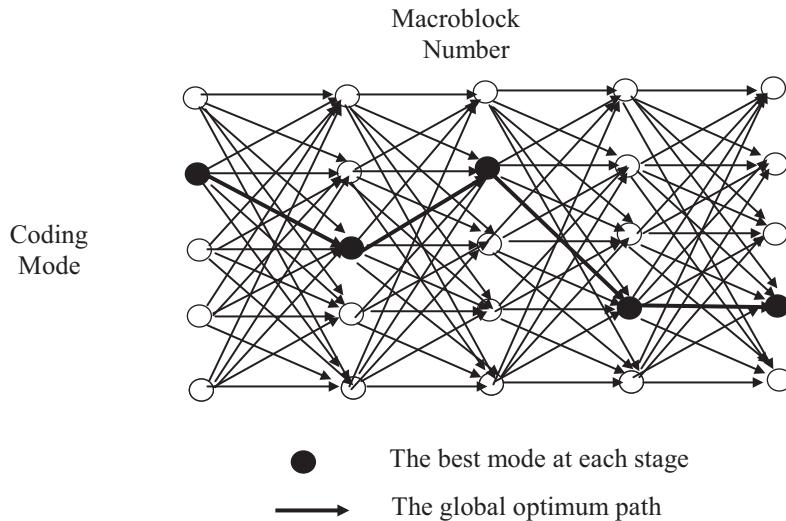
17.5.2 Procedure for Obtaining the Optimal Mode

17.5.2.1 Optimal Solution

The solution to the optimization problem is unique because the objective function is monotonic and the individual MB $R(D)$ functions are also monotonic. In order to solve for the optimal set of MB modes and quant-scales for the picture (mode and qscale), the differential encoding of motion vectors and intra dc coefficients as done in MPEG should be accounted for. According to MPEG, each slice has its own differential encoding chain. At the start of each slice, prediction motion vectors are reset to zero. As each MB is encoded in raster scan order, the MB motion vectors are encoded differentially with respect to prediction motion vectors that depend on the coding mode of the previous MB. These prediction motion vectors may be reset to zero in the case that the previous MB was coded as intra or skipped. Similarly, dc coefficients in continuous runs of intra MBs are encoded differentially with respect to the previous intra MB. The intra dc predictors are reset at the start of every slice, and at inter or skipped MBs. Slice boundaries delimit independent self-contained decodable units. Finding the optimal set of coding modes for the MBs in each slice entails a search through a trellis of dimensions S stages by M states per stage, with S being the slice size and M being the number of coding modes being considered (See Figure 17.23). This trellis structure arises because there are M^2 distinct rate distortion, $R_{mode|previous-mode}(D)$, characteristic curves corresponding to each of M coding modes, with each in turn having a different dependency for each of M coding modes of the previous MB. We now consider populating the trellis links with values by sampling the set of these M^2S rate-distortion curves at a specific distortion level. For a given fixed MB distortion level, D_{MB} , each link on the trellis is assigned a cost equal to the number of bits to code a MB in a certain mode given the mode from which the preceding MB was coded. For any group of links entering a node, the costs of these links differ only because of the difference in bits caused by the motion vector and dc coefficient coding dependency upon the prior MB.

The computational requirements per slice involves:

- To determine link costs in the trellis, the number of “code the MB” operations (i.e., DCT + Quantization + RLC/VLC) is equal to M^2S .
- After determining all trellis link costs, the number of path searches is equal to MS .

**FIGURE 17.23**

Full search trellis, M_s (M is number of modes at each stage and S is the length of slice) searches needed to obtain the best path.

A general iterative procedure for obtaining the optimal solution is as follows:

1. Initialize a guess for $D_{MB} = D_{MB0}$. Since D_{MB} is the same for every MB in the picture, this sets an initial guess for the operating distortion level of the picture.
2. Do for each slice in the picture:
 - For each MB in the slice and the mode considered, determine the quantizer scale that yields the distortion level D_{MB} , i.e., $q_s = f(D_{MB})$, where f is the function that describes the relationship between quantizer scale q_s and distortion D_{MB} . If we use spatial-masking-activity-weighted quantizer scale as a measure of distortion (as from equation [17.4]), then q_s equals $N_{act} * D_{MB}$.
 - Compute all the link costs in the trellis representing the slice.
 - The link costs, R_{MBi} (mode k | mode j), represents the number of resulting bits (total bits for coding residual, motion vectors, and MB header) for coding MB i in mode k given that the preceding MB was coded in mode j .
 - Search through the trellis to find the path that has the lowest $\sum R_{MBi}$ over the slice.
3. Compute $\sum R_{MBi}$ for all MBs in the picture and compare to target R_{PICT} .
 - If $|\sum R_{MBi} - R_{PICT}| < \epsilon$ then the optimal mode and qscale has been found for the picture. Repeat the process for the next picture.
 - If $\sum R_{MBi} < R_{PICT}$ then decrement $D_{MB} = D_{MB} - \Delta D_{MB}$ and go to step 2.
 - If $\sum R_{MBi} > R_{PICT}$ then increment $D_{MB} = D_{MB} + \Delta D_{MB}$ and go to step 2.

17.5.2.2 Near-Optimal Greedy Solution

The solution from the full exponential-order search requires an unwieldy amount of computations. In order to avoid the heavy computational burden, we can use a greedy approach (Lee and Dickerson 1994) to simplify and sidestep the dependency problems of the full-search method. In the greedy algorithm, the best coding mode selection for the current MB depends only upon the best mode of the previous coded MB. Therefore, the upper bound we obtain is a near-optimum solution instead of a global optimum. Figure 17.24 illustrates the greedy algorithm. After coding a MB in each of the M modes, the mode resulting in the least number of bits is chosen to be “best.” The very next MB is coded with dependencies to that chosen “best” mode. The computations per slice are reduced to MxS “code the MB” operations and MxS comparisons. A general iterative procedure for obtaining the greedy solution is as follows:

1. Initialize a guess for $D_{MB} = D_{MB0}$.
2. Do for each MB:
 - For each mode considered, determine the quantizer scale that yields the distortion level D_{MB} , i.e., $q_s = f(D_{MB})$, where f is the function we mentioned previously.
 - For each mode, code the MB in that mode with that q_s value and record the resulting number of generated bits, $R_{MBi}(\text{mode } i | \text{ mode } j)$. The MB is coded based on the already determined mode of the preceding MB.
 - The “best” mode for MB i is the mode for which $R_{MBi}(\text{mode } i | \text{ mode } j)$, mode is smallest. This yields R_{MBi} bits for MB i .
3. Compute $\sum R_{MBi}$ for all MBs in the picture and compare to target R_{PICT} .
 - If $|\sum R_{MBi} - R_{PICT}| < \epsilon$ then the optimal (mode and qscale) has been found for picture. Repeat the process for the next picture.
 - If $\sum R_{MBi} < R_{PICT}$ then decrement $D_{MB} = D_{MB} - \Delta D_{MB}$ and go to step 2.
 - If $\sum R_{MBi} > R_{PICT}$ then increment $D_{MB} = D_{MB} + \Delta D_{MB}$ and go to step 2.

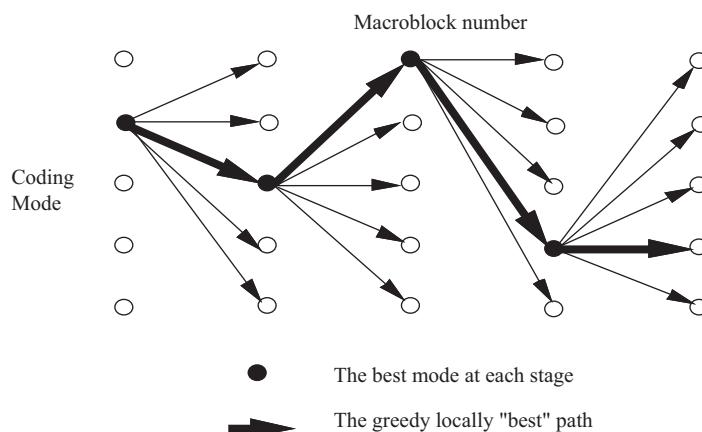


FIGURE 17.24

Greedy approach, MxS comparisons needed to obtain the locally “best” path.

17.5.3 Practical Solution with New Criteria for the Selection of Coding Mode

It is obvious that the near-optimal solution discussed in the previous section is not a practical method because of its complexity. In order to determine the best mode, we have to know how many bits it takes to code each MB in every mode with the same distortion level. The total number of bits for each MB, $R_{MB'}$, consists of three parts, bits for coding motion vectors, R_{mv} , bits for coding the predictive residue, R_{res} , and bits for coding MB header information, R_{header} , such as MB type, quantizer scale, and coded-block-pattern.

$$R_{MB} = R_{mv} + R_{res} + R_{header} \quad (17.25)$$

The number of bits for motion vectors, R_{mv} , can be easily obtained by VLC table look-up. But to obtain the number of bits for coding the predictive residue, one has to go through the three-step coding procedure: (1) DCT, (2) quantization, and (3) VLC, as shown in [Figure 17.24](#). At step 3, R_{res} is obtained with a look-up table according to the run-length of zeros and the level of quantized coefficients, i.e., R_{res} depends on the pair of values of run and level:

$$R_{res} = f(run, level) \quad (17.26)$$

As stated above, to obtain the upper-bound coding performance all three steps are needed for each coding mode, and then the coding mode resulting in the least number of bits is selected as the best mode.

To obtain a much less computationally intensive method, it is preferred to use a statistical model of DCT coefficient bit usage versus variance of the prediction residual and quantizer step size. This will provide an approximation of the number of residual bits, R_{res} . For this purpose, we assume that the run and level pair in (17.7) is strongly dependent on values of the quantizer scale, q_s , and the variance of the residue, V_{res} , for each MB. Intuitively, we would expect that the number of bits to encode a MB is proportional to the variance of the residual and inversely proportional to the value of quantizer step size. Therefore, a statistical model can be constructed by plotting R_{res} versus the independent variables V_{res} and q_s over a large set of representative MB pixels from images typical of natural video material. This results in a scatter plot showing tight correlation, and hence a surface can be fit through the data points. It was found that equation (17.24) can be approximately expressed as:

$$R_{res} \approx f(q_s, V_{res}) = (K/(C q_s + q_s^2)) V_{res} \quad (17.27)$$

where K and C are constants found through surface-fitting regression. If we assume R_{header} is a relatively fixed component that does not vary much with MB coding mode and can be ignored, then formula (17.23) can be approximately replaced by:

$$R_{MB'} = R_{mv} + (K/(C q_s + q_s^2)) V_{res} \quad (17.28)$$

The value of $R_{MB'}$ reflects the variable portion of bit usage that is dependent on coding mode, and can be used as the measure for selecting the coding mode in our encoder. For a given quantizer step size, the mode resulting in the smallest value of $R_{MB'}$ is chosen as the “best” mode. It is obvious that in the use of this new measurement to select the coding mode, the computational complexity increase over the Test Model method is very slight (the same identical calculation for V_{res} is made in the Test Model [Figure 17.25](#)).

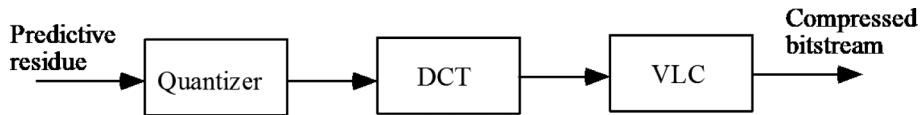


FIGURE 17.25
Coding stages to find out bit count.

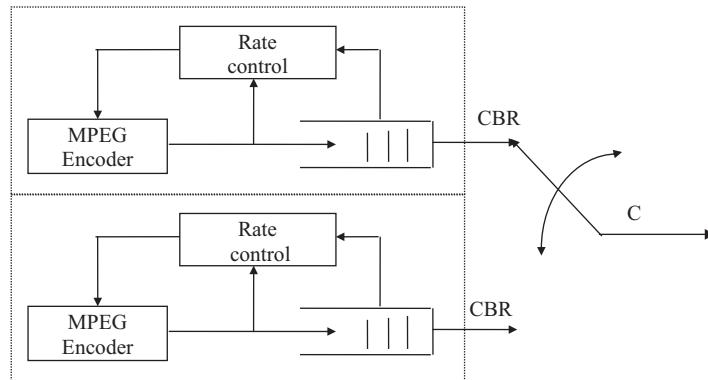
17.6 Statistical Multiplexing Operations on Multiple Program Encoding

In this section, the strategies for statistical multiplexing operation on the multiple program encoding will be introduced. This topic is an extension of rate control into the case of multiple program encoding. First, a background survey of general encoding and multiplexing modes is reviewed. Second, the specific algorithm used in some current systems is introduced, its shortcomings are addressed, and possible amendments to the basic algorithm are described. Some potential research topics such as modeling strategies and methods for solving the problem are proposed for investigation. These topics may be good research topics for the interested graduate student.

17.6.1 Background of Statistical Multiplexing Operation

In many applications, several video sources may often be combined or multiplexed onto a single link for transmission. At the receiving end, the individual sources of data from the multiplexed data are de-multiplexed and supplied to the intended receivers. For example, in an ATM network scenario many video sources originating from a local area are multiplexed onto a wide-area backbone trunk. In a satellite broadcasting scenario, several video sources are multiplexed for transmission through a transponder. In a cable TV scenario, hundreds of video programs are broadcast onto a cable bus. Since the transmission channel—such as a trunk, a transponder, or a cable—is always an expensive resource, the limited channel capacity should be exploited as much as possible. The goal of statistical multiplexing encoding is to make the best use of the limited channel capacity as possible. There are several approaches to encoding and multiplexing a plurality of video sources. In the following, we will compare the methods and describe the situation where each method is applicable. The qualitative comparisons are made in terms of tradeoffs among factors of computation; implementation complexity; and encoded picture quality, buffering delay, and channel utilization. To understand the statistical multiplexing method, we first introduce a simple case of deterministic multiplexing function of CBR encoder. The standard method for performing the encoding and multiplexing function is to independently encode the source with a CBR. The CBR encoder produces an encoded bit stream, representing the video supplied to it, at a predetermined CBR. To produce CBR, the CBR encoder utilizes a rate buffer and feedback control mechanism that continually modifies the amount of quantization applied to the video signal, as shown in [Figure 17.26](#).

The CBR encoder provides a CBR with varying encoded picture quality. This means that the degree of quantization applied depends upon the current frame's coding complexity offered to the MPEG compression algorithm. Fine quantization is then applied to those frames that have low spatial and/or temporal coding complexity, and conversely coarse quantization is applied to frames that possess high spatial and temporal coding

**FIGURE 17.26**

Independent encoding/muxing of CBR sources.

complexity in order to meet the bit rate. However, varying the quantization level corresponds to varying the video quality. Thus, in a CBR encoder, spatial and temporal complexity tends to be encoded in such a manner that the subjective quality of the reproduced image is lower than that of less complex images. This makes any form of rate control inherently bad in the sense that control is always imposed in a direction contrary to the goal of achieving uniform image quality. Usually, bit rates for CBR encoders are chosen so that the moderately difficult scenes can be coded to an acceptable quality level. Given that moderately difficult scenes give good results, all simpler scenes will yield even better results with the given rate, while very difficult scenes will result in noticeable degradation. Since CBR encoders produce CBR, the multiplexing of a plurality of sources is very simple. The required channel capacity would simply be the sum of all the individual CBRs. Deterministic time or frequency division multiplexing of the individual CBR bitstreams onto the channel in a well-known and simple process. So, with CBR encoding uniformly consistent image quality is impossible for the video sequence with varying scene complexity but the reward is the ease of multiplexing. But penalty of CBR coding with easy multiplexing may not only the non-uniform picture quality, also result in lower efficiency of channel bandwidth employment. Better efficiency can be gained by statistical multiplexing, whereby each source is encoded at a VBR coding approach. The VBR coding will result in uniform or consistent coded image quality by fixing the quantization scale or by modulating quantization scale to a limited extent according to activity masking attributes of the human visual system. Then, the bit rates generated by VBR coding vary with the incoming video source material's coding complexity. The statistical multiplexing is referred to as StatMux in short. The coding gain of StatMux is possible through sharing of the channel resource jointly among the encoders. For example, two MPEG encoders may assign the appearance of their I-pictures at different time; this may reduce the limitation of the maximum channel bandwidth requirement since coding I-picture may generate a large number of bits. This may not be a good example for practical applications. However, this explains that the process of StatMux is not a zero-sum game whereby one encoder's gain must be exactly another encoder's loss. In the process of StatMux, one encoder's gain is obtained by using the channel bandwidth, which another encoder does not need at that time or would bring a very marginal gain for another encoder at that time. More exactly, this concept of gains through sharing arises when the limited number of bits is dynamically appropriated towards encoders that can best utilize those bits in substantially

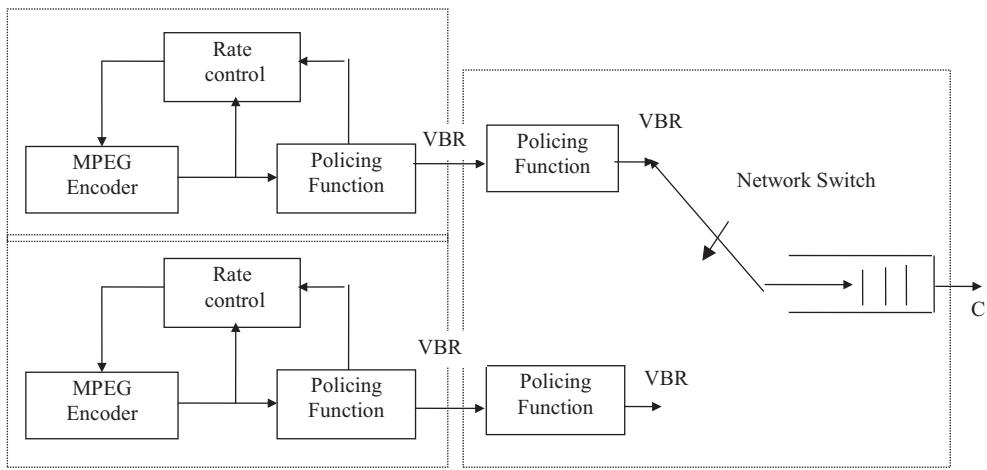
improving its image quality during complex segments and eschewed from encoders that can improve its image quality only marginally during easy segments. It is obvious that the CBR-encoded sources do not need statistical multiplexing since the bandwidth for each encoded source is well defined. The gain of statistical multiplexing can only possibly be obtained with VBR-encoded sources. In the following section, we are going to discuss two kinds of multiplexing with multiple VBR-encoded sources.

17.6.2 VBR Encoders in StatMux

There are two multiplexing methods for encoding multiple sources with VBR encoders: open-loop and close-loop. Each VBR encoder in open-loop multiplexing mode produces the most consistently uniform predefined image quality level regardless of the coding complexity of incoming video sources. The image quality is decided by fixing the quantization scale. When the quantization scale is fixed, the signal-to-noise ratio is fixed under assumption of white Gaussian quantization noise. Sometimes, the quantization scale is slightly modulated according to the image activity to match the human visual system, for example in the method in MPEG-2 TM5. The resulting VBR bit rate process is generated by allowing the encoder to freely use however many bits needed to meet the predetermined quality level. Usually, each video source encoded by VBR encoder in open-loop mode is not geographically co-located and cannot be encoded jointly. However, the resulting VBR processes do share the channel “jointly,” in the sense that the total channel bandwidth is not rigidly allocated among the sources in a fixed manner such as is done in CBR operation mode where each source has the fixed portion of channel bandwidth. The instantaneous combined rates of all the VBR encoders may exceed the channel capacity, especially in the case when all the encoders generate the bursts of bits at the same time the joint buffer will overflow, thereby leading to loss of data. However, there still exists a possibility to more efficiently utilize the channel capacity by carefully allocating the loading conditions without losing data. However, the totally open-loop VBR coding are not stationary and it is hard to achieve both good channel utilization and very limited data loss. A practical method of VBR transmission for use in the ATM environment involves placing limitations on the degree of variability allowed in VBR processes. [Figure 17.27](#) illustrates the idea of self-regulating VBR encoders.

The difference between the proposed VBR encoder and a totally open-loop VBR encoder is that a looser form of rate control is imposed to the VBR encoder in order to avoid violating transmission constraints that are agreed to by the user and the network as part of the contract negotiated during the call set up stage. The rate control will match the policing function, which is enforced by the network. Looser rate control means that the rate control is not so strict as one in the CBR case because it allows for the encoder to vary its output bit rate according to the coding complexity up to a certain degree as decided by the policing function.

In some applications such as TV broadcasting or cable TV, the video sources may be geographically co-located at the same site. In such scenarios, additional gains can be realized by the StatMux in which the sources are jointly encoded and jointly multiplexed. By using a common rate controller, all encoders operate in VBR mode but without contending and stepping over one another as in independent VBR encoding and multiplexing. The joint rate controller assigns the total available channel capacity to each encoder so that a certain common quality level is maintained. The bit rates assigned to each individual encoder by joint rate control dynamically change based on the coding complexities of each video

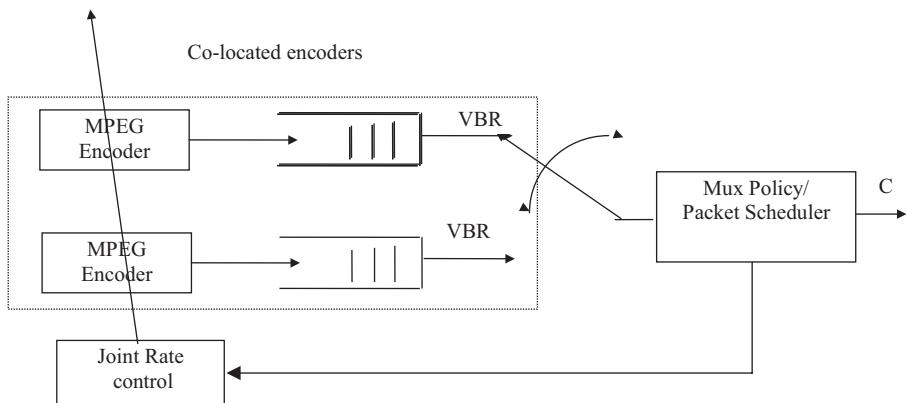
**FIGURE 17.27**

Independent encoding/muxing of geographically dispersed VBR sources.

source in order to achieve the most uniform quality among the encoders and along time for each encoder. In such a joint rate control method, although each encoder produces its own variable rate bits, the sum of bits produced by all encoders combined together is a CBR to fit the channel capacity. Such an idea is shown in [Figure 17.28](#).

17.6.3 Research Topics of StatMux

The major problem of StatMux is how to allocate the bit rate resource among the video sources that share the common channel bit rate and are jointly encoded by a joint rate controller. This allocation should be based on the coding complexity of each source. The bit rate, $R_i(t)$, for encoder i at time t according to the normalized coding complexity of all encoders for the GOP period ending at time t such as:

**FIGURE 17.28**

Method of joint rate control and multiplexing.

$$R_i(t) = \frac{X_i(t)}{\sum_{j=1}^N X_j(t)} \cdot C \quad (17.29)$$

where $X_i(t)$ is the coding complexity of source for encoder i at the time t over a GOP period and C is the total channel capacity. Also, the bit rate assignment has to be updated from time to time to trace the variation of source complexity. In the following, we will discuss several topics that may be the research topics for graduate students.

17.6.3.1 Forward Analysis

Without forward analysis, scene transitions are unanticipated and lead to incorrect bit allocation for a brief transient period following the scene changes. If the bit allocation of the current video segment is based on the complexity of the previous video segment and is adjusted by the available bit rate resource, those video segments that change from easy coding complexity to difficult coding complexity suffer the greatest degradation without pre-analysis of upcoming increased complexity. Pre-analysis could be performed with a dual set of encoders operating with a certain pre-processing delay ahead of the actual encoding process. As a simple example, if we start to assign the equal portion of bit rate for each encoder, then we can obtain the average quantization scale for this GOP that can be considered as the forward analysis results of coding complexity. The real coding process can operate on the coding complexity obtained by the pre-analysis. If we choose one or two GOPs according to the synchronous status of the input video sources to perform the pre-analysis, it will result in small buffering delay.

17.6.3.2 Potential Modeling Strategies and Methods

Several modeling strategies and methods have been investigated to find a suitable procedure for classifying sources and determining what groups of sources can appropriately be jointly encoded together for transmission over a common channel as so to meet a specified image quality level. These modeling strategies and methods include modeling of video encoding, modeling of source coding complexity, and source classification. The modeling of video encoding algorithm involves measuring the operating performance of the individual encoders or characterizing their rate distortion function for a variety of scenes. Embodied into this model are the MPEG algorithms implemented for motion estimation, mode decision, rate control, and their joint optimization issues. It has been speculated that a hyperbolic functional form of

$$\text{Rate} = X/\text{Distortion} \quad (17.30)$$

would be appropriate over the normal operating bit rate range of 3–7 Mbps for MPEG-2 encoded ITU-R 601-sized videos. The hyperbolic shape of rate distortion curves would be also suitable for all video scenes. Actually, we can use a set of collected rate distortion data pairs with an encoder to fit a hyperbola through the points as shown in [Figure 17.29](#) and estimate the shape parameter X . The value of X will be used to present the coding complexity offered to an encoder. For modeling at the GOP level, the rate would be the number of bits used to code that GOP and the distortion can be chosen as the averaging

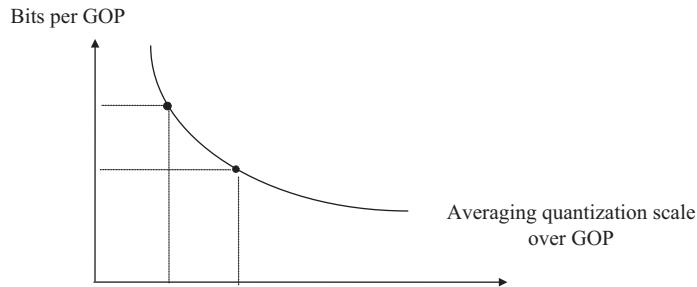


FIGURE 17.29
Rate distortion modeling of encoding algorithm and video source.

quantization scale over the GOP. In some literatures, the distortion is taken as the average PSNR over the GOP or overall sequence. If it is assumed that the quantization noise is modeled by white Gaussian noise, then both distortion measures are equivalent.

After obtaining the correct coding complexity parameters, we can improve the StatMux algorithm by assigning an encoding bit budget to each encoder based on the GOP level normalized complexity measure X that each encoder is encoding. The GOP level normalized complexity measure $X(n)$ is defined as:

$$X(n) = \sum_{i \in \text{GOP}} T(i)Q(i) \quad (17.31)$$

where n is the GOP number, $T(i)$ is the total number of bits used for encoding picture i , and $Q(i)$ is the average quantization scale used for encoding picture i . Some research results have shown that the $X(n)$ is insensitive to the operating bit rate; therefore, $X(n)$ is a reliable measure of a video source's loading characteristics. Therefore, the study of accurate model of the random process of $x(n)$ is very important for improving the operations of the StatMux algorithm. The accurate model of $X(n)$ reflects the video source's loading characteristics, which dictate the share of total bit budget that an encoder expects to get. Several statistical models have been proposed to describe the complexity measure, $X(n)$. For example, an auto-regressive process model is proposed for the intra-scene $X(n)$ process. This proposed model is based on the following observations: the complexity measure within a single scene has a skewed distribution by the Gamma function, the complexity measure within a scene displays a strong temporal correlation, and the form of the correlation is essentially exponential. The definition for the M th order auto-regressive model is:

$$X(n) = \sum_{m=1}^M a(m) \bullet X(n-m) + e(n) \quad (17.32)$$

where $e(n)$ is the white noise process and $a(m)$'s are the innovation filter coefficients. The statistics of the model such as the mean value, the variance, the correlation, and marginal distribution are used to match those of actual signals by adjusting $a(m)$'s, $e(n)$, and M . Other cases, such as scene transition model and inter-coded scene models, we leave as the project topics for the graduate students.

17.7 Summary

In this chapter, the technical detail of MPEG video was introduced. The technical detail of MPEG standards includes the decoding process of MPEG-1 and MPEG-2 video. Although the encoding process is not a standard part, it is very important for the content providers and service providers. We discussed the most important parts of encoding techniques. Some examples such as the joint optimizing of mode decision and rate control are good examples to understand how the standard is used.

Exercises

- 17.1 According to your understanding, give several reasons to explain why the MPEG standards specify only the decoding as normative part and define the encoding as informative part (Test Model).
 - 17.2 Can an MPEG-2 video decoder decode a bitstream generated by an MPEG-1 video encoder? Summarize the main difference between the MPEG-1 and MPEG-2 video standards.
 - 17.3 Pre-filtering may reduce the noise of the original video source and increase the coding efficiency. But at the same time the pre-filtering will result in a certain information loss. Conduct a project to investigate at what bit rate range the pre-filtering may benefit the coding efficiency for some video sources.
 - 17.4 Use TM5 rate control to encode several video sequences (such as the "Flower Garden" sequence) in two ways: (a) with adaptive quantization step and (b) without adaptive quantization step (Equation [6.16]). Compare and discuss the numerical results and subjective results (observe the smooth areas carefully).
 - 17.5 Why does MPEG-2 use different quantizer matrices for intra and inter coding? Conduct a project to use different quantization matrices to encode several video sequences and report the results.
 - 17.6 Conduct a project to encode several video sequences (a) with B-picture and (b) without B-picture. Compare the numerical and subjective results. Observe what difference exists between the sequences with fast motion and the sequence with slow motion. (Typical bit-rates for ITU-R 601 sequences are 4–6 Mbps).
-

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18

Application Issues of MPEG-1/2 Video Coding

This chapter is an extension of the previous chapter. We will introduce several important application issues of MPEG-1/2 video, which include the Advanced Television Standard Committee (ATSC) DTV standard that has been adopted by the Federal Communications Commission (FCC) as the TV standard in the United States, transcoding, down-conversion decoder, and error concealment.

18.1 Introduction

Digital video signal processing is an area of science and engineering that has developed rapidly over the past decade. The maturity of the Moving Picture Expert Group (MPEG) video coding standard is a very important achievement for the video industry and provides a strong support for digital transmission and storage of video signals. The MPEG coding standard is now being deployed for a variety of applications, which include high-definition television (HDTV), teleconferencing, direct broadcasting by satellite (DBS), interactive multimedia terminals, and digital video disc (DVD). The common feature of these applications is that the different source information such as video, audio, and data are all converted to the digital format and then mixed together to a new format, which is referred to as the bitstream. This new format of information is a revolutionary change in the multimedia industry, since the digitized information format, i.e., the bitstream, can be decoded by not only the traditional consumer electronic products such as television but also the digital computer. In this chapter, we will present several application examples of MPEG-1/2 video standards, which include the ATSC DTV standard, transcoding, down-conversion decoder, and error concealment. The DTV standard is the application extension of MPEG video standard. The transcoding and down-conversion decoders are the practical application issues that increase the features of compression-related products. The error concealment algorithms provide the tool for transmitting the compressed bitstream over noisy channels.

18.2 ATSC DTV Standards

18.2.1 A Brief History

The birth of digital television (DTV) in the United States has undergone several stages: the initial stage, the competition stage, the collaboration stage, and the approval stage (Reitmeier 1996). The concept of HDTV was proposed in Japan in the late 1970s and early 1980s.

During that period, Japan and Europe continued to make their efforts in the development of analog television transmission systems such as MUSE and HD-MAC systems. In early 1987, U.S. broadcasters fell behind in this field and felt they should take action to catch up with the new HDTV technology, so they petitioned the FCC to reserve spectrum for terrestrial broadcasting of HDTV. As a result, the Advisory Committee on Advanced Television Service (ACATS) was founded in August of 1987. This committee takes the role of recommending a standard to the FCC for approval. Thus, the process of selecting an appropriate HDTV system for the United States started. At the initial stage from 1987 to 1990, there were over 23 different analog systems proposed; among these systems two typical approaches were extended definition television (EDTV), which fits into a single 6 MHz channel, and the HDTV approach that requires two 6 MHz channels. By 1990, ACATS had established the Advanced Television Test Center (ATTC), an official testing laboratory sponsored by broadcasters to conduct extensive laboratory tests in Virginia and field tests in Charlotte, North Carolina. Also, the industry had formed the Advanced Television Standards Committee (ATSC) to perform the task of drafting the official standard documents of the selected winning system.

As we know, the current ATSC-proposed television standard is a digital system. In early 1990, the FCC issued a very difficult request to industry about DTV standards. The FCC required industry to provide full-quality HDTV service in a single 6 MHz channel. Having recognized the technical difficulty of this requirement at that time, the FCC also stated that this service could be provided by a simulcast service in which programs would be simultaneously broadcasted in both NTSC and the new television system. However, the FCC decided to not assign new spectrum bands for televisions. This means that simulcasting would occur in the already crowded VHF and UHF spectrums. The new television system had to use low-power transmission to avoid excessive interference with the existing NTSC services. Also, the new television system had to use a very aggressive compression approach to squeeze a full HDTV signal into the 6 MHz spectrum. One good thing was that backward compatibility with NTSC was not required. Actually, under these constraints the backward compatibility had already become impossible. Also, this goal could not be achieved by any of the previously proposed system and it caused most of the competing proponents to reconsider their approaches. Engineers realized that it was almost impossible to use the traditional analog approaches to reach this goal and that the solution may be in digital approaches. After a few months of considering, General Instrument announced their first digital system proposal for HDTV, Digicipher, in June 1990. In the following half year, three other digital systems were proposed: the Advanced Digital HDTV by the Advanced Television Research Consortium, which included Thomson, Philips, Sarnoff, and NBC in November 1990; Digital Spectrum Compatible HDTV by Zenith and AT&T in December 1990; and Channel Compatible Digicipher by General Instrument and the Massachusetts Institute of Technology in January 1991. Thus, the competition stage started. The prototypes of four competing digital systems and the analog system, Narrow MUSE, proposed by NHK, were officially tested and extensively analyzed during 1992. After a first round of tests, it was concluded that the digital systems would be continued for further improvement and would be adopted. In February 1992, the ACATS recommended digital HDTV for the U.S. standard. It also recommended that the competing systems be either further improved or re-tested, or be combined to a new system. In the middle of 1993, the former competitors joined in a Grand Alliance. Then the DTV development entered the collaboration stage. The Grand Alliance (1994) began a collaborative effort to create the best system that combines the best features and

capabilities of the formerly competing systems into a single “best of the best” system. After one year of joint effort by the seven Grand Alliance members, the Grand Alliance provided a new system that was prototyped and extensively tested in the laboratory and field. The test results showed that the system is indeed the best of the best compared with formerly competing systems. The ATSC then recommended this system to the FCC as the candidate HDTV standard in the United States. During the following period, the computer industry realized that DTV provides the signals that can now be used for computer applications and the TV industry was invading their terrain. They presented different opinion about the signal format and were especially opposed to the interlaced format. This reaction delayed the approval of the ATSC standard. After long time debate, the FCC finally approved the ATSC standard in early 1997. However, the FCC did not specify the picture formats and left this issue to be decided by the market.

18.2.2 Technical Overview of ATSC Systems

The ATSC DTV system has been designed to satisfy the FCC requirements. The basic requirement is that no additional frequency spectrum will be assigned for DTV broadcasting. In other words, during a transition period, both NTSC and DTV service will be simultaneously broadcast on different channels and DTV can only use the taboo channels. This approach allows a smooth transition to DTV, such that the services of the existing NTSC receivers will remain and gradually be phased out of existence in the year 2006. The simulcasting requirement causes some technical difficulties of DTV design. First, the high-quality HDTV program must be delivered in a 6 MHz channel to make efficient use of spectrum and fit allocation plans for spectrum assigned to television broadcasting. Second, a low-power and low-interference signal must be used so that simulcasting in the same frequency allocations as current NTSC service does not cause excessive interference to the existing NTSC receiving since the taboo channels are generally unsuitable for broadcasting an NTSC signal due to high interference. In addition to satisfying the frequency spectrum requirement, the DTV standard has several important features that allow DTV to achieve interoperability with computers and data communications. The first feature is the adoption of layered digital system architecture. Each individual layer of the system is designed to be interoperable with other systems at the corresponding layers. For example, the square-pixel and progressive-scan picture format should be provided to allow computers access to the compression layer or picture layer depending on the capacity of computers and the ATM-like packet format for ATM network to access the transport layer. Second, the DTV standard uses a header/descriptor approach to provide maximum flexible operating characteristics. Therefore, the layered architecture is the most important feature of DTV standards. The additional advantage of layering is that the elements of the system can be combined with other technologies to create new applications. The system of DTV standard includes four layers: picture layer, compression layer, transport layer, and transmission layer.

18.2.2.1 Picture Layer

At the picture layer, the input video formats have been defined. The Executive Committee of the Advanced Television Systems Committee has approved to release the statement regarding the identification of the HDTV and SDTV transmission formats within the ATSC DTV standards. There are six video formats in the ATSC DTV standard, which are “high-definition television.” These formats are listed in [Table 18.1](#).

TABLE 18.1

HDTV Formats

| Spatial Format (X × Y active pixels) | Aspect Ratio | Temporal Rate |
|---|--------------|-------------------------------|
| 1920 × 1080 (square pixel) | 16:9 | 23.976/24 Hz progressive scan |
| | | 29.97/30 Hz progressive scan |
| | | 59.94/60 Hz interlaced scan |
| 1280 × 720 (square pixel) | 16:9 | 23.976/24 Hz progressive scan |
| | | 29.97/30 Hz progressive scan |
| | | 59.94/60 Hz progressive scan |

TABLE 18.2

SDTV Formats

| Spatial Format (X × Y active pixels) | Aspect Ratio | Temporal Rate |
|---|--------------|-------------------------------|
| 704 × 480 (CCIR 601) | 16:9 or 4:3 | 23.976/24 Hz progressive scan |
| | | 29.97/30 Hz progressive scan |
| | | 59.94/60 Hz Progressive scan |
| 640 × 480 (VGA, square pixel) | 4:3 | 23.976/24 Hz progressive scan |
| | | 29.97/30 Hz progressive scan |
| | | 59.94/60 Hz progressive scan |

The remaining 12 video formats are not HDTV format. These formats represent some improvements over analog NTSC and are referred to as standard-definition television (SDTV).¹ These are listed in [Table 18.2](#).

These definitions are fully supported by the technical specifications for the various formats as measured against the internationally accepted definition of HDTV established in 1989 by the ITU and the definitions cited by the FCC during the DTV standard development process. These formats cover a wide variety of applications, which include motion picture film, currently available HDTV production equipment, the NTSC television standard, and computers such as personal computers and workstations. However, there is no simple technique that can convert images from one pixel format and frame rate to another that achieve interoperability among film and the various worldwide television standards. For example, all low-cost computers use square pixels and progressive scanning while current television uses rectangular pixels and interlaced scanning. The video industry has paid a lot of attention to developing the format converting techniques. Some techniques such as de-interlacing and down/up conversion for format conversion have already been developed. It should be noted that the broadcasters, content providers, and service providers can use any one of these DTV formats. This results in a difficult problem for DTV receiver manufacturers who have to provide all kinds of DTV receivers to decode all these formats and then to convert the decoded signal to its particular display format. On the other hand, this requirement also gives receiver manufacturers the flexibility to produce a wide variety of products that have different functionality and cost, and the consumer's freedom to choose among them.

18.2.2.2 Compression Layer

The raw data rate of HDTV of $1920 \times 1080 \times 30 \times 16$ (16 bits/pixel corresponds to 4:2:2 color format) is about 1 Gbps. The function of compression layer is to compress the raw

data from about 1 Gbps to the data rate of approximately 19 Mbps to satisfy the 6 MHz spectrum requirement. This goal is achieved by using the main profile and high level of MPEG-2 video standard. Actually, during the development of Grand Alliance HDTV system, many research results have been adopted by the MPEG-2 standard at the same time. For example, the support for interlaced video format and the syntax for data partitioning and scalability. The ATSC DTV standard is the first and important application example of the MPEG-2 standard. The use of MPEG-2 video compression fundamentally enables ATSC DTV devices to interoperate with MPEG-1/2 computer multimedia applications directly at the compressed bitstream level.

18.2.2.3 Transport Layer

The transport layer is another important issue for interoperability. The ATSC DTV transport layer uses the MPEG-2 System Transport stream syntax. It is a fully compatible subset of the MPEG-2 transport protocol. The basic function of the transport layer is to define the basic format of data packets. The purposes of packetization include:

- packaging the data into the fixed-size cells or packets for forward error correction (FEC) encoding to protect the bit error due to the communication channel noise
- multiplexing the video, audio, and data of a program into a bitstream
- providing time synchronization for different media elements
- providing flexibility and extensibility with backward compatibility

The transport layer of ATSC DTV uses a fixed-length packet. The packet size is 188 bytes, consisting of 184 bytes of payload and 4 bytes of header. Within the packet header, the 13-bit packet identifier (PID) is used to provide the important capacity to combine the video, audio, and ancillary data stream into a single bitstream as shown in [Figure 18.1](#). Each packet contains only a single type of data (video, audio, data, program guide, etc.) identified by the PID.

This type of packet structure packetizes the video, audio, and auxiliary data separately. It also provides the basic multiplexing function that produces a bitstream including video, five-channel surround-sound audio, and an auxiliary data capacity. This kind of transport layer approach also provides complete flexibility to allocate channel capacity to achieve any mix among video, audio, and other data services. It should be noted that the selection of 188-packet length is a trade-off between reducing the overhead due to the transport header and increasing the efficiency of error correction. Also, one ATSC DTV packet can

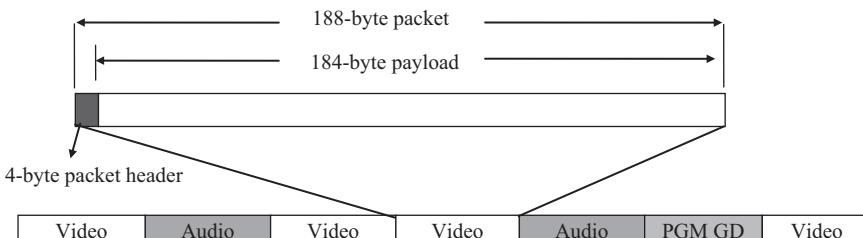


FIGURE 18.1

Packet structure of ATSC DTV transport layer.

be completely encapsulated with its header within four ATM packets by using 1 AAL byte per ATM header, leaving 47 usable payload bytes times 4 for 188 bytes. The details of the transport layer will be discussed in the chapter on MPEG systems.

18.2.2.3.1 Transmission Layer

The function of transmission layer is to modulate the transport bitstream into a signal that can be transmitted over 6 MHz analog channels. The ATSC DTV system uses a trellis-coded 8-level vestigial sideband (8-VSB) modulation technique to deliver approximately 19.3 Mbps in the 6 MHz terrestrial simulcast channel. VSB modulation inherently requires only processing the in-phase signal sampled at the symbol rate, thus reducing the complexity of the receiver and ultimately the cost of implementation. The VSB signal is organized in a data frame that provides a training signal to facilitate channel equalization for removing multipath distortion. However, from several field test results, the multipath distortion is still a serious problem of terrestrial simulcast receiving. The frame is organized into segments, each with 832 symbols. Each transmitted segment consists of one-synchronization byte (four symbols), 187 data bytes, and 20 R-S parity bytes. This corresponds to a 188-byte packet, which is protected by 20-byte R-S code. Interoperability at the transmission layer is required by different transmission media applications. The different media uses different modulation techniques now, such as QAM for cable and QPSK for satellite. Even for terrestrial transmission, European DVB systems use OFDM transmission. The ATV receivers will not only be designed to receive terrestrial broadcasts, but also the programs from cable, satellite, and other media.

18.3 Transcoding with Bitstream Scaling

18.3.1 Background

As indicated in the previous chapters, digital video signals exist everywhere in the format of compressed bitstreams. The compressed bitstreams of video signals are used for transmission and storage through different media such as terrestrial TV, satellite, cable, ATM network, and the Internet. The decoding of a bitstream can be implemented in either hardware or software. However, for high-bit-rate compressed video bitstreams of high-definition video signals, specially designed hardware is still the major decoding approach due to the speed limitation of current computer processors. The compressed bitstream as a new format of video signal is a revolutionary change of video industry since it enables many applications. For example, the coded video bitstreams can be decoded not only with DTVs or set-top boxes, but also with computers and mobile terminals such as cellular phones. Therefore, the problem of interactivity and integration of video data with computer, cellular, and television systems is relatively new and subject to a great deal of research worldwide. As the number of networks, types of devices, and content representation formats increase, interoperability between different systems and different networks is becoming more important. Thus, devices such as gateways, multipoint control units, and servers must be developed to provide a seamless interaction between content creation and consumption. Transcoding of video content is one key technology to make this possible. Generally speaking, transcoding can be defined as the conversion of one coded signal to another. In the earliest work on transcoding, the majority of interest focused on reducing

the bit rate to meet an available channel capacity. Additionally, researchers investigated conversions between constant bit-rate (CBR) streams and variable bit rate (VBR) streams to facilitate more efficient transport of video. As time moved on and mobile devices with limited display and processing power became a reality, transcoding to achieve spatial resolution reduction, as well as temporal resolution reduction, have also been studied. Furthermore, with the introduction of packet radio services over mobile access networks, error-resilience video transcoding has gained a significant amount of attention lately, where the aim is to increase the resilience of the original bit stream to transmission errors. Also, in some applications, the syntax conversion is needed between different compression standards such as JPEG, MPEG-1, MPEG-2, H.261, H.263, and H.264/AVC. In this section, we will focus on the topic of bit rate conversion since it finds wide application and the readers can extend the idea for other kinds of transcoding. Also, we limit ourselves to focus on the problem of scaling an MPEG CBR-encoded bitstream down to a lower CBR. A comprehensive survey of video transcoding can be found in Vetro (2003).

The basic function of bitstream scaling may be thought of as a black box, which passively accepts a pre-coded MPEG bitstream at the input and produces a scaled or size-reduced bitstream, which meets new constraints that are not known a-priori during the creation of the original pre-coded bitstream. The bitstream scaler is a transcoder, or filter, that provides a match between an MPEG source bitstream and the receiving load. The receiving load consists of the transmission channel, the destination decoder, and perhaps a destination storage device or display. The constraint on the new bitstream may be a bound by a variety of conditions. Among them, these conditions include the peak or average bit rate imposed by the communications channel, the total number of bits imposed by the storage device, and/or the variation of bit usage across pictures due to the amount of buffering available at the receiving decoder. While the idea of bitstream scaling has many concepts similar to those provided by the various MPEG-2 scalability profiles, the intended applications and goals differ. The scalable video coding (SVC) methods are aimed at providing encoding of source video into multiple service grades (that are predefined at the time of encoding) and multi-tiered transmission for increased signal robustness. The multiple bitstreams created by MPEG SVC are hierarchically dependent in such a way that by decoding an increasing number of bitstreams, higher service grades are reconstructed. Bitstream transcoding methods, in contrast, are primarily decoder/transcoder techniques for converting an existing pre-coded bitstream to another one that meets new rate constraints. Several applications that motivate bitstream scaling or transcoding include:

1. **Video On-Demand**—Consider a video on-demand (VOD) scenario wherein a video file-server includes a storage device containing a library of pre-coded MPEG bitstreams. These bitstreams in the library are originally coded at a high quality (e.g., studio quality). A number of clients may request retrieval of these video programs at one particular time. The number of users and the quality of video delivered to the users are constrained by the outgoing channel capacity. This outgoing channel, which may be a cable bus or an ATM trunk, for example, must be shared among the users who are admitted to the service. Different users may require different levels of video quality, and the quality of a respective program will be based on the fraction of the total channel capacity allocated to each user. To simultaneously accommodate a plurality of users, the video file-server must scale the stored pre-coded bitstreams to a reduced rate before it is delivered over the channel to respective users. The quality of the resulting scaled bitstream should not be significantly degraded compared to the quality of a hypothetical bitstream

so obtained by coding the original source material at the reduced rate. Complexity cost is not such a critical factor because only the file-server has to be equipped with the bitstream scaling hardware, not every user. Presumably, video service providers would be willing to pay a high cost for delivering the highest-possible-quality video at a prescribed bit rate.

As an option, a sophisticated video file-server may also perform scaling of multiple original pre-coded bitstreams jointly and statistically multiplex (Perkins and Arnstein 1995) the resulting scaled VBR bitstreams into the channel. By scaling the group of bitstreams jointly, statistical gains can be achieved. These statistical gains can be realized in the form of higher and more uniform picture quality for the same channel capacity. Statistical multiplexing over a DIRECTV transponder (Isnardi 1993) is one example of application of video statistical multiplexing.

2. Trick-play Track on Digital VTRs—In this application, the video bitstream is reduced to create a sidetrack on video tape recorders. This sidetrack contains very coarse quality video sufficient to facilitate trick-modes on the VTR (e.g., FF and REW at different speeds). Complexity cost for the bitstream scaling hardware is of significant concern in this application since the VTR is a mass consumer item subject to mass production.
3. Extended-Play Recording on Digital VTRs—In this application, video is broadcast to users' homes at a certain broadcast quality (~6 Mbps for standard-definition video and ~19 Mbps for high-definition video). With a bitstream scaling feature in their video tape recorders, users may record the video at a reduced rate, akin to extended play (EP) mode on today's VHS recorders, thereby recording a greater duration of video programs onto a tape at lower quality. Again, hardware complexity costs would be a major factor here.
4. Universal Multimedia Access (UMA): The concept of UMA is to enable access to any multimedia content over any type of network, such as Internet, Wireless LAN, or others, from any type of terminals with varying capabilities such as mobile phones, personal computers, and television sets (MPEG-21 2002). The primary function of UMA services is to provide the best QoS or user experience by either selecting appropriate content formats, adapting the content format directly to meet the playback environment, or adapting the content playback environment to accommodate the content. Towards the above goal, video transcoder can bridge the mismatch between the large amount of video data, bandwidth of communication channels, and capability of end-user terminals. The concept of UMA is illustrated in [Figure 18.2](#).

18.3.2 Basic Principles of Bitstream Scaling

As described previously, the idea of scaling an MPEG-2 compressed bitstream down to a lower bit rate is initiated by several applications. One problem is the criteria that should be used to judge the performances of an architecture that can reduce the size or rate of an MPEG-compressed bitstream. Two basic principles of bitstream scaling are: (1) the information in the original bitstream should be exploited as much as possible, and (2) the resulting image quality of the new bitstream with a lower bit rate should be as close as possible to a bitstream created by coding the original source video at the reduced rate. Here, we assume that for a given rate the original source is encoded in an optimal way. Of course, the implementation of hardware complexity also has to be considered.

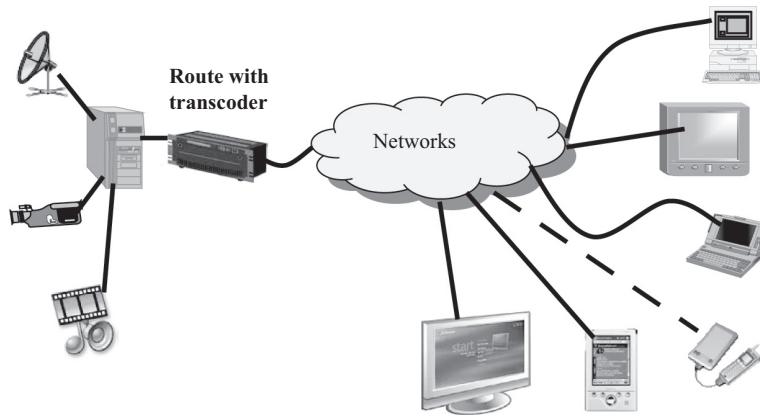


FIGURE 18.2
Concept of UMA.

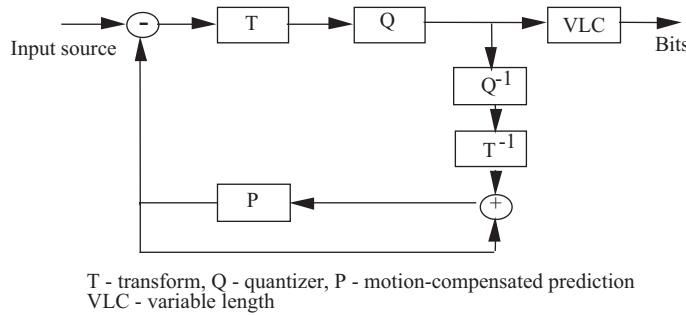


FIGURE 18.3
Simplified encoder structure.

Figure 18.3 shows a simplified encoding structure of MPEG encoding in which the rate control mechanism is not shown.

In this structure, a block of an image data is first transformed to a set of coefficients; the coefficients are then quantized with a quantizer step that is decided by the given bit rate budget, or number of bits assigned to this block. Finally, the quantized coefficients are coded in variable-length coding (VLC) to the binary format, which is called the bitstream or bits.

From this structure, it is obvious that the performance of changing the quantizer step will be better than cutting higher frequencies when the same amount of rate needs to be reduced. In the original bitstream, the coefficients are quantized with finer quantization steps that are optimized at the original high rate. After cutting the coefficients of higher frequencies, the rest of coefficients are not quantized with an optimal quantizer. In the method of re-quantization, all coefficients are re-quantized with an optimal quantizer that is determined by the reduced rate; the performance must be better than the one by cutting high frequencies to reach the reduced rate. The theoretical analysis is given in the appendix.

In the following, several different architectures that accomplish the bitstream scaling are discussed. The different methods have varying hardware implementation complexity, each having its own degree of tradeoff between required hardware and resulted image quality.

18.3.3 Architectures of Bitstream Scaling

Four architectures for bitstream scaling are discussed. Each of the scaling architectures described has its own particular benefits that are suitable for a particular application.

Architecture 1: The bitstream is scaled by cutting high frequencies.

Architecture 2: The bitstream is scaled by re-quantization.

Architecture 3: The bitstream is scaled by re-encoding the reconstructed pictures with motion vectors and coding decision modes extracted from the original high-quality bitstream.

Architecture 4: The bitstream is scaled by re-encoding the reconstructed pictures with motion vectors extracted from the original high-quality bitstream, but new coding decisions are computed based on reconstructed pictures.

Architectures 1 and 2 are considered for VTR applications such as trick-play modes and EP recording. Architectures 3 and 4 are considered for VOD and other applicable StatMux scenarios.

18.3.3.1 Architecture 1: Cutting AC Coefficients

A block diagram illustrating architecture 1 is shown in [Figure 18.4a](#). The method of reducing the bit rate in architecture 1 is based on cutting the higher-frequency coefficients. The incoming pre-coded CBR stream enters a decoder rate buffer. Following the top branch leading from the rate buffer, a VLD is used to parse the bits for the next frame in the buffer to identify all the variable-length codewords that correspond to AC coefficients used in that frame. No bits are removed from the rate buffer. The codewords are not decoded, but just simply parsed by the VLD parser to determine codeword lengths. The bit allocation analyzer accumulates these ac bit counts for every macroblock (MB) in the frame and creates an ac bit usage profile as shown in [Figure 18.4b](#). That is, the analyzer generates a running sum of ac DCT coefficient bits on a MB basis:

$$PV_n = \sum AC_BITS \quad (18.1)$$

where PV_n is the profile value of a running sum of AC codeword bits until to the MB N . In addition, the analyzer counts the sum of all coded bits for the frame, TB (total bits). After all MBs for the frame have been analyzed, a target value TV_{AC} of ac DCT coefficient bits per frame is calculated as:

$$TV_{AC} = PV_{LS} - \alpha * TB - B_{EX} \quad (18.2)$$

where TV_{AC} is the target value of AC codeword bits per frame, PV_{LS} is the profile value at the last MB, α is the percentage by which the pre-encoded bitstream is to be reduced, TB is the total bits, and B_{EX} is the number of bits by which the previous frame missed its desired target. The profile value of AC coefficient bits is scaled by the factor TV_{AC}/PV_{LS} . Multiplying each PV_n performs scaling by that factor to generate the linearly scaled profile shown in [Figure 18.4b](#). Following the bottom branch from the rate buffer, a delay is inserted equal to the amount of time required for the top branch analysis processing to be completed for the current frame. A second *VLD* parser accesses and removes all codeword bits from

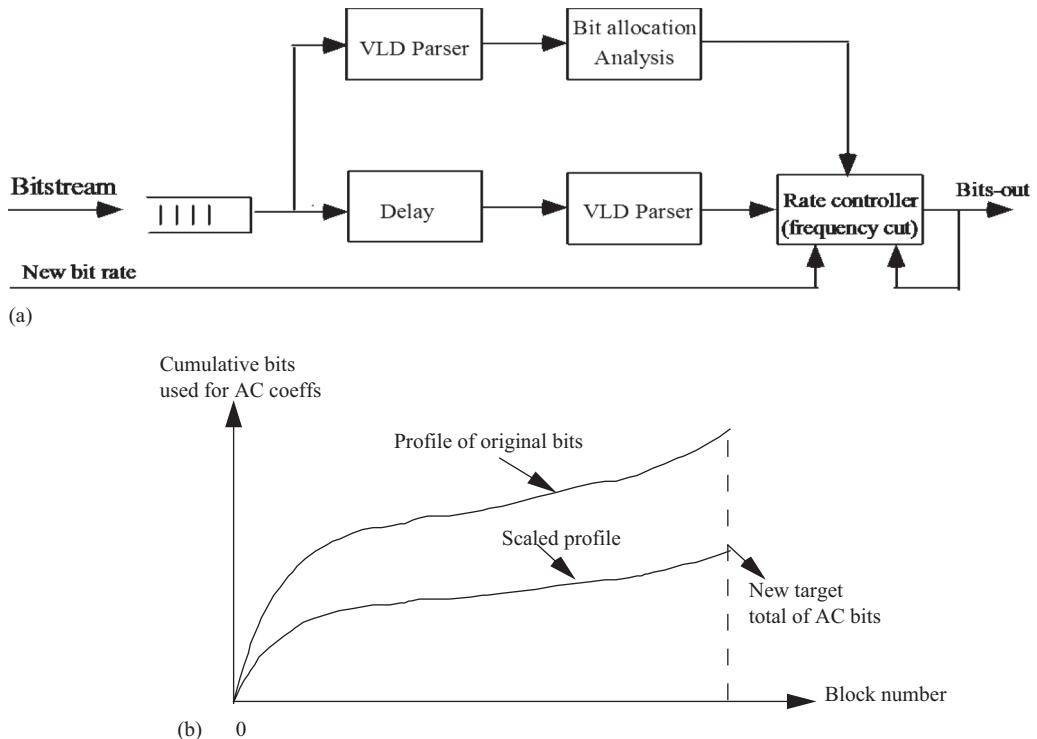
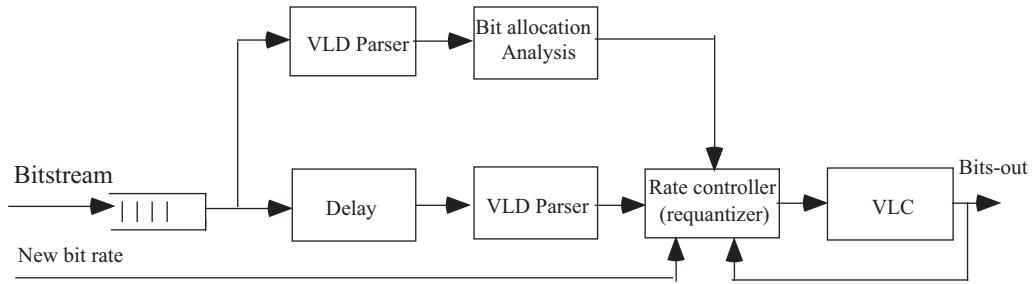


FIGURE 18.4
(a) Architecture 1: cutting high frequencies and (b) Profile map.

the buffer and delivers them to a rate controller. The rate controller receives the scaled target bit usage profile for the amount of ac bits to be used within the frame. The rate controller has memory to store all coefficients associated with the current MB it is operating on. All original codeword bits at a higher level than AC coefficients (i.e., all fixed-length header codes, motion vector codes, MB type codes, etc.) are held in memory and will be re-multiplexed with all AC codewords in that MB that have not been excised to form the outgoing scaled bitstream. The rate controller determines and flags in the MB codeword memory which AC codewords to keep and which to excise. AC codewords are accessed from the MB codeword memory in the order $AC_{11}, AC_{12}, AC_{13}, AC_{14}, AC_{15}, AC_{16}, AC_{21}, AC_{22}, AC_{23}, AC_{24}, AC_{25}, AC_{26}, AC_{31}, AC_{32}, AC_{33}$, etc., where AC_{ij} denotes the i -th AC codewords from j -th block in the MB if it is present. As the AC codewords are accessed from memory, the respective codeword bits are summed and continuously compared with the scaled profile value to the current MB, less the number of bits for insertion of end-of-block (EOB) codewords. Respective AC codewords are flagged as kept until the running sum of AC codewords bits exceeds the scaled profile value less EOB bits. When this condition is met, all remaining AC codewords are marked for being excised. This process continues until all MBs have their kept codewords reassembled to form the scaled bitstream.

18.3.3.2 Architecture 2: Increasing Quantization Step

Architecture 2 is shown in Figure 18.5. The method of bitstream scaling in architecture 2 is based on increasing the quantization step. This method requires additional de-quantizer/

**FIGURE 18.5**

Architecture 2: increasing quantization step.

quantizer and VLC hardware over the first method. Like the first method, it also makes a first VLD pass on the bitstream and obtains a similar scaled profile of target cumulative codeword bits vs. MB count to be used for rate control.

The rate control mechanism differs from this point on. After the second-pass VLD is made on the bitstream, quantized DCT coefficients are de-quantized. A block of finely quantized DCT coefficients is obtained as a result of this. This block of DCT coefficients is re-quantized with a coarser quantizer scale. The value used for the coarser quantizer scale is determined adaptively by making adjustments after every MB so that the scaled target profile is tracked as we progress through the MBs in the frame:

$$Q_N = Q_{NOM} + G * \left(\sum_{N-1} BU - PV_{N-1} \right) \quad (18.3)$$

where Q_N is the quantization factor for MB N , Q_{NOM} is an estimate of the new nominal quantization factor for the frame, $\sum_{N-1} BU$ is the cumulative number of coded bits up to MB $N-1$, and G is a gain factor that controls how tightly the profile curve is tracked through the picture. Q_{NOM} is initialized to an average guess value before the very first frame and updated for the next frame by setting it to Q_{LS} (the quantization factor for the last MB) from the frame just completed. The coarsely re-quantized block of DCT coefficients is variable-length-coded to generate the scaled bitstream. The rate controller also has provisions for changing some MB-layer codewords, such as the MB-type and coded-block-pattern, to ensure a legitimate scaled bitstream that conforms to MPEG-2 syntax.

18.3.3.3 Architecture 3: Re-encoding with Old Motion Vectors and Old Decisions

The third architecture for bitstream scaling is shown in [Figure 18.6](#). In this architecture, the motion vectors and MB coding decision modes are first extracted from the original bitstream, and at the same time the reconstructed pictures are obtained from the normal decoding procedure. Then the scaled bitstream is obtained by re-encoding the reconstructed pictures using the old motion vectors and MB decisions from the original bitstream. The benefits obtained from this architecture compared to full decoding and re-encoding is that no motion estimation and decision computation is needed.

18.3.3.4 Architecture 4: Re-encoding with Old Motion Vectors and New Decisions

Architecture 4 is a modified version of architecture 3 in which new MB decision modes are computed during re-encoding based on reconstructed pictures. The scaled bitstream

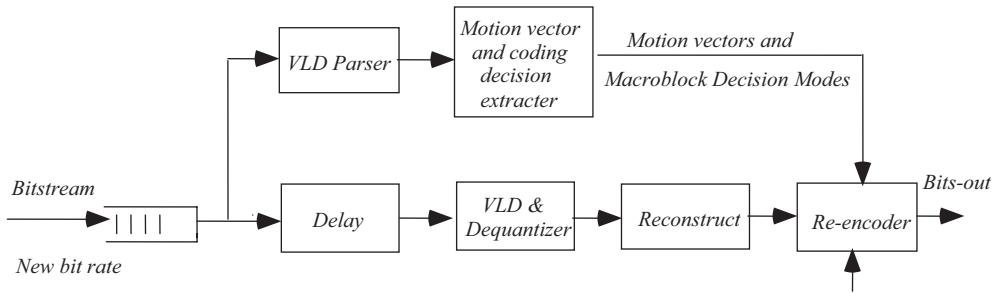


FIGURE 18.6
Architecture 3.

created this way is expected to yield an improvement in picture quality because the decision modes obtained from the high-quality original bitstream are not optimal for re-encoding at the reduced rate. For example, at higher rates the optimal mode decision for a MB is more likely to favor of bi-directional field motion compensation (MC) over forward frame MC. But at lower rates, only the opposite decision may be true. In order for the re-encoder to have the possibility of deciding on new MB coding modes, the entire pool of motion vectors of every type must be available. This can be supplied by augmenting the original high-quality bitstream with ancillary data containing the entire pool of motion vectors during the time it was originally encoded. It could be inserted into the user data every frame. For the same original bit rate, the quality of an original bitstream obtained this way is degraded compared to an original bitstream obtained from architecture 3 because the additional overhead required for the extra motion vectors steals away bits for actual encoding. However, the resulting scaled bitstream is expected to show quality improvement over the scaled bitstream from architecture 3 if the gains from computing new and more accurate decision modes can overcome the loss in original picture quality. [Table 18.3](#) outlines the hardware complexity savings of each of the three proposed architectures as compared to full decoding and re-encoding.

