

Mathematica Code For Simplex Method

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Abstract

The software below is based on the two-phase method and the development environment is Mathematica 6.0.3. It is capable of solving all the LP-problems theoretically. Tests from several textbooks justify its correctness, efficiency and robustness. The code below can be divided into three parts. The first part defines all the preliminary functions that will be called in the later part. The second one is the kernel of the application. The function—"cals"—can take record of the entire calculating-process and get the final result. The last part defines the GUI, which makes it more human interactive and convenient. We haven't envelop the first two parts into the last one, thus it is available anywhere in your mathematica dialog boxes after it has been activated. You can use these functions independently.

1 Introductions of the files

The attachment includes three files:

LP.nb (A mathematica file)

LP.tex (A La Tex file)

LP.pdf (Please open with Adobe Reader)

LP sample.JPG(A sample of calculation)

2 The original code

```
(*The first part of the original code, which defines the functions \
that will be called later*) enfont[x_String] :=(*To beautify the
output form*)
```

```
Style[x, FontFamily -> Times, Italic, Bold];
ifallnega[list_] :=
  (For[i = 1; t = True, i <= Length@list, i++,
    If[list[[i]] > 0, t = False; Break[]]; Return@t);
iftherenon0[list_] :=
  (For[i = 1; t = False, i <= Length@list, i++,
    If[list[[i]] != 0, t = True; Break[]]; Return@t);
ifthere0[list_] :=
  (For[i = 1; t = False, i <= Length@list, i++,
    If[list[[i]] == 0, t = True; Break[]]; Return@t);
```

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```

ifnound[ list_ , mm_ ] :=
  (t = False;
   For[j = 1, j <= Length@list , j++,
     If[list[[j]] > 0,
       For[i = 1, i <= Length@mm, i++,
         If[mm[[i, j]] > 0, Break[]];
       If[i == Length@mm + 1, t = True]
     ]
  ]; Return@t);
solu[ list1_ , list2_ , n_ ] :=
  (*To create an array that represents the solutions*)
  Module[
    {ss = Table[0, {n}]},
    For[i = 1, i <= Length@list1 , i++,
      ss[[list1[[i]]] = list2[[i]]
    ];
    Return@ss
  ];
innum[ list_ , matrix_ , j_ ] :=
  Module[
    {
      m = Length[list],
      tempmin = -8,
      tempnum = -1
    },
    For[i = 1, i <= m, i++,
      If[matrix[[i, j]] > 0,
        tempnum = i;
        tempmin = list[[i]]/matrix[[i, j]];
        Break[],
        Continue[]
      ];
    If[i > m, Print["No positive numbers in the column"],
      For[i = tempnum, i <= m, i++,
        If[matrix[[i, j]] > 0,
          If[list[[i]]/matrix[[i, j]] <= tempmin,
            tempnum = i;
            tempmin = list[[i]]/matrix[[i, j]],
            Continue[]
          ]
        ];
      Return[tempnum ]
    ];
  ];
r1matrix[bb_, mm_, {i_ , j_}] :=
  Module[
    {
      m = Dimensions[mm][[1]],
      n = Dimensions[mm][[2]]
    },
    nextmatrix = Table[0, {m}, {n}];
    nextbb = Table[0, {m}];
    If[mm[[i, j]] != 0,

```

```

    nextmatrix[[i]] = mm[[i]]/nm[[i, j]];
    nextbb[[i]] = bb[[i]]/nm[[i, j]],
    Print["Not_a_non-zero_number"];
For[k = 1, k <= m, k++,
    If[k == i, Continue[],
        nextmatrix[[k]] = mm[[k]] - nm[[k, j]]*nextmatrix[[i]];
        nextbb[[k]] = bb[[k]] - nm[[k, j]]*nextbb[[i]]
    ];
    Return[{nextbb, nextmatrix}]
];
findmaxnum[list_, num_] :=
Module[
{
    maxtemp = num[[1]],
    end = Length[num]
},
For[i = 2, i <= end, i++,
    If[list[[num[[i]]]] > list[[maxtemp]],
        maxtemp = num[[i]]
    ]
];
Return[maxtemp]
];
transback[list_, memo_] :=
(* Transform the the solutions to the original form through elimating \
the non-original variables *)
Module[
{s = Table[0, {Length@memo}]},
For[i = 1, i <= Length@memo, i++,
    If[memo[[i]] == 0, s[[i]] = list[[i]],
        If[memo[[i]] == -1, s[[i]] = -list[[i]],
            s[[i]] = list[[i]] - list[[memo[[i]]]]
        ]
    ]; Return@s
];
stringstatus[sta_] :=
Piecewise[
{
    {font@ "No_feasible_solutions", sta == -1},
    {font@ "Still_calculating", sta == 0},
    {font@ "An_unique_optimal_solution", sta == 1},
    {font@ "Multiple_optimal_solutions", sta == 2},
    {font@ "Unbounded", sta == 3}
}
];
outsigns[i_] :=
Piecewise[{{{"\[LessEqual]", i == -1}, {"=",
    i == 0}, {"\[GreaterEqual]", i == 1}}];
xoutform[
list_] := (Style[Subscript[x, #], Bold, Italic,
    FontFamily -> Times] &
/@ list);

```

*(*The second part starts here, where the key functions are achieved*)*

