

#### 4.4

- 1) Supposons que la fonction  $f$  admette l'asymptote oblique  $y = m x + h$ .  
Ainsi  $f(x) = m x + h + \delta(x)$  avec  $\lim_{x \rightarrow \infty} \delta(x) = 0$ .

$$(a) \lim_{x \rightarrow \infty} \frac{f(x)}{x} = \lim_{x \rightarrow \infty} \frac{m x + h + \delta(x)}{x} = \lim_{x \rightarrow \infty} \frac{m x}{x} + \frac{h}{x} + \frac{\delta(x)}{x} =$$

$$\lim_{x \rightarrow \infty} m + \lim_{x \rightarrow \infty} \frac{h}{x} + \lim_{x \rightarrow \infty} \frac{\delta(x)}{x} = m + 0 + 0 = m$$

$$(b) \lim_{x \rightarrow \infty} (f(x) - m x) = \lim_{x \rightarrow \infty} (m x + h + \delta(x) - m x) = \lim_{x \rightarrow \infty} h + \delta(x) =$$

$$\lim_{x \rightarrow \infty} h + \lim_{x \rightarrow \infty} \delta(x) = h + 0 = h$$

- 2) Supposons que  $\lim_{x \rightarrow \infty} \frac{f(x)}{x} = m$  et que  $\lim_{x \rightarrow \infty} (f(x) - m x) = h$ .

$$\text{Alors } f(x) = m x + h + \underbrace{(f(x) - m x - h)}_{\delta(x)}.$$

$$\lim_{x \rightarrow \infty} \delta(x) = \lim_{x \rightarrow \infty} f(x) - m x - h = \lim_{x \rightarrow \infty} (f(x) - m x) - h =$$

$$\lim_{x \rightarrow \infty} (f(x) - m x) - \lim_{x \rightarrow \infty} h = h - h = 0$$