18.3.3.5 Comparison of Bitstream Scaling Methods

We have described four architectures for bitstream scaling that are useful for various applications as described in the introduction. Among the four architectures, architectures 1 and 2 do not require entire decoding and encoding loops or frame store memory for reconstructed pictures, thereby saving significant hardware complexity. However, video quality tends to degrade through the group-of-pictures until the next I-picture due to drift in the absence of decoder/encoder loops. For large scaling, say for rate reduction greater

TABLE 18.3

Hardware Complexity Savings over Full Decoding/Re-encoding

| Coding Method | Hardware Complexity Savings |
|----------------|---|
| Architecture 1 | No decoding loop, no DCT/IDCT, no frame store memory, no encoding loop, no quantizer/dequantizer, no MC, no VLC, simplified rate control. |
| Architecture 2 | No decoding loop, no DCT/IDCT, no frame store memory, no encoding loop, no MC, simplified rate control. |
| Architecture 3 | No motion estimation, no MB coding decisions. |
| Architecture 4 | No motion estimation. |

than 25%, architecture 1 produces poor-quality blocky pictures, primarily because many bits were spent in the original high-quality bitstream on finely quantizing the dc and other very low-order AC coefficients. Architecture 2 is a particularly good choice for VTR applications since it is a good compromise between the hardware complexity and reconstructed image quality. Architectures 3 and 4 are suitable for VOD server applications and other StatMux applications.

Appendix

In this analysis, we assume that the optimal quantizer is obtained by assigning the number of bits according to the variance or energy of the coefficients. It is slightly different from MPEG standard that will be explained later, but the principal concept is the same and the results will hold for the MPEG standard. We first analyze the errors caused by cutting high coefficients and increasing the quantizer step. The optimal bit assignment is given by Jayant and Noll (1984):

$$R_{k0} = R_{av0} + \frac{1}{2} \log_2 \frac{\sigma_k^2}{\left(\prod_{i=0}^{N-1} \sigma_i^2\right)^{1/N}}, \quad k = 0, 1, \dots, N-1 \quad (18.4)$$

where N is the number of coefficients in the block, R_{k0} is the number of bits assigned to the k -th coefficient, R_{av0} is the average number of bits assigned to each coefficient in the block, i.e., $R_{T0}=N \cdot R_{av0}$ is the total bits for this block under a certain bit rate, and σ_k^2 is the variance of k -th coefficient. Under the optimal bit assignment (18.3), the minimized average quantizer error, σ_{q0}^2 , is

$$\sigma_{q0}^2 = \frac{1}{N} \sum_{k=1}^{N-1} \sigma_{qk}^2 = \frac{1}{N} \sum_{k=1}^{N-1} 2^{-2R_{k0}} \sigma_k^2 \quad (18.5)$$

where σ_{qk}^2 is the quantizer error of k -th coefficient. According to (18.4), we have two major methods to reduce the bit rate, cutting high coefficients or decreasing the Rav, i.e., increasing the quantizer step. We are now analyzing the effects on the reconstructed errors caused due to the cut of bits using these methods. Assume that the number of the bits assigned to the block is reduced from R_{T0} to R_{T1} . Then the bits to be reduced, ΔR_1 , are equal to $R_{T0} - R_{T1}$.

In the case of cutting high frequencies, say the number of coefficients is reduced from N to M , then

$$R_{k0} = 0 \text{ for } K < M, \text{ and } \Delta R_1 = R_{T0} - R_{T1} = \sum_{k=M}^{N-1} R_{k0} \quad (18.6)$$

the quantizer error increased due to the cutting is

$$\begin{aligned} \Delta \sigma q_1^2 &= \sigma q_1^2 - \sigma q_0^2 = \frac{1}{N} \left(\sum_{k=0}^{M-1} 2^{-2R_{k0}} \cdot \sigma k^2 + \sum_{k=M}^{N-1} \sigma k^2 - \sum_{k=0}^{N-1} 2^{-2R_{k0}} \cdot \sigma k^2 \right) \\ &= \frac{1}{N} \left(\sum_{k=M}^{N-1} \sigma k^2 - \sum_{k=M}^{N-1} 2^{-2R_{k0}} \cdot \sigma k^2 \right) \\ &= \frac{1}{N} \sum_{k=M}^{N-1} (1 - 2^{-2R_{k0}}) \cdot \sigma k^2 \end{aligned} \quad (18.7)$$

where σ_{q1}^2 is the quantizer error after cutting the high frequencies.

In the method of increasing quantizer step, or decreasing the average bits, from R_{av0} to R_{av2} , assigned to each coefficient, the number of bits reduced for the block is

$$\Delta R_2 = R_{T0} - R_{T2} = N \cdot (R_{av0} - R_{av2}) \quad (18.8)$$

and the bits assigned to each coefficient become now

$$R_{k2} = R_{av2} + \frac{1}{2} \log_2 \frac{\sigma_k^2}{\left(\prod_{i=0}^{N-1} \sigma_i^2\right)^{1/N}}, k = 0, 1, \dots, N-1 \quad (18.9)$$

The corresponding quantizer error increased by the cutting bits is

$$\begin{aligned} \Delta \sigma_{q2}^2 &= \sigma_{q2}^2 - \sigma_{q0}^2 = \frac{1}{N} \left(\sum_{k=0}^{N-1} 2^{-2R_{k2}} \sigma k^2 - \sum_{k=0}^{N-1} 2^{-2R_{k0}} \cdot \sigma k^2 \right) \\ &= \frac{1}{N} \sum_{k=0}^{N-1} (2^{-2R_{k2}} - 2^{-2R_{k0}}) \cdot \sigma k^2 \end{aligned} \quad (18.10)$$

where σ_{q2}^2 is the quantizer error at the reduced bit rate.

If the same number of bits is reduced, i.e., $\Delta R_1 = \Delta R_2$, it is obvious that $\Delta \sigma_{q2}^2$ is smaller than $\Delta \sigma_{q1}^2$ since σ_{q2}^2 is the minimized value at the reduced rate. This implies that the performance of changing the quantizer step will be better than cutting higher frequencies when the same amount of rate needs to be reduced. It should be noted that in the MPEG video coding, more sophisticated bit assignment algorithms are used. First, different quantizer matrices are used to improve the visual perceptual performance. Second, different VLC tables are used to code the DC values and the AC transform coefficients and the run-length coding is used to code the pairs of the zero-run length and the values of amplitudes. However, in general, the bits are still assigned according to the statistical model that indicates the energy distribution of the transform coefficients. Therefore, the above theoretical analysis will hold for the MPEG video coding.

18.3.4 MPEG-2 to MPEG-4 Transcoding

In this subsection, we are going to indicate that there is another kind of transcoding, which is to convert the bitstream between standards. An example is the transcoder between MPEG-2 to MPEG-4. The technical detail of MPEG-4 will be introduced in [Chapter 18](#). Since we have not learnt the MPEG-4 yet, here we just introduce the concept of transcoding between MPEG-2 to MPEG-4. This concept can be extended to other standards.

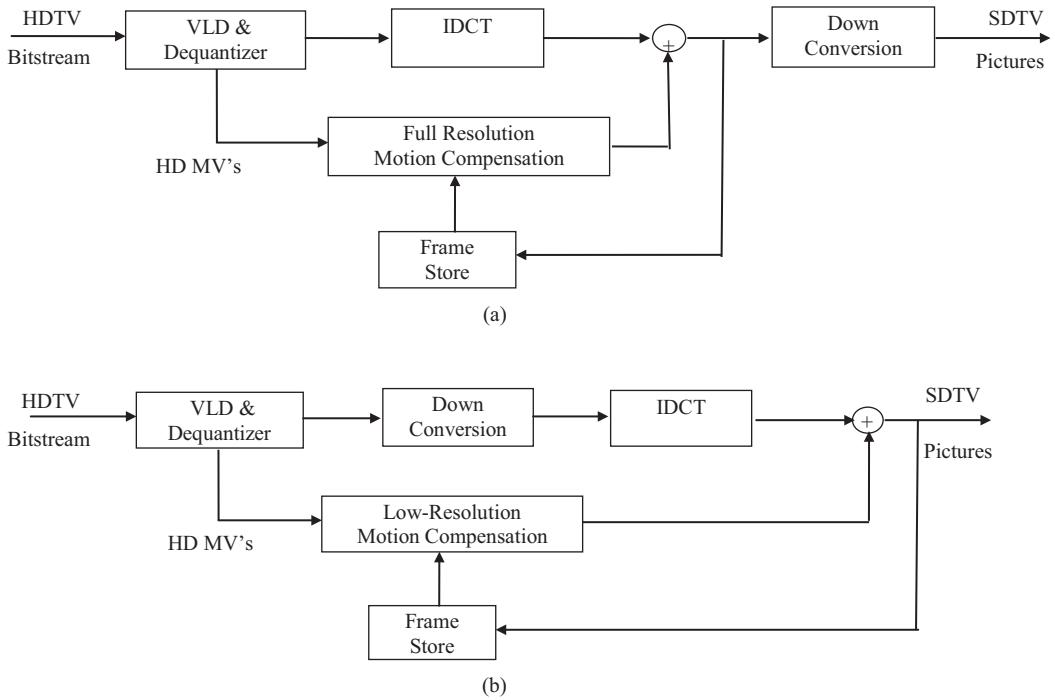
The transcoding methods themselves can be applied within the same syntax format as described in the previous section or between different syntax formats. Since MPEG-4 simple profile is adopted as the solution for mobile multimedia communications and a large amount of MPEG-1/2 contents is available, we focus our discussion on MPEG-2 to MPEG-4 transcoding. The transcoding from MPEG-2 to MPEG-4 is necessary and useful for allowing the mobile or PDA terminals to receive MPEG-2 compressed contents with their limited display size. In this section, we describe the principles and techniques used in the MPEG-2 to MPEG-4 video transcoder. The conversions include techniques for bit

rate reduction, spatial resolution down-sampling, temporal resolution down-scaling, and picture type change. The main difficulty of MPEG-2 to MPEG-4 transcoding is to perform transcoding on both bit rate reduction and spatial resolution reduction at the same time. The transcoding on bit rate reduction and spatial resolution reduction would cause serious error drift due to the change of predictive references. To address this problem, several issues have been investigated. First, an analysis of drift errors is provided to identify the sources of quality degradation when transcoding to a lower spatial resolution. Two types of drift error are considered: a reference picture error and error due to the non-commutative property of MC and down-sampling. To overcome these sources of error, several novel transcoding architectures are then presented. One architecture attempts to compensate for the reference picture error in the reduced resolution, while another architecture attempts to do the same in the original resolution. We present a third architecture that attempts to eliminate the second type of drift error and a final architecture that relies on an intra block refresh method to compensate all types of errors. In all these architectures, a variety of MB level conversions are required, such as motion vector mapping and texture down-sampling. These conversions are discussed in detail. Another important issue for the transcoder is rate control. This is especially important for the intra refresh architecture since it must find a balance between number of intra blocks used to compensate errors and the associated rate-distortion characteristics of the low-resolution signal. The complexity and quality of the architectures are compared. Based on the results, we find that the intra refresh architecture offers the best trade-off between quality and complexity, and is also the most flexible. After you learn MPEG-4 in [Chapter 18](#), you can find the technical detail of MPEG-2 to MPEG-4 transcoding in Yin et al. (2002).

18.4 Down-Conversion Decoder

18.4.1 Background

Digital video broadcasting has had a major impact in both academic and industrial communities. A great deal of effort has been made to improve the coding efficiency at the transmission side and offer cost-effective implementations in the overall end-to-end system. Along these lines, the notion of format conversion is becoming increasingly popular. On the transmission side, there are number of different formats that are likely candidates for digital video broadcast. These formats vary in horizontal, vertical, and temporal resolution. Similarly, on the receiving side, there are a variety of display devices that the receiver should account for. In this section, we are interested in the specific problem of how to receive an HDTV bitstream and display it at a lower spatial resolution. In the conventional method of obtaining a low-resolution image sequence, the HD bitstream is fully decoded then it is simply pre-filtered and sub-sampled (MPEG Test Model 5 1995). The block diagram of this system is shown in [Figure 18.7a](#); it will be referred to as a full-resolution decoder (FRD) with spatial down-conversion. Although the quality is very good, the cost is quite high due to the large memory requirements. As a result, low-resolution decoders (LRDs) have been proposed to reduce some of the costs (Ng 1993, Sun 1993, Boyce et al. 1995, Bao 1996). Although the quality of the picture will be compromised, significant reductions in the amount of memory can be realized; the block diagram for this system is shown in [Figure 18.7b](#). Here, incoming blocks are subject to down-conversion filters

**FIGURE 18.7**

Decoder Structures. (a) Block diagram of FRD with down-conversion in the spatial domain. The quality of this output will serve as a drift-free reference and (b) Block Diagram of LRD. Down-conversion is performed within the decoding loop and is a frequency domain process. MC is performed from a low-resolution reference using motion vectors that are derived from the full-resolution encoder. MC is a spatial domain process.

within the decoding loop. In this way, the down-converted blocks are stored into memory rather than the full-resolution blocks. To achieve a high-quality output with the LRD, it is important to take special care in the algorithms for down-conversion and MC. These two processes are of major importance to the decoder as they have significant impact on the final quality. Although a moderate amount of complexity within the decoding loop is added, the reductions in external memory are expected to provide significant cost savings, provided that these algorithms can be incorporated into the typical decoder structure in a seamless way.

As stated above, the filters used to perform the down-conversion are an integral part of the LRD. In Figure 18.7b, the down-conversion is shown to take place before the IDCT. Although the filtering is not required to take place in the DCT domain, we initially assume that it takes place before the adder. In any case, it is usually more intuitive to derive a down-conversion filter in the frequency domain rather than in the spatial domain; this has been described in Pang et al. (1996), Merhav and Bhaskaran (1997), and Mokry and Anastassiou (1994). The major drawback of these approaches is that high-frequency data is lost or not preserved very well. To overcome this, a method of down-conversion, which better preserves high-frequency data within the MB, has been reported in Bao (1996) and Vetro and Sun (1998a); this method is referred to as frequency synthesis.

Although the above statement of the problem has only mentioned filtering-based approaches to memory reduction within the decoding loop, readers should be aware that other techniques have also been proposed. For the most part, these approaches rely on

methods of embedded compression. For instance, in de With et al. (1998), the data being written to memory is quantized adaptively using a block-predictive coding scheme, then a segment of MBs is fit into a fixed-length packet. Similarly, in Yu et al. (1999), an adaptive min-max quantizer and edge detector is proposed. With this method, each MB is compressed to a fixed size to simplify memory access. Another simpler approach may be to truncate the 8-bit data to 7 or 6 bits. However, in this case, it is expected the drift would accumulate very fast and result in poor reconstruction quality. In Bruni et al. (1998), a vectors quantization method has been utilized, and in Lei (1999) a wavelet-based approach is described. Overall, these approaches offer exceptional techniques to reduce the memory requirements, but in most cases, the reconstructed video would still be a high-resolution signal. The reason is that compressed high-resolution data is stored in memory rather than the raw low-resolution data. For this reason, the remainder of this section emphasizes the filtering-based approach, in which the data stored in memory represent the actual low-resolution picture data.

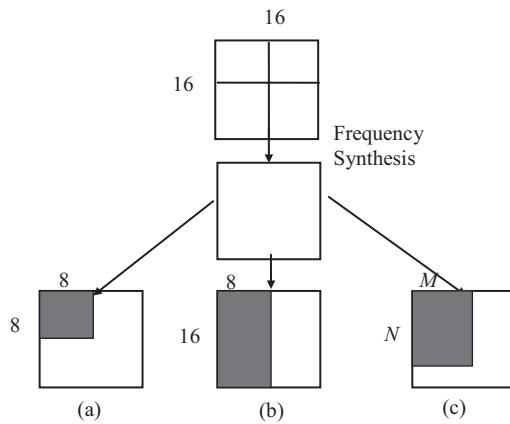
The main novelty of the system that we describe is the filtering that is used to perform the MC from low-resolution anchor frames. It is well known that prediction drift has been difficult to avoid. It is partly due to the loss of high-frequency data from the down-conversion and partly due to the inability to recover the lost information. Although prediction drift cannot be totally avoided in a LRD, it is possible to significantly reduce the effects of drift in contrast to simple interpolation methods. The solution that we described is optimal in the least-squares sense and is dependent on the method of down-conversion that is used (Vetro and Sun 1998b). In its direct form, the solution cannot be readily applied to a practical decoding scheme. However, it is shown that a cascaded realization is easily implemented into the FRD-type structure (Vetro et al. 1998c).

18.4.2 Frequency Synthesis Down-Conversion

The concept of frequency synthesis was first reported in Bao (1996) and later expanded upon in Vetro and Sun (1998b). The basic premise is to better preserve the frequency characteristics of a MB in comparison to simpler methods that extract or cut specified frequency components of an 8×8 block. To accomplish this, the four blocks of a MB are subject to a global transformation—this transformation is referred to as frequency synthesis. Essentially, a single frequency domain block can be realized using the information in the entire MB. From this, lower-resolution blocks can be achieved by cutting out the low-order frequency components of the synthesized block—this action represents the down-conversion process and is generally represented in the following way:

$$\tilde{A} = X A \quad (18.11)$$

where \tilde{A} denotes the original DCT MB, A denotes the down-converted DCT block, and X is a matrix that contains the frequency synthesis coefficients. The original idea for frequency synthesis down-conversion was to directly extract an 8×8 block from the 16×16 synthesized block in the DCT domain as shown in [Figure 18.8a](#). The advantage of doing this is that the down-converted DCT block is directly applicable to an 8×8 IDCT (for which fast algorithms exist). The major drawback with regard to computation is that each frequency component in the synthesized block is dependent on all of the frequency components in each of the 8×8 blocks, i.e., each synthesized frequency component is the result of a 256-tap filter. The major drawback with regard to quality is that interlaced video with field-based predictions should not be subject to frame-based filtering (Vetro and Sun 1998b).

**FIGURE 18.8**

Concept of frequency synthesis down-conversion, (a) 256-tap filter applied to every frequency component to achieve vertical and horizontal down-conversion by a factor of 2 frame-based filtering, (b) 16-tap filter applied to frequency components in the same row to achieve horizontal down-conversion by 2, picture structure is irrelevant, and (c) illustrates that the amount of synthesized frequency components that are retained is arbitrary.

If frame-based filtering is used, it becomes impossible to recover the appropriate field-based data that is required to make field-based predictions. In areas of large motion, severe blocking artefacts will result.

Obviously, the original approach would incur too much computation and quality degradation, so instead, the operations are performed separately and vertical down-conversion is performed on a field-basis. In Figure 18.8b, it is shown that a horizontal-only down-conversion can be performed. To perform this operation, a 16-tap filter is ultimately required. In this way, only the relevant row information is applied as the input to the horizontal filtering operation and the structure of the incoming video has no bearing on the down-conversion process. The reason is that the data in each row of a MB belongs to the same field, so the format of the output block will be unchanged. It is noteworthy that the set of filter coefficients is dependent on the particular output frequency index. For 1-D filtering, this means that the filters used to compute the second output index, for example, are different from those used to compute the fifth output index. Similar to the horizontal down-conversion, vertical down-conversion can also be applied as a separate process. As reasoned earlier, field-based filtering is necessary for interlaced video with field-based predictions.

However, since a MB consists of 8 lines for the even field and 8 lines for the odd field, and the vertical block unit is 8, frequency synthesis cannot be applied. Frequency synthesis is a global transformation and is only applicable when one wishes to observe the frequency characteristics over a larger range of data than the basic unit. Therefore, to perform the vertical down-conversion, we can simply cut the low-order frequency components in the vertical direction. This loss that we accept in the vertical direction is justified by the ability to perform accurate low-resolution MC that is free from severe blocking artefacts.

In the above, we have explained how the original idea to extract an 8×8 DCT block is broken down into separable operations. However, since frequency synthesis provides an expression for every frequency component in the new 16×16 block, it makes sense to generalize the down-conversion process so that decimation, which are multiples of 1/16, can be performed. In Figure 18.8c, a $M \times N$ block is extracted. Although this type of down-conversion filtering may not be appropriate before the IDCT operation and may not be appropriate for a bitstream containing field-based predictions, it may be applicable

elsewhere, e.g., as a spatial domain filter somewhere else in the system and/or for progressive material. To obtain a set of spatial domain filters, an appropriate transformation can be applied. In this way, Equation 18.8 is expressed as:

$$\tilde{a} = x\underline{a} \quad (18.12)$$

where the lowercase counterparts denote spatial equivalents. The expression that transforms X to x is derived in Appendix A.

18.4.3 Low-Resolution Motion Compensation

The focus of this section is to provide an expression for the optimal set of low-resolution MC filters given a set of down-conversion filters. The resulting filters are optimal in the least squares sense as they minimize the mean squared error between a reference block and a block obtained through low-resolution MC. The results that have been derived in Vetro and Sun (1998a) assume that a spatial domain filter, x , is applied to incoming MBs to achieve the down-conversion. The scheme shown in Figure 18.9a illustrates the process by which reference blocks are obtained. First, full-resolution MC is performed on MBs a , b , c , and d to yield \underline{h} . To execute this process, the filters $S_a^{(r)}$, $S_b^{(r)}$, $S_c^{(r)}$, and $S_d^{(r)}$ are used. Basically, these filters represent the masking/averaging operations of the MC in a matrix form. More on the composition of these filters can be found in the Appendix B. Once \underline{h} is obtained, it is down-converted to $\tilde{\underline{h}}$ via the spatial filter, x :

$$\tilde{\underline{h}} = x\underline{h} \quad (18.13)$$

The above block is considered to be the drift-free reference. On the other hand, in the scheme of Figure 18.9b (b), the blocks \underline{a} , \underline{b} , \underline{c} , and \underline{d} are first subject to the down-conversion filter, x , to yield the down-converted blocks, $\tilde{\underline{a}}$, $\tilde{\underline{b}}$, $\tilde{\underline{c}}$, and $\tilde{\underline{d}}$ respectively. Using these down-converted blocks as input to the low-resolution MC process, the following expression can be assumed:

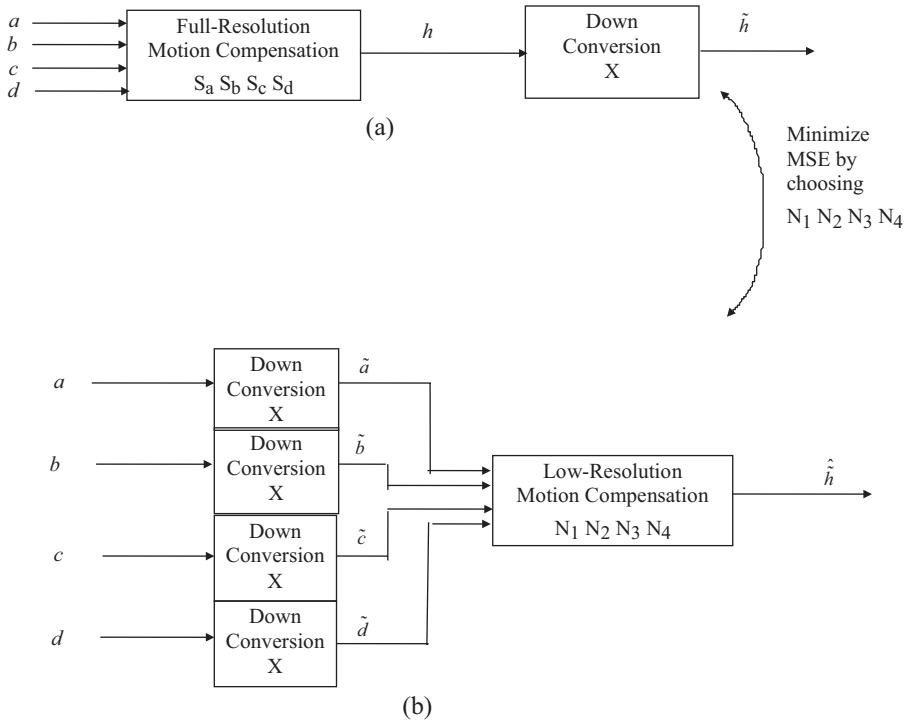
$$\hat{\underline{h}} = \begin{bmatrix} N_1 & N_2 & N_3 & N_4 \end{bmatrix} \begin{bmatrix} \tilde{\underline{a}} \\ \tilde{\underline{b}} \\ \tilde{\underline{c}} \\ \tilde{\underline{d}} \end{bmatrix} \quad (18.14)$$

Where, $N_k, k=1,2,3,4$ are the unknown filters that are assumed to perform the low-resolution MC, and $\hat{\underline{h}}$ is the low-resolution prediction. As in Vetro and Sun (1998a), these filters are solved for by differentiating the following objective function,

$$J\{N_k\} = \left\| \hat{\underline{h}} - \underline{h} \right\|^2 \quad (18.15)$$

with respect to each unknown filter and setting each result equal to zero. It can be verified that the optimal least square solution for these filters is given by:

$$\begin{aligned} N_1^{(r)} &= xS_a^{(r)}x^+; & N_2^{(r)} &= xS_b^{(r)}x^+ \\ N_3^{(r)} &= xS_c^{(r)}x^+; & N_4^{(r)} &= xS_d^{(r)}x^+ \end{aligned} \quad (18.16)$$

**FIGURE 18.9**

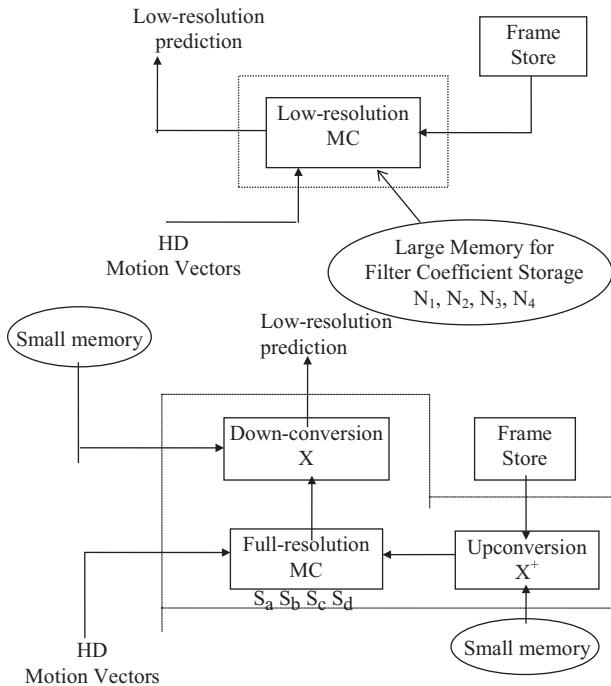
Comparison of decoding methods to achieve low-resolution image sequence. (a) FRD with spatial down-conversion and (b) LRD. The objective is to minimize the MSE between the two outputs by choosing N_1, N_2, N_3 , and N_4 for a fixed down-conversion.

where

$$x^+ = x^T (xx^T)^{-1} \quad (18.17)$$

is the Moore-Penrose Inverse (Lancaster and Tismenetsky 1985) for an $m \times n$ matrix with $m \leq n$. In the solution of (18.16), the superscript r is added to the filters, N_k , due to their dependency on the full-resolution MC filters. In using these filters to perform the low-resolution MC, the mean-squared-error between \tilde{h} and \hat{h} is minimized. It should be emphasized that equation (18.16) represents a generalized set of MC filters that are applicable to any $x, 8$ that operates on a single MB. For the special case of the 4×4 cut, these filters are equivalent to the ones that were determined in Mokry and Anastassiou (1994) to minimize the drift.

In Figure 18.10, two equivalent MC schemes are shown. However, for implementation purposes, the optimal MC scheme is realized in a cascade form rather than a direct form. The reason is that the direct form filters are dependent on the matrices, which perform full-resolution MC. Although these matrices were very useful in analytically expressing the full-resolution MC process, they require a huge amount of storage due to their dependency on the prediction mode, motion vector, and half-pixel accuracy. Instead, the three linear processes in (18.13) are separated, so that an up-conversion, full-resolution MC, and down-conversion can be performed. Although one may be able to guess such a scheme, we have proven here that it is an optimal scheme provided the up-conversion filter is Moore-Penrose inverse of the down-conversion filter. In Vetro and Sun (1998b), the optimal

**FIGURE 18.10**

Optimal low-resolution MC scheme: direct form (top) versus cascade form (bottom). Both forms yield equivalent quality, but vary significantly in the amount of internal memory.

MC scheme, which employs frequency synthesis, has been compared to a non-optimal MC scheme, which employs bilinear interpolation, and an optimal MC scheme, which employs the 4×4 cut down-conversion. Significant reductions in the amount of drift were realized by both optimal MC schemes over the method, which used bilinear interpolation as the method of up-conversion. But more importantly, a 35% reduction in the amount of drift was realized by the optimal MC scheme using frequency synthesis over the optimal MC scheme using the 4×4 cut.

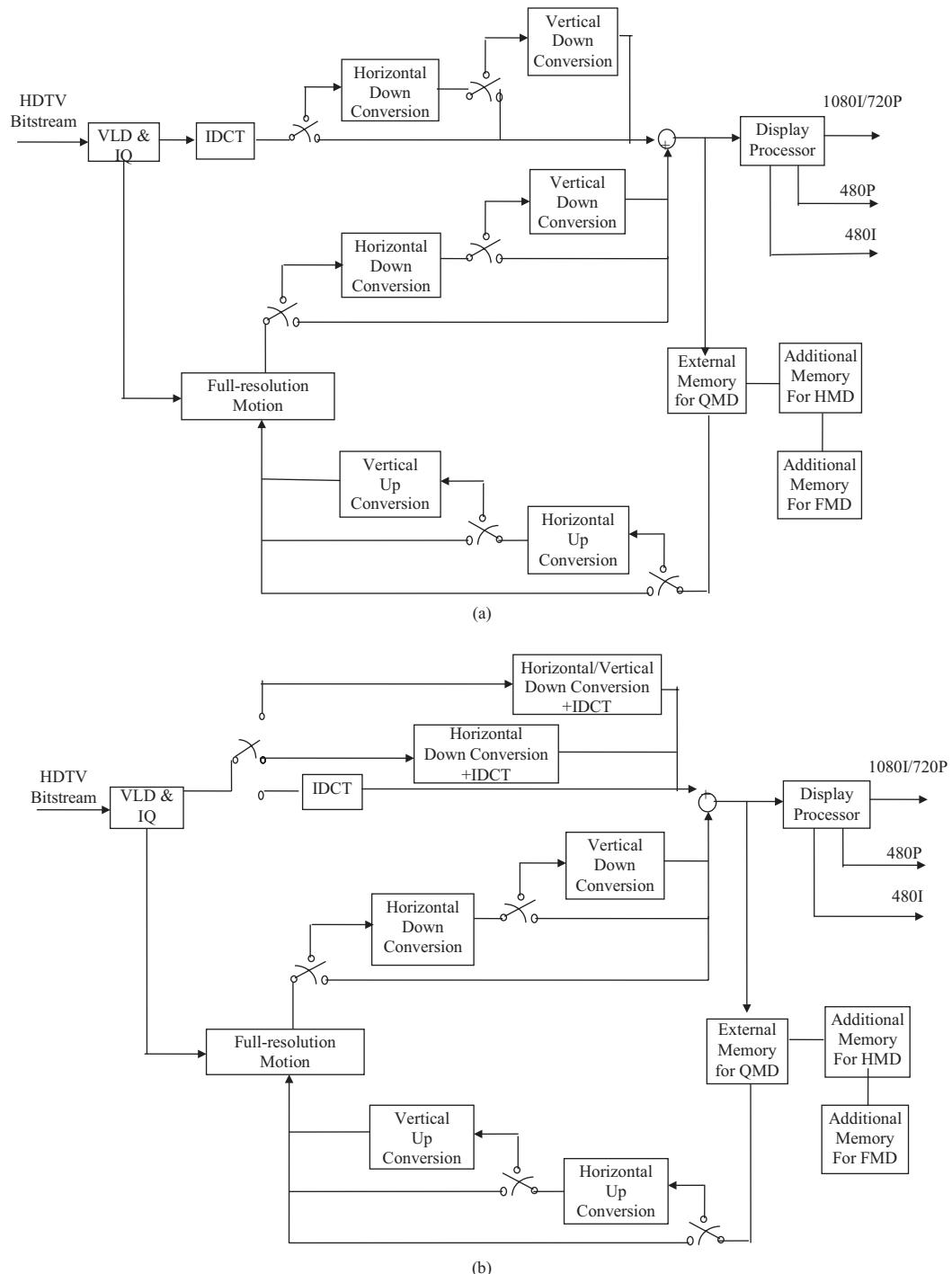
18.4.4 Three-Layer Scalable Decoder

In this section, we show how the key algorithms for down-conversion and MC are integrated into a three-layer scalable decoder. The central concept of this decoder is that three layers of resolution can be decoded using a decreased amount of memory for the lower-resolution layers. Also, regardless of which layer is being decoded, much of the logic can be shared. Three possible decoder configurations are considered: full-memory decoder (FMD), half-memory decoder (HMD), and quarter-memory decoder (QMD). The LRD configurations are based on the key algorithms, which were described for down-conversion and MC. In the following, three possible architectures are discussed that provide equal quality but vary in system level complexity. The first (ARCH1) is based on the LRD modeled in Figure 18.7b, the second (ARCH2) is very similar, but attempts to reduce the IDCT computation, while the third (ARCH3) is concerned with the amount of interface with an existing high-level decoder.

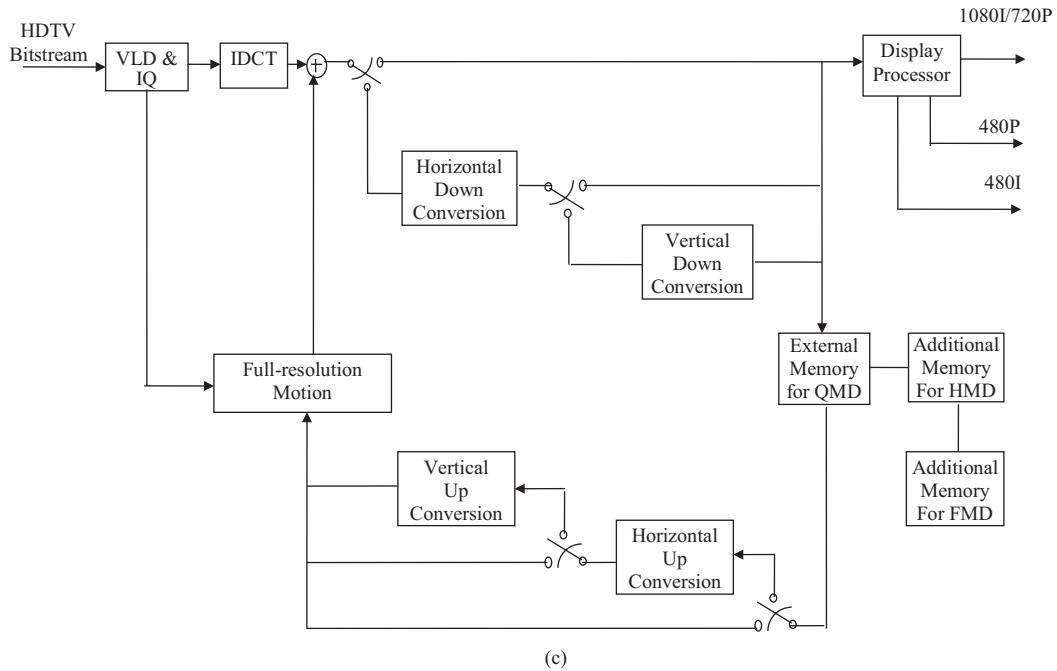
With regard to functionality, all of the architectures share similar characteristics. For one, an efficient implementation is achieved by arranging the logic in a hierarchical manner, i.e., employ separable processing. In this way, the FMD configuration is the simplest and serves as the logic core from which other decoder configurations are built on. In the HMD configuration, an additional horizontal down-conversion and up-conversion are performed. In the QMD configuration, all of the logic components from the HMD are utilized, such that an additional vertical down-conversion is performed after a horizontal down-conversion, and an additional vertical up-conversion is performed after a horizontal up-conversion. In summary, the logic for the HMD is built on the logic for the FMD, and the logic for the QMD is built on the logic of the HMD. The total system contains a moderate increase in logic, but HD bitstreams may be decoded to a lower resolution with a smaller amount of external memory. By simply removing external memory, lower layers can be achieved at a reduced cost.

The complete block diagram of ARCH1 is shown in [Figure 18.11a](#). The diagram shown here assumes two things: (i) the initial system model of a LRD from [Figure 18.7b](#) is assumed, and (ii) the down-conversions in the incoming branch are performed after the IDCT to avoid any confusion regarding MB format conversions in the DCT domain (Vetro and Sun 1998b). In looking at the resulting system, it is evident that full computation of the IDCT is required, and that two independent down-conversion operations must be performed. The latter is necessary so that low-resolution predictions are added to low-resolution residuals. Overall, the increase in logic for the added feature of memory savings is quite small. However, it is evident that ARCH1 is not the most cost-effective implementation, but it represents the foundation of previous assumptions, and allows us to better analyze the impact of the two modified architectures to follow.

In [Figure 18.11b](#), the block diagram of ARCH2 is shown. In this system, realizing that the IDCT operation is simply a linear filter reduces the combined computation for the IDCT and down-conversion. In the FMD, we know that a fast IDCT is applied separately to the rows and columns of an 8×8 block. For the HMD, our goal is to combine the horizontal down-conversion with the horizontal IDCT. In the 1-D case, an 8×16 matrix can represent the horizontal down-conversion, and an 8×8 matrix can represent the horizontal IDCT. Combining these processes such that the down-conversion operates on the incoming DCT rows first results in a combined 8×16 matrix. To complete the transformation, the remaining columns can then be applied to the fast IDCT. In the above description, computational savings is achieved in two places: first, the horizontal IDCT is fully absorbed into the down-conversion computation that must take place anyway, and second, the fast IDCT is utilized for a smaller number of columns. In the case of the QMD, these same principles can be used to combine the vertical down-conversion with the vertical IDCT. In this case, one must be aware of the MB type (field-DCT or frame-DCT) so that an appropriate filter can be applied. In contrast to the previous two architectures, ARCH3 assumes that the entire front-end processing of the decoder is used; it is shown in [Figure 18.6c](#). In this way, the adder is always a full-resolution adder, whereas in ARCH1 and ARCH2, the adder needed to handle all three layers of resolution. The major benefit of ARCH3 is that it does not require many interfaces with the existing decoder structure. The memory is really the only place where a new interface needs to be defined. Essentially, a down-conversion filtering may be applied before storing the data, and an up-conversion filtering may be applied, as the data is needed for full-resolution MC. This final architecture is similar in principle to the embedded compression schemes that were mentioned in the beginning of this section. The main difference is that the resolution of the data is decreased rather than compressed. This allows a simpler means of low-resolution display.

**FIGURE 18.11**

Block diagram of various three-layer scalable decoder architectures; all architectures provide equal quality with varying system complexity. (a) ARCH1, derived directly from block diagram of assumed LRD, (b) ARCH2, reduce computation of IDCT by combining down-conversion and IDCT filters, and (Continued)

**FIGURE 18.11 (Continued)**

(c) ARCH3, minimize interface with existing HL decoder by moving linear filtering for down-conversion outside of the adder.

18.4.5 Summary of Down-Conversion Decoder

A number of integrated solutions for a scalable decoder have been presented. Each decoder is capable of decoding directly to a lower resolution using a reduced amount of memory in comparison to the memory required by the high-level decoder. The method of frequency synthesis is successful in better preserving the high-frequency data within a MB and the filtering that is used to perform optimal low-resolution MC is capable of minimizing the drift. It has been shown that a realizable implementation can be achieved, such that the filters for optimal low-resolution MC are equivalent to an up-conversion, full-resolution MC, and down-conversion, where the up-conversion filters are determined by a Moore-Penrose inverse of the down-conversion. The amount of logic required by these processes is kept minimal since they are realized in a hierarchical structure. Since the down-conversion and up-conversion processes are linear, the architecture design is flexible in that equal quality can be achieved with varying levels of system complexity. The first architecture that we examined came from the initial assumptions that were made on the LRD, i.e., a down-conversion is performed before the adder. It was noted that a full IDCT computation was required and that a down-conversion must be performed in two places. As a result, a second architecture was presented to reduce the IDCT computation, and a third was presented to minimize the amount of interface with the existing high-level decoder. The major point here is that the advantages of ARCH2 and ARCH3 cannot be realized by a single architecture. The reason is that performing a down-conversion in the incoming branch reduces the IDCT computation, so a down-conversion must be performed after the full-resolution MC as well. In any case, equal quality is offered by each architecture and the quality is of commercial grade.

Appendix A: DCT-to-Spatial Transformation

Our objective in this section is to express the following DCT domain relationship:

$$\tilde{A}(k,l) = \sum_{p=0}^{M-1} \sum_{q=0}^{N-1} [X_{k,l}(p,q)A(p,q)] \quad (18.18)$$

as

$$\tilde{a}(i,j) = \sum_{s=0}^{M-1} \sum_{t=0}^{N-1} [x_{i,j}(s,t)a(s,t)] \quad (18.19)$$

where \tilde{A} and \tilde{a} are the DCT and spatial output, A and a are the DCT and spatial input, and X and x are the DCT and spatial filters, respectively. By definition, the $M \times N$ DCT transform is defined by:

$$A(k,l) = \sum_{i=0}^{M-1} \sum_{j=0}^{N-1} a(i,j)\psi_k^M(i)\psi_l^N(j) \quad (18.20)$$

and its inverse, the $M \times N$ IDCT by,

$$a(i,j) = \sum_{k=0}^{M-1} \sum_{l=0}^{N-1} A(k,l)\psi_k^M(i)\psi_l^N(j) \quad (18.21)$$

where the basis function is given by,

$$\psi_k^N = \sqrt{\frac{2}{N}}\alpha(k)\cos\left(\frac{2i+1}{2N}k\pi\right) \quad (18.22)$$

and

$$\alpha(k) = \begin{cases} \frac{1}{\sqrt{2}} & \text{for } k = 0; \\ 1 & \text{for } k \neq 0. \end{cases} \quad (18.23)$$

Substituting (18.22) into the expression for the IDCT yields,

$$\begin{aligned} \tilde{a}(i,j) &= \sum_{k=0}^{M-1} \sum_{l=0}^{N-1} \psi_k^M(i)\psi_l^N(j) \cdot \left[\sum_{p=0}^{M-1} \sum_{q=0}^{N-1} X_{k,l}(p,q)A(p,q) \right] \\ &= \sum_{p=0}^{M-1} \sum_{q=0}^{N-1} A(p,q) \cdot \left[\sum_{k=0}^{M-1} \sum_{l=0}^{N-1} X_{k,l}(p,q)\psi_k^M(i)\psi_l^N(j) \right] \end{aligned} \quad (18.24)$$

Substituting the DCT definition into the above gives the following,

$$\tilde{a}(i,j) = \sum_{p=0}^{M-1} \sum_{q=0}^{N-1} \left[\sum_{s=0}^{M-1} \sum_{t=0}^{N-1} a(s,t)\psi_p^M(s)\psi_q^N(t) \right] \sum_{k=0}^{M-1} \sum_{l=0}^{N-1} \left[X_{k,l}(p,q)\psi_k^M(i)\psi_l^N(j) \right] \quad (18.25)$$

Finally, equation (18.16) can be formed with,

$$x_{i,j}(s,t) = \sum_{k=0}^{M-1} \sum_{l=0}^{N-1} \psi_k^M(i) \cdot \psi_l^N(j) \left[\sum_{p=0}^{M-1} \sum_{q=0}^{N-1} (X_{k,l}(p,q) \cdot \psi_p^M(s) \psi_q^N(t)) \right] \quad (18.26)$$

and the transformation is fully defined.

Appendix B: Full-Resolution Motion Compensation in Matrix Form

In 2D, a motion-compensated MB may have contributions from at most 4 MBs per motion vector. As noted in [Figure 18.12](#), MBs *a*, *b*, *c*, and *d* include four 8×8 blocks each. These sub-blocks are raster-scanned so that each MB can be represented as a vector. According to the motion vector, (dx, dy) , a local reference, (y_1, y_2) , is computed to indicate where the origin of the motion-compensated block is located; the local reference is determined by:

$$\begin{aligned} y_1 &= dy - 16 \cdot [\text{Integer}(dy / 16) - \gamma(dy)] \\ y_2 &= dx - 16 \cdot [\text{Integer}(dx / 16) - \gamma(dx)] \end{aligned} \quad (18.27)$$

where,

$$\gamma(d) = \begin{cases} 1, & \text{if } d < 0 \quad \text{and} \quad d \bmod 16 = 0 \\ 0, & \text{otherwise.} \end{cases} \quad (18.28)$$

The reference point for this value is the origin of the upper-left-most input MB. With this, the motion-compensated prediction may be expressed as,

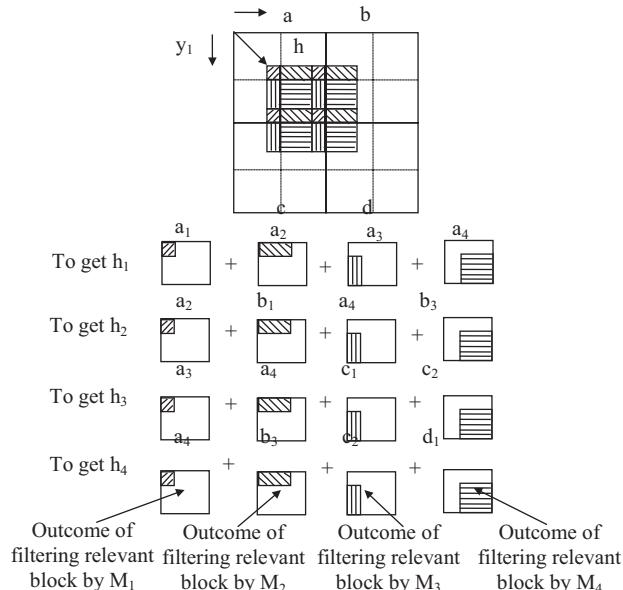


FIGURE 18.12

Relationship between the input and output blocks of the MC process in the FRD.

$$\underline{h} = \begin{bmatrix} \underline{h}_1 \\ \underline{h}_2 \\ \underline{h}_3 \\ \underline{h}_4 \end{bmatrix} = \begin{bmatrix} S_a^{(r)} & S_b^{(r)} & S_c^{(r)} & S_d^{(r)} \end{bmatrix} \cdot \begin{bmatrix} \underline{a} \\ \underline{b} \\ \underline{c} \\ \underline{d} \end{bmatrix}; r = 1, 2, 3, 4 \quad (18.29)$$

As an example, [Figure 18.12](#) considers $(y_1, y_2) \in [0, 7]$, which implies that $r = 1$. In this case the MC filters are given by:

$$S_a^{(1)} = \begin{bmatrix} M_1 & M_2 & M_3 & M_4 \\ 0 & M_1 & 0 & M_3 \\ 0 & 0 & M_1 & M_2 \\ 0 & 0 & 0 & M_1 \end{bmatrix}, \quad S_b^{(1)} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ M_2 & 0 & M_4 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & M_2 & 0 \end{bmatrix},$$

$$S_c^{(1)} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ M_3 & M_4 & 0 & 0 \\ 0 & M_3 & 0 & 0 \end{bmatrix}, \quad S_d^{(1)} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ M_4 & 0 & 0 & 0 \end{bmatrix} \quad (18.30)$$

In the above equations, the M_1 , M_2 , M_3 , and M_4 matrices operate on the relevant 8×8 blocks of a , b , c , and d . Their elements will vary according to the amount of overlap as indicated by (y_1, y_2) and the type of prediction. The type of prediction may be frame-based or field-based and is predicted with half-pixel accuracy. As a result, the matrices $S_a^{(r)}$, $S_b^{(r)}$, $S_c^{(r)}$, and $S_d^{(r)}$ are extremely sparse and may only contain non-zero values of 1, $1/2$, and $1/4$. For different values of (y_1, y_2) the configuration of the above matrices will change: $y_1 \in [0, 7]$ and $y_2 \in [8, 15]$ implies $r = 2$; $y_1 \in [8, 15]$ and $y_2 \in [0, 7]$ implies $r = 3$; and $y_1, y_2 \in [8, 15]$ implies $r = 4$. The resulting matrices can easily be formed using the concepts illustrated in [Figure 18.12](#).

18.5 Error Concealment

18.5.1 Background

Practical communications channels available for delivery of compressed digital video are characterized by occasional bit-error and/or packet loss, although the actual impairment mechanism varies widely with the specific medium under consideration. The class of decoder error concealment schemes described here is based on identification and predictive replacement of picture regions affected by bit-error or data loss. It is noted that this approach is based on conversion (via appropriate error/loss detection mechanisms) of the transmission medium into an erasure channel in which all error or loss events can be identified in the received bit-stream. In a block-structured compression algorithm such as MPEG, all channel impairments are manifested as erasures of video units (such as MPEG MBs or slices). Concealment at the decoder is then based on exploiting temporal and spatial picture redundancy to obtain an estimate of erased picture areas. The efficiency of error concealment depends on redundancies in pictures and on redundancies in the compressed

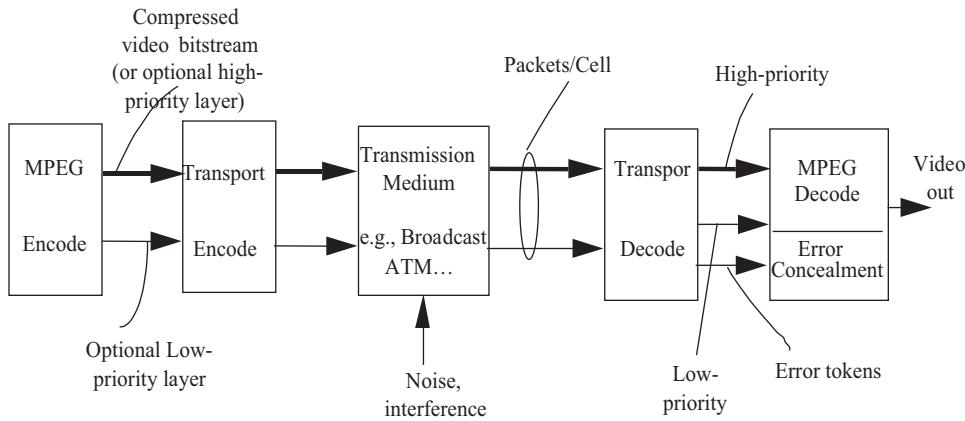


FIGURE 18.13
System block diagram of visual communication system.

bitstream that are not removed by source coding. Block compression algorithms do not remove a considerable amount of inter-block redundancies, such as structure, texture, and motion information about objects in the scene.

To be more specific, error resilience for compressed video can be achieved through the addition of suitable transport and error concealment methods, as outlined in the system block diagram shown in [Figure 18.13](#).

The key elements of such a robust video delivery system are outlined below:

- The video signal is encoded using an appropriate video compression syntax such as MPEG. Note that we have restricted consideration primarily to the practical case in which the video compression process itself is not modified, and robustness is achieved through additive transport and decoder concealment mechanisms (except for I-frame motion described in [Section 4.3](#)). This approach simplifies encoder design, since it separates media-independent video compression functions from media-dependent transport operations. On the receiver side, although a similar separation is substantially maintained, the video decoder must be modified to support an “error token” interface and error concealment functionality.
- Compressed video data is organized into a systematic data structure with appropriate headers for identification of the temporal and spatial pixel-domain location of encoded data (Joseph et al. 1992). When an erroneous/lost packet is detected, these video units serve as resynchronization points for resumption of normal decoding, while the headers provide a means for precisely locating regions of the picture that were not correctly received. Note that two-tier systems may require additional transport level support for high- and low-priority (HP/LP) resynchronization (Siracusa et al. 1993).
- The video bitstream may optionally be segregated into two layers for prioritized transport (Joseph et al. 1992a, 1992b, Siracusa et al. 1993, Ghanbari 1989, Kishino et al. 1989, Karlsson and Vetterli 1989, Zdepski et al. 1989) when a high degree of error resilience is required. Note that separation into high and low priorities may be achieved either by using a hierarchical (layered) compression algorithm (Siracusa et al. 1993, Ghanbari 1989) or by direct codeword parsing

(Zdepski et al. 1989, 1990). Note that both these layering mechanisms have been accepted for standardization by MPEG-2 (1995).

- Once the temporal and spatial location(s) corresponding to lost or incorrectly received packets is determined by the decoder, it will execute an error concealment procedure for replacement of lost picture areas with subjectively acceptable material estimated from available picture regions (Jeng and Lee 1991, Harthanck et al. 1986, Wang and Zhu 1991). Generally, this error concealment procedure will be applied to all erased blocks in one-tier (single priority) transmission systems, while for two-tier (HP/LP) channels the concealment process may optionally ignore loss of LP data.
- In the following sub-sections, the technical detail of some commonly used error concealment algorithms is provided. Specifically, we focus on the recovery of codeword errors and errors that affect the pixels within a MB.

18.5.2 Error Concealment Algorithms

In general, design of specific error concealment strategies depends on the system design. For example, if two-layered transmission is used, the receiver should be designed to conceal HP error and LP error with different strategies. Moreover, if some redundancy ("steering information") could be added to the encoder the concealment could be more efficient. However, we first assume that the encoder is defined for maximum compression efficiency, and that concealment is only performed in the receiver. It should be noted that some exemptions exist for this assumption. These exemptions include the use of I-frame motion vectors, scalability concealment, and limitation of slice length (in order to perform acceptable concealment in the pixel domain the limitation of slice length exists, i.e., the length of slices cannot be longer than one row of picture). [Figure 18.14](#) shows a block diagram of a generic one/two-tier video decoder with error concealment.

Note that the figure shows two stages of decoder concealment in the codeword domain and pixel domain, respectively. Codeword domain concealment, in which locally generated decodable codewords (e.g., B-picture motion vectors, EOB code, etc.) are inserted into the bit-stream, is convenient for implementation of simple temporal replacement functions (which in principle can also be performed in the pixel domain). The second stage of pixel

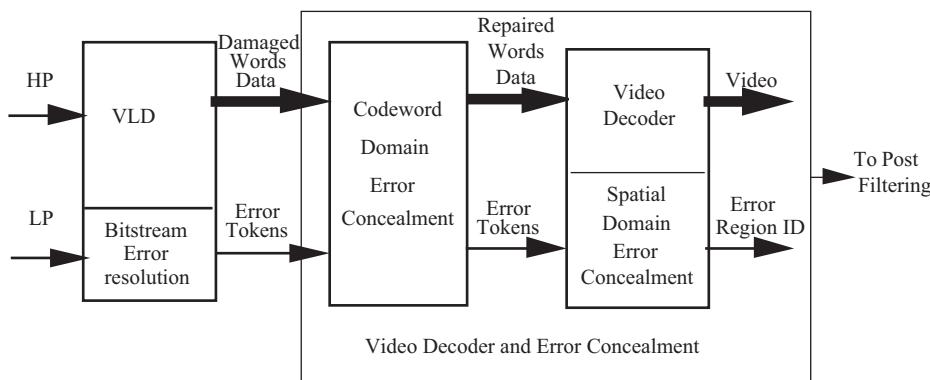


FIGURE 18.14

MPEG video decoder with error concealment.

domain processing is for temporal and spatial operations not conveniently done in the codeword domain. Advanced spatial processing will generally have to be performed in the pixel domain, although limited codeword domain options can also be identified.

18.5.2.1 Codeword Domain Error Concealment

The codeword domain concealment receives video data and error tokens from the transport processor/variable-length decoder (VLD). Under normal conditions, no action is taken and the data is passed along to the video decoder. When an error token is received, damaged data is repaired to the extent possible by insertion of locally generated codewords and resynchronization codes. An error region ID is also created to indicate the image region to be concealed by subsequent pixel domain processing. Two mechanisms have been used in codeword domain error concealment: neglect the effect of lost data by declaring an EOB or replace the lost data with a pseudo code to handle the MB-types or other VLC codes. If high-level data such as dc or MB header is lost, the codeword domain concealment with pseudo codes can only provide signal resynchronization (decodability) and replaces the image scene with a fixed gray level in the error region. Obviously, further improvement is needed in the video decoder. This task is implemented with the error concealment in the video decoder. It is desirable to replace erased I- or P-picture regions with a reasonably accurate estimate to minimize the impact of frame-to-frame propagation.

18.5.2.2 Spatio-temporal Error Concealment

In general, two basic approaches are used for spatial domain error concealment: temporal replacement and spatial interpolation. In temporal replacement, as shown in [Figure 18.15](#), the spatially corresponding ones in the previously decoded data with MC replace the damaged blocks in the current frame if motion information is available. This method exploits temporal redundancy in the reconstructed video signals and provides satisfactory results in areas with small motion and for which motion vectors are provided. If motion information is lost, this method will fail in the moving areas. In the method of spatial interpolation as shown in [Figure 18.16](#), the lost blocks are interpolated by the data from the adjacent non-error blocks with maximally smooth reconstruction criteria or other techniques.

In this method, the correlation between adjacent blocks in the received and reconstructed video signals is exploited. However, severe blurring will result from this method if data in adjacent blocks are also lost. In an MPEG decoder, temporal replacement outlined above is based on previously decoded anchor (I, P) pictures that are available in the frame memory.

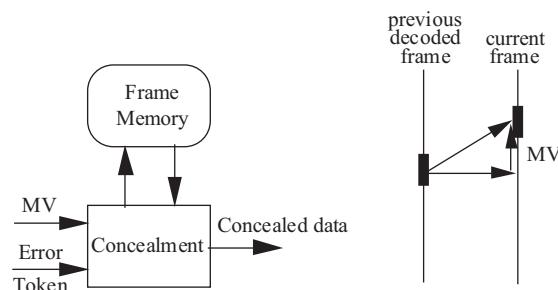
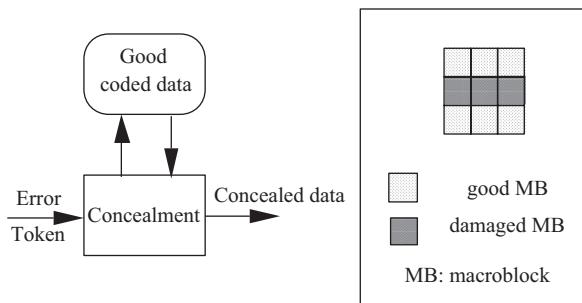


FIGURE 18.15

Error concealment uses temporal replenishment with MC.

**FIGURE 18.16**

Error concealment uses spatial interpolation with the data from good neighbors.

If motion vectors corresponding to pixels in the erasure region can also be estimated, this temporal replacement operation can be improved via MC. Also, in the MPEG decoder, groups of video pixels (blocks, MBs, or slices) are separately decoded, so that pixel values and motion information corresponding to adjacent picture regions are generally available for spatial concealment. However, estimation from horizontally adjacent blocks may not always be useful since cell-loss tends to affect a number of adjacent blocks (due to the MPEG and ATM data structures); also, differential encoding between horizontally adjacent blocks tends to limit the utility of data obtained from such neighbors. Therefore, most of the useable spatial information will be located in blocks above or below the damaged region. That is, vertical processing/concealment is found to be most useful due to the transmission order of the data.

For I-pictures, the damaged data can be reconstructed by either temporal replacement from the previously decoded anchor frame or by spatial interpolation from good neighbors. These two methods will be discussed later. For P- and B-pictures, the main strategy to conceal the lost data is to replace the region with pixels from the corresponding (and possibly motion-compensated) location in the previously decoded anchor. In this replacement, the motion vectors play a very important role. In other words, if “good” estimates of motion information can be obtained, its use may be the least noticeable correction. Since DPCM coding for motion vectors only exploited the correlations between the horizontally neighboring MBs, the redundancy between the vertical neighborhood still exists after encoding. Therefore, the lost motion information can be estimated from the vertical neighbors. In the following, three algorithms that have been developed for error concealment in the video decoder are described.

Algorithm 1: Spatial interpolation of missing I-picture data and temporal replacement for P and B-pictures with MC (Sun et al. 1992)

For I-pictures, dc values of damaged block are replaced by the interpolation from the closest top and bottom good neighbors; the AC coefficients of those blocks are synthesized from the dc values of the surrounding neighboring blocks.

For P-pictures, the previously decoded anchor frames with MC replace the lost blocks. The lost motion vectors are estimated by interpolation of the ones from the top and bottom MBs. If motion vectors in both top and bottom MBs are not available, zero motion vectors are used. The same strategy is used for B-pictures; the only difference is that the closest anchor frame is used. In other words, the damaged

part of the B-picture could be replaced by either the forward or backward anchor frame, depending on its temporal position.

Algorithm 2: Temporal replacement of missing I-picture data and temporal replacement for P and B-pictures with top MC

For I-pictures, the damaged blocks are replaced with the co-located ones in the previously decoded anchor frame.

For P- and B-pictures, the closest previously decoded anchor frame replaces the damaged part with MC as in the Algorithm 1. The only difference is that the motion vectors are estimated only from the closest top MB instead of interpolation of top and bottom motion vectors. This makes the implementation of this scheme much easier. If these motion vectors are not available then zero motion vectors are used.

In the above two algorithms, the damaged blocks in an I-picture (anchor frame) are concealed by two methods: temporal replacement and spatial interpolation. Temporal replacement is able to provide high-resolution image data to substitute for lost data; however, in motion areas, a big difference might exist between the current intra-coded frame and the previously decoded frame. In this case, temporal replacement will produce large shearing distortion unless some motion-based processing can be applied at the decoder. However, this type of processing is not generally available since it is a computationally demanding task to locally compute motion trajectories at the decoder. In contrast, the spatial interpolation approach synthesizes lost data from the adjacent blocks in the same frame. Therefore, the intra-frame redundancy between blocks in the same frame, while the potential problem of severe blurring due to insufficient high-order AC coefficients for the active areas. To alleviate this problem, an adaptive concealment strategy can be used as a compromise; this is described in algorithm 3.

Algorithm 3: Adaptive spatio-temporal replacement of missing I-picture data and temporal replacement with MC for P and B-pictures

For I-pictures, the damaged blocks are concealed with temporal replacement or spatial interpolation according to the decision made by the top and bottom MBs, which is shown in [Figure 18.7](#). The decision of which concealment method to use will be based on the more cheaply obtained measures of image activity from the neighboring top and bottom MBs. One candidate for the decision processor is to make the decision based on prediction error statistics measured in the neighborhood. The decision region is shown in [Figure 18.16](#), where:

$$\begin{aligned} \text{VAR} &= E[(x - \hat{x})^2], \\ \text{VAROR} &= E[x^2] - \mu^2 \end{aligned} \tag{18.31}$$

and x is the neighboring good MB data, \hat{x} is the data of the corresponding MB in the previously decoded frame at the co-located position, and μ is the average value of the neighboring good MB data in the current frame. One can appreciate that VAR is indicative of the local motion and VAROR of the local spatial detail. If $\text{VAR} > \text{VAROR}$ and $\text{VAR} > T$, where T is a preset threshold value that is set to 5 in the experiments, the concealment method is spatial interpolation; if $\text{VAR} < \text{VAROR}$ or $\text{VAR} < T$, the concealment method is temporal replacement ([Figure 18.17](#)).

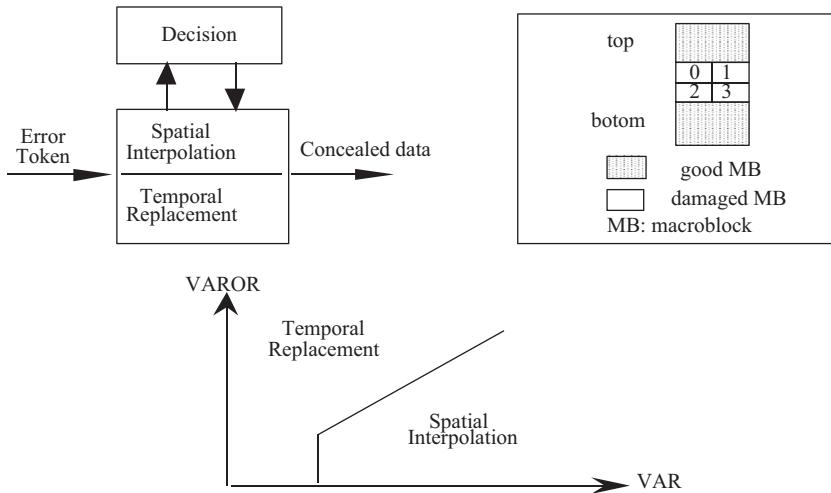


FIGURE 18.17

Adaptive error concealment strategy.

It should be noted that the concealment for luminance is performed on a block basis instead of MB basis, while the chrominance is still on the MB basis. The detailed decisions for the luminance blocks are described as follows:

If both top and bottom are temporally replaced, then four blocks (0, 1, 2, and 3) are replaced by the co-located ones (co-located means no MC) in the previously decoded frame.

If top is temporally replaced and bottom is spatially interpolated, then blocks 0 and 1 are replaced by the co-located ones in the previously decoded anchor frame and blocks 2 and 3 are interpolated from the block boundaries.

If top is spatially interpolated and bottom is temporally replaced, then blocks 0 and 1 are interpolated from the boundaries, and blocks 2 and 3 are replaced by the co-located ones in the previously decoded anchor frame.

If both top and bottom are not temporally replaced, all four blocks are spatially interpolated.

In spatial interpolation, a maximal smoothing technique with boundary conditions under certain smoothness measures is used. The spatial interpolation process is carried out with two steps: the mean value of the damaged block is first bilinear interpolated with ones from the neighboring blocks, then spatial interpolation for each pixel is performed with a Laplacian operator. Minimizing the Laplacian on the boundary pixels using the iterative process in Wang and Zhu (1991) enforces the process of maximum smoothness.

For P and B-pictures, a similar concealment method is used as in Algorithm 2 except motion vectors from top and bottom neighboring MBs are used for the top two blocks and bottom two blocks, respectively.