```

cals[c00i_, bases1i_, bli_, opermatrixi_, artifvi_] :=
Module[
{
m = Dimensions[opermatrixi][[1]],
n = Dimensions[opermatrixi][[2]],
c00 = c00i,
bases1 = bases1i,
b1 = bli,
opermatrix = opermatrixi,
c1 = {},
s = 0,
swap1 = {0, 0},
checks1 = {},
status1 = 0,
artifv = artifvi,
variables = {},
datas1 = {},
swaplist1 = {{0, 0}},
step = 0,
solutions = {},
tempsolu = 0,
memoremain = {},
tempremain = {},
nonbases1 = {}
},
(*To initialise the first section*)
step++;
variables = Range[n];
nonbases1 = Complement[Table[i, {i, 1, n}], bases1];
swaplist1 = {{0, 0}};
If[(s = Length@artifv) != 0,
c00 = Table[0, {n}];
For[i = 1, i <= s, i++,
c00[[artifv[[i]]] = -1]];
c1 = c00[[#]] & /@ bases1;
checks1 =
Table[
c00[[j]] - Sum[c1[[i]]*opermatrix[[i, j]], {i, 1, m}], {j, 1,
n}];
tempsolu = solu[bases1, b1, Dimensions[opermatrix][[2]]];
AppendTo[solutions, {tempsolu.c00, tempsolu}];
If[ifallnega[checks1],
If[iftherenon0[Intersection[bases1, artifv]],
status1 = -1,
If[ifthere0[checks1[[#]] & /@ nonbases1],
status1 = 2, status1 = 1]],
If[ifnobound[checks1, opermatrix],
status1 = 3, status1 = 0]

```

```

];
AppendTo[datas1, Grid[ArrayFlatten@
{{{{"c", SpanFromLeft, SpanFromLeft}}, {c00}},
{{{SpanFromAbove, SpanFromBoth,
SpanFromBoth}}, {Style[Subscript[x, #], Bold, Italic,
FontFamily -> Times] & /@ Range[n]}}},
{Transpose@{c1,
Style[Subscript[x, #], Italic, FontFamily -> Times] & /@
bases1, b1}, opermatrix}},
{{{{"\[Sigma]", SpanFromLeft, SpanFromLeft}}, {checks1}}}},
Background -> {None, None, {0, 0} -> Green}, Frame -> All,
FrameStyle -> Gray,
Dividers -> {
Rule [# , {Thickness[2.2], Blue}] & /@ {1, 4, -1},
Rule [# , {Thickness[2.2], Blue}] & /@ {1, 2, 3, -1, -2}
},
ItemSize -> {3, 2} ]];
(*The first Loop is starting,
meanwhile the corresponding tableau will be created*)
While[
status1 == 0,
swap1[[2]] = findmaxnum[checks1, nonbases1];
swap1[[1]] = innum[b1, opermatrix, swap1[[2]]];
datas1[[step, 2, 2, 3, 1]] = swap1 + {2, 3};
step++;
bases1[[swap1[[1]]]] = swap1[[2]];
nonbases1 = Complement[Table[i, {i, 1, n}], bases1];
c1 = c00[[#]] & /@ bases1;
{b1, opermatrix} = r1matrix[b1, opermatrix, swap1];
checks1 =
Table[
c00[[j]] - Sum[c1[[i]]*opermatrix[[i, j]], {i, 1, m}], {j, 1,
n}];
tempsolu = solu[bases1, b1, Dimensions[opermatrix][[2]]];
AppendTo[solutions, {tempsolu.c00, tempsolu}];
If[ifallnega[checks1],
If[iftherenon0[Intersection[bases1, artifv]], status1 = -1,
If[ifthere0[checks1[[#]] & /@ nonbases1], status1 = 2,
status1 = 1]],
If[ifnobound[checks1, opermatrix], status1 = 3, status1 = 0]
];
AppendTo[datas1, Grid[ArrayFlatten@
{{{{"c", SpanFromLeft, SpanFromLeft}}, {c00}},
{{{SpanFromAbove, SpanFromBoth,
SpanFromBoth}}, {Style[Subscript[x, #], Bold, Italic,
FontFamily -> Times] & /@ Range[n]}}},
{Transpose@{c1,
Style[Subscript[x, #], Italic, FontFamily -> Times] & /@
bases1, b1}, opermatrix}},
{{{{"\[Sigma]", SpanFromLeft, SpanFromLeft}}, {checks1}}}},
Background -> {None, None, {0, 0} -> Green}, Frame -> All,
FrameStyle -> Gray,

```

