1.7 1)
$$\frac{18}{4 - \sqrt{7}} = \frac{18(4 + \sqrt{7})}{(4 - \sqrt{7})(4 + \sqrt{7})} = \frac{72 + 18\sqrt{7}}{4^2 - (\sqrt{7})^2}$$
$$= \frac{72 + 18\sqrt{7}}{9} = \frac{9(8 + 2\sqrt{7})}{9} = 8 + 2\sqrt{7}$$

2)
$$\frac{-\sqrt{2}}{\sqrt{2} - \sqrt{5}} = \frac{-\sqrt{2}(\sqrt{2} + \sqrt{5})}{(\sqrt{2} - \sqrt{5})(\sqrt{2} + \sqrt{5})} = \frac{-\sqrt{2}\sqrt{2} - \sqrt{2}\sqrt{5}}{(\sqrt{2})^2 - (\sqrt{5})^2}$$
$$= \frac{-2 - \sqrt{10}}{-3} = \frac{2 + \sqrt{10}}{3}$$

3)
$$\frac{\sqrt{6}}{-\sqrt{3}-\sqrt{2}} = \frac{\sqrt{6}(-\sqrt{3}+\sqrt{2})}{(-\sqrt{3}-\sqrt{2})(-\sqrt{3}+\sqrt{2})} = \frac{-\sqrt{6}\sqrt{3}+\sqrt{6}\sqrt{2}}{(-\sqrt{3})^2-(\sqrt{2})^2}$$
$$= \frac{-\sqrt{18}+\sqrt{12}}{3-2} = \frac{-3\sqrt{2}+2\sqrt{3}}{1} = -3\sqrt{2}+2\sqrt{3}$$

4)
$$\frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = \frac{\left(\sqrt{5} - \sqrt{3}\right)^2}{\left(\sqrt{5} + \sqrt{3}\right)\left(\sqrt{5} - \sqrt{3}\right)} = \frac{\left(\sqrt{5}\right)^2 - 2\sqrt{5}\sqrt{3} + \left(\sqrt{3}\right)^2}{\left(\sqrt{5}\right)^2 - \left(\sqrt{3}\right)^2}$$
$$= \frac{5 - 2\sqrt{15} + 3}{5 - 3} = \frac{8 - 2\sqrt{15}}{2} = \frac{2\left(4 - \sqrt{15}\right)}{2} = 4 - \sqrt{15}$$

5)
$$\frac{5\sqrt{3} - 3\sqrt{5}}{\sqrt{5} - \sqrt{3}} = \frac{\left(5\sqrt{3} - 3\sqrt{5}\right)\left(\sqrt{5} + \sqrt{3}\right)}{\left(\sqrt{5} - \sqrt{3}\right)\left(\sqrt{5} + \sqrt{3}\right)}$$
$$= \frac{5\sqrt{3}\sqrt{5} + 5\sqrt{3}\sqrt{3} - 3\sqrt{5}\sqrt{5} - 3\sqrt{5}\sqrt{3}}{\left(\sqrt{5}\right)^2 - \left(\sqrt{3}\right)^2}$$
$$= \frac{5\sqrt{15} + 15 - 15 - 3\sqrt{15}}{5 - 3} = \frac{2\sqrt{15}}{2} = \sqrt{15}$$

6)
$$\frac{7\sqrt{5} + 5\sqrt{7}}{\sqrt{7} + \sqrt{5}} = \frac{(7\sqrt{5} + 5\sqrt{7})(\sqrt{7} - \sqrt{5})}{(\sqrt{7} + \sqrt{5})(\sqrt{7} - \sqrt{5})}$$

$$= \frac{7\sqrt{5}\sqrt{7} - 7\sqrt{5}\sqrt{5} + 5\sqrt{7}\sqrt{7} - 5\sqrt{7}\sqrt{5}}{(\sqrt{7})^2 - (\sqrt{5})^2}$$

$$= \frac{7\sqrt{35} - 35 + 35 - 5\sqrt{35}}{7 - 5} = \frac{2\sqrt{35}}{2} = \sqrt{35}$$

Algèbre : racines Corrigé 1.7