



# **Module 4 : Memory Management Virtual Memory Management**



# Memory Management

- Background
- Swapping
- Contiguous Memory Allocation
- Paging
- Structure of the Page Table
- Segmentation



# Objectives

- To provide a detailed description of various ways of organizing memory hardware
- To discuss various memory-management techniques, including paging and segmentation
- To provide a detailed description of the Intel Pentium, which supports both pure segmentation and segmentation with paging



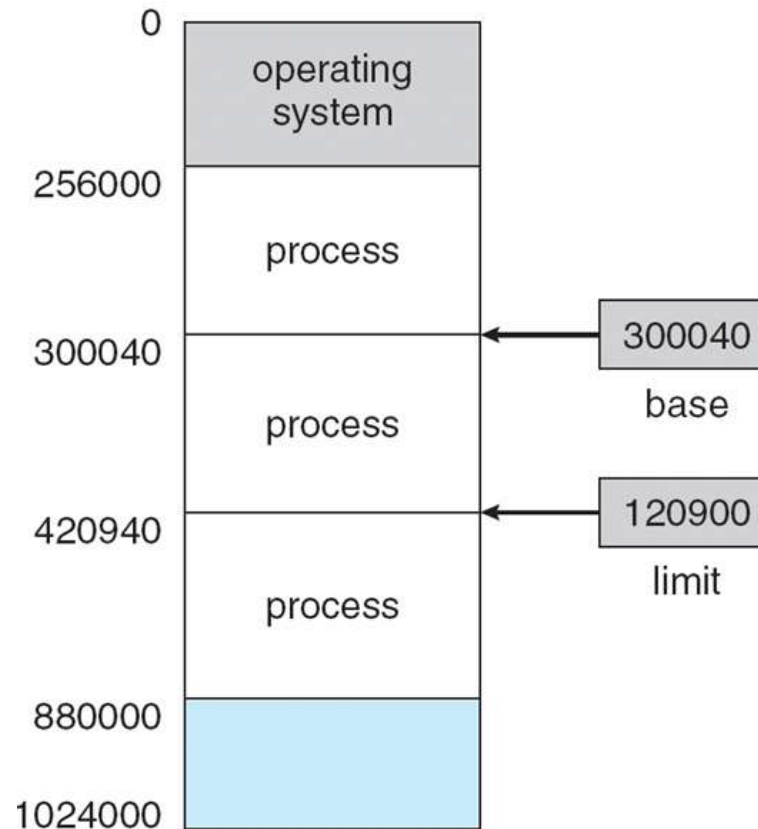
# Background

- Program must be brought (from disk) into memory and placed within a process for it to be run
- Main memory and registers are only storage CPU can access directly
- Register access in one CPU clock (or less)
- Main memory can take many cycles
- **Cache** sits between main memory and CPU registers
- Protection of memory required to ensure correct operation



# Base and Limit Registers

- A pair of **base** and **limit** registers define the logical address space



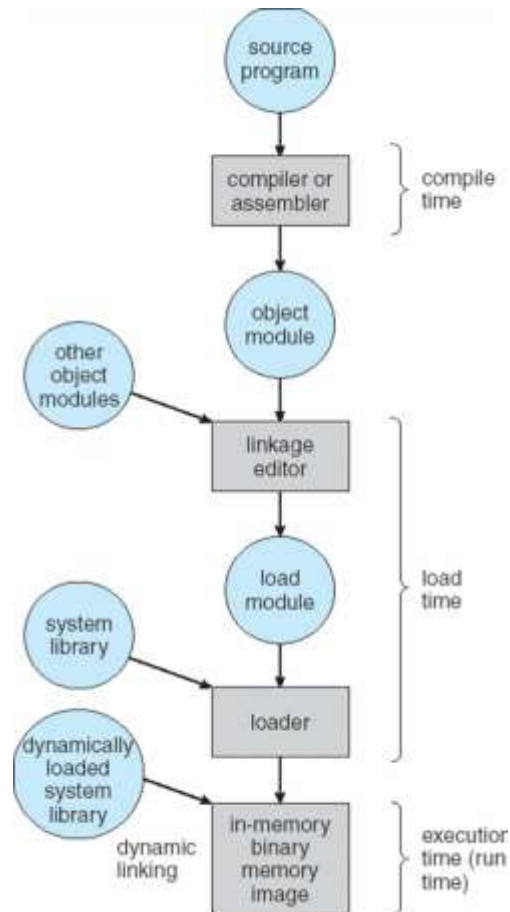


# Binding of Instructions and Data to Memory

- Address binding of instructions and data to memory addresses can happen at three different stages
  - **Compile time:** If memory location known a priori, **absolute code** can be generated; must recompile code if starting location changes
  - **Load time:** Must generate **relocatable code** if memory location is not known at compile time
  - **Execution time:** Binding delayed until run time if the process can be moved during its execution from one memory segment to another. Need hardware support for address maps (e.g., base and limit registers)



# Multistep Processing of a User Program





# Logical vs. Physical Address Space

- The concept of a logical address space that is bound to a separate **physical address space** is central to proper memory management
  - **Logical address** – generated by the CPU; also referred to as **virtual address**
  - **Physical address** – address seen by the memory unit
- Logical and physical addresses are the same in compile-time and load-time address-binding schemes; logical (virtual) and physical addresses differ in execution-time address-binding scheme



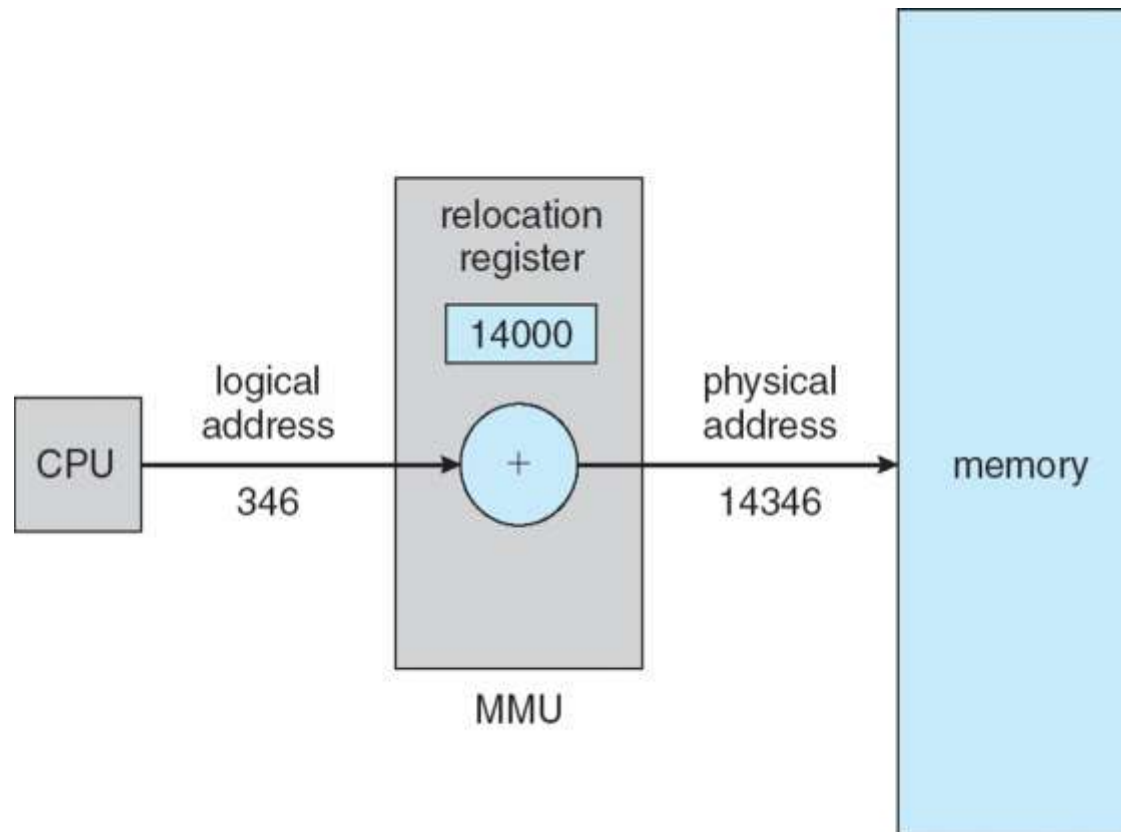


# Memory-Management Unit (MMU)

- Hardware device that maps virtual to physical address
- In MMU scheme, the value in the relocation register is added to every address generated by a user process at the time it is sent to memory
- The user program deals with *logical* addresses; it never sees the *real* physical addresses



# Dynamic relocation using a relocation register





# Dynamic Loading

- Routine is not loaded until it is called
- Better memory-space utilization; unused routine is never loaded
- Useful when large amounts of code are needed to handle infrequently occurring cases
- No special support from the operating system is required implemented through program design



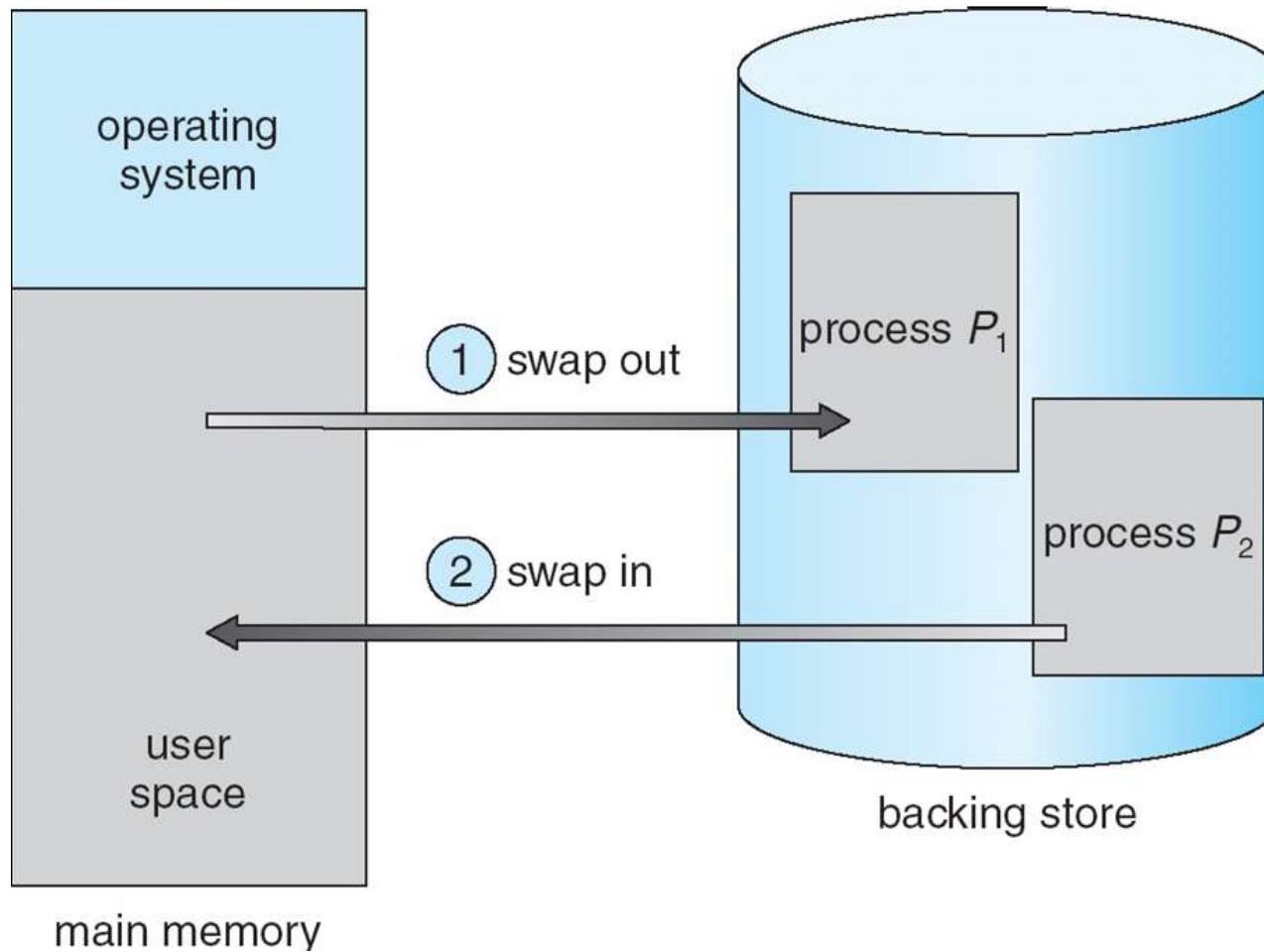
# Dynamic Linking

- Linking postponed until execution time
- Small piece of code, *stub*, used to locate the appropriate memory-resident library routine
- Stub replaces itself with the address of the routine, and executes the routine
- Operating system needed to check if routine is in processes' memory address
- Dynamic linking is particularly useful for libraries
- System also known as **shared libraries**



# Swapping

- A process can be swapped temporarily out of memory to a backing store, and then brought back into memory for continued execution
- **Backing store** – fast disk large enough to accommodate copies of all memory images for all users; must provide direct access to these memory images
- **Roll out, roll in** – swapping variant used for priority-based scheduling algorithms; lower-priority process is swapped out so higher-priority process can be loaded and executed
- Major part of swap time is transfer time; total transfer time is directly proportional to the amount of memory swapped
- Modified versions of swapping are found on many systems (i.e., UNIX, Linux, and Windows)
- System maintains a **ready queue** of ready-to-run processes which have memory images on disk