```

Dividers -> {
  Rule[#, {Thickness[2.2], Blue}] & /@ {1, 4, -1},
  Rule[#, {Thickness[2.2], Blue}] & /@ {1, 2, 3, -1, -2}
},
ItemSize -> {3, 2} ]
];
(*The second part will begin, if it exists*)
If[s != 0 && status1 != -1,
  step++;
  tempremain = Range[n];
  variables = Complement[variables, artifv];
  For[i = 1, i <= Length@artifv, i++,
    tempremain[[artifv[[i]]]] = 0 ];
  memoremain = Table[0, {n}];
  For[i = 1; j = 1, i <= n, i++,
    If[tempremain[[i]] != 0, memoremain[[i]] = j++] ];
  n -= s;
  c00 = Delete[c00i, Transpose@{artifv}];
  opermatrix = Delete[#, Transpose@{artifv}] & /@ opermatrix;
  nonbases1 = Complement[nonbases1, artifv];
  c1 =
    Table[
      c00[[memoremain[[bases1[[i]]]]]], {i, 1,
        Length@bases1}];
  checks1 =
    Table[
      c00[[j]] - Sum[c1[[i]]*opermatrix[[i, j]], {i, 1, m}], {j, 1,
        n}];
  tempsolu = solu[bases1, b1, Dimensions[opermatrixi][[2]]];
  AppendTo[solutions, {tempsolu.c00i, tempsolu}];

  If[ifallnega[checks1],
    If[iftherenon0[Intersection[bases1, artifv]], status1 = -1,
      If[
        ifthere0[
          Table[
            checks1[[memoremain[[nonbases1[[i]]]]]], {i, 1,
              Length@nonbases1}], status1 = 2, status1 = 1]],
        If[ifnobound[checks1, opermatrix], status1 = 3, status1 = 0]
      ];
  AppendTo[datas1, Grid[ArrayFlatten@
    {{{{"c", SpanFromLeft, SpanFromLeft}}, {c00}},
    {{SpanFromAbove, SpanFromBoth,
      SpanFromBoth}}, {Style[Subscript[x, #], Bold, Italic,
      FontFamily -> Times] & /@ variables}},
    {Transpose@{c1,
      Style[Subscript[x, #], Italic, FontFamily -> Times] & /@
        bases1, b1}, opermatrix}},
    {{{"\[Sigma]", SpanFromLeft, SpanFromLeft}}, {checks1}}},
  Background -> {None, None, {0, 0} -> Green}, Frame -> All,
  FrameStyle -> Gray,
  Dividers -> {

```

