



Lecture 2

Introduction to GAMS

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Moving to GAMS

- The Excel version of 1-2-3 is easily accessible, but must be highly simplified to be tractable.
- Using a higher level programming language enables us to include more economic structure and behavior.
- The Generalized Algebraic Modeling System (GAMS) is the language of choice for this kind of work.



Accessing GAMS

- The homepage of the GAMS corporation (www.gams.com) contains a lot of useful information.
- From the homepage, a full user guide can be downloaded at www.gams.com/docs/document.htm; the user guide contains the syntax for all GAMS commands and very helpful as a reference when writing GAMS models. Note that the user guide is also available via the Help function in GAMS-IDE.
- All readers are advised to study the introductory chapter of this manual when starting to learn the GAMS software.



Download and Installation

- There is a free version of GAMS available for installation on your own computer. This is a limited version of GAMS, which cannot solve large problems, but it can be used for the sample models in this course.
- A free copy of the restricted, student version is available for download at <http://www.gams.com/download>



Introduction to GAMS

- **Description:**

- automates the process of going from a mathematical statement of the problem to the solution.
- GAMS transforms the mathematical representation to representations required by specific *Solver* engines like OSL, CPLEX, ..
- models and solves complex *linear, nonlinear* and *integer* programming problems.
- lets you build your model in a natural, logical structure using compact algebraic statements.

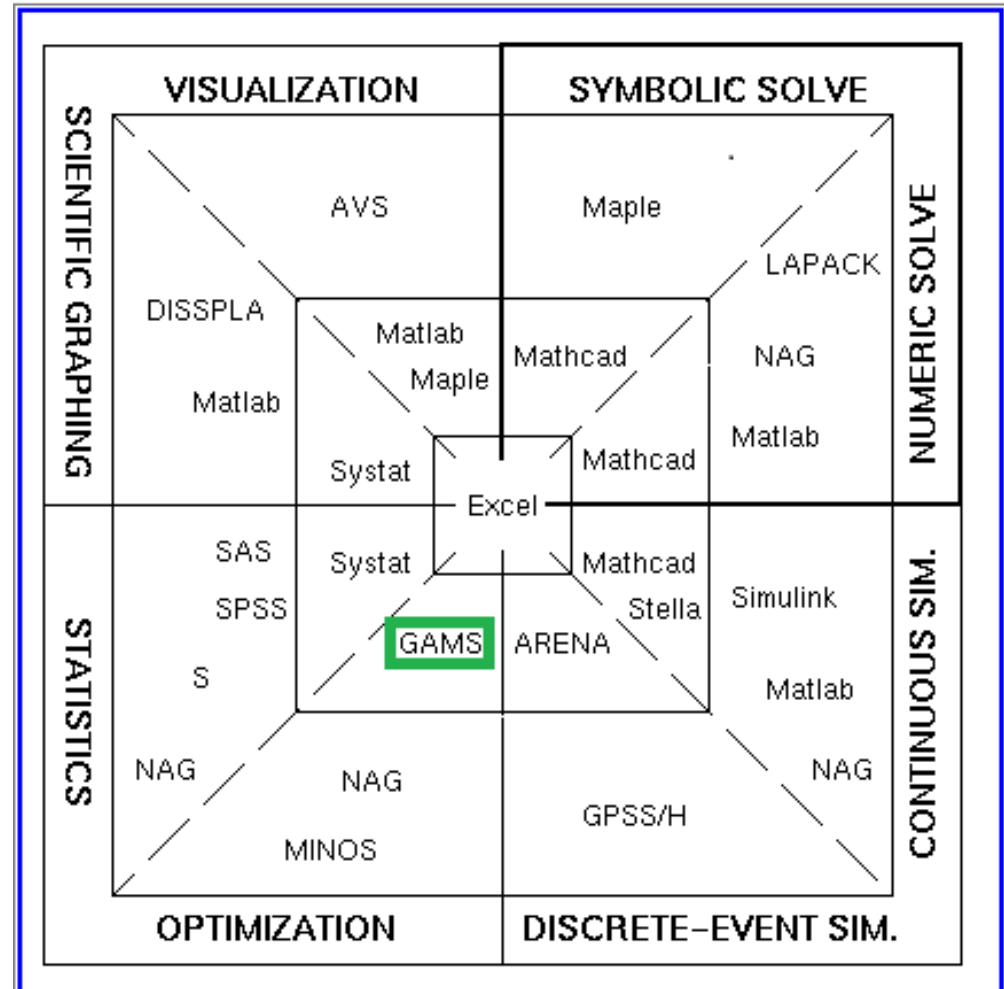
- **Typical use:**

- Optimization

Scientific Software Comparison Chart

As you move away from the centre of the diagram, the software is more advanced, but often less friendly.

Try the software in the second tier first if you are looking for a middle way.