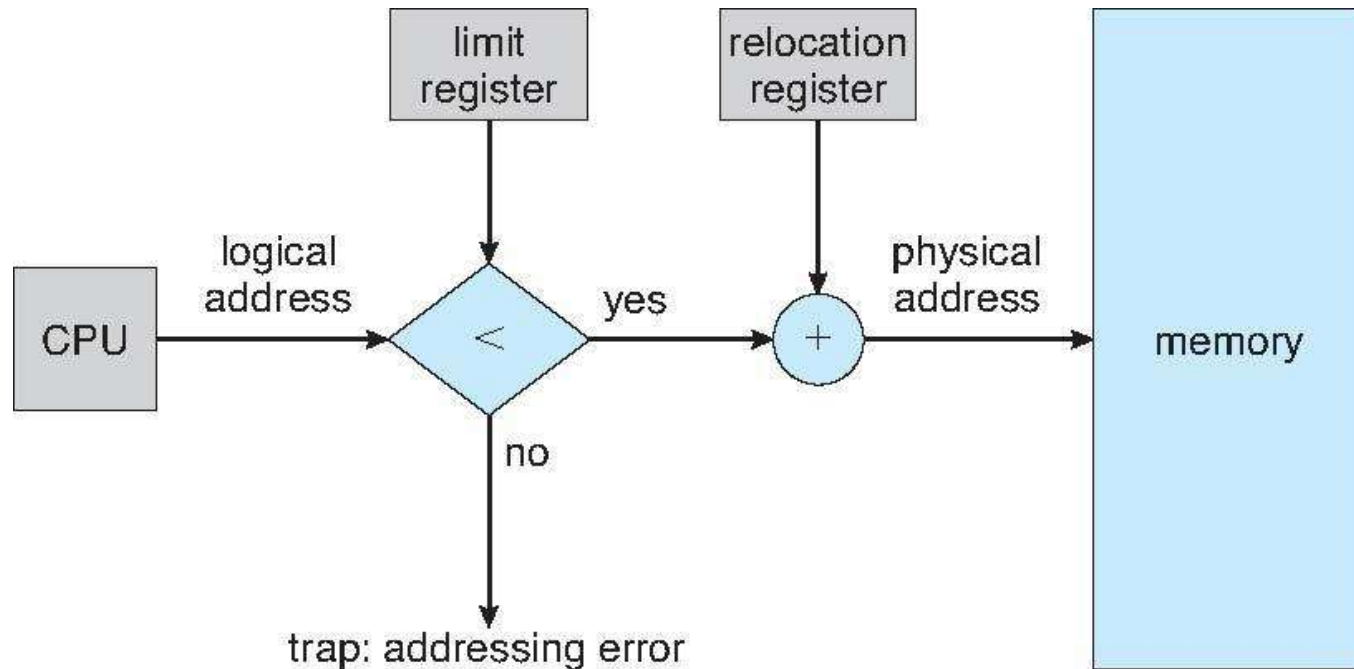


# Contiguous Allocation

- Main memory usually into two partitions:
  - Resident operating system, usually held in low memory with interrupt vector
  - User processes then held in high memory
- Relocation registers used to protect user processes from each other, and from changing operating-system code and data
  - Base register contains value of smallest physical address
  - Limit register contains range of logical addresses – each logical address must be less than the limit register
  - MMU maps logical address *dynamically*



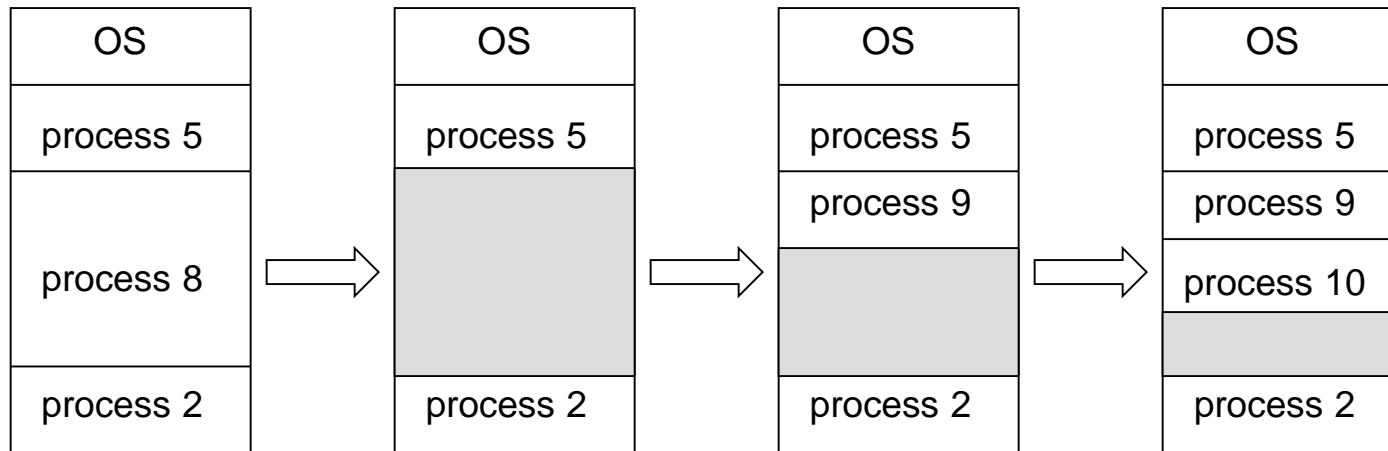
# Hardware Support for Relocation and Limit Registers







- Multiple-partition allocation
  - Hole – block of available memory; holes of various size are scattered throughout memory
  - When a process arrives, it is allocated memory from a hole large enough to accommodate it
  - Operating system maintains information about:
    - a) allocated partitions    b) free partitions (hole)





# Dynamic Storage-Allocation Problem

How to satisfy a request of size  $n$  from a list of free holes

- **First-fit:** Allocate the *first* hole that is big enough
- **Best-fit:** Allocate the *smallest* hole that is big enough; must search entire list, unless ordered by size
  - Produces the smallest leftover hole
- **Worst-fit:** Allocate the *largest* hole; must also search entire list
  - Produces the largest leftover hole

First-fit and best-fit better than worst-fit in terms of speed and storage utilization



# Fragmentation

- **External Fragmentation** – total memory space exists to satisfy a request, but it is not contiguous
- **Internal Fragmentation** – allocated memory may be slightly larger than requested memory; this size difference is memory internal to a partition, but not being used
- Reduce external fragmentation by **compaction**
  - Shuffle memory contents to place all free memory together in one large block
  - Compaction is possible *only* if relocation is dynamic, and is done at execution time
  - I/O problem
    - 4 Latch job in memory while it is involved in I/O
    - 4 Do I/O only into OS buffers



# Paging

- Logical address space of a process can be noncontiguous; process is allocated physical memory whenever the latter is available
- Divide physical memory into fixed-sized blocks called **frames** (size is power of 2, between 512 bytes and 8,192 bytes)
- Divide logical memory into blocks of same size called **pages**
- Keep track of all free frames
- To run a program of size  **$n$**  pages, need to find  $n$  free frames and load program
- Set up a page table to translate logical to physical addresses
- Internal fragmentation



# Address Translation Scheme

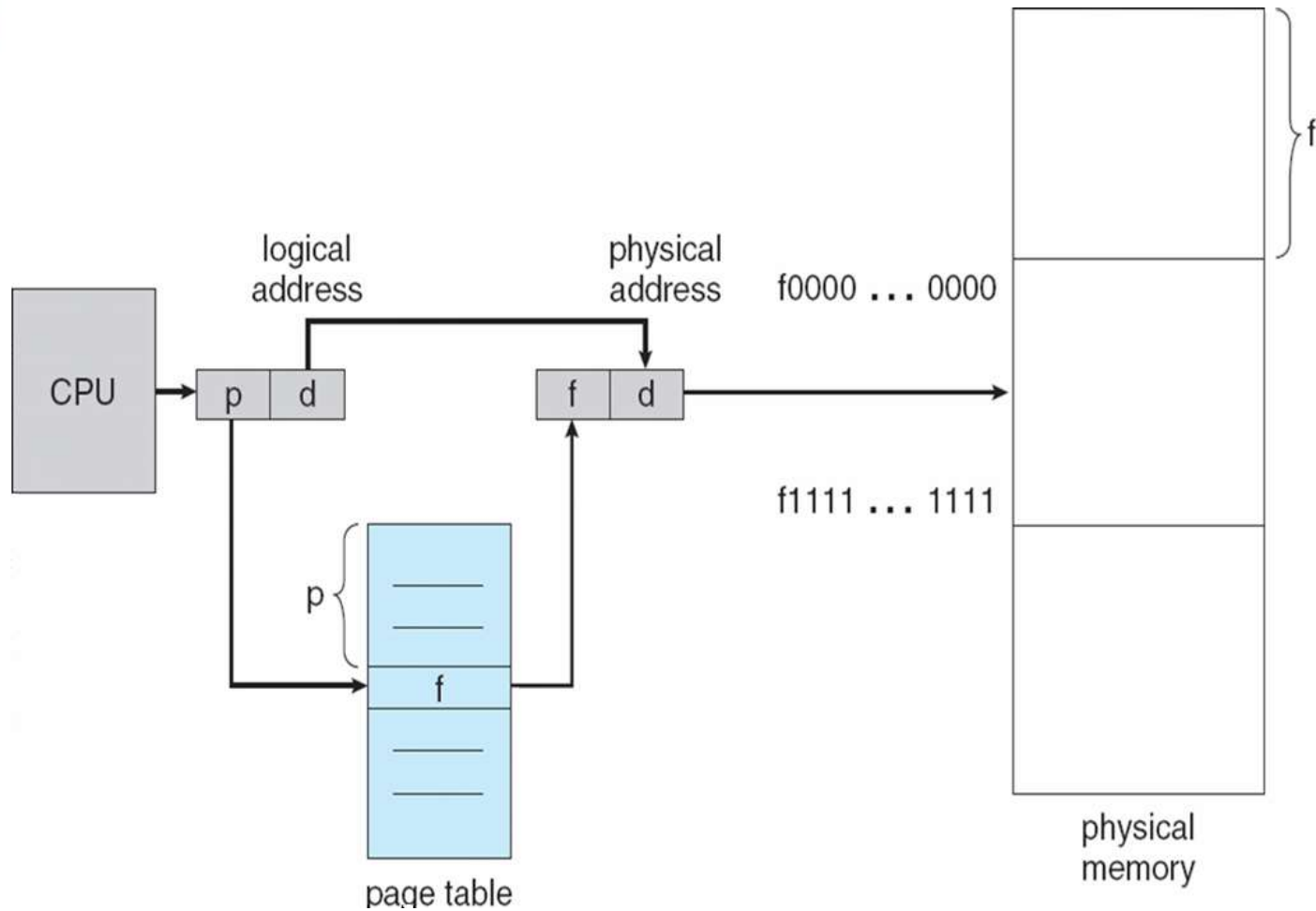
- Address generated by CPU is divided into:
  - **Page number ( $p$ )** – used as an index into a *page table* which contains base address of each page in physical memory
  - **Page offset ( $d$ )** – combined with base address to define the physical memory address that is sent to the memory unit

| page number | page offset |
|-------------|-------------|
| $p$         | $d$         |
| $m - n$     | $n$         |

- For given logical address space  $2^m$  and page size  $2^n$

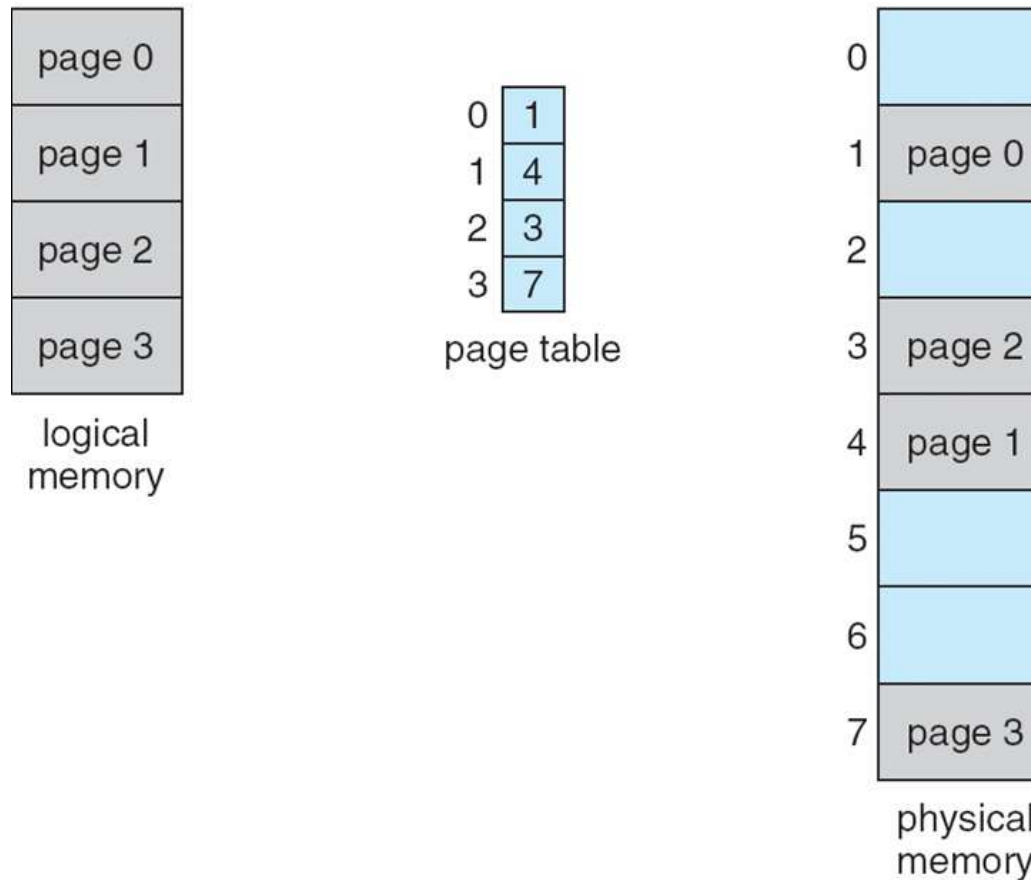


# Paging Hardware



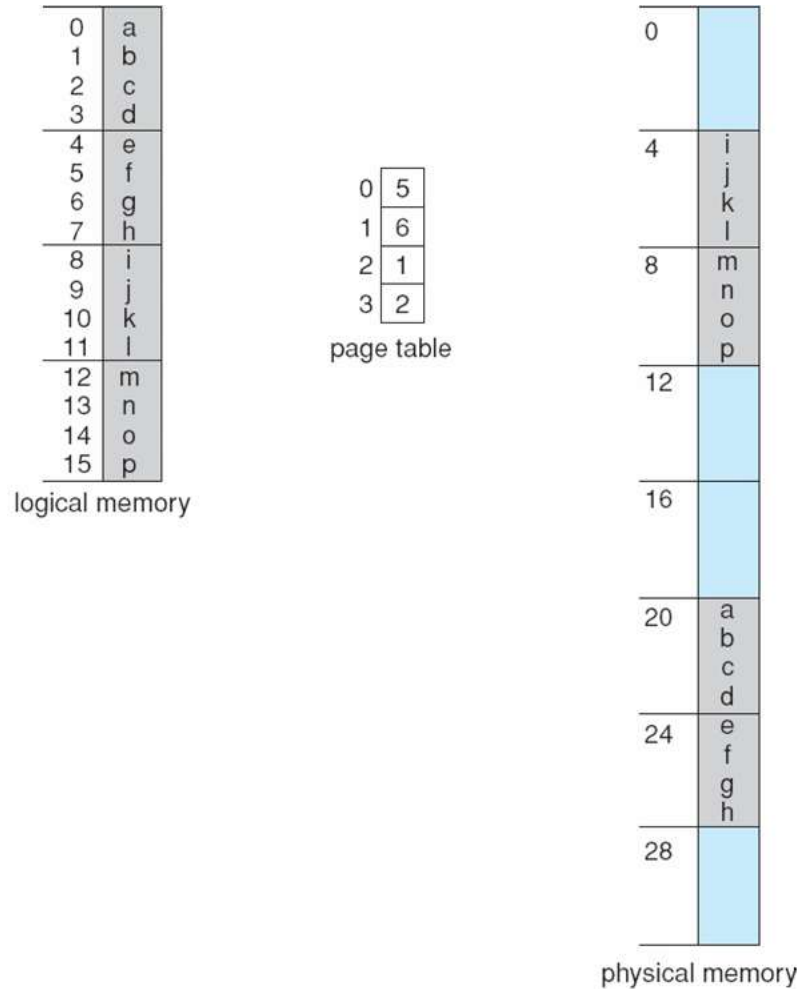


# Paging Model of Logical and Physical Memory





# Paging Example



32-byte memory and 4-byte pages

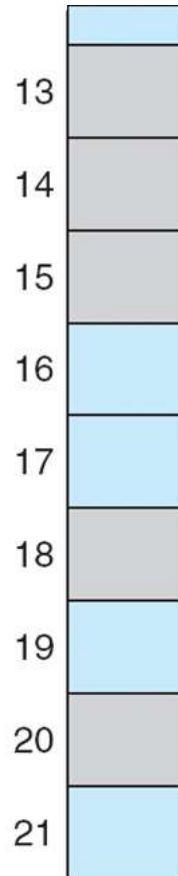
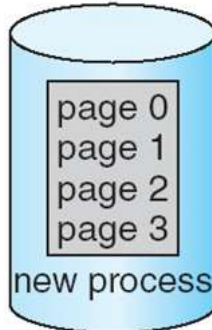