A schematic block diagram for implementation of adaptive error concealment for intra-coded frames is given in Figure 18.18. Corrupted MBs are first indicated by error tokens obtained via the transport interface. Then, a decision regarding which concealment method (temporal replacement or spatial interpolation) should be used is based on easily obtained measures of image activity from the neighboring top and bottom MBs. The corrupted MBs are first classified into two classes according to the local activities. If local motion is smaller than spatial detail, the corrupted MBs are defined as the first class and will be concealed by temporal replacement; when local motion is greater than local spatial detail, the corrupted MBs are

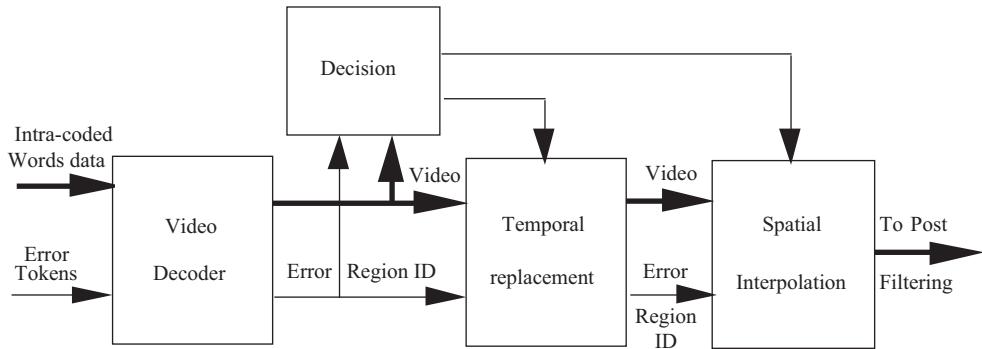


FIGURE 18.18
Two-stage error concealment strategy.

defined as the second class and will be concealed by spatial interpolation. The overall concealment procedure consists of two stages. First, temporal replacement is applied to all corrupted MBs of the first class throughout the whole frame. After the temporal replacement stage, the remaining unconcealed damaged MBs of the second class are more likely to be surrounded by valid image MBs. A stage of spatial interpolation is then performed on them. This will now result in less blurring, or the blurring will be limited to smaller areas. Therefore, a good compromise between shearing (discontinuity or shift of edge or line) and blurring can be obtained.

18.5.3 Algorithm Enhancements

As discussed above, I-picture errors, which are imperfectly concealed, will tend to propagate through all frames in the group of pictures (GOP). Therefore, it is desirable to develop enhancements for the basic spatio-temporal error concealment technique to further improve the accuracy with which missing I-picture pixels are replaced. Three new algorithms have been developed for this purpose. The first is an extension of the spatial restoration technique outlined earlier and is based on processing of edge information in a large local neighborhood to obtain better restoration of the missing data. The second and third are variations that involve encoder modifications aimed at improved error concealment performance. Specifically, information such as I-picture pseudo motion vectors, or low-resolution data in a hierarchical compression system are added in the encoder. These redundancies can significantly benefit error concealment in the decoders that must operate under higher cell loss/error conditions, while having a relatively modest impact on nominal image quality.

18.5.3.1 Directional Interpolation

Improvements in spatial interpolation algorithms (for use with MPEG I-pictures) have been proposed in Sun and Kwok (1995) and Kwok and Sun (1993). In these studies, additional smoothness criteria and/or directional filtering are used for estimating the picture area to be replaced. The new algorithms utilize spatially correlated edge information from a large local neighborhood of surrounding pixels and perform directional or multi-directional interpolation to restore the missing block. The block diagram illustrating the general principle of the restoration process is shown in Figure 18.19.

Three parts are included in the restoration processing: edge classification, spatial interpolation, and pattern mixing. The function of the classifier is to select the top one, two, or

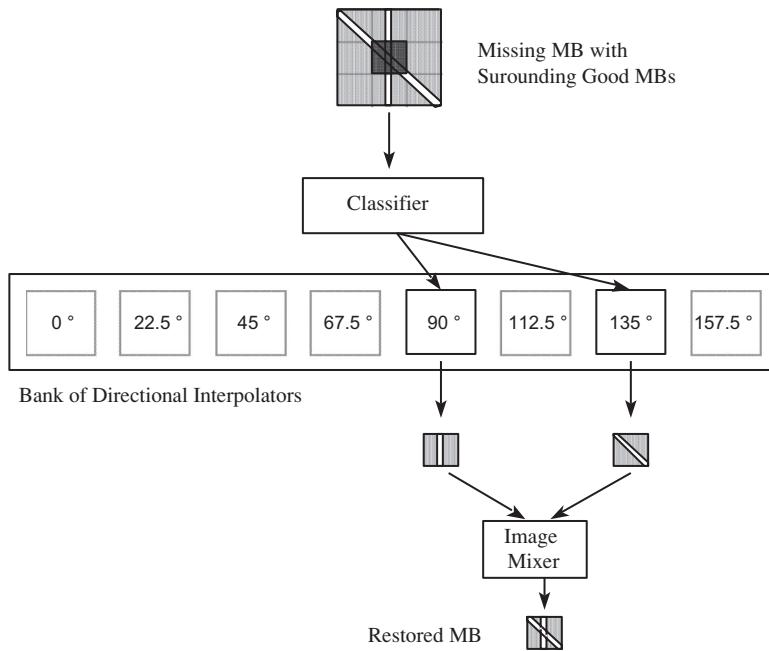


FIGURE 18.19
The multi-directional edge restoration process.

three directions that strongly characterize edge orientations in the surrounding neighborhood. Spatial interpolation is performed for each of the directions determined by the classifier. For a given direction, a series of one-dimensional interpolations are carried out along that direction. All of the missing pixels are interpolated from a weighted average of good neighborhood pixels. The weights depend inversely on the distance from the missing pixel to the good neighborhood pixels. The purpose of pattern mixing is to extract strong characteristic features of two or more images and merge them into one image, which is then used to replace the corrupted one. Results show that these algorithms are capable of providing subjectively better edge restoration in missing areas, and may thus be useful for I-picture processing in high-error-rate scenarios. However, the computational practicality of these edge-filtering techniques needs further investigation for given application scenarios.

18.5.3.2 I-picture Motion Vectors

Motion information is very useful in concealing losses in P and B frames, but is not available for I-pictures. This limits the concealment algorithm to spatial or direct temporal replacement options described above, which may not always be successful in moving areas of the picture. If motion vectors are made available for all MPEG frames (including intra-coded ones) as an aid for error concealment (Sun et al. 1992), good error concealment performance can be obtained without the complexity of adaptive spatial processing. Therefore, a syntax extension has been adopted by the MPEG-2 where motion vectors can be transmitted in an I-picture as the redundancy for error concealment purposes (Sun et al. 1992). The MB syntax is unchanged, however, motion vectors are interpreted in the following way: the decoded forward motion vectors belong to the MB spatially below the

current MB and describe how that MB can be replaced from the previous anchor frame in the event that the MB cannot be recovered. Simulation results have shown that subjective picture quality with I-picture motion vectors is noticeably superior to conventional temporal replacement, and that the overhead for transmitting the additional motion vectors is less than 0.7% of the total bit-rate at bit rate of about 6–7 Mbps.

18.5.3.3 Spatial Scalable Error Concealment

This approach for error concealment of MPEG video is based on the scalability (or hierarchy) feature of (MPEG-2 1995). Hierarchical transmission provides more possibilities for error concealment, when a corresponding two-tier transmission media is available. A block diagram illustrating the general principle of coding system with spatial scalability and error concealment is shown in Figure 18.20.

It should be noted that the concept of scalable error concealment is different from the two-tier concept with data partitioning. Scalable concealment uses the spatial scalability feature in MPEG-2, while the two-tier case uses the data partitioning feature of MPEG-2, in which the data corresponds to the same spatial resolution layer but is partitioned to two parts with a breakpoint. In spatial scalability, the encoder produces two separate bitstreams: one for the low-resolution base layer and another for the high-resolution enhancement. The high-resolution layer is encoded with an adaptive choice of temporal prediction from previous anchor frames and compatible spatial prediction (obtained from the up-sampled low-resolution layer) corresponding to the current temporal reference. In the decoder, redundancies that exist in the scaling data greatly benefit the error concealment processing. In a simple experiment with spatial scalable MPEG-2, we consider a scenario in which losses in the high-resolution MPEG-2 video are concealed with information from the low-resolution layer. Actually, there are two kinds of information in the lower layer that can be used to conceal the data loss in the high-resolution layer: up-sampled picture data and scaled motion information. Therefore, three error concealment approaches are possible:

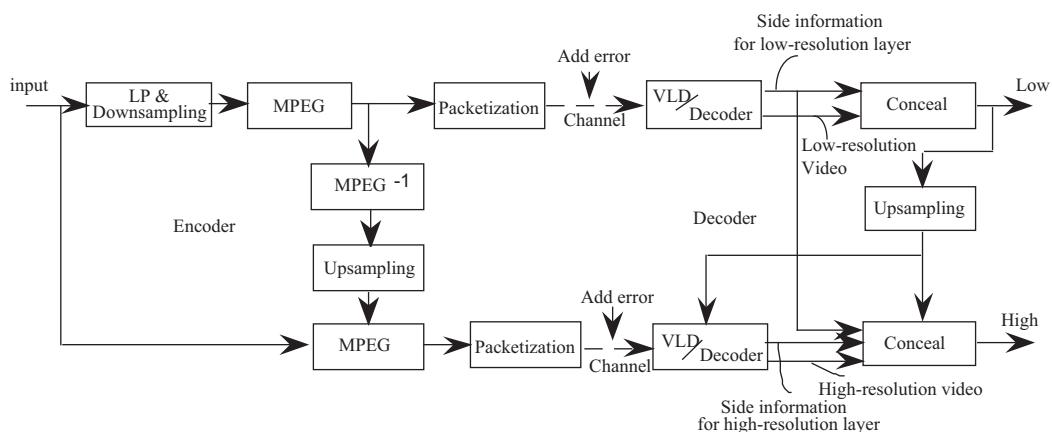


FIGURE 18.20
Block diagram of spatial scalability with error concealment.

1. Up-sampled substitution: lost data is replaced by co-located up-sampled data in the low-resolution decoded frame. The up-sampled picture is obtained from the low-resolution picture with proper up-sampling filter.
2. Mixed substitution: lost MBs in I-picture are replaced by co-located up-sampled MBs in the low-resolution decoded frame, while lost MBs in P and B-picture are temporally replaced by the previously decoded anchor frame with the motion vectors for the low-resolution layer.
3. Motion vector substitution: the previously decoded anchor frame with the motion vectors replaces lost MBs for the low-resolution layer appropriately scaled.

Since motion vectors are not available for I-pictures, obviously, method 3 does not work for I-picture (unless I-picture motion vectors (concealment motion vectors) of MPEG-2 are generated in the encoder). Simulation results have shown that, on average, the up-sampled substitution outperforms the other two, and mixed substitution also provides acceptable results in the case of video with smooth motion.

18.5.4 Summary of Error Concealment

In this section, a general class of error concealment algorithms for MPEG video has been discussed. The error concealment approaches that have been described are practical for current MPEG decoder implementations, and have been demonstrated to provide significant robustness. Specifically, it has been shown that the adaptive spatio-temporal algorithm can provide reasonable picture quality at cell loss ratios (CLR) as high as 10–3 when used in conjunction. These results confirm that compressed video is far less fragile than originally believed when appropriate transport and concealment techniques are employed. The results can be summarized as in [Table 18.4](#).

TABLE 18.4

Subjective Quality Comparison

| Picture Material | Items | Alg 1 | Alg 2 | Alg 3 | Comments |
|------------------|---|-------|-------|-------|---|
| Still | blurring | high | none | low | temporal replacement works very good in no-motion areas |
| | shearing | none | none | none | |
| | artefact blocking | med | none | low | |
| slow motion | blurring | high | none | low | temporal replacement |
| | shearing | none | low | low | works well in slow-motion areas |
| | artefact blocking | med | none | low | |
| fast motion | blurring | high | none | med | temporal replacement causes more shearing, |
| | shearing | none | high | low | spatial interpolation results in blurring, adaptive strategy limits blurring in smaller areas |
| | artefact blocking | high | low | med | |
| Overall | the adaptive strategy of steering the temporal replacement and spatial interpolation according to the measures of local activity and local motion gives a good compromise between shearing and blurring | | | | |

Several concealment algorithm extensions based on directional filtering, I-picture pseudo-motion vectors, and MPEG-2 scalability were also considered and shown to provide performance gains that may be useful in certain application scenarios. In view of the practical benefits of robust video delivery, it is recommended that such error resilience functions (along with associated transport structures) be important for implementation in emerging TV, HDTV, teleconferencing, and multimedia systems if the cell loss rates on these transmission systems are significant. Particularly for terrestrial broadcasting and ATM network scenarios, we believe that robust video delivery based on decoder error concealment is an essential element of a viable system design.

18.6 Summary

In this chapter, several application issues of MPEG-2 have been discussed. The most successful application of MPEG-2 is US HDTV standard. The other application issues include transcoding with bitstream scaling, down-conversion decoding, and error concealment. Transcoding is a very interesting topic that converts the bitstreams between different standards. The error concealment is very useful in the noisy communication channels such as terrestrial television broadcasting. The down-conversion decoder responds to the market requirement during the DTV transition period and long-term need for displaying DTV signal on computer monitors.

Exercises

- 18.1 In DTV applications, describe the advantages and disadvantages of interlaced format and progressive format. Explain why the computer industry favors progressive format and TV manufacturers like interlaced format.
- 18.2 Do all DTV formats have square pixel format? Why is square pixel format important for DTV?
- 18.3 The bitstream scaling is one kind of transcoding; according to your knowledge, describe several other kinds of transcoding (such as MPEG-1 to JPEG) and propose a feasible solution to achieve the transcoding requirements.
- 18.4 What type of MPEG-2 frames will cause a higher degree of error propagation if errors occur? What technique of error concealment is allowed by the MPEG-2 syntax? Using this technique, perform simulations with several images to determine the penalty in the case of no errors.
- 18.5 In order to reduce the drift in a down-conversion decoder, what coding parameters can be chosen at the encoder? Will these actions affect the coding performance?
- 18.6 What are the advantages and disadvantages of a down-conversion decoder in the frequency-domain and spatial-domain?

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19

MPEG-4 Video Standard: Content-Based Video Coding

This chapter provides an overview of the ISO MPEG-4 standard. The MPEG-4 work includes natural video, synthetic video, audio, and systems. Both the natural and synthetic video have been combined into a single part of the standard, which is referred to as MPEG-4 visual [ISO/IEC 14496-2 1998]. It should be emphasized that neither MPEG-1 nor MPEG-2 considers synthetic video (or computer graphics) and the MPEG-4 is also the first standard to consider the problem of content-based coding. Here, we will focus on the video parts of the MPEG-4 standard.

19.1 Introduction

As we discussed in the previous chapters, MPEG has completed two standards: MPEG-1 that was mainly targeted for CD-ROM applications up to 1.5 Mbps and MPEG-2 for digital TV and HDTV applications at bit rates between 2 and 30 Mbps. In July 1993, MPEG started its new project, MPEG-4, which was targeted to provide technology for multimedia applications. The first working draft (WD) was completed in November 1996 and the committee draft (CD) of version 1 was reached in November 1997. The draft international standard (DIS) of MPEG-4 was completed in November of 1998. The international standard (IS) of MPEG-4 version 1 was completed in February of 1999. The goal of the MPEG-4 standard is to provide the core technology that allows efficient content-based storage, transmission, and manipulation of video, graphics, audio, and other data within a multimedia environment. As we mentioned before, there exist several video-coding standards such as MPEG-1/2, H.261, and H.263. Why do we need a new standard for multimedia applications? In other words, are there any new attractive features of MPEG-4 that the current standards do not have or cannot provide? The answer is yes. The MPEG-4 has many interesting features that will be described later in this chapter. Some of these features are focused on improving coding efficiency; some are used to provide robustness of transmission and interactivity with end-user. However, among these features the most important one is the content-based coding. MPEG-4 is the first standard that supports content-based coding of AVOs. For content providers or authors, the MPEG-4 standard can provide the greater reusability, flexibility, and manageability of the content that is produced. For network providers, MPEG-4 will offer transparent information, which can be interpreted and translated into the appropriate native signaling messages of each network. This can be accomplished with the help of relevant standards bodies that have the jurisdiction. For end users, MPEG-4 can provide much functionality to make the user terminal have more capabilities of interaction with the content. To reach these goals, MPEG-4 has the following important features:

The contents such as audio, video, or data are represented in the form of primitive audio-visual objects (AVOs). These AVOs can be natural scenes or sounds, which are recorded by video camera or synthetically generated by computers.

The AVOs can be composed together to create compound AVOs or scenes.

The data associated with AVOs can be multiplexed and synchronized so that they can be transported through network channels with certain quality requirements.

19.2 MPEG-4 Requirements and Functionalities

Since the MPEG-4 standard is mainly targeted for multimedia applications, there are many requirements to ensure that several important features and functionalities are offered. These features include the allowance of interactivity, high compression, universal accessibility, and portability of audio and video content. From the MPEG-4 video requirement document, the main functionalities can be summarized by the following three aspects: content-based interactivity, content-based efficient compression, and universal access.

19.2.1 Content-Based Interactivity

In addition to provisions for efficient coding of conventional video sequences, MPEG-4 video has the following features of content-based interactivity.

19.2.1.1 Content-Based Manipulation and Bitstream Editing

The MPEG-4 supports the content-based manipulation and bitstream coding without the need for transcoding. In MPEG-1 and MPEG-2, there is no syntax and no semantics for supporting true manipulation and editing in the compressed domain. MPEG-4 provides the syntax and techniques to support content-based manipulation and bitstream editing. The level of access, editing, and manipulation can be done at the object level in connection with the features of content-based scalability.

19.2.1.2 Synthetic and Natural Hybrid Coding

The MPEG-4 supports combining synthetic scenes or objects with natural scenes or objects. This is for “compositing” synthetic data with ordinary video, allowing for interactivity. The related techniques in MPEG-4 for supporting this feature include sprite coding, efficient coding of 2-D and 3-D surfaces, and wavelet coding for still textures.

19.2.1.3 Improved Temporal Random Access

The MPEG-4 provides efficient method to randomly access, within a limited time and with the fine resolution, parts, e.g., video frames or arbitrarily shaped image objects from an audio-visual sequence. This includes conventional random access at very low bit rate. This feature is also important for content-based bitstream manipulation and editing.

19.2.2 Content-Based Efficient Compression

One initial goal of MPEG-4 is to provide highly efficient coding tool with high compression at very low bit rates. But this goal has now extended to a large range of bit rates from 10 Kbps to 5 Mbps, which covers from QSIF to CCIR 601 video formats. Two important items are included in this requirement.

19.2.2.1 Improved Coding Efficiency

The MPEG-4 video standard provides subjectively better visual quality at comparable bit rates comparing to the existing or emerging standards, including MPEG-1/2 and H.263. MPEG-4 video contains many new tools, which optimize the code in different bit rate ranges. Some experimental results have shown that it outperforms MPEG-2 and H.263 at the low bit rates. Also, the content-based coding reaches the similar performance of the frame-based coding.

19.2.2.2 Coding of Multiple Concurrent Data Streams

The MPEG-4 provides the capability of coding multiple views of a scene efficiently. For stereoscopic video applications, MPEG-4 allows the ability to exploit redundancy in multiple viewing points of the same scene, permitting joint coding solutions that allow compatibility with normal video as well as the ones without compatibility constraints.

19.2.3 Universal Access

Another important feature of the MPEG-4 video is the feature of universal access.

19.2.3.1 Robustness in Error-Prone Environments

The MPEG-4 video provides strong error robustness capabilities to allow access to applications over a variety of wireless and wired networks and storage media. Enough error robustness is provided for low-bit-rate applications under severe error conditions (e.g., long error bursts).

19.2.3.2 Content-Based Scalability

The MPEG-4 video provides the ability to achieve scalability with fine granularity in content, quality (e.g., spatial and temporal resolution), and complexity. These scalabilities are especially intended to result in content-based scaling of visual information.

19.2.4 Summary of MPEG-4 Features

From the above description of MPEG-4 features, it is obvious that the most important application of MPEG-4 will be in a multimedia environment. The media that can use the coding tools of MPEG-4 include computer networks, wireless communication networks, and the Internet. Although it can also be used for satellite, terrestrial broadcasting, and cable TV, these are still the territories of MPEG-2 video since MPEG-2 already has made such a large impact in the market. Many silicon solutions exist and its technology is more mature compared to the current MPEG-4 standard. From the viewpoint of coding

theory, we can say there is no significant breakthrough in MPEG-4 video compared with MPEG-2 video. Therefore, we cannot expect to have a significant improvement of coding efficiency when using MPEG-4 video over MPEG-2. Even though MPEG-4 optimized its performance in a certain range of bit rates, its major strength is that it provides more functionality than MPEG-2. Recently, MPEG-4 added the necessary tools to support interlaced material. With this addition, MPEG-4 video does support all functionalities already provided by MPEG-1 and MPEG-2, including the provision to efficiently compress standard rectangular sized video at different levels of input formats, frame rates, and bit rates.

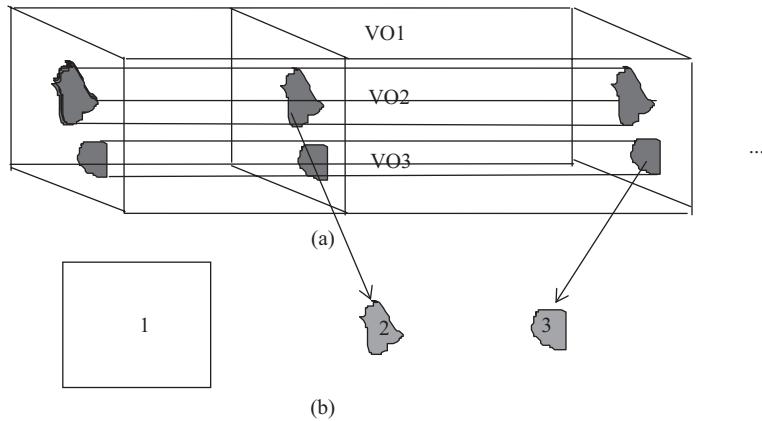
Overall, the incorporation of an object or content-based coding structure is the feature that allows MPEG-4 to provide more functionality. It enables MPEG-4 to provide the most elementary mechanism for interactivity and manipulation with objects of images or video in the compressed domain without the need for further segmentation or transcoding at the receiver, since the receiver can receive separate bitstreams for different objects contained in the video. To achieve content-based coding, the MPEG-4 uses the concept of a video object plane (VOP). It is assumed that each frame of an input video is first segmented into a set of arbitrary-shaped regions or VOPs. Each such region could cover a particular image or video object (VO) in the scene. Therefore, the input to the MPEG-4 encoder can be a VOP, and the shape and the location of the VOP can vary from frame to frame. A sequence of VOPs is referred to as a VO. The different VOs may be encoded into separate bitstreams. MPEG-4 specifies de-multiplexing and composition syntax, which provide the tools for the receiver to decode the separate VO bitstreams and composite them into a frame. In this way, the decoders have more flexibility to edit or rearrange the decoded video objects. The detailed technical issues will be addressed in the following sub-sections.

19.3 Technical Description of MPEG-4 Video

19.3.1 Overview of MPEG-4 Video

The major feature of MPEG-4 is to provide the technology for object-based compression, which is capable of separately encoding and decoding video objects. To clearly explain the idea of object-based coding, we should review the set of VO-related definitions. An image scene may contain several objects. In the example of [Figure 19.1](#), the scene contains the background and two objects. The time instant of each VO is referred to as the VOP. The concept of a VO provides several functionalities of MPEG-4 that are either impossible or very difficult in MPEG-1 or MPEG-2 video coding. Each VO is described by the information of texture, shape, and motion vectors (MVs). The video sequence can be encoded in a way that will allow the separate decoding and reconstruction of the objects and allow the editing and manipulation of the original scene by simple operation on the compressed bitstream domain. The feature of object-based coding is also able to support functionality such as warping of synthetic or natural text, textures, image, and video overlays on reconstructed video objects.

Since MPEG-4 aims at providing coding tools for multimedia environment, these tools not only allow one to efficiently compress natural video objects, but also compress synthetic objects, which are a subset of the larger class of computer graphics. The tools of MPEG-4 video include:

**FIGURE 19.1**

VO definition and format (a) Video object and (b) VOPs.

- Motion estimation (ME) and compensation
- Texture coding
- Shape coding
- Sprite coding
- Interlaced video coding
- Wavelet-based texture coding
- Generalized temporal and spatial as well as hybrid scalability
- Error resilience

The technical details of these tools will be explained in the following sections.

19.3.2 Motion Estimation and Compensation

For object-based coding, the coding task includes two parts: texture coding and shape coding. The current MPEG-4 video texture coding is still based on the combination of motion-compensated prediction and transform coding. Motion-compensated predictive coding is a well-known approach for video coding. The motion compensation (MC) is used to remove the inter-frame redundancy and the transform coding is used to remove the intra-frame redundancy, as in the MPEG-2 video-coding scheme. However, there are lots of modifications and technical details in MPEG-4 for coding a very wide range of bit rates. Moreover, MPEG-4 coding has been optimized for low bit-rate applications with several new tools. In other words, MPEG-4 video coding uses the most common coding technologies such as MC and transform coding, but at the same time, it modifies some traditional methods such as advanced MC and also creates some new features such as sprite coding.

The basic technique to perform motion-compensated predictive coding for coding a video sequence is ME. The basic ME method used in the MPEG-4 video coding is still the block matching technique. The basic principle of block matching for ME is to find the best-matched block in the previous frame for every block in the current frame. The displacement of the best-matched block relative to the current block is referred to as the MV. Positive values for both MV components indicate that the best-matched block is on the bottom-right of the current block.

The motion-compensated prediction difference block is formed by subtracting the pixel values of the best-matched block from the current block, pixel by pixel. The difference block is then coded by texture coding method. In MPEG-4 video coding, the basic technique of texture coding is a discrete cosine transformation (DCT). The coded MV information and difference block information is contained in the compressed bitstream, which is transmitted to the decoder. The major issues in the ME and compensation are the same as in the MPEG-1 and MPEG-2, which include the matching criterion, the size of search window (searching range), the size of matching block, the accuracy of MVs (one pixel or half pixel) and INTER/INTRA mode decision. We are not going to repeat these topics and we will focus on the new features in the MPEG-4 video coding. The feature of the advanced motion prediction is a new tool of MPEG-4 video. This feature includes two aspects: adaptive selection of a 16×16 block or four 8×8 blocks to match the current 16×16 block and overlapped MC for luminance block.

19.3.2.1 Adaptive Selection of 16×16 Block or Four 8×8 Blocks

The purpose of the adaptive selection of the matching block size is to further enhance coding efficiency. The coding performance may be improved at low bit rate since the bits for coding prediction difference could be greatly reduced at the limited extra cost for increasing MVs. Of course, if the cost of coding MVs is too high, this method will not work. The decision in the encoder should be very careful. For explaining the procedure of how to make decision, we define $\{C(i, j), i, j=0, 1, \dots, N-1\}$ to be the pixels of the current block and $\{P(i, j), i, j=0, 1, \dots, N-1\}$ to be the pixels in the search window in the previous frame. The sum of absolute difference (SAD) is calculated as:

$$SAD_N(x, y) = \begin{cases} \sum_{i=0}^{N-1} \sum_{j=0}^{N-1} |C(i, j) - P(i, j)| - T & \text{if } (x, y) = (0, 0); \\ \sum_{i=0}^{N-1} \sum_{j=0}^{N-1} |C(i, j) - P(i+x, j+y)| & \text{otherwise} \end{cases} \quad (19.1)$$

Where (x, y) is the pixel within the range of searching window and T is a positive constant. The following steps then make the decision:

Step 1: To find $SAD_{16}(MV_x, MV_y)$

Step 2: To find $SAD_8(MV1_x, MV1_y)$, $SAD_8(MV2_x, MV2_y)$, $SAD_8(MV3_x, MV3_y)$, and $SAD_8(MV4_x, MV4_y)$

Step 3: if

$$\sum_{i=1}^4 SAD_8(MV_{ix}, MV_{iy}) < SAD_{16}(MV_x, MV_y) - 128$$

then choose 8×8 predictions; otherwise, choose 16×16 predictions.

If the 8×8 prediction is chosen, there are four MVs for the four 8×8 luminance blocks that will be transmitted. The MV for the two chrominance blocks is then obtained by taking an average of these four MVs and dividing the average value by a factor of two. Since each MV for the 8×8 luminance block has half-pixel accuracy, the MV for the chrominance block may have a sixteenth-pixel accuracy.

19.3.2.2 Overlapped Motion Compensation

This kind of MC is always used for the case of four 8×8 blocks. The case of one MV for a 16×16 block can be considered as having four identical 8×8 MVs, each for an 8×8 block. Each pixel in an 8×8 of the best-matched luminance block is a weighted sum of three prediction values specified in the following equation:

$$p'(i, j) = (H_0(i, j) \cdot q(i, j) + H_1(i, j) \cdot r(i, j) + H_2(i, j) \cdot s(i, j)) / 8 \quad (19.2)$$

where division is with roundoff. The weighting matrices are specified as:

$$H_0 = \begin{bmatrix} 4 & 5 & 5 & 5 & 5 & 5 & 5 & 4 \\ 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 \\ 5 & 5 & 6 & 6 & 6 & 6 & 5 & 5 \\ 5 & 5 & 6 & 6 & 6 & 6 & 5 & 5 \\ 5 & 5 & 6 & 6 & 6 & 6 & 5 & 5 \\ 5 & 5 & 6 & 6 & 6 & 6 & 5 & 5 \\ 5 & 5 & 6 & 6 & 6 & 6 & 6 & 6 \\ 5 & 5 & 5 & 5 & 5 & 5 & 5 & 4 \end{bmatrix}, H_1 = \begin{bmatrix} 2 & 2 & 2 & 2 & 2 & 2 & 2 & 2 \\ 1 & 1 & 2 & 2 & 2 & 2 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 2 & 2 & 2 & 2 & 1 & 1 \end{bmatrix},$$

$$\text{and } H_2 = \begin{bmatrix} 2 & 1 & 1 & 1 & 1 & 1 & 1 & 2 \\ 2 & 2 & 1 & 1 & 1 & 1 & 2 & 2 \\ 2 & 2 & 1 & 1 & 1 & 1 & 2 & 2 \\ 2 & 2 & 1 & 1 & 1 & 1 & 2 & 2 \\ 2 & 2 & 1 & 1 & 1 & 1 & 2 & 2 \\ 2 & 2 & 1 & 1 & 1 & 1 & 2 & 2 \\ 2 & 2 & 1 & 1 & 1 & 1 & 2 & 2 \\ 2 & 1 & 1 & 1 & 1 & 1 & 1 & 2 \end{bmatrix}$$

It is noted that $H_0(i, j) + H_1(i, j) + H_2(i, j) = 8$ for all possible (i, j) . The value of $q(i, j)$, $r(i, j)$ and $s(i, j)$ are the values of the pixels in the previous frame at the locations,

$$\begin{aligned} q(i, j) &= p(i + MV_x^0, j + MV_y^0); \\ r(i, j) &= p(i + MV_x^1, j + MV_y^1); \\ s(i, j) &= p(i + MV_x^2, j + MV_y^2). \end{aligned} \quad (19.3)$$

where (MV_x^0, MV_y^0) is the MV of the current 8×8 luminance block $p(i, j)$, (MV_x^1, MV_y^1) is the MV of the block either above (for $j=0,1,2,3$) or below (for $j=4,5,6,7$) the current block, and (MV_x^2, MV_y^2) is the MV of the block either to the left (for $i=0,1,2,3$) or right (for $i=4,5,6,7$) of the current block. The overlapped MC can reduce the prediction noise at certain levels.

19.3.3 Texture Coding

Texture coding is used to code the INTRA VOPs and the prediction residual data after MC. The algorithm for video texture coding is based on the conventional 8×8 DCT with MC.

DCT is performed for each luminance and chrominance block, where the MC is performed only on the luminance blocks. This algorithm is like those in H.263 and MPEG-1 as well as MPEG-2. However, MPEG-4 video texture coding must deal with the requirement of object-based coding, which is not included in the other video coding standards. In the following, we will focus on the new features of the MPEG-4 video coding. These new features include: the INTRA DC and AC prediction for I-VOP and P-VOP, the algorithm of ME and compensation for arbitrary shape VOP, and the strategy of arbitrary shape-texture coding. The definitions of I-VOP, P-VOP, and B-VOP are like the I-Picture, P-Picture, and B-Picture in [Chapter 16](#) for MPEG-1 and MPEG-2.

19.3.3.1 INTRA DC and AC Prediction

In the intra-mode coding, the predictive coding is not only applied on the DC coefficients but also the AC coefficients to increase the coding efficiency. The adaptive DC prediction involves the selection of the quantized DC (QDC) value of the immediately left block or the immediately above block. The selection criterion is based on comparison of the horizontal and vertical DC gradients around the block to be coded. [Figure 19.2](#) shows the three surrounding blocks 'A,' 'B,' and 'C' to the current block 'X,' whose QDC is to be coded where block 'A,' 'B,' and 'C' are the immediately left, immediately left and above, and immediately above block to the 'X,' respectively. The QDC value of block 'X,' QDC_X , is predicted by either the QDC value of block 'A,' QDC_A , or the QDC value of block 'C,' QDC_C , based on the comparison of horizontal and vertical gradients as follows:

$$\text{If } |QDC_A - QDC_B| < |QDC_B - QDC_C|, QDC_P = QDC_C$$

$$\text{Otherwise, } QDC_P = QDC_A \quad (19.4)$$

The differential DC is then obtained by subtracting the DC prediction, QDC_P , from QDC_X . If any of block 'A,' 'B' or 'C' are outside of the VOP boundary, or they do not belong to an INTRA coded block, their QDC value are assumed to take a value of 128 (if the pixel is quantized to 8 bits) for computing the prediction. The DC prediction are performed similarly for the luminance and each of the two chrominance blocks.

For AC coefficient prediction, either coefficients from the first row or the first column of a previous coded block are used to predict the co-sited (same position in the block) coefficients in the current block. On a block basis, the same rule for selecting the best predictive direction (vertical or horizontal direction) for DC coefficients is also used for the AC coefficient prediction. A difference between DC prediction and AC prediction is the issue

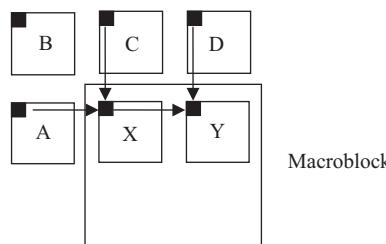


FIGURE 19.2

Previous neighboring blocks used in DC prediction.

of quantization scale. All DC values are quantized to the 8 bits for all blocks. However, the AC coefficients may be quantized by the different quantization scales for the different blocks. To compensate for differences in the quantization of the blocks used for prediction, scaling of prediction coefficients becomes necessary. The prediction is scaled by the ratio of the current quantization step size and the quantization step size of the block used for prediction. In the cases when AC coefficient prediction results in a larger range of prediction errors as compared to the original signal, it is desirable to disable the AC prediction. The decision of AC prediction switched on or off is performed on a macroblock basis instead of a block basis to avoid the excessive overhead. The decision for switching on or off AC prediction is based on a comparison of the sum of the absolute values of all AC coefficients to be predicted in a macroblock and that of their predicted differences. It should be noted that the same DC and AC prediction algorithm is used for the INTRA blocks in the inter-coded VOP. If any blocks used for prediction are not INTRA blocks, the QDC and QAC values used for prediction are set to 128 and 0 for DC ad AC prediction, respectively.

19.3.3.2 Motion Estimation/Compensation of Arbitrary-Shaped VOP

In the previous section, we discussed the general issues of ME and MC. Here we are going to discuss the ME and MC for coding the texture in the arbitrary-shaped VOP. In an arbitrary-shaped VOP, the shape information is given by either binary shape information or alpha components of a gray level shape information. If the shape information is available to both encoder and decoder, three important modifications must be considered for the arbitrarily shaped VOP. The first is for the blocks, which are in the border of the VOP. For these boundary blocks, the block-matching criterion should be modified. Secondly, a special padding technique is required for the reference VOP. Finally, since the VOPs have arbitrary shapes rather rectangular shapes, and the shapes change from time to time, an agreement on a coordinate system is necessary to ensure the consistency of MC. At the MPEG-4 video, the absolute frame coordinate system is used for referencing all the VOPs. At each time instance, a bounding rectangle that includes the shape of that VOP is defined. The position of upper-left corner in the absolute coordinate in the VOP spatial reference is transmitted to the decoder. Thus, the MV for a block inside a VOP is referred to as the displacement of the block in absolute coordinates.

The first and second modifications are related since the padding of boundary blocks will affect the matching of ME. The purpose of padding is aiming at more accurate block matching. In current algorithm, the repetitive padding is applied to the reference VOP for performing ME and compensation. The repetitive padding process is performed as the following steps:

Define any pixel outside the object boundary as a zero pixel.

Scan each horizontal line of a block (one 16×16 for luminance and two 8×8 for chrominance). Each scan line is possibly composed of two kinds of line segments: zero segments and non-zero segment. It is obvious that our task is to pad zero segments. There are two kinds of zero segments: (1) between an end point of the scan line and the end point of a non-zero segment and (2) between end points of two different non-zero segments. In the first case, all zero pixels are replaced by the pixel value of the end pixel of the non-zero segment; for the second kind of zero segments, all zero pixels take the averaged value of the two end pixels of the non-zero segments.

Scan each vertical line of the block and perform the identical procedure as described for the horizontal line.

If a zero pixel is located at the intersection of horizontal and vertical scan lines, this zero pixel takes the average of two possible values.

For the rest of the zero pixels, to find the closest non-zero pixel on the same horizontal scan line and the same vertical scan line (if there is a tie, the non-zero pixel on the left or the top of the current pixel is selected). Replace the zero pixel by the average of these two non-zero pixels.

For a fast-moving VOP, padding is further extended to the blocks outside the VOP but immediately next to the boundary blocks. These blocks are padded by replacing the pixel values of adjacent boundary blocks. This extended padding is performed in both horizontal and vertical directions. Since block matching is replaced by polygon matching for the boundary blocks of the current VOP, the SAD values are calculated by the modified formula:

$$SAD_N(x, y) = \begin{cases} \sum_{i=0}^{N-1} \sum_{j=0}^{N-1} |c(i, j) - p(i, j)| \cdot \alpha(i, j) - C & \text{if } (x, y) = (0, 0), \\ \sum_{i=0}^{N-1} \sum_{j=0}^{N-1} |c(i, j) - p(i + x, j + y)| \cdot \alpha(i, j) - C & \text{otherwise} \end{cases} \quad (19.5)$$

where $C = N_B/2 + 1$ and N_B is the number of pixels inside the VOP and in this block, and $\alpha(i, j)$ is the alpha component specifying the shape information and is not equal to zero here.

19.3.3.3 Texture Coding of Arbitrary-Shaped VOP

During encoding, the VOP is represented by a bounding rectangle that is formed to completely contain the VO but with a minimum number of macroblocks in it, as shown in Figure 19.3. The detailed procedure of VOP rectangle formation is given in MPEG-4 video VM (ISO/IEC 14496-2 1998).

There are three types of macroblocks in the VOP with arbitrary shape: the macroblocks that are completely located inside of the VOP, the macroblocks that are located along the boundary of the VOP, and the macroblocks outside of boundary. For the first kind of macroblock, there is no need for any particular modified technique to code them and just use of normal DCT with entropy coding of quantized DCT coefficients such as coding algorithm in H.263. The second kind of macroblocks, which are located along the boundary, contains two kinds of 8×8 blocks: the blocks lie along the boundary of VOP and the blocks do not belong to the arbitrary shape but lie inside the rectangular bounding box of the VOP.

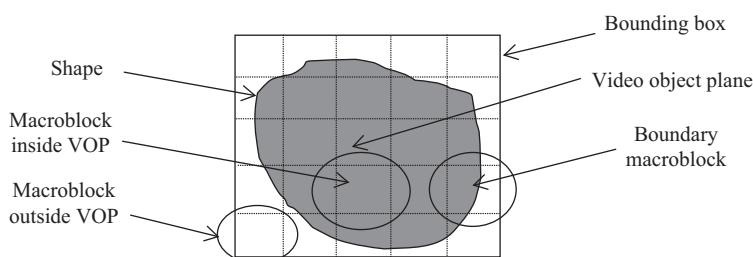


FIGURE 19.3

A VOP is represented by a bounding rectangular box.

The second kind of blocks is referred to as transparent blocks. For those 8×8 blocks that do lie along the boundary of the VOP, there are two different methods that have been proposed: low-pass extrapolation (LPE) padding and shape adaptive DCT (SA-DCT). All blocks in the macroblock outside of the boundary are also referred to as transparent blocks. The transparent blocks are skipped and not coded at all.

19.3.3.3.1 Low-Pass Extrapolation Padding Technique

This block padding technique is applied to intra-coded blocks, which are not completely within the object boundary. To perform this padding technique, we first assign the mean value of those pixels that are in the object boundary (both inside and outside) to each pixel outside the object boundary. Then an average operation is applied to each pixel $p(i, j)$ outside the object boundary starting from the upper-left corner of the block and proceeding row by row to the lower-right corner pixel:

$$p(i, j) = [p(i, j-1) + p(i-1, j) + p(i, j+1) + p(i+1, j)]/4 \quad (19.6)$$

If one or more of the four pixels used for filtering are outside of the block, the corresponding pixels are not considered for the average operation and the factor 1/4 is modified accordingly.

19.3.3.3.2 SA-DCT

The SA-DCT is only applied to those 8×8 blocks that are located on the object boundary of an arbitrary-shaped VOP. The idea of the SA-DCT is to apply one-dimensional DCT transformation vertically and horizontally according to the number of active pixels in the row and column of the block, respectively. The size of each vertical DCT is the same as the number of active pixels in each column. After vertical DCT is performed for all columns with at least one active pixel, the coefficients of the vertical DCTs with the same frequency index are lined up in a row. The DC coefficients of all vertical DCTs are lined up in the first row, the first-order vertical DCT coefficients are lined up in the second row, and so on. After that, horizontal DCT is applied to each row. As the same as for the vertical DCT, the size of each horizontal DCT is the same as the number of vertical DCT coefficients lined up in the particular row. The final coefficients of SA-DCT are concentrated into the upper-left corner of the block. This procedure is shown in [Figure 19.4](#).

The final number of the SA-DCT coefficients is identical to the number of active pixels of the image. Since the shape information is transmitted to the decoder, the decoder can perform the inverse shape-adapted DCT to reconstruct the pixels. The regular zigzag scan is modified so that the non-active coefficient locations are neglected when counting the runs for the run-length coding of the SA-DCT coefficients. It is obvious that for a block with all 8×8 active pixels, the SA-DCT becomes a regular 8×8 DCT and the scanning of the coefficients is identical

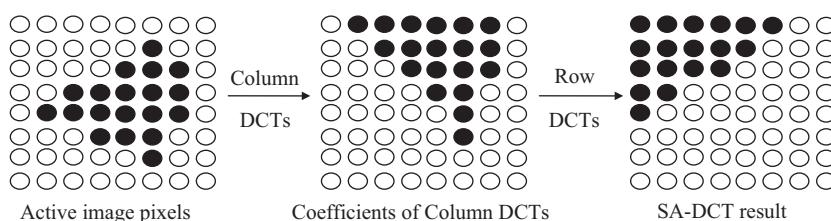


FIGURE 19.4
Illustration of SA-DCT.

to the zigzag scan. All SA-DCT coefficients are quantized and coded in the same way as the regular DCT coefficients employing the same quantizers and VLC code tables. The SA-DCT is not included in MPEG-4 video version 1, but it is considered for inclusion into version 2.

19.3.4 Shape Coding

Shape information of the arbitrary-shaped objects is very useful not only in the field of image analysis, computer vision and graphics, but also in object-based video coding. MPEG-4 video coding is the first to make effort at providing a standardized approach to compress the shape information of objects and contain the compressed results within a video bitstream. In the current MPEG-4 video coding standard, the video data can be coded on an object basis. The information in the video signal is decomposed to shape, texture, and motion. This information is then coded and transmitted within the bitstream. The shape information is provided in binary format or grayscale format. The binary format of shape information consists of a pixel map, which is generally the same size as the bounding box of the corresponding VOP. Each pixel takes on one of two possible values, indicating whether it is located within the VO or not. The grayscale format is like the binary format with the additional feature that each pixel can take on a range of values, i.e., times an alpha value. Alpha typically has a normalized value of 0–1. The alpha value can be used to blending two images on a pixel-by-pixel basis in such a way: new pixel = (alpha)(pixel A color)+(1-alpha)(pixel B color).

Now let us to discuss how to code the shape information. As we mentioned, the shape information is classified as binary shape or grayscale shape. Both binary and grayscale shapes are referred to as an alpha plane. The alpha plane defines the transparency of an object. The multi-level alpha maps are frequently used to blend different images. A binary alpha map defines whether a pixel belongs to an object. The binary alpha planes are encoded by modified content-based arithmetic encoding (CAE), while the grayscale alpha planes are encoded by motion-compensated DCT coding, which is like texture coding. For binary shape coding, a rectangular box enclosing the arbitrary-shaped VOP is formed as shown in [Figure 19.3](#). The bounded rectangle box is then extended in both vertical and horizontal directions on the right-bottom side to the multiple of 16×16 blocks. Each 16×16 block within the rectangular box is referred to as binary alpha block (BAB). Each BAB is associated with co-located macroblock. The BAB can be classified into three types: transparent block, opaque block, and alpha or shape block. The transparent block does not contain any information about the object. The opaque block is entirely located inside the object. The alpha or shape block is in the object boundary, i.e., a part of block is inside of object and the rest of block is in the background. The value of pixels in the transparent region is zero. For shape coding, the type information will be included in the bitstream and signaled to the decoder as macroblock type. But only the alpha blocks need to be processed by the encoder and decoder. The methods used for each shape format contain several encoding modes. For example, the binary shape information can be encoded using either an intra or inter mode. Each of these modes can be further divided into lossy and lossless option. Grayscale shape information also contains INTRA and INTER modes; however, only a lossy option is used.

19.3.4.1 Binary Shape Coding with CAE Algorithm

As mentioned previously, the CAE is used to code each binary pixel of the BAB. For a P-VOP, the BAB may be encoded in INTRA or INTER Mode. Pixels are coded in scan-line

| | | | | |
|----------------|----------------|----------------|----------------|----------------|
| | C ₉ | C ₈ | C ₇ | |
| C ₆ | C ₅ | C ₄ | C ₃ | C ₂ |
| C ₁ | C ₀ | X | | |

FIGURE 19.5

Template for defining the context of the pixel, X, to be coded in INTRA mode.

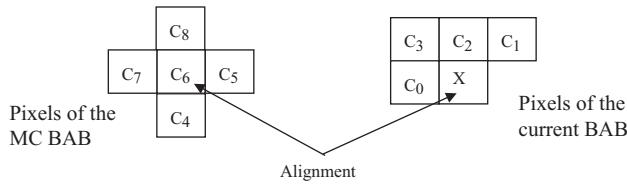
order, i.e., row by row for both modes. The process for coding a given pixel includes three steps: (1) compute a context number, (2) index a probability table using the context number, and (3) use the indexed probability to drive an arithmetic encoder. In INTRA mode, a template of 10 pixels is used to define the causal context for predicting the shape value of the current pixel, as shown in [Figure 19.5](#). For the pixels in the top and left boundary of the current macroblock, the template of causal context will contain the pixels of the already transmitted macroblocks on the top and on the left side of the current macroblock. For the two right-most columns of the VOP, each undefined pixel such as C₇, C₃ and C₂, of the context is set to the value of its closest neighbor inside the macroblock, i.e., C₇ will take the value of C₈ and C₃ and C₂ will take the value of C₄.

A 10-bit context is calculated for each pixel, X as

$$C = \sum_{k=0}^9 C_k \cdot 2^k \quad (19.7)$$

This causal context is used to predict the shape value of the current pixel. For encoding the state transition, a context-based arithmetic encoder is used. The probability table of the arithmetic encoder for the 1024 contexts was derived from sequences that are outside of the test set. Two bytes are allocated to describe the symbol probability for each context, the table size is 2048 bytes. To increase coding efficiency and rate control, the algorithm allows lossy shape coding. In lossy shape coding a macroblock can be downsampled by a factor of 2 or 4, resulting in a sub-block of size 8 by 8 pixels or 4 by 4 pixels, respectively. The sub-block is then encoded using the same method as for a full-size block. The downsampling factor is included in the encoded bitstream and then transmitted to the decoder. The decoder decodes the shape data and then upsamples the decoded sub-block to full macroblock size according to the downsampling factor. Obviously, it is more efficient to code shape using a high downsampling factor, but the coding errors may occur in the decoded shape after upsampling. However, in the case of low-bit-rate coding, lossy shape coding may be necessary since the bit budget may not be enough for lossless shape coding. Depending on the upsampling filter, the decoded shape can look somewhat blocky. Several upsampling filters were investigated. The best performing filter in terms of subjective picture quality is an adaptive non-linear upsampling filter. It should be noted that the coding efficiency of shape coding also depends on the orientation of the shape data. Therefore, the encoder can choose to code the block as described above or transpose the macroblock prior to arithmetic coding. Of course, the transposed information must be signaled to the decoder.

For shape coding in a P-VOP or B-VOP, the INTER mode may be used to exploit the temporal redundancy in the shape information with MC. For MC, a 2D integer pixel MV is estimated using full search for each macroblock to minimize the prediction error between the previous coded VOP shape and the current VOP shape. The shape MVs are predictively

**FIGURE 19.6**

Template for defining the context of the pixel, X , to be coded in INTER mode.

encoded with respect to the shape MVs of neighboring macroblocks. If no shape MV is available, texture MVs are used as predictors. The template for INTER mode differs from the one used for INTRA mode. The INTER mode template contains 9 pixels, of which five pixels in the previous frame and four are the current neighbors, as shown in [Figure 19.6](#).

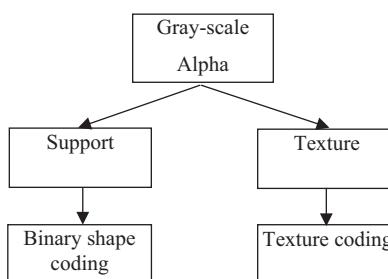
The INTER mode template defines a context of 9 pixels. Accordingly, a 9-bit context, or 512 contexts, can be computed in a similar way to (19.7).

$$C = \sum_{k=0}^8 C_k \cdot 2^k \quad (19.8)$$

The probability for one symbol is also described by 2 bytes, giving a probability table size of 1024 bytes. The idea of lossy coding can also be applied to the INTER mode shape coding by downsampling the original BABs. For INTER mode shape coding, the total bits for coding the shape consists of two parts, one part for coding MVs and other for prediction residue. The encoder may decide that the shape representation achieved by just using MVs is enough, so bits for coding the prediction error can be saved. There are seven modes to code the shape information of each macroblock: transparent, opaque, intra, inter with and without shape MVs, and inter with/without shape MVs and prediction error coding. These different options with optional downsampling and transposition allow for encoder implementations of different coding efficiency and implementation complexity. Again, this is a problem of encoder optimization, which does not belong to the standard.

19.3.4.2 Gray-Scale Shape Coding

The gray-scale shape information is encoded by separately encoding the shape and transparency information, as shown in [Figure 19.7](#). For a transparent object, the shape information is referred to as the support function and is encoded using the binary shape

**FIGURE 19.7**

Gray-scale shape coding.

coding method. The transparency or alpha values are treated as the texture of luminance and encoded using padding, MC, and the same 8×8 block DCT approach for the texture coding. For an object with varying alpha maps, shape information is encoded in two steps. The boundary of the object is first losslessly encoded as a binary shape, and then the actual alpha map is encoded as texture coding.

The binary shape coding allows one to describe objects with constant transparency, while grayscale shape coding can be used to describe objects with arbitrary transparency, providing for more flexibility for image composition. One application example is a grayscale alpha shape that consists of a binary alpha shape with the value around the edges tapered from 255 to 0 to provide for a smooth composition with the background. The description of each VO layer includes the information to give instruction for selecting one of six modes for feathering. These six modes include: no effects, linear feathering, constant alpha, linear feathering and constant alpha, feathering filter and feathering filter and constant alpha. The detailed description of the function of these modes is given in the reference of VM 12.0 (ISO/IEC 14496-2 1998).

19.3.5 Sprite Coding

As mentioned previously, MPEG-4 video has investigated several new tools that attempt to improve the coding efficiency at low bit rates compared with MPEG-1/2 video coding. Among these tools, sprite coding is an efficient technology to reach this goal. A sprite is a specially composed VO that is visible throughout an entire piece of video sequence. For example, the sprite generated from a panning sequence contains all the visible pixels of the background throughout the video sequence. Portions of the background may not be seen in certain frames due to the occlusion of the foreground objects or the camera motion. This example is one of the static sprites. In other words, a static sprite is a possible still image. Since the sprite contains all visible background scenes of a segment video sequence where the changes within the background content is mainly caused by camera parameters, the sprite can be used for direct reconstruction of the background VOPs or as the prediction of the background VOPs within the video segment. The sprite coding technology first efficiently transmits this background to the receiver and then stores it in a frame at both encoder and decoder. The camera parameters are then transmitted to the decoder for each frame so that the appropriate part of the background scene can be either used as the direct reconstruction or as the prediction of the background VOP. Both cases can significantly save the coding bits and increase the coding efficiency. There are two types of sprites, static sprite and dynamic sprite, which are being considered as coding tools for MPEG-4 video. A static sprite is used for a video sequence in which the objects in a scene can be separated into foreground objects and a static background. A static sprite is a special VOP that is generated by copying the background from a video sequence. This copying includes the appropriate warping and cropping. Therefore, a static sprite is always built off-line. In contrast, a dynamic sprite is dynamically built during the predictive coding. It can be built either on-line or off-line. The static sprite has shown significant coding gain over existing compression technology for certain video sequences. The dynamic sprite is more complicated in the real-time application due to the difficulty of updating the sprite during the coding. Therefore, the dynamic sprite has not been adopted by version 1 of the standard. Additionally, both sprites are not easily applied to the generic scene content. Also, there is another kind of classification of sprite coding according to the method of sprite generation: off-line and on-line sprites. Off-line is always used for static sprite generation. Off-line sprites are well suited for synthetic objects and objects

that mostly undergoes rigid motion. On-line sprites are only used for dynamic sprites. On-line sprites provide a no-latency solution in the case of natural sprite objects. Off-line dynamic sprites provide an enhanced predictive coding environment. The sprite is built with a similar way in both off-line and on-line methods. In particular, the same global ME algorithm is exploited. The difference is that the off-line sprite is built before starting the encoding process while in the on-line sprite case, both the encoder and the decoder build the same sprite from reconstructed VOPs. This is why the on-line dynamic sprites are more complicated in the implementation. The on-line sprite is not included in version 1 and will most likely not be considered for version 2, either. In sprite coding, the chrominance components are processed in the same way as the luminance components, with the properly scaled parameters according to the video format.

19.3.6 Interlaced Video Coding

Since June of 1997, MPEG-4 extended its application to support interlaced video. Interlaced video consists of two fields per frame, which are referred to as even field and odd field. MPEG-2 has several tools that are used to deal with field structure of video signals. These tools include frame/field-adaptive DCT coding and frame/field-adaptive MC. However, the field issue in MPEG-4 must be considered on a VOP basis instead of the conventional frame basis. When field-based MC is specified, two field MVs and the corresponding reference fields are used to generate the prediction from each reference VOP. The shape information must be considered in the interlaced video for MPEG-4.

19.3.7 Wavelet-Based Texture Coding

In MPEG-4 there is a texture-coding mode that is used to code the texture or still image such as in JPEG. The basic technique used in this mode is the wavelet-based transform coding. The reason for adopting wavelet transform instead of DCT for still-texture coding is not only high coding efficiency, but also because the wavelet can provide excellent scalability, both spatial scalability and SNR scalability. Since the principle of the wavelet-based transform coding for image compression has been explained in [Chapter 8](#), we just briefly describe the coding procedure of this mode. The block diagram of the encoder is shown in [Figure 19.8](#).

19.3.7.1 Decomposition of the Texture Information

The texture or still image is first decomposed into bands using a bank of analysis filters. This decomposition can be applied recursively on the obtained bands to yield a decomposition tree of subbands. An example of decomposition to depth 2 is shown in [Figure 19.9](#).

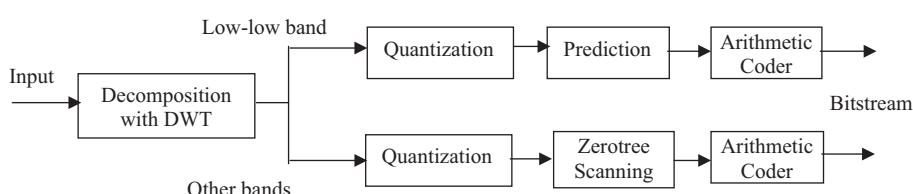
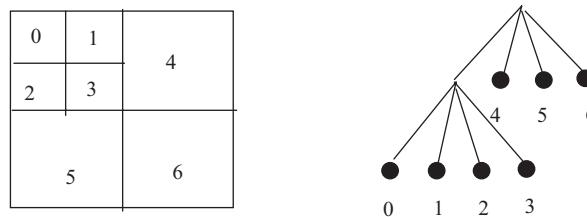


FIGURE 19.8

Block diagram of encoder of wavelet-based texture coding, DWT stands for discrete wavelet transform.

**FIGURE 19.9**

An example of wavelet decomposition of depth 2.

19.3.7.2 Quantization of Wavelet Coefficients

After decomposition, the coefficients of the lowest band are coded independently from the other bands. These coefficients are quantized using a uniform midrise quantizer. The coefficients of high bands are quantized with a multilevel quantization. The multilevel quantization provides a very flexible approach to support the right trade-off between levels and type of scalability, complexity, and coding efficiency for any application. All quantizers for the higher bands are uniform midrise quantizers with a dead zone that is two times the quantizer step size. The levels and quantization steps are determined by the encoder and specified in the bitstream. To achieve scalability, a bi-level quantization scheme is used for all multiple quantizers. This quantizer is also uniform and midrise with a dead zone that is two times the quantization step. The coefficients outside of the dead zone are quantized to one bit. The number of quantizers is equal to the maximum number of bit planes in the wavelet transform representation. In this bi-level quantizer, the maximum number of bit planes instead of quantization step size is specified in the bitstream.

19.3.7.3 Coding of Wavelet Coefficients of Low-Low Band and Other Bands

The quantized coefficients at the lowest band are DPCM coded. Each of the current coefficients is predicted from three other quantized coefficients in its neighborhood in a way shown in [Figure 19.10](#).

$$\text{If } |W_A - W_B| < |W_B - W_C|, W_{Xp} = W_C, \text{ else } W_{Xp} = W_A.$$

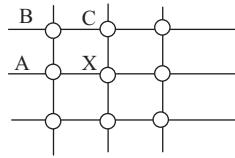
The coefficients in high bands are coded with zerotree algorithm (Shapiro 1993), which has been discussed in [Chapter 8](#).

19.3.7.4 Adaptive Arithmetic Coder

The quantized coefficients and the symbols generated by the zerotree are coded using an adaptive arithmetic coder. In the arithmetic coder three different tables that correspond to the different statistical models have been utilized. The method used here is very similar to one in [Chapter 8](#). The further detail can be found in MPEG-4 VM (ISO/IEC 14496-2 1998).

19.3.8 Generalized Spatial and Temporal Scalability

The scalability framework is referred to as generalized scalability that includes the spatial and the temporal scalability like MPEG-2. The major difference is that



If $|W_A - W_B| < |W_B - W_C|$, $W_{X_p} = W_C$, else $W_{X_p} = W_A$.

FIGURE 19.10
Adaptive DPCM coding of the coefficients in the lowest band.

MPEG-4 extends the concept of scalability to be content-based. This unique functionality allows MPEG-4 to be able to resolve objects into different VOPs. Using the multiple VOP structure, different resolution enhancement can be applied to different portions of a video scene. Therefore, the enhancement layer may be only applied to a particular object or region of the base layer instead of the entire base layer. This is a feature that MPEG-2 does not have.

In spatial scalability, the base layer and the enhancement layer can have different spatial resolution. The base-layer VOPs are encoded in the same way as the non-scalable encoding technique described previously. The VOPs in the enhancement layer are encoded as P-VOPs or B-VOPs as shown in [Figure 19.11](#). The current VOP in the enhancement layer can be predicted from either the upsampled base layer VOP or the previously decoded VOP at the same layer. It can also be predicted using the two methods together. The down-sampling and up-sampling processing in spatial scalability is not a part of the standard and can be defined by the user.

In temporal scalability, a sub-sequence of sub-sampled VOP in the time domain is coded as a base layer. The remaining VOPs can be coded as enhancement layers. In this way, the frame rate of a selected object can be enhanced so that it has a smoother motion than other objects. An example of the temporal scalability is illustrated in [Figure 19.12](#). In 19.12, the VOL0 is the entire frame with both an object and a background, while VOL1 is a particular object in VOL0. VOL0 is encoded with a low frame rate and VOL1 is the enhancement layer. The high frame rate can be reached for the particular object by combining the decoded data from both the base layer and the enhancement layer. Of course, the B-VOP is also used in temporal scalability for coding the enhancement layer, which is another type of temporal scalability. As in spatial scalability, the enhancement layer can be used to improve either the entire base layer frame resolution or only a portion of the base layer resolution.

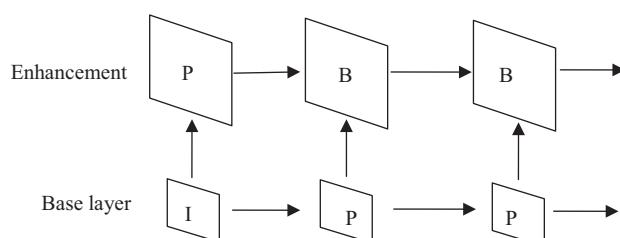


FIGURE 19.11
Illustration of spatial scalability.

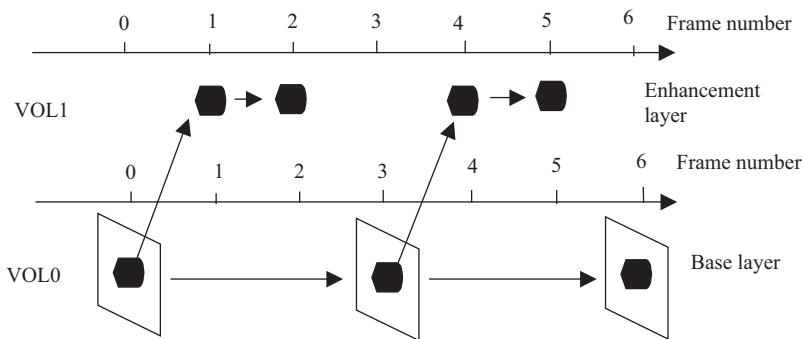


FIGURE 19.12
An example of temporal scalability.

19.3.9 Error Resilience

The MPEG-4 visual coding standard provides error robustness and resilience to allow access of image and video data over a wide range of storage and transmission media. The error resilience tool development effort is divided into three major areas: resynchronization, data recovery, and error concealment. As with other coding standards, MPEG-4 makes heavy use of variable-length coding to reach high coding performance. However, if even one bit is lost or damaged, the entire bitstream becomes undecodable due to loss of synchronization. The resynchronization tools attempt to enable resynchronization between the decoder and the bitstream after a transmission error or errors have been detected. Generally, the data between the synchronization point prior to the error and the first point, where synchronization is reestablished, is discarded. The purpose of resynchronization is to effectively localize the amount of data discarded by the decoder, then the other methods such as error concealment can be used to conceal the damaged areas of a decoded picture. Currently, the resynchronization approach adopted by MPEG-4 is referred to as a packet approach. This approach is like the group of blocks (GOBs) structure used in H.261 and H.263. In the GOB structure, the GOB contains a start code, which provides the location information of the GOB. MPEG-4 adopted a similar approach in which a resynchronization marker is periodically inserted into the bitstream at the particular macroblock locations. The resynchronization marker is used to indicate the start of a new video packet. This marker is distinguished from all possible VLC codewords as well as the VOP start code. The packet header information is then provided at the start of a video packet. The header contains the information necessary to restart the decoding process. These include the macroblock number of the first macroblock contained in this packet and the quantization parameter necessary to decode the first macroblock. The macroblock number provides the necessary spatial resynchronization while the quantization parameter allows the differential decoding process to be resynchronized. It should be noted that when the error resilience is used within MPEG-4, some of the compression efficiency tools need to be modified. For example, all predictively encoded information must be contained within a video packet to avoid error propagation. In conjunction with the video packet approach to resynchronization, MPEG-4 has also adopted fixed interval synchronization method, which requires that VOP start codes and resynchronization markers appear only at legal fixed interval locations in the bitstream. This will help to avoid the problems associated with start codes emulation. In this case, when fixed interval synchronization is utilized, the decoder is only required to search for a VOP start code at

the beginning of each fixed interval. The fixed interval synchronization method extends this approach to be any predetermined interval.

After resynchronization is reestablished, the major problem is recovering lost data. A new tool called reversible variable-length codes (RVLC) is developed for the purpose of data recovery. In this approach, the variable length codes are designed such that the codes can be read both in the forward as well as the reverse direction. An example of such code includes a codeword like 111, 101, 010. All these codewords can be read reversibly. However, it is obvious that this approach will reduce the coding efficiency that is achieved by the entropy coder. Therefore, this approach is used only in the case where the error resilience is important.

Error concealment is an important component of any error-robust video coding. The error-concealment strategy is highly dependent on the performance of the resynchronization technique. Basically, if the resynchronization method can efficiently localize the damaged data area, the error-concealment strategy becomes much more tractable. Error concealment is a decoder issue if there is no additional information provided by the encoder. There are many approaches of error concealment, which can be referred to in [Chapter 17](#).