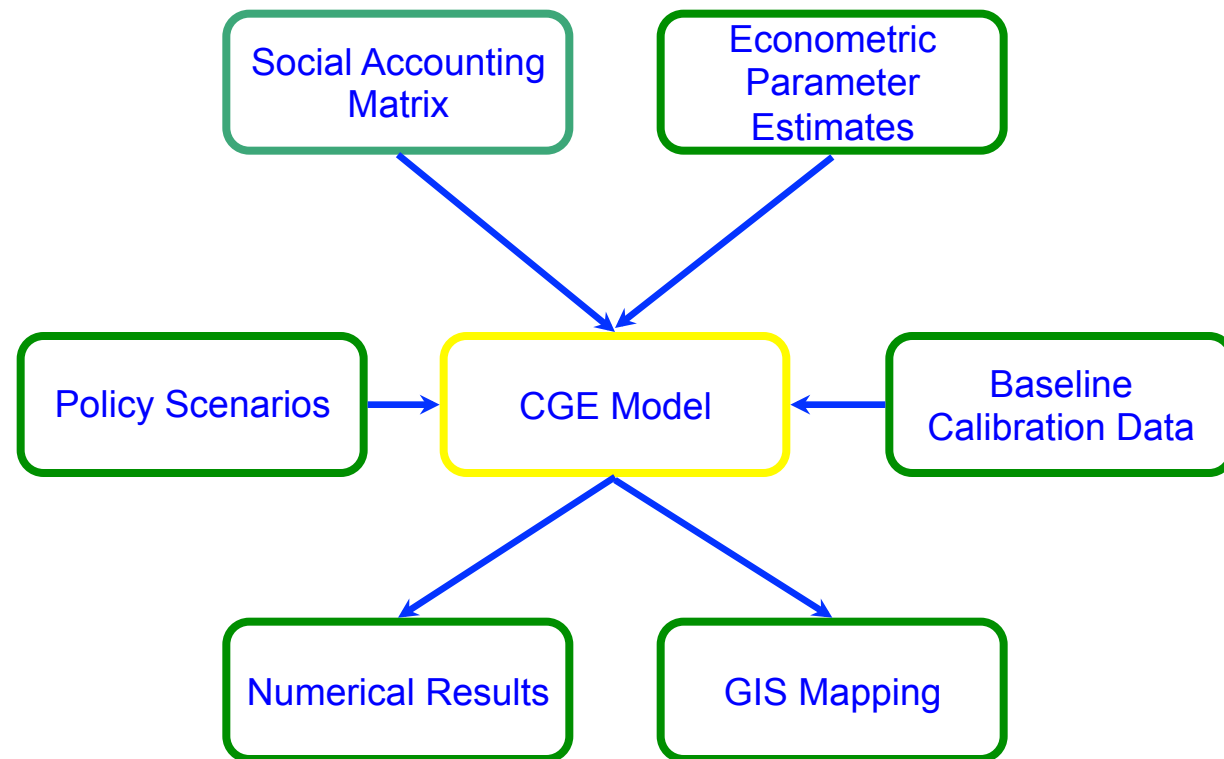


GAMS for CGE Models: A Schematic View

Develop
ment

Simulatio
n

Analysis



Box Color Key to Software Implementation:
Green – Microsoft Excel
Yellow – GAMS



Sample Transportation Problem

- Satisfy market demand, but with minimal costs of transporting the goods from producers to the markets
- we are given the supplies at several plants and the demands at several markets for a single commodity, and we are given the unit costs of shipping the commodity from plants to markets. The economic question is: how much shipment should there be between each plant and each market so as to minimize total transport cost?



Transportation Problem (cont.)

- Indices:
 - i = plants
 - j = markets
- Given Data:
 - a_i = supply of commodity of plant i (in cases)
 - b_j = demand for commodity at market j (cases)
 - c_{ij} = cost per unit shipment between plant i and market j (\$/case)
- Variables:
 - costs
 - x_{ij} = amount of commodity to ship from plant i to market j (cases),
 - where $x_{ij} \geq 0$, for all i, j

Transportation Problem (cont.)

Objective Function:

$$\text{Minimize } \sum_i \sum_j c_{ij} x_{ij} \quad (\$K)$$

Constraints:

Observe supply limit at plant i : $\sum_j x_{ij} \leq a_i$ for all i (cases)

Satisfy demand at market j : $\sum_i x_{ij} \geq b_j$, for all j (cases)



GAMS Program

- Model definition and *Solve* statement
- Model definition
 - what is in the model (indices): sets
 - data: scalars, parameters, tables
 - What you are looking for: variables
 - relationships: equations
 - Model statement
 - Solve statement



Defining Model Components

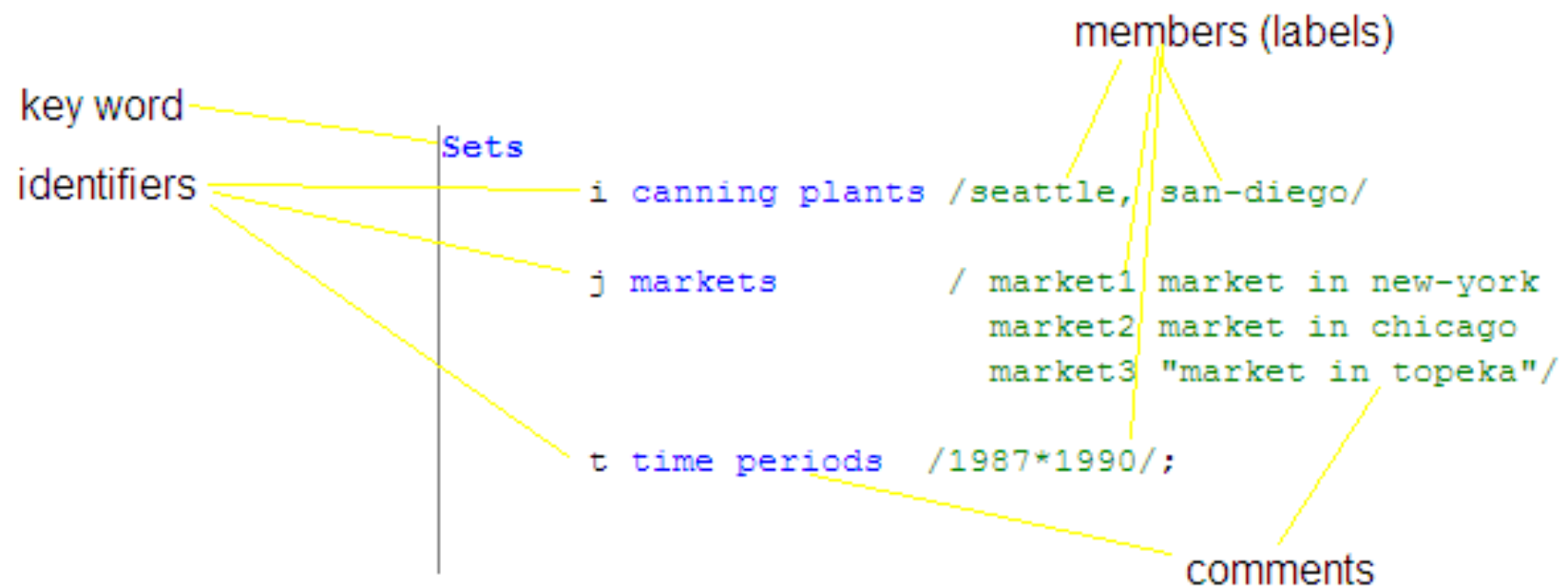
- Declaration
 - declaring the existence of something and giving it a *unique* name – “identifier”
- Definition/Assignment
 - giving a specific value or form
 - e.g., labels - set elements