# Free Frames

free-frame list

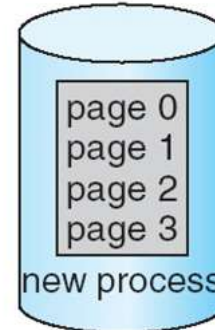
14  
13  
18  
20  
15



(a)

Before allocation

free-frame list  
15

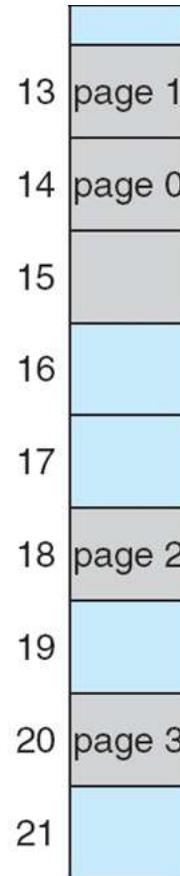


|   |    |
|---|----|
| 0 | 14 |
| 1 | 13 |
| 2 | 18 |
| 3 | 20 |

new-process page table

(b)

After allocation





- Page table is kept in main memory
- **Page-table base register (PTBR)** points to the page table
- **Page-table length register (PRLR)** indicates size of the page table
- In this scheme every data/instruction access requires two memory accesses. One for the page table and one for the data/instruction.
- The two memory access problem can be solved by the use of a special fast-lookup hardware cache called **associative memory** or **translation look-aside buffers (TLBs)**
- Some TLBs store **address-space identifiers (ASIDs)** in each TLB entry – uniquely identifies each process to provide address-space protection for that process



# Associative Memory

- Associative memory – parallel search

| Page # | Frame # |
|--------|---------|
|        |         |
|        |         |
|        |         |
|        |         |

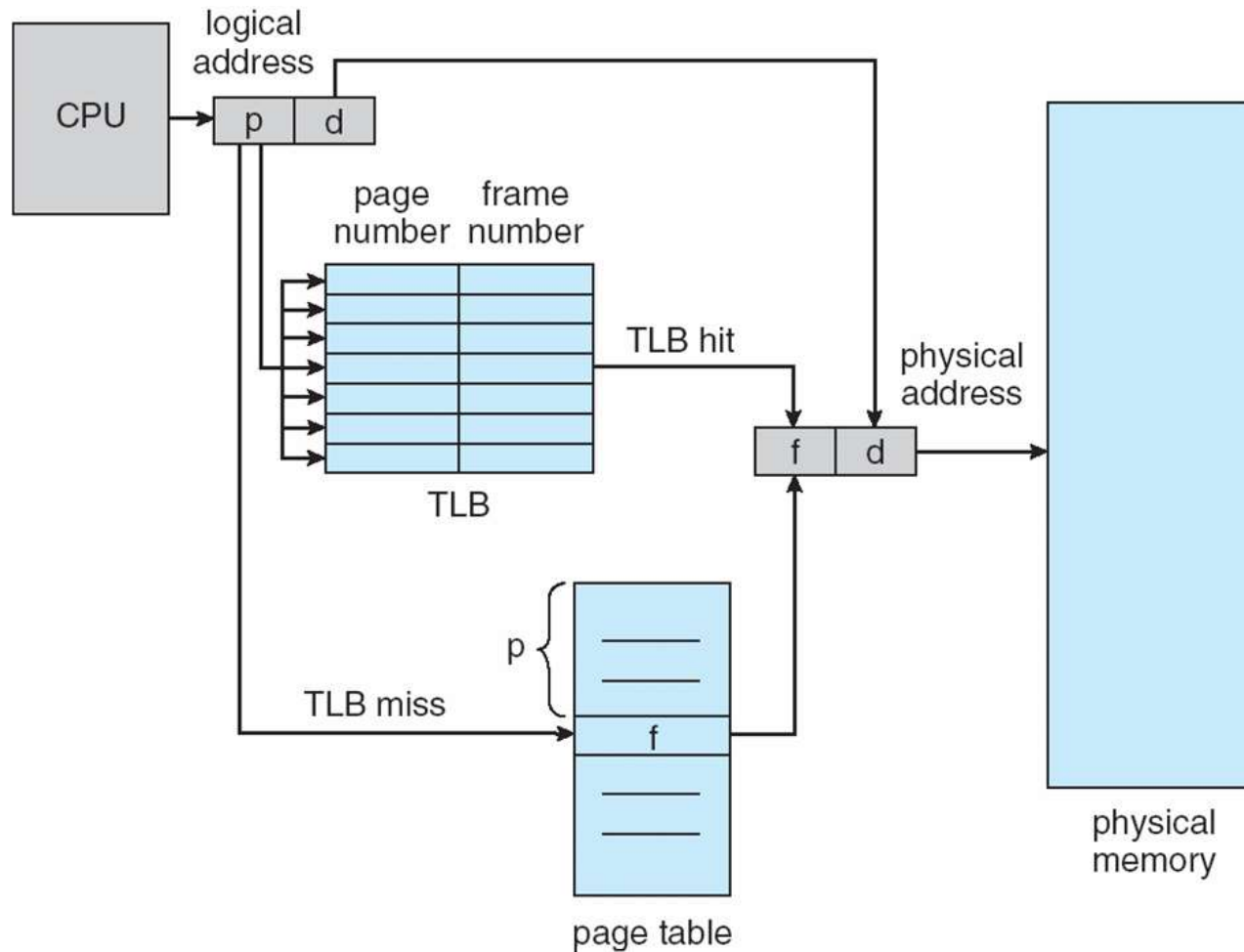
Address translation (p, d)

- If p is in associative register, get frame # out
- Otherwise get frame # from page table in memory



# Paging Hardware With TLB

*Go, change the world*





# Effective Access Time

- Associative Lookup =  $\epsilon$  time unit
- Assume memory cycle time is 1 microsecond
- Hit ratio – percentage of times that a page number is found in the associative registers; ratio related to number of associative registers
- Hit ratio =  $\alpha$
- **Effective Access Time** (EAT)

$$\begin{aligned} \text{EAT} &= (1 + \epsilon) \alpha + (2 + \epsilon)(1 - \alpha) \\ &= 2 + \epsilon - \alpha \end{aligned}$$



# Memory Protection

- Memory protection implemented by associating protection bit with each frame
- **Valid-invalid** bit attached to each entry in the page table:
  - “valid” indicates that the associated page is in the process’ logical address space, and is thus a legal page
  - “invalid” indicates that the page is not in the process’ logical address space



# Valid (v) or Invalid (i) Bit In A Page Table

|        |        |
|--------|--------|
| 00000  | page 0 |
|        | page 1 |
|        | page 2 |
|        | page 3 |
|        | page 4 |
| 10,468 | page 5 |
| 12,287 |        |

| frame number |   | valid-invalid bit |
|--------------|---|-------------------|
| 0            | 2 | v                 |
| 1            | 3 | v                 |
| 2            | 4 | v                 |
| 3            | 7 | v                 |
| 4            | 8 | v                 |
| 5            | 9 | v                 |
| 6            | 0 | i                 |
| 7            | 0 | i                 |

page table

|   |          |
|---|----------|
| 0 |          |
| 1 |          |
| 2 | page 0   |
| 3 | page 1   |
| 4 | page 2   |
| 5 |          |
| 6 |          |
| 7 | page 3   |
| 8 | page 4   |
| 9 | page 5   |
|   | ⋮        |
|   | page $n$ |



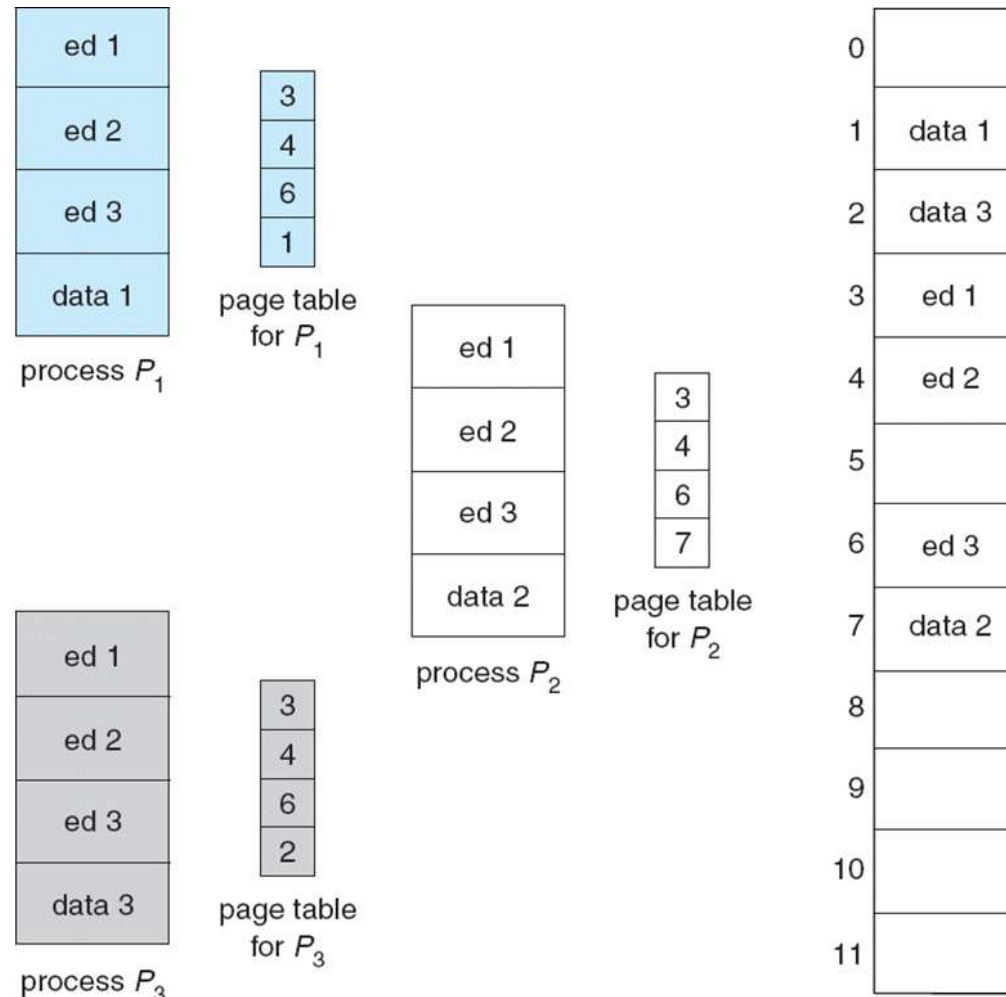
# Shared Pages

- **Shared code**
  - One copy of read-only (reentrant) code shared among processes (i.e., text editors, compilers, window systems).
  - Shared code must appear in same location in the logical address space of all processes
- **Private code and data**
  - Each process keeps a separate copy of the code and data
  - The pages for the private code and data can appear anywhere in the logical address space





# Shared Pages Example





- Hierarchical Paging
- Hashed Page Tables
- Inverted Page Tables

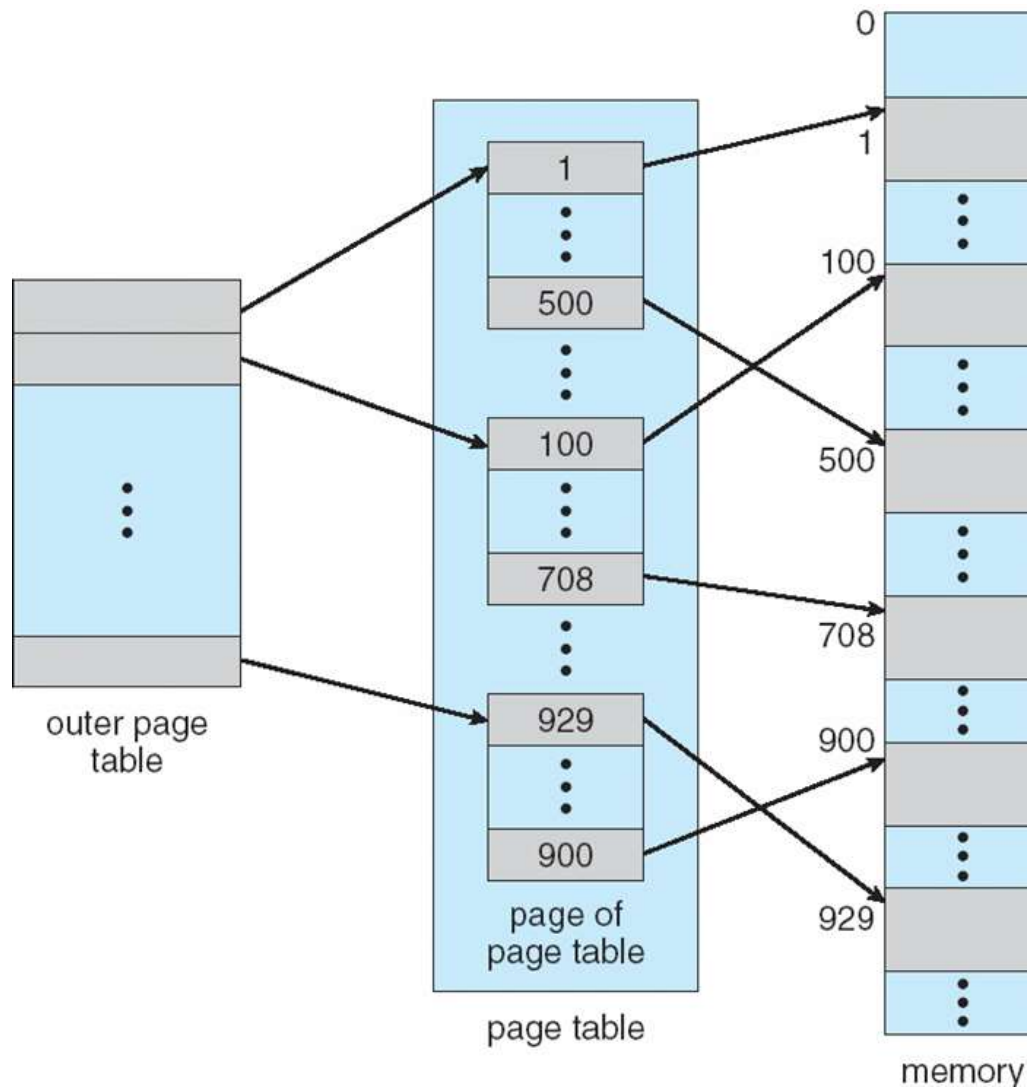


# Hierarchical Page Tables

- Break up the logical address space into multiple page tables
- A simple technique is a two-level page table



