

Model fidelity and its impact on power grid  
resource planning under high renewable  
penetration

by

Daniel Xavier Wolbert

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Daniel Xavier Wolbert

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**Tamas Terlaky**, Thesis Director, Chair  
(Must Sign with Blue Ink)

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**Accepted Date**

Committee Members

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**Robert H. Storer**



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# Chapter 1

## Introduction

Variable Energy Resources (usually refereed as VERs) plays an important role in the energy grid nowadays. It is expected that in 2020, x% of all average consumed power in United States comes from them. One of important characteristics of them is the unpredictable behaviour for demand. With the deregulation of the energy market and the decarbonization rules, the grid operators have the challenge to plan efficiently their non-renewable resources (such as oil, coal and gas) in order to keep the grid in security and operational parameters while running the grid at a minimal cost. This work analyses the classical LP version of Economic Dispatch (known as ED) and a MIP instance of Unit Commitment(UC) under different operational constraints and VERs penetration scenarios.



# Chapter 2

## Literature Review

The first optimal power flow formulation was proposed by [put the guy here in 1962];

Connolly et al. reviews 68 tools to power grid planning with renewable resources, discussing at the end goals, limitations and features of 37 tools [3]. The authors emphasize that, although all the tools are essential to an accurate power planning with renewable resources, there is no perfect tool, and it should be chosen accordingly to project goals, data limitations, horizon and other features. Yamin discusses different techniques to solve the unit commitment and economic dispatch problems, categorizing them in deterministic, heuristic or stochastic, pointing out the computational challenges and the quality of results for each one of them [18]. Padhy formulates the unit commitment as a general optimization problem and presents a bibliographical survey of the main techniques in the last 30 years, from exhaustive methods such as priority listing, dynamic programming, mixed integer-programming until complex heuristics like fuzzy programming, genetic algorithms and evolutionary programming, emphasizing that these one were not exhaustively tested yet.

Models can be classified according to different features, that include:

1. Time frame: decade, year, hour, sub hour
2. Scale: global, national, regional, local
3. Deterministic vs stochastic

#### 4. Optimization vs Simulation

#### 5. Algorithmic vs Heuristic

Cain et al. categorizes the general power flow according to 3 major categories: Power Flow (PF), Economic Dispatch (ED) and Optimal Power Flow (OPF) and describe them based on the assumptions and operational constraints, as shown in table 2.1 [2].

In Kassakian et al. report, the authors points new trends and challenges for electric grid management. It discusses the impact of VER's

Under a scenario where renewable resources have a considerable penetration in the power system, it is necessary to study their impact. Deane et al. studies the impact of UC and ED results at different solving temporal resolutions under one year, on a scenario of high wind penetration [4]. The author discusses that sub-hourly resolutions can deal more accurately with non-thermal inflexibilities, renewable demand variabilities and ramping behaviours than one-hour resolution. This difference is evaluated again in this thesis.

This project covers the LP Economic Dispatch problem and the MIP Unit Commitment.

**Table 2.1:** Optimal power flow categories [2]

Category	Name	Constraints					Costs
		Voltage		Transmission	Contingency	Losses	Generator
		Angle	Magnitude				
OPF	ACOPF	x	x	x		x	x
OPF	DCOPF			x	x	x	x
OPF	DOPF	x	x	x		x	
OPF	SCED	x		x	x	x	x
OPF	SCOPF	x	x	x	x	x	x
PF	PF		x			x	x
ED	ED					x	x

More details of AC and DC power flows are presented in appendix

# Chapter 3

## Development

### 3.1 Data

### 3.2 Models

This thesis covers the Economic Dispatch and Unit Commitment models, developed exhaustively in the literature.

#### 3.2.1 Indices and Sets

$g \in \mathcal{G}$	Set of generators
$b \in \mathcal{B}$	Set of buses
$g \in \mathcal{G}^{NR}$	Subset of non-renewable generators
$g \in \mathcal{G}^R$	Subset of renewable generators
$gt \in \mathcal{GT}$	Set of generator types
$u \in \mathcal{U}$	Set of unit groups
$l \in \mathcal{L}$	Set of transmission lines
$rr \in \mathcal{RR}$	Set of reserve requirements
$rp \in \mathcal{RP}$	Set of reserve products
$t \in \mathcal{T}$	Set of time periods
$g \in \mathcal{G}^l$	Set of generators in each bus $b$

### 3.2.2 Parameters

$D_{b,t}$	Load at bus $b$ in time $t$
$C_g$	Generation cost for generator $g$ (\$ / MW) $t$
$S_g$	Start-up cost for generator $g$
$R_g^{up}$	Ramp up limit for generator $g$
$R_g^{down}$	Ramp down limit for generator $g$
$G_g^{max}$	Maximum generation capacity for generator $g$
$G_g^{min}$	Minimum generation capacity for generator $g$
$T_l^{min}$	Minimum transmission of transmission line $l$
$T_l^{max}$	Maximum transmission of transmission line $l$
$P_{g,t}^R$	Power generation of renewable generator $g$ in time $t$

Note 1: The generation of renewable resources are not in the decision variables. The developed models only decides the generation for non-renewable resources. Therefore the generation is considered a deterministic parameter, not a variable in the model.