19.4 MPEG-4 Visual Bitstream Syntax and Semantics

The common feature of MPEG-4 with MPEG-1 and MPEG-2 is the layered structure of the bitstream. MPEG-4 defines a syntactic description language to describe the exact binary syntax of an AVO bitstream, as well as that of the scene description information. This provides a consistent and uniform way of describing the syntax in a very precise form, while at the same time it simplifies bitstream compliance testing. The visual syntax hierarchy includes the layers of:

- Video session (VS)
- VO
- Video object layer (VOL) or texture object layer (TOL)
- Group of video object planes (GOV)
- VOP

A typical video syntax hierarchy is shown in [Figure 19.13](#).

The video session (VS) is the highest syntactic structure of the coded video bitstream. A VS is a collection of one or more VOs. A VO can consist of one or more layers. Since MPEG-4 is extended from video coding to visual coding, the type of visual objects not only includes video objects, but also still texture objects, mesh objects, and face objects. These layers can be either video or texture. Still texture coding is designed for high visual quality applications in transmission and rendering of texture. The still coding algorithm supports a scalable representation of image or synthetic scene data such as luminance, color, and shape. This is very useful for progressive transmission of images or 2D/3D synthetic scenes. The images can be gradually built-up in the terminal monitor as they are received. The bitstreams for coded mesh objects are non-scalable; they define the structure and motion of a 2D mesh. The texture of the mesh must be coded as a separate video object.

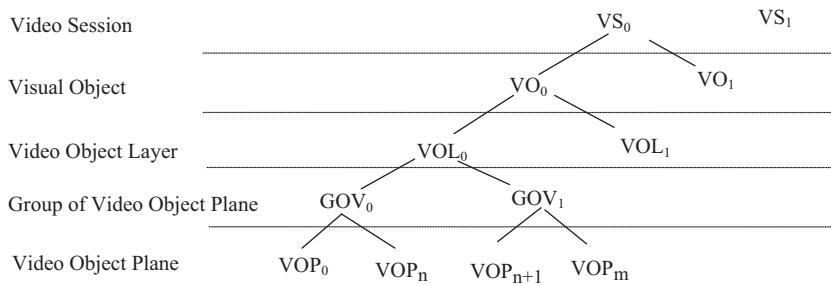


FIGURE 19.13
MPEG-4 video syntax hierarchy.

The bitstreams for face objects are also non-scalable; these bitstreams contain the face animation parameters. Video objects are coded with different types of scalability. The base layer can be decoded independently and the enhancement layers can only be decoded with the base layer. In the special case of a single rectangular VO, all the MPEG-4 layers can be related to MPEG-2 layers. That is, VS is the same as VO since in this case a single VO is a video sequence, VOL or TOL is the same as the sequence scalable extension, GOV is like the GOP and VOP is a video frame. Visual object sequence may contain one or more visual objects coded concurrently. The visual object header information contains the start code followed by profile and level identification and a visual object identification to indicate the type of object, which may be a video object, a still texture object, a mesh object, or a face object. The VO may contain one or more VO layers. In the VO layer, the VO can be coded with spatial or temporal scalability. Also, the VO may be encoded in several layers from coarse to fine resolution. Depending on the application need, the decoder can choose the number of layers to decode. A VO at a specified time is called a VOP. Thus, a VO contains many VOPs. A scene may contain many VOs. Each VO can be encoded to an independent bitstream. A collection of VOPs in a VOL is called a group of VOPs (GOV). This concept corresponds to the group of pictures (GOP) in MPEG-1 and MPEG-2. A VOP is then coded by shape coding and texture coding, which is specified at lower layers of syntax, such as macroblock and block layer. The VOP or higher-than-VOP layer always commences with a start code and is followed by the data of lower layers, which is like the MPEG-1 and MPEG-2 syntax.

19.5 MPEG-4 Visual Profiles and Levels

In MPEG-4, many profiles have been defined. In this section, we have only introduced some visual profiles. There is a total of 19 visual profiles defined for different applications:

- Simple
- Simple Scalable
- Core
- Main
- N-Bit

- Hybrid
- Basic Animated Texture
- Scalable Texture
- Simple Face Animation
- Simple FBA
- Advanced Real-Time Simple
- Core Scalable
- Advanced Coding Efficiency
- Advance Core Profile
- Advanced Scalable Texture
- Simple Studio
- Core Studio
- Advanced Simple
- FGS

Among these visual profiles, two profiles—simple profile and advanced simple profile—have been extensively used by industry for mobile application and streaming on the networks.

The simple profile is used to code the rectangular video with intra (I) and predicted (P) VOPs, as with MPEG-2 frame-based coding. The simple profile permits the use of three compression levels with bit rates from 64 kbps in Level 1 to 384 kbps in Level 3.

The advanced simple profile is also used to code the rectangular video with intra (I) and predicted (P) VOPs, but it is enhanced to add bidirectional (B) VOPs for better coding efficiency than the simple profile. It supports six compression levels (0 to 5). Levels 0 to 3 have bit rates from 128 to 768 kbps. The support for interlaced coding is added for Levels 4 and 5 with bit rates from 3 to 8 Mbps.

19.6 MPEG-4 Video Verification Model

Since all video-coding standards define only the bitstream syntax and decoding process, the use of a test model to verify and optimize the algorithms is needed during the development process. For this purpose, a common platform with a precise definition of encoding and decoding algorithms must be provided. The test model (TM) of MPEG-2 took the above-mentioned role. The TM of MPEG-2 was updated continually from version 1.0 to version 5.0, until the MPEG-2 Video IS was completed. MPEG-4 video uses a similar tool during the development process; this tool in MPEG-4 is called the verification model (VM). So far, the MPEG-4 video VM has gradually evolved from version 1.0 to version 12.0 and in the process has addressed an increasing number of desired functionalities such as content-based scalability, error resilience, coding efficiency, and so on. The material presented in this section is different from [section 19.3](#). [Section 19.3](#) presented the technologies adopted or will be adopted by MPEG-4, while this section provides an example how to use the standard—for example, how to encode or generate the MPEG-4 compliant bitstream. Of course, the decoder is also included in the VM.

19.6.1 VOP-Based Encoding and Decoding Process

Since the most important feature of MPEG-4 is an object-based coding method, the input video sequence is first decomposed into separate video objects (VOs); these video objects are then encoded into separate bitstreams so that the user can access and manipulate (cut, paste, etc.) the video sequence in the bitstream domain. Instances of VO in a given time are called VOPs. The bitstream contains also the composition information to indicate where and when each VOP is to be displayed. At the decoder, the user may be allowed to change the composition of the scene displayed by interactively changing the composition information.

19.6.2 Video Encoder

For an object-based coding, the encoder mainly consists of two parts: the shape coding and the texture coding of the input VOP. The texture coding is based on the DCT coding with traditional motion-compensated predictive coding. The VOP is represented by means of a bounding rectangular as described previously. The phase between luminance and chrominance pixels of the bounding rectangular must be correctly set to the 4:2:0 format as in MPEG-1/2. The block diagram of encoding structure is shown in [Figure 19.14](#).

The core technologies used in VOP coding of MPEG-4 have been described previously. Here we are going to discuss several encoding issues. Although these issues are essential to the performance and application, they are not dependent on the syntax. As a result, they are not included as normative parts of the standard, but are included as informative annexes.

19.6.2.1 Video Segmentation

Object-based coding is the most important feature of MPEG-4. Therefore, the tool for object boundary detection or segmentation is a key issue in efficiently performing the object-based coding scheme. But the method of decomposing a natural scene to several separate objects is not specified by the standard since it is a pre-processing issue.

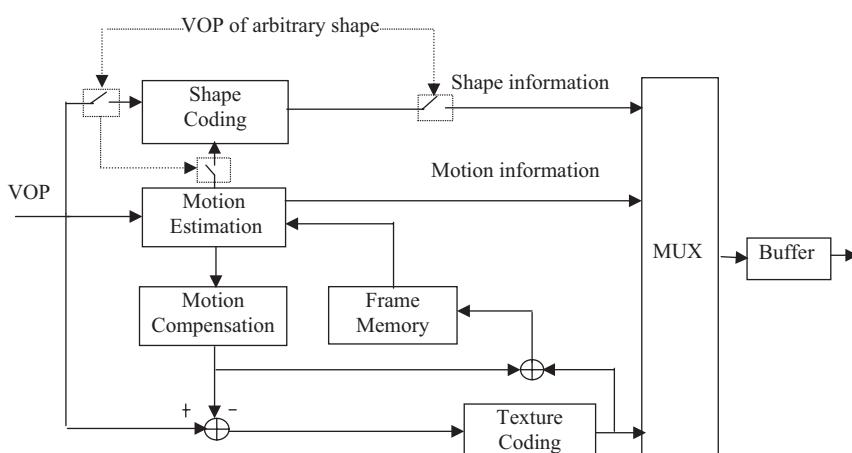


FIGURE 19.14

Block diagram of MPEG-4 video encoder structure.

There are currently two kinds of algorithms for segmentation of video objects. One kind of algorithm is an automatic segmentation algorithm. In the case of real-time applications, the segmentation must be done automatically. Real-time automatic segmentation algorithms are currently not mature. An automatic segmentation algorithm has been proposed in Colonnese (1996). This algorithm separates regions corresponding to moving objects from regions belonging to a static background for each frame of a video sequence. The algorithm is based on a motion analysis for each frame. The motion analysis is performed along several frames to track each pixel of the current frame and to detect whether the pixel belongs to the moving objects.

Another kind of segmentation algorithm is one that is user-assisted or “semi-automatic.” In non-real-time applications, the semi-automatic segmentation may be used effectively and give better results than the automatic segmentation. In the core experiments of MPEG-4, a semi-automatic segmentation algorithm was proposed in Choi et al. (1998). The block diagram of the semi-automatic segmentation is shown in [Figure 19.15](#).

This technique consists of two steps. First, the intra-frame segmentation is applied to the first frame, which is considered as a frame that either contains newly appeared objects or a reset frame. Then the inter-frame segmentation is applied to the consecutive frames. For intra-frame, the segmentation is processed by a user manually or semi-automatically. The user uses a graphical user interface (GUI) to draw the boundaries of interested objects. The user can mask the entire objects all the way around objects using a mouse with a predefined thickness of the line (number of pixels). A marked swath is then resulted by the mouse and this marked area is assumed to contain the object boundaries. A boundary detection algorithm is applied to the marked area to create the real object boundaries. For inter-frame segmentation, an object boundary-tracking algorithm is proposed to obtain the object boundaries of the consecutive frames. At first, the boundary of the previous object is extracted and the ME is performed on the object boundary. The object boundary of the current frame is initially obtained by MC and then refined by using temporal information and spatial information all the way around the object boundary. Finally, the refined object boundary can be obtained. As mentioned previously, the segmentation technique is

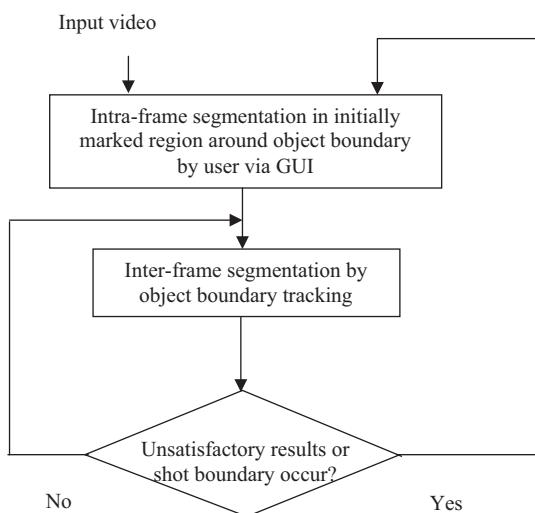


FIGURE 19.15

Block diagram of a user-assisted VO segmentation method.

an important tool for object-based processing in MPEG-4, but it is not defined by the standard. The method described here is just an example provided by the core experiments of MPEG-4. There are many other algorithms under investigation such as the circular Viterbi algorithm described in Lin et al. (1998).

19.6.2.2 Intra/Inter Mode Decision

For inter-VOP coding, a macroblock can be coded in one of the four modes. These four modes include direct coding mode, forward coding, backward coding, and bi-directional coding. In the encoder we must decide which mode is the best. The mode decision is the important part of encoding optimization. An example of the selection of optimized mode decision has been given in [Chapter 17](#) for MPEG-2 encoder. The same technique can be extended to an MPEG-4 encoder. The basic idea of mode decision is to choose the coding mode that results in the best operation point on the rate distortion curve. For obtaining the best operation point on the rate distortion curve, the encoder must compare all possible coding modes and choose the best one. This is a very complicated procedure. In the MPEG-2 case, we used a quadratic model to unify the measures of bits used to code prediction residues and the MVs. A simplified mode but near-optimized mode decision method has resulted. Here, the VM.12 proposes the following steps to make coding mode decisions. First, the motion-compensated prediction error is calculated by each of the four modes. Next, the SAD of each of the motion-compensated prediction macroblocks is calculated and compared with the variance of the macroblock to be coded. Then a mode of generating the smallest SAD (for direct mode, a bias is applied) is selected. For the interlaced video, more coding modes are involved. This method of mode decision is simple, but it is not optimal since the cost for coding MVs is not considered. Consequently, the mode may not lie on the best operation point on the distortion curve. But again, this is an encoding issue, and the encoding designers have the freedom to use their own algorithm. The VM just provides an example of an encoder that can generate the compliant bitstream.

19.6.2.3 Off-line Sprite Generation

The sprite is a useful tool in MPEG-4 for coding a certain kind of video sequences at very low bit rates. The method of generating a sprite for a video sequence is an encoder issue. The VM gives an example of off-line sprite generation. For a natural video object, sprite is referred to as a representative view collected from a video sequence. Before decoding, the sprite is transmitted to the decoder. Then the MC can be performed by using the sprite from which the video can be reconstructed. The effectiveness of video reconstruction depends on whether the motion of the object can be effectively represented by a global motion model such as translation, zooming, affine, and perspective. The key technology of the sprite generation is the ME to find perspective motion parameters. This can be implemented by many algorithms described in this book such as the three-step matching technique. The block diagram of sprite generation using the perspective ME is shown as in [Figure 19.16](#).

The sprite is generated from the input video sequence by the following steps. First, the first frame is used as the initial value of sprite. From the second frame, the ME is applied to find the perspective motion parameters between two frames. The current frame is wrapped towards the initial sprite using the perspective MVs to get wrapped image. Then the wrapped image is blended with initial sprite to obtain an updated sprite. This procedure is continued to the entire video sequence. The final sprite is then generated.

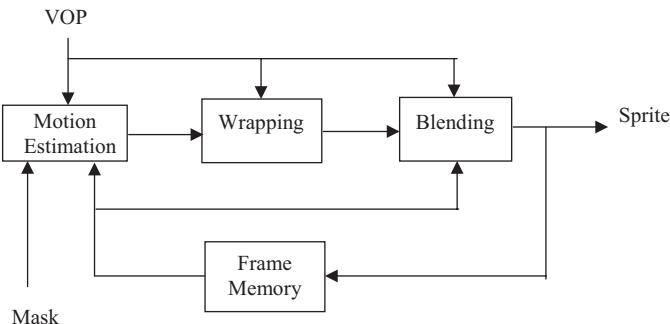


FIGURE 19.16
Block diagram of sprite generation.

19.6.2.4 Multiple VO Rate Control

As we know, the purpose of rate control is to obtain the best coding performance for a given bit rate in the constant bit rate video coding. In MPEG-4 video coding, there is an additional objective for rate control, how to assign the bits among multiple video objects. In the multiple VO video coding rate-control algorithm, the total target is first adjusted based on the buffer fullness and then distributed proportional to the size of the object, the motion that the object is experiencing, and its maximum absolute differences. Based on the new individual targets and second-order model parameters (Lee et al. 1997), appropriate quantization parameters can be calculated for each video object. To compromise the tradeoffs in spatial and temporal coding, two modes of operation have been introduced. With these modes, suitable decisions can be made to differentiate between low- and high-bit-rate coding. In addition, a shape-rate control algorithm has been included. The algorithm for performing the joint rate control can be decomposed into a pre-encoding stage and a post-encoding. The pre-encoding stage consists of: i) the target bit estimation, ii) joint buffer control, iii) pre-frameskip control, and iv) the quantization level and alpha threshold calculation, whereas the post-encoding stage consists of: i) updating the rate-distortion model, ii) post-frameskip control, and iii) determining mode of operation. The initialization process is very similar to the single VOP initialization process. Since a single buffer is used, the buffer drain rate and initializations remains the same, but many of the parameters are extended to vector quantities. As a means of regulating the trade-offs between spatial and temporal coding, two modes of operation are introduced: low mode and high mode. When encoding at high bit rates, the availability of bits allows the algorithm to be flexible in its target assignment to each VO. Under these circumstances, it is reasonable to impose homogeneous quality among each VO. Therefore, the inclusion of $MAD^2[i]$ is essential to the target distribution and should carry the highest weighting. On the other hand, when the availability of bits is limited, it is very difficult (if not impossible) to achieve homogeneous quality among the VO. Under these conditions, it is desirable to spend less bits on the background and more bits on the foreground. Consequently, the significance of the variance has decreased and the significance of the motion has increased. Besides regulating the quality within each frame, it is also important to regulate the temporal quality as well, i.e., keep the frame skipping to a minimum. In high mode, this is very easy to do since the availability of bits is plentiful. However, in low mode, frame skipping occurs much more often. In fact, the number of frames being skipped is a good indication of which mode the algorithm should be operating. Overall, this algorithm can successfully achieve the target bit rate, effectively code arbitrarily shaped objects, and maintain a stable buffer (Vetro et al. 1999).

19.6.3 Video Decoder

The decoder mainly consists of three parts: shape, motion, and texture decoding. The decoder block diagram is shown in [Figure 19.17](#). At the decoder the bitstream is first demultiplexed into shape information and motion information as well as texture information. The reconstructed VOP is obtained by the right combination of the shape, texture, and motion information. The shape decoding is a unique feature of the MPEG-4 decoder. The basic technology of shape decoding is the context-based arithmetic decoding and block-based MC.

The primary data structure is denoted is the BAB. The BAB is a square block of binary pixels representing the opacity or transparency for the pixels in a specified block-shaped spatial region of size 16×16 pixels that is co-located with each texture macroblock. The block diagram of texture decoder is shown in [Figure 19.18](#).

The texture decoding is like the video decoder in MPEG-1/2 except with the inverse DC/AC prediction and more quantization methods. The DC prediction is different from the one used in MPEG-1/2. In MPEG-4 the DC coefficient is adaptively predicted from the above block or left block. The AC prediction is like the one used in H.263 but is not used in the MPEG-1/2. For MC, the MVs must be decoded. The horizontal and vertical MV components are decoded differentially by using a prediction from the spatial neighborhood consisting of three MVs already decoded. The final MV is obtained by adding the prediction MV values to the decoded differential motion values. Also, in MPEG-4 video coding the several advanced MC modes such as four 8×8 MV compensation and overlapped MC must be handled. The other issue of MC in MPEG-4 is raised by VOP-based coding.

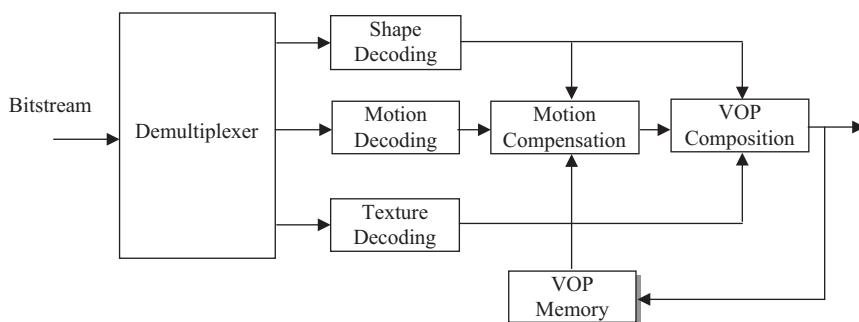


FIGURE 19.17
VOP decoder structure.

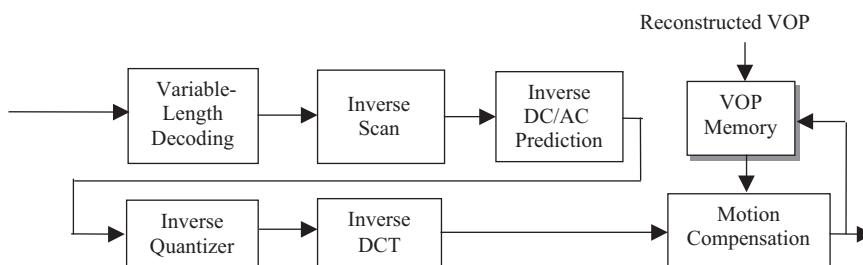


FIGURE 19.18
Block diagram of texture decoding.

To perform motion-compensated prediction on a VOP basis, a special padding technique is used to each macroblock that lies on the shape boundary of the VOP. The padding process defines the values of pixels that are located outside the VOP for prediction of arbitrary-shaped objects. Padding for luminance pixels and chrominance pixels is defined in the standard [mpeg4 visual]. The additional decoding issues that are special for MPEG-4 include sprite decoding, generalized scalable decoding, and still texture decoding. We do not go into further detail for these topics. Interested readers can get detail from the standard documents. The outputs of decoded results are the reconstructed VOPs that are finally sent to the compositor. In the compositor, the VOPs are recursively blended in the order specified by the VOP composition order. It should be noted that the decoders could take advantage of object-based decoding. They can be flexible in the composition of the reconstructed VOPs such as re-allocating, rotation, or other editing actions.

19.7 Summary

In this chapter, the new video coding standard, MPEG-4, has been introduced. The unique feature of MPEG-4 video is the content-based coding. This feature allows the MPEG-4 to provide much functionality that other video coding standards do not have. The key technologies used in MPEG-4 video have been described. These technologies provide basic tools for MPEG-4 video to provide object-based coding functionality. Finally, the video verification model, a platform of MPEG-4 development, and an encoding and decoding example have been described.

Exercises

- 19.1 Why is object- (or content)-based coding the most important feature of the MPEG-4 visual coding standard? Describe several applications for this feature.
- 19.2 What are the new coding tools in MPEG-4 visual coding that are different from MPEG-2 video coding? Is MPEG-4 backward compatible to MPEG-2?
- 19.3 MPEG-4 video coding has the feature of using either 16×16 block MV or 8×8 block MV; for what kind of video sequences will the 8×8 block motion increase coding efficiency? For what kind of video sequences will the 8×8 block MC decrease the coding efficiency?
- 19.4 What approaches for error resilience are supported by the MPEG-4 syntax? Make a comparison with the error resilience method adopted in MPEG-2 (supported by MPEG-2 syntax) and indicate their relative advantages and disadvantages.
- 19.5 Design an arithmetic coder for zerotree coding and write a program to test it with several images.
- 19.6 The sprite is a new feature of MPEG-4 video coding. MPEG-4 specifies the syntax for sprite coding, but does not give any detail how to generate a sprite. Conduct a

project to generate an off-line sprite for a video sequence and use it for coding the video sequence. Do you observe any increased coding efficiency? When do you expect to see such an increase?

- 19.7 Shape coding (binary-shape coding) is an important part of MPEG-4 due to object-based coding. Beside the shape coding method used in MPEG-4, name another shape coding method. Conduct a project to compare the method you know with the method proposed in MPEG-4. (Do not expect to get better performance, but expect to reduce the complexity).
-

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20

ITU-T Video Coding Standards H.261 and H.263

This chapter introduces ITU-T video coding standards H.261 and H.263, which are established mainly for videophony and videoconferencing. The basic technical detail of H.261 is presented. The technical improvements with which H.263 achieves high coding efficiency are discussed. Features of H.263+, H.263++, and H.26L are presented.

20.1 Introduction

Very-low-bit-rate video coding has found many industry applications such as wireless and network communications. The rapid convergence of standardization of digital video coding standards is the reflection of several factors: the maturity of technologies in terms of algorithmic performance, hardware implementation with VLSI technology, and the market need for rapid advances in wireless and network communications. As stated in the previous chapters, these standards include JPEG for still image coding and MPEG-1/2 for CD-ROM storage and digital television (DTV) applications. In parallel with the ISO/IEC development of the MPEG-1/2 standards, the ITU-T has developed H.261 (ITU-T Recommendation H.261 1993) for video-telephony and video-conferencing applications in an ISDN environment.

20.2 H.261 Video Coding Standard

The H.261 video coding standard was developed by ITU-T study group XV from 1988 to 1993. It was adopted in 1990 and the final revision approved in 1993. This is also referred to as the Px64 standard because it encodes the digital video signals at the bit rates of Px64 Kbps, where P is an integer from 1 to 30, i.e., at the bit rates 64 Kbps to 1.92 Mbps.

20.2.1 Overview of H.261 Video Coding Standard

The H.261 video coding standard has many common features with the MPEG-1 video coding standard. However, since they target different applications, there exist many differences between the two standards such as data rates, picture quality, end-to-end delay, and others. Before indicating the differences between two coding standards, we describe the major similarity between H.261 and MPEG-1/2. First, both standards are used to code the similar video format. H.261 is mainly used to code the video with CIF or QCIF spatial resolution for teleconference application. MPEG-1 uses CIF, SIF, or higher spatial resolution

for CD-ROM application. The original motivation of developing the H.261 video coding standard was to provide a standard that can be used for both PAL and NTSC television signals. Now, however, the H.261 is mainly used for video conferencing and the MPEG-1/2 is used for DTV, Video CD (VCD), and Digital Video Disk (DVD). The two TV systems, PAL and NTSC, use different line and picture rates. The NTSC, which is used in North America and Japan, uses 525 lines per interlaced picture at 30 frames per second. The PAL system is used for most other countries and it uses 625 lines per interlaced picture at 25 frames per second. For this purpose, the common intermediate format (CIF) was adopted as the source video format for H.261 video coder. The CIF format consists of 352 pixels per line, 288 lines per frame, and 30 frames per second. This format represents half the active lines of the PAL signal and the same picture rate of the NTSC signal. The PAL systems need only perform a picture rate conversion and NTSC systems need only perform a line numbers conversion. Color pictures consist of one luminance and two color-difference components (referred to as YC_bC_r format) as specified by the CCIR 601 standard. The C_b and C_r components are half the size in both the horizontal and vertical directions and have 176 pixels per line and 144 lines per frame. Another format, quarter-CIF (QCIF) is used for very-low-bit-rate applications. QCIF has half the number of pixels and half the number of lines of the CIF format. Secondly, the key coding algorithms of H.261 and MPEG-1 are very similar. Both H.261 and MPEG-1 use DCT-based coding to remove intra-frame redundancy and motion compensation to remove inter-frame redundancy.

Now let us to describe the main differences between the two coding standards with respect to coding algorithms. The main differences include:

H.261 uses only I and P -macroblocks (MBs) but no B -MBs while MPEG-1 uses three MB types, I -, P -, and B -MBs (I -MB is intra-frame coded MB, P -MB is predictive coded MB, and B -MB is bi-directionally coded MB) as well as three picture types, I -, P -, and B -pictures, as defined in [Chapter 16](#) for the MPEG-1 standard.

There is a constraint of H.261 that for every 132 inter-frame coded MBs, which corresponds to four groups of blocks (GOBs) or to one third of CIF pictures, it requires at least one intra-frame-coded MB. In order to obtain better coding performance in low-bit-rate applications, most encoding schemes of H.261 prefer not to use intra-frame coding on all the MBs of a picture but only on a few MBs in every picture with a rotational scheme. MPEG-1 uses the group of pictures (GOP) structure, where the size of GOP (the distance between two I-pictures) is not specified.

The end-to-end delay is not a critical issue for MPEG-1 but is critical for H.261. The video encoder and video decoder delays of H.261 need to be known to allow audio compensation delays to be fixed when H.261 is used in interactive applications. This will allow lip synchronization to be maintained.

The accuracy of motion compensation in MPEG-1 is up to a half-pixel, but only a full-pixel in H.261. However, H.261 uses a loop-filter to smooth the previous frame. This filter attempts to minimize the prediction error.

In H.261, a fixed picture aspect ratio of 4:3 is used. In MPEG-1, several picture aspect ratios can be used and the picture aspect ratio is defined in the picture header.

Finally, in H.261, the encoded picture rate is restricted to allow up to three skipped frames. This would allow the control mechanism in the encoder some flexibility to control the encoded picture quality and satisfy the buffer regulation. Although MPEG-1 has no restriction on skipped frames, the encoder usually does not perform frame skipping. Rather, the syntax for B-frames is exploited, as B-frames require much fewer bits than P-pictures.

20.2.2 Technical Detail of H.261

The key technologies used in the H.261 video coding standard are the DCT and motion compensation. The main components in the encoder include DCT, prediction, quantization (Q), inverse DCT (IDCT), inverse quantization (IQ), loop filter, frame memory, variable length coding (VLC), and coding control unit. A typical encoder structure is shown in [Figure 20.1](#).

The input video source is first converted to the CIF frame and then is stored in the frame memory. The CIF frame is then partitioned into GOBs. The GOB contains 33 MBs, which are one-twelfth of a CIF picture or one-third of a QCIF picture. Each MB consists of six 8×8 blocks, among which four are luminance (Y) blocks and two are chrominance blocks (one of C_b and one of C_r).

For intra-frame mode, each 8×8 block is first transformed with DCT and then quantized. The VLC is applied to the quantized DCT coefficients with a zigzag scanning order such as in MPEG-1. The resulting bits are sent to the encoder buffer to form a bitstream.

For inter-frame coding mode, the frame prediction is performed with motion estimation in a similar manner to that in MPEG-1, but only P-MBs and P-pictures and no B-MBs and B-pictures are used. Each 8×8 block of differences or prediction residues is coded by the same DCT coding path as for the intra-frame coding. In the motion-compensated predictive coding, the encoder should perform the motion estimation with the reconstructed pictures instead of the original video data, as it will be done in the decoder. Therefore, the IQ and IDCT blocks are included in the motion-compensation loop to reduce the error propagation drift. Since the VLC operation is lossless, there is no need to include the VLC block in the motion-compensation loop. The role of spatial filter is to minimize the prediction error by smoothing the previous frame that is used for motion compensation.

The loop filter is a separable 2-D spatial filter that operates on an 8×8 block. The corresponding 1-D filters are non-recursive with coefficients 1/4, 1/2, and 1/4. At block boundaries, the coefficients are 0, 1, and 0 to avoid having the taps fall outside the block. It should be noted that MPEG-1 uses sub-pixel-accurate motion vectors

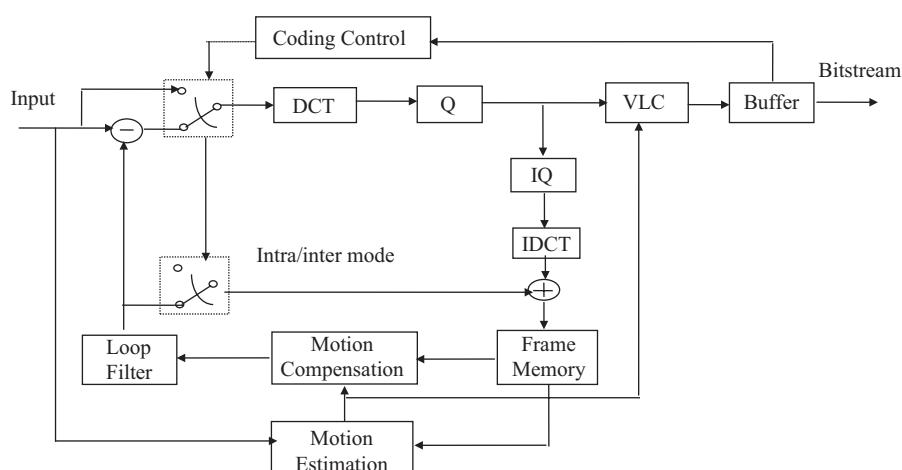


FIGURE 20.1
Block diagram of a typical H.261 video encoder.

instead of a loop filter to smooth the anchor frame. The performance comparison of the two methods should be interesting.

The role of coding control includes the rate control, the buffer control, the quantization control, and the frame rate control. These parameters are intimately related. The coding control is not part of the standard; however, it is an important part for the encoding process. For a given target bit rate, the encoder has to control several parameters to reach the rate target and at the same time provide reasonable coded picture quality.

Since H.261 is a predictive coder and the VLCs are used everywhere such as coding quantized DCT coefficients and motion vectors, a single transmission error may cause a loss of synchronization and consequently cause problems for the reconstruction. To enhance the performance of the H.261 video coder in the noisy environment, the transmitted bitstream of H.261 can optionally contain a Bose, Chaudhuri, and Hocquengham (BCH) (511,493) forward error correction code.

The H.261 video decoder performs the inverse operations of the encoder. After optional error-correction decoding, the compressed bitstream enters the decoder buffer and then is parsed by the variable-length decoder (VLD). The VLD output is applied to the IQ and IDCT where the data are converted to the values in the spatial domain. For inter-frame coding mode, the motion compensation is performed and the data from the MBs in the anchor frame are added to the current data to form the reconstructed data.

20.2.3 Syntax Description

The syntax of H.261 video coding has a hierarchical layered structure. From the top to the bottom the layers are: picture layer, group of blocks (GOB) layer, MB layer, and block layer.

20.2.3.1 Picture Layer

The picture layer begins with a 20-bit picture start code (PSC). Following the PSC, there are temporal reference (five-bit), picture type information (PTYPE, six-bit), extra insertion information (PEI, one-bit) and spare information (PSPARE). Then the data for GOBs are followed.

20.2.3.2 Group of Blocks Layer

A GOB corresponds to 176 pixels by 48 lines of Y and 88 pixels by 24 lines of C_b and C_r . The GOB layer contains the following data in order: 16-bit GOB start code (GBSC), four-bit group number (GN), five-bit quantization information (GQUANT), one-bit extra insertion information (GEI), and spare information (GSPARE). The number of bits for GSPARE is variable depending on the set of GEI bit. If GEI is set to "1," then nine bits follow, consisting of eight bits of data and another GEI bit to indicate whether a further nine bits follow and so on. Data of GOB header is then followed by data for MBs.

20.2.3.3 Macroblock Layer

Each GOB contains 33 MBs, which is arranged as in [Figure 20.2](#).

A MB consists of 16 pixels by 16 lines of Y that spatially correspond to eight pixels by eight lines of each C_b and C_r . Data in the bitstream for a MB consists of an MB

| | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 |
| 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 |

FIGURE 20.2

Arrangement of MBs in a GOB.

header followed by data for blocks. The MB header may include MB address (MBA) (variable length), type information (MTYPE) (variable length), quantizer (MQUANT) (five bits), motion vector data (MVD) (variable length), and coded block pattern (CBP) (variable length). The MBA information is always present and is coded by variable-length code (VLC). The VLC table for MB addressing is shown in [Table 20.1](#). The presence of other items depends on MB type information, which is shown in the VLC [Table 20.2](#).

20.2.3.4 Block Layer

Data in the block layer consists of the transformed coefficients followed by an end-of-block (EOB) marker (10). The data of transform coefficients (TCoeff) is first converted to the pairs of RUN and LEVEL according to the zigzag scanning order. The RUN represents the number of successive zeros and the LEVEL represents the value of non-zero coefficients. The pairs of RUN and LEVEL are then encoded with VLCs. The DC coefficient of an intra block is coded by a fixed length code with eight bits. All VLC tables can be found in the standard document (ITU-T Recommendation H.261 1993).

TABLE 20.1

VLC Table for Macroblock Addressing

| MBA | Code | MBA | Code | MBA | Code |
|-----|-----------|-----|---------------|--------------|---------------------|
| 1 | 1 | 13 | 0000 1000 | 25 | 0000 0100 000 |
| 2 | 011 | 14 | 0000 0111 | 26 | 0000 0011 111 |
| 3 | 010 | 15 | 0000 0110 | 27 | 0000 0011 110 |
| 4 | 0011 | 16 | 0000 0101 11 | 28 | 0000 0011 101 |
| 5 | 0010 | 17 | 0000 0101 10 | 29 | 0000 0011 100 |
| 6 | 0001 1 | 18 | 0000 0101 01 | 30 | 0000 0011 011 |
| 7 | 0001 0 | 19 | 0000 0101 00 | 31 | 0000 0011 010 |
| 8 | 0000 111 | 20 | 0000 0100 11 | 32 | 0000 0011 001 |
| 9 | 0000 110 | 21 | 0000 0100 10 | 33 | 0000 0011 000 |
| 10 | 0000 1011 | 22 | 0000 0100 011 | MBA stuffing | 0000 0001 111 |
| 11 | 0000 1010 | 23 | 0000 0100 010 | Start code | 0000 0000 0000 0001 |
| 12 | 0000 1001 | 24 | 0000 0100 001 | | |

TABLE 20.2

VLC Table for Macroblock Type

| PREDICTION | MQUANT | MVD | CBP | TCOEFF | VLC |
|------------------|--------|-----|-----|--------|--------------|
| Intra | | | | x | 0001 |
| Intra | x | | | x | 0000 001 |
| Inter | | | x | x | 1 |
| Inter | x | | X | x | 0000 1 |
| Inter + MC | | x | | | 0000 0000 1 |
| Inter + MC | | x | X | x | 0000 0001 |
| Inter + MC | x | x | X | x | 0000 0000 01 |
| Inter + MC + FIL | | x | | | 001 |
| Inter + MC + FIL | | x | X | x | 01 |
| Inter + MC + FIL | x | x | x | x | 0000 01 |

Notes:

1 "x" means that the item is present in the MB.

2 It is possible to apply the filter in a non-motion-compensated MB by declaring it as MC + FIL but with a zero vector.

20.3 H.263 Video Coding Standard

The H.263 video coding standard (ITU-T Recommendation H.263 1996) is specifically designed for very-low-bit-rate applications such as practical video telecommunication. Its technical content was completed in late 1995 and the standard was approved in early 1996.

20.3.1 Overview of H.263 Video Coding

The basic configuration of the video source coding algorithm of H.263 is based on the H.261. Several important features that are different from H.261 include the following new options: unrestricted-motion vectors, syntax-based arithmetic coding, advanced prediction, and PB-frames. All these features can be used together or separately for improving the coding efficiency. The H.263 video standard can be used for both 625-line and 525-line television standards. The source coder operates on the non-interlaced pictures at picture rate about 30 pictures per second. The pictures are coded as luminance and two-color difference components (Y , C_b , and C_r). The source coder is based on a CIF. Actually, there are five standardized formats: sub-QCIF, QCIF, CIF, 4CIF, and 16CIF. The detail of formats is shown in [Table 20.3](#).

It is noted that for each format, the chrominance is a quarter size of the luminance picture, i.e., the chrominance pictures are half the size of the luminance picture in both horizontal and vertical directions. This is defined by the ITU-R 601 format. For CIF format, the number of pixels per line is compatible with sampling the active portion of the luminance and color difference signals from a 525 or 626-line source at 6.75 MHz and 3.375 MHz, respectively. These frequencies have a simple relationship to those defined by the ITU-R 601 format.

TABLE 20.3

Number of Pixels Per Line and the Number of Lines for Each Picture Format

| Picture Format | Number of Pixels for Luminance (dx) | Number of Lines for Luminance (dy) | Number of Pixels for Chrominance (dx/2) | Number of Lines for Chrominance (dy/2) |
|----------------|-------------------------------------|------------------------------------|---|--|
| Sub-QCIF | 128 | 96 | 64 | 48 |
| QCIF | 176 | 144 | 88 | 72 |
| CIF | 352 | 288 | 176 | 144 |
| 4CIF | 704 | 576 | 352 | 288 |
| 16CIF | 1408 | 1152 | 704 | 576 |

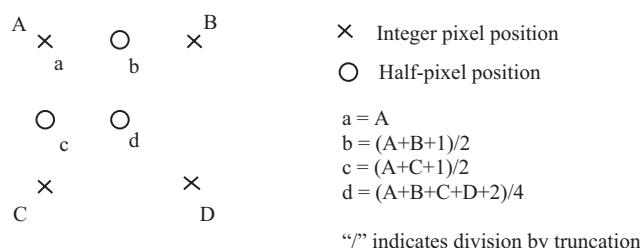
20.3.2 Technical Features of H.263

The H.263 encoder structure is similar to the H.261 encoder with the exception that there is no loop filter in H.263 encoder. The main components of the encoder include block transform, motion-compensated prediction, block quantization, and VLC. Each picture is partitioned into GOBs. A GOB contains multiple number of 16 lines, $k * 16$ lines, depending on the picture format ($k = 1$ for sub-QCIF, QCIF; $k = 2$ for 4CIF; $k = 4$ for 16CIF). Each GOB is divided into MBs that are the same as in H.261, each MB consists of four 8×8 luminance blocks and two 8×8 chrominance blocks. Compared to H.261, H.263 has several new technical features for the enhancement of coding efficiency for very-low-bit-rate applications. These new features include picture-extrapolating motion vectors (or unrestricted-motion vector mode), motion compensation with half-pixel accuracy, advanced prediction (which includes variable-block size motion compensation and overlapped block-motion compensation), syntax-based arithmetic coding, and PB-frame mode.

20.3.2.1 Half-Pixel Accuracy

In H.263 video coding, the half-pixel accuracy motion compensation is used. The half pixel values are found using bilinear interpolation as shown in [Figure 20.3](#).

Note that H.263 uses sub-pixel accuracy for motion compensation instead of using a loop filter to smooth the anchor frames as in H.261. This is also done in other coding standards such as MPEG-1 and MPEG-2, which also use half-pixel accuracy for motion compensation. In MPEG-4 video, quarter-pixel accuracy for motion compensation has been adopted as a tool for the version 2.

**FIGURE 20.3**

Half-pixel prediction by bilinear interpolation.

20.3.2.2 Unrestricted-Motion Vector Mode

Usually, the motion vectors are limited within the coded picture area of anchor frames. In the unrestricted-motion vector mode, the motion vectors are allowed to point outside the pictures. When the values of motion vectors exceed the boundary of anchor frame in the unrestricted-motion vector mode, the picture-extrapolating method is used. The values of reference pixels outside the picture boundary will take the values of boundary pixels. The extension of motion vector range is also applied to the unrestricted-motion vector mode. In the default prediction mode, the motion vectors are restricted to the range of $[-16, 15.5]$. In the unrestricted mode, the maximum range for motion vectors is extended to $[-31.5, 31.5]$ under certain conditions.

20.3.2.3 Advanced-Prediction Mode

Generally, the decoder will accept no more than one motion vector per MB for baseline algorithm of H.263 video coding standard. However, in the advanced-prediction mode, the syntax allows up to four motion vectors to be used per MB. The decision of using one or four vectors is indicated by the MB type and CBP for chrominance (MCBPC) codeword for each MB. How to make this decision is the task of the encoding process.

The following example gives the steps of motion estimation and coding mode selection for advanced-prediction mode in the encoder.

Step 1: Integer pixel motion estimation

$$SAD_N(x, y) = \sum_{t=0}^{N-1} \sum_{j=0}^{N-1} |original - previous| \quad (20.1)$$

where SAD is the sum of absolute difference, values of (x, y) is within the search range, N is equal to 16 for 16×16 blocks, and N is equal to 8 for 8×8 block.

$$SAD4 \times 8 = \sum SAD8(x, y) \quad (20.2)$$

$$SAD_{inter} = \min(SAD16(x, y), SAD4 \times 8) \quad (20.3)$$

Step 2: Intra/Inter Mode Decision

If $A < (SAD_{inter} - 500)$, this MB is coded as Intra-MB
otherwise, it is coded as Inter-MB

where SAD_{inter} is determined in step 1, and

$$A = \sum_{i=0}^{15} \sum_{j=0}^{15} |original - MB_{mean}| \quad (20.4)$$

$$MB_{mean} = \frac{1}{256} \sum_{i=0}^{15} \sum_{j=0}^{15} original$$

If this MB is determined to be coded as Inter-MB, go to step 3

Step 3: Half-pixel search

In this step, half-pixel search is performed for both 16×16 block and 8×8 blocks as shown in [Figure 20.3](#).

Step 4: Decision on 16×16 or four 8×8 (one motion vector or four motion vectors per MB)

If $SAD4 \times 8 < SAD16 - 100$, four motion vectors per MB will be used, one of which is used for all pixels in one of the four luminance blocks in the MB; otherwise, one motion vector will be used for all pixels in the MB.

Step 5: Differential coding of motion vectors for each 8×8 luminance block is performed as in [Figure 20.4](#).

$$MVDx = MVx - Px$$

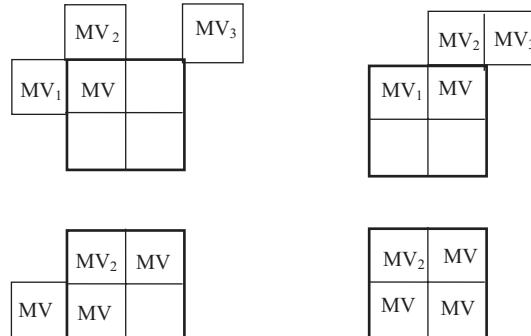
$$MVDy = MVy - Py$$

$$Px = \text{Median}(MV1x, MV2x, MV3x)$$

$$Py = \text{Median}(MV1y, MV2y, MV3y)$$

$$Px = Py = 0, \text{ if MB is Intra coded or block is outside of picture boundary}$$

When it has been decided to use four motion vectors, the MVD_{CHR} motion vector for both chrominance blocks is derived by calculating the sum of the four luminance vectors and dividing by 8. The component values of the resulting sixteenth-pixel resolution vectors are modified towards the position as indicated in the [Table 20.4](#).



$$MVD_x = MV_x - Px$$

$$MVD_y = MV_y - Py$$

$$Px = \text{Median}(MV_{1x}, MV_{2x}, MV_{3x})$$

$$Py = \text{Median}(MV_{1y}, MV_{2y}, MV_{3y})$$

$$Px = Py = 0, \text{ if MB is Intra coded or block is outside of picture boundary}$$

FIGURE 20.4

Differential coding of motion vectors.

TABLE 20.4

Modification of Sixteenth-Pixel Resolution Chrominance Vector Components

| Sixteenth-pixel position | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | /16 |
|--------------------------|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|-----|
| Resulting position | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | /2 | |

Another advanced-prediction mode is overlapped motion compensation for luminance. Actually, this idea is also used by MPEG-4, which has been described in [Chapter 19](#). In the overlapped motion-compensation mode, each pixel in an 8×8 luminance block is a weighted sum of three values divided by 8 with rounding. The three values are obtained by the motion compensation with three motion vectors: the motion vector of the current luminance block and two of four “remote” vectors. These remote vectors include the motion vector of the block to the left or right of the current block and the motion vector of the block above or below the current block. The remote motion vectors from other GOBs are used in the same way as remote motion vectors inside the current GOB. For each pixel to be coded in the current block, the remote motion vectors of the blocks at the two nearest block borders are used, i.e., for the upper half of the block the motion vector corresponding to the block above the current block is used while for the lower half of the block the motion vector corresponding to the block below the current block is used. Similarly, the left half of the block uses the motion vector of the block at the left side of the current block and the right half uses the one at the right side of the current block. To make this more clear, let (MV_x^0, MV_y^0) be the motion vector for the current block, (MV_x^1, MV_y^1) be the motion vector for the block either above or below, and (MV_x^2, MV_y^2) be the motion vector of the block either to the left or right of the current block. Then the value of each pixel, $p(x, y)$ in the current 8×8 luminance block is given by:

$$p(x, y) = (q(x, y) \cdot H_0 + r(x, y) \cdot H_1 + s(x, y) \cdot H_2(x, y) + 4) / 8 \quad (20.5)$$

where

$$\begin{aligned} q(x, y) &= p(x + MV_x^0, y + MV_y^0), \quad r(x, y) = p(x + MV_x^1, y + MV_y^1), \text{ and} \\ s(x, y) &= p(x + MV_x^2, y + MV_y^2), \end{aligned} \quad (20.6)$$

H_0 is the weighting matrix for prediction with the current block-motion vector, H_1 is the weighting matrix for prediction with the top or bottom block-motion vector, and H_2 is the weighting matrix for prediction with the left or right block-motion vector. This applies to the luminance block only. The values of H_0 , H_1 and H_2 are shown in [Figure 20.5](#).

$$H_0 \ H_1 \ H_2$$

It should be noted that the above coding scheme is not optimized in the selection of mode decision since the decision depends only on the values of predictive residues. Optimized mode decision techniques that include the above possibilities for prediction have been considered in Weigand (1996).

20.3.2.4 Syntax-Based Arithmetic Coding

As in other video coding standards, H.263 uses variable length coding and decoding (VLC/VLD) to remove the redundancy in the video data. The basic principle of VLC is to encode a symbol with a specific table based on the syntax of the coder. The symbol is mapped to an entry of the table in a table look-up operation, then the binary codeword specified by the entry is sent to a bitstream buffer for transmitting to the decoder. In the decoder, an inverse operation, VLD, is performed to reconstruct the symbol by the table look-up operation based on the same syntax of the coder. The tables in the decoder must be the same as

| H_0 | | | | | | | | H_1 | | | | | | | | H_2 | | | | | | | | |
|-------|---|---|---|---|---|---|---|-------|---|---|---|---|---|---|---|-------|---|---|---|---|---|---|---|---|
| 4 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 4 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 |
| 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 1 | 1 | 2 | 2 | 2 | 2 | 1 | 1 | 2 | 2 | 1 | 1 | 1 | 1 | 2 | 2 |
| 5 | 5 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 1 | 1 | 1 | 1 | 2 | 2 |
| 5 | 5 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 1 | 1 | 1 | 1 | 2 | 2 |
| 5 | 5 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 1 | 1 | 1 | 1 | 2 | 2 |
| 5 | 5 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 1 | 1 | 1 | 1 | 2 | 2 |
| 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 1 | 1 | 2 | 2 | 2 | 2 | 1 | 1 | 2 | 2 | 1 | 1 | 1 | 1 | 2 | 2 |
| 4 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 4 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 |

FIGURE 20.5

Weighting matrices for overlapped motion compensation.

the one used in the encoder for encoding the current symbol. In order to obtain the better performance, the tables are generated in a statistically optimized way (such as a Huffman coder) with a large number of training sequences. This VLC/VLD process implies that each symbol must be encoded into a fixed integral number of bits. An optional feature of H.263 is to use arithmetic coding to remove the restriction of fixed integral number bits for symbols. This syntax-based arithmetic coding mode may result in bit rate reductions.

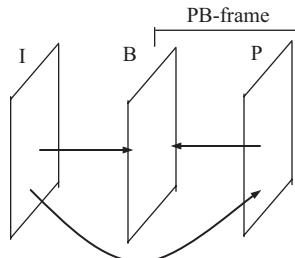
20.3.2.5 PB-frames

The PB-frame is a new feature of H.263 video coding. A PB-frame consists of two pictures, one P-picture and one B-picture, being coded as one unit as shown in [Figure 20.6](#). Since H.261 does not have B-pictures, the concept of a B-picture comes from the MPEG video coding standards. In a PB-frame, the P-picture is predicted from the previous decoded I- or P-picture and the B-picture is bi-directionally predicted both from the previous decoded I- or P-picture and the P-picture in the PB-frame unit, which is currently being decoded.

Several detailed issues have to be addressed at MB level in PB-frame mode:

If a MB in PB-frame is intra-coded, the P-MB in the PB unit is intra-coded and the B-MB in the PB unit is inter-coded. The motion vector of inter-coded PB-MB is used for the B-MB only.

A MB in PB-frame contains 12 blocks for 4:2:0 format, six (four luminance blocks and two chrominance blocks) from P-frame and six from B-frame. The data for six P-blocks is transmitted first and then the data for six B-blocks is transmitted.

**FIGURE 20.6**

Prediction in PB-frames mode.

Different parts of a B-block in a PB-frame can be predicted with different modes. For pixels where the backward vector points inside of coded P-MB, bi-directional prediction is used. For all other pixels, forward prediction is used.

20.4 H.263 Video Coding Standard Version 2

20.4.1 Overview of H.263 Version 2

The H.263 version 2 (ITU-T Recommendation H.263 1998) video coding standard, also known as H.263+, was approved in January of 1998 by the ITU-T. H.263 version 2 includes a number of new optional features based on the H.263 video coding standard. These new optional features are added in order to broaden the application range of H.263 and to improve its coding efficiency. The main features are flexible video format, scalability, and backward-compatible supplemental enhancement information. Among these new optional features, five of them are intended to improve the coding efficiency and three of them are proposed to address the needs of mobile video and other noisy transmission environments. The features of scalability provide the capability of generating layered bitstream that are spatially, temporally, and SNR-scalable, similar to those defined by the MPEG-2 video coding standard. There are also other modes of H.263 version 2 that provide some enhancement functions. We will describe these features in the following section.

20.4.2 New Features of H.263 Version 2

The H.263 version 2 includes a number of new features. In the following, we briefly describe the key techniques used for these features.

20.4.2.1 Scalability

The scalability function allows for encoding the video sequences in a hierarchical way that partitions the pictures into one basic layer and one or more enhancement layers. The decoders have the option to decode only the base layer bitstream to obtain lower quality reconstructed pictures or further decode the enhancement layers to obtain the higher quality decoded pictures. There are three types of scalability in H.263: temporal scalability, SNR scalability, and spatial scalability.

Temporal scalability is achieved by using B-pictures as the enhancement layer. All three types of scalability are similar to the ones in MPEG-2 video coding standard. The B-pictures are predicted from either or both a previous and subsequent decoded picture in the base layer ([Figure 20.7](#)).

In the SNR scalability, the pictures are first encoded with coarse quantization in the base layer. The differences or coding error pictures between a reconstructed picture and its original in the base layer encoder are then encoded in the enhancement layer and sent to the decoder providing an enhancement of signal-to-noise ratio. In the enhancement layer there are two types of pictures. If a picture in the enhancement layer is only predicted from the base layer, it is referred to as an EI picture. It is a bi-directionally predicted picture if it uses both a prior enhancement layer picture and a temporally simultaneous base layer reference picture for prediction. Note that the prediction from the reference layer

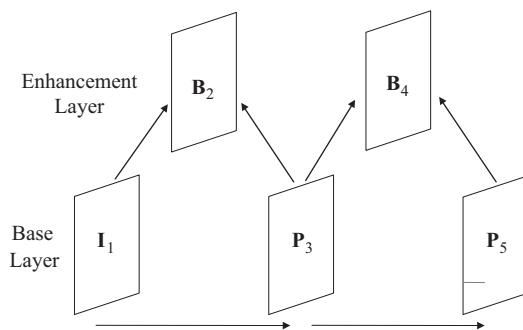


FIGURE 20.7
Temporal scalability.

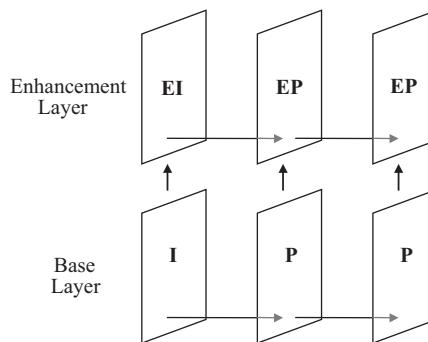


FIGURE 20.8
SNR scalability.

uses no motion vectors. However, EP (enhancement P-) pictures use motion vectors when predicted from their temporally prior reference picture in the same layer. Also, if more than two layers are used, the reference may be the lower layer instead of the base layer ([Figure 20.8](#)).

In the spatial scalability, lower-resolution pictures are encoded in the base layer or lower layer. The differences or error pictures between upsampled decoded base layer pictures and its original picture are encoded in the enhancement layer and sent to the decoder providing the spatial enhancement pictures. As in MPEG-2, spatial interpolation filters are used for the spatial scalability. There are also two types of pictures in the enhancement layer: EI and EP. If a decoder is able to perform spatial scalability, it may also need to be able to use a custom picture format. For example, if the base layer is sub-QCIF (128×96), the enhancement layer picture would be 256×192 , which does not belong to a standard picture format ([Figure 20.9](#)).

The scalability in H.263 can be performed with multi-layers. In the case of multi-layer scalability, the picture layer used for upward prediction in an EI or EP picture may be an I, P, EI, or EP picture, or may be the P part of a PB or improved PB frame in the base layer, as shown in [Figure 20.10](#).

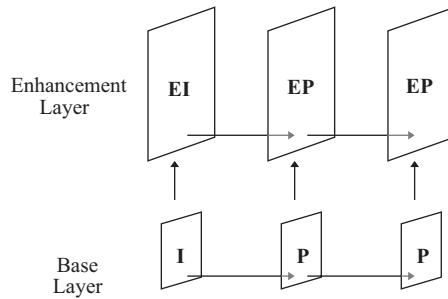


FIGURE 20.9
Spatial scalability.

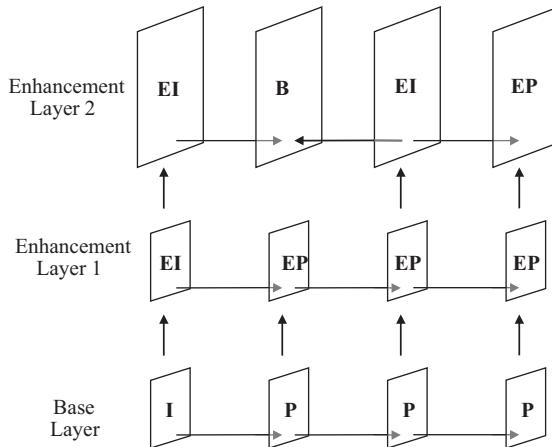


FIGURE 20.10
Multi-layer scalability.

20.4.2.2 Improved PB-frames

The difference between the PB-frame and the improved PB-frame is that bi-directional prediction is used for B MBs in the PB-frame, while in the improved PB-frame, B MBs can be coded in three prediction modes: bi-directional prediction, forward prediction, and backward prediction. This means that in forward prediction or backward prediction only one motion vector is used for a 16×16 MB instead of using two motion vectors for a 16×16 MB in bi-directional prediction. In very-low-bit-rate case, this mode can improve the coding efficiency by saving bits for coding motion vectors.

20.4.2.3 Advanced Intra Coding

The advantage of intra coding is to protect the error propagation since intra coding does not depend on the previous decoded picture data. However, the problem of intra coding is that more bits are needed since the temporal correlation between frames is not exploited. The idea of advanced intra coding (AIC) is used to address this problem. The coding efficiency of intra coding is improved by the use of the following three methods:

1. Intra-block prediction using neighboring intra blocks for the same color component (Y , C_b or C_r): a particular intra-coded block may be predicted from the block above or left to the current block being decoded, or from both. The main purpose of these predictions tries to use the correlation between neighboring blocks. For example, the first row of AC coefficients may be predicted from those in the block above, the first column of AC coefficients may be predicted from those in the left, and the DC value may be predicted as an average from the block above and left.
2. Modified IQ for intra coefficients: IQ of the intra DC coefficient is modified to allow a varying quantization step size. IQ of all intra AC coefficients is performed without a “dead-zone” in the quantizer reconstruction spacing.
3. A separate VLC for intra coefficients: in order to improve intra coding a separate VLC table is used for all intra DC and intra AC coefficients. The price paid for this modification is the use of more tables.

20.4.2.4 Deblocking Filter

The deblocking filter (DBF) is used to further improve the decoded picture quality by smoothing the block artifacts. Its function on improving picture quality is similar to the overlapped block motion compensation. The filter operations are performed across 8×8 block edges using a set of four pixels on both horizontal and vertical directions at the block boundaries such as shown in [Figure 20.11](#). In the figure, the filtering process is applied to the edges. The edge pixels, A , B , C , and D , are replaced by A_1 , B_1 , C_1 , and D_1 by the following operations:

$$B_1 = \text{clip}(B + d_1) \quad (20.7)$$

$$C_1 = \text{clip}(C - d_1) \quad (20.8)$$

$$A_1 = A - d_2 \quad (20.9)$$

$$D_1 = D + d_2 \quad (20.10)$$

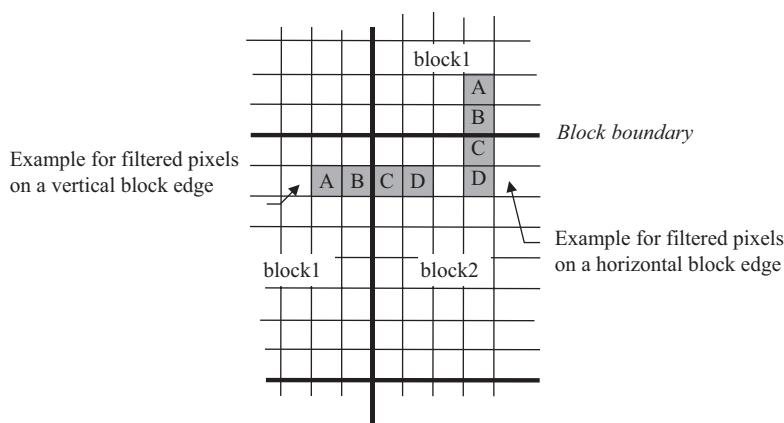


FIGURE 20.11
Positions of filtered pixels.

$$d = (A - 4B + 4C - D)/8 \quad (20.11)$$

$$d_1 = f(d, S) \quad (20.12)$$

$$d_2 = \text{clip } d_1 ((A - D)/4, d_1/2) \quad (20.13)$$

where clip is a function of clipping the value to the range of 0 to 255, clip $d(x, d)$ is a function that clips x to the range of from $-d$ to $+d$, and the value S is a function of quantization step QUANT that is defined in [Table 20.5](#).

The function $f(d, S)$ is defined as

$$f(d, S) = \text{SIGN}(d) * (\text{MAX}(0, \text{abs}(d)) - \text{MAX}(0, 2^* \text{abs}(d) - S))) \quad (20.14)$$

This function can be described by [Figure 20.12](#). From the figure, it can be seen that this function is used to control the amount of distortion introducing by filtering. The filter has an effect only if d is smaller than $2S$. Therefore, some features such as an isolated pixel, corner, etc. would be reserved during the nonlinear filtering since for those features the value d may exceed the $2S$. The function $f(d, S)$ is also designed to ensure that a small mismatch between encoder and decoder will remain small and will not allow the mismatch to be propagated over multiple pictures. For example, if the filter is simply switched on or off with a mismatch of only $+1$ or -1 for d , then this will cause the filter to be switched on at the encoder and off at the decoder, or vice versa. It should be noted that the DBF proposed here is an optional selection. It is a result of a large number of simulations; it may be effective for some sequences but may be not effective for all kinds of video sequences.

20.4.2.5 Slice-Structured Mode

A slice contains a video picture segment. In the coding syntax, a slice is defined as a slice header followed by consecutive MBs in scanning order. The slice-structured (SS) mode is

TABLE 20.5

The Value S as a Function of Quantization Step (QUANT)

| QUANT | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
|-------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| S | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 4 | 5 | 5 | 6 | 6 | 7 | 7 | 7 |
| QUANT | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | |
| S | 8 | 8 | 8 | 9 | 9 | 9 | 10 | 10 | 10 | 11 | 11 | 11 | 12 | 12 | 12 | 12 |

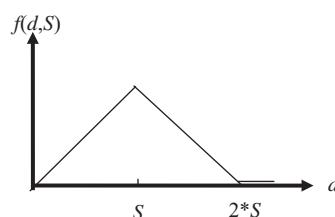


FIGURE 20.12

The plot of function of $f(d, S)$.

designed to address the needs of mobile video and other unreliable transmission environments. This mode contains two submodes: the rectangular slice (RS) submode and the arbitrary slice ordering (ASO) submode. In the RS submode, a slice contains a rectangular region of a picture, such that the slice header specifies the width. The MBs in this slice are in scan order within the rectangular region. In the ASO submode, the slices may appear in any order within the bitstream. The arbitrary arrangement of slices in the picture may provide an environment for obtaining better error concealment. The reason is that the damaged area caused by packet loss may be isolated from each other and can be easily concealed by the good decoded neighboring blocks. In this submode, there is usually no data dependency that can cross the slice boundaries, except for the DBF mode since the slices may not be decoded in the normal scan order.

20.4.2.6 Reference Picture Selection

With optional mode of the reference picture selection (RPS), the encoder is allowed to use a modified interframe prediction method. In this method, additional picture memories are used. The encoder may select one of the picture memories to suppress the temporal error propagation due to the interframe coding. The information to indicate which picture is selected for prediction is included in the encoded bitstream that is allowed by syntax. The strategy used by the encoder to select the picture to be used for prediction is open for algorithm design. This mode can use the backward channel message that is sent from a decoder to an encoder to inform the encoder which part of which pictures have been correctly decoded. The encoder can use the message from the backward channel to decide which picture will provide better prediction. From the above description of RPS mode, it becomes evident that this mode is useful for improving the performance over unreliable channels.

20.4.2.7 Independent Segmentation Decoding

The independent segmentation decoding (ISD) mode is another option of H.263 video coding that can be used for unreliable transmission environment. In this mode, each video picture segment is decoded without the presence of any data dependencies across slice boundaries or across GOB boundaries, i.e., with complete independence from all other video picture segments and all data outside the same video picture segment location in the reference pictures. This independence includes no use of motion vectors outside of the current video picture segment for motion prediction or remote motion vectors for overlapped motion compensation in the advanced-prediction mode, no DBF operation, and no linear interpolation across the boundaries of the current video picture segment.

20.4.2.8 Reference Picture Resampling

The reference picture resampling (RPR) mode allows a prior coded picture to be resampled, or wrapped, before it is used as a reference picture. The idea of using this mode is similar to the idea of global motion, which is expected to obtain better performance of motion estimation and compensation. The wrapping is defined by four motion vectors for the corners of the reference picture as shown in [Figure 20.13](#).

