## Astrophysical Dynamics (ASTP-617) Notes

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# Chapter 1

# Introduction and Historical Overview

## Chapter 2

# Observations of Galactic Nuclei and Supermassive Black Holes

## 2.1 Structure of galaxies and galactic nuclei

### 2.1.1 Intensity profiles

Intensity profiles are functions used to describe the intensity of a galaxy as a function of distance from the center, I(R).

The **Sérsic profile** is commonly used, as it is simple and effective. The general form is:

$$\ln I(R) = \ln I_e - b \, n \left[ \left( R/R_e \right)^{1/n} - 1 \right]. \tag{Merritt 2.3}$$

The **Sérsic index**, n, characterizes the shape of the function, and in practice,  $n \in [0.5, 8]$ . b is typically chosen such that  $R_e$ , the **effective radius**, contains half of the total light. The effective intensity,  $I_e$ , is thus defined as  $I_e \equiv I(R_e)$ .

To make the function a little more intuitive, one may use differentiation to put it in the form:

$$\frac{\mathrm{d}\ln I}{\mathrm{d}\ln R} = -\frac{b}{n} \left(\frac{R}{R_e}\right)^{1/n} \tag{Merritt 2.4}$$

This form illustrates the fact that the slope on a log-log plot of the intensity grows with R by  $(R/R_e)^{1/n}$ . In many galaxies, within a radius  $R_b$ , there is a break in the intensity profile (shown in Merritt Figure 2.2). For this reason, it is necessary to define a **core-Sérsic profile**:

$$I(r) = \begin{cases} I_b \left(\frac{R_b}{R}\right)^{\Gamma}, & R \leq R_b, \\ I_b \exp\left(b(R_b/R_e)^{1/n}\right) \exp\left(-b(R/R_e)^{1/n}\right), & R > R_b. \end{cases}$$
(Merritt 2.8)

- 2.2 Techniques for weighing black holes
- 2.3 Supermassive black holes in the Local Group
- 2.4 Phenomenology
- 2.5 Evidence for intermediate-mass black holes
- 2.6 Evidence for binary and multiple supermassive black holes

### 2.7 Gravitational waves

The amplitude, h, of a gravitational wave is a dimensionless quantity given by

$$h \approx \frac{G}{c^4} \frac{\ddot{Q}}{D} \approx \frac{GM_Q}{c^2 D} \frac{v^2}{c^2},$$
 (Merritt 2.55)

where v is the internal velocity of the source,  $M_Q$  is the portion of the source's mass (in units of mass, not just 0–1) participating in the quadrupolar motions, and D is the distance to the source.

To understand the detector size needed to observe a gravitational wave, consider the ideal case, where the entire mass is participating in quadrupolar motions ( $M_Q = M_{12}$ ), and the binary is located at a distance D from the observer and a from each other. Then we have  $v^2 \approx G M_{12}/a$ , and from (Merritt 2.55) we have

$$h \approx \frac{GM_{12}}{c^2 D} \frac{GM_{12}}{ac^2}$$

$$\approx \frac{G^2}{c^4} M_{12}^2 a^{-1} D^{-1}$$

$$\approx 2 \times 10^{-16} \left(\frac{M_{12}}{10^{-8} M_{\odot}}\right)^2 \left(\frac{a}{\text{mpc}}\right)^{-1} \left(\frac{D}{100 \text{Mpc}}\right)^{-1}$$
(Merritt 2.58)