

Exoplanets

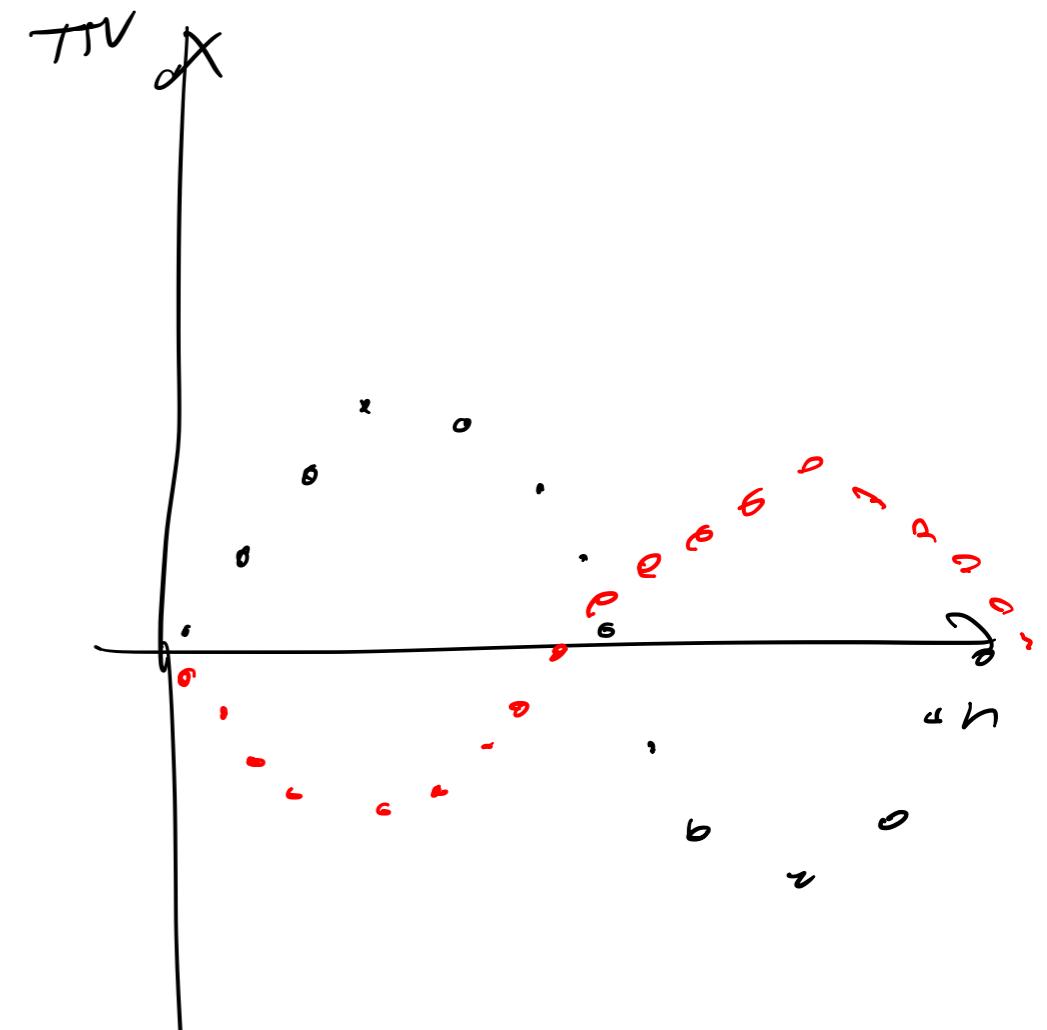
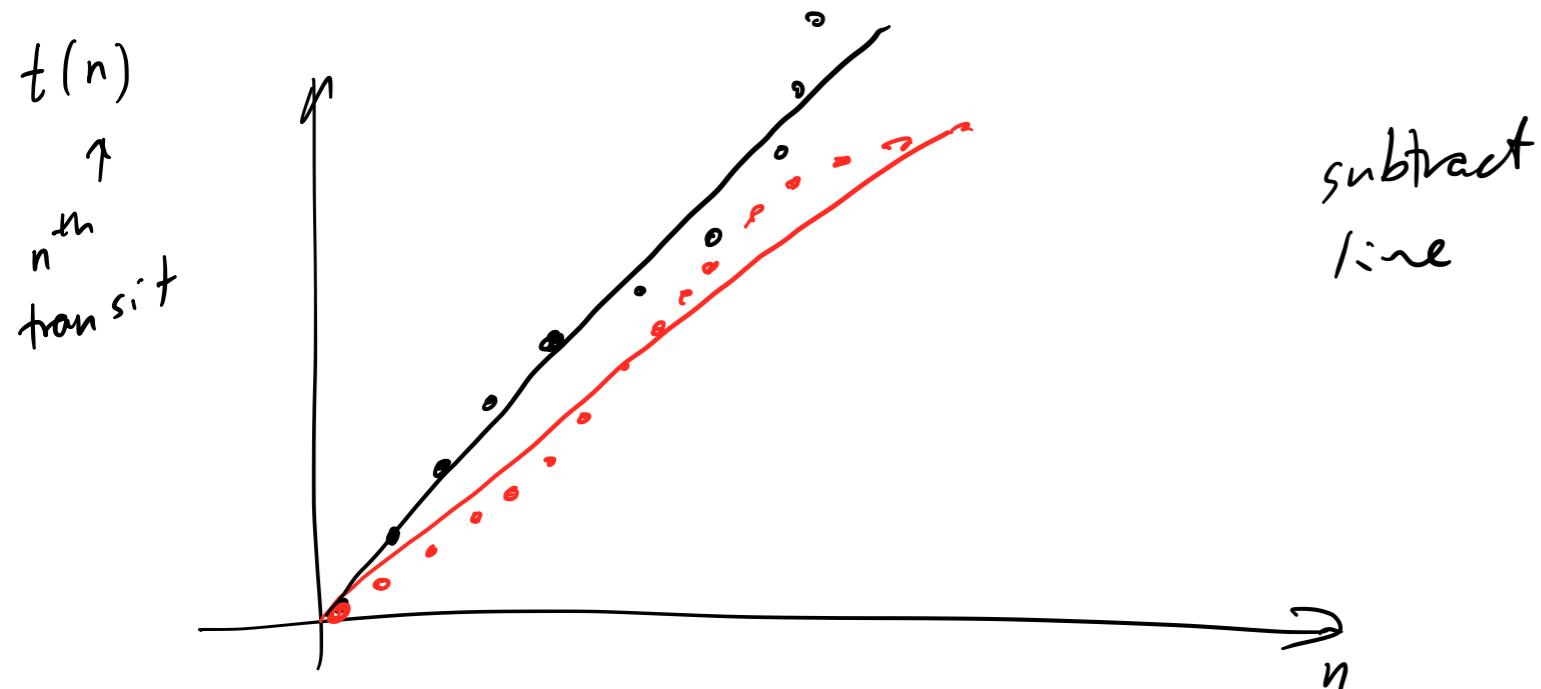
Lecture 11

Eric Agol, Autumn 2022

Transit timing overview

- For a single planet orbiting a star: transit times are precisely periodic (ignoring non-Newtonian effects)
GR, tidal oblateness
- Residuals to linear fit to transit times are transit-timing variations or “TTVs”
Discover planets : KOI 872.02
Kepler object of interest
- TTVs scale with:
Exomoons : eventually ?
 - 1). mass ratio of companion planets to star;
 - 2). orbital per.;
 - 3). scale with proximity of planets to one another & to mean motion resonances.
periods close to $j:j+1$ (j is an integer).
first-order