For the current picture with horizontal size H and vertical size V , four conceptual motion vectors, MV_{OO} , MV_{OV} , MV_{HO} and MV_{HV} are defined for the upper left, low left, upper right and low right corners of the picture, respectively. These motion vectors as

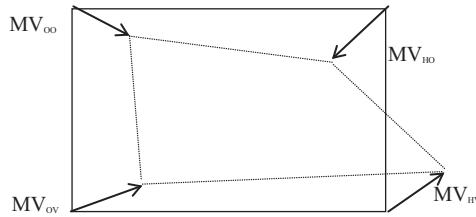


FIGURE 20.13
RPR.

wrapping parameters have to be coded with VLC and included in the bitstream. These vectors are used to describe how to move the corners of the current picture to map them onto the corresponding corners of the previous decoded pictures as shown in [Figure 20.13](#). The motion compensation is performed using bi-linear interpolation in the decoder with the wrapping parameters.

20.4.2.9 Reduced-Resolution Update

When encoding a video sequence with highly active scenes, the encoder may have a problem to provide sufficient subjective picture quality at low-bit-rate coding. The reduced-resolution update (RRU) mode is expected to be used in this case for improving the coding performance. This mode allows the encoder to send update information for a picture that is encoded at a reduced resolution to create a final image at the higher resolution. At the encoder, the pictures in the sequence are first down-sampled to a quarter size (half in both horizontal and vertical directions) and then the resulting low-resolution pictures are encoded as shown in [Figure 20.14](#).

The decoder with this mode is more complicated than one without this mode. The block diagram of decoding process with the RRU mode is shown in [Figure 20.15](#).

The decoder with RRU mode has to deal with several new issues. First, the reconstructed pictures are upsampled to the full size for display. However, the reference pictures have to be extended to the integer times of 32 by 32 MBs if it is necessary. The pixel values in the extended areas take the values of original border pixels. Second, the motion vectors for 16×16 MBs in the encoder are used for the upsampled 32×32 MB in the decoder.

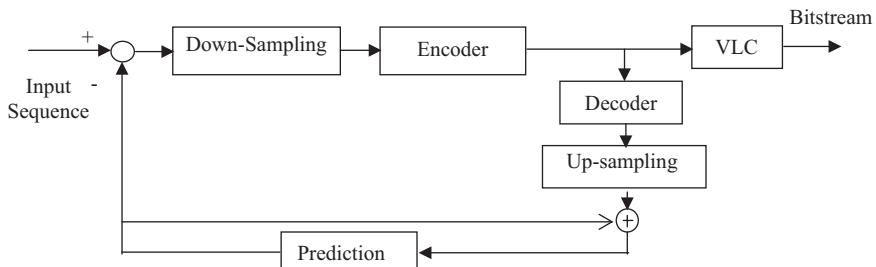


FIGURE 20.14
Block diagram of encoder with RRU mode.

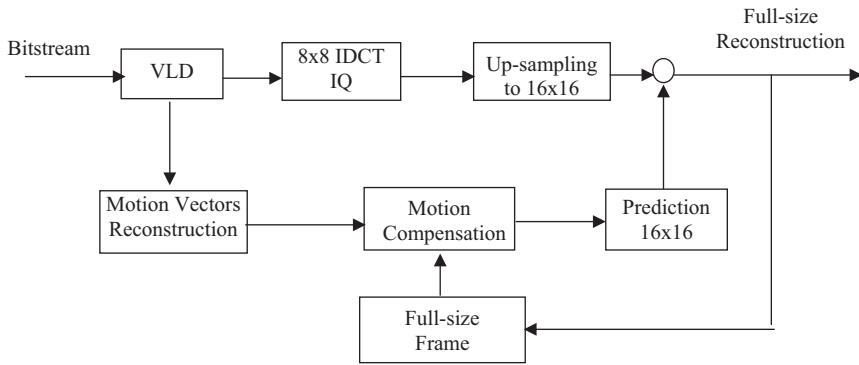


FIGURE 20.15
Block diagram of decoder with RRU mode.

Therefore, an additional procedure is needed to reconstruct the motion vectors for each upsampled 16×16 MBs including chrominance MBs. Third, bi-linear interpolation is used for upsampling in the decoder loop. Finally, in the boundary of reconstructed picture, a block boundary filter is used along the edges of the 16×16 reconstructed blocks at the encoder as well as on the decoder. There are two kinds of block boundary filters that have been proposed. One is the previously described DBF. The other one is defined as follows. If two pixels, A and B , are neighboring pixels and A is in block 1 and B is in block 2, respectively, then the filter is designed as:

$$A_1 = (3 * A + B + 2)/4 \quad (20.15)$$

$$B_1 = (A + 3 * B + 2)/2 \quad (20.16)$$

Where A_1 and B_1 are the pixels after filtering and “/” is division with truncation.

20.4.2.10 Alternative INTER VLC (AIV) and Modified Quantization

The alternative inter VLC mode is developed for improving coding efficiency of inter-picture coding for the pictures containing significant scene changes. This efficiency improvement is obtained by allowing some VLC codes originally designed for intra-picture to be used for inter-picture coefficients. The idea is very intuitive and simple. When the rapid scene change occurs in the video sequence, the inter-picture prediction becomes difficult. This results in large prediction differences, which are similar to the intra-picture data. Therefore, the use of intra-picture VLC tables instead of using inter-picture tables may obtain better results. However, there is no syntax definition for this mode. In other words, the encoder may use the intra VLC table for encoding an inter block without informing the decoder. After receiving all coefficient codes of a block, the decoder will first decode these codewords with the inter VLC tables. If the addressing of coefficients stays inside the 64 coefficients of a block, the variable-length decoding will accept the results even if some coding mismatch exists. Only if coefficients outside the block are addressed, the codewords will be interpreted according to the intra VLC table. The modified quantization mode is designed for providing several features that can improve the coding efficiency. First, with this mode, more flexible control of the

quantizer steps can be specified in the dequantization field. The dequantization field is no longer a two-bit fixed length field, it is a variable length field that can either be two bits or six bits depending on the first bit. Secondly, in this mode, the quantization parameter of the chrominance coefficients is different from the quantization parameter of the luminance coefficients. The chrominance fidelity can be improved by specifying a smaller quantization step for chrominance than that for luminance. Finally, this mode allows the extension of the range of coefficient values. This provides more accurate representation of any possible true coefficient value with the accuracy allowed by the quantization step. However, the range of quantized coefficient levels is restricted to those that can reasonably occur, to improve the detectability of errors and minimize decoding complexity.

20.4.2.11 Supplemental Enhancement Information

The usage of supplemental information may be included in the bitstream in the picture layer to signal enhanced display capabilities or to provide tagging information for external usage. This supplemental enhancement information includes full-picture freeze/freeze-release request, partial-picture freeze/freeze-release request, resizing partial-picture freeze request, full-picture snapshot tag, partial-picture snapshot tag, video time segment start/end tag, progressive refinement segment start/end tag, and chroma key information. The full-picture freeze request is used to indicate that the contents of the entire prior displayed video picture will be kept and not updated by the contents in current decoded picture. The picture freeze will be kept under this request until the full-picture freeze-release request occurs in the current or subsequent PTYPE information. The partial-picture freeze request indicates that the contents of a specified rectangular area of the prior displayed video picture are frozen until the release request is received or timeout occurs. The resizing partial-picture freeze request is used to change the specified rectangular area for the partial picture. One use of this information is to keep the contents of the picture in the corner of display unchanged for a time period for commercial use or some other purpose. All information given by the tags indicates that the current picture is labeled as either a still-image snapshot or a sub-sequence of video data for external usage. The progressive refinement segment tag is used to indicate the display period of the pictures with better quality. The chroma keying information is used to request “transparent” and “semi-transparent” pixels in the decoded video pictures (Chen et al. 1997). One application of the chroma key is to simply describe the shape information of objects in a video sequence.

20.5 H.263++ Video Coding and H.26L

H.263++ is the next version of H.263 that is considering adding more optional enhancements to H.263. It is the extension of H.263 version 2 and is currently scheduled to be completed late in the year 2000. H.26L is a project to seek more efficient video-coding algorithms that will be much better than the current H.261 and H.263 standards, where the L stands for long term. The algorithms for H.26L can be fundamentally different from the current DCT with motion-compensation framework that is used for H.261, H.262 (MPEG-2), and H.263. The expected improvements from the current standards include

several aspects: higher coding efficiency, more functionality, low-complexity permitting software implementation, and enhanced error robustness. H.26L addresses very-low-bit-rate, real-time, low end-to-end delay applications. The potential application targets can be Internet video phones, sign language or lip-reading communications, video storage and retrieval service, multi-point communication, and other visual communication systems. H.263L is currently scheduled for approval in the year 2002.

20.6 Summary

In this chapter, the video coding standards for low-bit-rate applications have been introduced. These standards include H.261, H.263, H.263 version 2 and the versions under development: H.263++, and H.26L. H.261 and H.263 are extensively used for video conferencing and other multimedia applications at low bit rates. In H.263 version 2, all new negotiable coding options are developed for special applications. Among these options, five—AIC mode, alternative inter VLC mode, modified quantization mode, de-blocking filter mode, and improved PB-frame mode—are intended to improve coding efficiency. Three modes—SS mode, RPS mode, and independent segment decoding mode—are used to meet the need of mobile video application. The others provide the functionality of scalability such as spatial, temporal, and SNR scalability. H.26L is a future standard to meet the requirements of very-low-bit-rate, real-time, low end-to-end delay, and other advanced performance.

Exercises

- 20.1 What is the enhancement of H.263 over H.261? Describe the applications of each enhanced tool of H.263.
 - 20.2 Compared to MPEG-1 and MPEG-2, which features of H.261 and H.263 are used to improve coding performance at low bit rates? Explain the reasons.
 - 20.3 What is the difference between spatial scalability and reduced-resolution update mode in H.263 video coding?
 - 20.4 Conduct a project to compare the results by using the DFs in the coding loop and out of the coding loop. Which method will cause less drift if a large number of pictures are contained between two consecutive I-pictures?
-

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21

Video Coding Standard—H.264/AVC

Many video coding standards have been developed during past two decades. In this chapter, we are going to introduce a recently developed video coding standard, H.264 or MPEG-4 Part 10 Advanced Video Coding (AVC) [h264], which has been developed and standardized collaboratively by the Joint Video Team (JVT) of ISO/IEC MPEG and ITU-T VCEG. The main objective of H.264 is for high coding efficiency. The test results have shown that it has made an important milestone of video coding standard at the coding efficiency improvement.

21.1 Introduction

Several video coding standards have been introduced in the previous chapters including MPEG-1/2/4 and H.261 as well as H.263. Recently, the JVT of ISO/IEC MPEG and ITU-T Video Coding Expert Group (VCEG) has developed a new video coding standard, which is referred to formally as (ITU-T Recommendation H.264 2005) and ISO/IEC MPEG-4 (Part 10) Advanced Video Coding. It is referred to in short as H.264/AVC. The work of H.264/AVC actually started in early 1998 when the VCEG issued a call for proposals for a project called H.26L. The target of H.26L is to greatly improve the coding efficiency over any existing video coding standards. The first draft of H.26L was completed in October 1999. The JVT was formed in December 2001, with the mission to finalize the new coding standard based on H.26L. The draft of new video coding standard was submitted for formal approval as the final committee draft (FCD) in March 2003 and promoted to final draft international standard (FDIS) in June 2003. The current MPEG-4 AVC standard itself is ISO/IEC 14496-10:2004. The FRext enhancements have also received final approval as ISO/IEC 14496-10:2004/AMD 1.

The H.264/AVC mainly targets for high coding efficiency. Based on the conventional block-based motion-compensated hybrid video coding concepts H.264/AVC provides approximately a 50% bitrate savings from equivalent perceptual quality relative to the performance of prior standards. This has been shown from extensive simulation results. The superior coding performance of H.264/AVC is obtained because many new features are incorporated such as enhanced prediction capability and smaller block size motion compensation. The details of these features will be described in the following sections. With high coding efficiency, the H.264/AVC can provide technical solutions for many applications including broadcasting over different media, video storage on optical and magnetic devices, high-definition DVD, and others. However, it will not be that easy to replace the current existing standard such as MPEG-2 with H.264/AVC in some applications such as in the area of the digital televisions. However, it may be used for new application areas,

such as high-definition DVD, mobile video transmission, and others. From the other side, to achieve the high coding efficiency H.264/AVC has to use a lot of new tools or modified tools from existing standards that substantially increases the complexity of the codec; it would be about four times higher for the decoder and nine times higher for the encoder compared with the MPEG-2 video coding standard. However, with fast advances of semiconductor technique, the silicon solution can alleviate the problem of high complexity.

21.2 Overview of the H.264/AVC Codec Structure

To address the variety of applications and networks, the H.264/AVC codec design consists of two layers: video coding layer (VCL) and network abstraction layer (NAL). The layered structure of the H.264/AVC video encoder is shown in [Figure 21.1](#).

From [Figure 21.1](#), the input of video source is first compressed in the VCL into a bit-stream. The function of the VCL is to efficiently compress the video content. The network abstract layer (NAL) is a new concept, which is designed for efficient transmission of the compressed bitstream in different network or storage environments. These include all current and future protocols and network architectures. These applications include broadcasting over terrestrial, cable and satellite networks; streaming over IP-networks, wireless and ISDN channels. In this layer, the head information is added to the coded bitstream for handling a variety of transport layers or storage media. The interface of NAL is designed to enable a seamless integration of the coded video data with all possible protocols and network architectures.

The bitstream can be in one of two formats: the NAL unit stream or the byte stream. The NAL unit stream format consists of a sequence of syntax structures called NAL units. The format of an NAL unit is shown in [Figure 21.2](#).

In the header of a NAL unit (NALU), the first bit is a 0 bit, and the next 2 bits are used to indicate whether the NALU contains the sequence or picture parameter set or a slice of a reference picture. The next 5 bits are used to indicate type of NALU units, which corresponds to the type of data being carried in that NALU unit. There is a total 32 types of NAL units allowed. The 32 types of NAL units can be classified in two categories: VCL NAL units and non-VCL NAL units. The VCL units carry the data corresponding to the

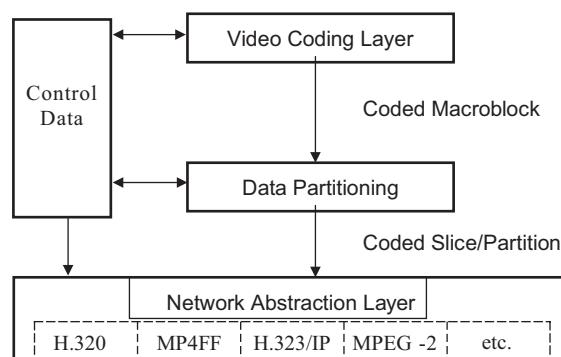


FIGURE 21.1

Layered structure of the H.264/AVC video encoder.

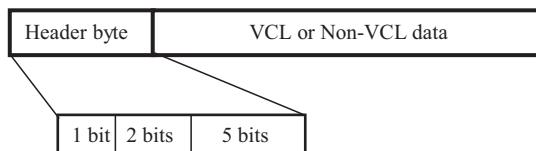


FIGURE 21.2
NAL unit format.

VCL, while the non-VCL NAL units carry information like supplemental enhancement information (SEI), sequence and picture parameter set, access unit delimiter, and others. The detail can be found in the specification of H.264/AVC [h264].

In the NAL unit stream the NAL units are decoded on the decoding order. The byte stream can be constructed from the NAL unit stream by ordering the NAL units in decoding order and adding a start code to each NAL unit and zero or more zero-valued bytes to form a stream of bytes. The NAL unit stream can be extracted from the byte stream by removing the start code that has the unique start code prefix pattern within this byte stream. The NAL unit is a syntax structure containing an indication of the type of data to follow and bytes containing that data in the form of a raw byte sequence payload (RBSP) interspersed as necessary with emulation prevention bytes. The emulation prevention byte is a byte equal to 0×03 that may be present within a NAL unit. The presence of emulation prevention bytes ensures that no sequence of consecutive byte-aligned bytes in the NAL unit contains a start code prefix, which is a unique sequence of three bytes equal to 0×000001 embedded in the byte stream as a prefix to each NAL unit. The location of a start code prefix can be used by a decoder to identify the beginning of a new NAL unit and the end of a previous NAL unit. Emulation of start code prefixes is prevented within NAL units by the inclusion of emulation prevention bytes. An NAL unit specifies a generic format for use in both packet-oriented and bitstream systems. The format of NAL units for both packet-oriented transport and bitstream delivery is identical except that each NAL unit can be preceded by a start code prefix in a bitstream-oriented transport.

Compared to other existing video coding standards, the basic coding structure of H.264/AVC is similar, which is the structure with the motion-compensated transform coding. The block diagram of the H.264/AVC video encoder is shown as in [Figure 21.3](#).

In addition to many common tools, the H.264/AVC includes many highlighted features that are enable to greatly improve the coding efficiency and increase the capability of error robustness and the flexibility for operation over a variety of network environments. Features for improving coding efficiency can be divided into two parts: the first is to improve the accuracy of prediction for the picture to be encoded and the second includes the method of transform and entropy coding. Several tools have been adopted in H.264/AVC to improve inter and intra prediction, which are briefly summarized as follows.

Variable block size for motion compensation with small block sizes is used, in which a total of seven selections of block sizes are used for motion compensation in H.264/AVC; among those, the smallest block size for luma motion compensation can be as small as 4×4 .

The quarter-pel accurate motion compensation is adopted in H.264/AVC. The quarter-pel accurate motion compensation has been used in the advanced profile of MPEG-4 Part 2, but H.264/AVC further reduces the complexity of the interpolation process.

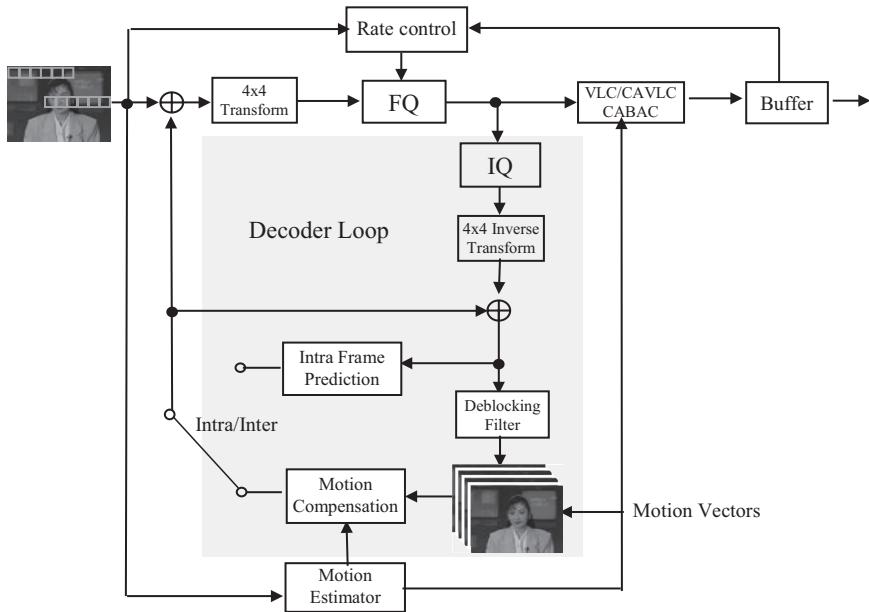


FIGURE 21.3
Block diagram of the H.264 encoder.

Multiple reference pictures for motion compensation and weighted prediction are used to predict the P-pictures and B-pictures. The number of reference pictures can be up to 15 for level 3.0 or lower and four for levels higher than 3.0. When the multiple reference pictures are used for motion-compensation prediction, the contribution of prediction from different references should be weighted and offset by amounts specified by the encoder. This can greatly improve coding efficiency for those scenes that contain fades.

Directional spatial prediction for intra coding is adopted for further improving coding efficiency. In this technique, the intra-coded regions are predicted with the references of the previously coded areas, which can be selected from different spatial directions. In such a way, the edges of the previously decoded areas of the current picture can be extrapolated into the current intra-coded regions.

Skip mode in P-picture and direct mode for B-picture is used to alleviate the problem for using too many bits for coding motion vectors in the inter-frame coding. H.264/AVC uses the skip mode for P-picture and direct mode for B-pictures. In these modes, the reconstructed signal is obtained directly from the reference frame with the motion vectors derived from previously encoded information by exploiting either spatial (for skip mode) or temporal (for direct mode) correlation of the motion vectors between adjacent macroblocks or pictures. In such a way, bit savings for coding motion vectors can be achieved.

The use of loop-deblocking filters is another feature that is used to reduce the block artefacts and improve both objective and subjective video quality. The difference from MPEG-1/2 is that in H.264/AVC the deblocking filter is brought within the motion-compensation loop, so that it can be used for improving the inter-frame prediction and therefore improving the coding efficiency.

H.264/AVC uses a small transform block size of 4×4 instead of 8×8 as in most video coding standards. The merit of using the small transform block size is its ability to encode

the picture in a more local adaptive fashion, which would reduce the coding artefacts such as ringing noise. However, the problem of using small transform block size may cause coding performance degradation because the correlations of large area may not be exploited for certain pictures. H.264/AVC uses two ways to alleviate this problem; one is by using a hierarchical transform to extend the effective block size of non-active chroma information to an 8×8 block, and another is by allowing the encoder to select a special coding type of intra coding that enables the extension of the length of the luma transform for non-active area to a 16×16 block size. As mentioned previously, the basic functions of integer transform used in H.264/AVC do not have equal norm. To solve this problem, quantization table size has been increased.

Two very powerful entropy coding methods, content-adaptive variable-length coding (CAVLC) and context-adaptive binary arithmetic coding (CABAC), are used in H.264/AVC for further improving coding performance.

In H.264/AVC several tools have been adopted for increasing the capability of error robustness.

Flexible slice size allows encoder to adaptively select the slice size for increasing the capability of error robustness.

Flexible macroblock ordering (FMO) allows partitioning the macroblocks into slices in a flexible order. Since each slice is an independently decodable unit, the FMO can significantly enhance error robustness by managing the spatial relationship between the macroblocks in the slice.

There are also several features that are used to increase the flexibility for operation over a variety of network environments.

The parameter set structure is used to provide a more flexible way to protect the key header information and increase the error robustness.

The NAL unit syntax structure allows for carrying video content in a manner appropriate for each specific network in a customized way.

Arbitrary slice ordering (ASO) is used to improve end-to-end delay in real-time application, particularly for the applications on the Internet protocol networks.

Switching P (SP) and switching I (SI) slices are new slice types. They are specially encoded slices that allow efficient switching between video bitstreams and efficient random access for video decoders. This feature can be used for efficiently switching a decoder to decode different bitstreams with different bit rates, recovery from errors, and trick modes.

An overview of the H.264/AVC video coding standard can be found in Wiegand et al. (2003) and the detailed specification can be found in [h264]. The technical details of the above tools will be described in the following sections.

21.3 Technical Description of H.264/AVC Coding Tools

In the previous section we briefly described the features of the H.264/AVC video coding standard. In this section we introduce the technical details of some of those important features.

21.3.1 Instantaneous Decoding Refresh Picture

It is well known that in the previous MPEG video coding standards the input video sequence is organized into groups of pictures (GOPs). Each GOP consists of three types of

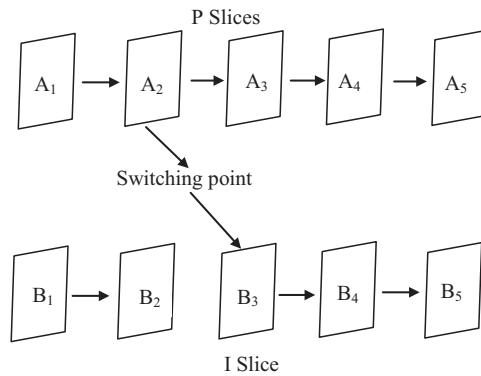
frames or pictures, which are Intra-coded (I) frame or picture, Predictive-coded (P) frame or picture, and Bi-directionally predictive-coded (B) frame or picture. As in MPEG-2 we use the word “picture” instead of the word “frame” in order to provide a more general discussion, because a picture can either be a frame or a field. It should be noted that there is no I, P, B-Picture concept in the H.264/AVC. There are only slice types, which can be I, P or B slices. Therefore, strictly speaking, there is no such thing as an I picture in the H.264/AVC video standard. The term is not used. However, a picture can contain I, P, or B slices in any combination.

To satisfy requirements for some applications, the H.264/AVC video coding standard has specified a new picture type, instantaneous decoding refresh (IDR) picture. Its exact definition is a coded picture in which all slices are I or SI slices that cause the decoding process to mark all reference pictures as “unused for reference” immediately after decoding the IDR picture. This means that after the decoding of an IDR picture all following coded pictures in decoding order can be decoded without inter prediction from any picture decoded prior to the IDR picture. The first picture of each coded video sequence is an IDR picture.

Based on this definition, the primary difference between IDR picture of H.264 and I-picture of MPEG-2 is that for H.264 after sending an IDR picture, the encoder cannot use any pictures that preceded the IDR picture (in decoding order) as references for the inter prediction of any pictures that follow the IDR picture (in decoding order). So, the presence of an IDR picture in H.264/AVC is roughly similar to the presence of an MPEG-2 GOP header in which the closed_gop flag is set to 1. The closed_gop flag is a one-bit flag that indicates the nature of the predictions used in the first consecutive B-pictures (if any) immediately following the first coded I-frame following the group of picture header. The closed_gop is set to ‘1’ to indicate that these B-pictures have been encoded using only backward prediction or intra coding. The presence of a H.264/AVC “I- picture” that is not an IDR picture but contains all I slices is similar to either an MPEG-2 I-picture without a GOP header or an MPEG-2 GOP header in which the closed_gop flag is equal to 0. Also, the presence of an IDR picture in H.264/AVC causes a reset of the PicOrderCount and frame_num counters of the decoding process, while an “I picture” that is not an IDR picture does not. Therefore, it should be noted that an IDR picture is a more severe event than an MPEG-2 I- picture, as it prohibits “open GOP” behavior, that means the references for inter prediction have to be within a GOP. In an open GOP, the reference pictures from the previous GOP at the current GOP boundary can be exploited. For example, the GOP is open when B-pictures at the start of a GOP rely on I or P-pictures from the immediately previous GOP.

21.3.2 Switching I Slices and Switching P Slices

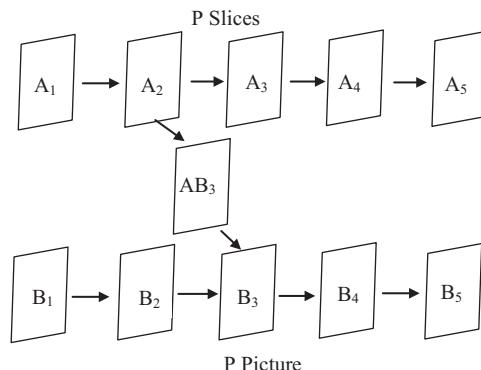
In addition to the new concept of IDR picture introduced in the previous section, H.264 has other new types of slices, SP and SI slices (Karczewisz and Kurceren 2003). The main purpose of SP and SI slices is to enable efficient switching between video streams and efficient random access for video decoders. Video streaming is an important application over IP networks and 3G wireless networks. However, due to varying of network conditions, the effective bandwidth to a user may vary accordingly. Therefore, the video server should scale the bit rate of the compressed video streams to accommodate the bandwidth variations. There are several ways to achieve bitstream scaling such as video transcoding, but the simplest way for real-time application is to generate several separate pre-encoded bitstreams for the same video sequence with different bit rates, of course at different quality levels at the same time. The server can then dynamically switch from higher rate bitstream to the lower

**FIGURE 21.4**

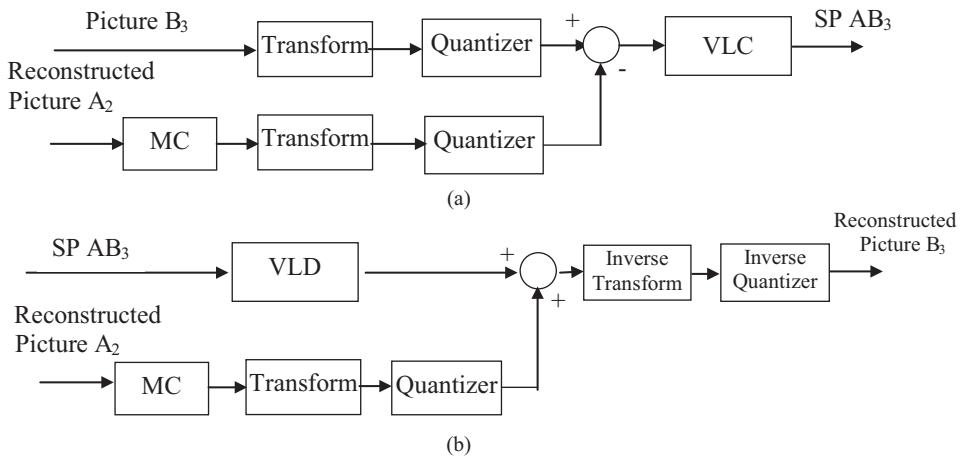
A decoder is decoding Stream A and wants to switch to decoding Stream B.

rate bitstream when the network bandwidth drops. This can be described in [Figure 21.4](#). In [Figure 21.4](#), we assume that each frame is encoded as a single slice type and predicted from one reference. Also, assume that stream A is coded with higher bit rate and stream B is coded with lower bit rate. After decoding P slices A₁ and A₂ in Stream A, the decoder wants to switch to Stream B and decode B₃, B₄, and so on. In this case, it is obvious that the B₃ has to be coded as an I slice. If B₃ is coded as P slices, then the decoder will not have the correct decoded reference pictures required to reconstruct B₃ since B₃ is predicted from the decoded frame B₂, which does not exist in stream A. Therefore, the bitstream switching can be accomplished by inserting an I slice at regular intervals in the coded sequence to create “switching points.” However, an I slice does not exploit any temporal redundancy and it likely requires much more bits to be coded than a P slice. This would result in a peak in the coded bitstream at each switching point. To address this problem, the SP slices are proposed to support switching without the increased bit rate penalty of I slices.

The idea behind SP slice assumes that we encode a video sequence with different encoding parameters and generate multiple independent streams with different bit rates. For simplicity, assume we have two streams A and B as in [Figure 21.4](#). We use the same scenario for bitstream switching. After decoding P slices A₁ and A₂ in Stream A, the decoder wants to switch to Stream B and decode B₃, B₄, and so on. The SP slices are placed at the switching points as shown in [Figure 21.5](#).

**FIGURE 21.5**

Switching streams using SP slices.

**FIGURE 21.6**

(a) SP slice encoding and (b) SP slice decoding.

The key point is that the SP slice AB_3 is encoded as P slice with B_3 as input picture and reconstructed A_2 as predictive reference. The encoding and decoding procedure of AB_3 are shown in Figure 21.6.

It is clear that the SP slice will not result in a peak in the bitstream since it is coded using motion-compensated prediction as a P slice, which is more efficient than intra coding. From Figure 21.5, it is shown that the SP slice AB_3 can be decoded using reference frame A_2 . It should be noted that the decoder output picture B_3 is identical whether decoding B_2 followed by B_3 or A_2 followed by AB_3 . If we want to switch the bitstream in another direction, another SP slice, BA_3 , would be required. But this is still more efficient than encoding frames A_3 and B_3 as I slices. However, the SI slice may be used for switching from one sequence to a completely different sequence, where the motion-compensated prediction is not efficient due to significant scene changes.

It should be indicated that the SP and SI slices are not only used for stream switching, but can also be used for error resilience video coding. The feature of SP and SI slices can be exploited in the adaptive intra refresh mechanism.

21.3.3 Transform and Quantization

The previous video coding standards such as MPEG-1/2, MPEG-4 Part 2, JPEG, H.261, and H.263 all use 8×8 DCT transform as the basic transform. In H.264/AVC the block size used in transform coding is 4×4 . There are several questions that should be answered to understand why the H.264/AVC chooses 4×4 integer transform. The first question is the selection of block size of 4×4 instead of 8×8 as in most previous video coding standards. In general, the larger block size could be better for exploiting the global correlations to increase the coding efficiency. From the other side, the smaller block size could be better for exploiting the adaptivity according to the local activity in content and also it is obvious that the complexity of implementation is greatly reduced. In addition, the smaller block size could be more adaptively matched the motion compensation with variable block size used in H.264/AVC, the smallest block size for motion compensation is 4×4 .

In the H.264 video, three transforms have been used for three different applications, which include 4×4 Hadamard transform for the 4×4 luma DC coefficients in intra

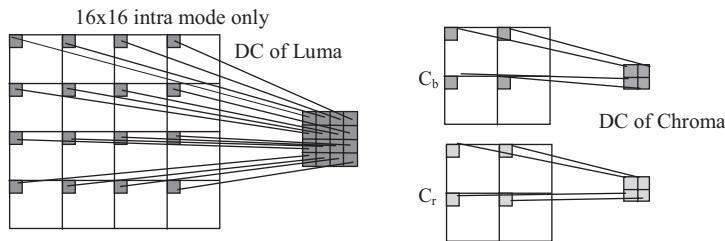


FIGURE 21.7
Matrix formation for DC coefficients of luma and chroma.

macroblocks predicted in 16×16 mode, 2×2 transform for 2×2 of chroma DC coefficients in any macroblock and 4×4 integer transform for 4×4 blocks for the luma residual data. The matrices of 4×4 (luma) and 2×2 (chroma) DC coefficients are formed as in Figure 21.7.

As shown in Figure 21.7, for the 16×16 intra mode there are a total of 16 4×4 blocks. After 4×4 transform, 16 Luma DC coefficients are extracted to form a 4×4 block, which is coded by a 4×4 Hadamard transform coding. Accordingly, the chroma DC coefficients are used to form a 2×2 block, which is coded by a 2×2 Hadamard transform coding. The function of two-DC transform coding is to remove the spatial redundancy among 16 4×4 neighboring blocks. This two-level transform is referred to as a hierarchical transformation, which aims at higher coding efficiency and lower complexity. The two transforms used to code luma and chroma DC coefficients are as follows:

$$H_L = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & 1 & -1 \end{bmatrix} \quad H_C = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

The most important transform used in H.264/AVC is the 4×4 integer transform, which is referred to as high-correlation transform (HCT) (Cham 1983, Hallapuro et al. 2002). The 4×4 HCT is applied to 4×4 predicted residual blocks. The forward transform is represented in the matrix format as follows:

$$[H_f] = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 2 & 1 & -1 & -2 \\ 1 & -1 & -1 & 1 \\ 1 & -2 & 2 & -1 \end{bmatrix}$$

This matrix is an integer approximation of 4×4 discrete cosine transform (DCT). The inverse transform is represented by:

$$[H_i] = \begin{bmatrix} 1 & 1 & 1 & 1/2 \\ 1 & 1/2 & -1 & -1 \\ 1 & -1/2 & -1 & 1 \\ 1 & -1 & 1 & -1/2 \end{bmatrix}$$

It can be seen that the HCT transform used in H.284/AVC is not orthogonal due to the approximation of DCT transform, which can be found from the following:

$$[H_f] \cdot [H_i] = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 2 & 1 & -1 & -2 \\ 1 & -1 & -1 & 1 \\ 1 & -2 & 2 & -1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 1 & 1 & 1/2 \\ 1 & 1/2 & -1 & -1 \\ 1 & -1/2 & -1 & 1 \\ 1 & -1 & 1 & -1/2 \end{bmatrix} = \begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 5 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 5 \end{bmatrix}$$

Therefore, in the inverse transform of decoding, all scale factors resulting from this operation have to be compensated by the quantization process.

The H.264 uses a scalar quantizer. As we mentioned previously, we use integer transform to avoid division and floating-point arithmetic, so we need to add rescaling function in the inverse quantization. The detailed procedure can be found in Hallapuro et al. (2002).

21.3.4 Intra Frame Coding with Directional Spatial Prediction

In the new video coding standard, H.264/AVC, a new intra frame technique based on the directional spatial prediction has been adopted. The basic idea of this technique is to predict the macroblocks to be coded as intra with the previously coded regions selected from proper spatial direction in the same frame. The merit of directional spatial prediction is able to extrapolate the edges of previously decoded parts of the current picture to the macroblocks to be coded. This can greatly improve the accuracy of the prediction and improve the coding efficiency. For the 4×4 intra mode, in addition to DC prediction, there are a total of eight prediction directions as shown in Figure 21.8. For the 16×16 intra mode, there are four prediction modes: vertical, horizontal, DC, and plan prediction. For the technical detail, please refer to (Wiegand et al. 2003).

21.3.5 Adaptive Block Size Motion Compensation

In many video-coding standards, a macroblock consisting of a 16×16 block of luma pixels and two corresponding blocks of chroma pixels is used as the basic processing unit of the video decoding process. A macroblock can be further partitioned for

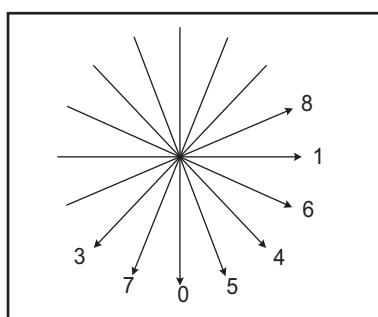


FIGURE 21.8

Eight predictive directions for intra 4×4 prediction in H.264/AVC.

inter prediction. The selection of the block size for inter prediction partitions is a compromise result between the bit saving provided by using motion compensation with smaller blocks and the increased number of bits needed for coding motion vectors. In MPEG-4 there is an advanced motion-compensation mode. In this mode the inter prediction process can be performed with adaptive selection of 16×16 block or 8×8 block. The purpose of the adaptive selection of the matching block size is to further enhance coding efficiency. The coding performance may be improved at low bit rate since the bits for coding prediction difference could be greatly reduced at the limited extra cost for increasing motion vectors. Of course, if the cost for coding motion vectors becomes too high, the mode for using small block size will not be selected. The decision made in the encoder should be very careful. If the 8×8 prediction is chosen, four motion vectors for the four 8×8 luminance blocks in a macroblock will be transmitted. The motion vectors for coding two chrominance blocks are then obtained by taking an average of these four motion vectors and dividing the average value by a factor of two. Since each motion vector for the 8×8 luminance block has half-pixel accuracy, the motion vector for the chrominance block may have a sixteenth-pixel accuracy. The issues of motion estimation process in the encoder and the selection of whether to use inter prediction for each region of the video content are not specified in the standards. The encoding issues are usually described in the informative parts of the standards. In the recently developed MPEG and ITU joint standard, H.264/AVC, the 16×16 macroblock is further partitioned into even smaller blocks as shown in [Figure 21.9](#).

In [Figure 21.9](#), it can be seen that a total of eight kinds of blocks can be used for adaptive selection of motion estimation/compensation. With optimal selection of motion-compensation mode in the encoder, coding efficiency can be greatly improved for some sequences. Of course, this is again an encoding issue, and an optimal mode selection algorithm is needed.

21.3.6 Motion Compensation with Multiple References

As we discussed previously, in most standards three picture types—I, P, and B—have been defined. Also, usually no more than two reference frames have been used for motion compensation. In the recently developed new standard, H.264/AVC, a proposal for using more than two reference frames has been adopted. The comparison of H.264/AVC with MPEG-2/4 about the reference frames is shown in [Figure 21.10](#).

The number of reference frames of H.264 can be up to 15 frames. The major reason for using multiple reference frames is to improve the coding efficiency. It is obvious that better

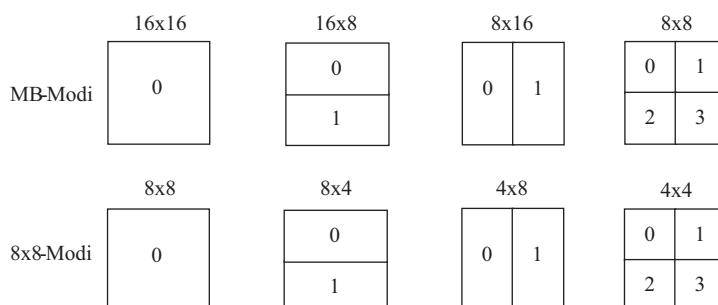
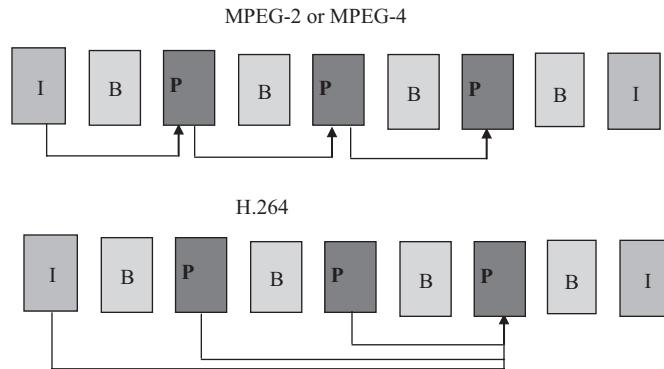


FIGURE 21.9

Macroblock partitioning in H.264.

**FIGURE 21.10**

Comparison on reference frames between MPEG-2/4 with H.264.

matching would be found by using multiple reference frames than by using fewer or equal than two frames in the motion estimation. Such an example is shown in [Figure 21.11](#).

MPEG-2/4-Part 2 Motion Estimation cannot always get better reference.

21.3.7 Entropy Coding

The H.264/AVC video standard specifies two types of entropy coding: context-based adaptive variable-length coding (CAVLC) and binary arithmetic coding (CABAC). The major function of both schemes is to improve the coding performance, but among these two schemes the former has less complexity and the latter is more complicated algorithm. As we know in the previous video coding standards, such as MPEG-2 and MPEG-4 part 2, the fixed variable-length coding (VLC) method is used for coding each syntax element or sets of syntax elements. The VLC codes are designed with the statistical characteristics of each syntax element under the assumption that the statistical characteristics are closely matched to the video data to be coded and, also, they are stationary. However, this is not true in practice; for example, the statistical behavior of the predictive residues in a motion-compensated code is non-stationary and highly depends on the video content and the accuracy of the prediction model. In the CAVLC of H.264/AVC, a total of 32 different VLCs are used. Most of these VLCs are tables, but some of the VLCs enable simple on-line calculation of any codeword with no need of storing the code tables.

Since the CAVLC is simpler than CABAC, it becomes the baseline entropy coding for H.264/AVC. In the CAVLC scheme, inter-symbol redundancies are used by switching VLC tables for different syntax components depending on the history of transmitted coding symbols. The basic coding tools in the CAVLC are the Exponential Golomb codes (Exp-Golomb codes). The Exp-Golomb codes are variable-length codes that consist of a prefix part (1, 01, 001, ...) and a suffix part that is a set of bits ($x_0, x_1 \times 0, x_2 \times 1 x_0, \dots$), where x_i is a binary bit and code structure is shown in [Table 21.1](#).

It can be seen that in [Table 21.1](#) (a), the structure of codeword can be represented as:

$$[M \text{ 0s}][1][\text{INFO}],$$

where INFO is an M-bit suffix part carrying information. Each Exp-Golomb codeword can be constructed by its index code_num as follows:

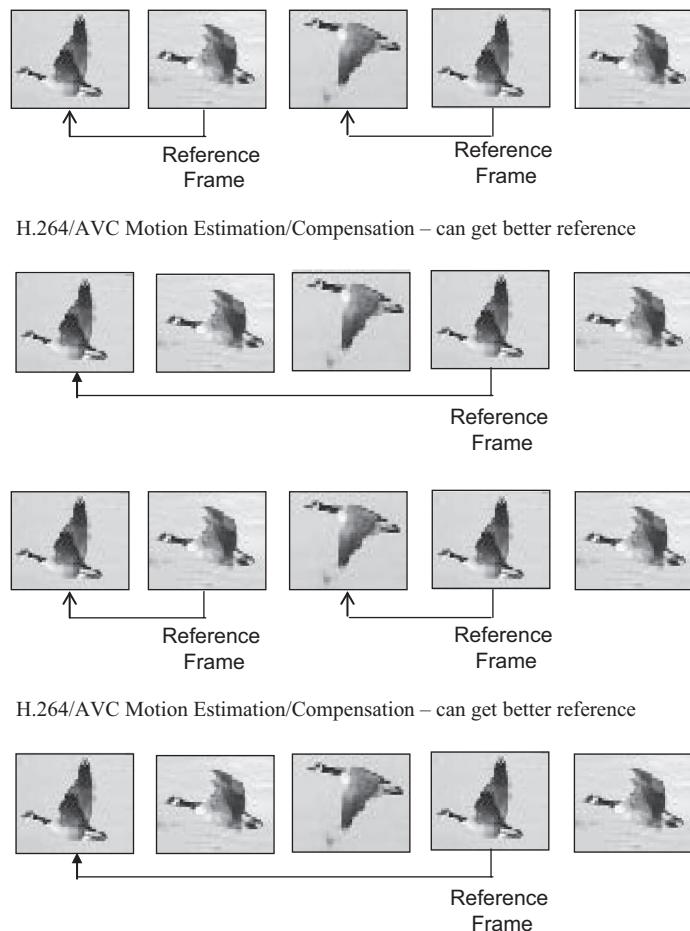


FIGURE 21.11

An example to explain the benefit by using multiple reference frames, it is noted that the better reference can be obtained by using multiple reference pictures for the video sequences with periodic changes.

TABLE 21.1

(a) Codeword Structure with Prefix and Suffix, (b) Exp-Golomb Codewords, (c) Mapping for Signed Exp-Golomb Codewords

| Codeword | Range | Codeword | code_num | code_num | Syntax Element Value (v) |
|---|-------|----------|----------|----------|--------------------------|
| 1 | 0 | 1 | 0 | 0 | 0 |
| $01 \times_1$ | 1–2 | 010 | 1 | 1 | 1 |
| $001 \times_1 x_0$ | 3–6 | 011 | 2 | 2 | -1 |
| $0001 \times_2 x_1 \times_0$ | 7–14 | 00100 | 3 | 3 | 2 |
| $00001 \times_3 x_2 \times_1 x_0$ | 15–30 | 00101 | 4 | 4 | -2 |
| $000001 \times_4 x_3 \times_2 x_1 \times_0$ | 31–62 | 00110 | 5 | 5 | 3 |
| ... | ... | ... | ... | ... | ... |

$$M = \log_2 (code_num - 1)$$

$$INFO = code_num + 1 - 2^M$$

There are three ways of mapping in the Exp-Golomb coder. The first is the unsigned direct mapping, $ue(v)$, which is used for coding macroblock type, reference frame index, and others. In this mapping, $code_num=v$. The second is the signed mapping, $se(v)$, which is used for motion vector difference, delta QP, and others. The mapping is described in [Table 21.1](#) (c), the relation between syntax element value (v) and $code_num$ is:

$$code_num = 2|v|, \text{ for } v < 0;$$

$$code_num = 2|v| - 1, \text{ for } v > 0.$$

In the third mapping, $me(v)$ is the mapped symbols. In this mapping the parameter v is mapped to $code_num$ according to the table specified in the standard [h264]. The basic principle of these mappings is to produce the codewords according to the statistics, i.e., the short codewords are used to encode the components with higher probability and longer codewords are used to code the components with small probability.

The CAVLC is the method used to encode the predictive residual, zigzag order of 4×4 (and 2×2) blocks of transform coefficients. In the CAVLC, there is no end-of-block code such as in MPEG-2. For a given 4×4 block, after prediction, transformation, and quantization the statistical distribution shows that only a few coefficients have significant values and many coefficients have magnitude equal to 1. An example of a typical block is shown below.

| | | | |
|---|----|----|---|
| 0 | 3 | -1 | 0 |
| 0 | -1 | 1 | 0 |
| 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

After zigzag reordering, the coefficients can be given as:

$$0, 3, 0, 1, -1, -1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0.$$

In the CAVLC, the number of non-zero quantized coefficients (which are noted as TotalCoeff) and the actual value and position of the coefficients are encoded separately. The coefficients with value equal to 1 are called trailing 1's (T1). For this example, the TotalCoeff=4, T1s=3.

At the first step of encoding, a coeff_token is used to code the number of coefficients and T1s. There are four look-up tables used for encoding coeff_token. These tables are described as Num-VLC0, Num-VLC1, Num-VLC2, and Num-FLC (three variable-length code tables and a fixed-length [FL] code). In order to use the correlation between neighboring blocks (context-based adaptive), the choice of table depends on the number of non-zero coefficients in upper and left-hand previously coded blocks Nu and NL. The parameter N is defined as follows: if blocks U and L are available (i.e., in the same coded slice), $N=(Nu + NL)/2$; if only block U is available, $N=N_U$; if only block L

is available, $N=N_L$; if neither is available, $N=0$. After N is decided, the look-up table for coding coeff_token can be decided:

If $N=0$ or 1, Num-VLC0 is selected; if $N=2$ or 3, Num-VLC1 is selected; if $N=4, 5, 6$, or 7, Num-VLC2 is selected; finally, if $N=8$ or above, the Num-FLC is selected.

When you check the tables in the standard, you can find that Num-VLC0 is used for small numbers of coefficients; the short codes are assigned to low values of TotalCoeffs (0 and 1) and the long codes are used for large value of TotalCoeffs. Num-VLC1 is used for medium numbers of coefficients (TotalCoeff values around 2–4 are assigned relatively short codes), Num-VLC2 is used for higher numbers of coefficients, and FLC assigns a fixed 6-bit code to every value of TotalCoeff.

The second step is to encode the sign of each T1. At this step, one bit is used to code the sign of each T1 with the order from highest frequency.

The third step is to encode the levels of the remaining non-zero coefficients. The choice of VLC table to encode each level adapts depending on the value of each successive coded level, and the encoding is reverse order, i.e., starting with the highest frequency towards the DC coefficient. For this step of encoding we have seven VLC tables to choose from, starting from Level_VLC0 for coding lower level value and to Level_VLC1 for encoding slightly higher values and so on. The way to select the look-up table depends on the threshold values; for example, Level_VLC0 will be initially used unless there are more than 10 non-zero coefficients and fewer than three trailing ones, in which case start with Level_VLC1. Then we encode the highest-frequency non-zero coefficient. If the value of this coefficient is larger than a pre-defined threshold, move up to the next VLC table. In this way, the choice of level is matched to the value of the recently encoded coefficients. The thresholds are listed in [Table 21.2](#); the first threshold is zero, which means that the table is always incremented after the first coefficient level has been encoded.

The fourth step is to encode the total number of zeros before the last coefficient. TotalZeros is the sum of all zeros preceding the highest non-zero coefficient in the zigzag or alternative reordered array. The reason to use a separate VLC table to encode TotalZeros is that many blocks contain a number of non-zero coefficients at the start of the array and this approach means that zero-runs at the start of the array need not be encoded.

The fifth step is to encode each run of zeros, run_before. The run_before is the number of consecutive zero-valued quantized transform coefficients in the reverse scan order starting from the last non-zero valued coefficient. Each block run_before specifies zero-runs before the last non-zero coefficient.

TABLE 21.2

Thresholds for Determining Whether to Increment Level Table Number

| Current VLC Table | Threshold to Increment Table |
|-------------------|------------------------------|
| VLC0 | 0 |
| VLC1 | 3 |
| VLC2 | 6 |
| VLC3 | 12 |
| VLC4 | 24 |
| VLC5 | 48 |
| VLC6 | N/A (highest table) |

Now we use the above example to explain how to perform the encoding.

- Reordered block: 0,3,0,1,-1,-1,0,1,0...
- TotalCoeffs = 5
- TotalZeros = 3
- T1s = 3 (in fact there are four trailing ones but only three can be encoded as a “special case”)

The encoding procedure is described in the [Table 21.3](#).

The final result of transmitted bitstream for this block is 000010001110010111101101. For typical test conditions and test sequences, the CAVLC can obtain 2%–7% saving in bit rate compared with a conventional VLC scheme based on a single Exp-Golomb code.

The CAVLC is a simple and efficient entropy coding method. However, the CAVLC cannot provide adaptation to the actual conditional symbol statistics that limit its performance. Furthermore, the symbols with probabilities higher than 0.5 cannot be efficiently coded with CAVLC since those symbols appear to be coded with a high fractional accuracy in bits whereas VLC coding is limited with lower accuracy of 1 bit/symbol. As we mentioned previously, another entropy coding scheme adopted in H.264/AVC is context-adaptive binary arithmetic coding (CABAC). The CABAC achieves better performance than CAVLC with 10%–15% average bit rate saving at the cost of increasing the complexity. The main reasons for obtaining better performance include the following factors. The first is that CABAC is to select probability model for each syntax element according to the element’s context. The second reason is to adapt probability estimation based on local statistics in CABAC. Finally, the CABAC uses arithmetic coding, which could reach high fractional accuracy in bits.

The CABAC encoder consists of four steps: binarization, context modeling, arithmetic coding, and probability updating. In the step of binarization, only the non-binary valued syntax elements, such as transformed coefficients and motion vectors, are uniquely mapped to a binary number, a so-called bin string. Those binary-valued syntax elements will bypass this step. The reason for the need of the binarization step is to reduce the alphabet size of the syntax elements, which would result in fast and accurate estimation of conditional probabilities, subsequently minimizing the computational complexity involved in performing each elementary operation of probability estimation and subsequent arithmetic coding. In this

TABLE 21.3
Encoding Procedure of CAVLC

| Element | Value | Code |
|---------------|---------------------------|-----------------------------|
| coeff_token | TotalCoeffs=5, T1s=3 | 0000100 |
| T1 sign (4) | + | 0 |
| T1 sign (3) | - | 1 |
| T1 sign (2) | - | 1 |
| Level (1) | +1 (use Level_VLC0) | 1 |
| Level (0) | +3 (use Level_VLC1) | 0010 |
| Total Zeros | 3 | 111 |
| run_before(4) | ZerosLeft=3; run_before=1 | 10 |
| run_before(3) | ZerosLeft=2; run_before=0 | 1 |
| run_before(2) | ZerosLeft=2; run_before=0 | 1 |
| run_before(1) | ZerosLeft=2; run_before=1 | 01 |
| run_before(0) | ZerosLeft=1; run_before=1 | No code required; last coef |

step, four basic schemes of binarization and its derivatives have been used: unary, truncated unary (TU), k th order Exp-Golomb (EG k), and FL binarization schemes. From the four basic binarization schemes, three more binarization schemes are derived by concatenation. The first is a concatenation of a 4-bit FL prefix as a representation of the luminance related part of coded block pattern and a TU suffix with S=2 representation of the chrominance part of coded block pattern. The second and third concatenation schemes are derived from the TU and EG k binarization. The detail of these schemes can be found in Marpe et al. (2003).

The context model is the conditional probability for one or more bins of the binarized symbols. At the step of context modeling selection, a context model is assigned to the given symbols from a selection of available models depending on the statistics of recently coded symbols.

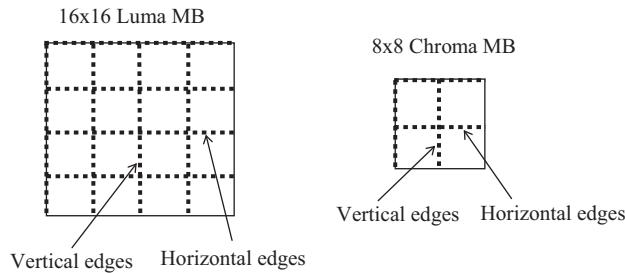
The third step is the arithmetic encoding. At this step, an arithmetic coder is used to encode each bin according to the selected probability model. The encoding is performed with recursive subdivision to fractional accuracy of an existing interval; in general, the initial interval is the range from 0 to 1.

Finally, the selected context model is updated based on the actual coded value. Since the statistical model determines the code and its efficiency, it is very important to choose an adequate model that explores the statistical dependencies of recently coded symbols.

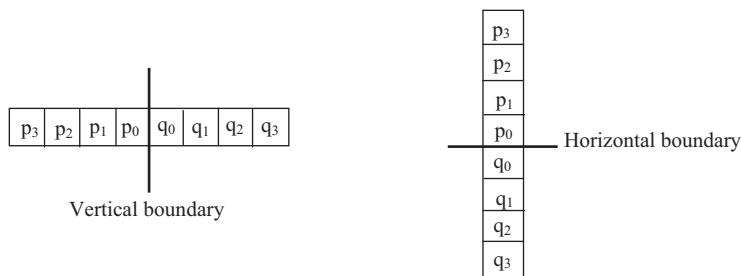
21.3.8 Loop Filter

It is similar to other video coding standards; the block artefacts could be introduced in H.264/AVC video coding since its coding scheme is block based. The most significant block artefact in H.264 is caused by 4×4 integer transformation in intra and inter frame predictive residue coding followed by quantization. The coarse quantization of transformed coefficients would result in visible discontinuities at the block boundaries. Also, for inter coded blocks, the motion-compensated reference may not be perfect and if there are not enough bits to code the predictive residues; this would cause the edge discontinuities for the blocks to be compensated. There are two ways to reduce the block artefacts. The first is the post-filtering, which operates on the display buffer and outside of the coding loop. The post-filtering is an optional for the decoder and it is not a normative part of the standard. In H.264/AVC, the deblocking filter is a normative part of the standard; it has to be in both encoder and decoder. The deblocking filter has been used in the coding loop to every decoded macroblock in order to reduce blocking artefacts. In the coding loop, the filter operation is applied after the inverse transform before reconstructing and storing the macroblock for future predictions in the encoder and before reconstructing and displaying the macroblock in the decoder. The use of deblocking filter wants to reach two main goals. The first is to smooth block edges and improve the appearance of decoded images, particularly at higher compression ratios. The second goal is to reduce the predictive residue for motion-compensated prediction of further frames in the encoder. It should be noted that the intra prediction is carried out using unfiltered reconstructed macroblocks to form the prediction, though intra-coded macroblocks are filtered. Filtering is applied to vertical or horizontal edges of 4×4 blocks in a macroblock as shown in [Figure 21.12](#).

In [Figure 21.12](#), the block boundaries in a MB are filtered in the following orders. The vertical boundaries are filtered first from left to right, and then the vertical boundaries are filtered from top to bottom. This is the same for both luma and chroma. Each filtering operation is applied to a set of pixels at either side of the block boundary; a total of 8 pixels across vertical or horizontal boundaries of the block are involved as shown in [Figure 21.13](#). [Figure 21.13](#) shows 4 pixels on either side of a vertical or horizontal boundary in adjacent blocks p and r (p_0, p_1, p_2, p_3 and q_0, q_1, q_2, q_3). Depending on the current quantizer, the

**FIGURE 21.12**

Boundaries in a MB to be filtered (dark lines represent the block boundaries to be filtered).

**FIGURE 21.13**

Boundary-adjacent pixels would be involved in filtering operation.

coding modes of neighboring blocks and the gradient of image samples across the boundary, several outcomes are possible, ranging from no filtering at all or all 8 pixels are filtered.

The decision of whether the filtering operation would be conducted depends on the boundary strength and the gradient of image samples across the boundary. The boundary strength parameter B_s is derived based on macroblock type, motion vectors, reference picture ID and MB coding parameters and is defined as follows:

If pixels of p and q are intra coded and boundary is a macroblock boundary, B_s is assigned to 4, which means that the strongest filtering is needed; if pixels of p and r are intra coded but they are not the macroblock boundary, B_s is assigned to 3. If neither pixels of p or q are intra coded but these pixels contain coded coefficients, then B_s is equal to 2; if pixels of p and q have different reference pictures or a different number of reference or different motion vector values, B_s is set to 1; finally, neither pixels p nor q are intra coded, neither p nor q contain coded coefficients, and p and q have the same reference picture as well as identical motion vectors, and B_s is equal to 0.

The value of B_s indicates the strength of filtering process performed on the block boundaries including a selection between the three filtering modes. From the rule of value assignment to B_s , it can be seen that the filtering operation is stronger at places where there is likely to be significant blocking distortion, such as the boundary of an intra coded macroblock or a boundary between blocks that contain coded coefficients.

In cases of $B_s=0$, the filtering process is not conducted for the current 4×4 block boundary. For $B_s>0$, the filtering operation will be conducted and the strength of filtering depends on the difference between boundary pixels, and threshold values of α and β . We know that the block artefacts are most visible in very smooth areas where the pixel values do not change much across block boundaries. Therefore, the filtering threshold values should be derived based on the pixel values. The values of α and β are defined in List (2003).

In general, the values of α and β increase with the average quantizer parameter QP of the two neighboring blocks p and q. When $B_s > 0$, and $|p_0 - q_0|$, $|p_1 - p_0|$ and $|q_1 - q_0|$ are all less than the thresholds α or β then $(p_2, p_1, p_0, q_0, q_1, q_2)$ are filtered. The reason for switching filtering operation on when the difference or gradient is low can be described as follows. When the quantization parameter, QP, is small and the difference or gradient of pixels across boundary is likely to be due to image features rather than blocking effects. In this case the gradient should be preserved and so the thresholds α and β are low. When QP is larger, blocking distortion is likely to be more significant and α , β are higher so that the chance for switching filtering on is higher.

The detailed filtering operation is as follows. For $0 < B_s < 4$, a four-tap linear filter is applied with inputs p_1, p_0, q_0 and q_1 producing filtered outputs P_0 and Q_0 . In addition, if $|p_2 - p_0|$ is less than threshold α , a four-tap linear filter is applied with inputs p_2, p_1, p_0 , and q_0 , producing filtered output P_1 . If $|q_2 - q_0|$ is less than threshold β , a four-tap linear filter is applied with inputs q_2, q_1, q_0 , and p_0 , producing filtered output Q_1 . It should be noted that p_1 and q_1 are never filtered for chroma, only for luma data.

For $B_s = 4$, if $|p_2 - p_0| < a$ and $|p_0 - q_0| < \text{round}(b / 4)$, P_0 is produced by five-tap filtering of p_2, p_1, p_0, q_0 , and q_1 , P_1 is produced by four-tap filtering of p_2, p_1, p_0 , and P_2 (luma only) is produced by five-tap filtering of p_3, p_2, p_1, p_0 , and q_0 ; otherwise P_0 is produced by three-tap filtering of p_1, p_0 , and q_1 . If $|q_2 - q_0| < a$ and $|p_0 - q_0| < \text{round}(b / 4)$, Q_0 is produced by five-tap filtering of q_2, q_1, q_0, p_0 , and p_1 , Q_1 is produced by four-tap filtering of q_2, q_1, q_0 , and p_0 , Q_2 (luma only) is produced by five-tap filtering of q_3, q_2, q_1, q_0 , and p_0 ; otherwise Q_0 is produced by three-tap filtering of q_1, q_0 , and p_1 .

21.3.9 Error Resilience Tools

While coding efficiency is the most important aspect in the design of any video coding scheme, the transmission of compressed video through noisy channels has always been a key consideration. This is evident by the many error-resilience tools that are available in video coding standards, such as in MPEG-2, MPEG-4 Part 2, and some only in H.264/AVC.

The first category of error-resilience tools is the localization. These tools are used to remove the spatial and temporal redundancy between segments of the video to prevent error propagation. It is well known that video compression efficiency is achieved by exploiting the redundancy in both the spatial and temporal dimensions of the video. Due to the high correlation within and among neighboring frames, predictive coding schemes are employed to exploit this redundancy. While the predictive coding schemes are able to reach high compression ratios, they are highly susceptible to the propagation of errors. Localization techniques essentially break the predictive coding loop so that if an error does occur, then it is not likely to affect other parts of the video. Obviously, a high degree of localization will lead to lower compression efficiency. There are two methods for localization of errors in a coded video: spatial localization and temporal localization. The spatial localization technique is supported in MPEG-2 and H.264/AVC using slices, and in MPEG-4 using video packets. The resynchronization marker insertion is suitable to provide a spatial localization of errors. The temporal localization is usually implemented for preventing error propagation with the insertion of intra-coded MBs by decreasing the temporal dependency in the coded video sequence. While this is not a specific tool for error-resilience, the technique is widely adopted and recognized as being useful for this purpose. The higher percentage of intra blocks used for coding the video will reduce the coding efficiency, but reduce the impact of error propagation on successively coded frames. In the most extreme case, all blocks in every frame are

coded as intra blocks. In this case, there will be no temporal propagation of errors, but a significant increase in bit-rate could be expected. The selection of intra-coded blocks may be cyclic, in which the intra-coded blocks are selected according to a predetermined pattern; the intra-coded blocks may also be randomly chosen or adaptively chosen according to content characteristics.

The second category of error resilience tools is the data partitioning. It is well known that every bit in a compressed video bitstream is not of equal importance. Some bits belong to segments defining vital information such as picture types, quantization values, etc. When coded video bit-streams are transported over error-prone channels, errors in such segments cause a much longer lasting and severe degradation on the decoded video than that caused by errors in other segments. Therefore, data partition techniques have been developed to group together coded bits according to their importance to the decoding such that different groups may be more effectively protected using unequal protection techniques. For example, during the bitstream transmission over a single channel system, the more important partitions can be better protected with stronger channel codes than the less important partitions. Alternatively, with a multi-channel system, the more important partitions could be transmitted over the more reliable channel. This kind of tool is defined in MPEG-2 and MPEG-4 Part 2 video but not in H.264/AVC.

The third category is redundant coding. This category of techniques tries to enhance error resilience by adding redundancy to the coded video. The redundancy may be added explicitly, such as the concealment motion vectors, or implicitly in the coding scheme, as in the reversible variable-length codes (RVLC) and multiple description coding (MD).

All of these strategies for error-resilience indirectly lead to an increase in the bit-rate and loss of coding efficiency, where the overhead with some is more than others. In the following, we describe each tool in terms of the benefit it provides for error-resilient transmission, as well as its impact on coding efficiency.