# Two-Level Page-Table Scheme





# Two-Level Paging Example

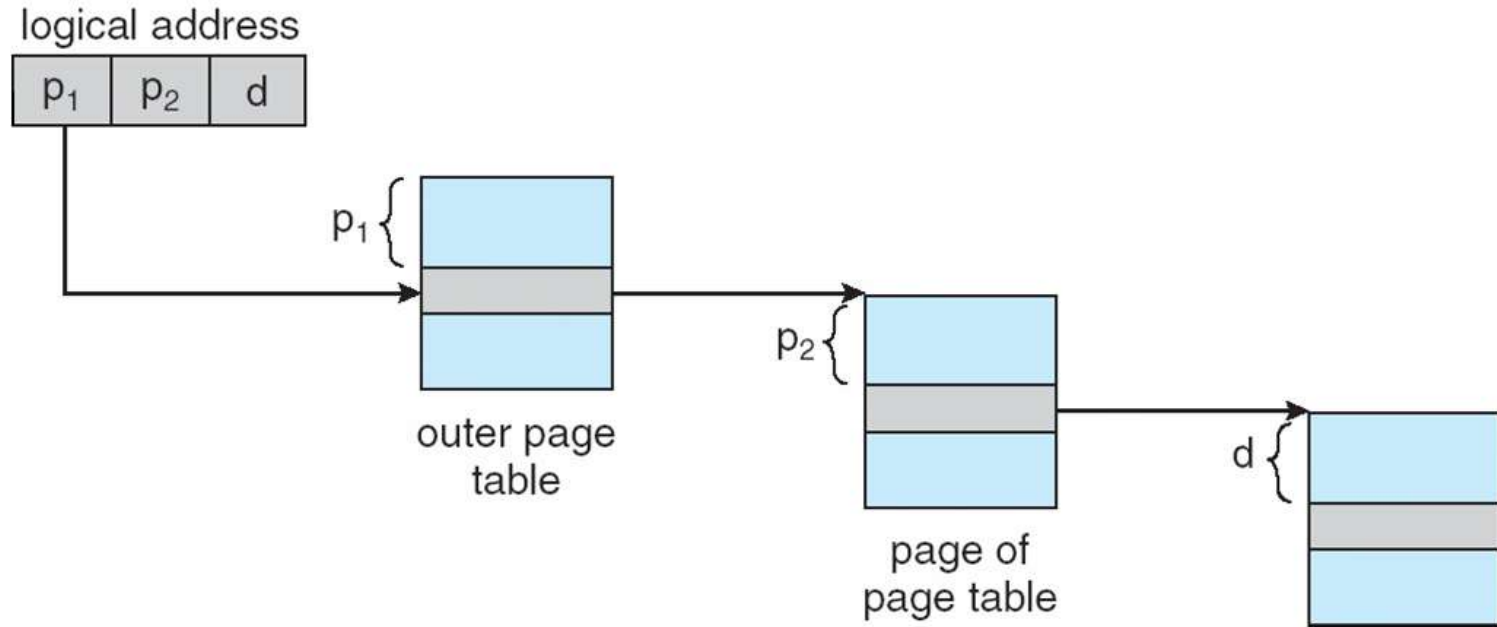
- A logical address (on 32-bit machine with 1K page size) is divided into:
  - a page number consisting of 22 bits
  - a page offset consisting of 10 bits
- Since the page table is paged, the page number is further divided into:
  - a 12-bit page number
  - a 10-bit page offset
- Thus, a logical address is as follows:

| page number |       | page offset |
|-------------|-------|-------------|
| $p_1$       | $p_2$ | $d$         |
| 12          | 10    | 10          |

where  $p_1$  is an index into the outer page table, and  $p_2$  is the displacement within the page of the outer page table



# Address-Translation Scheme





# Three-level Paging Scheme

| outer page | inner page | offset |
|------------|------------|--------|
| $p_1$      | $p_2$      | $d$    |
| 42         | 10         | 12     |

| 2nd outer page | outer page | inner page | offset |
|----------------|------------|------------|--------|
| $p_1$          | $p_2$      | $p_3$      | $d$    |
| 32             | 10         | 10         | 12     |



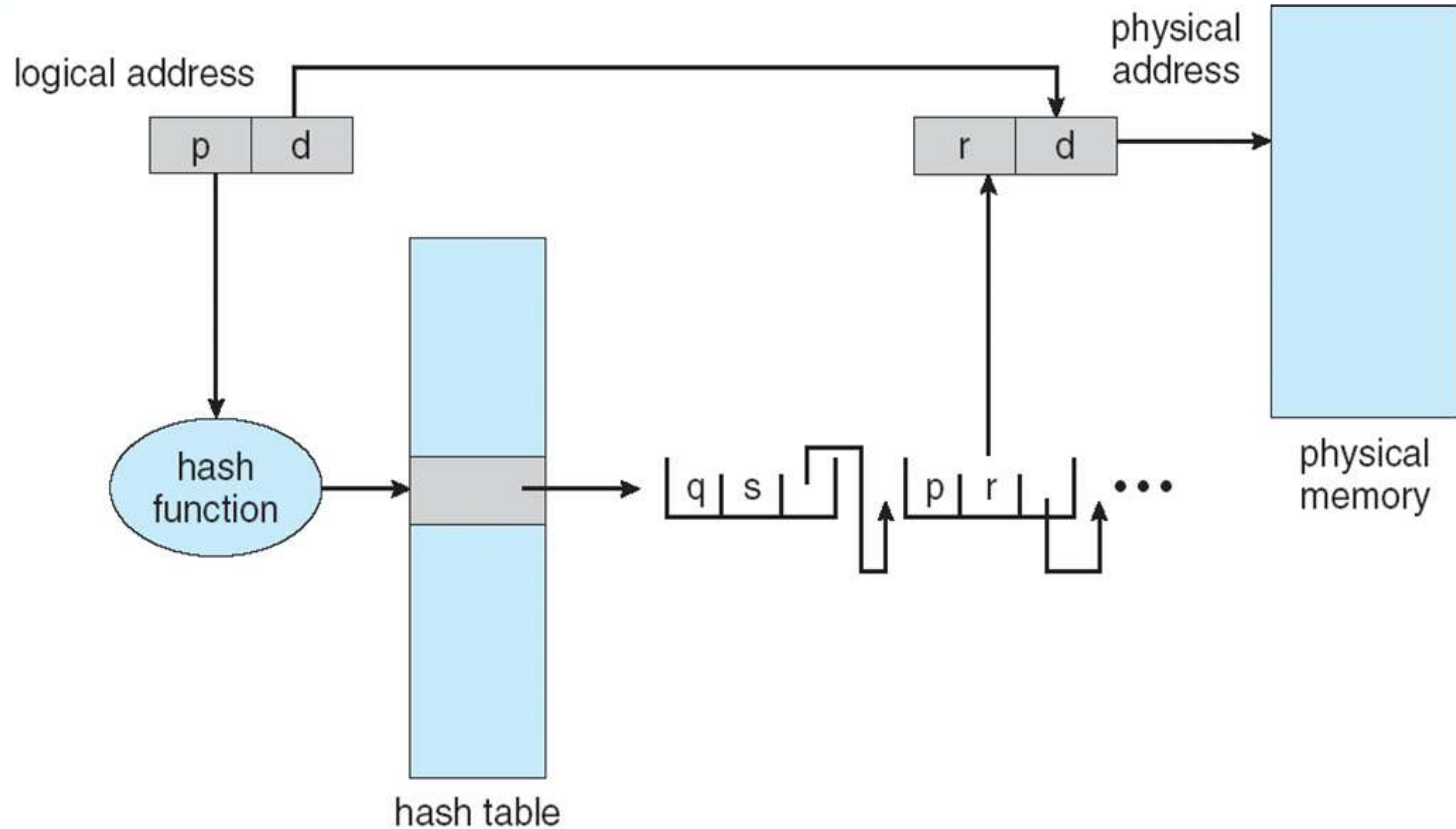
# Hashed Page Tables

- Common in address spaces  $> 32$  bits
- The virtual page number is hashed into a page table
  - This page table contains a chain of elements hashing to the same location
- Virtual page numbers are compared in this chain searching for a match
  - If a match is found, the corresponding physical frame is extracted





# Hashed Page Table



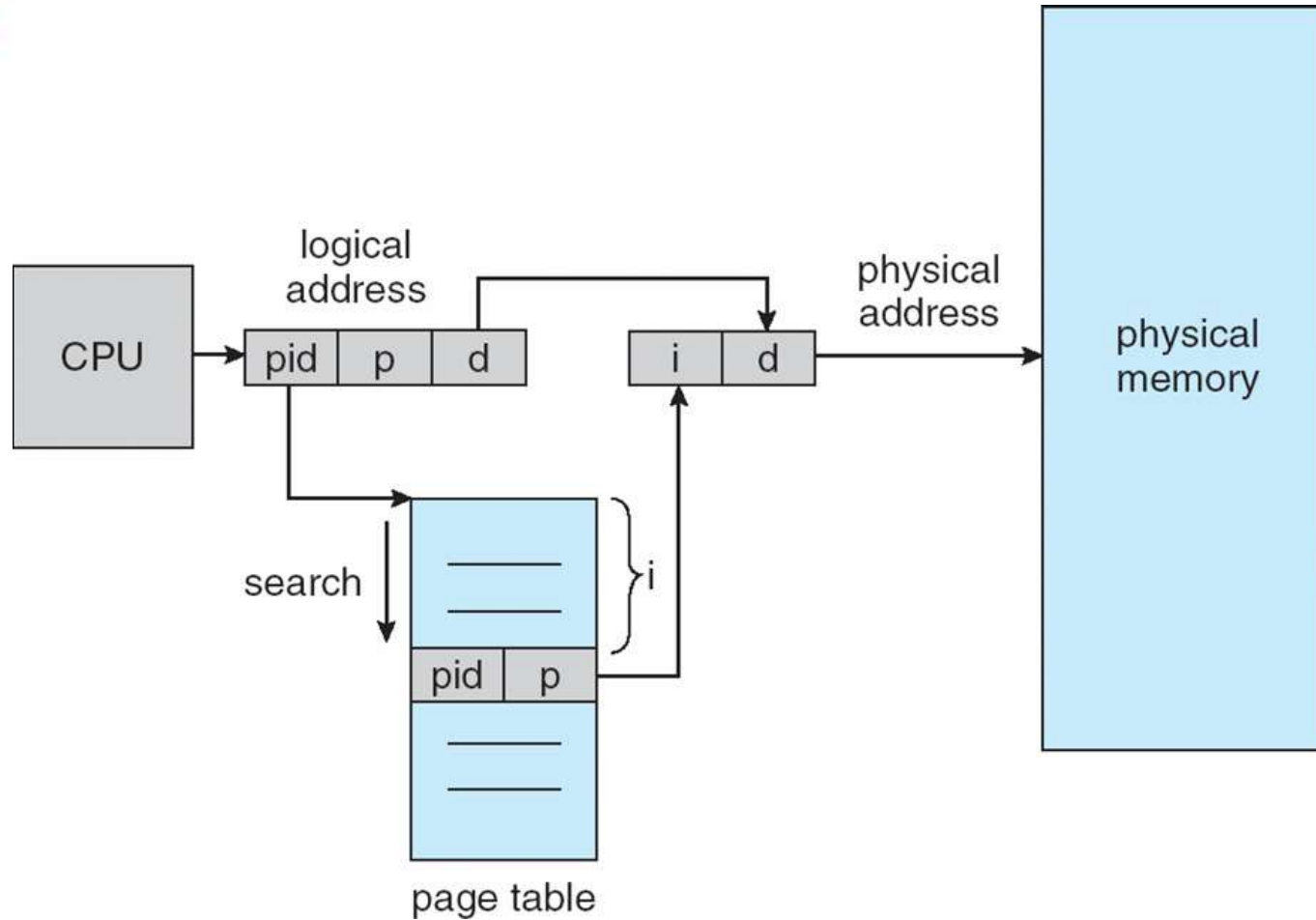


# Inverted Page Table

- One entry for each real page of memory
- Entry consists of the virtual address of the page stored in that real memory location, with information about the process that owns that page
- Decreases memory needed to store each page table, but increases time needed to search the table when a page reference occurs
- Use hash table to limit the search to one — or at most a few — page-table entries



