1.4 1) 
$$(4 - \sqrt{3}) \cdot \sqrt{3} = 4 \cdot \sqrt{3} - \sqrt{3} \cdot \sqrt{3}$$
  
=  $4\sqrt{3} - 3$ 

2) 
$$(\sqrt{5} - \sqrt{3}) \cdot \sqrt{15} = \sqrt{5} \cdot \sqrt{15} - \sqrt{3} \cdot \sqrt{15}$$
  
 $= \sqrt{5 \cdot 15} - \sqrt{3 \cdot 15}$   
 $= \sqrt{5 \cdot 5 \cdot 3} - \sqrt{3 \cdot 3 \cdot 5}$   
 $= 5\sqrt{3} - 3\sqrt{5}$ 

3) 
$$(3+\sqrt{5})(2-\sqrt{5}) = 3 \cdot 2 - 3 \cdot \sqrt{5} + 2 \cdot \sqrt{5} - \sqrt{5} \cdot \sqrt{5}$$
  
=  $6 - 3\sqrt{5} + 2\sqrt{5} - 5$   
=  $1 - \sqrt{5}$ 

4) 
$$(7+2\sqrt{6})(9-5\sqrt{6}) = 7 \cdot 9 - 7 \cdot 5\sqrt{6} + 2 \cdot 9\sqrt{6} + 2 \cdot 5\sqrt{6}\sqrt{6}$$
  
=  $63 - 35\sqrt{6} + 18\sqrt{6} + 10 \cdot 6$   
=  $3 - 17\sqrt{6}$ 

5) 
$$(9\sqrt{12}+3)(\sqrt{3}+8) = (9 \cdot 2\sqrt{3}+3)(\sqrt{3}+8) = (18\sqrt{3}+3)(\sqrt{3}+8)$$
  
=  $18\sqrt{3}\sqrt{3}+18\cdot 8\sqrt{3}+3\sqrt{3}+3\cdot 8$   
=  $18\cdot 3+144\sqrt{3}+3\sqrt{3}+24$   
=  $78+147\sqrt{3}$ 

6) 
$$(4\sqrt{3} + \sqrt{45}) (\sqrt{5} - 2\sqrt{27}) = (4\sqrt{3} + 3\sqrt{5}) (\sqrt{5} - 6\sqrt{3})$$
  
 $= 4\sqrt{3}\sqrt{5} - 4 \cdot 6\sqrt{3}\sqrt{3} + 3\sqrt{5}\sqrt{5} - 3 \cdot 6\sqrt{5}\sqrt{3}$   
 $= 4\sqrt{15} - 72 + 15 - 18\sqrt{15}$   
 $= -57 - 14\sqrt{15}$ 

7) 
$$(\sqrt{50} - 5\sqrt{7}) (2\sqrt{28} - \sqrt{18}) = (5\sqrt{2} - 5\sqrt{7}) (4\sqrt{7} - 3\sqrt{2})$$
  
 $= 5 \cdot 4\sqrt{2}\sqrt{7} - 5 \cdot 3\sqrt{2}\sqrt{2} - 5 \cdot 4\sqrt{7}\sqrt{7} + 5 \cdot 3\sqrt{7}\sqrt{2}$   
 $= 20\sqrt{14} - 30 - 140 + 15\sqrt{14}$   
 $= -170 + 35\sqrt{14}$ 

8) 
$$(6+12\sqrt{7})(3-5\sqrt{7}) = 6 \cdot 3 - 6 \cdot 5\sqrt{7} + 12 \cdot 3\sqrt{7} - 12 \cdot 5\sqrt{7}\sqrt{7}$$
  
=  $18 - 30\sqrt{7} + 36\sqrt{7} - 420$   
=  $-402 + 6\sqrt{7}$ 

Algèbre : racines Corrigé 1.4

9) 
$$(3\sqrt{3} + 2\sqrt{28} - \sqrt{12} + 16\sqrt{2})(\sqrt{3} - 2\sqrt{2}) =$$
  
 $(3\sqrt{3} + 4\sqrt{7} - 2\sqrt{3} + 16\sqrt{2})(\sqrt{3} - 2\sqrt{2}) =$   
 $3\sqrt{3}\sqrt{3} - 3\cdot 2\sqrt{3}\sqrt{2} + 4\sqrt{7}\sqrt{3} - 4\cdot 2\sqrt{7}\sqrt{2} - 2\sqrt{3}\sqrt{3} + 2\cdot 2\sqrt{3}\sqrt{2} + 16\sqrt{2}\sqrt{3} - 16\cdot 2\sqrt{2}\sqrt{2} =$   
 $9 - 6\sqrt{6} + 4\sqrt{21} - 8\sqrt{14} - 6 + 4\sqrt{6} + 16\sqrt{6} - 64 =$   
 $-61 + 14\sqrt{6} - 8\sqrt{14} + 4\sqrt{21}$ 

10) 
$$(4-3\sqrt{7})(\sqrt{28}-1)(2-\sqrt{7})(4+\sqrt{63}) =$$
  
 $(4-3\sqrt{7})(2\sqrt{7}-1))((2-\sqrt{7})(4+3\sqrt{7})) =$   
 $(8\sqrt{7}-4-42+3\sqrt{7})(8+6\sqrt{7}-4\sqrt{7}-21) =$   
 $(-46+11\sqrt{7})(-13+2\sqrt{7}) =$   
 $598-92\sqrt{7}-143\sqrt{7}+154 =$   
 $752-235\sqrt{7}$ 

Algèbre : racines Corrigé 1.4