Model Components: Sets

- Indices
- Group of elements with similar characteristics
- Define what you are considering in the model
 - Producers, markets, time periods...

Set: declaration and definition



- Describe what you know
- Different presentation of data: dimensionality
- Scalars, parameters, and tables

Scalars

A number

```
Scalar f freight in dollars per case per thousand miles /90/ ;
```

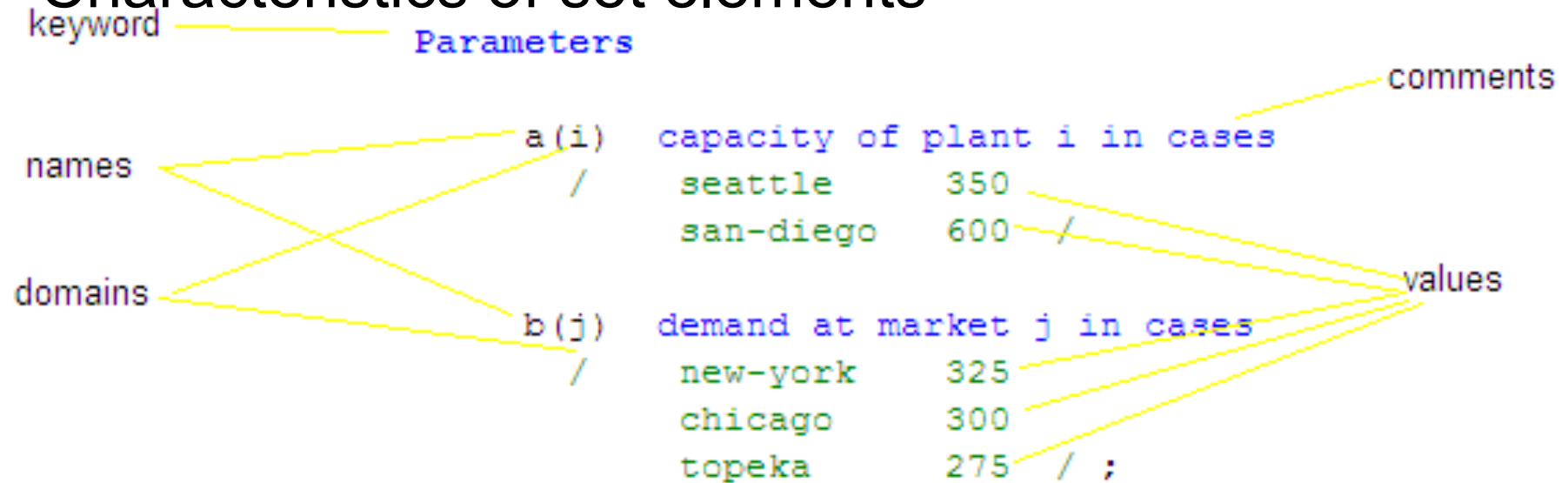
keyword
identifier

description

value

Parameters: declaration and definition

Characteristics of set elements



Tables

keyword — identifier — domain — description

| Table d(i,j) | | | |
|--------------------------------|----------|---------|--------|
| distance in thousands of miles | | | |
| | new-york | chicago | topeka |
| seattle | 2.5 | 1.7 | 1.8 |
| san-diego | 2.5 | 1.8 | 1.4 |

values

;

Direct assignment of data values

Example 1: declare parameter c and assign its value

```
Parameter c(i,j)  transport cost in thousands of dollars per case ;  
  
    c(i,j) = f * d(i,j) / 1000 ;
```

Valid only if the values of f and $d(i,j)$ are previously assigned

Example 2: Assignment of a value to an element

```
| c('seattle', 'new-york') = 0.40;
```



Exponent operator

- $x^{**}n$
 - x should always have a positive value
 - n can be any number
- `power(x,n)`
 - positive or negative value of x
 - n is integer

Index Operations

- sum

summation over controlling index,

$$x_1 + x_2 + \dots + x_{10} = \sum_{k=1}^{10} x_k$$

`sum(k, x(k))`

- prod

product over controlling index

$$x_1 \cdot x_2 \cdot \dots \cdot x_{10} = \prod_{k=1}^{10} x_k$$

`prod(k, x(k))`

- smin, smax

minimum and maximum over controlling index

`smin(k, x(k))`



Model Components: Variables

- What you are looking for
- Declaration, assignment of type, assignment of bounds and/or initial values

Variables

```
x(i,j)  shipment quantities in cases  
z       total transportation costs in thousands of dollars ;
```

Positive Variable x ;



Variable Types

| Variable Type | Allowed Range of Variable |
|----------------|---------------------------|
| free (default) | $-\infty$ to $+\infty$ |
| positive | 0 to $+\infty$ |
| negative | $-\infty$ to 0 |
| binary | 0 or 1 |
| integer | 0,1,..., 100 (default) |