### 3.2.3 Variables

$P_{g,t}^{NR}$	Power generation of non-renewable generator $g$ in time $t$ (MW)
$T_{i,j,t}$	Power transmitted from bus $i$ to bus $j$ in time $t$ (MW)
$T_{i,j,t}^{loss}$	Power loss in transmission from bus $i$ to bus $j$ in time $t$ (MW)
$S_{g,t}$	On/off status of generator $g$ at time $n$
$S_{g,t}^{on}$	Start-up status of generator $g$ at time $n$
$S_{g,t}^{off}$	Shut-down status of generator $g$ at time $n$
$V_{b,t}^-$	Under generation slack variable at each bus $b$ in time $t$
$V_{b,t}^+$	Over generation slack variable at each bus $b$ in time $t$

### 3.2.4 Economic Dispatch Models

The economic dispatch model satisfies the load and transmission requirements at a minimum cost, following operational requirements such as generation, transmission and ramp limits. In this model, we assume that the commitment decisions has been

already made.

### Simple Economic Dispatch Model

$$\min \sum_{t \in T} \sum_{g \in G^{NR}} P_{g,t}^{NR} C_g + \sum_{t \in T} \sum_{b \in B} V_{b,t}^- + \sum_{t \in T} \sum_{b \in B} V_{b,t}^+ \quad (3.1a)$$

$$s.t. \quad \sum_{t \in T} P_{g,t}^{NR} + \sum_{t \in T} P_{g,t}^R + \sum_{t \in T} V_{b,t}^- = \sum_{t \in T} D_{b,t} + \sum_{t \in T} V_{b,t}^+ \quad \forall t \in T \quad (3.1b)$$

$$P_{g,t}^{NR} - P_{g,t-1}^{NR} \leq R_g^{up} \quad \forall t \in T, g \in \mathcal{G}^R \quad (3.1c)$$

$$P_{g,t-1}^{NR} - P_{g,t}^{NR} \leq R_g^{down} \quad \forall t \in T, g \in \mathcal{G}^R \quad (3.1d)$$

$$G_g^{min} \leq P_{g,t}^{NR} \leq G_g^{max} \quad \forall t \in T, g \in \mathcal{G}^R \quad (3.1e)$$

The constraint 3.1b states the energy balance in every time. The constraints 3.1d and 3.1c states that every generator has to obey the ramp limits. The constraint 3.1e states the generation limits for each generator. The use of slack variables  $V_{b,t}^-$  and  $V_{b,t}^+$  is necessary to always have feasible solutions, and it is important for scenarios where there is a huge renewable penetrations, when there's an abrupt variation of generation and there is a over or under generation.

### Economic Dispatch with Transmission Constraints

In this case, the model has to consider transmission limits and losses, without transmission costs associated. The objective function 3.1a remains the same, and the constraints 3.1c, 3.1d and 3.1e are also used. The constraint 3.1b is replaced by

$$\sum_{g \in G^b} P_{g,t}^{NR} + \sum_{g \in G^b} P_{g,t}^R + \sum_{b^{in} \in B} T_{b^{in},b,t} + V_{b,t}^- = D_{b,t} + V_{b,t}^+ + \sum_{b^{out} \in B} T_{b,b^{out},t} \quad \forall b \in B, t \in T \quad (3.2a)$$

$$T_l^{min} \leq T_{b^{in},b^{out},t} \leq T_l^{max} \quad \forall b \in B, t \in T \quad (3.2b)$$

Constraint 3.2a guarantees that the energy balance is always satisfied for every bus: everything that is generated and received from other buses should be equal



to what is loaded and sent throughout the line with the respective losses. If this balance is not satisfied then it is represented in the slack variables. (TODO: put loss in the equation). The constraint 3.2b defines the transmission bounds for each line.

### **Economic dispatch model with unit commitment constraints**

This optimization model is a mixed-integer linear program (MILP). This model includes decision variables to capture “on” and “off” decisions for thermal generators in each time period. The objective function must be modified to account for start up and shut down costs with thermal generators.

## **3.3 Implementation**

Here write about how it was implemented, in AIMMS, put some running times in a table, some images, put a brief description about what is AIMMS and why it is used, and etc. If I cite this one, will it appear? [1].

# Chapter 4

## Analysis

In the analysis make all the scenario runs, describe the data.



## Chapter 5

## Conclusion



# Appendix A

## Power Systems Operation Background



# Appendix B

## Data and Analysis





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