Transit-timing variations (TTV)



i). Correct for light-travel time across solar system

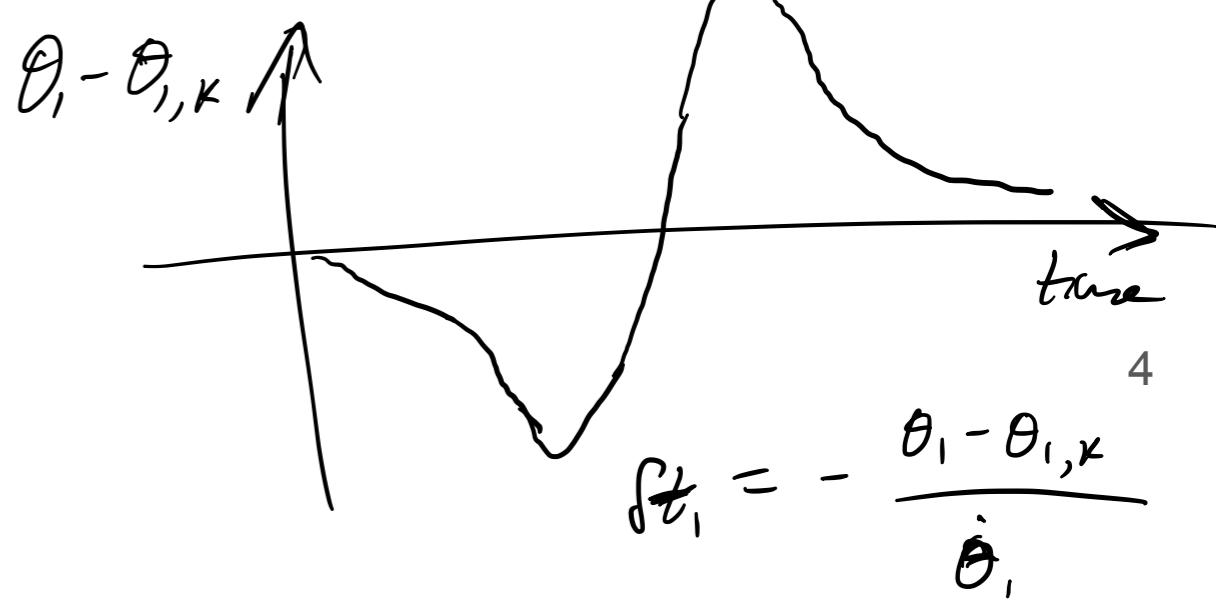
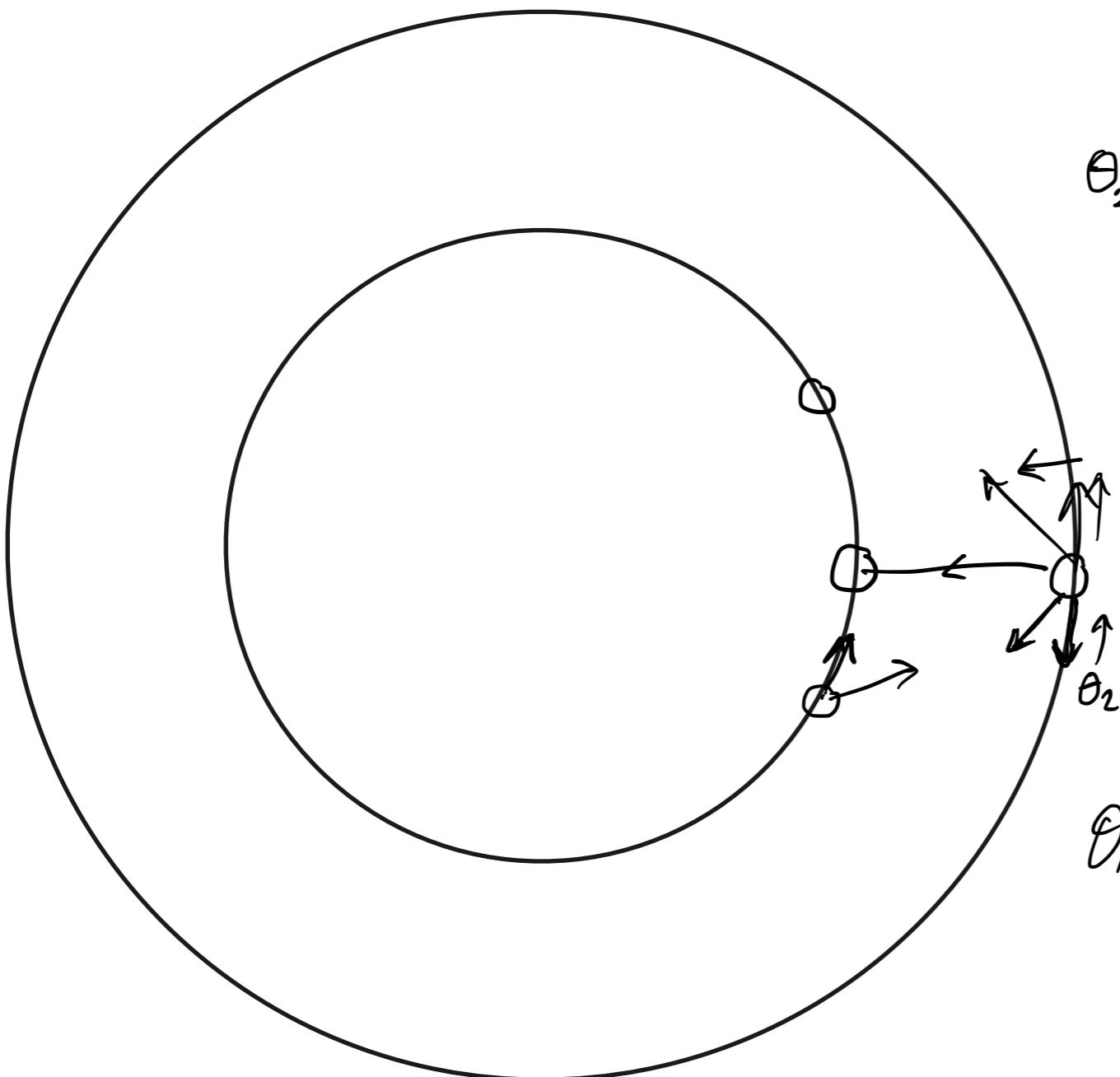
→ to barycenter of solar system.

"Barycentric Julian Date"

↑ corrected for light-travel time

Perturbations at conjunctions

Perturbations occur at harmonics of the conjunction timescale.



Resonant perturbations

- near-resonant interactions

- Epicyclic frequency = orbital frequency for $1/r^2$ potential

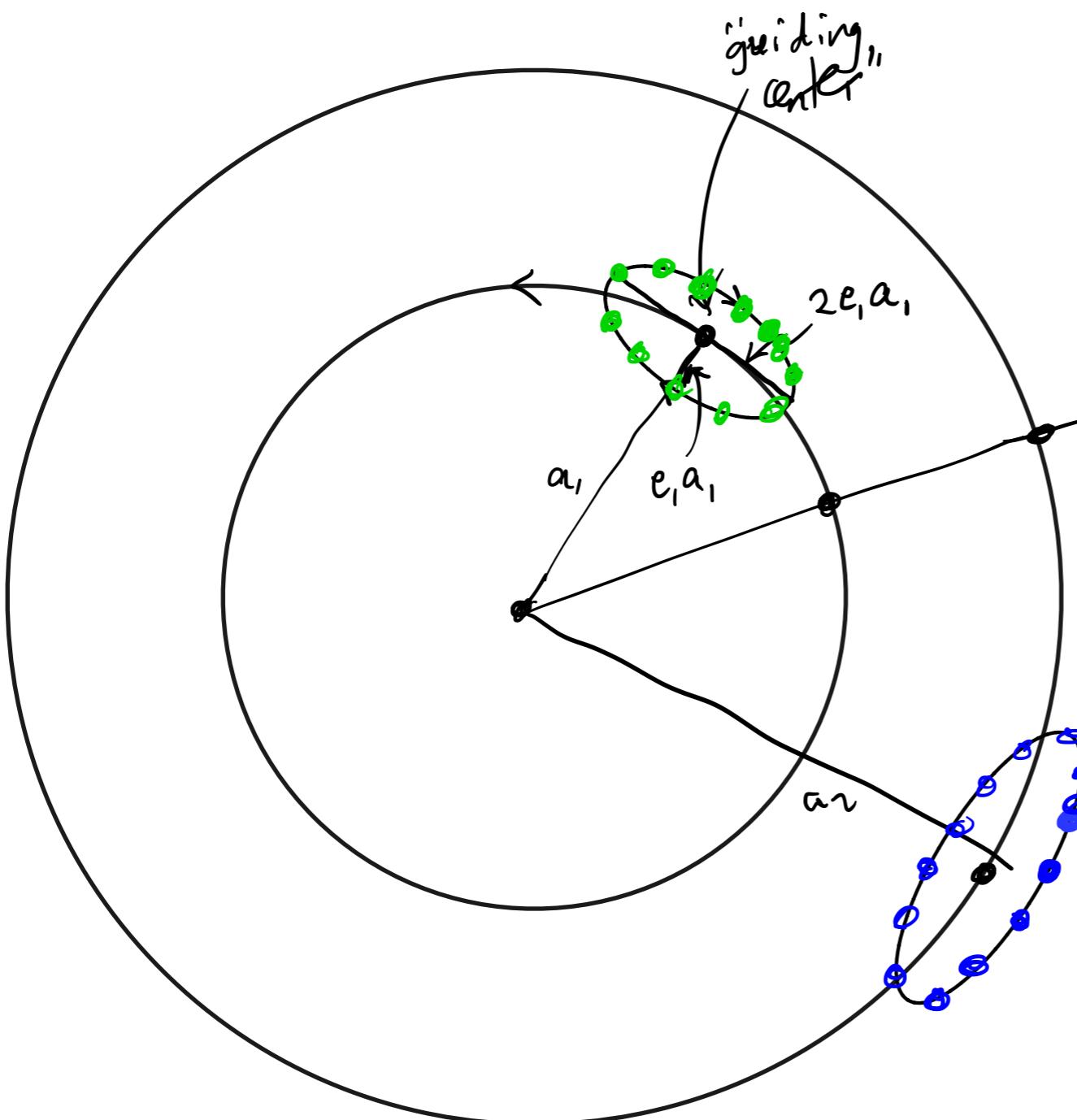
- If planets are close to resonance, $\frac{P_1}{P_2} \approx \frac{j}{j+1}$

