## Model fidelity and its impact on power grid resource planning under high renewable penetration

by

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### Contents

List of Tables								$\mathbf{v}$		
List of Figures								vii		
Abstract							1			
1	Introduction							3		
2	2 Literature Review						5			
3	Development							7		
	3.1	Data						7		
	3.2	Mode	els					7		
		3.2.1	Indices and Sets					7		
		3.2.2	Parameters					8		
		3.2.3	Variables					8		
		3.2.4	Economic Dispatch Models					8		
	3.3	Imple	ementation					10		
4 Analysis								11		
5	5 Conclusion							13		
<b>.</b> 7:	Vita							15		



### List of Tables

# List of Figures

### Introduction

Literature Review

### Development

### 3.1 Data

### 3.2 Models

This thesis covers the Economic Dispatch and Unit Commitment models, developed exhaustively in the literature.

#### 3.2.1 Indices and Sets

```
g \in \mathcal{G}
               Set of generators
b \in \mathcal{B}
               Set of buses
g \in \mathcal{G}^{NR}
               Subset of non-renewable generators
g \in \mathcal{G}^R
               Subset of renewable generators
qt \in \mathcal{GT}
               Set of generator types
u \in \mathcal{U}
               Set of unit groups
l \in \mathcal{L}
               Set of transmission lines
rr \in \mathcal{RR}
               Set of reserve requirements
rp \in \mathcal{RP}
               Set of reserve products
t \in \mathcal{T}
               Set of time periods
g \in \mathcal{G}^{\lfloor}
               Set of generators in each bus b
```

#### 3.2.2 Parameters

- $D_{b,t}$ Load at bus b in time t $C_g$ Generation cost for generator g (\$ / MW) t $S_q$ Start-up cost for generator g  $R_a^{up}$ Ramp up limit for generator g Ramp down limit for generator g  $G_g^{max}$ Maximum generation capacity for generator g  $G_g^{min}$ Minimum generation capacity for generator g  $T_l^{min}$ Minimum transmission of transmission line l  $T_l^{max}$ Maximum transmission of transmission line l  $P_{g,t}^R$ Power generation of renewable generator g in time t
- Note 1: The generation of renewable resources are not in the decision variables. The developed models only decides the generation for non-renewable resources. Therefore the generation is considered a deterministic parameter, not a variable in the model.

#### 3.2.3 Variables

 $P_{g,t}^{NR}$  Power generation of non-renewable generator g in time t (MW)  $T_{i,j,t}$  Power transmitted from bus i to bus j in time t (MW)  $T_{i,j,t}^{loss}$  Power loss in transmission from bus i to bus j in time t (MW)  $S_{g,t}$  On/off status of generator g at time n  $S_{g,t}^{on}$  Start-up status of generator g at time n  $S_{g,t}^{off}$  Shut-down status of generator g at time n  $V_{b,t}^{-}$  Under generation slack variable at each bus b in time t  $V_{b,t}^{+}$  Over generation slack variable at each bus b in time t

### 3.2.4 Economic Dispatch Models

The economic dispatch model satisfies the load and transmission requirements at a minimum cost, following operational requirements such as generation, transmission and ramp limits. In this model, we assume that the commitment decisions has been already made.

#### Simple Economic Dispatch Model

$$min \sum_{t \in T} \sum_{g \in G^{NR}} P_{g,t}^{NR} C_g + \sum_{t \in T} \sum_{b \in B} V_{b,t}^- + \sum_{t \in T} \sum_{b \in B} V_{b,t}^+$$
(3.1a)

$$s.t. \quad \sum_{t \in T} P_{g,t}^{NR} + \sum_{t \in T} P_{g,t}^{R} + \sum_{t \in T} V_{b,t}^{-} = \sum_{t \in T} D_{b,t} + \sum_{t \in T} V_{b,t}^{+} \ \forall t \in T$$

$$(3.1b)$$

$$P_{q,t}^{NR} - P_{q,t-1}^{NR} \le R_q^{up} \qquad \forall t \in T, g \in \mathcal{G}^R \qquad (3.1c)$$

$$P_{g,t-1}^{NR} - P_{g,t}^{NR} \le R_g^{down} \qquad \forall t \in T, g \in \mathcal{G}^R \qquad (3.1d)$$

$$G_q^{min} \le P_{q,t}^{NR} \le G_q^{max}$$
  $\forall t \in T, g \in \mathcal{G}^R$  (3.1e)

The constraint 3.1b states the energy balance in every time. The constraints 3.1d and 3.1c states that every generator has to obey the ramp limits. The constraint 3.1e states the generation limits for each generator. The use of slack variables  $V_{b,t}^-$  and  $V_{b,t}^+$  is necessary to always have feasible solutions, and it is important for scenarios where there is a huge renewable penetrations, when there's an abrupt variation of generation and there is a over or under generation.

#### **Economic Dispatch with Transmission Constraints**

In this case, the model has to consider transmission limits and losses, without transmission costs associated. The objective function 3.1a remains the same, and the constraints 3.1c, 3.1d and 3.1e are alsused. The constraint 3.1b is replaced by

$$\sum_{g \in G^b} P_{g,t}^{NR} + \sum_{g \in G^b} P_{g,t}^{R} + \sum_{b^{in} \in B} T_{b^{in},b,t} + V_{b,t}^{-} = D_{b,t} + V_{b,t}^{+} + \sum_{b^{out} \in B} T_{b,b^{out},t} \ \forall b \in B, t \in t$$
(3.2a)

$$T_l^{min} \le T_{b^{in}, b^{out}, t} \le T_l^{max}$$
  $\forall b \in B, t \in t$  (3.2b)

Constraint 3.2a guarantees that the energy balance is always satisfied for every bus: everything that is generated and received from other buses should be equal to what is loaded and sent throughout the line with the respective losses. If this balance is not satisfied then it is represented in the slack variables. (TODO: put lossed in the equation). The constraint 3.2b defines the transmission bounds for each line.

#### Economic dispatch model with unit commitment constraints

This optimization model is a mixed-integer linear program (MILP). This model includes decision variables to capture "on" and "off" decisions for thermal generators in each time period. The objective function must be modifies to account for start up and shut down costs with thermal generators.

### 3.3 Implementation

Here write about how it was implemented, in AIMMS, put some running times in a table, some images, put a brief description about what is AIMMS and why it is used, and etc.

## Analysis

In the analysis make all the scenario runs, describe the data.

Conclusion

# Bibliography