```

    Rule[#, {Thickness[2.2], Blue}] & /@ {1, 4, -1},
    Rule[#, {Thickness[2.2], Blue}] & /@ {1, 2, 3, -1, -2}
  },
  ItemSize -> {3, 2}   ];
(* Having initialized, it will enter the second loop*)
While[
  status1 == 0,
  swap1[[2]] = findmaxnum[checks1,
    Table[
      memoremain[[nonbases1[[i]]], {i, 1, Length@nonbases1}]];
  swap1[[1]] = innum[b1, opermatrix, swap1[[2]]];
  datas1[[step, 2, 2, 3, 1]] = swap1 + {2, 3};
  step++;
  bases1[[swap1[[1]]]] = variables[[swap1[[2]]   ]];
  nonbases1 = Complement[variables, bases1];
  c1 =
    Table[
      c00[[      memoremain[[ bases1[[i]]   ]]   ]], {i, 1,
        Length@bases1}];
  {b1, opermatrix} = rlmatrix[b1, opermatrix, swap1];
  checks1 =
    Table[
      c00[[j]] - Sum[c1[[i]]*opermatrix[[i, j]], {i, 1, m}], {j, 1,
        n}];
  tempsolu = solu[bases1, b1, Dimensions[opermatrixi][[2]]];
AppendTo[solutions, {tempsolu.c00i, tempsolu}];
If[ifallnega[checks1],
  If[iftherenon0[Intersection[bases1, artifv]], status1 = -1,
  If[
    ifthere0[
      Table[
        checks1[[memoremain[[nonbases1[[i]]]]], {i, 1,
          Length@nonbases1}]], status1 = 2, status1 = 1]],
    If[ifnound[checks1, opermatrix], status1 = 3, status1 = 0]
  ];
AppendTo[datas1, Grid[ArrayFlatten@
  {{{{"c", SpanFromLeft, SpanFromLeft}}, {c00}},
  {{{SpanFromAbove, SpanFromBoth,
    SpanFromBoth}}, {Style[Subscript[x, #], Bold, Italic,
    FontFamily -> Times] & /@ variables}},
  {Transpose@{c1,
    Style[Subscript[x, #], Italic, FontFamily -> Times] & /@
    bases1, b1}, opermatrix},
  {{{" \[Sigma]", SpanFromLeft, SpanFromLeft}}, {checks1}}}],
Background -> {None, None, {0, 0} -> Green}, Frame -> All,
FrameStyle -> Gray,
Dividers -> {
  Rule[#, {Thickness[2.2], Blue}] & /@ {1, 4, -1},
  Rule[#, {Thickness[2.2], Blue}] & /@ {1, 2, 3, -1, -2}
},
  ItemSize -> {3, 2}   ]
]

```

```

];
  Return[{status1, solutions[[step]], solutions, datas1}]
];
(*Here is the third part, which defines all the graphic user \
interfaces and makes the application more human interactive*)
DynamicModule[
{
  m = 0,
  n = 0,
  tempm = 3,
  tempn = 3,
  maxQ = 1,
  maxQ1 = {{1}},
  head1 = {},
  object = {},
  object1 = {},
  v1 = {},
  signsofv = {},
  signsofv1 = {},
  num1 = {},
  inputmatrix = {},
  inputmatrix1 = {},
  signsofeq0 = {},
  signsofeq1 = {},
  signsofeq = {},
  b0 = {},
  b1 = {},
  b = {},
  calmatrix = {{0}},
  c = {},
  nc = 0,
  ncend = 0,
  memo = {},
  bases = {},
  nonbases = {},
  swapnum = {1, 1},
  checknum = {},
  artifv = {},
  artifvend = 0,
  insertrow1 = {},
  deleterow1 = {},
  insertcol1 = {},
  deletocol2 = {},
  addnewrow1 = {},
  addnewcol1 = {},
  start1 = True,
  start2 = False,
  start3 = False,
  opermatrix = {} ,
  operobject = {},
  calresults = {},
  solustatus = 0,

```