- Motion of conjunctions about epicycle determines how they interact

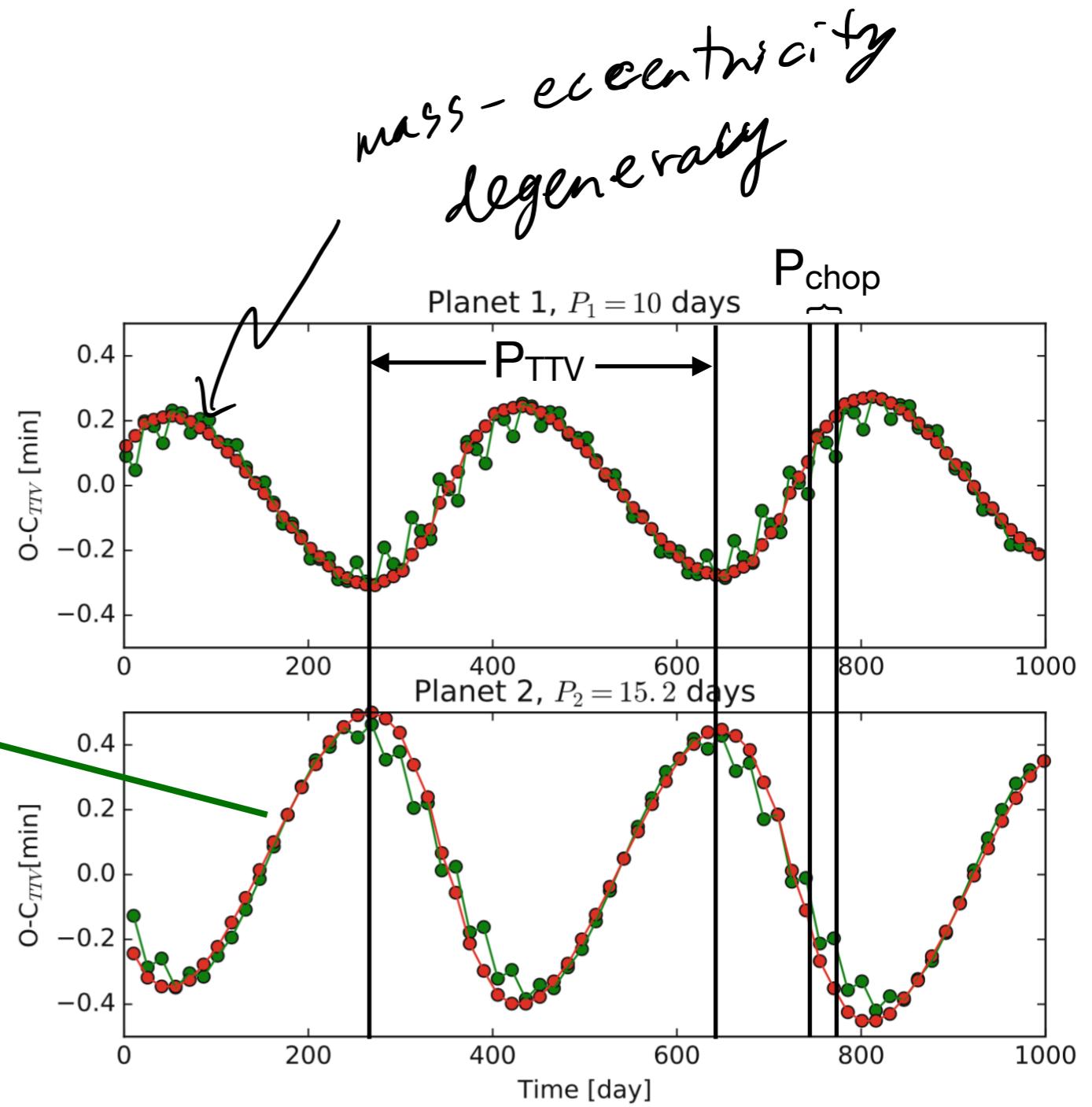
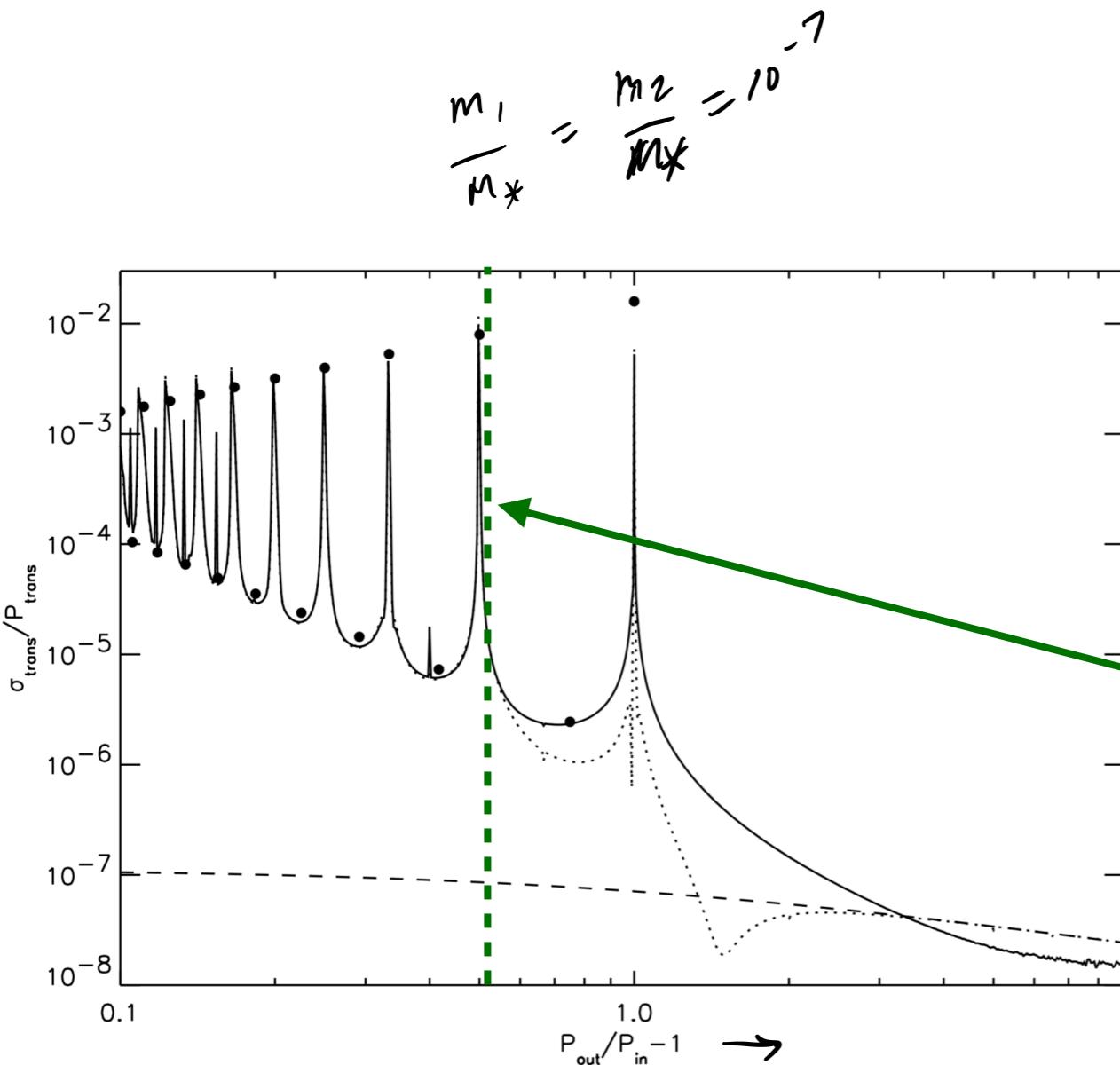
- Oscillations in perturbations of orbits.

