Lindo Systems, Inc.

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## 1 Introduction

GAMS/LINDOGlobal finds guaranteed globally optimal solutions to general nonlinear problems with continuous and/or discrete variables. GAMS/LINDOGlobal supports most mathematical functions, including functions that are nonsmooth, such as abs(x) and or even discontinuous, such as floor(x). Nonlinear solvers employing methods like successive linear programming (SLP) or generalized reduced gradient (GRG) return a local optimal solution to an NLP problem. However, many practical nonlinear models are non-convex and have more than one local optimal solution. In some applications, the user may want to find a global optimal solution.

The LINDO global optimization procedure (GOP) employs branch-and-cut methods to break an NLP model down into a list of subproblems. Each subproblem is analyzed and either a) is shown to not have a feasible or optimal solution, or b) an optimal solution to the subproblem is found, e.g., because the subproblem is shown to be convex, or c) the subproblem is further split into two or more subproblems which are then placed on the list. Given appropriate tolerances, after a finite, though possibly large number of steps a solution provably global optimal to tolerances is returned. Traditional nonlinear solvers can get stuck at suboptimal, local solutions. This is no longer the case when using the global solver.

GAMS/LINDOGlobal can automatically linearize a number of nonlinear relationships, such as  $\max(x,y)$ , through the addition of constraints and integer variables, so the transformed linearized model is mathematically equivalent to the original nonlinear model. Keep in mind, however, that each of these strategies will require additional computation time. Thus, formulating models, so they are convex and contain a single extremum, is desirable. In order to decrease required computing power and time it is also possible to disable the global solver and use GAMS/LINDOGlobal like a regular nonlinear solver.

GAMS/LINDOGlobal has a multistart feature that restarts the standard (non-global) nonlinear solver from a number of intelligently generated points. This allows the solver to find a number of locally optimal points and report the best one found. This alternative can be used when global optimization is costly. A user adjustable parameter controls the maximum number of multistarts to be performed.

LINDOGlobal automatically detects problem type and uses an appropriate solver, e.g., if you submit an LP model to LINDOGlobal, it will be solved as an LP at LP speed, regardless of what you said in the "solve using" statement. With the NLP parameter  $NLP_{-}QUADCHK$  turned on, LINDOGlobal can detect hidden quadratic expressions and automatically recognize convex QCPs, as well as second-order cones (SOCP), like in Value-at-Risk models, allowing dramatically faster solution times via the barrier solver. When such models have integer variables, LINDOGlobal would use the barrier solver to solve all subproblems leading to significantly improved solution times when compared to the case with the standard NLP solver.

## 1.1 Licensing and software requirements

In order to use GAMS/LINDOGlobal, users need a GAMS/LINDOGlobal license. Additionally a GAMS/CONOPT license is required for solving nonlinear subproblems. The GAMS/LINDOGlobal license places upper limits on model size of 3,000 variables and 2,000 constraints. The GAMS/LINDOGlobal license does not include the Barrier solver option. LINDOGlobal would be able to use the barrier solver when the user has a separate license for the GAMS/MOSEK barrier solver.

## 1.2 Running GAMS/LINDOGlobal

GAMS/LINDOGlobal is capable of solving models of the following types: LP, MIP, RMIP, NLP, DNLP, QCP, MIQCP, RMINLP and MINLP. If GAMS/LINDOGlobal is not specified as the default solver for these models, it can be invoked by issuing the following command before the solve statement:

```
option xxx=lindoglobal;
```

where xxx is one of: LP, MIP, RMIP, NLP, DNLP, QCP, MIQCP, RMINLP, or MINLP.

You can also find global optima to math programs with equilibrium or complementarity constraints, type MPEC, by using the GAMS/NLPEC translator in conjunction with LINGOGlobal. You use NLPEC to translate complementarities into standard mathematical statements, e.g.  $h^*y = 0$ , and then use LINDOGlobal as the DNLP(Discontinuous Nonlinear) solver to solve the translated model. The following little GAMS model illustrates:

```
$TITLE simple mpec example
variable f, x1, x2, y1, y2; positive
variable y1; y2.lo = -1; y2.up = 1;

equations cost, g, h1, h2;

cost.. f =E= x1 + x2;
   g.. sqr(x1) + sqr(x2) =L= 1;
   h1.. x1 =G= y1 - y2 + 1;
   h2.. x2 + y2 =N= 0;

* declare h and y complementary
model example / cost, g, h1.y1, h2.y2 /;

option mpec= nlpec;
option dnlp=lindoglobal;
solve example using mpec min f;
```

## 2 Supported nonlinear functions

GAMS/LINDOGlobal supports most nonlinear functions in global mode, including +, -, \*, /, floor, modulo, sign, min, max, sqr, exp, power, ln, log, sqrt, abs, cos, sin, tan, cosh, sinh, tanh, arccos, arcsin, arctan and logic expressions AND, OR, NOT, and IF. Be aware that using highly nonconvex functions may lead to long solve times.

# 3 GAMS/LINDOGlobal output

Starting global search ...

Initial upper bound on objective: +2.931083e-002 Initial lower bound on objective: -3.167052e+022

The log output below is obtained for the NLP model mhw4d.gms from the GAMS model library using LINDOs global solver.

```
8Apr10 23.4.0 WIN 17007.17023 VS8 x86/MS Windows
LINDOGLOBAL
   LINDOGLOBAL Driver
   Lindo Systems Inc, www.lindo.com
Lindo API version 6.0.1.406 built on Mar 17 2010 22:51:09
Barrier Solver Version 5.0.0.127, Nonlinear Solver Version 3.14T
Platform Windows x86
Number of constraints:
                                                                                     0 (ne:0)
                                   le:
                                             0, ge:
                                                          0, eq:
                                                                        3, rn:
Number of variables :
                             5
                                             0, ub:
                                                          0, fr:
                                                                        5, bx:
                                                                                     0 (fx:0)
                                   lb:
Number of nonzeroes
                                   density=0.0053(%)
Nonlinear variables :
Nonlinear constraints:
Nonlinear nonzeroes :
                              5+5
Starting global optimization ...
Number of nonlinear functions/operators: 3
EP_MULTIPLY EP_POWER EP_SQR
Starting GOP presolve ...
Pre-check unboundedness
Computing reduced bound...
Searching for an initial solution...
Initial objective value: 0.029311
Starting reformulation ...
Model
                                                 Atomic
                                                               Convex
                         Input
                                    Operation
Number of variables
                             5
                                            6
                                                     20
                                                                  20
Number of constraints:
                             3
                                            4
                                                     18
                                                                  46
                                            0
integer variables
                                                      0
                                                                    0
nonlinear variables :
                             5
                                            5
                                                      9
                                                                    0
```

