2.14 1)
$$\frac{\sqrt[3]{a^4}}{\sqrt{a}} = \frac{a^{\frac{4}{3}}}{a^{\frac{1}{2}}} = a^{\frac{4}{3} - \frac{1}{2}} = a^{\frac{5}{6}} = \sqrt[6]{a^5}$$

2)
$$\frac{\sqrt[6]{a^5}}{\sqrt[4]{a^3}} = \frac{a^{\frac{5}{6}}}{a^{\frac{3}{4}}} = a^{\frac{5}{6} - \frac{3}{4}} = a^{\frac{1}{12}} = \sqrt[12]{a}$$

3)
$$\frac{\sqrt{a^3}}{\sqrt[5]{a^3}} = \frac{a^{\frac{3}{2}}}{a^{\frac{3}{5}}} = a^{\frac{3}{2} - \frac{3}{5}} = a^{\frac{9}{10}} = \sqrt[10]{a^9}$$

4)
$$\frac{\sqrt[6]{a^5}}{\sqrt{a}\sqrt[3]{a}} = \frac{a^{\frac{5}{6}}}{a^{\frac{1}{2}} \cdot a^{\frac{1}{3}}} = a^{\frac{5}{6} - \frac{1}{2} - \frac{1}{3}} = a^0 = 1$$

5)
$$\frac{\sqrt{a}\sqrt[3]{a}}{\sqrt[4]{a}} = \frac{a^{\frac{1}{2}} \cdot a^{\frac{1}{3}}}{a^{\frac{1}{4}}} = a^{\frac{1}{2} + \frac{1}{3} - \frac{1}{4}} = a^{\frac{7}{12}} = \sqrt[12]{a^7}$$

6)
$$\frac{a}{\sqrt[3]{a^2}\sqrt[4]{a}} = \frac{a}{a^{\frac{2}{3}} \cdot a^{\frac{1}{4}}} = a^{1 - \frac{2}{3} - \frac{1}{4}} = a^{\frac{1}{12}} = \sqrt[12]{a}$$

$$7) \ \frac{\sqrt[3]{a^5} \sqrt[6]{a}}{a^3} = \frac{a^{\frac{5}{3}} \cdot a^{\frac{1}{6}}}{a^3} = a^{\frac{5}{3} + \frac{1}{6} - 3} = a^{-\frac{7}{6}} = \frac{1}{a^{\frac{7}{6}}} = \frac{1}{\sqrt[6]{a^7}} = \frac{1}{\sqrt[6]{a^6 \cdot a}} = \frac{1}{a \sqrt[6]{a}}$$

8)
$$\frac{(\sqrt{a})^3}{a\sqrt[3]{a^2}} = \frac{(a^{\frac{1}{2}})^3}{a \cdot a^{\frac{2}{3}}} = \frac{a^{3 \cdot \frac{1}{2}}}{a^{1 + \frac{2}{3}}} = \frac{a^{\frac{3}{2}}}{a^{\frac{5}{3}}} = a^{\frac{5}{2} - \frac{5}{3}} = a^{-\frac{1}{6}} = \frac{1}{a^{\frac{1}{6}}} = \frac{1}{\sqrt[6]{a}}$$

Algèbre : puissances Corrigé 2.14