

5.14 En utilisant tour à tour les exercices 5.13 et 5.11, on trouve :

$$\begin{aligned}\varphi(n) &= \varphi(p_1^{\alpha_1} p_2^{\alpha_2} \dots p_k^{\alpha_k}) \\&= \varphi(p_1^{\alpha_1}) \varphi(p_2^{\alpha_2}) \dots \varphi(p_k^{\alpha_k}) \\&= p_1^{\alpha_1} \left(1 - \frac{1}{p_1}\right) p_2^{\alpha_2} \left(1 - \frac{1}{p_2}\right) \dots p_k^{\alpha_k} \left(1 - \frac{1}{p_k}\right) \\&= p_1^{\alpha_1} p_2^{\alpha_2} \dots p_k^{\alpha_k} \left(1 - \frac{1}{p_1}\right) \left(1 - \frac{1}{p_2}\right) \dots \left(1 - \frac{1}{p_k}\right) \\&= n \left(1 - \frac{1}{p_1}\right) \left(1 - \frac{1}{p_2}\right) \dots \left(1 - \frac{1}{p_k}\right)\end{aligned}$$