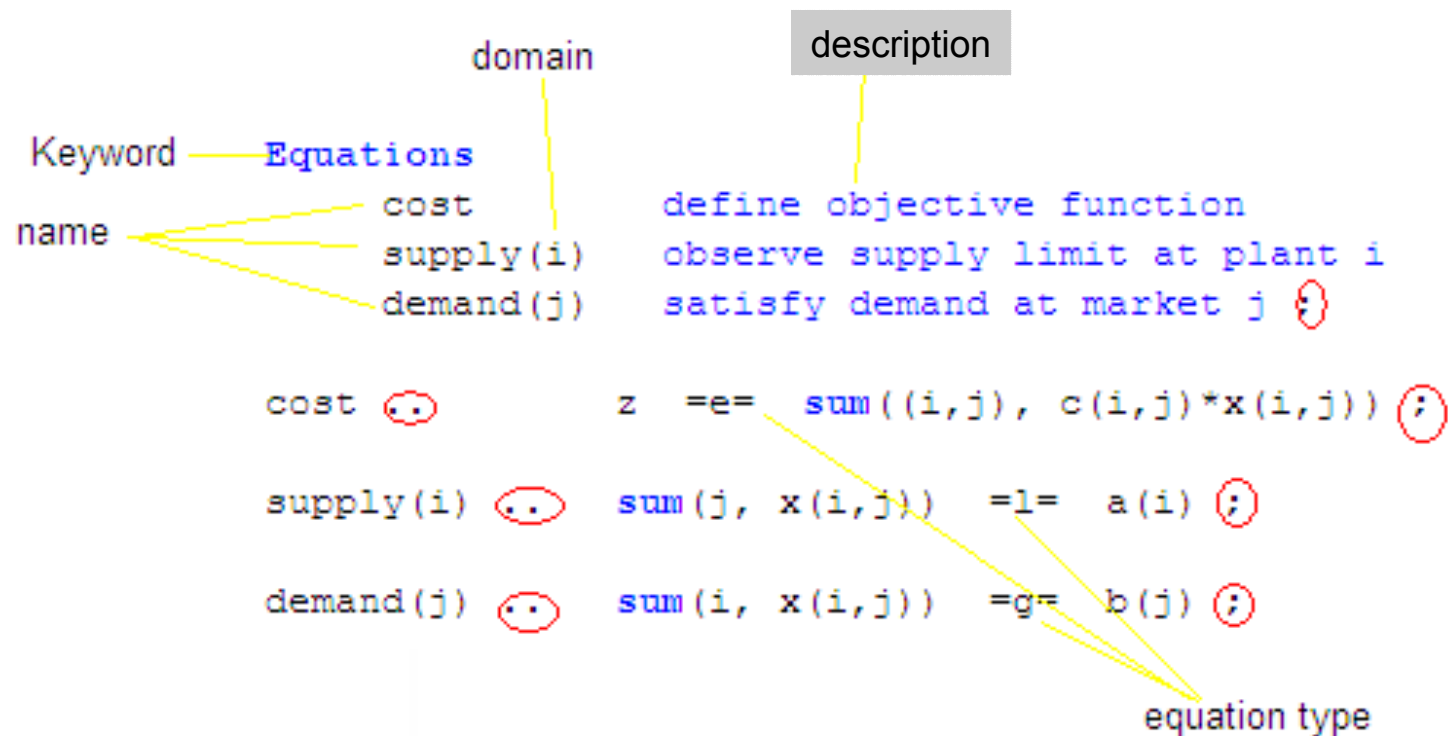
Variable attributes

| Variable attribute | Variable suffix | Description |
|--------------------------|-----------------|--|
| lower bound | .lo | The lower bound for the variable. Set by the user either explicitly or through default values. |
| upper bound | .up | The upper bound for the variable. Set by the user either explicitly or through default values. |
| fixed value | .fx | The fixed value for the variable. |
| activity level | .l | The activity level for the variable. This is also equivalent to the current value of the variable. Receives new values when a model is solved. |
| marginal or dual value | .m | The marginal value for the variable. Receives new values when a model is solved. |
| scale value | .scale | This is the scaling factor on the variable. This is normally an issue with nonlinear programming problems and is discussed in detail later. |
| branching priority value | .prior | This is the branching priority value of a variable. This parameter is used in mixed integer programming models only, and is discussed in detail later. |

Example: $y.fx = 1000;$

Model Components: Equations

- Relationships among variables and parameters
- Declaration, definition





Equation Types

| Equation type | Description |
|---------------|---|
| =e= | Equality: rhs must equal lhs |
| =g= | Greater than: lhs must be greater than or equal to rhs |
| =l= | Less than: lhs must be less than or equal to rhs |
| =n= | No relationships enforced between lhs and rhs. This equation type is rarely used. |



Equation Values

| Type | .lo | .up | .l |
|------|------|-----|-----|
| =e= | rhs | rhs | rhs |
| =l= | -inf | rhs | rhs |
| =g= | rhs | inf | rhs |
| =n= | -inf | inf | any |



Quick Note: “=” and “=e=”

- “=”
 - used only in direct assignments
 - gives a desired value to a parameter
 - executed before solver is called
 - must not involve variables
- “=e=”
 - used only in equation definitions
 - executed after the solver is called
 - must contain variables

Model Components:

Model statement

- Model – collection of equations
- Declaration and definition

Examples:

```
Model transport /all/ ;
```

```
Model nortonL    linear version    /cb, rc, dfl, bc, obj/  
    nortonN      nonlinear version  /cb, rc, dfn, bc, obj/ ;
```