# Inverted Page Table Architecture





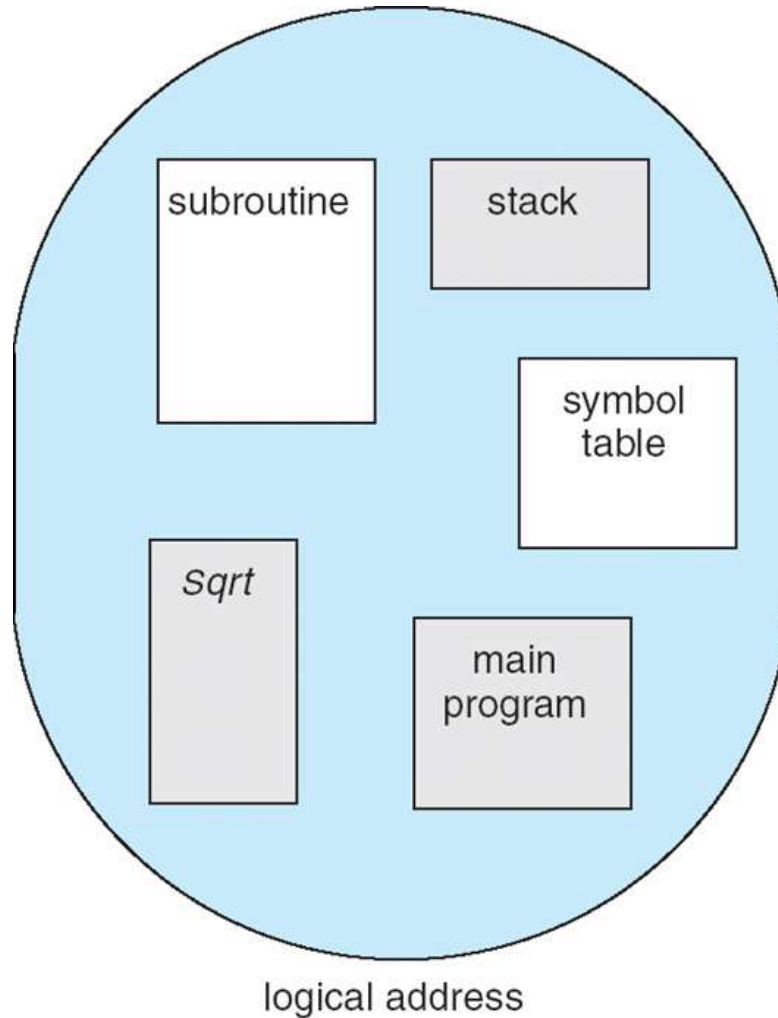
# Segmentation

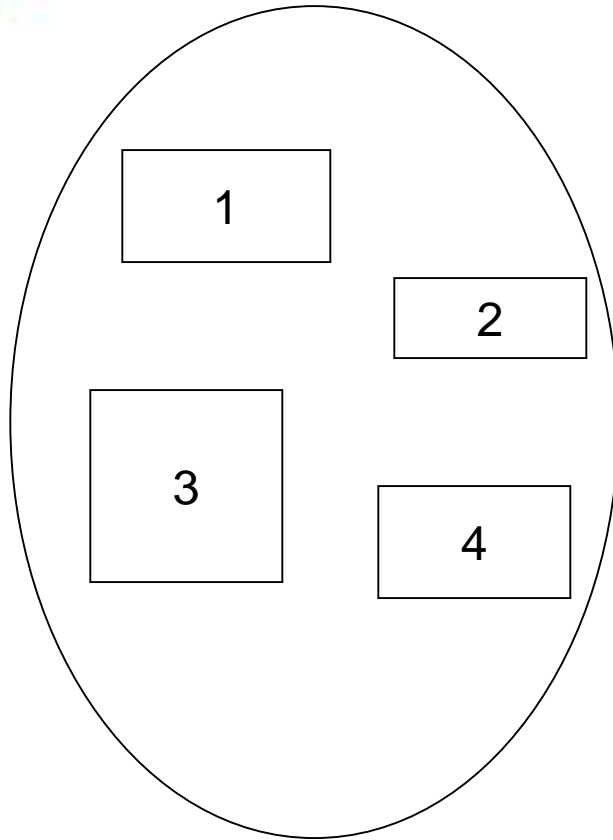
- Memory-management scheme that supports user view of memory
- A program is a collection of segments
  - A segment is a logical unit such as:
    - main program
    - procedure
    - function
    - method
    - object
    - local variables, global variables
    - common block
    - stack
    - symbol table
    - arrays



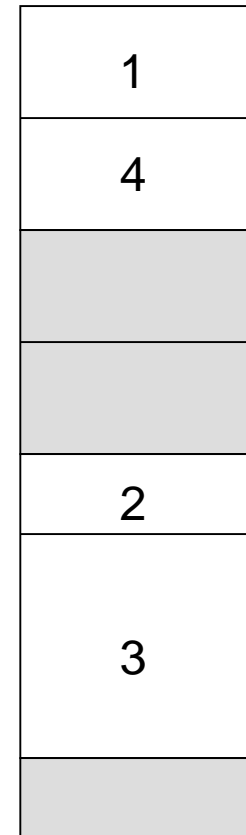
# User's View of a Program

*Go, change the world*





user space



physical memory space



- Logical address consists of a two tuple:  
    <segment-number, offset>,
- **Segment table** – maps two-dimensional physical addresses; each table entry has:
  - **base** – contains the starting physical address where the segments reside in memory
  - **limit** – specifies the length of the segment
- **Segment-table base register (STBR)** points to the segment table's location in memory
- **Segment-table length register (STLR)** indicates number of segments used by a program;  
    segment number **s** is legal if **s** < **STLR**



# Segmentation Architecture (Cont.)

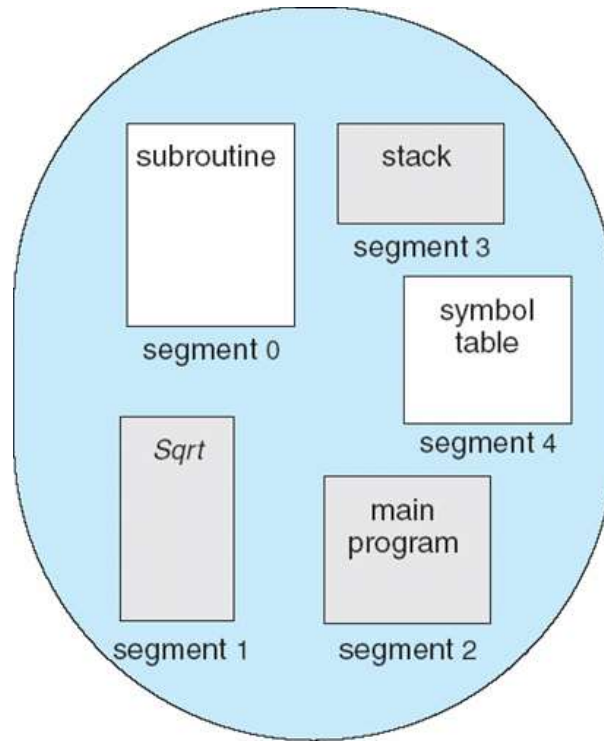
- Protection
  - With each entry in segment table associate:
    - 4 validation bit = 0  $\Rightarrow$  illegal segment
    - 4 read/write/execute privileges
- Protection bits associated with segments; code sharing occurs at segment level
- Since segments vary in length, memory allocation is a dynamic storage-allocation problem
- A segmentation example is shown in the following diagram





# Example of Segmentation

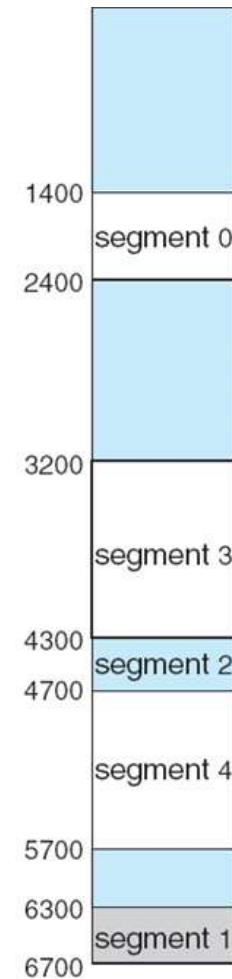
*Go, change the world*



logical address space

|   | limit | base |
|---|-------|------|
| 0 | 1000  | 1400 |
| 1 | 400   | 6300 |
| 2 | 400   | 4300 |
| 3 | 1100  | 3200 |
| 4 | 1000  | 4700 |

segment table



physical memory



# Virtual Memory Management



# Virtual Memory

- Background
- Demand Paging
- Copy-on-Write
- Page Replacement
- Allocation of Frames
- Thrashing



# Objectives

- To describe the benefits of a virtual memory system
- To explain the concepts of demand paging, page-replacement algorithms, and allocation of page frames
- To discuss the principle of the working-set model

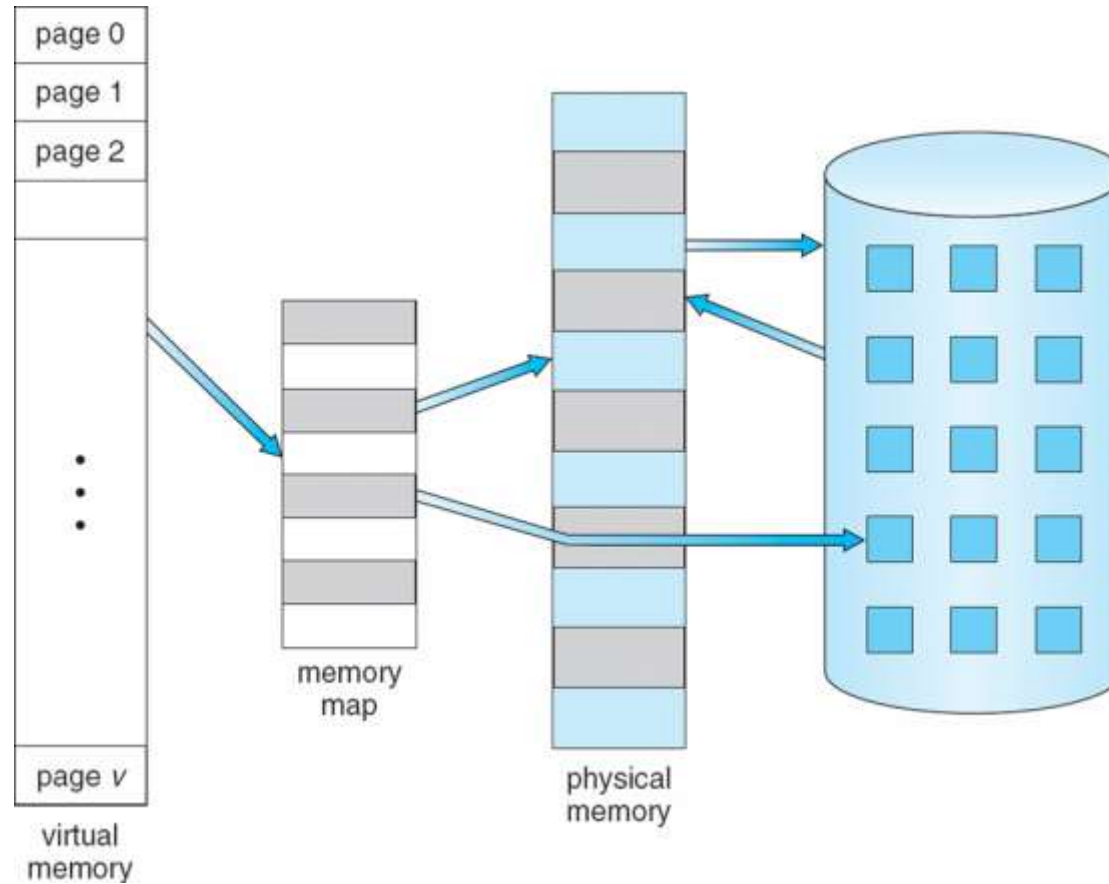


# Background

- **Virtual memory** – separation of user logical memory from physical memory.
  - Only part of the program needs to be in memory for execution
  - Logical address space can therefore be much larger than physical address space
  - Allows address spaces to be shared by several processes
  - Allows for more efficient process creation
- Virtual memory can be implemented via:
  - Demand paging
  - Demand segmentation