	#ITERs	TIME(s)	LOWER BOU	ND UPPER	R BOOND	BUXES				
	1 41		-3.167052e+ +2.630106e-			1 35 (*	I)			
Terminating global search										
Global optimum found										
	bjective		:	0.029	3108307216					
В	est Bound		:	0.028	3736126217					
F	actors (o	k,stb)	:		892	2 (100.00,99.78)				
Simplex iterations					4060					
Barrier iterations					0					
Nonlinear iterations					627					
Box iterations					41					
Total number of boxes					35					
M	ax. Depth		:		8					
T	otal time	(sec.)	:		0					

After determining the different kinds of nonlinear operators LINDOGlobal tries to linearize these within the presolving. When a feasible starting point is found the optimization starts and the log provides information about the progress. At the end it is reported if an optimum could be found and then the results as well as the used resources are summarized.

# 4 Summary of LINDOGlobal Options

LINDOGlobal offers a diverse range of user-adjustable parameters to control the behavior of its solvers. While the default values of these parameters work best for most purposes, there may be cases the users prefer to work with different settings for a subset of the available parameters. This section gives a list of available LINDOGlobal parameters, categorized by type, along with their brief descriptions. A more detailed description is given in the section that follows.

## 4.1 LINDOGlobal Options File

In order to set LINDOGlobal options, you need to set up an option file *lindoglobal.opt* in your GAMS project directory. You must indicate in the model that you want to use the option file by inserting before the solve statement, the line:

```
<modelname>.optfile = 1;
```

#### <modelname>

where

is the name of the model referenced in the model statement. The option file is in plain text format containing a single LINDOGlobal option per line. Each option identifier is followed by its target value with space or tab characters separating them. The lines starting with \* character are treated as comments.

A sample option file *lindoglobal.opt* looks like below

\* Use(1) or Disable(0) global optimization for NLP/MINLP models

USEGOP C

\* Enable Multistart NLP solver

NLP\_SOLVER 9

\* Allow a maximum of 3 multistart attempts

MAXLOCALSEARCH 3

\* Set an overall time limit of 200 secs.

SOLVER\_TIMLMT 200

## 4.2 General Options

DECOMPOSITION\_TYPE decomposition to be performed on a linear or mixed integer model

SOLVER\_IUSOL flag for computing basic solution for infeasible model

SOLVER\_TIMLMT time limit in seconds for continuous solver

SOLVER\_FEASTOL feasibility tolerance SOLVER\_RESTART starting basis flag SOLVER\_OPTTOL dual feasibility tolerance

## 4.3 LP Options

SPLEX\_SCALE scaling flag

SPLEX\_ITRLMT simplex iteration limit

SPLEX\_PPRICING pricing option for primal simplex method

SPLEX\_REFACERQ number of simplex iterations between two consecutive basis

re-factorizations

PROB\_TO\_SOLVE controls whether the explict primal or dual form of the given LP

problem will be solved

SPLEX\_DPRICING pricing option for dual simplex method SPLEX\_DUAL\_PHASE controls the dual simplex strategy

LP\_PRELEVEL controls the amount and type of LP pre-solving SOLVER\_CUTOFFVAL solver will exit if optimal solution is worse than this

SOLVER\_USECUTOFFVAL flag for using cutoff value

## 4.4 MIP Options

MIP\_TIMLIM time limit in seconds for integer solver

MIP\_AOPTTIMLIM time in seconds beyond which the relative optimality tolerance

will be applied

MIP\_LSOLTIMLIM time limit until finding a new integer solution

MIP\_PRELEVEL controls the amount and type of MIP pre-solving at root node

MIP\_NODESELRULE specifies the node selection rule
MIP\_INTTOL absolute integer feasibility tolerance
MIP\_RELINTTOL relative integer feasibility tolerance
MIP\_RELOPTTOL MIP relative optimality tolerance