$$P_{TTV} = \frac{1}{\left| \frac{j}{P_1} - \frac{j+1}{P_2} \right|}$$

- leads to sinusoidal transit timing variations on this longer timescale



Transit-timing anatomy



Agol Steffen Sari &
Clarkson (2005)

$$P_{\text{TTV}} = |j/P_{\text{in}} - (j+1)/P_{\text{out}}|^{-1}$$

$$= |2/10 - 3/15.2|^{-1} = 380 \text{ d}$$

$$P_{\text{chop}} = |1/P_{\text{in}} - 1/P_{\text{out}}|^{-1} = 29.2 \text{ d}$$

Agol & Fabrycky (2017)

A 150 mass-eccentricity - eccentricity degeneracy

TTV applications

1. Confirm of multi-transiting planets. (*not multiple stars or not diluted EBS*)
2. Detection of non-transiting companions.
KOI-872
3. Characterize of masses, eccentricities.
4. Discovery of exomoons.
5. With RV, measurement of absolute masses.

$$K_* \propto P^{-\frac{1}{3}} \frac{M_1 \sin i}{M_*^{\frac{2}{3}}} \quad \left. \begin{array}{l} M_1, \sin i \\ M_*^{\frac{2}{3}} \end{array} \right\}$$

RV + TTV

→ measure
mass of
star

$$\delta t_1 \propto P_1 \frac{M_2}{M_*} \quad \left. \begin{array}{l} M_2 \\ M_* \end{array} \right\}$$

$$\delta t_2 \propto P_2 \frac{M_1}{M_*} \quad \left. \begin{array}{l} M_1 \\ M_* \end{array} \right\}$$

TTV drawbacks

1. Requires long term monitoring of transits
2. Aliasing limits the dynamical information
- 3 ~~4.~~ Degeneracy between mass and eccentricity (low precision)
- 4.5. Degeneracy between planets' eccentricity and longitude of periastron of 2 planets.
5. Unknown planets (don't transit or shallow) which perturb TTVs.

Trappist survey

- “Ultracool dwarfs”: lamppost effect:
 - smallest stars
 - most common → close proximity
 - Low-T stars have highest temperate transit probability (Charbonneau & Deming 2007) Gould 2003
 - Two telescopes: La Silla, Morocco - 60cm, I+z (>700nm)
 - 50 stars surveyed
- 2016: first planet system - TRAPPIST-1

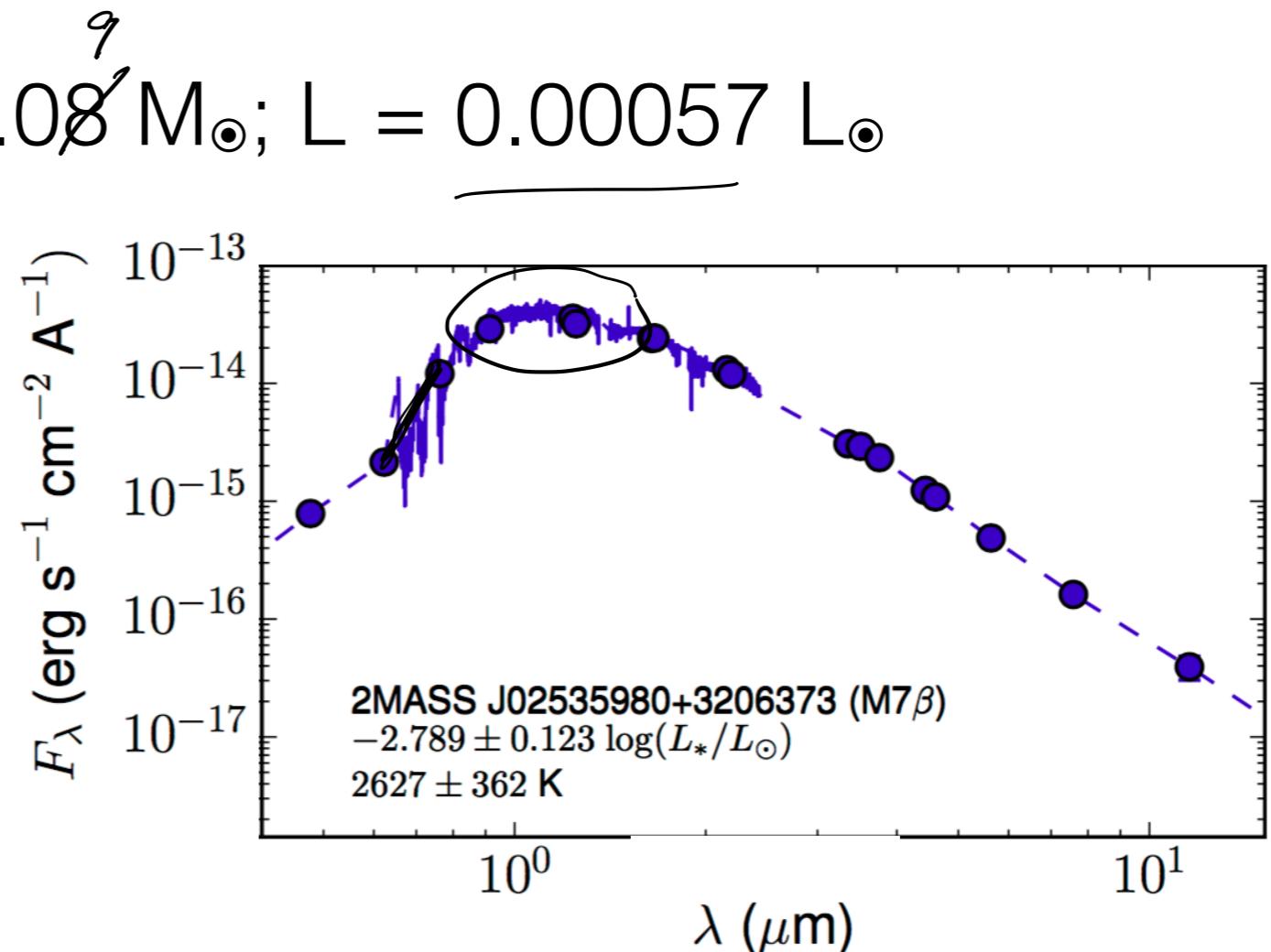
Trappist-1 host star

$R = \underline{0.12} R_\odot; M = \underline{0.08} M_\odot; L = \underline{0.00057} L_\odot$



SDSS image

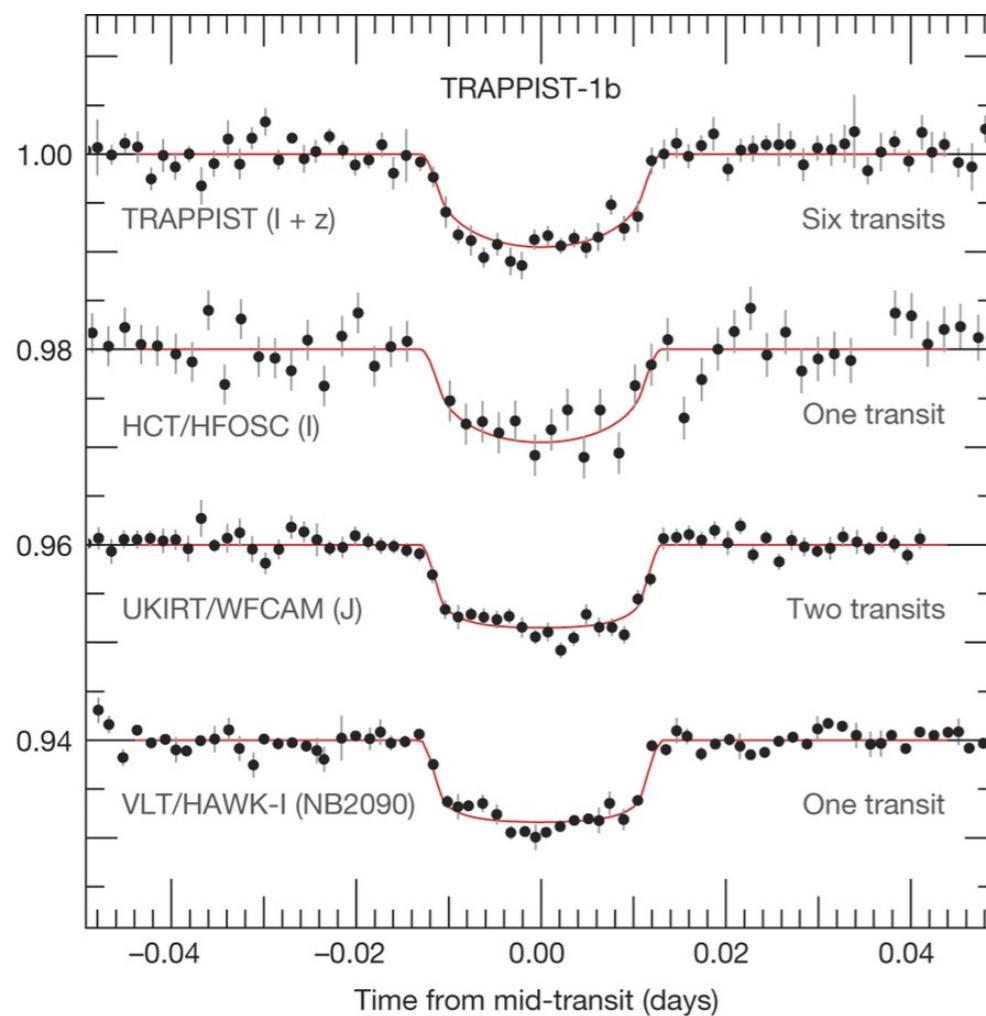
$T_{\text{eff}} = \underline{2560}$ K; $d = 12.2$ pc; $7.6+2.2$ Gyr (Burgasser & Mamajek 2017); $[\text{Fe}/\text{H}] = 0.04 \pm 0.08$