```

finalvalue = 0,
finalsolus = {},
originalsolus = {},
originalvalue = 0,
initiQ = False
},
Column@{
  Grid@
  {
    {
      Text["The_number_of_equations:"],
      InputField[Dynamic[tempm], Number, ImageSize -> {35, 20},
        Enabled -> Dynamic@start1],
      Button["+", If[(++tempm) < 1, tempm = 1],
        Enabled -> Dynamic@start1],
      Button["-", If[(--tempm) < 1, tempm = 1],
        Enabled -> Dynamic@start1],
      Dynamic@If[IntegerQ[tempm], "OK", tempm = IntegerPart[tempm]],
      Dynamic@If[tempm < 1, tempm = 1, "OK"]
    },
    {
      Text["The_number_of_variables:"],
      InputField[Dynamic[tempn], Number, ImageSize -> {35, 20},
        Enabled -> Dynamic@start1],
      Button["+", If[(++tempn) < 1, tempn = 1],
        Enabled -> Dynamic@start1],
      Button["-", If[(--tempn) < 1, tempn = 1],
        Enabled -> Dynamic@start1],
      Dynamic@If[IntegerQ[tempn], "OK", tempn = IntegerPart[tempn]],
      Dynamic@If[tempn < 1, tempn = 1, "OK"]
    },
    {
      Button[
        "Create_Input_Tableau",
        If[tempm < 1, m = tempm = 1, m = tempm];
        If[tempn < 1, n = tempn = 1, n = tempn];
        maxQ = 1;
        maxQ1 = {{PopupMenu[
          Dynamic[maxQ], {0 -> "min", 1 -> "max"}]}};
        head1 = {{Style["No.", Bold, Italic, FontColor -> Green]}};
        object = Table[0, {n}];
        object1 = {InputField[Dynamic[object[[#]]], Number,
          ImageSize -> {50, 20}] & /@ Range[n]};
        v1 = {Style[Subscript[x, #], Bold, Italic,
          FontFamily -> Times] &
          /@ Range[n]};
        signsofv = Table[1, {n}];
        signsofv1 = {PopupMenu[Dynamic[signsofv[[#]]],
          {-1 -> "\[LessEqual]0", 1 -> "\[GreaterEqual]0",
            2 -> "?"}] & /@ Range[n]};
        num1 =
          Table[{Style["(" < ToString[i] < ")", Bold,

```

```

        FontFamily -> Times]], {i, 1, m}];
inputmatrix = Table[0, {m}, {n}];
inputmatrix1 = Array[

    InputField[Dynamic@inputmatrix[[#1, #2]], Number,
        Appearance -> Frameless,
        ImageSize -> {25, 20}] &,
    {m, n}];
signsofeq0 = Table[0, {m}];
signsofeq1 = Array[
    {PopupMenu[Dynamic@signsofeq0[[#]],
        {-1 -> "[LessEqual]", 0 -> "=",
        1 -> "[GreaterEqual]"}]] &, m];
signsofeq = Table[0, {m}];
b0 = Table[0, {m}];
b1 = Array[{InputField[Dynamic@b0[[#]],
    Number, ImageSize -> {50, 20}]] &, m];
b = Table[0, {m}];
bases = Table[0, {m}];
start1 = False;
start2 = True;
start3 = False

,
Enabled -> Dynamic@start1
],
Button["Reset",
    start1 = True;
    start2 = False;
    start3 = False;
m = 0;
n = 0;
tempm = 3;
tempn = 3;
maxQ = 1;
maxQ1 = {{1}};
head1 = {{}};
object = {};
object1 = {{}};
v1 = {{}};
signsofv = {};
signsofv1 = {{}};
num1 = {{}};
inputmatrix = {{}};
inputmatrix1 = {{}};
signsofeq0 = {};
signsofeq1 = {{}};
signsofeq = {};
b0 = {};
b1 = {{}};
b = {};
calmatrix = {{0}};
c = {};

```

```

nc = 0;
ncend = 0;
memo = {};
bases = {};
nonbases = {};
swapnum = {1; 1};
checknum = {};
artifv = {};
artifvend = 0;
insertrow1 = {{}};
deleterow1 = {{}};
insertcol1 = {{}};
deletecol2 = {{}};
addnewrow1 = {{}};
addnewcol1 = {{}};
opermatrix = {{}} ;
operobject = {};
calresults = {};
solustatus = 0;
finalvalue = 0;
finalsolus = {};
originalsolus = {};
originalvalue = 0;
initiQ = False]
}
},
Dynamic@If[m > 0 && n > 0,
Grid[ArrayFlatten@
{
{maxQ1, object1, "#", "#"},
{"#", v1, "#", "#"},
{head1, signsofv1, "#", "#"},
{num1, inputmatrix1, signsofeq1, b1}
},
Frame -> All],
"Not_Initialized"],
Button
[
"To_Get_Initial_matrix",
nc = n;
ncend = n;
signsofeq = signsofeq0;
For[j = 1, j <= n, j++, If[signsofv[[j]] == 2, ncend++]];
For[i = 1, i <= m, i++,
If[signsofeq[[i]]*If[b0[[i]] >= 0, 1, -1] == 1,
ncend += 2; artifvend++,
If[signsofeq[[i]]*If[b0[[i]] >= 0, 1, -1] == 0,
ncend++; artifvend++,
ncend++
]
]];
memo = Table[0, {n}];

```