MIP\_PEROPTTOL MIP relative optimality tolerance in effect after MIP\_AOPTTIMLIM

seconds

MIP\_MAXCUTPASS\_TOP number passes to generate cuts on the root node

MIP\_MAXCUTPASS\_TREE number passes to generate cuts on the child nodes percentage of constraint cuts that can be added MIP\_ADDCUTPER MIP\_ADDCUTPER\_TREE percentage of constraint cuts that can be added at child nodes MIP\_MAXNONIMP\_CUTPASS number of passes allowed in cut-generation that does not improve current relaxation MIP\_CUTLEVEL\_TOP combination of cut types to try at the root node when solving a MIP MIP\_CUTLEVEL\_TREE combination of cut types to try at child nodes in the B&B tree when solving a MIP MIP\_CUTTIMLIM time to be spent in cut generation threshold value for the depth of nodes in the B&B tree MIP\_CUTDEPTH MIP\_CUTFREQ frequency of invoking cut generation at child nodes MIP\_HEULEVEL specifies heuristic used to find integer solution MIP\_CUTOFFOBJ defines limit for branch & bound MIP\_USECUTOFFOBJ flag for using branch and bound limit depth from the root in which strong branching is used MIP\_STRONGBRANCHLEVEL MIP\_TREEREORDERLEVEL tree reordering level MIP\_BRANCHDIR first branching direction MIP\_TOPOPT optimization method to use when there is no previous basis optimization method to use when doing reoptimization MIP\_REOPT MIP\_SOLVERTYPE optimization method to use when solving mixed-integer models MIP\_KEEPINMEM flag for keepin LP bases in memory MIP\_BRANCHRULE rule for choosing the variable to branch cutoff value as a percentage of the reduced costs MIP\_REDCOSTFIX\_CUTOFF MIP\_ADDCUTOBJTOL required objective improvement to continue generating cuts minimum time in seconds to be spent in finding heuristic solutions MIP\_HEUMINTIMLIM MIP\_BRANCH\_PRIO controls how variable selection priorities are set and used MIP\_SCALING\_BOUND maximum difference between bounds of an integer variable for enabling scaling MIP\_PSEUDOCOST\_WEIGT weight in pseudocost computations for variable selection MIP\_LBIGM Big-M value used in linearizing nonlinear expressions MIP\_DELTA near-zero value used in linearizing nonlinear expressions MIP\_DUAL\_SOLUTION flag for computing dual solution of LP relaxation MIP\_BRANCH\_LIMIT limit on the total number of branches to be created during branch and bound MIP\_ITRLIM iteration limit for branch and bound MIP\_AGGCUTLIM\_TOP max number of constraints involved in derivation of aggregation cut at root node MIP\_AGGCUTLIM\_TREE max number of constraints involved in derivation of aggregation cut at tree nodes MIP\_ANODES\_SWITCH\_DF threshold on active nodes for switching to depth-first search MIP\_ABSOPTTOL MIP absolute optimality tolerance MIP\_MINABSOBJSTEP value to update cutoff value each time a mixed integer solution is found MIP\_PSEUDOCOST\_RULE specifies the rule in pseudocost computations for variable selection frequency of enumeration heuristic MIP\_USE\_ENUM\_HEU MIP\_PRELEVEL\_TREE amount and type of MIP pre-solving at tree nodes MIP\_REDCOSTFIX\_CUTOFF\_TREE cutoff value as a percentage of the reduced costs at tree nodes controls if all MIP calculations would be based on absolute  $MIP\_USE\_INT\_ZERO\_TOL$ integer feasibility tolarance MIP\_USE\_CUTS\_HEU controls if cut generation is enabled during MIP heuristics MIP\_BIGM\_FOR\_INTTOL threshold for which coefficient of a binary variable would be considered as big-M MIP\_STRONGBRANCHDONUM minimum number of variables to try the strong branching on MIP\_MAKECUT\_INACTIVE\_COUNT threshold for times a cut could remain active after successive reoptimization

controls fill-in introduced by eliminations during pre-solve

MIP\_PRE\_ELIM\_FILL

## 4.5 NLP Options

NLP\_SOLVE\_AS\_LP flag indicating if the nonlinear model will be solved as an LP

NLP\_SOLVER type of nonlinear solver NLP\_SUBSOLVER type of nonlinear subsolver

NLP\_PSTEP\_FINITEDIFF value of the step length in computing the derivatives using finite

differences

NLP\_DERIV\_DIFFTYPE flag indicating the technique used in computing derivatives with

finite differences

NLP\_REDGTOL feasibility tolerance for nonlinear constraints
NLP\_USE\_CRASH flag for using simple crash routines for initial solution
NLP\_USE\_STEEPEDGE flag for using steepest edge directions for updating solution
NLP\_USE\_SLP flag for using sequential linear programming step directions for

updating solution

NLP\_USE\_SELCONEVAL flag for using selective constraint evaluations for solving NLP

NLP\_PRELEVEL controls the amount and type of NLP pre-solving

NLP\_ITRLMT nonlinear iteration limit

NLP\_LINEARZ extent to which the solver will attempt to linearize nonlinear models

NLP\_STARTPOINT flag for using initial starting solution for NLP

NLP\_QUADCHK flag for checking if NLP is quadratic
NLP\_AUTODERIV defining type of computing derivatives
NLP\_MAXLOCALSEARCH maximum number of local searches

NLP\_USE\_LINDO\_CRASH flag for using advanced crash routines for initial solution

NLP\_STALL\_ITRLMT iteration limit before a sequence of non-improving NLP iterations is

declared as stalling

NLP\_AUTOHESS flag for using Second Order Automatic Differentiation for solving NLP

## 4.6 Global Options

OPTTOL optimality tolerance
FLTTOL floating-point tolerance

BOXTOL minimal width of variable intervals
WIDTOL maximal width of variable intervals
DELTATOL delta tolerance in GOP convexification

BNDLIM max magnitude of variable bounds used in GOP convexification

TIMLIM time limit in seconds for GOP branch-and-bound OPTCHKMD criterion used to certify the global optimality

BRANCHMD direction to branch first when branching on a variable

MAXWIDMD maximum width flag for the global solution PRELEVEL amount and type of GOP presolving POSTLEVEL amount and type of GOP postsolving

BBSRCHMD node selection rule in GOP branch-and-bound

DECOMPPTMD decomposition point selection rule in GOP branch-and-bound

ALGREFORMMD algebraic reformulation rule for a GOP

RELBRNDMD reliable rounding in the GOP branch-and-bound

USEBNDLIM max magnitude of variable bounds flag for GOP convexification BRANCH\_LIMIT limit on the total number of branches to be created in GOP tree

CORELEVEL strategy of GOP branch-and-bound OPT\_MODE mode for GOP optimization

HEU\_MODE heuristic used in global solver
SUBOUT\_MODE substituting out fixed variables

LSOLBRANLIM USEGOP

branch limit until finding a new nonlinear solution use global optimization

## 4.7 Link Options

CHECKRANGE WRITEMPI calculate feasible range for variables write MPI file of processed model

# 5 Detailed Descriptions of LINDOGlobal Options

## DECOMPOSITION\_TYPE (integer)

This refers to the type of decomposition to be performed on a linear or mixed integer model.

```
(default = 1)
```

- 0 Solver decides which type of decomposition to use
- 1 Solver does not perform any decompositions and uses the original model
- 2 Attempt total decomposition
- 3 Decomposed model will have dual angular structure
- 4 Decomposed model will have block angular structure
- 5 Decomposed model will have both dual and block angular structure

#### SPLEX\_SCALE (integer)

This is the scaling flag. Scaling multiplies the rows and columns of the model by appropriate factors in an attempt to avoid numerical difficulties by reducing the range of coefficient values.

```
(default = 1)
```