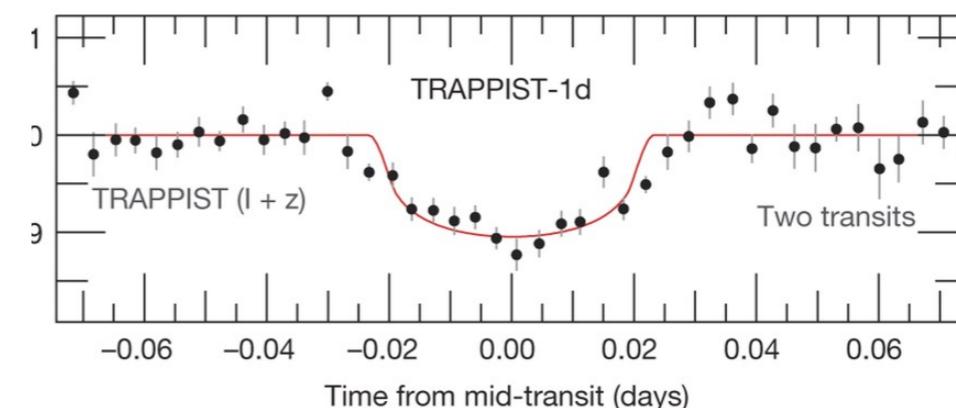
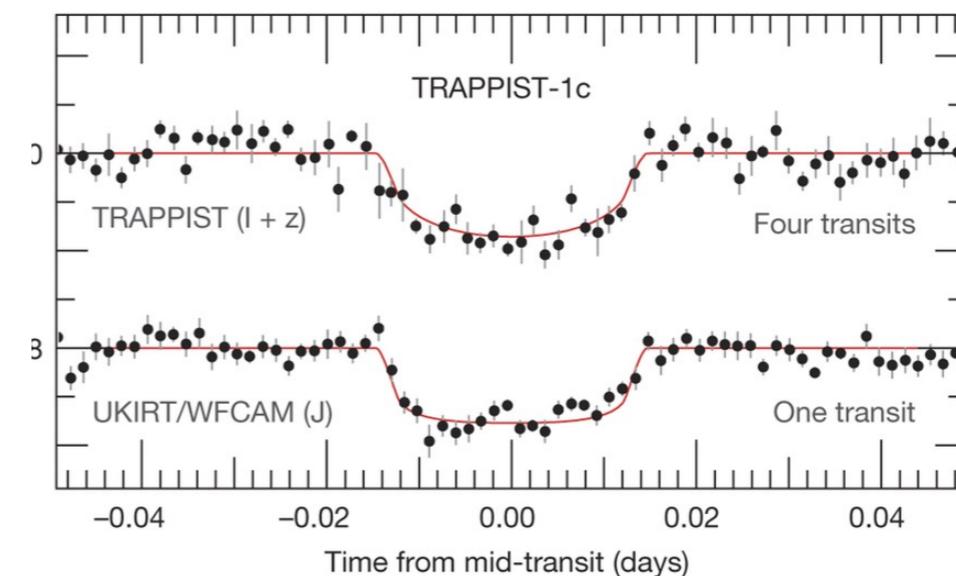
George Wallerstein notation

Trappist 1b,c

1.5 d



\sim 2.4 d



Gillon et al. (2016)

Plus hints of other transits...

Size comparison

Sun:



29.5"

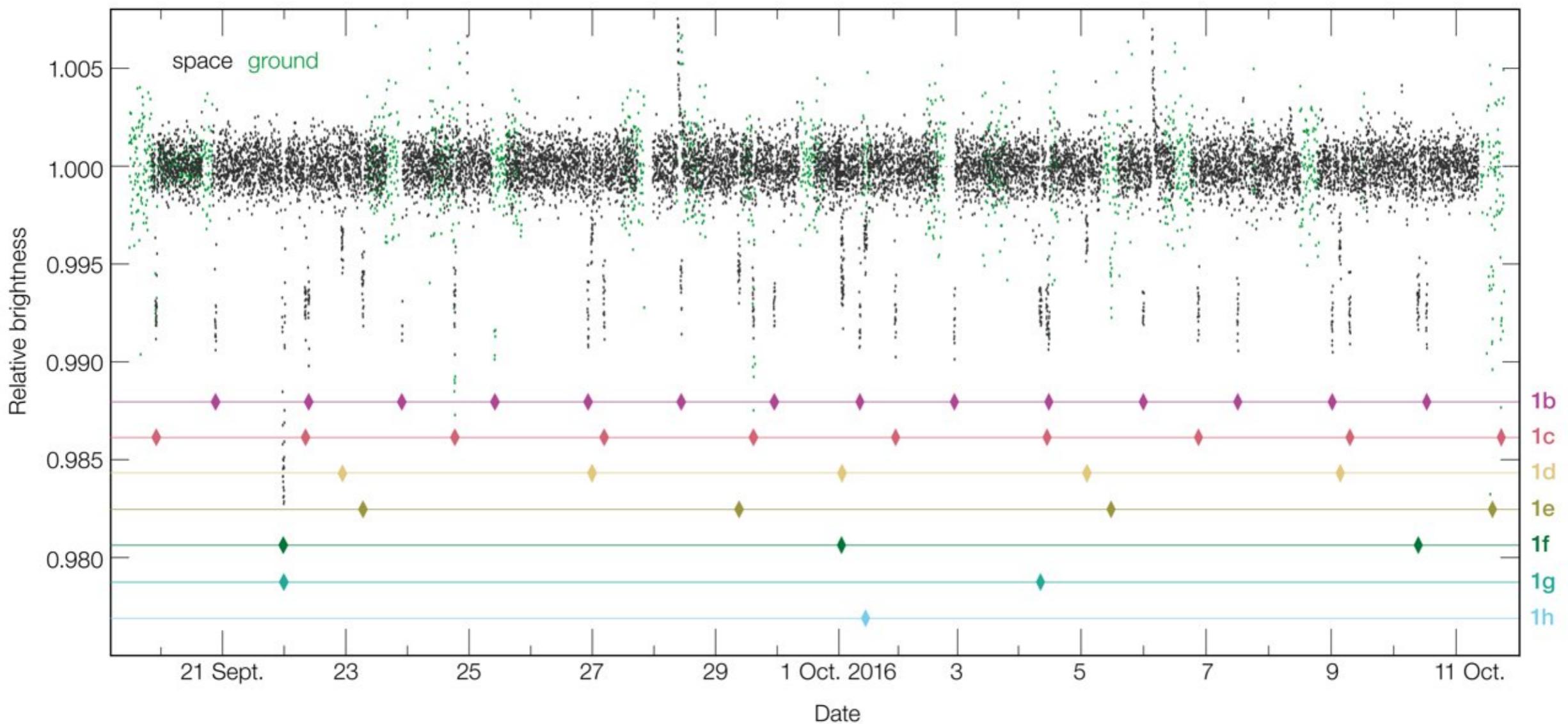
TRAPPIST-1: 1.1"



Planets b-h: 1/8"



