

2.28

$$1) \binom{20}{8} \left(\frac{1}{6}\right)^8 \left(1 - \frac{1}{6}\right)^{20-8} = \frac{20!}{8!(20-8)!} \left(\frac{1}{6}\right)^8 \left(\frac{5}{6}\right)^{12} = 125\,970 \cdot \frac{1}{1\,679\,616} \cdot \frac{244\,140\,625}{2\,176\,782\,336} \\ = \frac{5\,125\,732\,421\,875}{609\,359\,740\,010\,496} \approx 0,8412 \%$$

2) On obtient toujours au moins 2 trois, sauf si l'on n'en obtient aucun OU seulement un seul.

$$1 - \left(\binom{20}{0} \left(\frac{1}{6}\right)^0 \left(1 - \frac{1}{6}\right)^{20-0} + \binom{20}{1} \left(\frac{1}{6}\right)^1 \left(1 - \frac{1}{6}\right)^{20-1} \right) = \\ 1 - \left(\frac{20!}{0!(20-0)!} \left(\frac{1}{6}\right)^0 \left(\frac{5}{6}\right)^{20} + \frac{20!}{1!(20-1)!} \left(\frac{1}{6}\right)^1 \left(\frac{5}{6}\right)^{19} \right) = \\ 1 - \left(1 \cdot 1 \cdot \frac{95\,367\,431\,640\,625}{3\,656\,158\,440\,062\,976} + 20 \cdot \frac{1}{6} \cdot \frac{19\,073\,486\,328\,125}{609\,359\,740\,010\,496} \right) = \\ 1 - \frac{95\,367\,431\,640\,625}{3\,656\,158\,440\,062\,976} - \frac{95367431640625}{914039610015744} = \frac{3\,179\,321\,281\,859\,851}{3\,656\,158\,440\,062\,976} \approx 86,96 \%$$