- 0 Scaling is suppressed
- 1 Scaling is performed

#### SPLEX\_ITRLMT (integer)

This is a limit on the number of iterations the solver will perform before terminating. If this value is a nonegative integer, then it will be used as an upper bound on the number of iterations the solver will perform. If this value is -1, then no iteration limit will be used. The solution may be infeasible.

```
(default = GAMS IterLim)
```

#### SPLEX\_PPRICING (integer)

This is the pricing option to be used by the primal simplex method.

```
(default = -1)
```

- -1 Solver decides the primal pricing method
- 0 Partial pricing
- 1 Devex

## SPLEX\_REFACFRQ (integer)

This is a positive integer scalar referring to the simplex iterations between two consecutive basis refactorizations. For numerically unstable models, setting this parameter to smaller values may help.

```
(default = 100)
```

## PROB\_TO\_SOLVE (integer)

This flag controls whether the explict primal or dual form of the given LP problem will be solved.

```
(default = 0)
```

- 0 Solver decides
- 1 Explicit primal form
- 2 Explicit dual form

## SPLEX\_DPRICING (integer)

This is the pricing option to be used by the dual simplex method.

```
(default = -1)
```

- -1 Solver decides the dual pricing method
- 0 Partial pricing
- 1 Steepest edge

#### SPLEX\_DUAL\_PHASE (integer)

This controls the dual simplex strategy, single-phase versus two-phase.

```
(default = 0)
```

- 0 Solver decides
- 1 Single-phase
- 2 Two-phase

## LP\_PRELEVEL (integer)

This controls the amount and type of LP pre-solving to be used.

```
(default = 126)
```

- +2 Simple pre-solving
- +4 Probing
- +8 Coefficient reduction
- +16 Elimination
- +32 Dual reductions
- +64 Use dual information
- +512 Maximum pass

## SOLVER\_IUSOL (integer)

This is a flag that, when set to 1, will force the solver to compute a basic solution to an infeasible model that minimizes the sum of infeasibilities and a basic feasible solution to an unbounded problem from which an extreme direction originates. When set to the default of 0, the solver will return with an appropriate status flag as soon as infeasibility or unboundedness is detected. If infeasibility or unboundedness is declared with presolver's determination, no solution will be computed.

```
(default = 0)
```

- 0 Return appropriate status if infeasibility is encountered
- 1 Force the solver to compute a basic solution to an infeasible model

#### SOLVER\_TIMLMT (integer)

This is a time limit in seconds for the LP solver. The default value of -1 imposes no time limit.

```
(default = GAMS ResLim)
```

## SOLVER\_CUTOFFVAL (real)

If the optimal objective value of the LP being solved is shown to be worse than this (e.g., if the dual simplex method is being used), then the solver will exit without finding a feasible solution. This is a way of saving computer time if there is no sufficiently attractive solution. SOLVER\_USECUTOFFVAL needs to be set to 1 to activate this value.

```
(default = 0)
```

#### SOLVER\_FEASTOL (real)

This is the feasibility tolerance. A constraint is considered violated if the artificial, slack, or surplus variable associated with the constraint violates its lower or upper bounds by the feasibility tolerance.

```
(default = 1e-7)
```

## SOLVER\_RESTART (integer)

This is the starting basis flag. 1 means LINDO API will perform warm starts using any basis currently in memory. 0 means LINDO API will perform cold starts discarding any basis in memory and starting from scratch.

```
(default = 0)
```

- 0 Perform cold start
- 1 Perform warm start

## SOLVER\_OPTTOL (real)

This is the optimality tolerance. It is also referred to as the dual feasibility tolerance. A dual slack (reduced cost) is considered violated if it violates its lower bound by the optimality tolerance.

```
(default = 1e-7)
```

## SOLVER\_USECUTOFFVAL (integer)

This is a flag for the parameter SOLVER\_CUTOFFVAL

```
(default = 0)
```

- 0 Do not use cutoff value
- 1 Use cutoff value

## NLP\_SOLVE\_AS\_LP (integer)

This is a flag indicating if the nonlinear model will be solved as an LP. 1 means that an LP using first order approximations of the nonlinear terms in the model will be used when optimizing the model with the LSoptimize() function.

```
(default = 0)
```

- 0 NLP will not be solved as LP
- 1 NLP will be solved as LP

#### NLP\_SOLVER (integer)

This value determines the type of nonlinear solver.

```
(default = 7)
```

- 4 Solver decides
- 7 Uses CONOPTs reduced gradient solver
- 9 Uses CONOPT with multistart feature enabled

#### NLP\_SUBSOLVER (integer)

This controls the type of linear solver to be used for solving linear subproblems when solving nonlinear models.

```
(default = 1)
```

- 1 Primal simplex method
- 2 Dual simplex method
- 3 Barrier solver with or without crossover

#### NLP\_PSTEP\_FINITEDIFF (real)

This controls the value of the step length in computing the derivatives using finite differences.

```
(default = 5e-7)
```

#### NLP\_DERIV\_DIFFTYPE (integer)

This is a flag indicating the technique used in computing derivatives with Finite Differences.

```
(default = 0)
```

- 0 The solver decides
- 1 Use forward differencing method
- 2 Use backward differencing method
- 3 Use center differencing method

## NLP\_FEASTOL (real)

This is the feasibility tolerance for nonlinear constraints. A constraint is considered violated if the artificial, slack, or surplus variable associated with the constraint violates its lower or upper bounds by the feasibility tolerance.

```
(default = 1e-6)
```

#### NLP\_REDGTOL (real)

This is the tolerance for the gradients of nonlinear functions. The (projected) gradient of a function is considered to be the zero-vector if its norm is below this tolerance.

```
(default = 1e-7)
```

## NLP\_USE\_CRASH (integer)

This is a flag indicating if an initial solution will be computed using simple crash routines.

```
(default = 0)
```

- 0 Do not use simple crash routines
- 1 Use simple crash routines

## NLP\_USE\_STEEPEDGE (integer)

This is a flag indicating if steepest edge directions should be used in updating the solution.

```
(default = 0)
```

- 0 Do not use steepest edge directions
- 1 Use steepest edge directions

#### NLP\_USE\_SLP (integer)

This is a flag indicating if sequential linear programming step directions should be used in updating the solution.

```
(default = 1)
```

- 0 Do not use sequential linear programming step directions
- 1 Use sequential linear programming step directions