Spitzer light curve

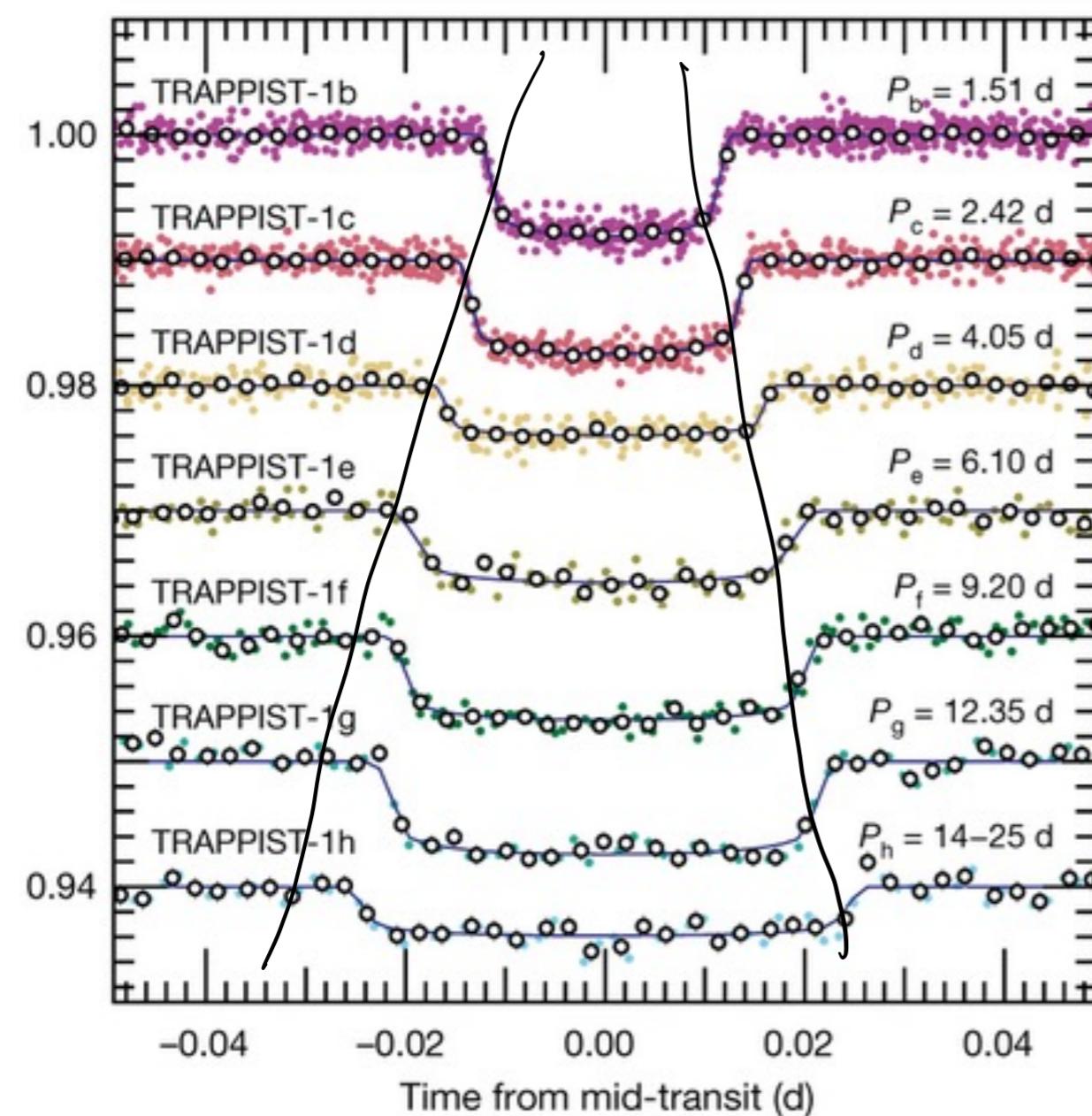


Transits occur 6% of the time!

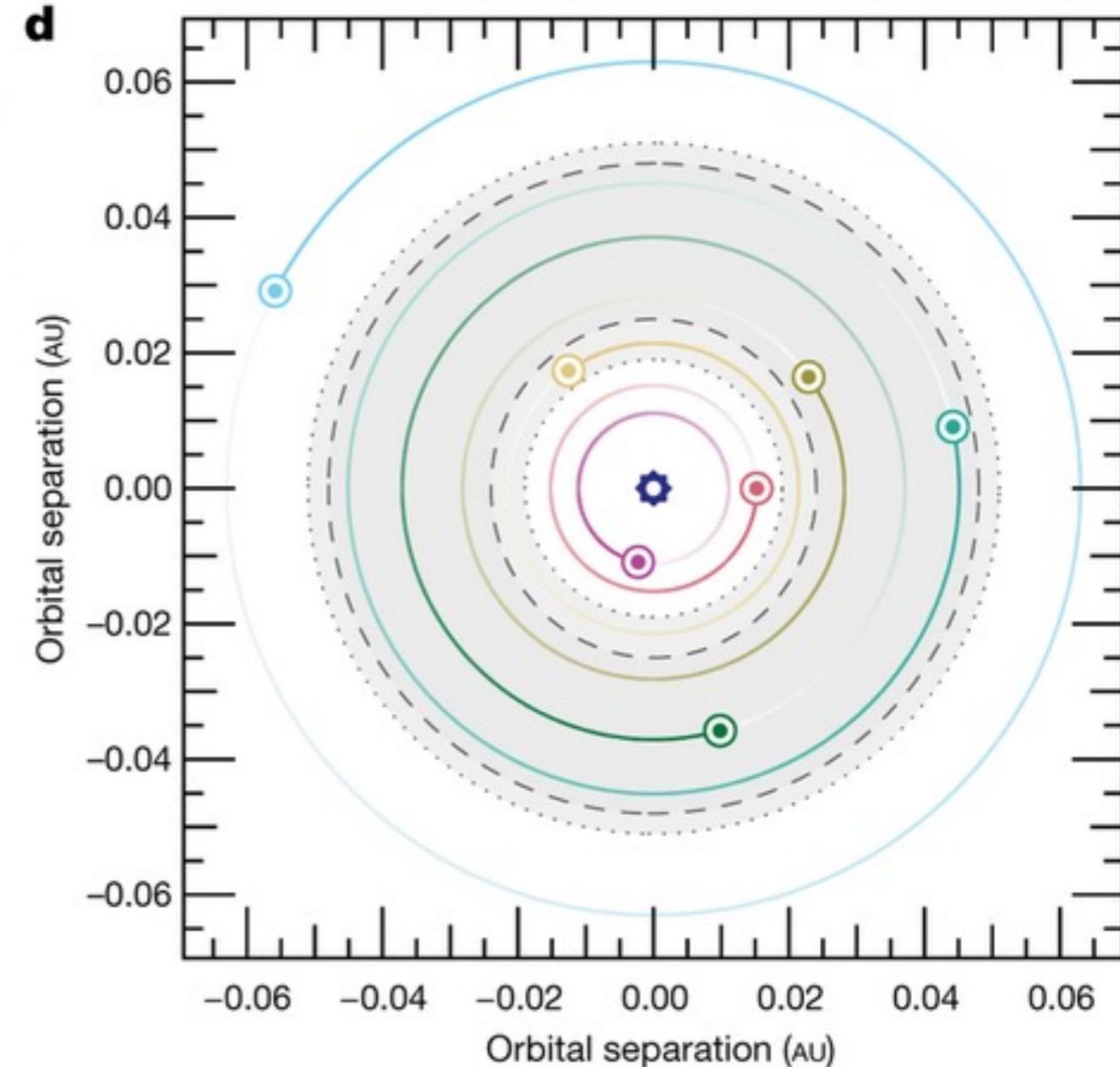
GILLON ET AL. 2017

$$P_c/P_b, P_d/P_c, P_e/P_d, P_f/P_e \text{ & } P_g/P_f \approx 8/5, 5/3, 3/2, 3/2 \text{ & } 4/3$$