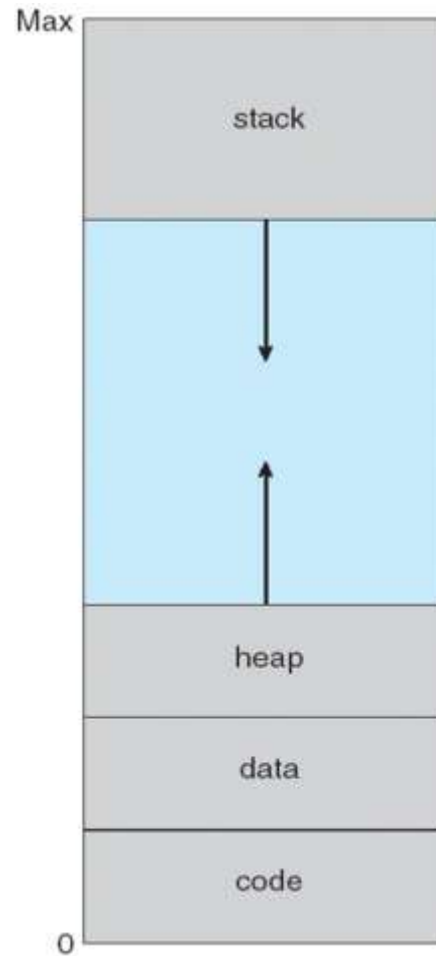


# Virtual Memory That is Larger Than Physical Memory



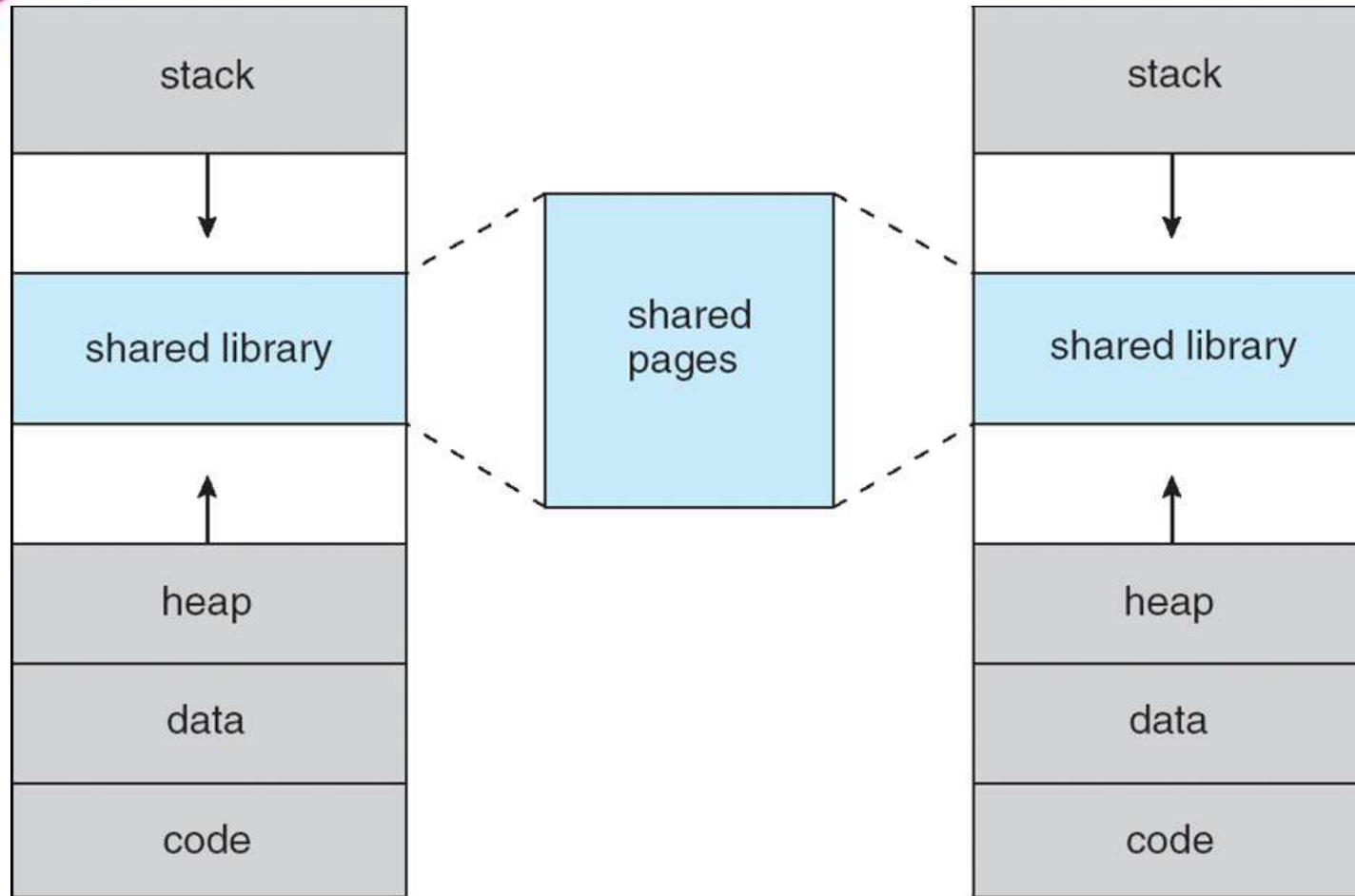


# Virtual-address Space





# Shared Library Using Virtual Memory





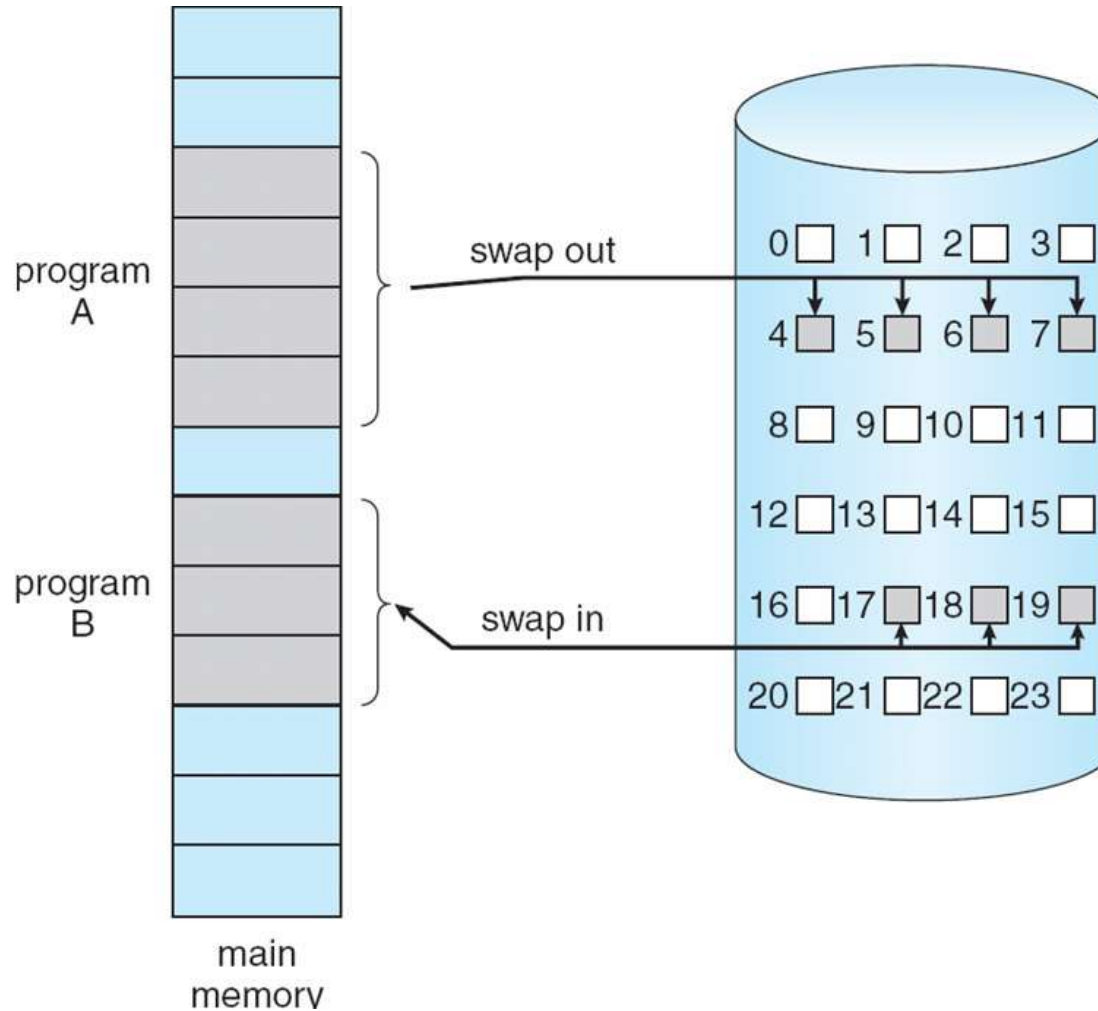


# Demand Paging

- Bring a page into memory only when it is needed
  - Less I/O needed
  - Less memory needed
  - Faster response
  - More users
- Page is needed  $\Rightarrow$  reference to it
  - invalid reference  $\Rightarrow$  abort
  - not-in-memory  $\Rightarrow$  bring to memory
- **Lazy swapper** – never swaps a page into memory unless page will be needed
  - Swapper that deals with pages is a **pager**



# Transfer of a Paged Memory to Contiguous Disk Space





# Valid-Invalid Bit

- With each page table entry a valid–invalid bit is associated (**v**  $\Rightarrow$  in-memory, **i**  $\Rightarrow$  not-in-memory)
- Initially valid–invalid bit is set to **i** on all entries
- Example of a page table snapshot:

| Frame # | valid-invalid bit |
|---------|-------------------|
|         | <b>v</b>          |
|         | <b>v</b>          |
|         | <b>v</b>          |
|         | <b>v</b>          |
|         | <b>i</b>          |
| ....    |                   |
|         | <b>i</b>          |
|         | <b>i</b>          |

page table

- During address translation, if valid–invalid bit in page table entry is **i**  $\Rightarrow$  page fault



# Page Table When Some Pages Are Not in Main Memory

|   |   |
|---|---|
| 0 | A |
| 1 | B |
| 2 | C |
| 3 | D |
| 4 | E |
| 5 | F |
| 6 | G |
| 7 | H |

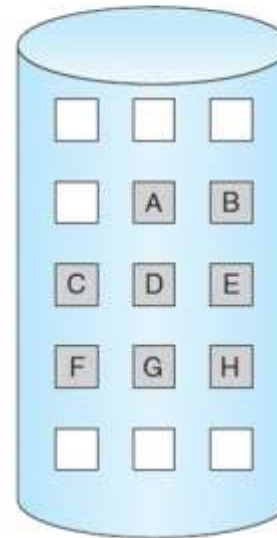
logical  
memory

| valid-invalid<br>bit |   |   |
|----------------------|---|---|
| frame                |   |   |
| 0                    | 4 | v |
| 1                    |   | i |
| 2                    | 6 | v |
| 3                    |   | i |
| 4                    |   | i |
| 5                    | 9 | v |
| 6                    |   | i |
| 7                    |   | i |

page table

|    |
|----|
| 0  |
| 1  |
| 2  |
| 3  |
| 4  |
| 5  |
| 6  |
| 7  |
| 8  |
| 9  |
| 10 |
| 11 |
| 12 |
| 13 |
| 14 |
| 15 |

physical memory





# Page Fault

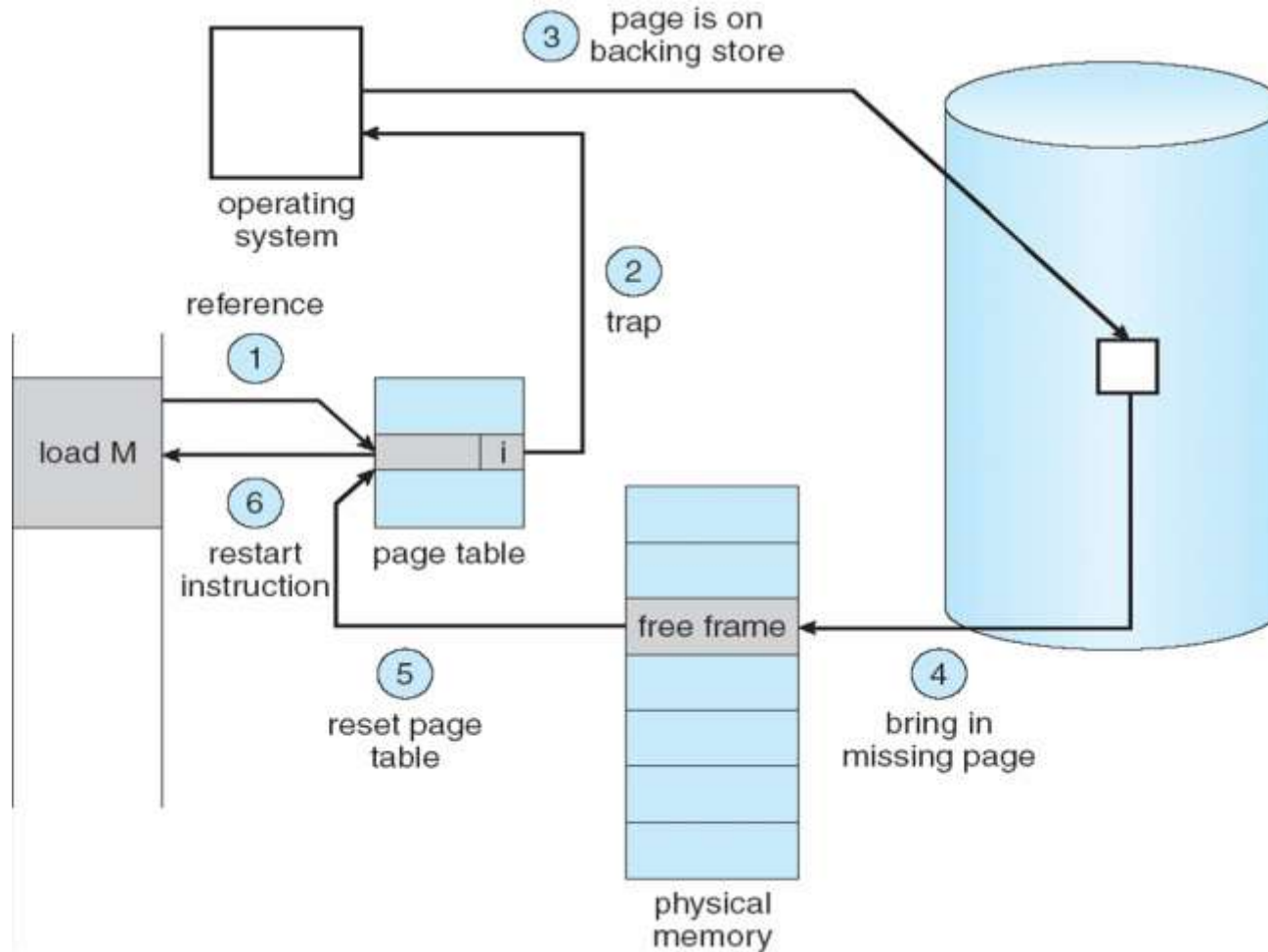
- If there is a reference to a page, first reference to that page will trap to operating system:

## page fault

1. Operating system looks at another table to decide:
  - Invalid reference  $\Rightarrow$  abort
  - Just not in memory
2. Get empty frame
3. Swap page into frame
4. Reset tables
5. Set validation bit = **v**
6. Restart the instruction that caused the page fault



# Steps in Handling a Page Fault





# Performance of Demand Paging

- Page Fault Rate  $0 \leq p \leq 1.0$ 
  - if  $p = 0$  no page faults
  - if  $p = 1$ , every reference is a fault

- Effective Access Time (EAT)

$$\begin{aligned} \text{EAT} = & (1 - p) \times \text{memory access} \\ & + p (\text{page fault overhead} \\ & \quad + \text{swap page out} \\ & \quad + \text{swap page in} \\ & \quad + \text{restart overhead} \\ & ) \end{aligned}$$



# Demand Paging Example

- Memory access time = 200 nanoseconds
- Average page-fault service time = 8 milliseconds
- Effective access time =  $p \times \text{time taken to access memory in page fault} + (1 - p) \times \text{time taken to access memory}$
- $$\begin{aligned} \text{EAT} &= (1 - p) \times 200 + p (8 \text{ milliseconds}) \\ &= (1 - p) \times 200 + p \times 8,000,000 \\ &= 200 + p \times 7,999,800 \end{aligned}$$
- If one access out of 1,000 causes a page fault, then  
EAT = 8.2 microseconds.  
This is a slowdown by a factor of 40!!