In the H.264/AVC, several new error-resilience tools, which are different from previous standards, MPEG-2 or MPEG-4 Part 2, have been adopted. These tools include FMO, ASO, and redundant slices. The idea of FMO is to specify a pattern that allocates the macroblocks in a picture to one or several slice groups not in normal scanning order, but in a flexible way. In such a way, the spatially consecutive macroblocks are assigned to different slice groups. Each slice group is transmitted separately. If a slice group is lost, the image pixels in spatially neighboring macroblocks that belong to other correctly received slice groups can be used for efficient error concealment. The allowed patterns of FMO range from rectangular patterns to regular scattered patterns, such as checkerboards, or completely random scatter patterns. Furthermore, the idea of FMO can be extended to the slice level. In some profiles of the H.264/AVC standard the slices can be sent in an arbitrary order to increase the capability of error resilience. The slices can also be bundled into slice groups, which may contain one or more slices. The exact number of slices is specified by a parameter in the picture parameter set.

21.4 Profiles and Levels of H.264/AVC

In this section, we would like to give brief description about H.264/AVC profiles. It is the same as in MPEG-2 and MPEG-4; a profile defines a set of coding tools or algorithms, which are used in generating a compliant bitstream with this profile. If a decoder is claimed to conform a specific profile, it must support all tools and algorithms in that profile.

21.4.1 Profiles of H.264/AVC

There are a total of seven profiles defined in the H.264/AVC so far, which are the baseline, main, extended, high, high 10, high 4:2:2, and high 4:4:4. The process is carried on to replace the High 4:4:4 Profile with a better one, which is the Advanced High 4:4:4 Profile. In the following we briefly introduce each of these profiles.

The baseline profile supports all following features in H.264/AVC:

- Support I and P slice types, but no B slice type.
- NAL unit streams do not contain the coded slices, which is a non-IDR picture.
- Sequence parameter sets contain the parameters such that every coded picture of the coded video sequence is a coded frame containing only frame macroblocks.
- Support 4:2:0 chroma format, 8-bit luma and chroma pixels.
- The transform coefficient decoding process and picture construction process prior to deblocking filter process shall not use the transform bypass operation.
- Use only flat quantization matrix, it means that all components in the matrix are 16.
- Weighted prediction shall not be applied to P and SP slices and the default weighted prediction specified in [h264] shall be applied to B slices.
- Entropy coding uses Exp-Golomb codes or CAVLC and does not support CABAC.
- Support FMO.
- Use only 4×4 transformation, same quantization matrix specified in sequence level and no quantization offset.
- No interlacing support.
- No SP/SI slices and slice data partitioning.

Also, there are several flags and their combinations used to define the conformance of a bitstreams to the Baseline Profile. The detail can be found in the specification [h264].

The Main Profile supports the following features:

- Support I, P, and B slices
- NAL unit streams do not contain the coded slices, which is a non-IDR picture
- Not support ASO and FMO
- Support 4:2:0 chroma format, 8-bit luma, and chroma pixels
- Support interlacing
- All slices of the picture belong to the same slice group
- No slice partitioning
- Use only 4×4 transformation, same quantization matrix specified in sequence level, and no quantization offset

The features of the extended profile include:

- Support I, P, and B slices and interlaced tools.
- Support 4:2:0 chroma format, 8-bit luma, and chroma pixels.
- Entropy coding uses Exp-Golomb codes or CAVLC and does not support CABAC.

- Support FMO and ASO.
- Support SI, SP slices, and data partitioning.
- Use only 4×4 transformation, same quantization matrix specified in sequence level, and no quantization offset.

In summary, the main profile supports all features except SP/SI slices, slice partitioning, FMO, ASO, and redundant pictures. The extended profile supports all features except CABAC. Therefore, these three profiles are not the subset each other and target for different applications. The baseline profile is used for videophone, mobile communication, and low-delay applications. The main profile targets interlaced video, broadcast, and packaged media applications. The extended profile mainly targets streaming video and wireless transmission applications. Compared with MPEG-2 video, the main profile of H.264/AVC can provide 50%–100% improvement on the coding efficiency but increase about 2.5 to 4 times of decoder complexity.

There are also several profiles that have been defined in H.264/AVC. These profiles include High Profile, High 10 Profile, High 4:2:2 Profile, and the recently developed advanced 4:4:4 Profile.

High Profile is a superset of Main Profile. The main difference with Main Profile is that the High Profile supports both 8×8 and 4×4 transformations, which can improve the coding performance at high bit rates for HDTV sequences. High Profile has also the tools for enabling to change the quantization parameter offset differently for two chroma components for better subjective quality.

High 10 Profile is defined for 10-bit video sequences. The applications of this profile include medical image sequences and some other high-quality image sequences encoding.

The several High 4:4:4 Profiles have been developed that provide better coding performance and more functionality and they are more appropriate to high-quality applications such as studio camcorders, professional digital video recording and editing systems, digital cinema with large-screen digital imagery, high-fidelity display systems, etc. For these new profiles the JVT has recently developed two new amendments to the MPEG4-AVC/H.264 standard that specify a set of five new profiles, two new SEI messages, and two new extended gamut color space indicators. The new profiles are called the High 10 Intra, High 4:2:2 Intra, High 4:4:4 Intra, CAVLC 4:4:4 Intra and High 4:4:4 Predictive profiles. They include substantial feature enhancements for high-quality video applications, including improved-efficiency 4:4:4 video format coding, improved-efficiency lossless macroblock coding, coding 4:4:4 video pictures using three separately coded color planes, and bit depths up to 14 bits per sample. In addition, all-Intra coding profiles will be widely used in content creation, production, and post-production applications, primarily for ease of editing. Four of the five new profiles have thus been defined for all Intra coding to enable applications requiring simple editing of bitstreams without imposing the burden of implementing the extra inter-picture decoding functionality that would not be needed in such applications. In these new profiles, new “post-filter hint” and “tone mapping” SEI messages are defined to further enhance the decoded image quality on displays even with different characteristics. Additionally, to support future high-quality display technology, the ability to indicate the use of the extended gamut color spaces defined by IEC 61966-2-4 (xvYCC₆₀₁ and xvYCC₇₀₉) and ITU-R BT.1361 has been enabled (Sullivan 2007).

21.4.2 Levels of H.264/AVC

As we discussed in the previous section, a profile specifies a subset of the entire bit-stream syntax of the standard for certain applications. However, within the specified

limitations imposed by a given profile it may still be possible to require a very large variation in the processing power and memory size of encoders and decoders. Those variations depend upon the factors such as the picture size, the frame rate, the maximum bit rate, and the maximum number of reference frames. Therefore, within a profile we have to define the levels that specify a set of constraints on values. The following table shows the levels specified in the standard of H.264/AVC. A decoder compliant with a specified profile and level must be able to decode the bitstreams compliant to that profile and level as well as those bitstreams with levels lower than that level. The detail of the level definition can be found in the H.264 specification and shown in [Table 21.4](#).

TABLE 21.4

Level Limits

| Level Number | Typical Picture Size | Typical Frame Rate | Max Video Bit Rate (K bits/s) | Vertical MV Component Range (Luma Frame Samples) | Maximum Number of Reference Frames | Max Number of Motion Vectors Per Two Consecutive MBs |
|--------------|---|--------------------|-------------------------------|--|------------------------------------|--|
| 1 | QCIF | 15 | 64 | [−64,+63.75] | 4 | — |
| 1b | QCIF | 30 | 128 | [−64,+63.75] | 4 | — |
| 1.1 | QVGA (320 × 240) | 10 | 192 | [−128,+127.75] | 3 | — |
| | QCIF | 30 | | | 9 | |
| 1.2 | CIF | 15 | 384 | [−128,+127.75] | 6 | — |
| 1.3 | CIF | 30 | 768 | [−128,+127.75] | 6 | — |
| 2 | CIF | 30 | 2 000 | [−128,+127.75] | 6 | — |
| 2.1 | HHR (352 × 480) (352 × 576) | 30 25 | 4 000 | [−256,+255.75] | 7 | — |
| 2.2 | SD (720 × 480) (720 × 576) | 30 25 | 4 000 | [−256,+255.75] | 6 | — |
| 3 | SD (720 × 480) (720 × 576) VGA (640 × 480) | 30 25 30 | 10 000 | [−256,+255.75] | 6 | 32 |
| 3.1 | 1280 × 720P SVGA (800 × 600) 1280 × 720P | 30 56 60 | 14 000 | [−512,+511.75] | 5 | 16 |
| 3.2 | 4VGA (1280 × 960) | 45 | 20 000 | [−512,+511.75] | 4 | 16 |
| 4 | HD (1280 × 720P) (1920 × 1080I) (2Kx1K) | 60 30 30 | 20 000 | [−512,+511.75] | 9 4 4 | 16 |
| 4.1 | HD Formats (1280 × 720) (1920 × 1080) | 60 30 | 50 000 | [−512,+511.75] | 9 4 | 16 |
| 4.2 | 1920 × 1080 | 60 | 50 000 | [−512,+511.75] | 4 | 16 |
| 5 | 2Kx1K 16VGA | 72 30 | 135 000 | [−512,+511.75] | 14 5 | 16 |
| 5.1 | 2Kx1K 4Kx2K | 120 30 | 240 000 | [−512,+511.75] | 16 5 | 16 |

21.5 Summary

In this chapter, the new video coding standard, MPEG-4 Part 10 Advanced Video Coding Standard, or H.264, which is jointly developed by JVC of MPEG and ITU-T VCEG, has been introduced. The H.264/AVC is an efficient and state-of-the-art video compression standard, which coding efficiency is about two times better than that of MPEG-2. The H.264/AVC has been planned for many applications including HD-DVD, DTV for satellite and wireless networks, IPTV, and many others.

Exercises

- 21.1 Indicate at least three new tools that make H.264/AVC have better coding performance. Explain why? If it is possible, please conduct computer simulations to verify it.
 - 21.2 What are the entropy coding schemes used in H.264/AVC? Explain each of them.
 - 21.3 Describe the principle of the deblocking filter of H.264/AVC. Conduct a simulation experiment to compare the subjective quality of decoded images with and without the deblocking filter.
 - 21.4 What are the new tools that are different from previous MPEG video for increasing the error robustness of the H.264 video coding scheme? Give explanation.
 - 21.5 Describe the principle of the integer transform in H.264. Why is integer transformation adopted by H.264 video? What is the problem of integer transformation and how to solve this problem in H.264?
 - 21.6 Describe the intra prediction algorithm used in H.264.
-

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22

A New Video Coding Standard—HEVC/H.265

After several important video coding standards such as MPEG-2, MPEG-4 part 2 and part 10/H.264 have been successfully developed, a new video coding standard, high-efficiency video coding (HEVC) in MPEG or referred to as H.265 in ITU, has been developed and standardized collaboratively by the Joint Video Team (JVT) of ISO/IEC MPEG and ITU-T VCEG in 2013. It is the same as for H.264/MPEG-4 AVC; the main objective of HEVC/H.265 is further improving the coding efficiency. Additionally, HEVC/H.265 targets the optimization of the coding performance for the new video format such as for color format of 4:4:4, high-resolution video 4K × 2k, or even higher-resolution such as 8K × 4K and videos with screen contents. Therefore, the standard contains its basic version of 1.0 and version of range extensions. The test results have shown that it has made another important milestone of video coding standard at the coding efficiency improvement. Compared with H.264/MPEG-4 AVC, bit savings of about 50% can be achieved at the same visual subjective quality.

The first version of HEVC/H.265 has been approved in 2013. Actually, HEVC/H.265 was approved by ITU-T on April 13, 2013 and formally published by ITU-T on June 7, 2013 and by ISO/IEC on November 25, 2013 [h265]. The second version of HEVC/H.265 contains three extensions, the MV-HEVC, the range extension (RExt), and the scalability extension (SHVC) [shvc]. The version 2 was approved on October 29, 2014.

22.1 Introduction

HEVC [h265] is the recently developed international video coding standard, which is standardized as ITU-T Recommendation H.265 and ISO/IEC 23008 (MPEG-H Part 2) or HEVC. Based on the previous standards, HEVC/H.265 adopted several new tools for coding performance improvement. Also, some existing tools have been carefully tuned and improved, resulting in significant coding performance improvement. Compared with previous coding standards, H.264/MPEG-4 advanced video coding (AVC) (ITU-T Rec. H.264 / ISO/IEC 11496-10 [2005]), bit savings of about 50% can be achieved (Wedi and Tan 2005). in the subjective tests. Since the basic structure of H.265 is similar to the one in H.264/AVC, therefore, we will mainly introduce the different features that H.264 does not have. The main differences of HEVC/H.265 with H.264/MPEG-4 AVC include coding block (CB) size extended from 16×16 to sizes up to 64×64 , improved variable-block-size segmentation, improved intra prediction within the same frames, improved motion vector prediction and motion region merging, improved motion-compensation filtering, and an additional filtering step referred to as sample-adaptive offset filtering. Obviously, to implement these

changes requires much more signal processing power than we had before, but we can implement more complicated coding tools with these available computing powers due to great advances of the semiconductor industry. We are now able to perform encoding/decoding process for the large amount of video data with acceptable complexity increases of implementation.

22.2 Overview of HEVC/H.265 Codec Structure

The basic codec structure of HEVC/H.265 is similar to the previous coding standards such as MPEG-2 and H.264. It is based on the block coding structure with motion estimation (ME)/compensation for inter-frame coding with entropy coding. The basic coding structure is described in the [Figure 22.1](#).

From [Figure 22.1](#), the input of video source is first decomposed into basic coding units (CUs). The basic CU in HEVC/H.265 is called a coding tree unit (CTU), which can be up to 64×64 in luma samples (ITU-T Rec. H.265 and ISO/IEC 23008-2 [2013]). During encoding process the CTU is hierarchically split into CUs with the mode selection algorithms. According to the coding mode, the CU size will be variable; it can be from 8×8 to 64×64 in luma samples. Also, each CU can be coded with either intra prediction or inter prediction depending on the encoder decisions. It is different with H.264/AVC; in H.265/HEVC the

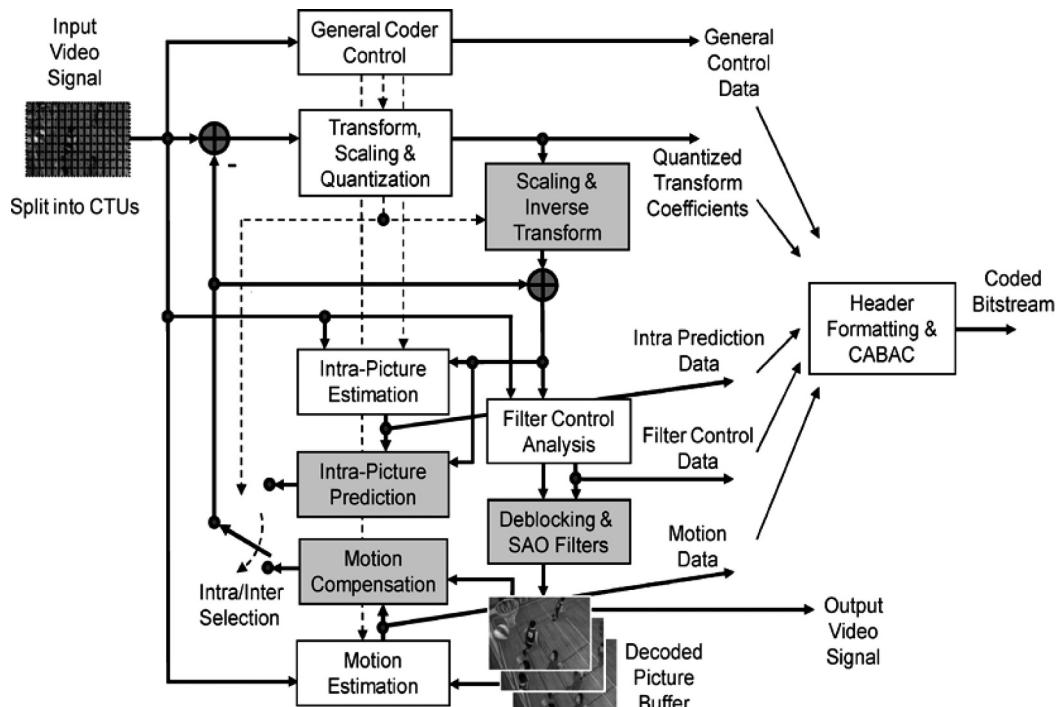


FIGURE 22.1

Block diagram of HEVC/H.265 encoder. (From Sullivan, G. J. et al., *IEEE Transactions on Circuits and Systems for Video Technology*, IEEE, 22, 2012.)

CU is not always the same as the prediction unit (PU). The CU can be further split into PUs. The PU is the basic unit to perform the prediction operations and all the pixels in one PU are predicted using the same rule. Eight kinds of PU are supported in HEVC. Another basic unit in the H.265/HEVC is the transform unit (TU), which is used to process the predictive residue information. Within an intra coded CU, a TU is always part of a PU, while for an inter-frame coded CU, a TU can cross different PUs.

After decomposition of input video, the CUs are coded with specified block partitioning shape and the side information of block partitioning will be included in the bitstream and conveyed to the decoder. As with the previous coding standards, the first frame or first frame at random access point in the input video sequence is always encoded with intra frame coding. The predictive coding methods, intra-frame prediction or inter-frame prediction, will be applied to all CUs. The intra frame prediction uses directional prediction within the same frame. The inter-frame predictions perform ME in the encoder and motion compensation in the decoder. The motion vector information and coding mode information are contained in the bitstream as side information, which can be used in the decoder.

The predictive residuals from either intra-prediction or inter-frame prediction will then be converted to the transform domain with a linear transformation. The transformed coefficients are then scaled and quantized. Finally, the scaled and quantized coefficients are sent to the entropy coder to further reduce the size of the bitstream.

It should be mentioned that before entropy coding, the filtering processing is applied to the scaled and quantized coefficients for further improving the coding performance. The filter process is included in the decoder loop. In the decoder, exactly inverse processing as in the encoder will be performed to reconstruct the video data.

Each described step looks the same as previous coding standards, but there are many new ideas that have been added. The technical detail of prediction and transform will be described in the next section.

22.3 Technical Description of H.265/HEVC Coding Tools

In the previous section we briefly give an overview of H.265/HEVC video coding structure. In this section we introduce the technical details of some of those important features. Most of these features address the problems of coding performance improvement, some are used to optimize applications such as for higher resolution videos such as 4k x 2k or 8k x 4k and higher frame rates. Also, some features, such as parallel processing, are used for faster processing. The features for range extensions and 3D applications will be described in separate sections.

22.3.1 Video Coding Block Structure (Codesequois 2012)

One common feature of video coding standards developed so far is that all use block-based coding structure. The differences between early coding standards with late developed successors are presented in the following aspects. First are the block sizes, which are getting bigger and bigger in the late standards. The second is the types of partitioning that are increased from early standards to their successors. The purpose of increasing the block partitioning is to perform better predictions and reduce the predictive residues.

The HEVC/H.265 uses several new terminologies to describe its unique block structure, which is different with previous standards. In the previous section we have mentioned some of these names. Here we will give a complete set of these terminologies used in HEVC/H.265. These terminologies include: CTU, CU, coding tree block (CTB), CB, prediction block (PB), and transform block (TB).

To describe these names, we start from the beginning of the coding procedure. It is the same as for previous coding standards; the input video data is first divided into CTUs as in [Figure 22.2](#). It can be seen that the CTU is the replacement of macroblock in the previous coding standards. The sizes of CTU can be 64×64 , 32×32 , or 16×16 [h265].

If the input video is Y(luma), Cb, and Cr (chroma) format, a CTU consists of three blocks, one luma and two chroma, and each has the name of CTB, as in [Figure 22.3](#).

It can be seen that each luma CTB has the same size as CTU such as 64×64 , 32×32 , or 16×16 , depending on encoding selection. In order to perform better predictions for the video frames contain different natured contents, such as smoothing, active, slow motion, or fast motion. CTB may be too big to decide which coding mode such as intra-prediction or inter-prediction should be performed. For this reason, each CTB can be further split

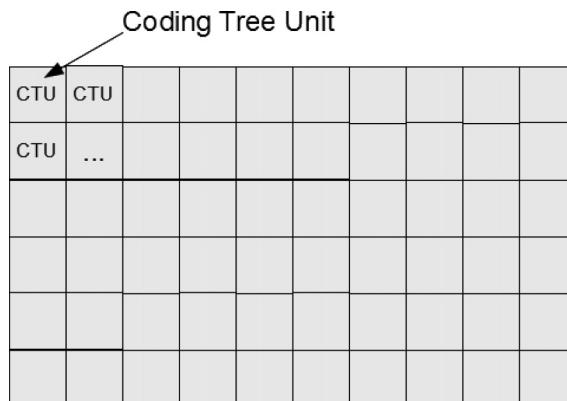


FIGURE 22.2
An input frame is partitioned into CTUs.

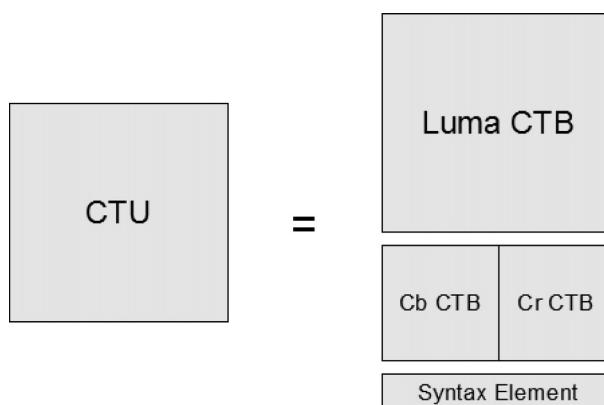


FIGURE 22.3
A CTU consists of one luma CTB and two chroma CTB.

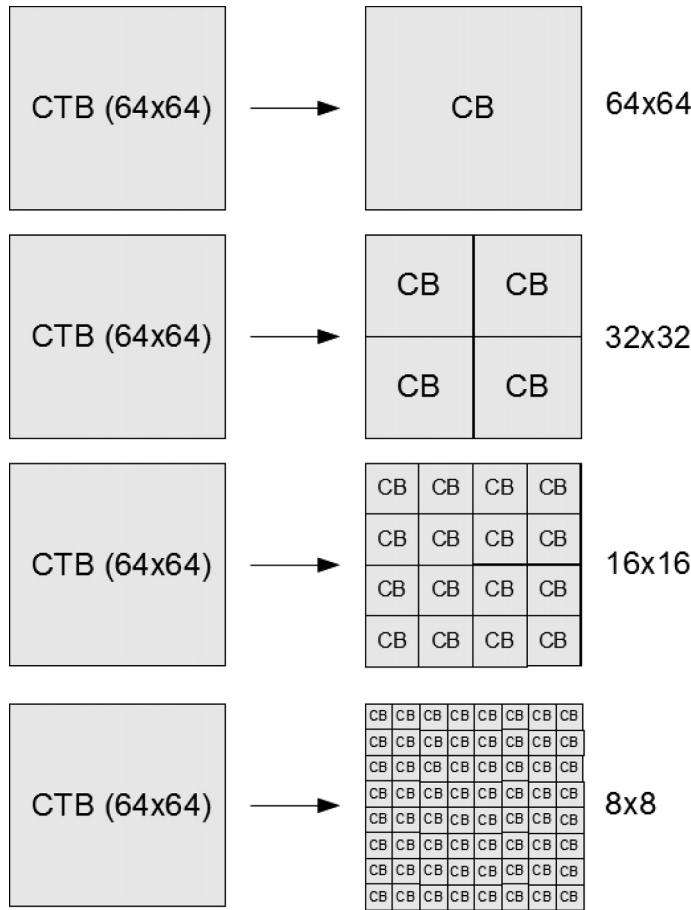


FIGURE 22.4
CB sizes.

into multiple **CBs**, which may have smaller sizes than **CTB** as shown in [Figure 22.4](#). The encoder can make the decision to select prediction type at **CB** level. For example, some **CTBs** are split to 16×16 **CBs** while others are further split to 8×8 **CBs**. The syntax of HEVC/H.265 specified the **CB** size can be from the same size as **CTB** to as small as 8×8 .

For the aspect of ME/compensation, **CB** is good enough for prediction-type decision, but it could still be too large to store motion vectors (inter prediction) or intra prediction mode. For example, a very small object may be moving in the middle of 8×8 **CB**, so we want to use different MVs depending on the portion in **CB**. Therefore, the concept of **PB** is introduced. Each **CB** can be further split to **PBs** differently depending on the temporal and/or spatial predictability as shown in [Figure 22.5](#).

Once the prediction is made, we need to code residual (difference between predicted image and actual image) with DCT-like transformation. Again, **CB** could be too big for this because a **CB** may contain both a detailed part (high frequency) and a flat part (low frequency). Therefore, each **CB** can be differently split into **TBs**, as shown in [Figure 22.6](#). Note that **TB** does not have to be aligned with **PB**. It is possible and often makes sense to perform single transform across residuals from multiple **PBs** and vice versa ([Figure 22.7](#)).

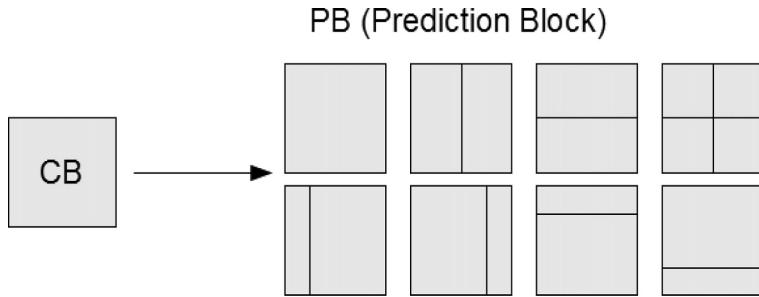


FIGURE 22.5
Relation between CB and PB.

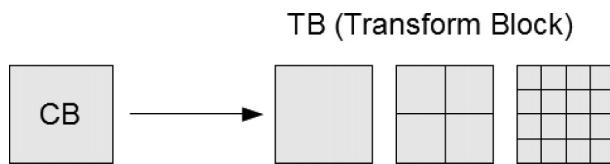


FIGURE 22.6
Relation between CB and TB.

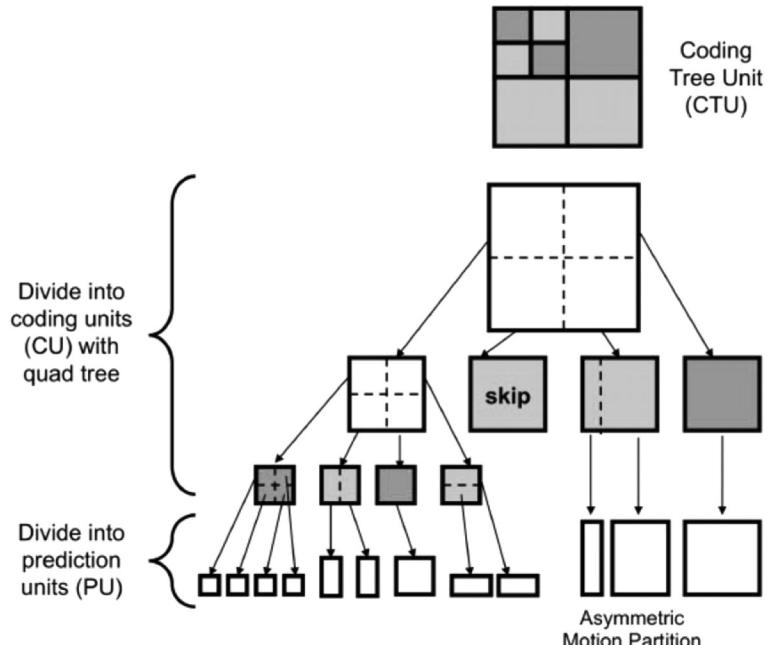


FIGURE 22.7
Tree structure of CB. (From Sze 2014.)

22.3.2 Predictive Coding Structure

As with previous coding standards, predictive coding methods are used in HEVC/H.265. Predictive processes include intra prediction and inter prediction. The purpose of intra prediction is to remove the redundancy within a frame. In HEVC/H.265, for luma component, total 35 prediction modes can be used including 33 angular directional intra prediction, DC mode, and planar mode, as shown in [Figure 22.8](#).

DC mode is the same as in H.264/AVC. It is used to efficiently predict smoothing areas in the image, but for non-smoothing area it gives a coarse prediction and is not efficient for

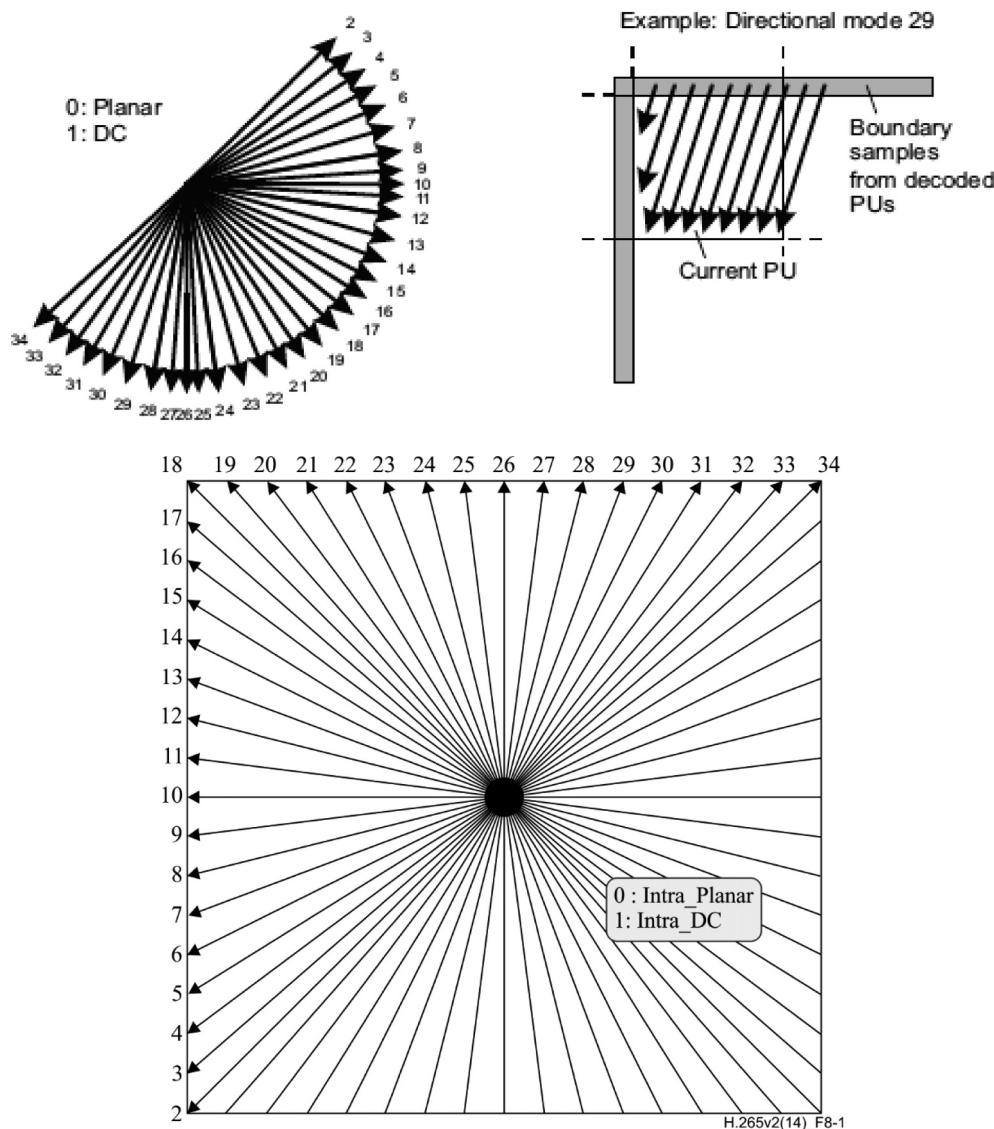


FIGURE 22.8

Intra prediction mode directions. (From Sullivan, G. J. et al., *IEEE Transactions on Circuits and Systems for Video Technology*, IEEE, 22, 2012.)

those areas. The value of each pixel of the PB is an average of the reference pixels that are the boundary pixels in the top and left neighboring TBs.

The planar mode was introduced to improve the subjective quality of regions containing smooth gradients. This mode is similar to the planar mode in H.264/AVC and is known as mode 0 in HEVC/H.265. Planar mode is essentially defined as an average value of two linear predictions using the values of four corner reference pixels. This mode is implemented as shown in [Figure 22.9](#). The pixel X is the first sample predicted as an average of the samples D and E, then the right column pixels (blue samples) are predicted using bilinear interpolation between samples in D and X, and the bottom row samples (orange samples) are predicted using bilinear interpolation between samples in E and X. The remaining samples are predicted as the averages of bilinear interpolations between boundaries samples and previously coded samples (Wiegand et al. 2003). The pixel X is the first sample predicted as an average of the samples D and E, then the right column pixels (blue samples) are predicted using bilinear interpolation between samples in D and X, and the bottom row samples (orange samples) are predicted using bilinear interpolation between samples in E and X. The remaining samples are predicted as the averages of bilinear interpolations between boundaries samples and previously coded samples (Wiegand et al. 2003).

To synchronize with transform operation, the intra prediction is performed on the TU level to make better use of the surrounding pixels already being reconstructed. The sizes of PBs can be from 4×4 up to 64×64 . Since the strong correlations exist between luma and chroma components, the chroma intra prediction process can be simplified and only five modes—the horizontal, vertical, planar, DC and luma direction—will be used. But when luma direction is one of the previous four directions, mode 18, left-downward diagonal mode will be used. The chroma components reusing the luma direction is also referred to as direct mode (DM). It is obvious that the two chroma components share the same direction.

In order to improve the subjective quality of intra prediction, the smoothing filter is applied to the reference pixels in the boundary depending on the size of the blocks and the directionalities of the prediction. The smoothing filter is applied to the first prediction row and column for DC mode, or the first prediction row for pure horizontal prediction, or the first prediction column for pure vertical prediction. For DC mode the smoothing filter consists of a two-tap finite impulse response filter, with a gradient-based smoothing filter for horizontal (mode 10) and vertical (mode 26) prediction. The smoothing filter is

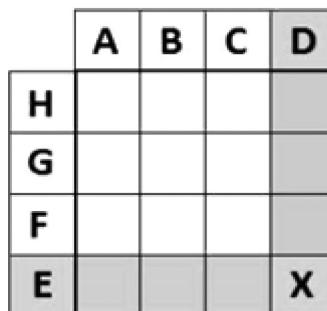


FIGURE 22.9

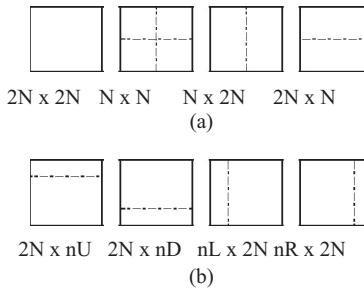
Planar intra prediction modes. (From Ling, N. High efficiency video coding and its 3D extension: A research perspective, *Keynote Speech, ICIEA, 2150–2155, Singapore, 2012*.)

not applied to chroma since the chroma components tend to be already smooth. As a result, contouring artefacts caused by boundaries in the reference pixels can be drastically reduced.

There are 35 available modes for intra prediction. The encoder is trying to select the best one with the cheapest rate-distortion (RD) cost. The reference data that are obtained from the already decoded top and left CUs are interpolated to form the prediction for the current CU regarding the angular modes. The large number of prediction modes can greatly improve the coding performance. However, this will greatly increase the encoder complexity since more modes will participate in the decision process. Therefore, it is necessary to develop a fast and efficient algorithm for mode selection on intra prediction, especially for real-time applications. For this purpose, HEVC/H.265 developed fast mode selection algorithm, which is based on the three most probable modes (MPMs) for each PU based on the modes of the neighboring PUs. The selection of the set of three MPMs is based on modes of two neighboring PUs, one left of and one above the current PU. The modes used in two previously decoded neighboring PUs are known as the set of MPMs. The detailed operation of MPM can be found in the reference (Sullivan et al. 2012).

As with previous video coding standards, HEVC/H.265 uses inter prediction to remove temporal redundancy. The inter prediction performs ME on the encoder side and motion compensation on the decoder side.

At the encoder side, each frame is first partitioned into CU blocks of 64×64 pixels. Each of these blocks is also referred to as the largest coding block (LCU). Each LCU is further split recursively into four sub-blocks until the smallest coding units (SCUs) of size 8×8 are reached. The partitioning process can be illustrated as a quadtree structure shown in [Figure 22.7](#). As with H.264/AVC case, the references of inter prediction comes from the already decoded frames. As such, inter-prediction makes use of a list of reference frames, which are the predictive frame (P-frame) and the bi-predictive frame (B-Frame). The operation of ME is to find the best match from reference frames for the blocks in the frame that is currently being encoded. This match may be represented with a set of motion vectors, at a special case if the motion vectors are zero, which means there is no motion and encoded block is located with the same location in the reference frame. The predictive residuals, which are the difference between the original block of pixels, will be further processed with transform and quantization and the motion vector data will be as the side information included together in the encoded bitstream with predictive residues. As we mentioned previously, the CU may be too big as a unit of ME since it may contain small moving objects within. In other words, a single motion vector may not be the best way to represent the prediction of the CU in terms of RD cost. For this reason, CUs are further split into PUs for more accurately reflecting the different motion vectors within the single block of pixels. For the process of ME, theoretically search for all the possible blocks in the search window; the full-search algorithm can reach the best match in terms of minimum distortion and low cost of number of bits to represent the encoded region. But the full search is too complicated and expensive for real-time applications, so many fast ME algorithms are developed to compromise between complexity and performance [HM-9.0.1] (Li 2014, Purnachand et al. 2012). It should be noted that in H.264/AVC the ME is always performed in the way of symmetric partitioning, but for HEVC/H.265 both symmetric and asymmetric partitioning can be used. The asymmetrical PUs are also referred to as asymmetrical motion prediction (AMP). This is especially efficient when only a small part within the region shows a different motion vector. There are four AMP PU

**FIGURE 22.10**

HEVC inter-picture PU modes (a) Symmetric and (b) Asymmetric. (From Bross, B. et al., *Inter-Picture Prediction in High Efficiency Video Coding (HEVC)*, 113–140, Springer, 2014.)

modes— $2N \times nU$, $2N \times nD$, $nL \times 2N$, and $nR \times 2N$ —as shown in Figure 22.10. For 8×8 CU blocks, only the $N \times N$ PU configuration is used. It is to be noted that the smallest-size CUs do not check for the AMP PU modes. They only adopt the $2N \times 2N$, $N \times 2N$, $2N \times N$, and $N \times N$ PU configurations (Bross et al. 2014). Once the PU configuration for each CU has been determined in the quad tree, a comparison is performed in a bottom-up way to identify whether the parent CU is more optimized compared to the combined RD-cost of the four subblocks. If the parent CU along with the appropriate PU mode is more optimized, it is retained. Otherwise, the four subblocks, each with their independent PU configuration, are adopted.

Since sub-pixels are also used in the ME/compensation in HEVC/H.265, the interpolation process is performed on the fractional luma pixel positions. In HEVC/H.265 an eight-tap filter for one-dimensional half-pixel interpolation is used and a seven-tap filter is used for quarter-pixel interpolation. This has improved precision due to the longer interpolation filter and the elimination of the intermediate rounding error (Sullivan et al. 2012). For 4:2:0 video, the chroma pixels are interpolated with separable one-dimensional four-tap filtering to generate eighth-sample precision.

In HEVC/H.265, the advanced motion vector prediction (AMVP) and the merge mode are also adopted. In AMVP mode, several most probable candidates based on data from adjacent PBs and the reference picture are derived. The merge mode allows for the MVs to be inherited from temporally or spatially neighboring PBs. This is similar to the “skipped” and “direct” motion inference modes in H.264/AVC. But HEVC/H.265 made two improvements on these modes. First, HEVC/H.265 uses index information to select one of several available candidates. The second is that HEVC/H.265 uses information from the reference picture list and reference picture index (Sullivan et al. 2012).

At the decoder side, motion-compensation process will be performed to reconstruct the videos from the bitstream transferred from the encoder. It is a total reverse process of the encoding.

22.3.3 Transform and Quantization

HEVC/H.265 uses transform coding of the predictive residual in a similar manner as in prior standards. The residual block is partitioned into multiple square TBs, as described previously. The supported TB sizes in HEVC/H.265 are 4×4 , 8×8 , 16×16 , and 32×32 . HEVC uses two-dimensional transforms for all transform sizes. Multiple transform sizes improve compression performance, but also increase the complexity of implementation. Therefore, the core transforms in HEVC/H.265 is carefully designed.

Except using discrete cosine transform, HEVC/H.265 also specifies an alternate 4×4 integer transform based on the discrete sine transform (DST) for coding 4×4 Intra blocks (Sullivan et al. 2012).

In HEVC/H.265, the core transform uses two-dimensional transforms, which are computed by applying 1-D transforms in the horizontal and vertical directions. The elements in the core transform matrices are derived by approximating scaled DCT basis functions. Considering several facts such as limiting the necessary dynamic range for transform computation and maximizing the precision and closeness to orthogonality, the core transform matrix is designed as integer values. For simplicity, only one integer matrix for the 32×32 transform is specified as in [h265], and subsampled versions are used for other sizes. The way to derive the small transform cores is shown in [Figure 22.11](#). For example, the matrices for the length-8 and length-4 transforms can be derived by using the first eight entries of rows 0, 2, 4, ..., and using the first four entries of rows 0, 4, 8, ..., respectively. In such a way, the values of the entries in the matrix have key symmetry properties that enable fast partially factored implementations with far fewer mathematical operations than an ordinary matrix multiplication. Also, in this way the larger transforms can be constructed by using the smaller transforms as building blocks.

As it is mentioned at the beginning of this section, HEVC/H.265 uses an alternative 4×4 DST transform for 4×4 luma residual blocks. The basis function of the DST is designed to better fit the statistical property of residual values, which tend to increase as the distance from the boundary pixels that are used as prediction reference becomes larger. Compared with 4×4 DCT transform the complexity of the 4×4 DST transform is not increased to much, and it provides approximately 1% bit-rate reduction in the intra predictive coding.

For quantization, as with H.264/AVC, the HEVC/H.265 uses essentially the same uniform reconstruction quantization (URQ) scheme of quantization control with quantization scaling matrices supported for the various TB sizes. The range of the quantization parameter (QP) values is defined from 0 to 51, and an increase by 6 doubles the quantization step size such that the mapping of QP values to step sizes is approximately logarithmic.

22.3.4 Loop Filters

In HEVC/H.265, two loop filters, the deblocking filter (DBF) and the sample adaptive offset (SAO) filter, have been specified [h265]. These filters are applied in the inter prediction loop. This means only the reference pictures stored in the decoded picture buffer are filtered with these filters. The filters are performed sequentially with DBF applied first and SAO applied afterwards.

The DBF in HEVC/H.265 is applied to all pixels adjacent to a PU or TU boundary but not for picture or slice boundary. In some cases of inter prediction CBs, the PU boundaries are not always aligned with TU boundaries; therefore, both PU and TU boundaries should be filtered by DBF. The DBF in HEVC/H.265 is designed to favor parallel processing. For this purpose, the DBF is only applied to 8×8 blocks instead of 4×4 blocks in H.264/AVC in such way that DBF no longer causes cascading interaction between nearby filtering operations. Also, The DBF is first applied to horizontal edges in the picture and then to the vertical edges in the picture.

Similar to the H.264/AVC, the strength of the DBF of HEVC/H.265 is also controlled by the values of several syntax elements. The difference is that only three strengths

| | | | | | | | | | | | | | | | | | | | | | | | |
|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|----|----|----|----|----|----|----|----|
| 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 |
| 90 | 90 | 88 | 85 | 82 | 78 | 73 | 67 | 61 | 54 | 46 | 38 | 31 | 22 | 13 | 4 | | | | | | | | |
| 90 | 87 | 80 | 70 | 57 | 43 | 25 | 9 | -9 | -25 | -43 | -57 | -70 | -80 | -87 | -90 | | | | | | | | |
| 90 | 82 | 67 | 46 | 22 | -4 | -31 | -54 | -73 | -85 | -90 | -88 | -78 | -61 | -38 | -13 | | | | | | | | |
| 89 | 75 | 50 | 18 | -18 | -50 | -75 | -89 | -89 | -75 | -50 | -18 | 18 | 50 | 75 | 89 | | | | | | | | |
| 88 | 67 | 31 | -13 | -54 | -82 | -90 | -78 | -46 | -4 | 38 | 73 | 90 | 85 | 61 | 22 | | | | | | | | |
| 87 | 57 | 9 | -43 | -80 | -90 | -70 | -25 | 25 | 70 | 90 | 80 | 43 | -9 | -57 | -87 | | | | | | | | |
| 85 | 46 | -13 | -67 | -90 | -73 | -22 | 38 | 82 | 88 | 54 | -4 | -61 | -90 | -78 | -31 | | | | | | | | |
| 83 | 36 | -36 | -83 | -83 | -36 | 36 | 83 | 83 | 36 | -36 | -83 | -83 | -36 | 36 | 83 | | | | | | | | |
| 82 | 22 | -54 | -90 | -61 | 13 | 78 | 85 | 31 | -46 | -90 | -67 | 4 | 73 | 88 | 38 | | | | | | | | |
| 80 | 9 | -70 | -87 | -25 | 57 | 90 | 43 | -43 | -90 | -57 | 25 | 87 | 70 | -9 | -80 | | | | | | | | |
| 78 | -4 | -82 | -73 | 13 | 85 | 67 | -22 | -88 | -61 | 31 | 90 | 54 | -38 | -90 | -46 | | | | | | | | |
| 75 | -18 | -89 | -50 | 50 | 89 | 18 | -75 | -75 | 18 | 89 | 50 | -50 | -89 | -18 | 75 | | | | | | | | |
| 73 | -31 | -90 | -22 | 78 | 67 | -38 | -90 | -13 | 82 | 61 | -46 | -88 | -4 | 85 | 54 | | | | | | | | |
| 70 | -43 | -87 | 9 | 90 | 25 | -80 | -57 | 57 | 80 | -25 | -90 | -9 | 87 | 43 | -70 | | | | | | | | |
| 67 | -54 | -78 | 38 | 85 | -22 | -90 | 4 | 90 | 13 | -88 | -31 | 82 | 46 | -73 | -61 | | | | | | | | |
| 64 | -64 | -64 | 64 | 64 | -64 | -64 | 64 | 64 | -64 | -64 | 64 | 64 | -64 | -64 | 64 | | | | | | | | |
| 61 | -73 | -46 | 82 | 31 | -88 | -13 | 90 | -4 | -90 | 22 | 85 | -38 | -78 | 54 | 67 | | | | | | | | |
| 57 | -80 | -25 | 90 | -9 | -87 | 43 | 70 | -70 | -43 | 87 | 9 | -90 | 25 | 80 | -57 | | | | | | | | |
| 54 | -85 | -4 | 88 | -46 | -61 | 82 | 13 | -90 | 38 | 67 | -78 | -22 | 90 | -31 | -73 | | | | | | | | |
| 50 | -89 | 18 | 75 | -75 | -18 | 89 | -50 | -50 | 89 | -18 | -75 | 75 | 18 | -89 | 50 | | | | | | | | |
| 46 | -90 | 38 | 54 | -90 | 31 | 61 | -88 | 22 | 67 | -85 | 13 | 73 | -82 | 4 | 78 | | | | | | | | |
| 43 | -90 | 57 | 25 | -87 | 70 | 9 | -80 | 80 | -9 | -70 | 87 | -25 | -57 | 90 | -43 | | | | | | | | |
| 38 | -88 | 73 | -4 | -67 | 90 | -46 | -31 | 85 | -78 | 13 | 61 | -90 | 54 | 22 | -82 | | | | | | | | |
| 36 | -83 | 83 | -36 | -36 | 83 | -83 | 36 | 36 | -83 | 83 | -36 | -36 | 83 | -83 | 36 | | | | | | | | |
| 31 | -78 | 90 | -61 | 4 | 54 | -88 | 82 | -38 | -22 | 73 | -90 | 67 | -13 | -46 | 85 | | | | | | | | |
| 25 | -70 | 90 | -80 | 43 | 9 | -57 | 87 | -87 | 57 | -9 | -43 | 80 | -90 | 70 | -25 | | | | | | | | |
| 22 | -61 | 85 | -90 | 73 | -38 | -4 | 46 | -78 | 90 | -82 | 54 | -13 | -31 | 67 | -88 | | | | | | | | |
| 18 | -50 | 75 | -89 | 89 | -75 | 50 | -18 | -18 | 50 | -75 | 89 | -89 | 75 | -50 | 18 | | | | | | | | |
| 13 | -38 | 61 | -78 | 88 | -90 | 85 | -73 | 54 | -31 | 4 | 22 | -46 | 67 | -82 | 90 | | | | | | | | |
| 9 | -25 | 43 | -57 | 70 | -80 | 87 | -90 | 90 | -87 | 80 | -70 | 57 | -43 | 25 | -9 | | | | | | | | |
| 4 | -13 | 22 | -31 | 38 | -46 | 54 | -61 | 67 | -73 | 78 | -82 | 85 | -88 | 90 | -90 | | | | | | | | |

| | | | | | | | | | | | | | | | | | | | | | | | | |
|-----------------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|--|--|--|
| Q | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | | | | | |
| B' | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 6 | 7 | 8 | | | | |
| t_{c'} | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | | | |
| Q | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | | | | | |
| B' | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 20 | 22 | 24 | 26 | 28 | 30 | 32 | 34 | 36 | | | | | |
| t_{c'} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 3 | 3 | 3 | 3 | 4 | 4 | 4 | 4 | | | | | |
| Q | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | | | | | | | | |
| B' | 38 | 40 | 42 | 44 | 46 | 48 | 50 | 52 | 54 | 56 | 58 | 60 | 62 | 64 | - | - | | | | | | | | |
| t_{c'} | 5 | 5 | 6 | 6 | 7 | 8 | 9 | 10 | 11 | 13 | 14 | 16 | 18 | 20 | 22 | 24 | | | | | | | | |

FIGURE 22.11

4-point (green shading), 8-point (pink shading) and 16-point (yellow shading) forward transform matrices are embedded in the 32-point transform matrix (Budagavi 2013).

are used in HEVC/H.265 rather than five in H.264/AVC. The three-strength value of 0 (no deblocking), 1 (weak deblocking), and 2 (strong deblocking) are used according to the following rules. The strength value 2 is assigned when one of the two neighboring 8×8 blocks is an intra PB. Otherwise, the strength value 1 is assigned if any of the following conditions is satisfied:

- At least one of two neighboring 8×8 blocks has nonzero transform coefficient.
- The reference indices of two neighboring blocks are not equal.
- The difference between a motion vector component of two neighboring blocks is greater than or equal to one integer sample.

If none of the above conditions is met, the strength value 0 is used, which means that the deblocking process is not applied.

According to the filter strength and the average QPs of two neighboring blocks, two thresholds, t_c and β , are determined from predefined [Table 22.1](#).

For luma pixels, one of three cases, no filtering, strong filtering, and weak filtering, is selected based on threshold value β . The decision of filtering is shared across four luma rows or columns using the first and the last rows or columns to reduce the computational complexity. For chroma pixels, there are only two cases, no filtering and normal filtering.

The SAO filter is applied after the DBF and is designed to increase picture quality, reduce banding artifacts, and reduce ringing artifacts. The SAO filter is a non-linear operation. For each CTB, the SAO filter can be classified to edge offset and band offset. There are four types of edge offset according to edge directions (0, 90, 135, 45 degrees) as shown on the diagram below, respectively ([Figure 22.12](#)).

TABLE 22.1

Relationship Between QP and Two Threshold Values

| QP | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
|----------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| β' | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 6 | 7 | 8 |
| t_c' | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| Q | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 |
| β' | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 20 | 22 | 24 | 26 | 28 | 30 | 32 | 34 | 36 |
| t_c' | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 3 | 3 | 3 | 3 | 4 | 4 | 4 | |
| Q | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | | | |
| β' | 38 | 40 | 42 | 44 | 46 | 48 | 50 | 52 | 54 | 56 | 58 | 60 | 62 | 64 | — | — | | | |
| t_c' | 5 | 5 | 6 | 6 | 7 | 8 | 9 | 10 | 11 | 13 | 14 | 16 | 18 | 20 | 22 | 24 | | | |

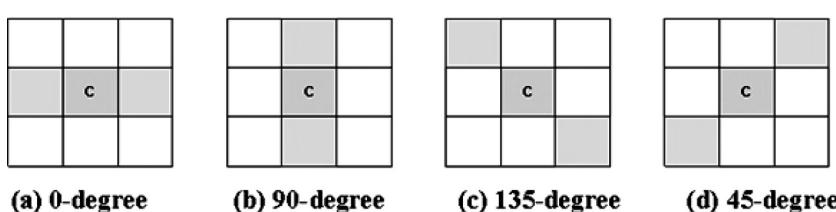


FIGURE 22.12

Type of edge offset. (From Mody 2013.)

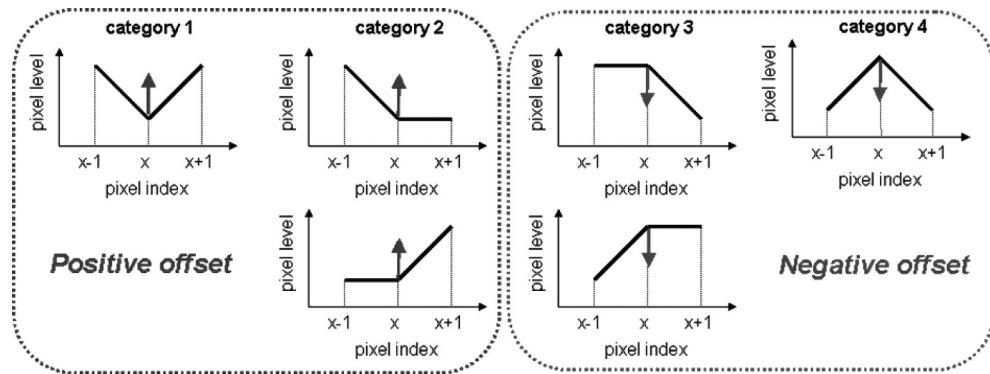


FIGURE 22.13

Categories of edge/index and pixel mapping. (From Mody 2013.)

There are four offsets corresponding to four edge shapes (i.e., categories/edge index) for the selected direction. The edge index is referred to as SAO-subtype for EO. The figure below shows the different types of categories.

The edge offset mode is operated by comparing the value of a sample to two of its eight neighbors using one of four directional gradient patterns as shown in Figure 22.13. Based on a comparison with these two neighbors, the edges are classified into one of five categories: minimum (the sample is smaller than two neighbors), maximum (the sample is greater than two neighbors), an edge with the sample having the lower value, an edge with the sample having the higher value, or monotonic. For each of the first four categories an offset is performed.

For the band offset mode, the whole pixels range (0–255 for 8 bpp) is equally divided into 32 bands (histogram bins). There are four offsets provided for four consecutive bands from the start band. The information of start band number with four offset values is included in the bitstream. The start band position is also called as the SAO sub-type for BO. Offset value is added to each de-blocked pixel value if it belongs to the range covered by one of the four bands; otherwise, pixel value is not affected.

22.3.5 Entropy Coding

In HEVC/H.265, the context-adaptive binary arithmetic coding (CABAC) is used for entropy coding. This entropy coding is similar to the CABAC scheme in H.264/AVC, but has made several modifications to improve its throughput speed, especially for parallel-processing architectures and the coding performance as well as to reduce its context memory requirements (Sze and Budagavi 2012).

The CABAC involves three main functions: binarization, context modeling, and arithmetic coding. The function of binarization is to map the syntax elements to binary symbols (bins). Context modeling is used to provide an accurate probability estimate of the bin. Based on the estimated probability, the arithmetic coding can efficiently compress the bins to bits.

It is well known that the CABAC in H.264/AVC has a problem of throughput bottleneck in the video codec implementations. In order to improve the throughput of CABAC in HEVC/H.265, several techniques have been adopted. It may cause coding performance loss when we try to increase the capability of throughput. Therefore, one criterion for selecting these techniques is to check if the techniques cause minimal coding loss. These techniques include: reduce context-coded bins, group bypass-coded bins, group bins with the same

context, reduce context-selection dependencies, reduce total number of bins, reduce parsing dependencies, and reduce the memory requirements. These technologies have been proposed in the JCTVC meetings, and you can find the technical detail from the meeting documents (Sze and Budagavi 2012).

22.3.6 Parallel Processing Tools

In HEVC/H.265, several tools have been adopted to support parallel processing. These tools include slices, tiles, and wavefront parallel processing (WPP) (Sullivan et al. 2012).

As with H.264/AVC, a frame is divided into slices that are groups of CTUs in scan order separated by start code. Slices are used for resynchronization when the data loss happened. There are two types of slices: dependent and nondependent. Dependencies of dependent slice include the following:

- Slice header dependency: short slice header is used where the missing elements are copied from the preceding normal slice
- Context model dependency: CABAC context models are not initialized to defaults at the beginning of a dependent slice
- Spatial prediction dependency: no breaking intra and motion vector prediction

Each dependent slice must be followed by a non-dependent slice. The picture always starts with a normal slice followed by zero or more dependent slices.

Slices are effective for network packetization for MTU size matching and favorite for low-delay applications and parallel processing. The problems of slices include the penalty on coding performance due to the breaking of dependencies at the slice boundaries, in addition to the overhead added by the slice header.

Tile is a new tool adopted by HEVC/H.265 that divides a frame into independent, rectangular regions. It is used to support parallel processing. Tiles is different with original concept of slices. Tiles are always rectangular, which contain a number of CTUs according to their width and the height. Slices simply contain a number of CTUs that are located in raster scan order. The difference can be seen from [Figure 22.14](#).

From [Figure 22.14](#), it can be seen that slices and tiles can be arranged at the same time so that a slice can contain tiles or a tile can contain slices. A special case is that slices and tiles contain the same number of CTUs. The common feature of tiles and slices is that both do not allow prediction across the boundaries or entropy coding dependencies. Only the DBF can be optionally across tiles in order to reduce the visual artifacts. Both tiles and slices are coded independently. Therefore, tiles and slices can be used as a tool to support parallel processing (Bross et al. 2012, Misra and Segall 2011). If tiles are used, the size must be at least 64 pixels high and 256 pixels wide with a limit on the number of tiles allowed.

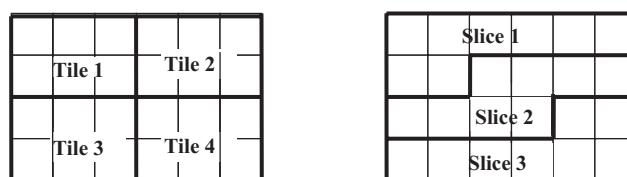


FIGURE 22.14
Tiles and slices.

WPP is a new tool to support parallel processing in HEVC/H.265. In WPP a picture is divided into rows of CTUs in which the first row is processed in an ordinary way. The second row can be delayed until two first CTUs in the first row completed. The third row can be processed after first CTUs in the second row have been made. Each additional row requires that decisions be made in the previous row. The context models of the entropy coder in each row are inherited from those in the proceeding row with a small fixed lag. Actually, the context models are inherited from the second CTU of the previous row. WPP has the entropy encoder use information from the preceding row of CTUs and allows for a method of parallel processing that may allow for better compression than tiles.

22.4 HEVC/H.265 Profiles and Range Extensions (Sullivan et al. 2013)

In this section, we would like to give brief description about the profiles, tiers, and levels of HEVC/H.265 (Wiki 2017). Profiles, tiers, and levels specify conformance restrictions on the bitstreams and hence specify the capabilities needed in the decoders to reconstruct the video from the bitstreams. Profiles, tiers, and levels may also be used to implement the standard in an interoperable way across various applications with similar requirements.

A profile defines a set of coding tools or algorithms, which are used in generating a compliant bitstream with this profile. Each profile specifies a subset of algorithmic features and limits that shall be supported by all decoders conforming to that profile. If a decoder is claimed to conform a specific profile, it must support all tools and algorithms in that profile.

A level places constraints on certain key parameters of the bitstream, corresponding to decoder processing load and memory capabilities. Level restrictions are always determined in terms of the extreme values such as maximum sample rate, maximum picture bit rate, minimum compression ratio, and capacities of the decoder picture buffer (DPB) and the coded picture buffer (CPB), which holds compressed data prior to its decoding for data flow management purposes. However, in some cases, certain applications may only differ in terms of maximum bit rate and CPB capabilities. To address this issue, the concept of tiers has been proposed. Two tiers are specified for some levels, a main tier for most applications and a high tier for use in the most demanding applications.

22.4.1 Version 1 of HEVC/H.265

Several versions have been developed in HEVC/H.265. Version 1 is the first approved version of HEVC/H.265, which was published on April 12, 2013. Version 1 contains several profiles, Main, Main 10, and Main Still Pictures.

The Main profile allows for a bit depth of 8-bits per sample with 4:2:0 chroma sampling, which is the most common type of video used in consumer devices (Sullivan et al. 2012) [h.265] (Fröjd 2013).

The Main 10 profile allows for a bit depth of 8-bits to 10-bits per sample with 4:2:0 chroma sampling. HEVC decoders that conform to the Main 10 profile must be capable of decoding bitstreams made with both Main and Main 10 [h.265] 8-bits per sample allows for 256 shades per primary color (a total of 16.78 million colors) while 10-bits per sample allows for 1024 shades per

primary color (a total of 1.07 billion colors). A higher bit depth allows for a smoother transition of color, which resolves the problem known as color banding (Furgusson 2013, Forrest 2013). The Main 10 profile allows for improved video quality since it can support video with a higher bit depth than what is supported by the Main profile (Duenas and Malamy 2012). Additionally, in the Main 10 profile 8-bit video can be coded with a higher bit.

The Main Still Picture profile allows for a single still picture to be encoded with the same constraints as the Main profile. As a subset of the Main profile the Main Still Picture profile allows for a bit depth of 8-bits per sample with 4:2:0 chroma sampling (Sullivan et al. 2012) [h.265] (Fröjd 2013). An objective performance comparison was done in April 2012, in which HEVC reduced the average bit rate for images by 56% compared to JPEG (Nguyen and Marpe 2012). A PSNR-based performance comparison for still image compression has also shown the big improvement compared to JPEG (Hanhart et al. 2013).

22.4.2 Version 2 of HEVC/H.265

Version 2 of HEVC/H.265 has been approved on April 13, 2013, The Version 2 of HEVC contains 21 range extension profiles, two scalable extensions profiles, and one multi-view profile: Monochrome, Monochrome 12, Monochrome 16, Main 12, Main 4:2:2 10, Main 4:2:2 12, Main 4:4:4, Main 4:4:4 10, Main 4:4:4 12, Monochrome 12 Intra, Monochrome 16 Intra, Main 12 Intra, Main 4:2:2 10 Intra, Main 4:2:2 12 Intra, Main 4:4:4 Intra, Main 4:4:4 10 Intra, Main 4:4:4 12 Intra, Main 4:4:4 16 Intra, Main 4:4:4 Still Picture, Main 4:4:4 16 Still Picture, High Throughput 4:4:4 16 Intra, Scalable Main, Scalable Main 10, and Multiview Main [h265] (Sharman et al. 2014). Also, all of the inter frame range extensions profiles have an Intra profile [h265].

The **Monochrome** profile allows for a bit depth of 8-bits per sample with support for 4:0:0 chroma sampling [h265]. The **Monochrome 12** profile supports a bit depth of 8-bits to 12-bits per sample with support for 4:0:0 chroma sampling [h265]. The Monochrome 16 profile allows for a bit depth of 8-bits to 16-bits per sample with support for 4:0:0 chroma sampling. HEVC decoders that conform to the Monochrome 16 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Monochrome 12, and Monochrome 16 [h265].

The **Main 12** profile allows for a bit depth of 8-bits to 12-bits per sample with support for 4:0:0 and 4:2:0 chroma sampling. HEVC decoders that conform to the Main 12 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Monochrome 12, Main, Main 10, and Main 12 [h265].

The **Main 4:2:2 10** profile allows for a bit depth of 8-bits to 10-bits per sample with support for 4:0:0, 4:2:0, and 4:2:2 chroma sampling. HEVC decoders that conform to the Main 4:2:2 10 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 10, and Main 4:2:2 10 [h265].

The **Main 4:2:2 12** profile allows for a bit depth of 8-bits to 12-bits per sample with support for 4:0:0, 4:2:0, and 4:2:2 chroma sampling. HEVC decoders that conform to the Main 4:2:2 12 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Monochrome 12, Main, Main 10, Main 12, Main 4:2:2 10, and Main 4:2:2 12 [h265].

The **Main 4:4:4** profile allows for a bit depth of 8-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. HEVC decoders that conform to the Main 4:4:4 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, and Main 4:4:4 [h265].

The **Main 4:4:4 10** profile allows for a bit depth of 8-bits to 10-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. HEVC decoders that conform to the Main 4:4:4 10 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 10, Main 4:2:2 10, Main 4:4:4, and Main 4:4:4 10 [h265].

The **Main 4:4:4 12** profile allows for a bit depth of 8-bits to 12-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. HEVC decoders that conform to the Main 4:4:4 12 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 10, Main 12, Main 4:2:2 10, Main 4:2:2 12, Main 4:4:4, Main 4:4:4 10, Main 4:4:4 12, and Monochrome 12 [h265].

The **Main 4:4:4 16 Intra** profile allows for a bit depth of 8-bits to 16-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. HEVC decoders that conform to the Main 4:4:4 16 Intra profile must be capable of decoding bitstreams made with the following profiles: Monochrome Intra, Monochrome 12 Intra, Monochrome 16 Intra, Main Intra, Main 10 Intra, Main 12 Intra, Main 4:2:2 10 Intra, Main 4:2:2 12 Intra, Main 4:4:4 Intra, Main 4:4:4 10 Intra, and Main 4:4:4 12 Intra [h265].