Types of Problems

| Model Type | Description |
|------------|--|
| LP | Linear Programming. There are no nonlinear terms or discrete (binary or integer) variables in the model |
| NLP | Nonlinear programming. There are nonlinear terms involving only “smooth” functions in the model, but no discrete variables |
| MIP, MINLP | Mixed Integer Programming. The model can contain discrete (integer or binary) variables |
| Other | DNLP, RMIP, MPEC, MCP, CNS |

Model Components: Solve statement

keyword `Solve` transport using lp minimizing z ;

 solution procedure name of variable to be optimized

 name of the model keyword keyword

- Objective variable: scalar and type free



Display Statement

```
Display x.l, x.m ;
```

- Only non-default values are displayed
- Default value is generally zero
- for the .lo and .up subtypes of variables and equations the default values can be zero, -INF or +INF
- Display control examples:
 - option decimals = 1; - number of digits after decimal point for all displayed variables
 - option x : 5; - number of digits after decimal point for variable x;



Solve execution

1. Model is translated into *Solver* language
2. Comprehension aid is written to output
3. Error check, if error – program termination
4. *Solver* solves the model
5. GAMS reports the status of the solution and load solution values from *Solver*

Reports results, facilitates debugging

- Echo Print
- Reference Map
- Equation Listing
- Column Listing
- Model Statistics
- Status Report Solver report
- Solution Report
- Report Summary
- Results



Echo Print

- Copy of input file with line numbers
- Dollar-print-control statements
 - output control
 - start in column 1
 - examples:
 - \$Title TEXT print TEXT on top of each page
 - \$Ontext
 - \$Offtext comments
 - \$Offlisting no printing of the input file



Reference Map

- Summaries of the input file for debugging purposes
- Two parts of cross-reference map
 - alphabetical list of all entities and a coded reference of each appearance
 - List of all entries grouped by type



Equation Listing

- Does GAMS generate the model you intended?
- Describe equations for specific values of set elements and parameters
- Nonlinear system – first order Taylor approximation (i.e. linear approximation)



Column Listing

- shows the coefficients of three specific variables for each generic variable
- control of equation and column listing:

option limrow = r, limcol = c ;

r – desired number of equations

c – desired number of columns



Model Statistics

- BLOCK counts – number of generic equations and variables
- SINGLE counts refer to individual equations and variables
- NON ZERO ELEMENTS - number of non-zero coefficients in the problem matrix
- NONLINEAR N-Z – number of nonlinear entries in nonlinear models



Model Statistics (cont.)

- CODE LENGTH, DERIVATIVE POOL, CONSTANT POOL – type of nonlinearity in nonlinear models
- GENERATION TIME - time used since the syntax check finished



Status Report

- solve summary
- Desired SOLVER STATUS: 1 NORMAL COMPLETION
- Desired MODEL STATUS:
 - Linear model: 1 OPTIMAL
 - Nonlinear model: 2 LOCALLY OPTIMAL
 - Integer model: 8 INTEGER SOLUTION



Solver Status

solverstat

1

2

3

4

5

6

7

8

9

10

11

12

13

solver status

normal completion

iteration interrupt

resource interrupt

terminated by solver

evaluation error limit

unknown

(unused)

error preprocessor error

error setup failure

error solver failure

error internal solver error

error post-processor error

error system failure



Model Status

| modelstat | model status |
|-----------|--------------------------|
| 1 | optimal |
| 2 | locally optimal |
| 3 | unbounded |
| 4 | infeasible |
| 5 | locally infeasible |
| 6 | intermediate infeasible |
| 7 | intermediate non-optimal |
| 8 | integer solution |
| 9 | intermediate non-integer |
| 10 | integer infeasible |
| 11 | (unused) |
| 12 | error unknown |
| 13 | error no solution |

The background of the slide features a green-tinted image of a globe with a grid of latitude and longitude lines. The globe is shown from a low angle, making it appear to curve upwards and fill the top half of the frame. The text 'Solver Report' is overlaid on the right side of this image in a bright yellow color.

Solver Report

- message identifying the solver and its authors
- diagnostic messages if anything unusual was detected
- specific performance details



Solution Report

- Results of optimization
- Four levels of equations – low bound, level value, upper bound, and marginal
- Values
 - “ . ” – zero
 - EPS – close to zero
 - INFES - infeasible
 - NOPT - marginal values of the wrong sign
 - UNBND – unbounded
- Turned off by line: *option solprint = off*



Report Summary

- total number of non-optimal, infeasible, and unbounded rows and columns
- INFES – row/column is infeasible. The level value is not between upper and lower bounds
- NOPT – row/column is non-optimal. Marginal value is incorrect
- UNBND – row/column is unbounded



Error Report

- coded message following the line with error
- Look for ****
- contain a "\$" directly below the point at which the compiler thinks the error occurred



Debugging Tips

- Always check carefully for the cause of the first error
- Look at the previous line (especially for missing semicolons) if nothing seems obvious
- More at:

http://ageco.tamu.edu/faculty/mccarl/641clas/04_641_model_inspection_error.pdf

- You are free to use either upper- or lower- case letters
- GAMS treats singular and plural synonymously
 - E.g., **Set** and **Sets**
- Multi-word names are not allowed. Use hyphens
 - E.g., ‘New-York’ instead of ‘New York’
- Tips:
 - Use “*match parentheses*” button
 - Use “*Alt*” key to select a column



GAMS Integrated Development Environment (IDE)

- Most users of GAMS can run the system in the Integrated Development Environment (IDE).
- When GAMS-IDE is started, a window will appear with a menu bar along the top and a main Edit Window for GAMS applications. As with most such systems, input and output operations are controlled by the **File** pull down menu, with other menu items used in edit operations, and in running the GAMS system.
- The IDE version provides for standard, mouse-driven editing of input files in the main GAMS Edit Window. If the appropriate file is not already displayed, use the **New** or **Open** commands on the **File** menu to activate one. Then create or correct the file with the mouse and tools provided on the **Edit** and **Search** menus. The **Matching Parenthesis** button helps with the many parentheses in GAMS by skipping the cursor to the parenthesis that corresponds to the one it is now positioned in front of. The **Find in file** is also a useful tool, if you work with a complex model.