# Process Creation

- Virtual memory allows other benefits during process creation:
  - Copy-on-Write
  - Memory-Mapped Files (later)



# Copy-on-Write

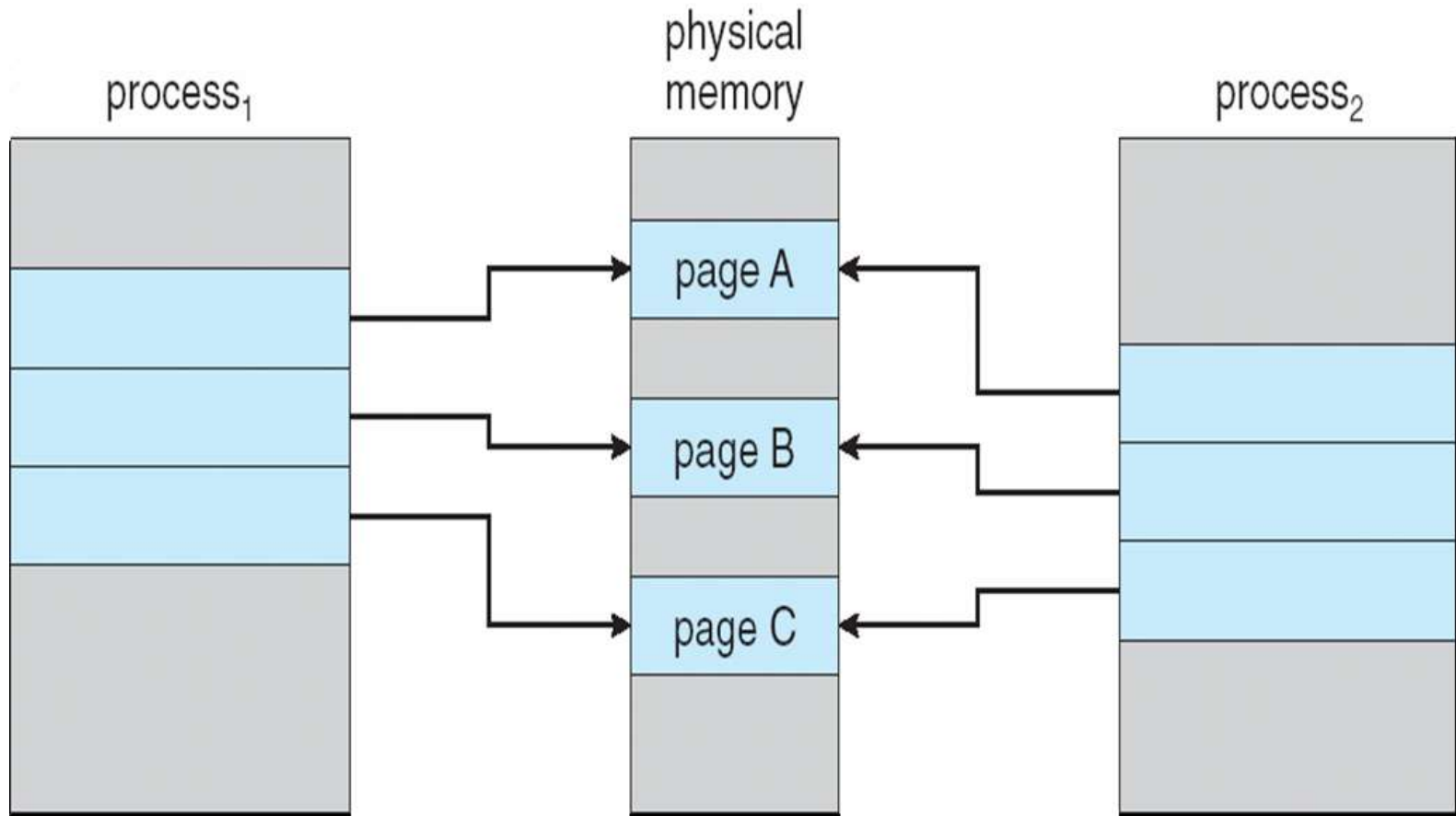
- Copy-on-Write (COW) allows both parent and child processes to initially *share* the same pages in memory

If either process modifies a shared page, only then is the page copied

- COW allows more efficient process creation as only modified pages are copied
- Free pages are allocated from a **pool** of zeroed-out pages

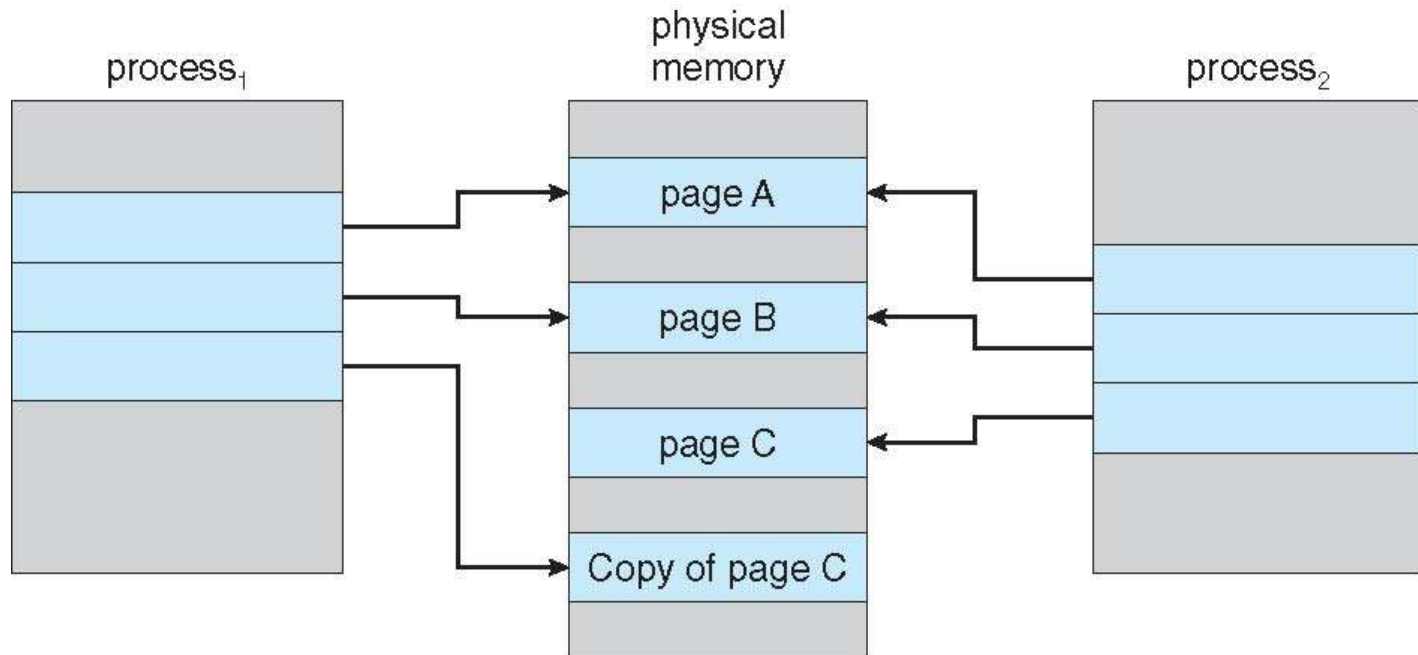


# Before Process 1 Modifies Page C





# After Process 1 Modifies Page C





# What happens if there is no free frame?

- Page replacement – find some page in memory, but not really in use, swap it out
  - algorithm
  - performance – want an algorithm which will result in minimum number of page faults
- Same page may be brought into memory several times

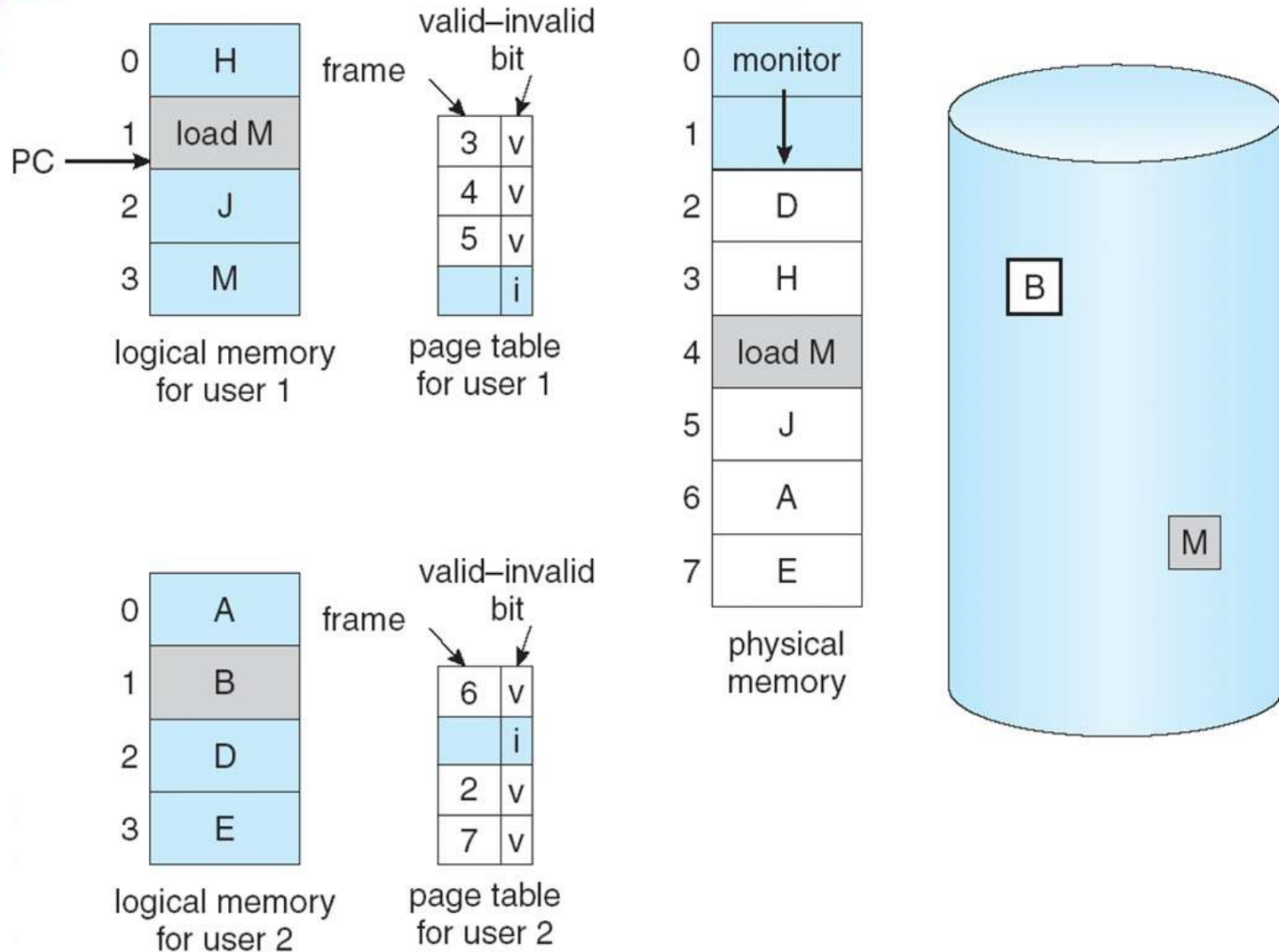


# Page Replacement

- Prevent over-allocation of memory by modifying page-fault service routine to include page replacement
- Use **modify (dirty) bit** to reduce overhead of page transfers – only modified pages are written to disk
- Page replacement completes separation between logical memory and physical memory – large virtual memory can be provided on a smaller physical memory



# Need For Page Replacement





# Basic Page Replacement

1. Find the location of the desired page on disk
2. Find a free frame:
  - If there is a free frame, use it
  - If there is no free frame, use a page replacement algorithm to select a **victim** frame
3. Bring the desired page into the (newly) free frame; update the page and frame tables
4. Restart the process





# Page Replacement

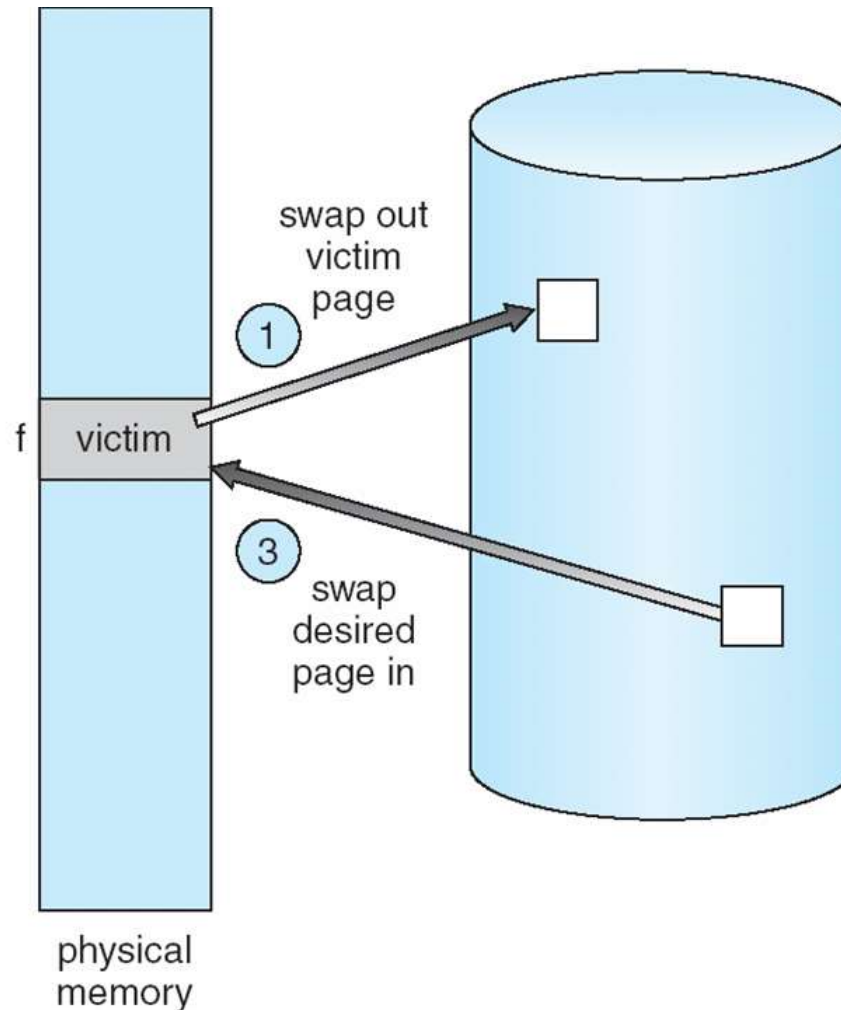
frame      valid-invalid bit

|   |   |
|---|---|
|   |   |
| 0 | i |
| f | v |
|   |   |
|   |   |

page table

② change  
to invalid

④  
reset page  
table for  
new page





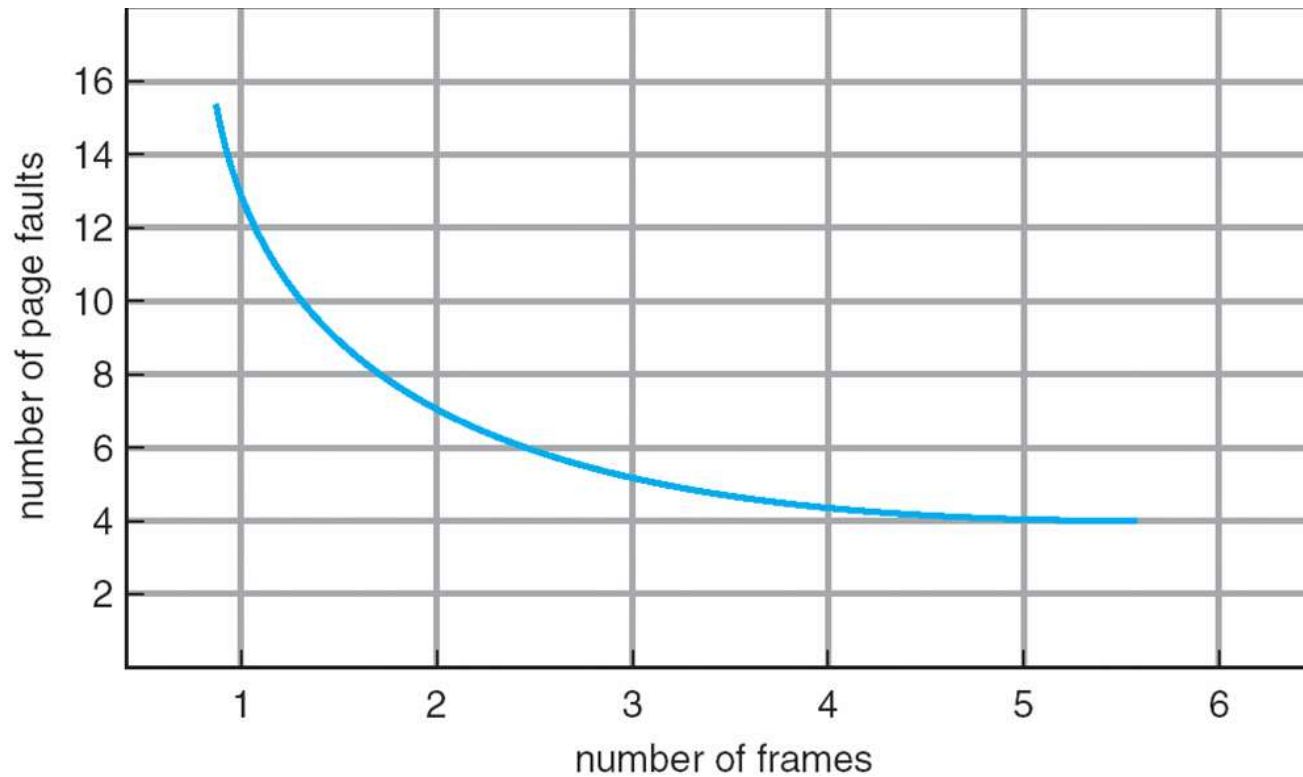
# Page Replacement Algorithms

- Want lowest page-fault rate
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
- In all our examples, the reference string is