## NLP\_USE\_SELCONEVAL (integer)

This is a flag indicating if selective constraint evaluations will be performed in solving a nonlinear model.

```
(default = 1)
```

- 0 Do not use selective constraint evaluations
- 1 Use selective constraint evaluations

#### NLP\_PRELEVEL (integer)

This controls the amount and type of NLP pre-solving.

```
(default = 126)
```

- +2 Simple pre-solving
- +4 Probing
- +8 Coefficient reduction
- +16 Elimination
- +32 Dual reductions
- +64 Use dual information
- +512 Maximum pass

## NLP\_ITRLMT (integer)

This controls the iteration limit on the number of nonlinear iterations performed.

```
(default = GAMS IterLim)
```

#### NLP\_LINEARZ (integer)

This determines the extent to which the solver will attempt to linearize nonlinear models.

```
(default = 0)
```

- 0 Solver decides
- 1 No linearization occurs
- 2 Linearize ABS MAX and MIN functions
- 3 Same as option 2 plus IF AND OR NOT and all logical operators are linearized

## NLP\_STARTPOINT (integer)

This is a flag indicating if the nonlinear solver should accept initial starting solutions.

```
(default = 1)
```

- 0 Do not use initial starting solution for NLP
- 1 Use initial starting solution for NLP

## NLP\_QUADCHK (integer)

This is a flag indicating if the nonlinear model should be examined to check if it is a quadratic model.

```
(default = 0)
```

- 0 Do not check if NLP is quadratic
- 1 Check if NLP is quadratic

## NLP\_AUTODERIV (integer)

This is a flag to indicate if automatic differentiation is the method of choice for computing derivatives and select the type of differentiation.

```
(default = 0)
```

- 0 Finite Differences approach will be used
- 1 Forward type of Automatic Differentiation will be used
- 2 Backward type of Automatic Differentiation will be used

## NLP\_MAXLOCALSEARCH (integer)

This controls the maximum number of local searches (multistarts) when solving a NLP using the multistart solver.

```
(default = 5)
```

#### NLP\_USE\_LINDO\_CRASH (integer)

This is a flag indicating if an initial solution will be computed using advanced crash routines.

```
(default = 1)
```

- 0 Do not use advanced crash routines
- 1 Use advanced crash routines

## NLP\_STALL\_ITRLMT (integer)

This specifies the iteration limit before a sequence of non-improving NLP iterations is declared as stalling, thus causing the solver to terminate.

```
(default = 100)
```

#### NLP\_AUTOHESS (integer)

This is a flag to indicate if Second Order Automatic Differentiation will be performed in solving a nonlinear model. The second order derivatives provide an exact/precise Hessian matrix to the SQP algorithm, which may lead to less iterations and better solutions, but may also be quite expensive in computing time for some cases.

```
(default = 0)
```

- 0 Do not use Second Order Automatic Differentiation
- 1 Use Second Order Automatic Differentiation

#### MIP\_TIMLIM (integer)

This is the time limit in seconds for branch-and-bound. The default value is -1, which means no time limit is imposed. However, the value of SOLVER\_TIMLMT will be applied to each continuous subproblem solve. If the value of this parameter is greater than 0, then the value of SOLVER\_TIMLMT will be disregarded. If this time limit is reached and a feasible integer solution was found, it will be installed as the incumbent (best known) solution.

```
(default = GAMS ResLim)
```

#### MIP\_AOPTTIMLIM (integer)

This is the time in seconds beyond which the relative optimality tolerance, MIP\_PEROPTTOL will be applied.

```
(default = 100)
```

#### MIP\_LSOLTIMLIM (integer)

```
(default = -1)
```

#### MIP\_PRELEVEL (integer)

This controls the amount and type of MIP pre-solving at root node.

```
(default = 510)
```

- +2 Simple pre-solving
- +4 Probing
- +8 Coefficient reduction
- +16 Elimination
- +32 Dual reductions
- +64 Use dual information

- +128 Binary row presolving
- +256 Row aggregation
- +512 Maximum pass

#### MIP\_NODESELRULE (integer)

This specifies the node selection rule for choosing between all active nodes in the branch-and-bound tree when solving integer programs. Possible selections are: 0: Solver decides (default). 1: Depth first search. 2: Choose node with worst bound. 3: Choose node with best bound. 4: Start with best bound. If no improvement in the gap between best bound and best integer solution is obtained for some time, switch to: if (number of active nodes;10000) Best estimate node selection (5). else Worst bound node selection (2). 5: Choose the node with the best estimate, where the new objective estimate is obtained using pseudo costs. 6: Same as (4), but start with the best estimate.

(default = 0)

- 0 Solver decides
- 1 Depth first search
- 2 Choose node with worst bound
- 3 Choose node with best bound
- 4 Start with best bound
- 5 Choose the node with the best estimate
- 6 Same as 4 but start with the best estimate

## MIP\_INTTOL (real)

An integer variable is considered integer feasible if the absolute difference from the nearest integer is smaller than this.

(default = 1e-6)

#### MIP\_RELINTTOL (real)

An integer variable is considered integer feasible if the difference between its value and the nearest integer value divided by the value of the nearest integer is less than this.

(default = 8e-6)

## MIP\_RELOPTTOL (real)

This is the MIP relative optimality tolerance. Solutions must beat the incumbent by at least this relative amount to become the new, best solution.

(default = 1e-5)

## MIP\_PEROPTTOL (real)

This is the MIP relative optimality tolerance that will be in effect after T seconds following the start. The value T should be specified using the MIP\_AOPTTIMLIM parameter.

(default = 1e-5)

#### MIP\_MAXCUTPASS\_TOP (integer)

This controls the number passes to generate cuts on the root node. Each of these passes will be followed by a reoptimization and a new batch of cuts will be generated at the new solution.