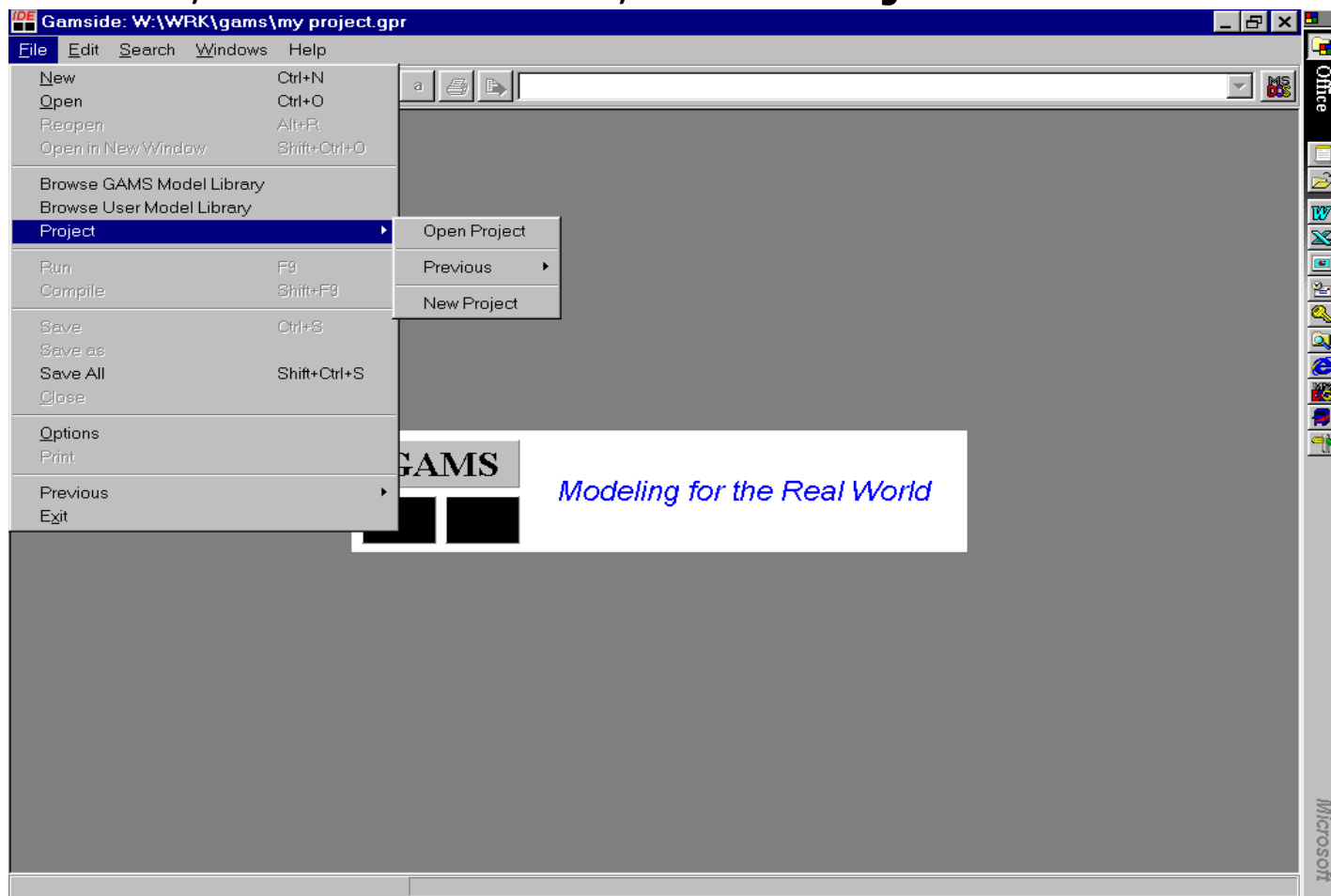


IDE - Continued

- Users should begin each session by selecting a "project". A project is a system file you save but never have to touch. Still, its location is important because the folder (directory) of the current project file is where (.gms) input and (.lst) output files are saved by default.
- This allows you to easily keep all the input and output files for any task together in the same directory, and use different directories for different projects.
- The starting project file (if any) is shown at the top of the main GAMS window.

Initiating a Project

In the picture below, the starting project file is "W:\WRK\GAMS\my project.gpr". To select another, or create a new one, use the **Project** item on the **File** menu.