**1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5**



# Graph of Page Faults Versus The Number of Frames





# First-In-First-Out (FIFO) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- 3 frames (3 pages can be in memory at a time per process)

|   |   |   |   |               |
|---|---|---|---|---------------|
| 1 | 1 | 4 | 5 |               |
| 2 | 2 | 1 | 3 | 9 page faults |
| 3 | 3 | 2 | 4 |               |

- 4 frames

|   |   |   |   |                |
|---|---|---|---|----------------|
| 1 | 1 | 5 | 4 |                |
| 2 | 2 | 1 | 5 | 10 page faults |
| 3 | 3 | 2 |   |                |
| 4 | 4 | 3 |   |                |

- Belady's Anomaly: more frames  $\Rightarrow$  more page faults



# FIFO Page Replacement

reference string

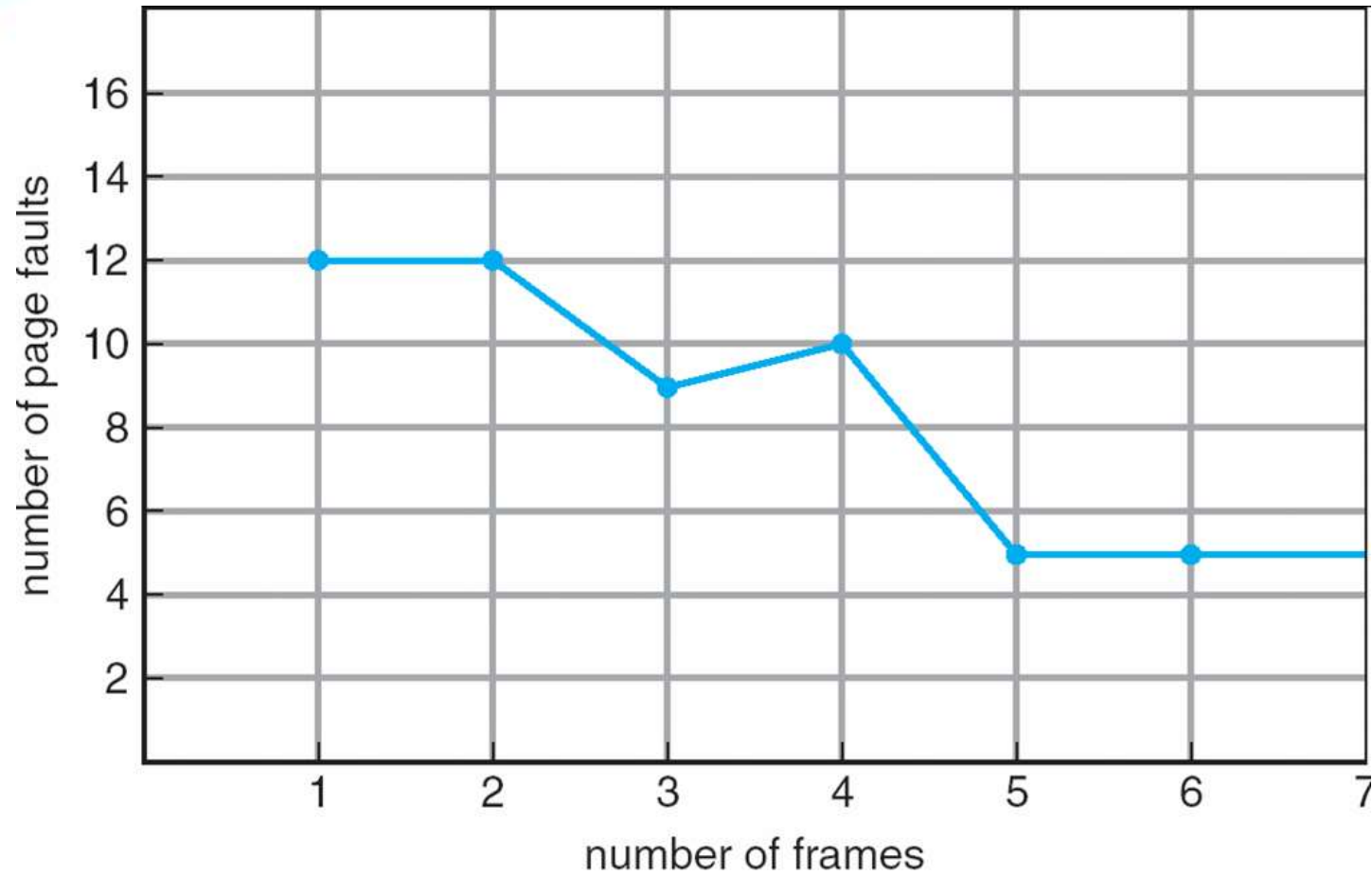
7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

|   |   |   |   |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|---|---|---|---|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|
| 7 | 7 | 7 | 2 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|   | 0 | 0 | 0 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|   |   | 1 | 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|   |   |   |   |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

page frames



# FIFO Illustrating Belady's Anomaly





# Optimal Algorithm

- Replace page that will not be used for longest period of time
- 4 frames example

1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

|   |
|---|
| 1 |
| 2 |
| 3 |
| 4 |

4

6 page faults

5

- How do you know this?
- Used for measuring how well your algorithm performs



reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

|   |   |   |   |  |   |  |   |  |  |   |  |  |  |  |  |  |   |  |  |
|---|---|---|---|--|---|--|---|--|--|---|--|--|--|--|--|--|---|--|--|
| 7 | 7 | 7 | 2 |  | 2 |  | 2 |  |  | 2 |  |  |  |  |  |  | 7 |  |  |
|   | 0 | 0 | 0 |  | 0 |  | 0 |  |  | 0 |  |  |  |  |  |  | 0 |  |  |
|   |   | 1 | 1 |  | 3 |  | 3 |  |  | 3 |  |  |  |  |  |  | 1 |  |  |

page frames





# Least Recently Used (LRU) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, **5**, 1, 2, **3**, **4**, **5**

|   |          |          |          |          |
|---|----------|----------|----------|----------|
| 1 | 1        | 1        | 1        | <b>5</b> |
| 2 | 2        | 2        | 2        | 2        |
| 3 | <b>5</b> | 5        | <b>4</b> | 4        |
| 4 | 4        | <b>3</b> | 3        | 3        |

- Counter implementation
  - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
  - When a page needs to be changed, look at the counters to determine which are to change



# LRU Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

|   |   |   |   |  |   |  |   |   |   |   |  |  |   |  |   |  |   |  |
|---|---|---|---|--|---|--|---|---|---|---|--|--|---|--|---|--|---|--|
| 7 | 7 | 7 | 2 |  | 2 |  | 4 | 4 | 4 | 0 |  |  | 1 |  | 1 |  | 1 |  |
|   | 0 | 0 | 0 |  | 0 |  | 0 | 0 | 3 | 3 |  |  | 3 |  | 0 |  | 0 |  |
|   |   | 1 | 1 |  | 3 |  | 3 | 2 | 2 | 2 |  |  | 2 |  | 2 |  | 7 |  |

page frames



# LRU Algorithm (Cont.)

- Stack implementation – keep a stack of page numbers in a double link form:
  - Page referenced:
    - ▶ move it to the top
    - ▶ requires 6 pointers to be changed
  - No search for replacement



## Use Of A Stack to Record The Most Recent Page References

reference string

4 7 0 7 1 0 1 2 1 2 7 1 2

|   |
|---|
| 2 |
| 1 |
| 0 |
| 7 |
| 4 |

stack  
before  
a

|   |
|---|
| 7 |
| 2 |
| 1 |
| 0 |
| 4 |

stack  
after  
b

↑  
a

↑  
b



# LRU Approximation Algorithms

## ■ Reference bit

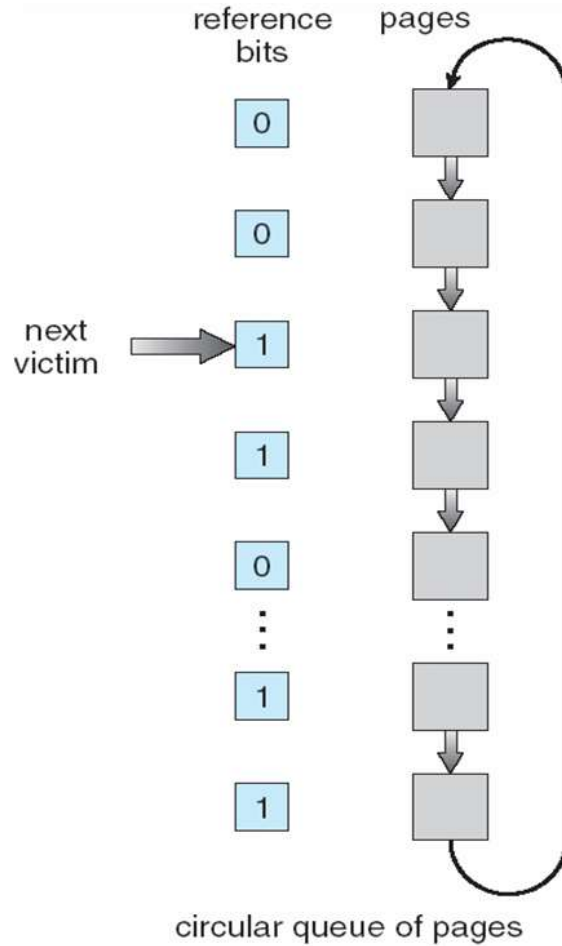
- With each page associate a bit, initially = 0
- When page is referenced bit set to 1
- Replace the one which is 0 (if one exists)
  - ▶ We do not know the order, however

## ■ Second chance

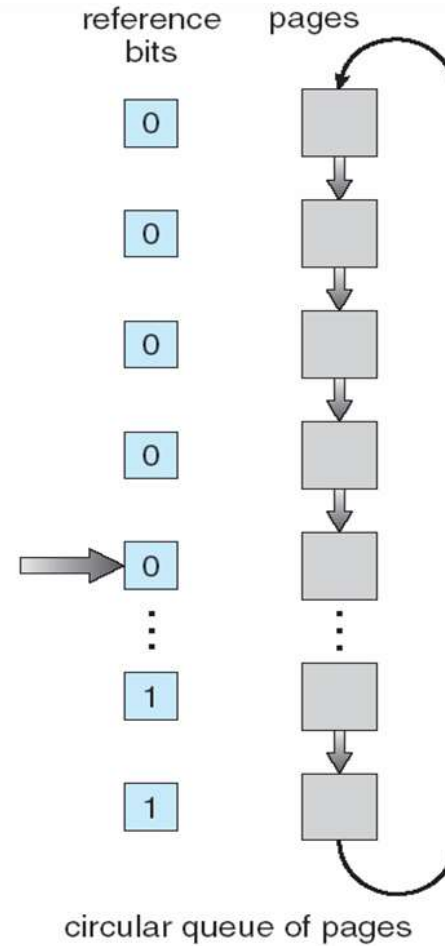
- Need reference bit
- Clock replacement
- If page to be replaced (in clock order) has reference bit = 1 then:
  - ▶ set reference bit 0
  - ▶ leave page in memory
  - ▶ replace next page (in clock order), subject to same rules



# Second-Chance (clock) Page-Replacement Algorithm



(a)



(b)



# Counting Algorithms

- Keep a counter of the number of references that have been made to each page
- **LFU Algorithm**: replaces page with smallest count
- **MFU Algorithm**: based on the argument that the page with the smallest count was probably just brought in and has yet to be used



# Allocation of Frames

- Each process needs *minimum* number of pages
- Example: IBM 370 – 6 pages to handle SS MOVE instruction:
  - instruction is 6 bytes, might span 2 pages
  - 2 pages to handle *from*
  - 2 pages to handle *to*
- Two major allocation schemes
  - fixed allocation
  - priority allocation





# Fixed Allocation

- Equal allocation – For example, if there are 100 frames and 5 processes, give each process 20 frames.
- Proportional allocation – Allocate according to the size of process
  - $s_i$  = size of process  $p_i$
  - $S = \sum s_i$
  - $m$  = total number of frames
  - $a_i$  = allocation for  $p_i = \frac{s_i}{S} \times m$

$$m = 64$$

$$s_i = 10$$

$$s_2 = 127$$

$$a_1 = \frac{10}{137} \times 64 \approx 5$$

$$a_2 = \frac{127}{137} \times 64 \approx 59$$



# Priority Allocation

- Use a proportional allocation scheme using priorities rather than size
- If process  $P_i$  generates a page fault,
  - select for replacement one of its frames
  - select for replacement a frame from a process with lower priority number



- **Global replacement** – process selects a replacement frame from the set of all frames; one process can take a frame from another
- **Local replacement** – each process selects from only its own set of allocated frames



# Thrashing

- If a process does not have “enough” pages, the page-fault rate is very high. This leads to:
  - low CPU utilization
  - operating system thinks that it needs to increase the degree of multiprogramming
  - another process added to the system
  
- **Thrashing**  $\equiv$  a process is busy swapping pages in and out



# Thrashing (Cont.)