The **High Throughput 4:4:4 16 Intra** profile allows for a bit depth of 8-bits to 16-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling [h265]. The High Throughput 4:4:4 16 Intra profile has an HbrFactor 12 times higher than other HEVC profiles, allowing it to have a maximum bit rate 12 times higher than the Main 4:4:4 16 Intra profile [h265] (Sharman et al. 2014). The High Throughput 4:4:4 16 Intra profile is designed for high-end professional content creation and decoders for this profile are not required to support other profiles (Sharman et al. 2014).

The **Main 4:4:4 Still Picture** profile allows for a single still picture to be encoded with the same constraints as the Main 4:4:4 profile. As a subset of the Main 4:4:4 profile the Main 4:4:4 Still Picture profile allows for a bit depth of 8-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling [h265].

The **Main 4:4:4 16 Still Picture** profile allows for a single still picture to be encoded with the same constraints as the Main 4:4:4 16 Intra profile. As a subset of the Main 4:4:4 16 Intra profile the Main 4:4:4 16 Still Picture profile allows for a bit depth of 8-bits to 16-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling [h265].

The **Scalable Main** profile allows for a base layer that conforms to the Main profile of HEVC [h265].

The **Scalable Main 10** profile allows for a base layer that conforms to the Main 10 profile of HEVC [h265].

The **Multiview Main** profile allows for a base layer that conforms to the Main profile of HEVC [h265].

Some features of some profiles in version 1 and 2 are summarized in [Table 22.2](#).

TABLE 22.2 Feature Support in Some of the Video Profiles [h265]

22.4.3 Versions 3 and 4 of HEVC/H.265

Version 3 of HEVC/H.265 was approved on April 29, 2015. Version 3 of HEVC/H.265 contains one 3D profile: 3D Main. In December 22, 2016, Version 4 of HEVC/H.265 was approved and contains seven screen content coding extensions profiles, three high-throughput extensions profiles, and four scalable extensions profiles: Screen-Extended Main, Screen-Extended Main 10, Screen-Extended Main 4:4:4, Screen-Extended Main 4:4:4 10, Screen-Extended High Throughput 4:4:4, Screen-Extended High Throughput 4:4:4 10, Screen-Extended High Throughput 4:4:4 14, High Throughput 4:4:4, High Throughput 4:4:4 10, High Throughput 4:4:4 14, Scalable Monochrome, Scalable Monochrome 12, Scalable Monochrome 16, and Scalable Main 4:4:4.

The **3D Main profile** allows for a base layer that conforms to the Main profile of HEVC [h265].

The **Screen-Extended Main** profile allows for a bit depth of 8-bits per sample with support for 4:0:0 and 4:2:0 chroma sampling. HEVC decoders that conform to the Screen-Extended Main profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, and Screen-Extended Main. The Screen-Extended Main 10 profile allows for a bit depth of 8-bits to 10-bits per sample with support for 4:0:0 and 4:2:0 chroma sampling. HEVC decoders that conform to the Screen-Extended Main 10 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 10, Screen-Extended Main, and Screen-Extended Main 10 (Joshi 2016).

The **Screen-Extended Main 4:4:4** profile allows for a bit depth of 8-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. HEVC decoders that conform to the Screen-Extended Main 4:4:4 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 4:4:4, Screen-Extended Main, and Screen-Extended Main 4:4:4 (Joshi 2016).

The **Screen-Extended Main 4:4:4 10** profile allows for a bit depth of 8-bits to 10-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. HEVC decoders that conform to the Screen-Extended Main 4:4:4 10 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 4:2:2 10, Main 4:4:4, Main 4:4:4 10, Screen-Extended Main, Screen-Extended Main 10, Screen-Extended Main 4:4:4, and Screen-Extended Main 4:4:4 10 (Joshi 2016).

The **Screen-Extended High Throughput 4:4:4** profile allows for a bit depth of 8-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. The Screen-Extended High Throughput 4:4:4 profile has an HbrFactor six times higher than most inter frame HEVC profiles allowing it to have a maximum bit rate six times higher than the Main 4:4:4 profile. HEVC decoders that conform to the Screen-Extended High Throughput 4:4:4 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 4:4:4, Screen-Extended Main, Screen-Extended Main 4:4:4, Screen-Extended High Throughput 4:4:4, and High Throughput 4:4:4 (Joshi 2016).

The **Screen-Extended High Throughput 4:4:4 10** profile allows for a bit depth of 8-bits to 10-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. The Screen-Extended High Throughput 4:4:4 10 profile has an HbrFactor six times higher than most inter frame HEVC profiles allowing it to have a maximum bit rate six times higher than the Main 4:4:4 10 profile. HEVC decoders that conform to the Screen-Extended High Throughput 4:4:4 10 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 10, Main 4:2:2 10, Main 4:4:4, Main 4:4:4 10, Screen-Extended Main, Screen-Extended Main 10, Screen-Extended Main 4:4:4, Screen-Extended Main 4:4:4 10, Screen-Extended High Throughput 4:4:4, Screen-Extended High Throughput 4:4:4 10, High Throughput 4:4:4, and High Throughput 4:4:4 (Joshi 2016).

The **Screen-Extended High Throughput 4:4:4 14** profile allows for a bit depth of 8-bits to 14-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. The Screen-Extended High Throughput 4:4:4 14 profile has an HbrFactor six times higher than most inter frame HEVC profiles. HEVC decoders that conform to the Screen-Extended High Throughput 4:4:4 14 profile must be capable of decoding bitstreams made with the following profiles: Monochrome, Main, Main 10, Main 4:2:2 10, Main 4:4:4, Main 4:4:4 10, Screen-Extended Main, Screen-Extended Main 10, Screen-Extended Main 4:4:4, Screen-Extended Main 4:4:4 10, Screen-Extended High Throughput 4:4:4, Screen-Extended High Throughput 4:4:4 10, Screen-Extended High Throughput 4:4:4 14, High Throughput 4:4:4, High Throughput 4:4:4 10, and High Throughput 4:4:4 14 (Joshi 2016).

The **High Throughput 4:4:4** profile allows for a bit depth of 8-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. The High Throughput 4:4:4 profile has an HbrFactor six times higher than most inter frame HEVC profiles allowing it to have a maximum bit rate six times higher than the Main 4:4:4 profile. HEVC decoders that conform to the High Throughput 4:4:4 profile must be capable of decoding bitstreams made with the following profiles: High Throughput 4:4:4 (Joshi 2016).

The **High Throughput 4:4:4 10** profile allows for a bit depth of 8-bits to 10-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. The High Throughput 4:4:4 10 profile has an HbrFactor six times higher than most inter frame HEVC profiles allowing it to have a maximum bit rate six times higher than the Main 4:4:4 10 profile. HEVC decoders that conform to the High Throughput 4:4:4 10 profile must be capable of decoding bitstreams made with the following profiles: High Throughput 4:4:4 and High Throughput 4:4:4.

The **High Throughput 4:4:4 14** profile allows for a bit depth of 8-bits to 14-bits per sample with support for 4:0:0, 4:2:0, 4:2:2, and 4:4:4 chroma sampling. The High Throughput 4:4:4 14 profile has an HbrFactor six times higher than most inter frame HEVC profiles. HEVC decoders that conform to the High Throughput 4:4:4 14 profile must be capable of decoding bitstreams made with the following profiles: High Throughput 4:4:4, High Throughput 4:4:4 10, and High Throughput 4:4:4 14 (Joshi 2016).

The **Scalable Monochrome** profile allows for a base layer that conforms to the Monochrome profile of HEVC/h.265 (Joshi 2016).

The **Scalable Monochrome 12** profile allows for a base layer that conforms to the Monochrome 12 profile of HEVC (Joshi 2016).

The **Scalable Monochrome 16** profile allows for a base layer that conforms to the Monochrome 16 profile of HEVC/h.265 (Joshi 2016).

The **Scalable Main 4:4:4** profile allows for a base layer that conforms to the Main 4:4:4 profile of HEVC/H.265 (Joshi 2016).

22.5 Performance Comparison with H.264/AVC

In this section, we would like to give a comparison between HEVC/H.265 and H.264/AVC.

22.5.1 Technical Difference Between H.264/AVC and HEVC/H.265

Before making the performance comparison, we first give a brief introduction about the technical differences between two standards (Unterweger 2012, Ohm et al. 2012). Most tools have been introduced at the previous technical description of HEVC/H.265.

From block structure, H.264/AVC uses 16×16 macroblocks, $16 \times 4 \times 4$ sub-blocks or $1 \times 16 \times 16$ block for intra blocks and 16×16 , 16×8 , 8×16 , 8×8 , and subpartitions for inter block. HEVC/H.265 uses CTBs that use 16×16 , 32×32 , and 64×64 blocks. The CTBs are subpartitioned into quadtree-like CBs. The minimum CB size is 8×8 , if it is specified the larger block size can be used. The chroma is partitioned accordingly.

In H.264/AVC the prediction and transform are static. The prediction is coupled with block partition size. Transform size is always 4×4 (or adaptively 8×8 in high profile [HP]). Intra/inter decision is made on higher level of 16×16 block. In HEVC/H.265, the prediction and transform are flexible. CBs are split into PBs, and minimum block size is 4×4 . CBs are split into TBs, and the minimum size is also 4×4 . The intra/inter decision is on CB level, and the minimum CB size is 8×8 .

For intra prediction, in H.264/AVC the number of total modes depends on the block sizes. 16 are used for 4×4 sub-blocks or 1 for 16×16 block. For 16×16 blocks, DC, plane, horizontal, or vertical predictions are used. For 8×8 blocks in HP, models for 16×16 blocks are used. Different modes are used for chroma blocks (but not for 8×8 luma). Smoothing filters are used for reference pixels for 8×8 block prediction. Additional Hadamard transform is used for 16×16 blocks. In HEVC/H.264, a total of 35 modes are used including DC planar and 33 directional predictions. Blocks sizes are from 32×32 down to 4×4 blocks. The same modes are used for chroma but no 2×2 blocks. 1/32th sample accuracy is used with bilinear interpolation. Adaptive smoothing filter is used for most reference pixels. Additional boundary value smoothing is performed.

For inter prediction, H.264/AVC uses symmetrical partitioning including 16×16 , 16×8 , 8×16 , and 8×8 . The 8×8 is further partitioned into 8×4 , 4×8 , and 4×4 . The HEVC/H.265 adaptively uses both symmetric and asymmetric partitioning as shown in [Figure 22.5](#). Both H.264/AVC and HEVC/H.265 use $\frac{1}{4}$ th accuracy for ME/

compensation, but H.265/AVC uses six-tap filter for half pixels and averaging for quarter pixels while HEVC/H.265 uses eight-tap filter for half pixels and seven-tap for quarter pixels. In H.265/AVC, the DM uses MV prediction while in HEVC/H.265 a merge mode is used that chooses one derived MV candidate based on MVs from temporal and spatial neighbors.

For transform, H.264/AVC uses 4×4 integer DCT transform for all blocks and adaptively uses 8×8 integer DCT transform in HP. In HEVC/H.265 all transforms use square block and block sizes can be 4×4 , 8×8 , 16×16 , and 32×32 . Only 4×4 intra coding could use a DST transform to make bit saving since residuals tend to increase with distance from boundary.

For DBF, H.264/AVC uses in-loop filter on the TB boundary for 4×4 grid with adaptive strength from 0–5. HEVC/H.265 uses two DBFs. The in-loop DBF are used for 8×8 grid on PB and TB boundaries with adaptive strength from 0–2. The additional filter, sample-adaptive offset (SAO) is used in HEVC/H.265. The idea is to sharpen edges and remove banding.

For tools to support parallel processing H.264/AVC uses slices, which provide independently decodable picture areas. HEVC/H.265 also uses the concept of slices but it has additional tools, tiles, and wavefront parallel processing. The differences between slices and tiles have been described previously.

For entropy coder, H.264/AVC has CAVLC and CABAC. CAVLC is easy and faster but less efficient. HEVC/H.265 has only CABAC, but it also has some new features. The CABAC of HEVC/H.265 use the same principle of multiple contexts as for H.264/AVC but fewer than in H.264/AVC. The coefficients in HEVC/H.265 are always scanned on a 4×4 block basis and its scan pattern is more dependent.

For random access, both H.264/AVC and HEVC/H.265 have IDR, I, P, and B pictures. Additionally, HEVC/H.265 has clean random access (CRA) pictures, which like IDRs, but without DPB flush. Some subsequent pictures may have to be discarded. Tagged for discard (TFD) pictures have smaller display order and the decodable leading pictures (DLPs) are allowed. Also, HEVC/H.265 has broken-link access (BLA) pictures, which are originally changed from CRA pictures and used for splice points in concatenated bit streams. BLA pictures may also be followed by TFD pictures and DLPs. In summary, HEVC/H.265 has more random-access pictures: IDRs, CRAs, and BLAs.

22.5.2 Performance Comparison Between H.264/AVC and HEVC/H.265

We have introduced the differences between HEVC/H.265 with H.264/AVC. Now we would like to see the results and how these new features added in HEVC/H.265 provide the coding performance improvements. For this purpose, the performance comparison has been conducted between the HEVC/H.265 Main Profile (MP) and H.264/AVC HP (Ohm et al. 2012). The test video sequences are used entertainment applications. The encoding uses twelve different bitrates for the nine video test sequences with a HM-8.0 HEVC encoder being used. The nine video test sequences include five of HD resolution and four of WVGA (800×480) resolution. The comparison has been made based on both PSNR and subjective quality tests. For PSNR performance comparison, the bit rate saving, example operating RD curves are provided. For subjective quality tests, bit rate saving and example curves are shown.

For PSNR performance comparison, HEVC/H.265 MP has achieved a bit rate reduction of 35.4% compared with H.264/AVC HP. HEVC/H.265 MP has also been

compared with H.264/AVC HP for subjective video quality. The subjective test was done at an earlier date than the PSNR comparison and so it used an earlier version of the HEVC/H.265 encoder that had slightly lower performance. The overall subjective bitrate reduction for HEVC/H.265 MP compared with H.264/AVC HP was 49.3% (Tan 2014).

École Polytechnique Fédérale de Lausanne (EPFL) has conducted additional subjective tests to evaluate the subjective video quality of HEVC/H.265 at resolutions higher than HDTV. The test was performed on three videos with resolutions of 3840×1744 at 24 fps, 3840×2048 at 30 fps, and 3840×2160 at 30 fps. In this test, five bitrates were used. For the encoders, HEVC/H.265 uses HM-6.1.1 and H.264/AVC uses JM-18.3. This study has shown that the average bit saving for HEVC/H.265 compared with H.264/AVC was 65% based on subjective assessment using mean opinion score values (Tan 2014).

Furthermore, in a subjective video performance comparison released in May 2014, the JCT-VC compared the HEVC/H.265 Main profile to the H.264/AVC HP. The comparison was conducted by the BBC and the University of the West of Scotland. The subjective tests used mean opinion score values. The video sequences were encoded using the HM-12.1 HEVC/H.265 encoder and the JM-18.5 H.264/AVC encoder. The results have shown that the average bit rate reduction for HEVC was 59% compared with H.264/AVC. The average bit rate reduction for HEVC was 52% for 480p, 56% for 720p, 62% for 1080p, and 64% for 4K UHD compared with H.264/AVC (Ohm et al. 2012).

| Subjective Video Performance Comparison (Ohm et al. 2012) | | | | | |
|---|---|------|-------|-------|--|
| Video coding standard | Average bit rate reduction compared with H.264/AVC HP | | | | |
| | 480p | 720p | 1080p | 2160p | |
| HEVC/H.265 | 52% | 56% | 62% | 64% | |

Also, the study was conducted to evaluate the performance of individual tools in HEVC/H.265. The results are shown in [Table 22.3](#). From the results it can be seen that the HEVC/H.265 mostly benefits from the use of larger CTU sizes.

TABLE 22.3

Performance of Individual Coding Tools

| Seq. Class | Spatial Res. | 16 × 16 CTB | Up to 8 × 8 Transform | RQT Depth =1 | TMVP Off | SAO Off | AMP Off |
|------------|--------------|-------------|-----------------------|--------------|----------|---------|---------|
| Class A | 4K | 28.2% | 12.2% | 0.8% | 2.6% | 2.4% | 0.6% |
| Class B | 1080p | 18.4% | 9.3% | 1.1% | 2.2% | 2.4% | 0.7% |
| Class C | WVGA | 8.5% | 4.2% | 1.1% | 2.4% | 1.7% | 1.1% |
| Class D | QWVGA | 4.2% | 2.4% | 1.1% | 2.7% | 0.5% | 0.9% |
| Average | | 11.0% | 5.4% | 1.0% | 2.5% | 1.6% | 0.9% |

Source: Ohm, J.R. et al. *IEEE. T. Circ. Syst. Vid.*, 22, 1669–1684, 2012.

Note: Tool performance quantified by the % coding efficiency loss incurred if the specific tool is turned off.

22.6 Summary

In this chapter, the newly developed video coding standard, HEVD/H, which is jointly developed by the JVC of MPEG and ITU-T VCEG, has been introduced. The HEVC/H.265 has reached the goal to have another bit reduction of 50% compared with previous coding standard H.264/AVC. This is a new milestone for the video coding standard. However, the study for future video coding is still going on. It can be expected that we will see another milestone again in the near future.

Exercises

- 22.1 Indicate at least three new tools that make HEVC/H.265 have better coding performance. Explain why? If it is possible, please conduct computer simulations to verify it.
 - 22.2 Describe the new feature entropy coding schemes used in HEVC/H.265 compared with H.264/AVC?
 - 22.3 Describe the principle of the DBFs of HEVC/H.265. Conduct a simulation experiment to compare the subjective quality of decoded images with and without the DBFs.
 - 22.4 What are the new tools that are different from H.264/AVC for increasing the capability of parallel processing of HEVD/H.265 video coding scheme? Give explanation.
 - 22.5 Describe the principle of the integer transform in HEVC/H.265.
 - 22.6 Describe the intra prediction algorithm used in HEVC/H.265 and conduct the performance comparison with JPEG using still picture profile of HEVC/H.265.
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23

Internet Video Coding Standard—IVC

Many video coding standards have been developed during past two decades. Most video coding standards are not royalty free and require licensing payments for many uses. In this chapter, we are going to introduce a royalty free video coding standard, Internet video coding standard (IVC), which is developed by MPEG. The main objective of IVC is to provide a royalty-free video codec that may not have high coding performance but provides an option for some applications in the industry.

23.1 Introduction

Before we introduce the MPEG IVC standard, we would like to give a background of royalty-free video codec development in the industry. On March 24, 2015, Xiph.org proposed Daala codec to the IETF as a candidate for The Internet Video Codec (NETVC) (<https://en.wikipedia.org/wiki/NETVC>). NETVC is a standardization project for a royalty-free video codec hosted by the IETF. On July 22, 2015, Cisco Systems presented “Thor” video codec to the IETF as a candidate for their NETVC video standard (NETVC IETF 93 2015). Thor is being developed by Cisco Systems and uses some Cisco elements that are also used by HEVC (Thor 2015). At the IETF there are now also other partners involved in the development of NETVC. On September 1, 2015, seven leading Internet companies—Amazon, Cisco, Google, Intel Corporation, Microsoft, Mozilla, and Netflix—announced formation of the Alliance for Open Media (AOMedia). AOMedia is a non-profit organization whose first project is to develop a new open video codec and format, Av1, as a successor to VP9 and a royalty-free alternative to HEVC/H.265 (https://en.wikipedia.org/wiki/Alliance_for_Open_Media). The Alliance’s initial focus is to develop a new royalty-free video codec that includes the following features (<http://aomedia.org/press-releases/alliance-to-deliver-next-generation-open-media-formats/>):

- Interoperable and open
- Optimized for the web
- Scalable to any modern device at any bandwidth
- Designed with a low computational footprint and optimized for hardware
- Capable of consistent, highest-quality, real-time video delivery
- Flexible for both commercial and non-commercial content, including user-generated content

The October 2015 NETVC provided basic draft requirements that support 8–10 bits per sample 4:2:0, 4:2:2 chroma subsampling, 4:4:4 YUV color formats, with features of low coding-delay capability, feasible real-time decoder/encoder software implementations,

temporal scalability, and error resilience tools. Later, it added optional draft requirements for NETVC in support of a bit depth of up to 16-bits per sample, 4:2:2 chroma subsampling, RGB video, auxiliary channel planes, high dynamic range, and parallel processing tools (Filippov 2015).

Before industry actions on the royalty-free video codec development, MPEG started its work on this issue. In response to the requirements of royalty-free codec from the industry, MPEG issued the call for proposals (CfP) for IVC (CfP 2011) in July 2011. MPEG envisions the IVC standard to be potentially used in the following Internet applications:

- Real-time communications, video chat, video conferencing
- Mobile streaming, broadcast, and communications
- Mobile devices and Internet-connected embedded devices
- Internet broadcast streaming, downloads
- Content sharing

MPEG expect to develop a baseline profile of royalty-free codec with the following requirements.

To reach the goal of royalty free, the first important consideration is the IPR issue. The IVC standard should be sufficiently different from existing approaches to avoid large swaths of patents. Also, during the standard development the process should follow the ISO/IEC Common Patent Policy and the related Guidelines. All technical contributors and the patent owners of the MPEG IVC standard must be prepared to grant a free-of-charge license to an unrestricted number of applicants on a worldwide, non-discriminatory basis and under other reasonable terms and conditions to make, use, and sell implementations of the Baseline Profile of MPEG IVC standard in accordance with the ISO/IEC Common Patent Policy.

Another important consideration is the coding performance of the MPEG IVC standard. The coding performance of the baseline profile of MPEG IVC standard should be comparable to the existing standards such as H.264/AVC. Of course, due to patent restrictions, it is hard to reach the coding performance of the recently developed video coding standard such as HEVC/H.264. Other technical requirements of the MPEG IVC standard include efficient adaptation and integration with system and delivery layers and video bitstream segmentation and packetization methods. The error resilience tools also are expected for this standard when the networks subject to burst errors and packet loss, the video data can be recovered.

Another important consideration of MPEG IVC standard is the implementation issue for interactive use on the Internet. The complexity of this standard should allow for feasible implementation of real-time encoding and decoding on generally available personal computers and mobile devices. These requirements include parallel processing, fast rate control (for encoding), scalability, and some content-specific tools.

To respond to the CfP, three royalty-free codecs have been proposed to MPEG, which are Web video coding (WVC) (Kolarov 2011), video coding for browsers (VCB) (Alvestrand et al. 2013), and IVC (Wang et al. 2012). WVC was proposed jointly by Apple, Cisco, Fraunhofer HHI, Magnum Semiconductor, Polycom, RIM, and others. The main coding methods proposed are the H.264/AVC baseline plus Hierarchical P frames. VCB is based on VP8 codec developed by Google. The IVC was proposed by several universities, consisting of Peking University, Tsinghua University, Zhejiang University, Hanyang University, Korea Aerospace University, and others. Recently, the coding performance of IVC has

outperformed both WVC and VCB, and approximately reached equal coding performance with the H.264/AVC high profile (HP) for typical operational settings, both for streaming and low-delay applications (Baroncini 2015). In June 2015, IVC was approved as ISO/IEC 14496-33 (MPEG-4 Internet Video Coding). In the following sections, we will mainly introduce the MPEG IVC standard.

23.2 Coding Structure of IVC Standard

The coding structure of MPEG IVC is similar to previous standards. It is still based on traditional hybrid transform and motion-compensation framework as shown in [Figure 23.1](#).

The input video frame is first partitioned into basic coding units that are macroblocks, as in MPEG-2. Each macroblock consists of a 16×16 luminance block and two corresponding chroma blocks for YUV 420 frame. For intra-frame coding, the macroblocks are partitioned into a quad-tree structure. An intra macroblock can be coded with 16×16 block or four 8×8 blocks, and each 8×8 block can be further divided into four 4×4 blocks according to the mode selection process in the encoder. For intermacroblock coding, the motion estimation/compensation can be performed on 16×8 , 8×16 , and 8×8 blocks (Bjontegaard 1999). The technical details of main coding tools adopted in MPEG IVC are presented briefly in the following subsections. These coding tools are mostly the same as for other video coding standards, which include intra prediction, inter prediction, adaptive transform and quantization, deblocking loop filters, and entropy coding.

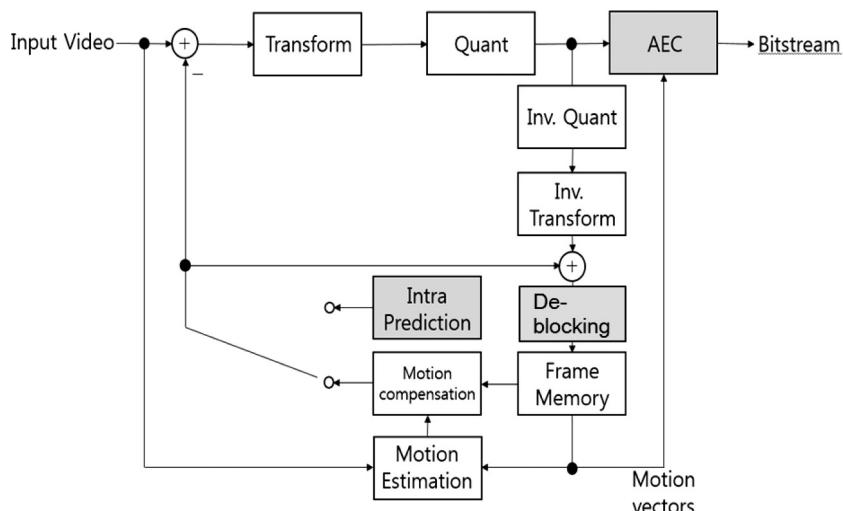


FIGURE 23.1

Block diagram of IVC codec. (From Wang, P. et al., *IEEE Signal Process. Mag.*, 33, 46–53, 2016.)

23.2.1 Adaptive Transform

In the process of IVC encoding, the partitioned blocks are first processed with intra or inter predictions. The predictive residues are then converted to the transformed coefficients with integer transforms. The integer transforms are performed on the 16×16 , 8×8 , and 4×4 , respectively. The integer transforms are derived by scaling and rounding the DCT cores of 16×16 , 8×8 , and 4×4 , respectively (Cham 1989, Chen 1989). For both intra prediction and inter prediction, the transform sizes used are matched with predictive partitioned sizes. If the 16×16 macroblock size is used, then the 16×16 transform is applied on this macroblock. If the macroblock is partitioned into 8×8 blocks, then 8×8 transform is applied on each 8×8 block within this macroblock partition. For the intra macroblock partition, the transform size is coupled with the partition size from 16×16 , 8×8 , and 4×4 . The inverse transform process is specified as:

$$RN_{ij} = (TN_{ij}^T * CN_{ij} * TN_{ij} + [1 << left_shift]) >> right_shift, \text{ for } i, j = 0 \dots N-1.$$

where RN is the $N \times N$ residual matrix, TN is the $N \times N$ transform matrix, and CN is the transformed $N \times N$ matrix. For the 16×16 , 8×8 , and 8×8 inverse transforms, the parameters of $\{N, left_shift, right_shift\}$ are set as $\{16, 13, 14\}$, $\{8, 4, 5\}$, and $\{4, 15, 16\}$, respectively.

23.2.2 Intra Prediction

As with H.264/AVC standard, for intra prediction, the decoded boundary samples of adjacent blocks are used as reference data for spatial prediction in regions where inter prediction is not performed. During the encoding process, the macroblocks for intra prediction are partitioned from 16×16 into 8×8 or 4×4 according to the mode decisions. For luma prediction, one among five modes—Intra_Vertical, Intra_Horizontal, Intra_DC, Intra_Down_left, and Intra_Down_right—will be selected. For chroma prediction, one of four modes—Intra_Chroma_DC, Intra_Chroma_Horizontal, Intra_Chroma_Vertical, and Intra_Chroma_Plane—will be selected for each 8×8 chroma block.

23.2.3 Inter Prediction

For inter prediction, there are five coding modes that can be selected; these include skip mode, forward prediction, backward prediction, multiple-hypothesis, and symmetrical modes. For each inter macroblock partition, approximately two to four modes among the five modes are available to be selected depending on the current picture coding type and partition size, as shown in [Table 23.1](#).

The five coding modes in the inter prediction are defined as follows.

The skip mode just keeps its mode type information in the bit-stream and skips all syntax elements. If skip mode is selected to code the current macroblock partition, both the motion vector difference and prediction residuals are set to 0s.

For the forward prediction mode only one reference macroblock in the forward reference pictures is used to predict the current macroblock. The resulting motion vector differences and the prediction residuals are transmitted in bit-stream.

From its name, we know that in the backward prediction mode, only one block in its backward reference picture is used to predict the current macroblock partition. The information added to bit-stream includes motion vector difference and the inter prediction residuals.

TABLE 23.1

Available Inter Prediction Modes for Each Type of Macroblock Partition

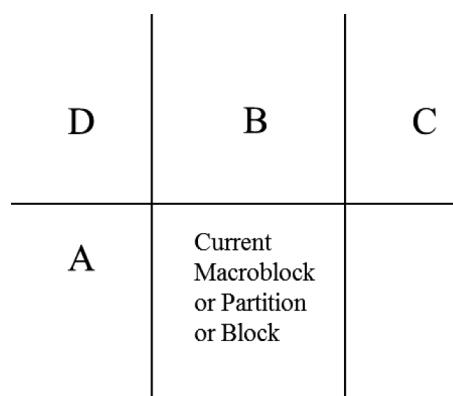
| MBPart | P_16 × 16 | P_16 × 8 | P_8 × 16 | P_8 × 8 | B_Skip | B_16 × 16 | B_16 × 8 | B_8 × 16 | B_8 × 8 |
|---------------------|-----------|----------|----------|---------|--------|-----------|----------|----------|---------|
| Mode | ○ | | | | ○ | ○ | | | ○ |
| Skip | ○ | | | | | | | | |
| Forward prediction | ○ | ○ | ○ | ○ | | ○ | ○ | ○ | ○ |
| Backward prediction | | | | | | ○ | ○ | ○ | ○ |
| Multiple-hypothesis | ○ | ○ | ○ | ○ | | | | | |
| Symmetrical | | | | | | ○ | ○ | ○ | ○ |

The fourth mode is the multiple-hypothesis prediction mode (Sullivan 1993). This mode combines two forward predictions to get the final inter prediction for the macroblock partition. In this mode, the motion vector of the first prediction is obtained by the motion vector estimation, and the motion vector of the second prediction is derived with forward motion estimation. The motion vector difference of the second predictor and the inter prediction residuals are transmitted in bit-stream.

The last mode is the symmetrical mode. This mode combines one forward prediction and one backward prediction to get the final inter prediction for the macroblock partition. The motion vector of the forward prediction is derived from forward motion estimation while the backward motion vector is derived based on the forward motion vector, the distance between the forward reference picture and the current picture, and the distance between the backward reference picture and the current picture. Finally, the motion vector difference of the forward prediction and the inter prediction residuals are contained in the bit-stream.

23.2.4 Motion Vector Prediction

In order to reduce the cost of transmitting the motion vectors, the motion vectors of current macroblock E can be predicted from its four neighboring macroblock partitions of left (A), above (B), left-above (D), and right-above (C), as shown in Figure 23.2.

**FIGURE 23.2**

Determination of neighboring macroblock, blocks, and partitions (From Wang, P. et al., *IEEE Signal Process. Mag.*, 33, 46–53, 2016.)

If one macroblock is intra coded or has not been reconstructed, the motion vectors of these macroblocks are unavailable and will be set as zero vectors. When the motion vectors of all four reference blocks are unavailable, the motion vectors of the current macroblock E are set to zero; when only one motion vectors of four reference macroblock partition are available, the prediction of the current macroblock E are set as that available motion vectors. If motion vectors in C are unavailable, then they are replaced with ones in D. The process of prediction for macroblock E with motion vectors in A, B, and C follows the following process. First, the signs of each horizontal component of motion vectors in A, B, and C are compared; if the sign of one motion vector is different from the other two, this motion vector will be excluded from motion vector prediction process. The prediction of horizontal component takes the averaging value of the horizontal component from the other two motion vectors. Otherwise, the Euler distance of the horizontal component of each pair of neighboring motion vectors are calculated, and the motion vector pair with the smallest Euler distance will be selected; then, the prediction of horizontal component is the averaging of the horizontal component of the selected motion vector pair. The vertical component of E is predicted in the same way as the horizontal component.

23.2.5 Sub-pel Interpolation

As with H.264/AVC, a quarter-pel motion compensation is used for luma components and eighth-pel is used for chroma components. Two-dimensional separable Lanczos filters are adopted to generate the sub-pel position values (Duchon 1979). For each sub-pel position, horizontal one-dimensional filter is used on neighboring integer pixels, then vertical one-dimensional filter is used on the middle results of horizontal filtering. Both filters for horizontal and vertical directions are the same, and they are all one-dimensional filters. Either 4-tap, 6-tap, or 10-tap interpolation filters can be used. The 4-tap filters are used on the sequence that is larger than 1080P, the 6-tap filters are used on the sequence that is between 1080P and 720P, and the 10-tap filters are used on the sequence that is smaller than 720P. Eighth-pel motion compensation is adopted for chroma component. Two-dimensional separable filter similar to luma component is used to generate the sub-pel position values. Four-tap filters are used on interpolating different sub-pel positions.

23.2.6 Reference Frames

As with MPEG-2, MPEG IVC has three types of pictures that use different coding methods: an intra-coded (I) picture is coded using information only from itself; a predictive-coded (P) picture is a picture that is coded using motion-compensated prediction from a past reference frame; a bidirectionally predictive-coded (B) picture is a picture that is coded using motion-compensated prediction from a past and/or future reference frame(s). P frame can use up to eight (at maximum) forward frames as reference, but in the current software reference model ITM the number of reference frames is five, which can be changed by encoding configuration; B frame can refer to one forward reference frame and one backward reference frame. In the backward prediction, the skip mode, or the symmetrical mode, the inter prediction process refers to only one reference frame.

For forward directional prediction, let the temporal position of the current frame be at t, and then the current frame refers to the reference pictures at the following five locations: t-1, t-2, t-4, t-8, and t-12. If the number of reference frames is set to more than five, then the current frame will refer to t-1, t-2, and t-4*n (for n = 1, 2, 3, ...).

In a case where a sample indicated by a motion vector is outside of the reference picture boundary, the boundary padding process will be performed. The boundary padding will use the value of the nearest integer sample inside a picture from the indicated outside position. For the luma sample matrix, samples in a reference block shall not surpass 16 samples either horizontally or vertically outside of the reference picture boundary. For each chroma sample matrix, if color format is 4:2:0, samples in a reference block shall not surpass eight samples either horizontally or vertically outside of the reference picture boundary.

The MPEG IVC defines three sub-types of P picture: P picture, non-reference P frame, and non-reference P frame with reference picture buffer (RPB) swapping. Non-reference is not used as a reference frame for motion-compensated inter-frame prediction. After decoding a non-reference P frame with RPB swapping, the newest two decoded pictures placed in RPB exchange their positions in the buffer. The non-reference P picture can be used in low-delay applications.

23.2.7 Entropy Coding

The entropy coding in MPEG IVC standard has adopted an arithmetic coding method in logarithmic domain as entropy coding engine (Yu et al. 2015). The entropy coding contains three steps: binarization, context model selection, and arithmetic encoding. The proposed adaptive binary arithmetic coding is based on a logarithmic domain arithmetic coding and a probability estimation based on the logarithmic binary coding. Both the logarithmic coding and the probability estimation based on the logarithmic binary coding achieve a high data-compression ratio with low complexity and they are also hardware-efficient structures. The algorithms introduce a mapping mechanism between the logarithmic domain and the original domain for both the coding process and the probability estimation. This entropy coding scheme proposed has high accuracy and constitutes an efficient binary arithmetic coding. In the adopted entropy code, neither multiplication and division operations nor lookup tables are used, and only addition and shifting operations are required. This entropy coder is designed to favor the coding of multiple symbols and has high throughput and achieves a good tradeoff between accuracy and speed in probability estimation through a single parameter.

23.2.8 Loop Filtering

In this standard, the loop filtering is applied to all 8×8 block edges of a picture, except edges at the boundary of the picture. The filtering process is performed on a macroblock basis. The de-blocking filter process is performed separately for the luma and chroma components. The filtering is performed on the macroblock basis. For each macroblock, vertical edges are filtered first, from left to right, and then horizontal edges. Therefore, the filtered vertical edges will be used as input for filtering horizontal edges. The order of filtering process is from top to bottom of a frame. The pixels located above and left of the current macroblock belong to the previous reconstructed macroblocks, which have already been filtered. These pixels will be used as input to the de-blocking filter to filter the current macroblock and the values of these pixels may be further modified during the filtering process for the current macroblock. The edge is defined as the difference between pixel values at the borders of all 8×8 blocks inside the macroblock, and the upper and left of current macroblock. If the level differences between the two border pixels in the same block and between the two border pixels across adjacent blocks are larger than certain levels, the loop filtering will be

performed. There are three types of filtering strength: strong loop filtering, normal loop filtering, and weak loop filtering. The strength of filtering depends on the levels of the edges (Honjo 1993).

23.3 Performance Evaluation

As we mentioned previously, the MPEG IVC is a royalty-free video codec standard, the application of this standard greatly depends on its coding performance and complexity of implementation. Since it is royalty free, we cannot expect that its performance can outperform the video coding standards such as HEVC/H.265, which are not for free use. However, we would like to determine the coding performance level achieved by the MPEG IVC and whether the performance reaches the goals for certain applications. To evaluate the performance of MPEG IVC, some researchers conducted performance tests with test model 12 (ITM12), which is the open source codec software of MPEG IVC. Also, they made performance comparisons with WVC, VCB, and H.264/AVC HP. To enable comparison at approximately the same bit rate points, the following approach had been used for conducting the test described in MPEG Video (2013): to set the encoding configurations for each codecs to generate the bitstreams with target bit rates within $+/-3\%$ for the sequences given in [Table 23.2](#). To achieve this with a minimum change of quality, one change of the quantization parameters by one step is allowed per sequence. This change in quantization parameters shall persist from that point onward.

The encoding processes are set with the following conditions:

- Allow QP (or quantizer step size) variation within a sequence within a periodic pattern of frame types (where frame types are differentiated by syntax or by a reference picture handling mechanism) within a sequence. However, pictures

TABLE 23.2

Test Sequences and Rate Points

| Class A [1920 × 1080p] | | Rate 1 | Rate 2 | Rate 3 | Rate 4 |
|------------------------------------|-------|---------------|---------------|---------------|---------------|
| S03 Kimono | 24fps | 1.6 Mbit/s | 2.5 Mbit/s | 4.0 Mbit/s | 6.0 Mbit/s |
| S04 Park Scene | 24fps | 1.6 Mbit/s | 2.5 Mbit/s | 4.0 Mbit/s | 6.0 Mbit/s |
| S05 Cactus | 50fps | 3.0 Mbit/s | 4.5 Mbit/s | 7.0 Mbit/s | 10.0 Mbit/s |
| S06 BasketballDrive | 50fps | 3.0 Mbit/s | 4.5 Mbit/s | 7.0 Mbit/s | 10.0 Mbit/s |
| Class B [836 × 480p (WVGA)] | | Rate 1 | Rate 2 | Rate 3 | Rate 4 |
| S08 BasketballDrill | 50fps | 512 kbit/s | 768 kbit/s | 1.2 Mbit/s | 2.0 Mbit/s |
| S09 BQMall | 60fps | 512 kbit/s | 768 kbit/s | 1.2 Mbit/s | 2.0 Mbit/s |
| S10 PartyScene | 50fps | 512 kbit/s | 768 kbit/s | 1.2 Mbit/s | 2.0 Mbit/s |
| S11 RaceHorses | 30fps | 512 kbit/s | 768 kbit/s | 1.2 Mbit/s | 2.0 Mbit/s |
| Class D [1280 × 720p] | | Rate 1 | Rate 2 | Rate 3 | Rate 4 |
| S16 Johnny | 60fps | 384 kbit/s | 512 kbit/s | 850 kbit/s | 1.5 Mbit/s |
| S17 KristenAndSara | 60fps | 384 kbit/s | 512 kbit/s | 850 kbit/s | 1.5 Mbit/s |
| S18 FourPeople | 60fps | 384 kbit/s | 512 kbit/s | 850 kbit/s | 1.5 Mbit/s |

that correspond to the same frame type shall be quantized with a constant step size. The difference in quantization quality for different frame types shall not exceed a ratio of 4 between the smallest and the largest quantizer step size (e.g., $QP_{large} = QP_{small} + 12$ in the case of a logarithmic quantizer scale factor coding as defined in AVC, and $QS_{large} = QS_{small} * 4$ in the case of a linear quantizer scale factor). The encoder shall use the same quantizer ratio settings for all test cases.

- No per sequence adaptation of the pattern of frame types shall be used.
- No sequence-specific tuning of coding parameters (such as enabling/disabling of special tools, certain modes, limitation of motion search range, etc.) shall be used.
- No rate control shall be used.
- No pre-processing shall be used.
- No post-processing of the decoder output shall be used, unless it is part of a normative decoding process (such as filtering of reference pictures for subsequent predictions).

Encoded bitstreams are to be provided for the following two constraint cases:

- Constraint set 1 (CS1): structural delay of processing units not larger than an eight-picture “group of pictures (GOPs)” and random-access intervals of 1.1 seconds or less.
- Constraint set 2 (CS2): no structural delay of processing units, with essentially no picture reordering between decoder processing and output. Furthermore, no sequence-level multi-pass encoding shall be allowed.

The subjective visual tests included H.264/AVC high-profile (HP) anchors produced by a JM 18.6 reference software encoder. Encoding of those anchors was performed under same configuration constraints as for the other encoders. Detailed encoding settings can be found in MPEG Video (2013). [Table 23.3](#) shows the performance of the three tested encoders according

TABLE 23.3

Performances Comparison of IVC, VCB and WVC with H.264/AVC HP

| Class | Sequences | RA | | | LDP | | |
|---------|-----------------|-------|-------|-------|-------|-------|-------|
| | | WVC | VCB | IVC | WVC | VCB | IVC |
| Class A | Kimono | 47.9% | 24.5% | 13.0% | 37.0% | 2.8% | 5.0% |
| | ParkScene | 25.4% | 38.0% | 19.8% | 17.0% | 8.1% | 7.3% |
| | Cactus | 45.9% | 32.2% | 11.5% | 25.4% | 9.5% | 4.2% |
| | BasketballDrive | 41.5% | 32.1% | 16.3% | 28.1% | 8.6% | 6.6% |
| Class B | BasketballDrill | 28.5% | 15.5% | 7.6% | 17.9% | 17.6% | 4.6% |
| | BQMall | 30.2% | 36.9% | 5.8% | 18.2% | 7.3% | 4.8% |
| | PartyScene | 25.0% | 32.5% | -5.2% | 13.5% | 5.1% | -7.2% |
| | RaceHorses | 22.2% | 20.4% | 21.6% | 16.1% | 4.2% | 10.3% |
| Class D | FourPeople | 46.2% | 67.8% | 18.6% | 27.5% | 40.9% | 14.0% |
| | Johnny | 40.8% | 41.2% | 9.5% | 22.9% | 23.1% | 13.5% |
| | KristenAndSara | 37.6% | 34.3% | 8.9% | 21.8% | 15.8% | 8.3% |
| | Average | 35.6% | 34.1% | 11.6% | 22.3% | 13.0% | 6.5% |

to the established Bjøntegaard delta bit rate ((BD)-BR) criterion, using AVC HP as the anchor. Positive percentages indicate a bit rate increase relative to the reference of the comparison. In the RA constraint cases (CS1), IVC clearly outperforms WVC and VCB in terms of BD bit rate in overall average by 22.5% and 24% respectively, and underperforms AVC HP by 11.6%. In the LD constraint cases (CS2), IVC outperforms WVC and VCB by 15.8% and 6.5% respectively in terms of BD bit rate, and IVC underperforms AVC HP by 6.5%.

As we know that the objective tests can provide a comparison for reference, but sometimes the objective tests may not consist with the subjective results. Therefore, the final results are always based on the subjective performance. The MPEG video group organized viewing test to compare the subjective performance between IVC and AVC HP, the results on 1080P sequences are shown in [Figure 23.3](#). The results are obtained based on the test mythology described in Baroncini (2015). From the results, it is concluded that MPEG IVC and H.264/AVC HP provide very similar performance for the tested cases (in most cases with confidence intervals that are overlapping, in some cases MPEG IVC is visually better than H.265/AVC HP, in some cases H.265/AVC HP is better than MPEG IVC). In general, MPEG IVC seems to have slightly better performance than the H.265/AVC HP anchors used in the low-delay cases.

From the performance evaluation, it can be concluded that in general the performance of MPEG IVC is better than WVC and VCB, and close to H.264/AVC HP under both random-access and low-delay constraints.

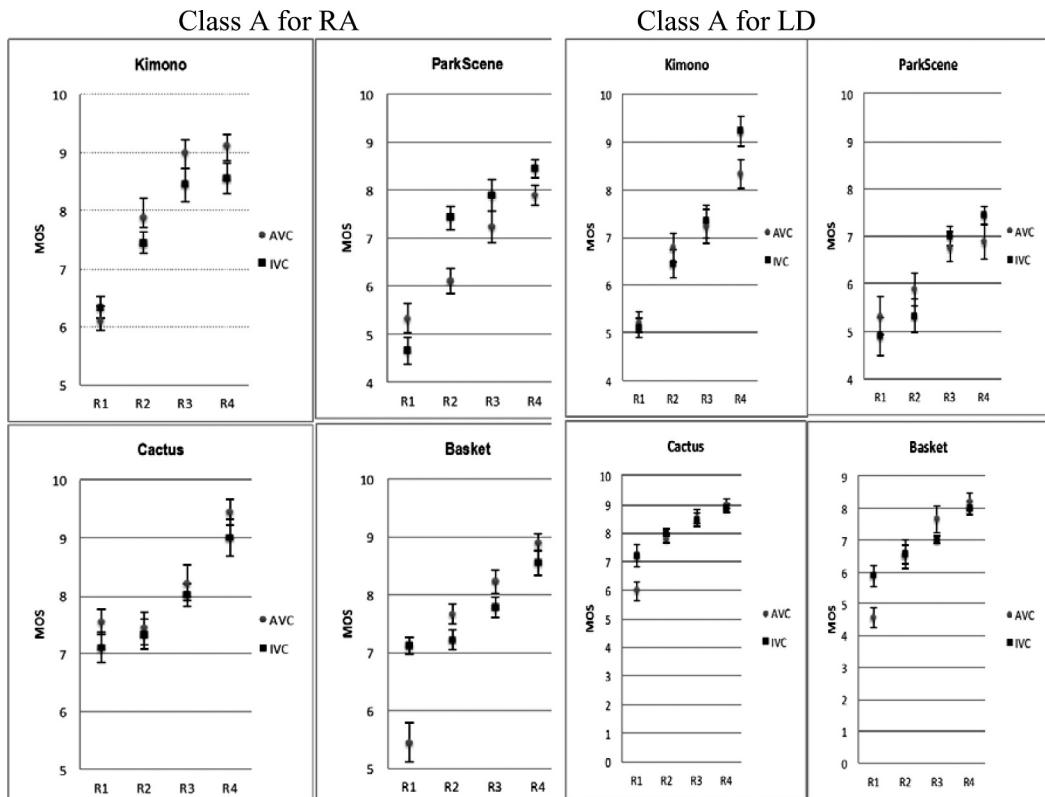


FIGURE 23.3

Subjective test results for 1080P sequences.

23.4 Summary

In this chapter, we presented the royalty-free video codec standard, MPEG IVC, and evaluated its performance against WVC, VCB, and AVC HP. The results showed that IVC outperforms both WVC and VCB and is very similar to AVC HP in terms of objective and subjective performances. The materials including the numerical test results of this chapter mostly are from the reference (Wang 2016). The goal of this chapter is to introduce the efforts made by a number of researchers for royalty-free video codec and thank them for their great contributions to the industry and society.

Exercises

- 23.1 Indicate what is the purpose of MPEG IVC development.
 - 23.2 What are the entropy-coding schemes used in MPEG IVC? Indicate the differences of IVC entropy coding with HEVC.
-

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24

MPEG Media Transport

In this chapter, we present the methods and standards for transportation, which include MPEG-2 system, MPEG-4 system, MPEG media transport (MMT), and MPEG Dynamic Adaptive Streaming over Hypertext Transfer Protocol (HTTP DASH).

24.1 Introduction

ISO/IEC MPEG has completed work on the ISO/IEC 11172 and 13818 standards known as MPEG-1, MPEG-2, MPEG-4 Part 2 and Part 10 (MPEG AVC or H.264) as well as HEVC/H.265, respectively, which deal with the coding of digital audio and video signals. As mentioned in the previous chapters, the MPEG-1, 2, and 4 standards are designed as a generic standard and as such are suitable for use in a wide range of audio-visual applications. The coding part of the standards convert the digital visual, audio, and data signals to the compressed formats that are represented as binary bits. The task of MPEG systems or transportation standards is focused on multiplexing and synchronizing the coded audio, video, and data into a single bitstream or multiple bitstreams. In other words, the digital compressed video, audio, and data all are first represented as binary formats that are referred to as bitstreams, and then the function of the system is to mix the bitstreams from video, audio, and data together. For this purpose, several issues have to be addressed by the system part of the standard:

- Distinguishing different data, such as audio, video, or other data
- Allocating bandwidth during muxing
- Reallocating or decoding the different data during demuxing
- Protecting the bitstreams in error-prone media and detecting the errors
- Dynamically multiplexing several bitstreams

Additional requirements for the system should include extensibility issues such as:

- New service extensions should be possible.
- Existing decoders should recognize and ignore data they cannot understand.
- The syntax should have extension capacity.

It should also be noted that all system-timing signals are included in the bitstream. This is the big difference between digital systems and traditional analog systems in which the timing signals are transmitted separately. In this chapter, we will introduce the concept

of systems and transportation standards and give detailed explanations for existing standards. However, we will not go through the standard page by page to explain the syntax; we will pay more attentions to those core parts of the standard and the parts that always cause confusion during the implementation.

24.2 MPEG-2 System

The MPEG-2 system standard is also referred to as ITU-T Rec. H.222.0/ISO/IEC 13818-1 (ISO/IEC 13818-1, 1996). The ISO document gives very detailed description of this standard. A simplified overview of this system is shown in [Figure 24.1](#).

The MPEG-2 system coding is specified in two forms: the transport stream and the program stream. Each is optimized for a different set of applications. The audio and video data are first encoded by audio and video encoder, respectively. The coded data are the compressed bitstreams, which follow the syntax rules specified by the video coding standard 13818-2 and audio coding standard 13818-3. The compressed audio and video bitstreams are then packetized to the packetized elementary streams (PES). The video PES and audio PES are coded by system coding to the transport stream or program stream according to the requirements of the application.

The system coding provides a coding syntax that is necessary and sufficient to synchronize the decoding and presentation of the video and audio information; at the same time, it also has to ensure that data buffers in the decoders do not overflow and underflow. Of course, the buffer regulation is also considered by the buffer control or rate control mechanism in the encoder. The video, audio, and data information are multiplexed according to the system syntax by inserting time stamps for decoding, presenting, and delivering the coded audio, video, and other data. It should be noted that both program stream and transport stream are packet-oriented multiplexing. Before we explain these streams, we first give a set of parameter definitions used in the system documents. Then, we describe the overall picture regarding the basic multiplexing approach for single video and audio elementary streams (ESs).

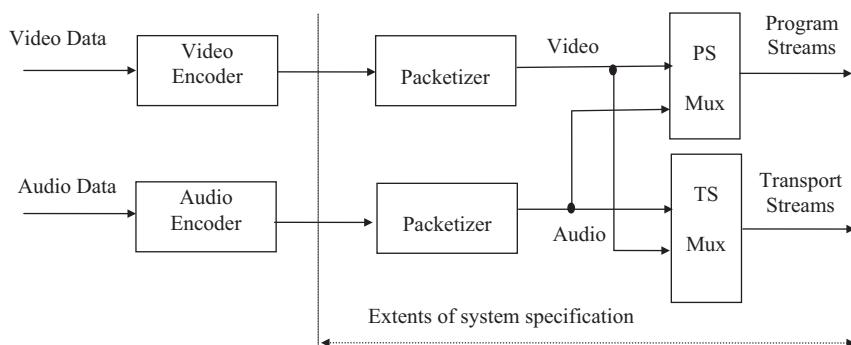


FIGURE 24.1
Simplified overview of system layer scope.

24.2.1 Major Technical Definitions in MPEG-2 System Document

In this section, the technical definitions that are often used in the system document are provided. First, the major packet and stream related definitions are given.

Access unit: A coded representation of a presentation unit. In the case of audio, an access unit is the coded representation of audio frame. In the case of video, an access unit indicates all the coded data for a picture, and any stuffing that follows it, up to but not including the start of the next access unit. In other words, the access unit begins with the first byte of the first start code. Except for the end of sequence, all bytes between the last byte of the coded picture and the sequence end code belong to the access unit.

DSM-CC: Digital storage media command and control.

ES: A generic term for one of the coded video, coded audio, or other coded bit streams in PES packets. One ES is carried in a sequence of PES packets with one and only one stream identification. This implies that one ES can only carry the same type of data such as audio or video.

Packet: A packet consists of a header followed by a number of contiguous bytes from an elementary data stream.

Packet identification (PID): A unique integer value used to associate ESs of a program in a single or multi-program transport stream. It is a 13-bit field, which indicates the type of data stored in the packet payload.

PES packet: The data structure used to carry ES data. It contains a PES packet header followed by PES packet payload.

PES Stream: A PES stream consists of PES packets, all of whose payloads consists of data from a single elementary steam, and all of which have the same stream identification. Specific semantic constraints apply.

PES Packet header: The leading fields in the PES packet up to and not including the PES packet data byte fields. Its function will be explained in the section of syntax description.

System target decoder (STD): A hypothetical reference model of a decoding process used to describe the semantics of the MPEG-2 system multiplexed bitstream.

Program-Specific Information (PSI): PSI includes normal data that will be used for demultiplexing of programs in the transport stream by decoders. One case of PSI, the non-mandatory network information table, is privately defined.

System header: The leading fields of program stream packets.

Transport stream packet header: The leading fields of program stream packets.

The following definitions are related to the timing information:

Time Stamp: A term that indicates the time of a specific action such as the arrival of a byte or the presentation of presentation unit.

System Clock Reference (SCR): A time stamp in the program stream from which decoder timing is derived.

Elementary Stream Clock Reference (ESCR): A time stamp in the PES stream from which decoders of PES stream may derive timing information.

Decoding Time Stamp (DTS): A time stamp that may be presented in a PES packet header used to indicate the time when an access unit is decoded in the STD.

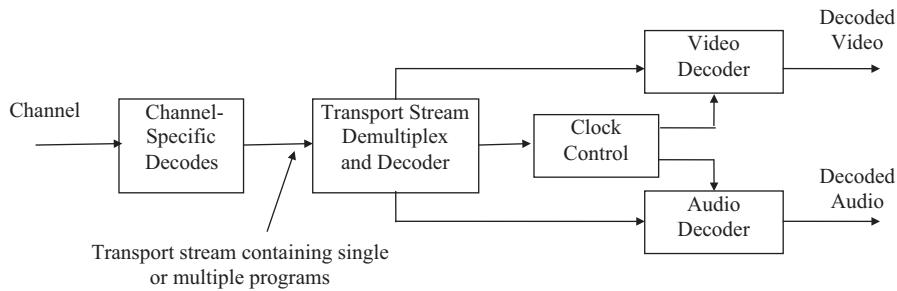
Program Clock Reference (PCR): A time stamp in the transport stream from which decoder timing is derived.

Presentation time stamp (PTS): A time stamp that may be presented in PES packet header used to indicate the time that a presentation unit is presented in the STD.

24.2.2 Transport Streams

The transport stream is a stream definition that is designed for communicating or storing one or more programs of coded video, audio, and other kinds of data in lossy or noisy environments where significant errors may occur. A transport stream combines one or more programs with one or more time bases into a single stream. However, there are some difficulties with constructing and delivering a transport stream containing multiple programs with independent time bases such that the overall bit rate is variable. As in other standards, the transport stream may be constructed by any method that results in a valid stream. In other words, the standards just specify the system coding syntax. In this way, all compliant decoders can decode bitstreams generated according to the standard syntax. However, the standard does not specify how the encoder generates the bitstreams. It is possible to generate transport streams containing one or more programs from elementary coded data streams, from program streams, or from other transport streams, which may themselves contain one or more program. An important feature of the transport stream is that the transport stream is designed in such a way that makes the following operations become possible with minimum effort. These operations include several transcoding requirements, which include:

- Retrieve the coded data from one program within the transport stream, decode it, and present the decoded results. In this operation, the transport stream is directly demultiplexed and decoded. The data in the transport stream is constructed in two layers: a system layer and a compression layer. The system decoder decodes the transport streams and demultiplexes them to the compressed video and audio streams that are further decoded to the video and audio data by the video decoder and the audio decoder, respectively. It should be noted that non-audio/video data is also allowed. The functions of the transport decoder includes demultiplexing, depacketization, and other such as error detection that will be explained in detail later. This procedure is shown in [Figure 24.2](#).
- Extract the transport stream packets from one program within the transport stream and produce as the output a new transport stream that contains only that one program. This operation can be seen as system layer transcoding that converts a transport stream containing multiple programs to a transport stream containing only a single program. In this case, the re-multiplexing operation may need the correction of PCR values to account for changes in the PCR locations in the bit stream.
- Extract the transport stream packets of one or more programs from one or more transport streams and produce as output of a new transport stream. This is another kind of transcoding that converts selected programs of one transport stream to a different one.

**FIGURE 24.2**

Example of transport demultiplexing and decoding.

- Extract the contents of one program from the transport stream and produce as output another program stream. This is a transcoding that converts the transport program to a program stream for certain applications.
- Convert a program stream to a transport stream that can be used in a lossy communication environment.

To answer the question of how to define the transport stream and then make the above transcoding become simpler and more efficient, we will begin to describe the technical detail of the systems specification in the following section.

24.2.2.1 Structure of Transport Streams

As described earlier, the task of the transport stream coding layer is to allow one or more programs to be combined into a single stream. Data from each ES is multiplexed together with timing information, which is used for synchronization and presentation of the ES during decoding. Therefore, the transport stream consists of one or more programs such as audio, video, and data ES access units. The transport stream structure is a layered structure. All the bits in the transport stream are packetized to the transport packets. The size of transport packet is chosen to be 188 bytes, among those 4 bytes are used as the transport stream packet header. In the first layer, the header of transport packets indicates whether the transport packet has an adaptation field. If there is no adaptation field, the transport payload may consist of only PES packets or consist of both PES packets and PSI packets. [Figure 24.3](#) illustrates the case of containing PES packets only.

If the transport stream carries both PES and PSI packets, then the structure of transport stream as shown [Figure 24.4](#) would result.

If the transport stream packet header indicates that the transport stream packet includes the adaptation field, then the construct is shown in [Figure 24.5](#).

In [Figure 24.5](#), the appearance of the optional field depends on the flag settings. The function of adaptation field will be explained in the syntax section. Before we go ahead, though, we should give a little explanation regarding the size of the transport stream packet. More specifically, why is a packet size of 188 bytes chosen? Actually, there are several reasons. First, the transport packet size needs to be large enough so that the overhead

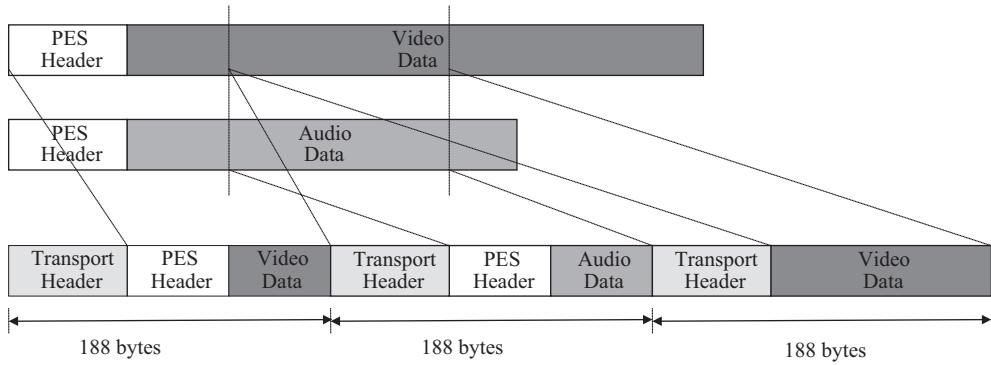


FIGURE 24.3
Structure of transport stream containing only PES packets.

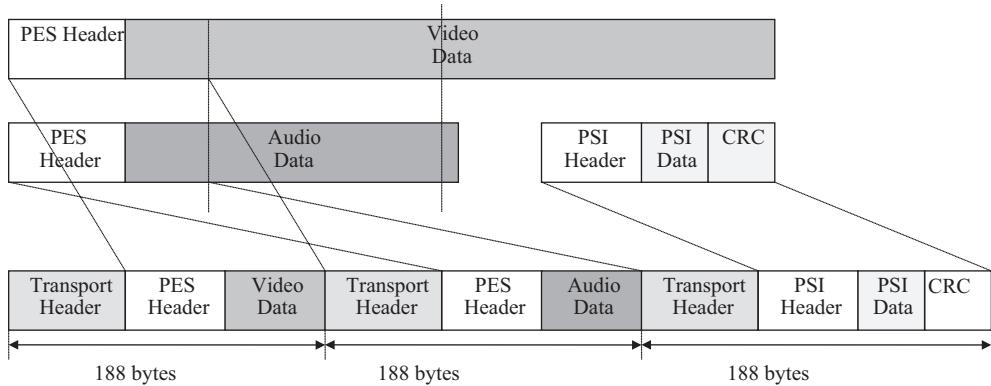


FIGURE 24.4
Structure of transport stream containing both PES packets and PSI packets.

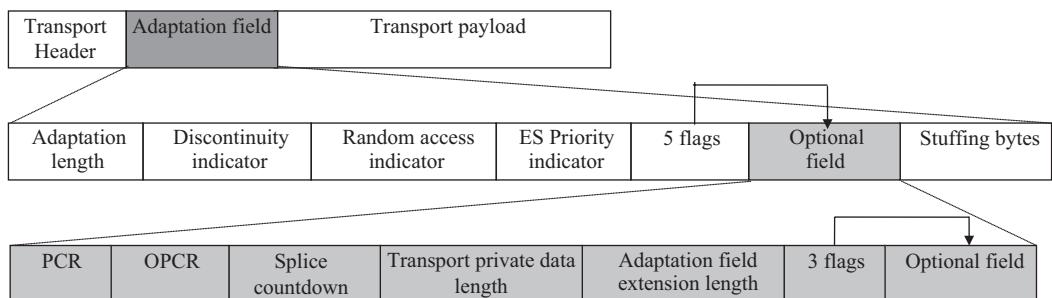


FIGURE 24.5
Structure of transport stream, in which header contains adaptation field.

due to the transport headers is not too significant. Second, the size should not be so large that the packet-based error correction code becomes inefficient. Finally, the size 188 bytes is also compatible with ATM packet size which is 47 bytes, then one transport stream packet is equal to the four ATM packets. So, the size of 188 bytes is not a theoretical solution but a practical and compromised solution.

24.2.2.2 Transport Stream Syntax

As we indicated, the transport stream is a layered structure. To explain the transport stream syntax, we start from the transport stream packet header. Since the header part is very important, it is the highest layer of the stream. We describe it in more details. For the rest, we do not repeat the standard document and just indicate the important parts that we think there may cause some confusion for the readers. The detail of other parts that are not covered here can be found from the MPEG standard document (ISO/IEC 13818-1, 1996).

24.2.2.2.1 Transport Stream Packet Header

This header contains four bytes that are assigned as eight parts:

| Syntax | No of Bits | Mnemonic |
|------------------------------|------------|----------|
| sync_byte | 8 | bslbf |
| transport_error_indicator | 1 | bslbf |
| payload_unit_start_indicator | 1 | bslbf |
| transport_priority | 1 | bslbf |
| PID | 13 | uimsbf |
| transport_scrambling_control | 2 | bslbf |
| adaptation_field_control | 2 | bslbf |
| continuity_counter | 4 | uimsbf |

The mnemonic in the above table means:

bslbf—bit stream left bit first

uimsbf—unsigned integer, most significant bit first

- The sync-byte is a fixed 8-bit field whose value is “0100 0111” (hexadecimal 47 = 71).
- The transport_error_indicator is a 1-bit flag; when it is set to “1,” it indicates that at least 1 uncorrectable bit error exists in the associated transport stream packet. It will not be reset to “0” unless the bit values in error have been corrected. This flag is useful for error concealment purpose, since it indicates the error location. When an error exists, either resynchronization or other concealment method can be used.
- The payload_unit_start_indicator is a 1-bit flag that is used to indicate whether the transport stream packets carry PES packets or PSI data. If it carries PES packets, then the PES header starts in this transport packet. If it contains PSI data, then a PSI table starts in this transport packet.
- The transport_priority is a one-bit flag which is used to indicate that the associated packet is of greater priority than other packets having the same PID that do not have the flag bit set to “1.” The original idea of adding a flag to indicate the priority of packets comes from video coding. The video elementary bitstream contains mostly bits that are converted from DCT coefficients. The priority indicator can set a partitioning point that can divide the data into a more important part and a less important part. The important part includes the header information and low-frequency coefficients and the less important part includes only the high-frequency coefficients that have less effect on the decoding and quality of reconstructed pictures.
- PID is a 13-bit field that provides information for multiplexing and demultiplexing by uniquely identifying which packet belongs to a particular bit stream.