(default = 200)

## MIP\_MAXCUTPASS\_TREE (integer)

This controls the number passes to generate cuts on the child nodes. Each of these passes will be followed by a reoptimization and a new batch of cuts will be generated at the new solution.

```
(default = 2)
```

## MIP\_ADDCUTPER (real)

This determines how many constraint cuts can be added as a percentage of the number of original rows in an integer programming model.

```
(default = 0.75)
```

#### MIP\_ADDCUTPER\_TREE (real)

This determines how many constraint cuts can be added at child nodes as a percentage of the number of original rows in an integer programming model.

```
(default = 0.5)
```

## MIP\_MAXNONIMP\_CUTPASS (integer)

This controls the maximum number of passes allowed in cut-generation that does not improve the current relaxation.

```
(default = 3)
```

## MIP\_CUTLEVEL\_TOP (integer)

This controls the combination of cut types to try at the root node when solving a MIP. Bit settings are used to enable the various cut types.

```
(default = 6142)
```

- +2 GUB cover
- +4 Flow cover
- +8 Lifting
- +16 Plant location
- +32 Disaggregation
- +64 Knapsack cover
- +128 Lattice
- +256 Gomory
- +512 Coefficient reduction
- +1024 GCD
- +2048 Obj integrality
- +4096 Basis Cuts
- +8192 Cardinality Cuts
- +16384 Disjunk Cuts

#### MIP\_CUTLEVEL\_TREE (integer)

This controls the combination of cut types to try at child nodes in the B&B tree when solving a MIP.

```
(default = 4094)
```

- +2 GUB cover
- +4 Flow cover
- +8 Lifting
- +16 Plant location
- +32 Disaggregation
- +64 Knapsack cover
- +128 Lattice
- +256 Gomory
- +512 Coefficient reduction

```
+1024 GCD
+2048 Obj integrality
+4096 Basis Cuts
+8192 Cardinality Cuts
+16384 Disjunk Cuts
```

#### MIP\_CUTTIMLIM (integer)

This controls the total time to be spent in cut generation throughout the solution of a MIP. The default value is -1, indicating that no time limits will be imposed when generating cuts.

```
(default = -1)
```

#### MIP\_CUTDEPTH (integer)

This controls a threshold value for the depth of nodes in the B&B tree, so cut generation will be less likely at those nodes deeper than this threshold.

```
(default = 8)
```

#### MIP\_CUTFREQ (integer)

This controls the frequency of invoking cut generation at child nodes. The default value is 10, indicating that the MIP solver will try to generate cuts at every 10 nodes.

```
(default = 10)
```

## MIP\_HEULEVEL (integer)

This specifies the heuristic used to find the integer solution. Possible values are: 0: No heuristic is used. 1: A simple heuristic is used. Typically, this will find integer solutions only on problems with a certain structure. However, it tends to be fast. 2: This is an advanced heuristic that tries to find a "good" integer solution fast. In general, a value of 2 seems to not increase the total solution time and will find an integer solution fast on many problems. A higher value may find an integer solution faster, or an integer solution where none would have been found with a lower level. Try level 3 or 4 on "difficult" problems where 2 does not help. Higher values cause more time to be spent in the heuristic. The value may be set arbitrarily high. However, >20 is probably not worthwhile. MIP\_HEUMINTIMLIM controls the time to be spent in searching heuristic solutions.

```
(default = 3)
```

## MIP\_CUTOFFOBJ (real)

If this is specified, then any part of the branch-and-bound tree that has a bound worse than this value will not be considered. This can be used to reduce the running time if a good bound is known.

```
(default = 1e30)
```

#### MIP\_USECUTOFFOBJ (integer)

This is a flag for the parameter MIP\_CUTOFFOBJ. If you do not want to lose the value of the parameter MIP\_CUTOFFOBJ, this provides an alternative to disabling the cutoff objective.

```
(default = 1)
```

- 0 Do not use current cutoff value
- 1 Use current cutoff value

## MIP\_STRONGBRANCHLEVEL (integer)

This specifies the depth from the root in which strong branching is used. The default value of 10 means that strong branching is used on a level of 1 to 10 measured from the root. Strong branching finds the real bound for branching on a given variable, which, in most cases, requires a solution of a linear program and may therefore also be quite expensive in computing time. However, if used on nodes close to the root node of the tree, it also gives a much better bound for that part of the tree and can therefore reduce the size of the branch-and-bound tree.

```
(default = 10)
```

## MIP\_TREEREORDERLEVEL (integer)

This specifies the tree reordering level.

```
(default = 10)
```

#### MIP\_BRANCHDIR (integer)

This specifies the direction to branch first when branching on a variable.

```
(default = 0)
```

- 0 Solver decides
- 1 Always branch up first
- 2 Always branch down first

## MIP\_TOPOPT (integer)

This specifies which optimization method to use when there is no previous basis.

```
(default = 0)
```

- 0 Solver decides
- 1 Use primal method
- 2 Use dual simplex
- 3 Use barrier solver

## MIP\_REOPT (integer)

This specifies which optimization method to use when doing reoptimization from a given basis.

```
(default = 0)
```

- 0 Solver decides
- 1 Use primal method
- 2 Use dual simplex
- 3 Use barrier solver

## MIP\_SOLVERTYPE (integer)

This specifies the optimization method to use when solving mixed-integer models.

```
(default = 0)
```

- 0 Solver decides
- 1 Use B&B only
- 2 Use Enumeration and Knapsack solver only

#### MIP\_KEEPINMEM (integer)

If this is set to 1, the integer pre-solver will try to keep LP bases in memory. This typically gives faster solution times, but uses more memory. Setting this parameter to 0 causes the pre-solver to erase bases from memory.

```
(default = 1)
```

- 0 Do not keep LP bases in memory
- 1 Keep LP bases in memory

## MIP\_BRANCHRULE (integer)

This specifies the rule for choosing the variable to branch on at the selected node.

```
(default = 0)
```

0 Solver decides

- 1 Basis rounding with pseudo reduced costs
- 2 Maximum infeasibility
- 3 Pseudo reduced costs only

#### MIP\_REDCOSTFIX\_CUTOFF (real)

This specifies the cutoff value as a percentage of the reduced costs to be used in fixing variables when using the reduced cost fixing heuristic.

```
(default = 0.9)
```

#### MIP\_ADDCUTOBJTOL (real)

This specifies the minimum required improvement in the objective function for the cut generation phase to continue generating cuts.

```
(default = 1.5625e-5)
```