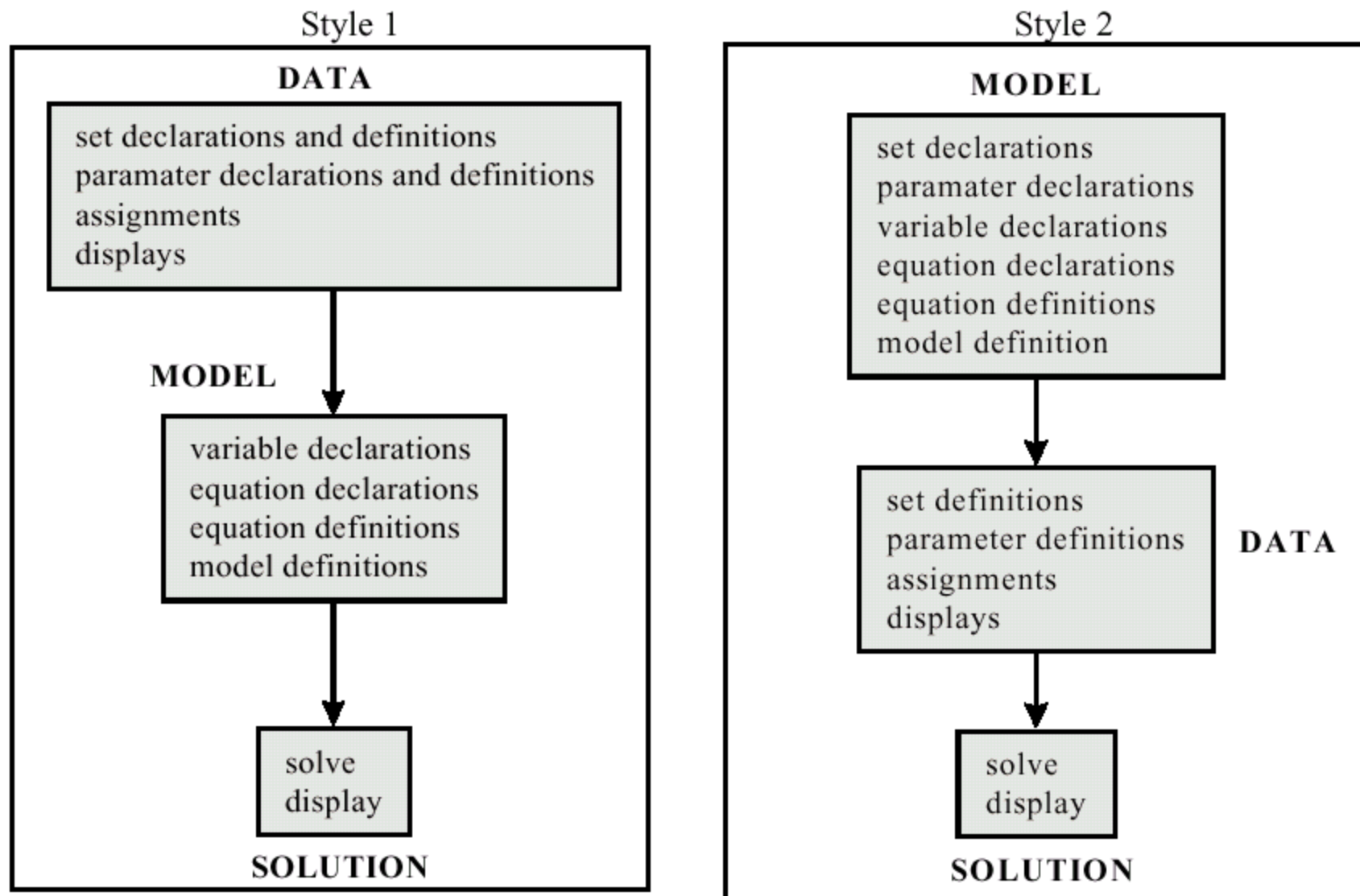
GAMS syntax: the manual

8 A GAMS TUTORIAL

| Inputs | Outputs |
|--|--|
| <ul style="list-style-type: none">• Sets<ul style="list-style-type: none">DeclarationAssignment of members• Data<ul style="list-style-type: none">(Parameters, Tables, Scalars)DeclarationAssignment of values• Variables<ul style="list-style-type: none">DeclarationAssignment of type• Assignment of bounds and/or initial values (optional)• Equations<ul style="list-style-type: none">DeclarationDefinition• Model and Solve statements• Display statement (optional) | <ul style="list-style-type: none">• Echo Print• Reference Maps• Equation Listings• Status Reports• Results |

GAMS logic: the manual

3.3 DATA TYPES AND DEFINITIONS



Parameter declarations

IDE Gamside: D:\Models\Small\small.gms ID:ATEACHU~1\TINBER~1\GCEMOD~1\DISK1\GAMSMO~1\GCE123\GCE123.GMS1

IDE File Edit Search W



cge123.gms

Parameters

```
* Here we define a mix of policy and functional parameters

PWm      world price of import good
PWe      world price of export good
tm        import tariff
te        export subsidy rate
ts        sales or excise of VAT tax rate
ty        direct income tax rate
tr        government transfers
ft        foreign transfers to government
re        foreign remittances to private sector
sr        average savings rate
X         aggregate output
G         government demand
B         balance of trade
at        technical shift term for CET expression
OMEGA     export transformation elasticity
rt        the CET exponential term
aq        technical shift term for CES expression
sigma     import substitution elasticity
rq        the CES exponential term
bq        the CES weight term in the Armington function
bt        the CET weight term in the national product function
values(vars,exp) a table to hold experiment values
;

*Initialization of parameters

PWm      = 0.8860;
PWe      = 1.0107;
tm        = 0.1287;
te        = 0.0107;
ts        = 0.0839;
ty        = 0.0350;
tr        = 0.1237;
```



cge123.gms

Equation definitions

\$Stitle equation definitions

Equations

**Real flow equations with numbering following Devarajan et al*

EQ621 definition of the product transformation surface
EQ622 definition of the Armington aggregation function
EQ623 expenditure definition of national income
EQ624 supply ratios based on EQ621
EQ625 supply ratios based on EQ622

**Nominal flows*

EQ626 government tax income definition
EQ627 value added definition of national income
EQ628 savings definition
EQ629 consumption definition

**Price equations*

EQ630 internal import prices
EQ631 internal export prices
EQ632 consumer prices
EQ633 national product price index
EQ634 producer prices for the composite good
EQ635 real exchange rate

**Market clearing Equations*

EQ636 domestic good excess demand
EQ637 Armington composite excess demand
EQ638 capital and current account relationship
EQ639 savings investment linkage

**Objective function*

OBJ This is the fake objective function for GAMS
;

IDE Gamside: D:\Models\Small\small.gpr - [D:\TEACHI~1\TINBER~1\CGEMOD~1\DISK\GAMSMO~1\CGE123\CGE123.GMS]