- The transport_scrambling_control is a 2-bit flag. 00 indicates that the packet is not scrambled; the other three (01, 10, and 11) indicate that the packet is scrambled by a user-defined scrambling method. It should be noted that the transport packet header and adaptation field (when it is present) should not be scrambled. In other words, only the payload of transport packets can be scrambled.
- The adaptation_field_control is a 2-bit indicator that used to inform whether there is an adaptation field present in the transport packet. 00 is reserved for future use. 01 indicates no adaptation field, 01 indicates that there is only an adaptation field and no payload. Finally, 11 indicates that there is an adaptation field followed by a payload in the transport stream packet.
- The continuity_counter is a 4-bit counter that increases with each transport stream packet having the same PID.

From the header of the transport stream packet, we can obtain the information about future bits. There are two possibilities, if the adaptation field control value is 10 or 11, then the bits following the header are adaptation field, otherwise the bits are payload. The information contained in the adaptation field is described as follows.

24.2.2.2 Adaptation Field

The structure of the adaptation field data is shown in [Figure 24.5](#). The functionality of these headers is basically related to the timing and decoding of the elementary bit steam. Some important fields are explained below:

- Adaptation-field-length is an 8-bit field specifying the number of bytes immediately following it in the adaptation field including stuffing bytes.
- Discontinuity-indicator is a 1-bit flag that, when it is set to "1," indicates that the discontinuity state is true for the current transport packet. When this flag is set to "0," the discontinuity is false. This discontinuity indicator is used to indicate two types of discontinuities; system time-based discontinuities and continuity counter discontinuities. In the first type, this transport stream packet is the packet of a PID designed as a PCR-PID. The next PCR represents a sample of a new system time clock (STC) for the associated program. In the second type, the transport stream packet could be any PID type. If the transport stream packet is not designated as a PCR-PID, the continuity counter may be discontinuous with respect to the previous packet with the same PID or when a system time-base discontinuity occurs. For those PIDs that are not designated as PCR-PIDs, the discontinuity indicator may be set to "1" in the next transport stream packet with the same PID, but will not be set to "1" in three consecutive transport stream packets with the same PID.
- Random-access-indicator is a 1-bit flag that indicates the current and subsequent transport stream packets with the same PID, containing some information to aid with random access at this point. Specifically, when this flag is set to "1," the next PES packet in the payload of transport stream packet with the current PID will contain the first byte of a video sequence header or the first byte of an audio frame.
- ES priority indicator is used for data partitioning application in the ES. If this flag is set to "1," the payload contains high-priority data such as the header information or low-order DCT coefficients of the video data. This packet will be highly protected.

- PCR-flag and OPCR-flag: if these flags are set to “1,” it means that the adaptation field contains the PCR data and original PCR data. These data are coded in two parts.
- Splicing-point-flag: when this flag is set to “1,” it indicates that a splice-countdown field will be present to specify the occurrence of a splicing point. The splice point is used to smoothly splice two bitstreams into one stream. SMPTE has developed a standard for seamless splicing of two streams (SMPTE, 1997). We will describe the function of splicing later.
- Transport-private-flag: this flag is used to indicate whether the adaptation field contains private data.
- Adaptation-filed-extension-flag: this flag is used to indicate whether the adaptation field contains the extension field that gives more detailed splicing information.

24.2.2.3 Packetized Elementary Stream

It is noted that the ES data is carried in PES packets. A PES packet consists of a PES packet header followed by packet data, or payload. The PES packet header begins with a 32-bit start-code that also identifies the stream or stream type to which the packet data belongs. The first byte of each PES packet header is located at the first available payload location of a transport stream packet. The PES packet header may also contain DTS, PTS, ESCR, and other optional fields such as DSM trick mode information. The PES packet data field contains a variable number of contiguous bytes from one ES. Readers can learn this part of syntax in the same way as described for the transport packet header and adaptation field.

24.2.2.4 Program-Specific Information

PSI includes both MPEG-2 system compliant data and private data. In the transport streams, the PSI is classified into four table structures: program association table, program map table, conditional access table, and network information table. The network information table is private data and the other three are MPEG-2 system-compliant data. The program-associated table provides the information of program number and the PID value of the transport stream packets. The program map table specifies PID values for components of one or more programs. The conditional access (CA) table provides the association between one or more CA systems, their entitlement management messages (EMM), and any special parameters associated with them. The EMM are private conditional access information that specify the authorization levels or the services of specific decoders. They may be addressed to a single decoder or groups of decoders. The network information table is optional and its contents are private. Its contents provide physical network parameters such as FDM frequencies, transponder numbers, etc.

24.2.3 Transport Streams Splicing

The operation of bitstream splicing is switching form one source to another according to the requirements of the applications. Splicing is the most common operation performed in TV stations today (Hurst 1997). The examples include: inserting commercials into programming, editing, inserting, or replacing a segment into an existing stream, and inserting local commercials or news into a network feed. The most important problem for bitstream splicing is managing the buffer fullness at the decoder. Usually, the encoded bitstream satisfies the buffer regulation with a buffer control algorithm at the encoder.

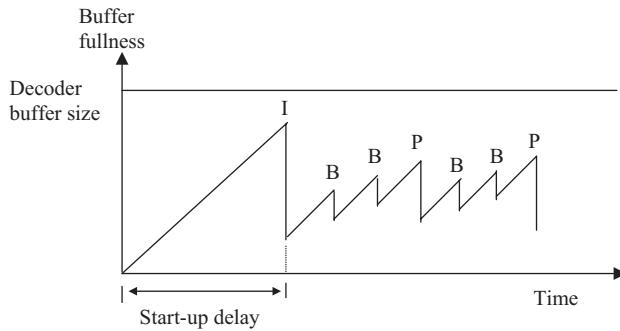


FIGURE 24.6
Typical buffer fullness trajectory at the decoder.

During decoding, this bitstream will not cause the decoder buffer to suffer from buffer overflow and underflow. A typical example of buffer fullness trajectory at the decoder is shown in Figure 24.6. However, after bitstream splicing, the buffer regulation is not guaranteed depending on the selection of splicing point and the bit rate of the new bitstream. It is necessary to have a rule for selecting the splicing point.

The committee on packetized television technology, PT20 of Society of Motion Picture and Television Engineers (SMPTE), has proposed a standard that deals with the splice point for MPEG-2 transport streams (SMPTE, 1997). In this standard, two techniques have been proposed for selecting splicing points. One is seamless splicing and other is non-seamless splicing. The seamless splicing approach can provide clean and instant switching of bitstreams, but it requires careful selection of splicing points on video bitstreams. The non-seamless splicing approach inserts a "drain-time" that is a period of time between the end of an old stream and the start of a new stream to avoid overflow in the decoder buffer. The "drain-time" assures that the new stream begins with an empty buffer. However, the decoder has to freeze the final presented picture of the old stream and wait for a period of start-up delay while the new stream is initially filling the buffer. The difference between the seamless splicing and the non-seamless splicing is shown in Figure 24.7.

In the SMPTE-proposed standard (SMPTE, 1997), the optional indicator data in the PID streams (all the packets with the same PID within a transport stream) is used to provide important information about the splice for the applications such as inserting commercial programs. The proposed standard defines a syntax that may be carried in the adaptation field in the packets of the transport stream. The syntax provides a way to convey two kinds of information. One type of information is splice-point information that consists of four splicing parameters: drain-time, in-point-flag, ground-ID and picture-param-type. The other types of information are splicing-point indicators that provide a method to indicate application-specific information. One such application example is the insertion indicator for commercial advertisement. This indicator includes flags to indicate that the original stream is obtained from the network and that the splice point is the time point where the network is going out or going in. Other fields give information about whether it is scheduled, how long it is expected to last as well as an ID code. The detail about splicing can be found in the proposed standard (SMPTE, 1997).

The committee on packetized television technology, PT20 of SMPTE, has proposed a standard that deals with the splice point for MPEG-2 transport streams (SMPTE, 1997).

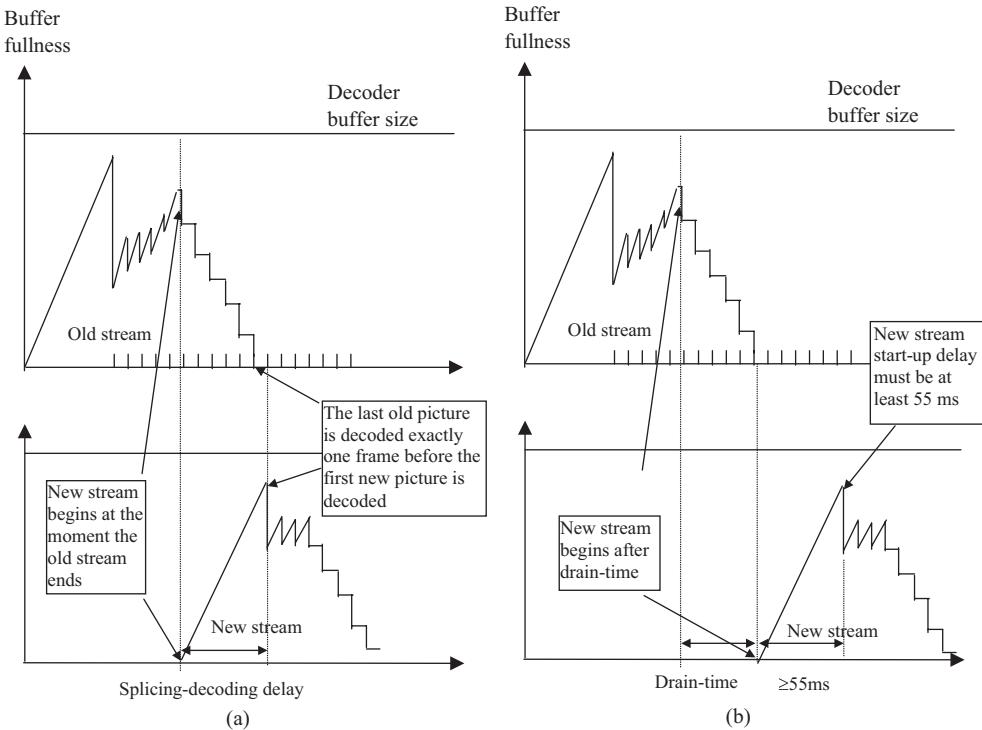


FIGURE 24.7
Difference between seamless splicing and non-seamless splicing (a) the VBV buffer behavior of seamless splicing, (b) the VBV buffer behavior of non-seamless buffer behavior.

Although the standard provides a tool for bitstream splicing, there are still some difficulties for performing bitstream splicing in practice. One problem is that the selection of a splicing point has to consider that the bitstream contains video that has been encoded by a predictive coding scheme. Therefore, the new stream should begin from the anchor picture. Other problems include uneven timing frames and splicing of bitstreams with different bit rates. In such cases, one needs to be aware of any consequences related to buffer overflow and underflow.

24.2.4 Program Streams

The program stream is defined for the multiplexing of audio, video, and other data into a single stream for communication or storage application. The essential difference between the program stream and transport stream is that the transport stream is designed for applications with noisy media, such as in terrestrial broadcasting. Since the program stream is designed for applications in the relatively error-free environment, such as in the digital video disk (DVD) and digital storage applications, the overhead in the program stream is less than in the transport stream.

A program stream contains one or more ESs. The data from ESs are organized in the form of PES packets. The PES packets from different ESs are multiplexed together. The structure of a program stream is shown in the [Figure 24.8](#).

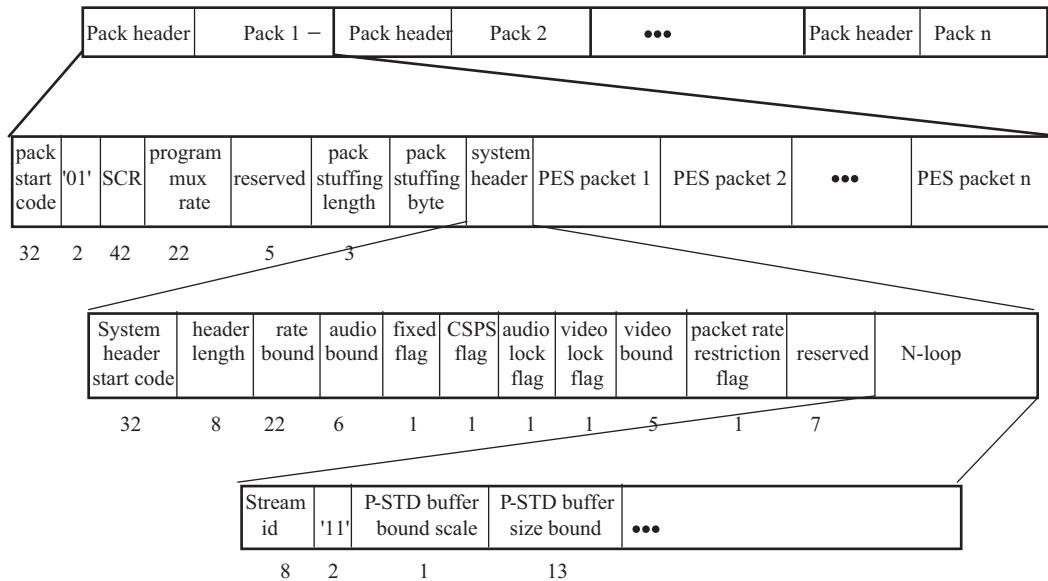


FIGURE 24.8
(a, b) Structure of program stream.

A program stream consists of packs. A pack begins from a pack header followed by PES packets. The pack header is used to carry timing and bit rate information. It begins with a 32-bit start-code followed by SCR information, program muxing rate, and stuffing bits. The SCR indicates the intended arrival time of the byte that contains the last bit of SCR base at the input of the decoder. The program muxing rate is a 22-bit integer that specifies the rate at the decoder. The value of this rate may vary from pack to pack. The stuffing-bits are inserted by the encoder to meet channel requirements. The pack header may contain a system header that may be repeated optionally. The system header contains the summary of the system parameters such as header length, rate bound, audio bound, video bound, stream ID, and other system parameters. The rate bound is used to indicate the maximum rate in any pack of the program stream, and it may be used to assess whether the decoder is capable of decoding the entire stream. The audio bound and video bound are used to indicate the maximum values of audio and video in the program stream. There are some other flags that are used to give some system information. A PES packet consists of a PES packet header followed by packet data. The PES packets have the same structure as in the transport stream.

A special type of PES packet is the program stream map; it is present when the stream ID value is 0xBC. The program stream map provides a description of the ESs in the program stream and their relationship to one another. The data structure of program stream map is shown in [Figure 24.9](#).

Other special types of PES packets include program stream directory and program element descriptors. The major information contained in the program stream directory includes the number of access units, packet stream ID, and PTS. The program and program descriptors provide the coding information about the ESs. There is a total of 17 descriptors including video descriptor, audio descriptor, and hierarchy descriptor. For the detail on these descriptors, the reader is referred to the standard document (ISO/IEC 13818-1, 1996).

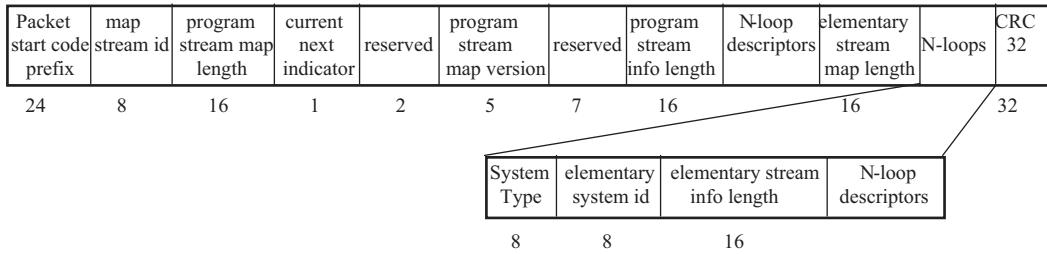


FIGURE 24.9
Data structure of program stream map.

24.2.5 Timing Model and Synchronization

The principal function of the MPEG system is to define the syntax and semantics of the bitstreams that allows the system decoder to perform two operations among multiple ESs: de-multiplexing and re-synchronization. Therefore, the system encoder has to add the timing information to the program streams or transport streams during the process of multiplexing the coded video, audio, and data ESs to a single stream or multiple streams. System, video, and audio all have a timing model in which the end-to-end delay from the signal input to an encoder to the signal output from a decoder is a constant. The delay is the sum of encoding, encoder buffering, multiplexing, transmission or storage, de-multiplexing, decoding buffering, decoding, and presentation delays. The buffering delays could be variable, while the sum of total delays should be constant.

In the program stream, the timing information for a decoding system is the SCR; in the transport stream, the timing information is given by the PCR. The SCR and PCR are time stamps that are used to encode the timing information of the bitstream itself. The 27 MHz SCR is the kernel time base for the entire system. The PCR is 90kHz, which is 1/300 of the SCR. In the transport stream, the PCR is encoded with 33 bits and is contained in the adaptation field of the transport stream. The PCR can be extended to the SCR with an additional 9 bits in the adaptation field. For the program stream, the SCR is directly encoded with 42 bits and it is located in the pack header of the program stream. The synchronization among multiple ESs is accomplished with a PTS (presentation time stamp) in the program and transport streams. The PTS is 90 kHz and represented with a 33-bit number coded in three separate parts contained in the PES packet header. In the case of audio, if a PTS is present, it will refer to the first access unit commencing in the PES packet. An audio access unit starts in a PES packet if the first byte of the audio access unit is present in the PES packet. In the case of video, if a PTS occurs in the PES packet header, it refers to the access-unit containing the first picture start code that commences in this PES packet. A picture start code commences in the PES packet if the first byte of the picture start code is present in the PES packet. In an MPEG-2 system, the SCR is specified to satisfy the following conditions:

$$27 \text{ MHz} - 810 \text{ Hz} \leq \text{SCR} \leq 27 \text{ MHz} + 810 \text{ Hz}$$

$$\text{Change rate of SCR} \leq 75 \times 10^{-3} \text{ Hz/second}$$

In the encoder, the SCR or PCR are encoded in the bitstream at intervals up to 100 ms in the transport stream and up to 700 ms in the program stream. As such, they can be used to

reconstruct the STC in the decoder with sufficient accuracy for all identified applications. The decoder has its own STC with the same frequency, 90 kHz for the transport stream and 27 MHz for the program stream. In a correctly constructed MPEG-2 system bitstream, each SCR arrives at the decoder at precisely the time indicated by the value of that SCR. If the decoder's clock frequency matches the one in the encoder, the decoding and presentation of video and audio will automatically have the same rate as those in the encoder, then the end-to-end delay will be constant. However, the STC in the decoder may not exactly match the one in the encoder due to the independent oscillators. Therefore, a decoder's system clock frequency may not match the encoder's system clock frequency that is sampled and indicated in the SCR. One method is to use a free-run 27 MHz in the decoder. The mismatch between the encoder's STC and the decoder's STC is handled by skipping or repeating frames. Another method to handle the mismatch is to use the received SCRs (which occur at least once in the intervals of 100 ms for transport stream and 700 ms for the program stream). In this way, the decoder's STC is a slave to the encoder's STC. This can be implemented with a phase-locked loop (PLL) as shown in [Figure 24.10](#).

The synchronization among multiple ESs can be achieved by adjusting the decoding of streams to a common master time base rather than by adjusting the decoding of one stream to match that of another. The master time base may be one of the many decoder clocks, the clock of the data source, or some external clock. Each program in a transport stream, which may contain multiple programs, may have its own time base. The time bases of different programs within a transport stream may be different.

In the digital video systems, the 13.5 MHz sampling rate of the luminance signal and 6.25 MHz chrominance signals of the CCIR601 digital video are all synchronized to 27 MHz STC. The NTSC or PAL TV signals are also phase-locked to the same 27 MHz clock such that the horizontal and vertical synchronous signals and the color burst clock are all locked to the 27 MHz STC.

In the TV studio applications, the entire TV studio equipment is synchronized to the same time base of a composite horizontal and vertical synchronization signals in order to perform the seamless video source switching and editing. It should be noted that this time base is definitely not synchronized to the PCRs from various remote encoder sites. The 27 MHz local decoder's STC is locked to the same studio composite horizontal and vertical synchronization signal. The 33 bits of video STC counter is initialized by the latest video PTS then calibrated using the 90 kHz clock derived from the 27 MHz system clock in the decoder. If the 27 MHz system clock in the decoder is synchronized with the system clock on the transmitting end, the STC counter will be always the same as the incoming PTS numbers. However, there may be some mismatch between the system clocks. As each

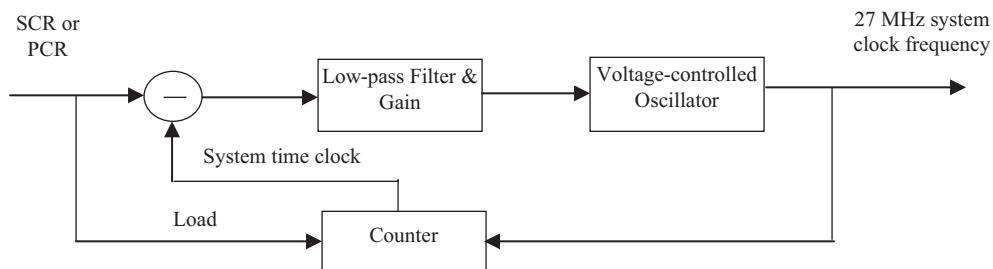


FIGURE 24.10

System time clock recovery using PLL.

new PTS arrives, the PTS will be compared with the STC counter. If the PTS is larger than the STC plus half of the duration of the PTS, it means that the 27 MHz decoder clock is too slow and the bit buffer may overflow. In this case, the decoder should skip some of current data to search for the next anchor frame so that decoding can be continued. If the PTS is less than the STC minus half of the duration of the PTS, the bit buffer may underflow. The decoding will halt and repeatedly display the current frame. The audio decoder will also be locked on the same 27 MHz system clock, where similar skipping and repeating of audio data is used to handle the mismatch.

In the low-cost consumer “set-top box (STB)” applications, a simple free run 27 MHz decoder system clock with the skipping and repeating frame scheme can provide pretty good results. In fact, the skipping or repeating frame may happen once in a two- or four-hour period with a free-run 27 MHz crystal clock. The STC counter will be set by the latest PTS, then count on the 90 kHz STC clock derived from the free run 27 MHz crystal clock. The same skipping or repeating display control as the TV studio will be used.

For a complex STC solution, a phase-locked loop with voltage-controlled crystal oscillator (VCXO) in the decoder is used to synchronize the incoming PCR data. The 33-bit decoder's PCR counter is initialized by the latest PCR data, and then the 27 MHz system clock is calibrated. If the decoder's system clock is synchronized with the encoder's remote 27 MHz system clock, every incoming PCR data will be the same as the decoder's PCR counter or have small errors from PCR jitter. The difference between the decoder's PCR counter and the incoming PCR data indicates this frequency jitter or drift. As long as the decoders 27 MHz system clock is locked on the PCR data, the STC counter will be initialized by the latest PTS then calibrated using the 90 kHz clock. The similar skipping and repeating frame scheme will be used again, but the 27 MHz system clock in the decoder is synchronized with the incoming PCR. As long as the decoder's 27 MHz is locked on the encoder's 27 MHz, there will be no skipping or repeating of frames. However, if the PCR PLL is not working properly, the skipping or repeating of frames will occur more often than when the free-run 27 MHz system clock is used.

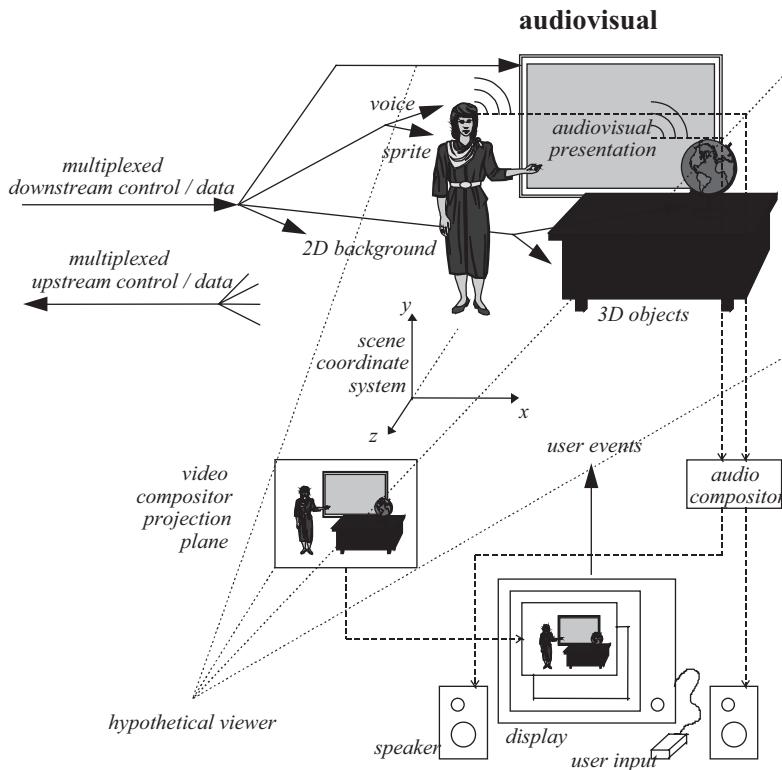
Finally, it should be noted that the PTS-DTS-flag is used to indicate whether the PTS, DTS, or both of them will be present in the PES packet header. The DTS is a 33-bit number coded in three separate fields in the PES packet header. It is used to indicate the decoding time.

24.3 MPEG-4 System

This section describes the specification of the MPEG-4 system or ISO/IEC 14496-1.

24.3.1 Overview and Architecture

The specification of the MPEG-4 system (ISO/IEC 14496-1, 1998) is used to define the requirements for the communication of interactive audio-visual scenes. An example of such a scene is shown in [Figure 24.11 \[mpeg4system\]](#). The overall operation of this system can be summarized as follows. At the encoder, the audio, visual, and other data information is first compressed and supplemented with synchronization timing information. The compressed data with timing information are then passed to a delivery layer that multiplexes these data into one or more coded binary streams for storing or transmission. At the decoder, these streams are first de-multiplexed and decompressed. The reconstructed audio and visual

**FIGURE 24.11**

An example of MPEG-4 audio-visual scene (ISO/IEC 14496-1, 1998).

objects are then composed according to the scene description and synchronization information. The composed audio-visual objects are then presented to the end user. The important feature of the MPEG-4 standard is that the end user may have the option to interact with this presentation since the compression is performed on the object or content basis. The interaction information can be processed locally or transmitted back to the encoder. The scene information is contained in the bitstreams and used in the decoding processes.

The system part of the MPEG-4 standard specifies the overall architecture of a general receiving terminal. Figure 24.12 shows the basic architecture of the receiving terminal. The major elements of this architecture are delivery layer, sync layer (SL), and compression layer. The delivery layer consists of the FlexMux and TransMux. At the encoder, the coded ESs, which include the coded video, audio, and other data with the synchronization and scene description information, are multiplexed to the FlexMux streams. The FlexMux streams are transmitted to the TransMux of the delivery layer from the network. The function of TransMux is not within the scope of the system standard and it can be any of the existing transport protocols such as MPEG-2 transport stream, RTP/UDP/IP, AAL5/ATM, and H223/Mux.

Only the interface to the TransMux layer is part of the standard. Usually, the interface is the DMIF application interface (DAI), which is not specified in the system part, but in part 6 of the MPEG-4 standard. The DAI specifies the data that needs to be exchanged between the SL and the delivery layer. The DAI also defines the interface for signaling information required for session and channel set up as tear down. For some simple applications, it does not require full functionality of the system specification. A simple multiplexing tool,

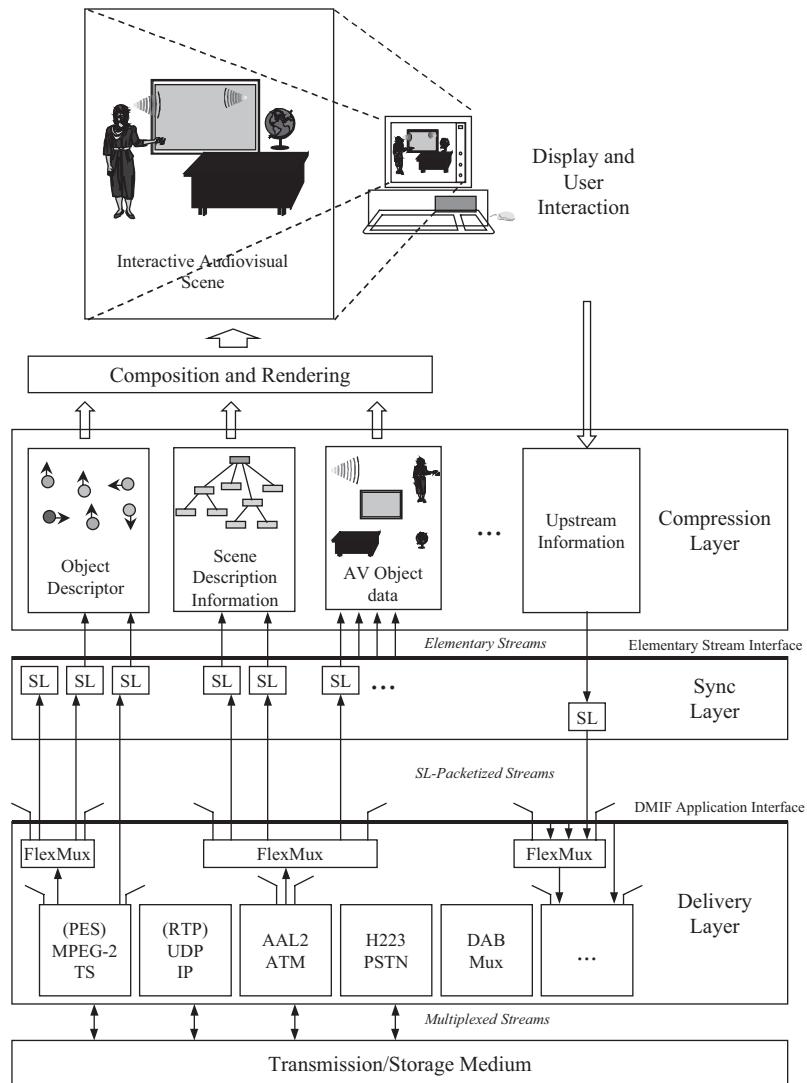


FIGURE 24.12
The MPEG-4 system terminal architecture.

FlexMux, with low delay and low overhead, is defined in the system part of MPEG-4. The FlexMux tool is a flexible multiplexer that accounts for the interleaving of SL-packetized streams with varying instantaneous bit rate. The FlexMux packet has a variable length that may contain one or more SL-packets. Also, the FlexMux tool provides the identification for the SL packets to indicate which ES it comes from. FlexMux packets with data from different SL packetized streams can therefore be arbitrary interleaved.

The SL specifies the syntax for packetizing the ESs to the SL-packets. The SL-packets contain a SL packet header and a SL packet payload. The SL packet header provides the information for continuity checking in case of data loss and also carries the timing and synchronization information as well as fragmentation and random-access information. The SL packet does not contain its length information. Therefore, SL packets must be

framed by the FlexMux tool. At the decoder, the SL packets are de-multiplexed to the ESs in the SL. At the same time, the timing and the synchronization information as well as fragmentation and random-access information are also extracted for synchronizing the decoding process and subsequently for composition of the ESs.

At the compression layer, the encoded ESs are decoded. The decoded information is then used for the reconstruction of audio-visual information. The operation of the reconstruction includes composition, rendering, and presentation with the timing synchronization information.

24.3.2 Systems Decoder Model

The systems decoder model (SDM) is a conceptual model that is used to describe the behavior of decoders complying with MPEG-4 systems. It may be used for the encoder to predict how the decoder or receiving terminal will behave in terms of buffer management and synchronization during the process of decoding, reconstructing, and composing of audio-visual objects. The SDM includes a system timing model and a system buffer model. These models specify the interfaces for accessing de-multiplexed data streams, decoding buffers for each ES, the behavior of ES decoder, composition memory for decoded data from each decoder, and the output behavior of composition memory towards the compositor. The SDM is shown in Figure 24.13.

The timing model defines the mechanisms that allow a decoder or receiving terminal to process time-dependent objects. This model also allows the decoder or receiving terminal to establish mechanisms to maintain synchronization both across and within particular media types as well as with user interaction events. In order to facilitate these functions at the decoder or receiving terminal, the timing model requires that the transmitted data streams contain implicit or explicit timing information. There are two sets of timing information that are defined in the MPEG-4 system. One indicates the periodic values of the encoder clock that is used to convey the encoder's time base to the decoder or the receiving terminal, while the other is the desired presentation timing for each audio-visual object. For real-time applications, the end-to-end delay from the encoder input to the decoder output is constant. The delay is equal to the sum of the delay due to the encoding process, buffering, multiplexing at the encoder, the delay due to the delivery layer and demultiplexing, decoder buffering, and decoding process at the decoder.

The buffer model is used for the encoder to monitor and control the buffer resources that are needed for decoding each ES at the decoder. The information of the buffer requirements

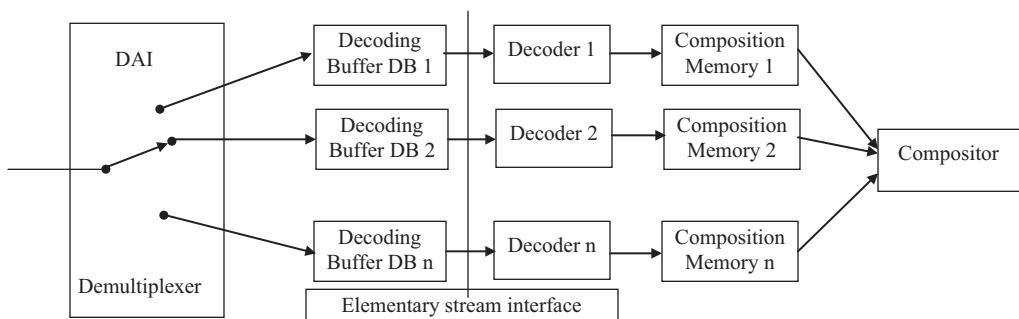


FIGURE 24.13
Block diagram of SDM.

is transmitted to the decoder by descriptors at the beginning of the decoding process. The decoder can then decide whether or not it is capable of handling this particular bitstream. In summary, the buffer model allows the encoder to schedule data transmission and to specify when the bits may be removed from these buffers. Then the decoder can choose proper buffers so that the buffers will not overflow or underflow during the decoding process.

24.3.3 Scene Description

In multimedia applications, a scene may consist of audio-visual objects that include the objects of natural video, audio, texture, 2-D or 3-D graphics and synthetic video. Since MPEG-4 is the first object-based coding standard, reconstructing or composing a multiple audio-visual scene is quite new. The decoder not only needs the ESs for the individual audio-visual objects, but also synchronization timing information and the scene structure. This information is called the scene description and it specifies the temporal and spatial relationships between the objects or scene structures. The information of the scene description can be defined in the encoder or interactively determined by the end user and transmitted with the coded objects to the decoder. The scene description only describes the scene structure. The action of assembling these audio-visual objects to a scene is called composition. The action of transmitting these objects from a common representation space to a specific presentation device is called rendering.

The MPEG-4 system defines the syntax and semantics of a bitstream that can be used to describe the relationships of the objects in space and time. However, for visual data, the system standard does not specify the composition algorithms. Only for audio data is the composition process specified in a normative manner. In order to allow the operations of authoring, editing, and interaction of visual objects at the decoder the scene descriptions are coded independent from the audio-visual media. This allows the decoder to modify the scene according to the requirements of the end user. Two kinds of user interaction are provided in the system specification. One is client-side interaction that involves object manipulations requested in the end user's terminal. The manipulation includes the modification of attributes of scene objects according to the specified user actions. The other type of manipulation is the serve-side interaction that the standard does not deal with.

The scene description is a hierarchical structure that can be represented as a graph. The example of the audio-visual scene in [Figure 24.11](#) can be represented as in [Figure 24.14](#). The scene description is represented by a parametric approach, the binary format for scenes (BIFS). The description consists of an encoded hierarchical tree of nodes with attributes and other information. In this tree, the leaf nodes correspond to the elementary audio-visual objects and information for grouping, transformation, and other operation.

24.3.4 Object Description Framework

The ESs carry data for audio or visual objects as well as for the scene description itself. The purpose of the object description framework is to provide the link between the ESs and the audio-visual scene description. The object description framework consists of a set of descriptors that allow identifying, describing and appropriately associating ESs to each other and to audio-visual objects used in the scene description. Each object descriptor is a collection of one or more ES descriptors that are associated to a single audio-visual object or a scene description. Object descriptors are themselves conveyed in ESs. Each object descriptor is assigned an identifier (object descriptor ID), which is unique within a defined name scope. This identifier is used to associate audio-visual objects in the scene description with a particular object

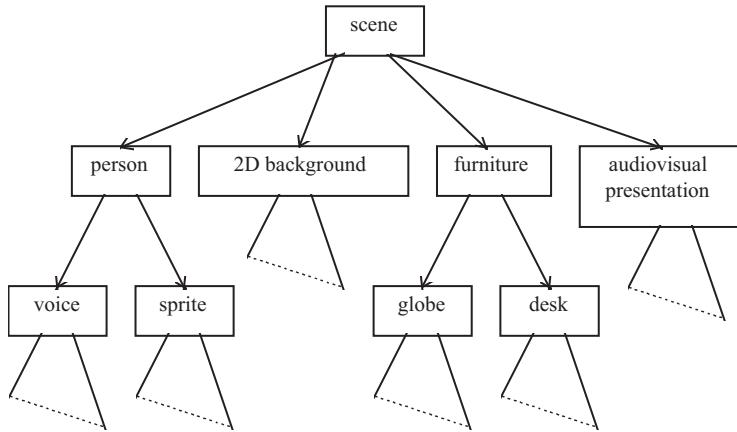


FIGURE 24.14
Hierarchical graph representation of an audio-visual scene [mpeg4system].

descriptor, and thus the ESs related to that particular object. ES descriptors include information about the source of the stream data, in the form of a unique numeric identifier (the ES ID) or a URL pointing to a remote source for the stream. ES descriptors also include information about the encoding format, configuration information for the decoding process and the SL packetization, as well as quality of service (QoS) requirements for the transmission of the stream and intellectual property identification. Dependencies between streams can also be signaled within the ES descriptors. This functionality may be used, for example, in scalable audio or visual object representations to indicate the logical dependency of an enhancement layer stream to a base-layer stream. It can also be used to describe alternative representations for the same content (e.g., the same speech content in various languages).

The object description framework provides the hooks to implement intellectual property management and protection (IPMP) systems. IPMP descriptors are carried as part of an object descriptor stream. IPMP ESs carry time variant IPMP information that can be associated to multiple object descriptors. The IPMP System itself is a non-normative component that provides intellectual property management and protection functions for the terminal. The IPMP System uses the information carried by the IPMP ESs and descriptors to make protected IS 14496 content available to the terminal. An application may choose not to use an IPMP System, thereby offering no management and protection features.

24.4 MMT

In this section, we will present the specification of MMT standard.

24.4.1 Overview

MMT is a *digital container standard* developed by MPEG. The MMT standard is referred to as ISO/IEC 23008-1 and as Part 1 of MPEG H (ISO/IEC 23008-1 [2017]). In the previous section, we have presented the MPEG-2 TS standard, which is effective for streaming multimedia

content for many users. However, in recent years, the MPEG-2 system standard is facing several challenges due to the new multimedia service environment. For example, new video formats such as 4Kx8K video format have been adopted by the video services. The pre-multiplexed stream of 188-byte fixed-size MPEG-2 TS packets is not quite suitable for IP-based delivery for the new video format due to the small and fixed packet size and rigid packetization and multiplexed rules. Also, it is difficult to transfer multilayer coded data such as scalable video as well as multiview video via multi-delivery channels. To address these emerging changes in multimedia service environments, the MMT standard has been developed as a part of MPEG-H to support *High Efficiency Video Coding* (HEVC) video (Nakachi 2013) (ISO/IEC 23008-1 [2017]). The MPEG MMT succeeds MPEG-2 TS as the media transport solution for broadcasting and IP network content distribution, with the aim of serving new applications like UHD, second screen, ..., etc., with full support of HTML5 and simplification of packetization and synchronization with a pure IP-based transport.

In the MMT standard, a set of tools to enable the building of multimedia delivery services has been developed. These tools are spread over four different functional areas: composition, encapsulation, delivery, and signaling. These tools may be used as a whole or just a subset according to the specific needs for a multimedia service. Figure 24.15 shows the different functions as well as their relationships to existing protocols and standards.

In the encapsulation functional area, the logical model and its associated encapsulation format for timed and non-timed media content are specified. The self-contained encapsulation structure enabling independent consumption of media data is included in the format. In the delivery functional area, the application layer transport protocol and the payload format are specified. The composition function is used to address delivery of synchronization information of the contents composed of various contents components. To efficiently deliver flexible synchronization information supporting such contents, the widely adopted presentation language, HTML5 with some extension is used. The technologies for signaling function specify the format of signaling messages carrying information for media content consumption such as specific location and delivery condition of media content.

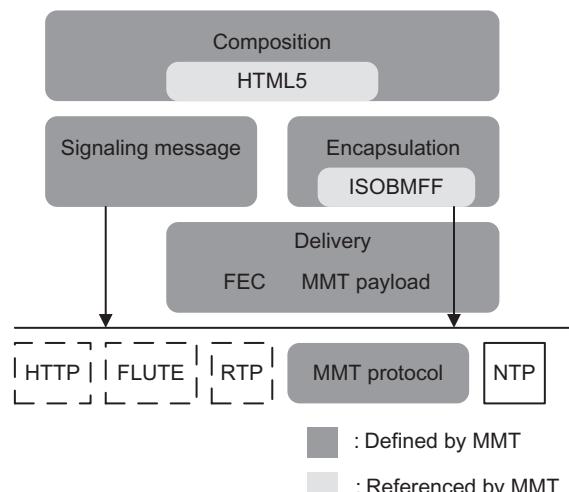


FIGURE 24.15
MMT protocol stack (ISO/IEC 23008-1 [2017]).

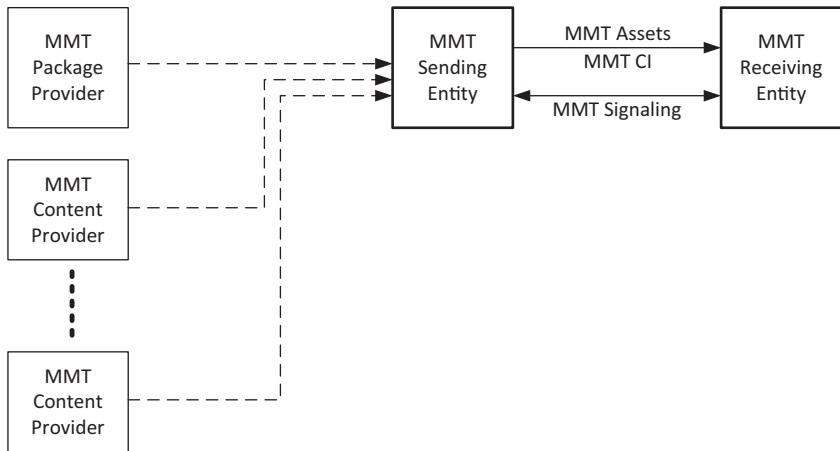


FIGURE 24.16
The end-to-end architecture of MMT (ISO/IEC 23008-1 [2017]).

Figure 24.16 describes the end-to-end architecture for the MMT standard. The MMT content providers and package provider provide the input information to the MMT sending entity. The sending entity is responsible for delivering the package to the receiving entity as packet flows. The sending entity collects the content from the content provider based on the composition information (CI) provided by the package provider. The signalling messages may be used to control the delivery session and the presentation of the package between the MMT sending entity and the MMT receiving entities. The standard only defines the interfaces between the sending entity and the receiving entity for the different functionalities.

24.4.2 MMT Content Model

It is the same as in MPEG-2 TS, the MMT is also a packet-based system. A package is the collection of coded media data and associated information including one CI, one or more assets, and for each asset an associated asset delivery characteristic (ADC) as shown in Figure 24.17.

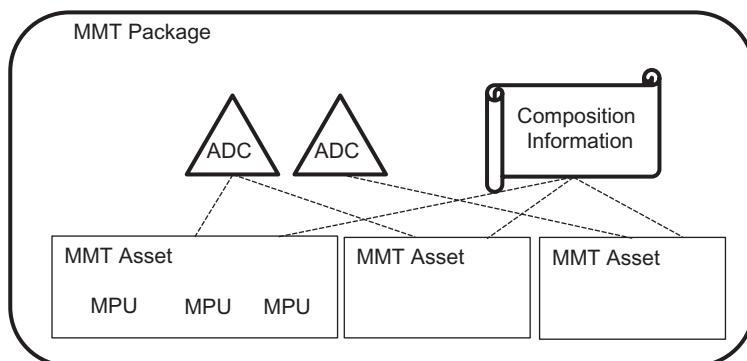


FIGURE 24.17
Overview of package (ISO/IEC 23008-1 [2017]).

From Figure 24.17, it can be seen that the contents in the package are MMT assets. An MMT asset is a component of a package that encapsulates coded media data such as audio or video or a web page data of timed or non-timed nature. An asset contains one or more MPUs whose asset ID is the same. The media processing unit (MPU) is media data, which may be independently and completely processed by an MMT entity and consumed by the media codec layer including decoding and presentation. If an MPU contains timed media, it will have at least one random-access point. The first byte of an MPU shall be a random-access point for processing by an MMT entity as well as decryption.

The CI is used to specify the spatial and temporal relationship among the assets for consumption and presentation by using HTML5 with extensions, so the CI may also be used to determine the delivery order of assets.

The ADCs will be used to provide the information for efficient transmission of assets. As it is seen from Figure 24.17, multiple assets can be associated with a single ADC, but a single asset shall not be associated with multiple ADCs.

24.4.3 Encapsulation of MPU

In this MMT standard, an MPU is encapsulated as a single ISOBMFF file. The MPU payload format is shown in Figure 24.18. In general, the contents stored in ISOBMFF can be streamed by MMT protocol. As it is seen in the Figure 24.18, the sequence number and asset ID of the MPU can be obtained in the ‘mmpu’ box, which is used to uniquely identify the MPU encapsulated in the file. Figure 24.18 also depicts two example MMT encapsulations, one for timed and one for non-timed media. For the timed media, a ‘sidx’ box may

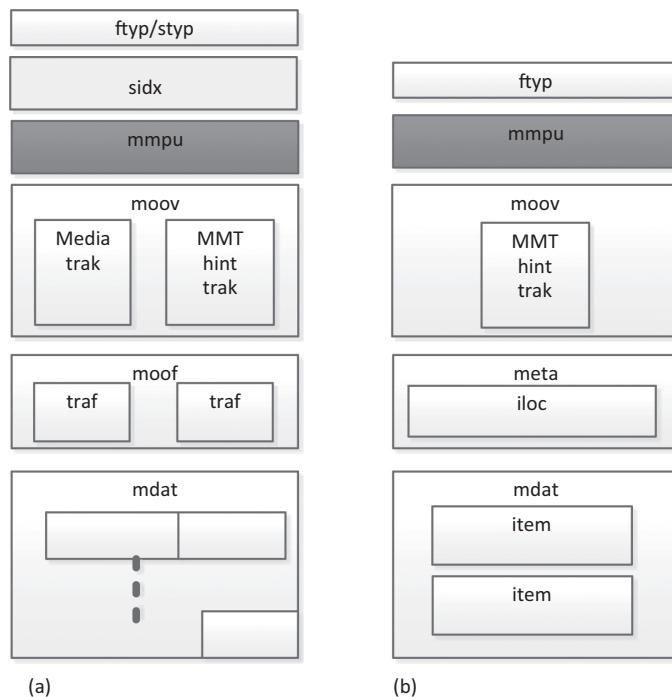


FIGURE 24.18
(a, b) Encapsulation of MPU (ISO/IEC 23008-1 [2017]).

be present to index movie fragments comprising MPU. As each MPU is self-contained, each file encapsulating MPU shall include the initialization data by using the 'ftyp,' 'styp,' and 'moov' boxes. The 'moov' box shall contain all codec configuration information for decoding and presentation of media data in MPU. For packetized delivery of MPU, MMT hint track provides the information to convert encapsulated MPU to MMT payloads and MMT packets.

24.4.4 Packetized Delivery of Package

The MPEG MMT standard defines the MMT payload format. The MMT payload format is a generic payload format. This format can be used to packetize any coded media data that is encapsulated as an MPU into a package for supporting media content streaming. For the details, the MMT payload has the following features:

- It can be used as a payload format for RTP or MMT and other packet transport protocols.
- It is also used to packetize signaling messages. The MMT protocol defines an application layer transport protocol supporting streaming delivery of the package through packet-based heterogeneous delivery network including IP network environments.
- The MMT protocol provides essential features for delivery of the package such as protocol-level multiplexing that enables various assets to be delivered over a single MMT packet flow, delivery timing model independent of presentation time to adapt to a wide range of network jitter, and information to support QoS.
- Since it is a generic payload, it can be used to packetize and carry assets and other information for consumption of the package using MMT protocol or other existing application layer transport protocol such as RTP.
- The MMT payload can be used to carry MPUs, signaling messages, FEC repair symbols, etc. For each data type, a single data unit for delivery is defined.
- The size of MMT payload header is fixed excluding header-extension field when single data unit is carried. The size of MMT payload header is variable when aggregation and fragmentation is performed. When aggregation or fragmentation is performed, the offset to the first byte of data implicitly indicates the size of payload header. The MMT payload can also include the padding bytes at the end of the payload. The size of padding byte is calculated by using the underlying transport layer protocol packet size.
- The MMT protocol is an application layer transport protocol designed to efficiently and reliably deliver the packages. This protocol can be used for the delivery of both timed and non-timed media data. The MMT protocol also addresses several essential problems of coded content delivery such as multiplexing, network jitter calculation, and QoS indication. The MMT protocol may run on top of the UDP and IP protocols.
- Because of the MMT protocol may run on top of the UDP and IP protocols and due to the wide variety of applications, congestion control is not specified in this standard but is rather left up to the implementation of sending entities. Several methods have been used to support congestion control. These include sender and receiver feedback to estimate delay, delay jitter and packet loss, receiver feedback

controlled through setting fraction of reporting receivers, inherent support for stream thinning and bitstream switching, and inherent support for receiver-driven layered multicasting through sub-flows that can be remixed at receiver effortlessly.

24.4.5 Cross Layer Interface

The MPEG MMT standard defines an interface for exchanging cross layer information between the application layer and the underlying network layer. The interface allows for exchanging the cross-layer information in the way of top-down or bottom-up flow. The cross-layer information can be used to optimize the overall delivery of the media data.

24.4.6 Signaling

The MMT signaling defines the set of message formats to be used to provide the information necessary for the delivery and consumption of the package. Six messages related to the consumption of the package are defined:

- Package Access (PA) message: It includes all tables required for package access including MMT Package Table (MPT) and MMT Composition Information Table.
- MMT Composition Information (MCI) message: It includes MCI table encapsulating a complete CI or a subset of CI. It may also include MPT corresponding MCI table for fast package consumption.
- MPT message: It includes MMT Package Table providing whole information or a part of information required for a single package consumption.
- Clock Relation Information (CRI) message: It includes CRI Table providing the CRI used for the mapping between the network time protocol (NTP) Clock and MPEG-2 System Time Clock.
- Device Capability Information (DCI) message: It includes DCI table providing the required DCI for a package consumption.
- Security Software Request (SSWR) message: It is used to request security software for consuming MMT package or asset by an MMT-receiving entity. It can also include PA table or MPT.

Six messages related to the delivery of the package are defined:

- Measurement Configuration (MC) message: It provides information to configure a measurement.
- Application Layer Forward Error Correction (AL-FEC) message: It provides AL-FEC configuration information.
- Hypothetical Receiver Buffer Model (HRBM) message: It provides information to configure HRBM operation.
- Automatic Repeat Request (ARQ) message: It provides information required for ARQ operation.
- Reception Quality Feedback (RQF) message: It defines a format of measurement report from a receiving entity.

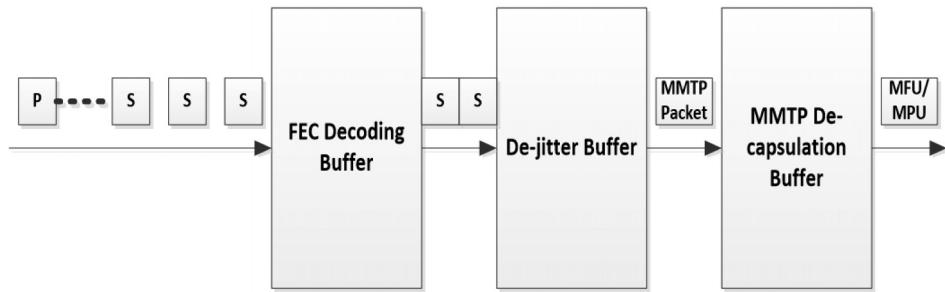


FIGURE 24.19
MMT protocol hypothetical receiver model.

- Network-Aware Media Feedback (NAMF) message: It defines a format of NAM parameter report from a receiving entity.

The detailed information about these signal formats can be found in the standard specification (ISO/IEC 23008-1 [2017]).

24.4.7 Hypothetical Receiver Buffer Model

Each network has its own transmission delay and error characteristics, which may result in various combinations of overall delays between sender and receiver in a hybrid delivery. The hypothetical buffer model is enabling a service to control the overall delay for delivery given various transmission jitters, transmission delay, and error recovery delay for each delivery network involved. The HRBM is shown in the Figure 23.19. The buffer model consists of three components: FEC decoding buffer, de-jitter buffer, and MMTP de-capsulation buffer. For the FEC decoding, the buffer size has to satisfy the requirement for storing sufficient incoming packets and repaired data to perform FEC decoding. The de-jitter buffer is used to ultimately ensure that MMT packets experience a fixed transmission delay from source to output of the MMT protocol stack at a maximum transmission delay. The MMTP packet de-encapsulation buffer is used to perform MMTP packet processing before output to the upper layers.

To ensure operation, a fixed end-to-end delay, and limited memory requirement for buffering of incoming MMT packets, the MMT sender runs the HRBM to ensure that any processing it performs on the packet stream is within the reception constraints in the MMT receiver. The sender determines the required buffering delay and the required buffer size and signals this information to the receivers. The HRBM defines operations of the buffers at the receiver to ensure that at any time the buffer occupancy is within the buffer size requirement.

24.5 Dynamic Adaptive Streaming over HTTP

In this section, we introduce an MPEG transport standard, MPEG DASH, which is used for the application of video streaming over the Internet (ISO/IEC DIS 23009-1.2 [2014]).

24.5.1 Introduction

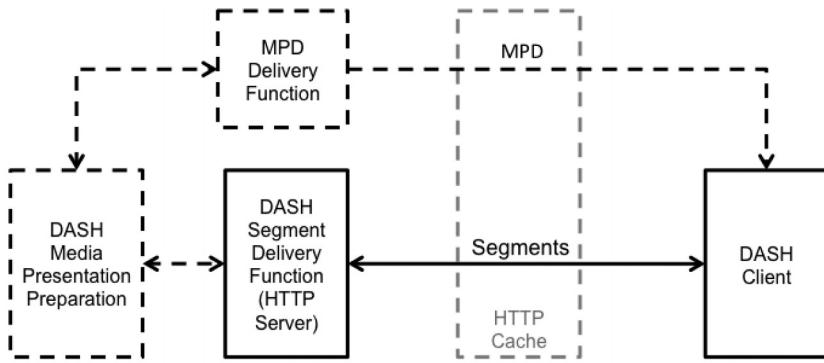
There are many challenges for video streaming over the Internet. The first challenge is the accessibility of video. Video may not be accessible due to several problems such as video behind firewall, plugins not available, insufficient bandwidth, and wrong format. The second challenge is low quality of experience such as long start-up latency, frequent rebuffering, and low playback quality. The MPEG DASH standard has been developed to address these challenges. It should be noted that DASH is not a system, protocol, presentation, codec, interactivity, and client specification. Actually, DASH is an enabler to provide formats to enable efficient and high-quality delivery of streaming service over the Internet. It is considered as one component of an end-to-end service. DASH also enables many issues including reuse of existing technologies such as codecs, DRM, containers, deployment on top of content delivery networks (HTTP-CDNs), selection based on the network and device capability, seamless switching, and many others.

HTTP is designed to enable communications between clients and servers and works as a request-response protocol between a client and server. For example, a web browser may be the client, and an application on a computer that hosts a web site may be the server. When a browser proposes an HTTP request to the web, then the web responds to the browser, this is an example of communication between clients and servers. Two commonly used methods for a request-response between a client and server are: GET and POST. GET requests data from a specified resource while POST submits data to be processed to a specified resource.

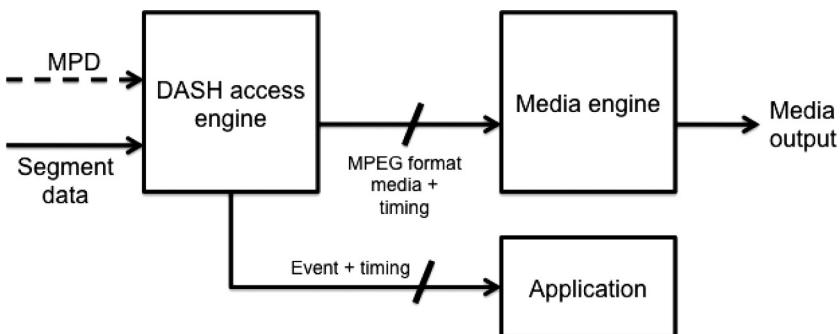
The MPEG DASH standard is referred to as ISO/IEC standard ISO/IEC 23009-1 (ISO/IEC DIS 23009-1.2 [2014]), which specifies two formats for the media presentation description (MPD) and segments. The first format is the MPD, which describes a media presentation, i.e., a bounded or unbounded presentation of media content. The second format is the segment format, which specifies the format of the entity body of the HTTP response to an HTTP GET request to a resource identified in the MPD. The segments are like the packets in MPEG systems that typically contain efficiently coded media data and metadata conforming to or at least closely aligned with common media formats. It should be noted that the MPEG-DASH specification only defines the MPD and the segment formats. The delivery of the MPD and the media encoding formats containing the segments as well as the client behavior for fetching, adaptation heuristics, and playing the content are outside of MPEG-DASH's scope (Sodagar 2011).

The MPD provides sufficient information for a client to provide a streaming service to the user by accessing the segments through the protocol specified in the scheme of the defined resources. In the context of this part of ISO/IEC 23009 the assumed protocol is HTTP/1.1. Such a client is referred to as a DASH Client in the remainder of 23009-1. However, this part of ISO/IEC 23009 does not provide a normative specification for such a client.

Figure 24.20 gives an example system that shows a possible architecture to use DASH formats defined in the ISO/IEC 23009. In the figure, the boxes with solid lines are the normative parts of the standard; they host or process the formats defined in this specification while the dashed boxes are conceptual or transparent. The standard deals with the definition of formats that are accessible on the interface to the DASH Client, indicated by the solid lines. In this reference architecture, the DASH Client has access to an MPD. The MPD provides sufficient information for the DASH Client that provides a streaming service to the user by requesting segments from an HTTP server and demultiplexing, decoding, and rendering the included media streams.

**FIGURE 24.20**

Example system for DASH formats (ISO/IEC DIS 23009-1.2 [2014]).

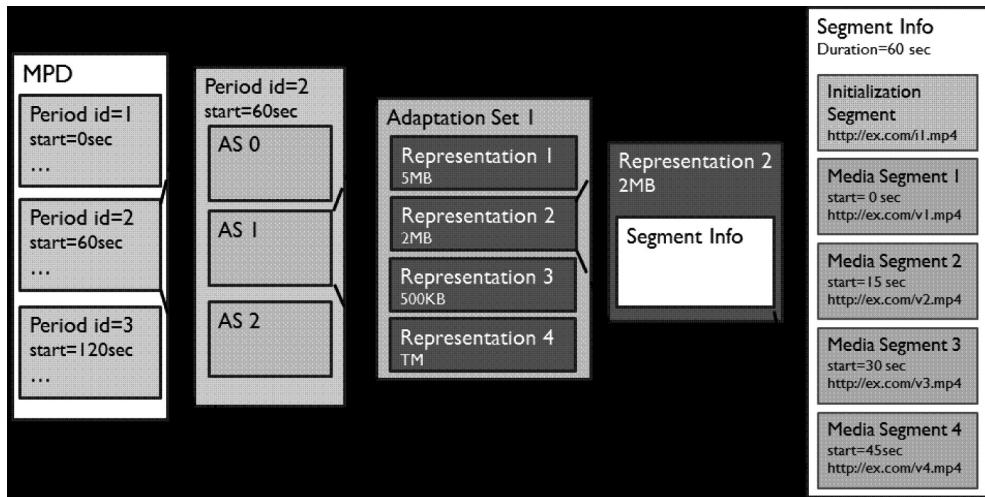
**FIGURE 24.21**

DASH client model.

The MPEG DASH is based on a client-centric approach since the client has the best view of network conditions. The informative client model introduced by ISO/IEC 23009 [x] is shown in [Figure 24.21](#). In this figure the MPD and segments or parts of segments input to the DASH access engine. The output of the DASH access engine consists of media in MPEG container formats (ISO Base Media File Format or MPEG-2 Transport Stream), and timing information that maps the internal timing of the media to the timeline of the media presentation. In addition, the DASH access client may also receive and extract events that are related to the media time. The events may be processed in the DASH client or may be forwarded to an application in the execution environment of the DASH client.

24.5.2 Media Presentation Description

As indicated in [Figure 24.4](#) DASH client model, The MPS Media is a document that contains metadata required by a DASH client with the format accessible for a streaming service to the user. In dynamic HTTP streaming applications, multimedia contents may consist of several components such as video, audio, and text; also, these contents may be compressed with different bitrates for the servers. The different characteristics of the multimedia contents are described and specified by the MPD of MPEG DASH, which is an

**FIGURE 24.22**

The MPD hierarchical data model. (From Sodagar, I., *J. IEEE Multimedia*, 18, 62–67, 2011.)

Extensible Markup Language (XML) document with a hierarchical data model as shown in Figure 24.22. From Figure 24.22, it can be seen that the MPD consists of a sequence of one or more periods, where a period is an interval of the program along the temporal axis. Each period contains a starting time and duration and one or more adaptation sets. An adaptation set contains the information about one or more media components and its various encoded alternatives such as videos or audios with different bitrates or different resolutions. Each adaptation set may contain one or more representations and each representation consists of one or more segments. Each segment has a URI, which is an addressable location on a server and can be downloaded using HTTP GET or HTTP GET with byte ranges. With this data model, the DASH client parses the MPD XML document first and then selects the set of representations based on descriptive elements in the MPD, the capabilities of the client and choices of its user. The client then creates a time-line for starting to play the multimedia contents by requesting appropriate media segments. The description of each representation contains the information about the segments, which are met the requests to be formulated in terms of HTTP URL and byte range. For live presentations, the MPD also provides availability of start time and end time, approximate media start time, and fixed or variable duration of segments.

24.5.3 Segment Format

The segment format is one of the normative parts of MPEG DASH standard that specifies the syntax and semantics of the resources that are associated with HTTP-URLs identified by the MPD. The media components such as videos or audios are encoded and multiplexed to the bitstreams, which are divided to multiple segments. A segment can be seen as the entity body of the response to the DASH client's HTTP GET or a partial HTTP GET. The first segment might be an initialization segment that contains the required information for initialization of the DASH client's media decoder. It does not include any actual media data. The consecutive segments contain the media contents. Each media segment is assigned a unique URL (possibly with byte range), an index, and explicit or implicit start

time and duration. In order to function as random access, each media segment also contains at least one stream access point (SAP). The SAP is a random-access point or switch to the point in the bit-stream where decoding starts from that point forward.

In some applications, one may need to download segments in multiple parts. For this purpose, the MPEG DASH standard defines a method of signaling sub-segments using a segment index box [8], which describes sub-segments and SAPs in the segment by signaling their durations and byte offsets. The index information of a segment can be put either in the single box at the beginning of that segment or spread among many boxes in the segment, and it can be used to request sub-segments using partial HTTP GETS. The different methods such as hierarchical, daisy-chain, or hybrid of spreading the index information have been developed to avoid putting a large data box at the beginning of the segment that may cause a possible initial download delay.

Finally, it should be noted that the MPEG DASH uses existing HTTP web server infrastructure. Therefore, the multimedia contents can be delivered to the different Internet-connected devices such as TV set-top boxes, desktop or laptop computers, cellphones, or tablets via the Internet coping with variable Internet receiving conditions.

24.6 Summary

In this chapter, the MPEG system and transportation issues have been discussed. The typical systems, MPEG-2 system, MPEG-4 system, MPEG MMT, and MPEG DASH, have been introduced. The major task of system and transportation layer is to multiplex and de-multiplex video, audio, and other data to a single bitstream with synchronization timing information and further packetized into packages for delivery over application layer protocols. The early MPEG systems are designed for the broadcasting applications, but new standards such as MMT and DASH are mainly designed for the application of media content streaming over networks.

Exercises

- 24.1 What are two major system streams provided by the MPEG-2 system? Describe some application examples for these two streams and explain the reasons.
- 24.2 The MPEG-2 system bitstream is a self-contained bitstream to facilitate synchronous playback of video, audio, and related data; describe what kind of timing signals are contained in the bitstream to achieve the goal of synchronization.
- 24.3 How does the MPEG-2 system deal with different system clocks between the encoder and decoder? Describe what a system may do when the decoder clock is running too slow or too fast?
- 24.4 Why is the 27 MHz system clock in MPEG-2 represented in two parts: 33-bit + 9-bit extension?
- 24.5 What is bitstream splicing of a transport stream? Give several application examples of bitstream splicing and indicate the problems that may arise.

- 24.6 Describe the difference between the MPEG-2 system and MPEG-4 system.
 - 24.7 Describe the reasons for developing MPEG MMT.
 - 24.8 Describe the reasons for developing MPEG DASH.
-

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