#### MIP\_HEUMINTIMLIM (integer)

This specifies the minimum time in seconds to be spent in finding heuristic solutions to the MIP model. MIP\_HEULEVEL controls the heuristic used to find the integer solution.

```
(default = 0)
```

#### MIP\_BRANCH\_PRIO (integer)

This controls how variable selection priorities are set and used.

```
(default = 0)
```

- 0 If the user has specified priorities then use them Otherwise let LINDO API decide
- 1 If user has specified priorities then use them Overwrite users choices if necessary
- 2 If user has specified priorities then use them Otherwise do not use any priorities
- 3 Let LINDO API set the priorities and ignore any user specified priorities
- 4 Binaries always have higher priority over general integers

## MIP\_SCALING\_BOUND (integer)

This controls the maximum difference between the upper and lower bounds of an integer variable that will enable the scaling in the simplex solver when solving a subproblem in the branch-andbound tree.

```
(default = 10000)
```

## MIP\_PSEUDOCOST\_WEIGT (real)

This specifies the weight in pseudocost computations for variable selection.

```
(default = 1.5625e-05)
```

## MIP\_LBIGM (real)

This refers to the Big-M value used in linearizing nonlinear expressions.

```
(default = 10000)
```

#### MIP\_DELTA (real)

This refers to a near-zero value used in linearizing nonlinear expressions.

```
(default = 1e-6)
```

#### MIP\_DUAL\_SOLUTION (integer)

This flag controls whether the dual solution to the LP relaxation that yielded the optimal MIP solution will be computed or not.

```
(default = 0)
```

0 Do not calculate dual solution for LP relaxation

1 Calculate dual solution for LP relaxation

#### MIP\_BRANCH\_LIMIT (integer)

This is the limit on the total number of branches to be created during branch-and- bound. The default value is -1, which means no limit is imposed. If the branch limit is reached and a feasible integer solution was found, it will be installed as the incumbent (best known) solution.

```
(default = -1)
```

#### MIP\_ITRLIM (integer)

This is the iteration limit for branch-and- bound. The default value is .1, which means no iteration limit is imposed. If the iteration limit is reached and a feasible integer solution was found, it will be installed as the incumbent (best known) solution.

```
(default = -1)
```

## MIP\_AGGCUTLIM\_TOP (integer)

This specifies an upper limit on the number of constraints to be involved in the derivation of an aggregation cut at the root node. The default is .1, which means that the solver will decide.

```
(default = -1)
```

## MIP\_AGGCUTLIM\_TREE (integer)

This specifies an upper limit on the number of constraints to be involved in the derivation of an aggregation cut at the tree nodes. The default is .1, which means that the solver will decide.

```
(default = -1)
```

## MIP\_ANODES\_SWITCH\_DF (integer)

This specifies the threshold on active nodes for switching to depth-first search rule.

```
(default = 50000)
```

#### MIP\_ABSOPTTOL (real)

This is the MIP absolute optimality tolerance. Solutions must beat the incumbent by at least this absolute amount to become the new, best solution.

```
(default = 0)
```

#### MIP\_MINABSOBJSTEP (real)

This specifies the value to update the cutoff value each time a mixed integer solution is found.

```
(default = 0)
```

#### MIP\_PSEUDOCOST\_RULE (integer)

This specifies the rule in pseudocost computations for variable selection.

```
(default = 0)
```

## MIP\_USE\_ENUM\_HEU (integer)

This specifies the frequency of enumeration heuristic.

```
(default = 4)
```

#### MIP\_PRELEVEL\_TREE (integer)

This controls the amount and type of MIP pre-solving at tree nodes.

```
(default = 174)
```

- +2 Simple pre-solving
- +4 Probing
- +8 Coefficient reduction
- +16 Elimination

- +32 Dual reductions
- +64 Use dual information
- +128 Binary row presolving
- +256 Row aggregation
- +512 Maximum pass

#### MIP\_REDCOSTFIX\_CUTOFF\_TREE (real)

This specifies the cutoff value as a percentage of the reduced costs to be used in fixing variables when using the reduced cost fixing heuristic at tree nodes.

```
(default = 0.9)
```

## MIP\_USE\_INT\_ZERO\_TOL (integer)

This flag controls if all MIP calculations would be based on the integrality tolarance specified by MIP\_INTTOL.

```
(default = 0)
```

- 0 Do not base MIP calculations on MIP\_INTTOL
- 1 Base MIP calculations on MIP\_INTTOL

#### MIP\_USE\_CUTS\_HEU (integer)

This flag controls if cut generation is enabled during MIP heuristics. The default is -1 (i.e. the solver decides).

```
(default = -1)
```

- -1 Solver decides
- 0 Do not use cut heuristic
- 1 Use cut heuristic

#### MIP\_BIGM\_FOR\_INTTOL (real)

This value specifies the threshold for which the coefficient of a binary variable would be considered as big-M (when applicable).

```
(default = 1e8)
```

## MIP\_STRONGBRANCHDONUM (integer)

This value specifies the minimum number of variables, among all the candidates, to try the strong branching on.

```
(default = 3)
```

## MIP\_MAKECUT\_INACTIVE\_COUNT (integer)

This value specifies the threshold for the times a cut could remain active after successive reoptimization during branch-and-bound. If the count is larger than the specified level the solver will inactive the cut.

```
(default = 10)
```

#### MIP\_PRE\_ELIM\_FILL (integer)

This is a nonnegative value that controls the fill-in introduced by the eliminations during pre-solve. Smaller values could help when the total nonzeros in the presolved model is significantly more than the original model.

```
(default = 100)
```

#### OPTTOL (real)

This value is the GOP optimality tolerance. Solutions must beat the incumbent by at least this amount to become the new best solution.

```
(default = 1e-6)
```

## FLTTOL (real)

This value is the GOP floating-point tolerance. It specifies the maximum rounding errors in the floating-point computation.

```
(default = 1e-10)
```

#### **BOXTOL** (real)

This value specifies the minimal width of variable intervals in a box allowed to branch.

```
(default = 1e-6)
```

#### WIDTOL (real)

This value specifies the maximal width of variable intervals for a box to be considered as an incumbent box containing an incumbent solution. It is used when MAXWIDMD is set at 1.

```
(default = 1e-4)
```