IDE File Edit Search Winc

Model specification

cge123.gms

```
- endog("Qd")                                     =e= 0;
EQ638..      B
- (PWm*endog("M") -PWe*endog("E") - ft - re)       =e= 0;
EQ639..      endog("Z")
- ((1/endog("Pt")) * endog("S"))                   =e= 0;
OBJ..
      GDP
- endog("Y")                                       =e= 0;

Model model1 / EQ621, EQ622, EQ623, EQ624, EQ625, EQ626, EQ627,
               EQ628, EQ629, EQ630, EQ631, EQ632, EQ633, EQ634,
               EQ635, EQ636, EQ637, EQ638, EQ639, OBJ / ;

option nlp=minos5;
model1.iterlim = 1000; model1.optfile=4;
Solve model1 maximizing GDP using nlp;

values(vars,exp) = endog.l(vars);

$Ontext

    In this next section we implement a free trade experiment,
    along the lines of the Devarajan et al chapter. We set the import
    tariff and export tax to zero

$Offtext

tm = 0;
te = 0;

option nlp=minos5;
model1.iterlim = 1000; model1.optfile=4;
Solve model1 maximizing GDP using nlp;
```

295: 62 Insert

Running in GAMS IDE

IDE Gamside: D:\Models\Small\small.gpr - [D:\TEACHI~1\TINBER~1\CGEMOD~1\DISK\GAMSMO~1\CGE123\CGE123.GMS]

File Edit Search Windows Help

- New Ctrl+N
- Open Ctrl+O
- Reopen Alt+R
- Open in New Window Shift+Ctrl+O
- Model Library
- Project
- Run F9**
- Compile Shift+F9
- Save Ctrl+S
- Save as
- Save All Shift+Ctrl+S
- Close
- Options
- Print
- Previous
- Exit

```
endog("E") - ft - re)

endog("S")

2, EQ623, EQ624, EQ625, EQ626, EQ627,
9, EQ630, EQ631, EQ632, EQ633, EQ634,
6, EQ637, EQ638, EQ639, OBJ / ;

model1.iterlim = 1000; model1.optfile=4;
Solve model1 maximizing GDP using nlp;

values(vars,exp) = endog.l(vars);

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    along the lines of the Devarajan et al chapter. We set the import
    tariff and export tax to zero

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tm = 0;
te = 0;

option nlp=minos5;
model1.iterlim = 1000; model1.optfile=4;
Solve model1 maximizing GDP using nlp;
```

295: 62 Insert Run GAMS

Start | qams | villars.doc | Microsoft P... | IDE Gamside | 1:32 PM

The solution screen

```
GAMS Rev 120 Copyright (C) 1987-2001 GAMS Development. All rights reserved
Licensee: Economics Department A010221:1033CP-WIN
Erasmus Universiteit Rotterdam DC418

--- Starting compilation
--- CGE123.GMS(333) 1 Mb
--- Starting execution
--- CGE123.GMS(276) 1 Mb
--- Generating model model1
--- CGE123.GMS(277) 2 Mb
--- 20 rows, 21 columns, and 65 non-zeroes.
--- CGE123.GMS(277) 2 Mb
--- Executing MINOS5

MINOS5 Feb 14, 2001 WIN.M5.M5 19.8 108.043.039.WAT

The options file could not be found -- using defaults
Work space allocated -- 0.04 Mb
Reading data...
Reading nonlinear code...

Major Minor Ninf Sinf,Objective Viol RG NSB Ncon Penalty Step
1 0 1 0.00000000E+00 8.4E-02 0.0E+00 14 3 1.0E+01 1.0E+00
2 14 0 1.13158934E+00 5.9E-03 0.0E+00 0 4 1.0E+01 1.0E+00
3 0 0 1.12985912E+00 8.9E-06 0.0E+00 0 5 1.0E+01 1.0E+00
4 0 0 1.12986053E+00 1.5E-11 0.0E+00 0 6 1.0E+01 1.0E+00
5 0 0 1.12986053E+00 2.2E-16 0.0E+00 0 7 0.0E+00 1.0E+00

EXIT -- OPTIMAL SOLUTION FOUND

Major, Minor itns 5 14
Objective function 1.1298605309416E+00
```

295: 62 Insert Double-Click to Open File

Some results

IDE Gamside: D:\Models\Small\small.gpr - [D:\Models\Small\CGE123.lst]

IDE File Edit Search Windows Help

cgel23.gms cgel23.lst

```
Execution

----- 333 PARAMETER values a table to hold experiment values

benchmark  freetrade  revenue_r~
E          0.3276     0.3371     0.3363
M          0.5030     0.5138     0.5129
Ds         0.6724     0.6626     0.6634
Dd         0.6724     0.6626     0.6634
Qs         1.1754     1.1760     1.1760
Qd         1.1754     1.1760     1.1760
Pe         1.0000     1.0107     1.0000
Pm         1.0000     0.8860     0.8860
Pd         0.9999     0.9405     0.9360
Pt         1.0839     0.9939     1.0487
Px         1.0000     0.9639     0.9573
Pq         1.0000     0.9169     0.9144
T          0.1920     0.1284     0.1920
R          1.0000     1.0000     1.0000
Sg         -0.0100    -0.0612     0.0044
Y          1.1299     1.0835     1.0766
C          0.8288     0.8668     0.8163
S          0.2660     0.2069     0.2713
Z          0.2454     0.2082     0.2587
ts         0.0839     0.0839     0.1469

EXECUTION TIME      =      0.050 SECONDS    1.4 Mb    WIN198-120

USER: Economics Department      A010221:1033CP-WIN
      Erasmus Universiteit Rotterdam      DC418
```

1:1 Read Only Insert



Thank you