```

c = Table[0, {ncend}];
artifv = {};
If[maxQ == 1,
  For[j = 1, j <= n, j++,
    c[[j]] = object[[j]],
  For[j = 1, j <= n, j++,
    c[[j]] = -object[[j]]
  ];
calmatrix = Table[0, {m}, {ncend}];
For[j = 1, j <= n, j++,
  If[
    signsofv[[j]] == 2,
    memo[[j]] = (++nc);
    For[i = 1, i <= m, i++,
      calmatrix[[i, j]] = inputmatrix[[i, j]];
      calmatrix[[i, nc]] = -inputmatrix[[i, j]]
    ],
    memo[[j]] = 0;
    If[signsofv[[j]] == -1,
      For[
        i = 1, i <= m, i++,
        calmatrix[[i, j]] = -inputmatrix[[i, j]]
      ],
      For[i = 1, i <= m, i++,
        calmatrix[[i, j]] = inputmatrix[[i, j]]
      ]
    ]
  ]; (* While ends *)
For[i = 1, i <= m, i++,
  If[b0[[i]] < 0,
    b[[i]] = -b0[[i]];
    calmatrix[[i]] = -calmatrix[[i]];
    signsofeq[[i]] = -signsofeq[[i]],
    b[[i]] = b0[[i]]
  ];
For[i = 1, i <= m, i++,
  If[signsofeq[[i]] == -1,
    calmatrix[[i, ++nc]] = 1;
    bases[[i]] = nc,
  If[signsofeq[[i]] == 0,
    calmatrix[[i, ++nc]] = 1;
    bases[[i]] = nc;
    AppendTo[artifv, nc],
    calmatrix[[i, ++nc]] = -1;
    calmatrix[[i, ++nc]] = 1 ;
    bases[[i]] = nc;
    AppendTo[artifv, nc]
  ]
];
initiQ = True;

```

```

start3 = True;
nonbases =
  Complement[Table[i, {i, 1, Dimensions[calmatrix][[2]]}], bases],
  Enabled -> Dynamic@start2
], (*Button ends*)
Style["Standardized:", FontFamily -> Times, Blue, FontSize -> 14,
  Italic],
Dynamic[Row@{
  If[maxQ == 1,
    "max" {c}.xoutform@Range@ncend,
    "min" {-c}.xoutform@Range@ncend]
  ]],
Dynamic@If[initIQ, Grid[Transpose@ArrayFlatten@{
  {{calmatrix.xoutform@Range@ncend}},
  {outsigns /@ signsofeq}
  }, Alignment -> Left, ItemSize -> {Automatic, 2}],
  "Not_initialized"],
Dynamic@If[m > 0 && n > 0, Grid[{
  {enfont@"Original_variables",
    Item[xoutform@Range[n], ItemSize -> 10]},
  {enfont@"Slack_&_surplus_variables",
    xoutform@Complement[Range[n + 1, ncend], artifv]}],
  {enfont@"Artificial_variables", xoutform@artifv},
  {enfont@"Basic_variables", xoutform@bases},
  {enfont@"Non-basic_variables", xoutform@nonbases}
  ], Frame -> All, ItemSize -> {12, 2}]],
Button["To_calculate",
  calresults = cal[c, bases, b, calmatrix, artifv];
  solustatus = calresults[[1]];
  finalvalue = calresults[[2, 1]];
  finalsolus = calresults[[2, 2]];
  originalsolus = transback[finalsolus, memo];
  originalvalue = If[maxQ == 1, finalvalue, -finalvalue];
  Print@Column@{
    Grid[{{enfont["Status"],
      stringstatus[solustatus]}, {enfont[
        "Current_optimal_value"],
        originalvalue}, {enfont["Current_optimal_solution"],
        originalsolus]}},
    ItemSize -> {12, 2.6}, Frame -> All],
    Column[calresults[[3]], Spacings -> 2],
    Column[calresults[[4]], Spacings -> 2]},
  Enabled -> Dynamic@start3
]
}
] (*The code ends. All the codes merged into only one cell, Press the \
Shift+Enter and enjoy its convenience and efficiency*)

```