c



d



$$T \propto P^{1/2}$$

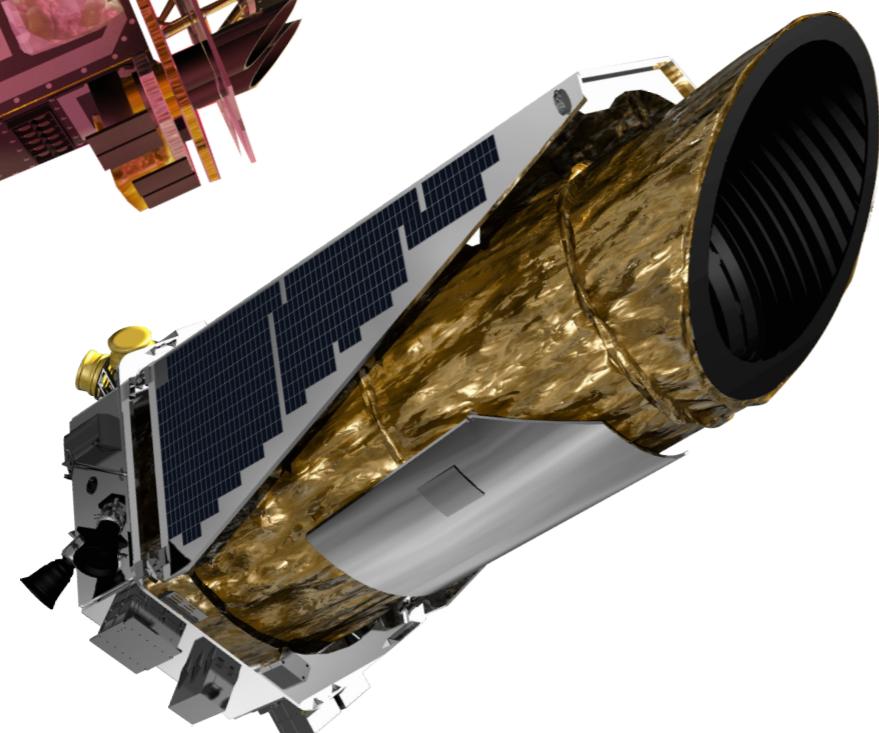
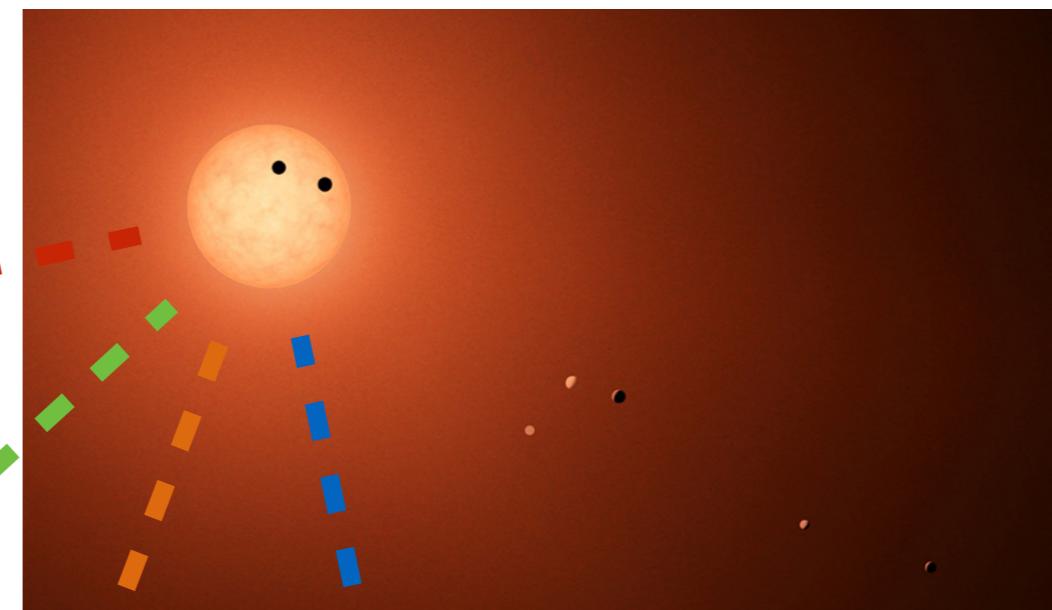
GILLON ET AL. 2017

Transit timing survey

Spitzer: **188**



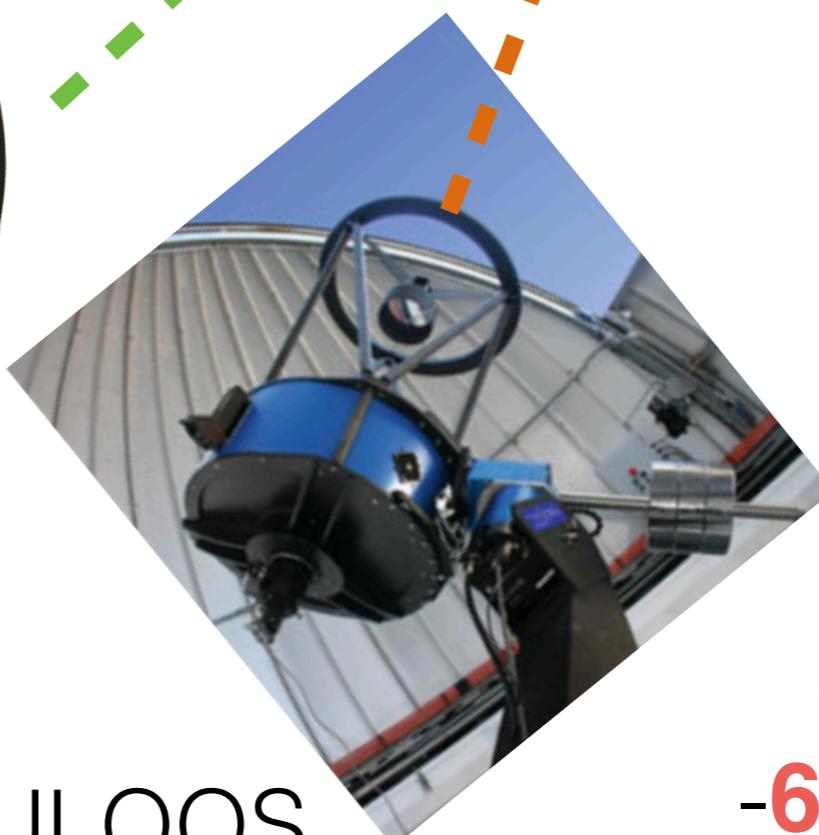
1 star:
 $0.09 M_{\odot}$,
 $0.12 R_{\odot}$
2570 K
12 pc



K2: **126**

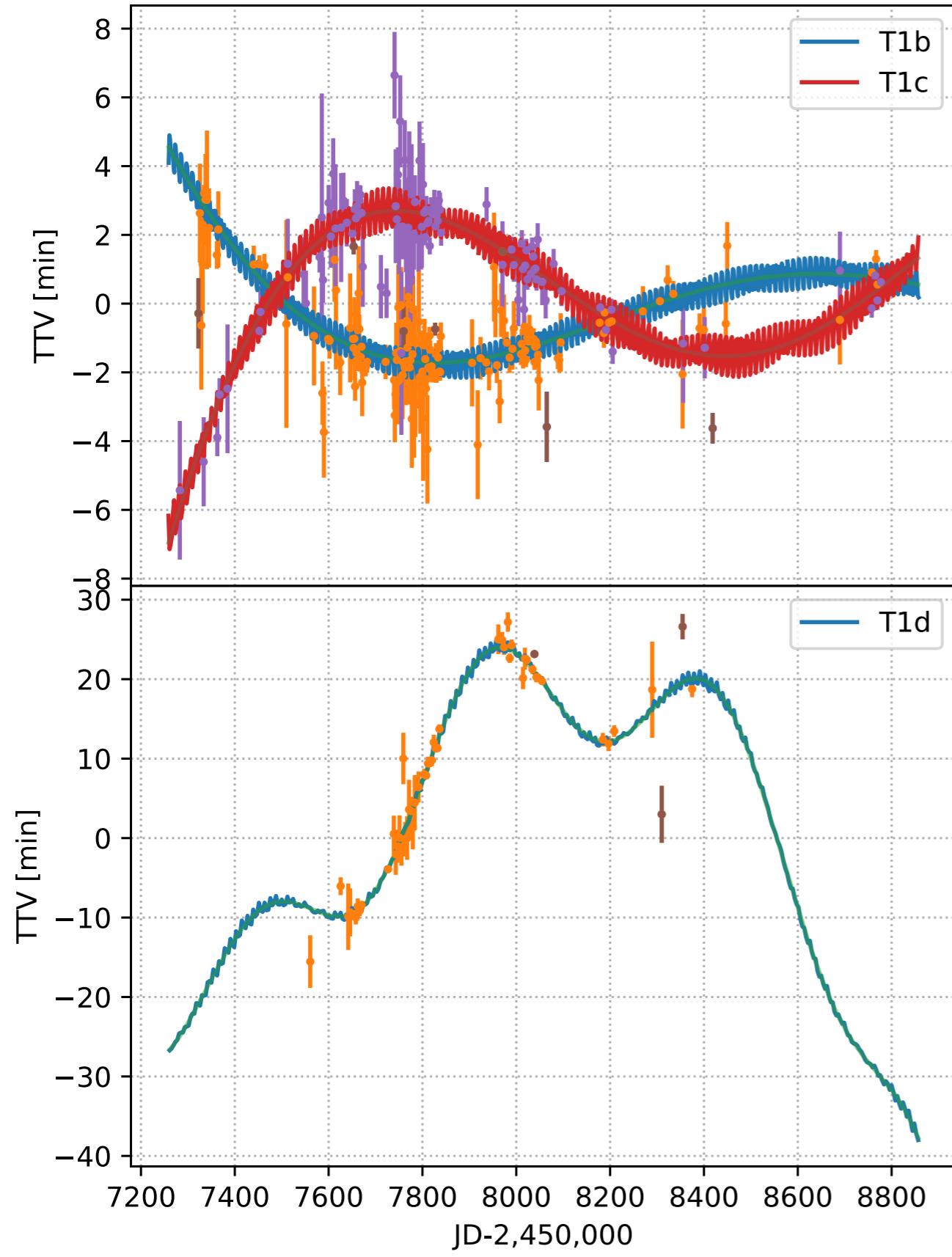
SPECULOOS,
TRAPPIST-N/S: **125**

7 planets:
1.5-19 days
 $0.75-1.1 R_{\oplus}$
 $0.3-1.4 M_{\oplus}$
 $0.1-4 S_{\oplus}$