## DELTATOL (real)

This value is the delta tolerance in the GOP convexification. It is a measure of how closely the additional constraints added as part of convexification should be satisfied.

```
(default = 1e-7)
```

#### BNDLIM (real)

This value specifies the maximum magnitude of variable bounds used in the GOP convexification. Any lower bound smaller than the negative of this value will be treated as the negative of this value. Any upper bound greater than this value will be treated as this value. This helps the global solver focus on more productive domains.

```
(default = 1e10)
```

#### TIMLIM (integer)

This is the time limit in seconds for GOP branch-and-bound.

```
(default = GAMS ResLim)
```

## OPTCHKMD (integer)

This specifies the criterion used to certify the global optimality. When this value is 0, the absolute deviation of objective lower and upper bounds should be smaller than OPTTOL at the global optimum. When its value is 1, the relative deviation of objective lower and upper bounds should be smaller than OPTTOL at the global optimum.

```
(default = 1)
```

#### BRANCHMD (integer)

This specifies the direction to branch first when branching on a variable. The branch variable is selected as the one that holds the largest magnitude in the measure.

```
(default = 5)
```

- 0 Absolute width
- 1 Locally relative width
- 2 Globally relative width
- 3 Globally relative distance from the convex minimum to the bounds
- 4 Absolute violation between the function and its convex envelope at the convex minimum
- 5 Relative violation between the function and its convex envelope at the convex minimum

#### MAXWIDMD (integer)

This is the maximum width flag for the global solution. The GOP branch-andbound may continue contracting a box with an incumbent solution until its maximum width is smaller than WIDTOL.

```
(default = 0)
```

- 0 The maximum width criterion is suppressed
- 1 The maximum width criterion is performed

## PRELEVEL (integer)

This controls the amount and type of GOP pre-solving. The default value is: 30 = 2+4+8+16 meaning to do all of the below options.

```
(default = 30)
```

- +2 Initial local optimization
- +4 Initial linear constraint propagation
- +8 Recursive linear constraint propagation
- +16 Recursive nonlinear constraint propagation

## POSTLEVEL (integer)

This controls the amount and type of GOP post-solving. The default value is: 6 = 2+4 meaning to do both of the below options.

```
(default = 6)
```

- +2 Apply LSgetBestBound
- +4 Reoptimize variable bounds

#### BBSRCHMD (integer)

This specifies the node selection rule for choosing between all active nodes in the GOP branch-and-bound tree when solving global optimization programs.

```
(default = 1)
```

- 0 Depth first search
- 1 Choose node with worst bound

#### DECOMPPTMD (integer)

This specifies the decomposition point selection rule. In the branch step of GOP branch-and-bound, a branch point M is selected to decompose the selected variable interval [Lb, Ub] into two subintervals, [Lb, M] and [M, Ub].

```
(default = 1)
```

- 0 Mid-point
- 1 Local minimum or convex minimum

#### ALGREFORMMD (integer)

This controls the algebraic reformulation rule for a GOP. The algebraic reformulation and analysis is very crucial in building a tight convex envelope to enclose the nonlinear/nonconvex functions. A lower degree of overestimation on convex envelopes helps increase the convergence rate to the global optimum.

```
(default = 18)
```

- +2 Rearrange and collect terms
- +4 Expand all parentheses
- +8 Retain nonlinear functions
- +16 Selectively expand parentheses

## RELBRNDMD (integer)

This controls the reliable rounding rule in the GOP branch-and-bound. The global solver applies many suboptimizations to estimate the lower and upper bounds on the global optimum. A rounding error or numerical instability could unintentionally cut off a good solution. A variety of reliable approaches are available to improve the precision.

```
(default = 0)
```

- +2 Use smaller optimality or feasibility tolerances and appropriate presolving options
- +4 Apply interval arithmetic to reverify the solution feasibility

#### USEBNDLIM (integer)

This value is a flag for the parameter BNDLIM.

```
(default = 2)
```

- 0 Do not use the bound limit on the variables
- 1 Use the bound limit right at the beginning of global optimization
- 2 Use the bound limit after the initial local optimization if selected

#### BRANCH\_LIMIT (integer)

This is the limit on the total number of branches to be created during branch-and- bound in GOP tree. The default value is -1, which means no limit is imposed. If the branch limit is reached and a feasible solution was found, it will be installed as the incumbent (best known) solution.

```
(default = -1)
```

## CORELEVEL (integer)

This controls the strategy of GOP branch-and-bound procedure.

```
(default = 14)
```

- +2 LP convex relaxation
- +4 NLP solving
- +8 Box Branching

## OPT\_MODE (integer)

This specifies the mode for GOP optimization.

```
(default = 1)
```

#### HEU\_MODE (integer)

This specifies the heuristic used in the global solver to find good solution. Typically, if a heuristic is used this will put more efforts in searching for good solutions, and less in bound tightening.

```
(default = 0)
```

- 0 No heuristic is used
- 1 A simple heuristic is used

## SUBOUT\_MODE (integer)

This is a flag indicating whether fixed variables are substituted out of the instruction list used in the global solver.

```
(default = 1)
```

- 0 Do not substitute out fixed variables
- 1 Substitute out fixed variables

## LSOLBRANLIM (integer)

This value controls the branch limit until finding a new nonlinear solution since the last nonlinear solution is found. The default value is -1, which means no branch limit is imposed.

```
(default = -1)
```

## CHECKRANGE (string)

If this option is set, Lindo calculates the feasible range (determined by an upper and lower bound) for every variable in each equation while all other variables are fixed to their level. If set, the value of this option defines the name of the GDX file where the results are written to. For every combination of equationand variable block there will be one symbol in the format  $EquBlock\_VarBlock(equ\_Ind\_1, ..., equ\_Ind\_M, var\_Ind\_1, ..., var\_Ind\_N, directions)$ .

```
(default = range.gdx)
```

## **USEGOP** (integer)

This value determines whether the global optimization will be used.

```
(default = 1)
```

- 0 Do not use global optimization
- 1 Use global optimization

## WRITEMPI (string)

If this option is set, Lindo write an MPI file of processed model. If set, the value of this option defines the name of the MPI file.