2.9 1)
$$8^{\frac{1}{3}} = (2^3)^{\frac{1}{3}} = 2^{3 \cdot \frac{1}{3}} = 2^1 = 2$$

2)
$$16^{\frac{1}{2}} = (2^4)^{\frac{1}{2}} = 2^{4 \cdot \frac{1}{2}} = 2^2 = 4$$

3)
$$5^{-1} = \frac{1}{5^1} = \frac{1}{5}$$

4)
$$9^{-\frac{1}{2}} = (3^2)^{-\frac{1}{2}} = 3^{2 \cdot (-\frac{1}{2})} = 3^{-1} = \frac{1}{3^1} = \frac{1}{3}$$

5)
$$27^{-\frac{1}{3}} = (3^3)^{-\frac{1}{3}} = 3^{3 \cdot (-\frac{1}{3})} = 3^{-1} = \frac{1}{3^1} = \frac{1}{3}$$

6)
$$2^{\frac{1}{2}} = \sqrt[2]{2^1} = \sqrt{2}$$

7)
$$4^{-\frac{1}{4}} = (2^2)^{-\frac{1}{4}} = 2^{2 \cdot (-\frac{1}{4})} = 2^{-\frac{1}{2}} = \frac{1}{2^{\frac{1}{2}}} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$

8)
$$\left(\frac{2}{3}\right)^{-1} = \frac{2^{-1}}{3^{-1}} = \frac{\frac{1}{2^{1}}}{\frac{1}{3^{1}}} = \frac{\frac{1}{2}}{\frac{1}{3}} = \frac{1}{2} \cdot \frac{3}{1} = \frac{3}{2}$$

9)
$$\left(\frac{4}{9}\right)^{\frac{1}{2}} = \left(\frac{2^2}{3^2}\right)^{\frac{1}{2}} = \frac{(2^2)^{\frac{1}{2}}}{(3^2)^{\frac{1}{2}}} = \frac{2^{2 \cdot \frac{1}{2}}}{3^{2 \cdot \frac{1}{2}}} = \frac{2^1}{3^1} = \frac{2}{3}$$

10)
$$\left(\frac{16}{25}\right)^{-\frac{1}{2}} = \left(\frac{2^4}{5^2}\right)^{-\frac{1}{2}} = \frac{(2^4)^{-\frac{1}{2}}}{(5^2)^{-\frac{1}{2}}} = \frac{2^{4 \cdot (-\frac{1}{2})}}{5^{2 \cdot (-\frac{1}{2})}} = \frac{2^{-2}}{5^{-1}} = \frac{\frac{1}{2^2}}{\frac{1}{5^1}} = \frac{\frac{1}{4}}{\frac{1}{5}} = \frac{5}{4}$$

11)
$$\left(\frac{25}{16}\right)^{\frac{1}{4}} = \left(\frac{5^2}{2^4}\right)^{\frac{1}{4}} = \frac{(5^2)^{\frac{1}{4}}}{(2^4)^{\frac{1}{4}}} = \frac{5^{2 \cdot \frac{1}{4}}}{2^{4 \cdot \frac{1}{4}}} = \frac{5^{\frac{1}{2}}}{2^1} = \frac{\sqrt{5}}{2}$$

12)
$$8^{\frac{2}{3}} = (2^3)^{\frac{2}{3}} = 2^{3 \cdot \frac{2}{3}} = 2^2 = 4$$

13)
$$16^{-\frac{3}{4}} = (2^4)^{-\frac{3}{4}} = 2^{4 \cdot (-\frac{3}{4})} = 2^{-3} = \frac{1}{2^3} = \frac{1}{8}$$

14)
$$36^{\frac{5}{2}} = (6^2)^{\frac{5}{2}} = 6^{2 \cdot \frac{5}{2}} = 6^5 = 7776$$

15)
$$2^{\frac{7}{2}} = \sqrt[2]{2^7} = \sqrt{2^{3 \cdot 2 + 1}} = \sqrt{(2^3)^2 \cdot 2} = 2^3 \sqrt{2} = 8\sqrt{2}$$

16)
$$\left(\frac{1}{25}\right)^{\frac{5}{2}} = \left(\frac{1}{5^2}\right)^{\frac{5}{2}} = (5^{-2})^{\frac{5}{2}} = 5^{(-2) \cdot \frac{5}{2}} = 5^{-5} = \frac{1}{5^5} = \frac{1}{3125}$$

17)
$$\left(\frac{4}{9}\right)^{-\frac{3}{2}} = \left(\frac{2^2}{3^2}\right)^{-\frac{3}{2}} = \frac{(2^2)^{-\frac{3}{2}}}{(3^2)^{-\frac{3}{2}}} = \frac{2^{2 \cdot (-\frac{3}{2})}}{3^{2 \cdot (-\frac{3}{2})}} = \frac{2^{-3}}{3^{-3}} = \frac{\frac{1}{2^3}}{\frac{1}{3^3}} = \frac{\frac{1}{8}}{\frac{1}{27}} = \frac{27}{8}$$

18)
$$625^{0,5} = (5^4)^{\frac{1}{2}} = 5^{4 \cdot \frac{1}{2}} = 5^2 = 25$$

19)
$$4^{1,5} = (2^2)^{\frac{3}{2}} = 2^{2 \cdot \frac{3}{2}} = 2^3 = 8$$

20)
$$2^{-3,5} = 2^{-\frac{7}{2}} = \frac{1}{2^{\frac{7}{2}}} = \frac{1}{\sqrt[2]{2^7}} = \frac{1}{\sqrt{2^{3 \cdot 2 + 1}}} = \frac{1}{\sqrt{(2^3)^2 \cdot 2}} = \frac{1}{2^3 \sqrt{2}}$$
$$= \frac{\sqrt{2}}{2^3 \cdot 2} = \frac{\sqrt{2}}{2^4} = \frac{\sqrt{2}}{16}$$

21)
$$9^{1,75} = (3^2)^{\frac{175}{100}} = (3^2)^{\frac{7}{4}} = 3^{2 \cdot \frac{7}{4}} = 3^{\frac{7}{2}} = \sqrt[2]{3^7} = \sqrt{3^{3 \cdot 2 + 1}} = \sqrt{(3^3)^2 \cdot 3}$$

= $3^3 \sqrt{3} = 27 \sqrt{3}$

22)
$$0.25^{0.5} = \left(\frac{1}{4}\right)^{\frac{1}{2}} = \left(\frac{1}{2^2}\right)^{\frac{1}{2}} = (2^{-2})^{\frac{1}{2}} = 2^{-2 \cdot \frac{1}{2}} = 2^{-1} = \frac{1}{2^1} = \frac{1}{2}$$

Algèbre : puissances Corrigé 2.9