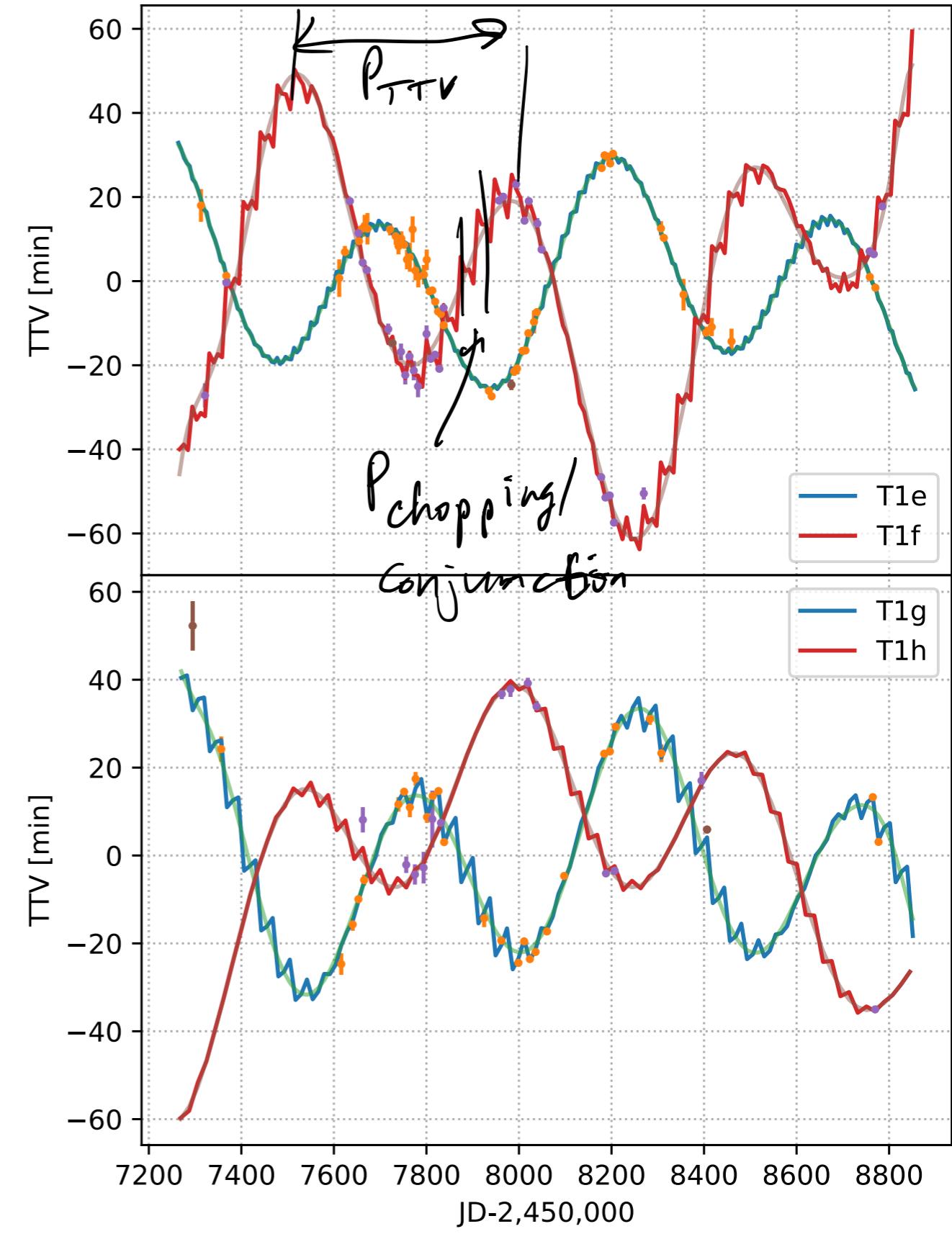


+Other: **69**
-**61** duplicates
= **447** transits 15

Final Spitzer TTV analysis

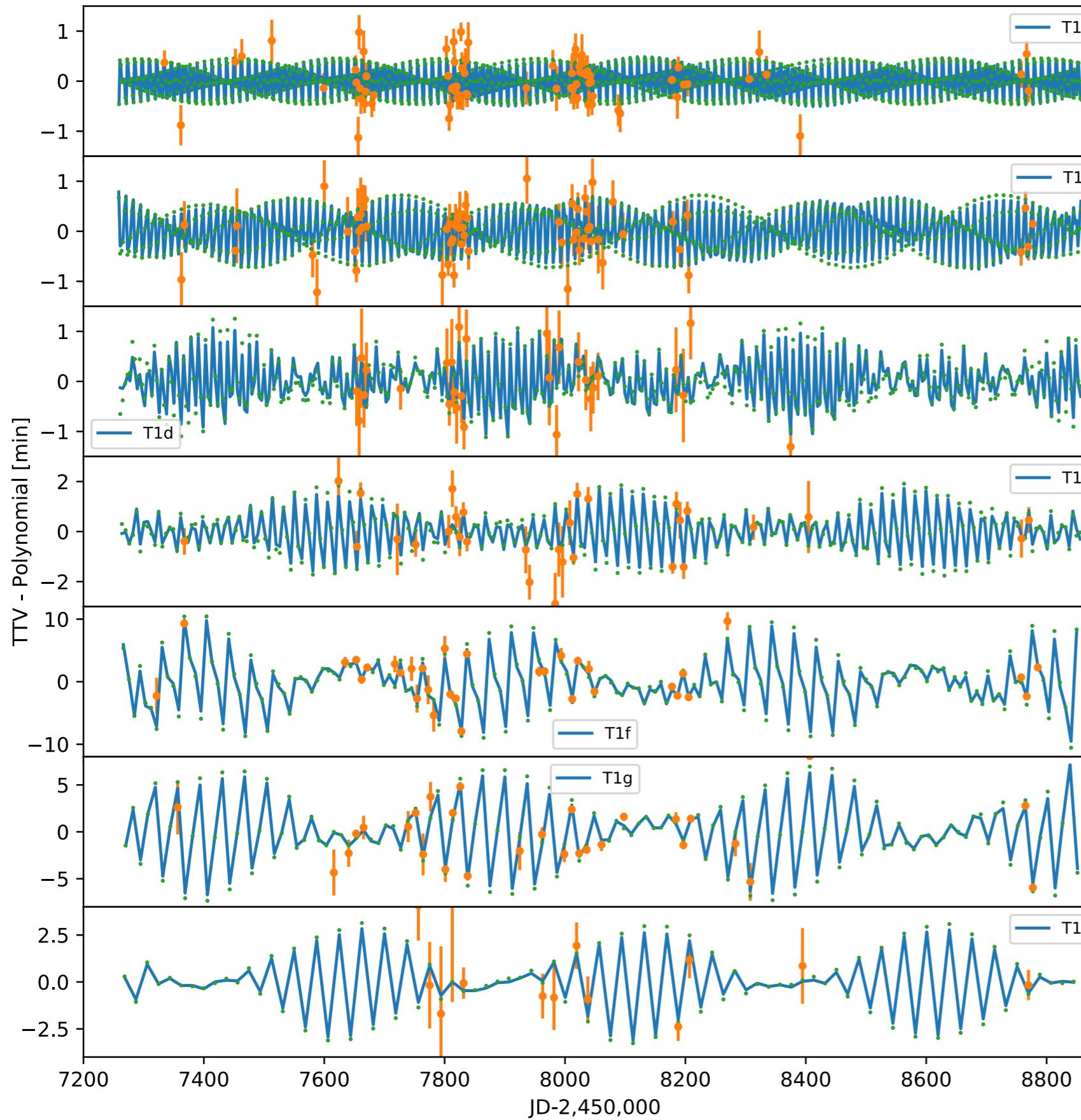


- Times through Oct 2019.

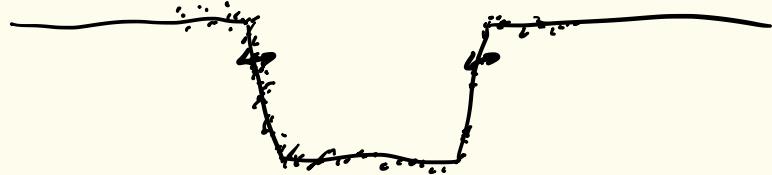


- Plane-parallel analysis

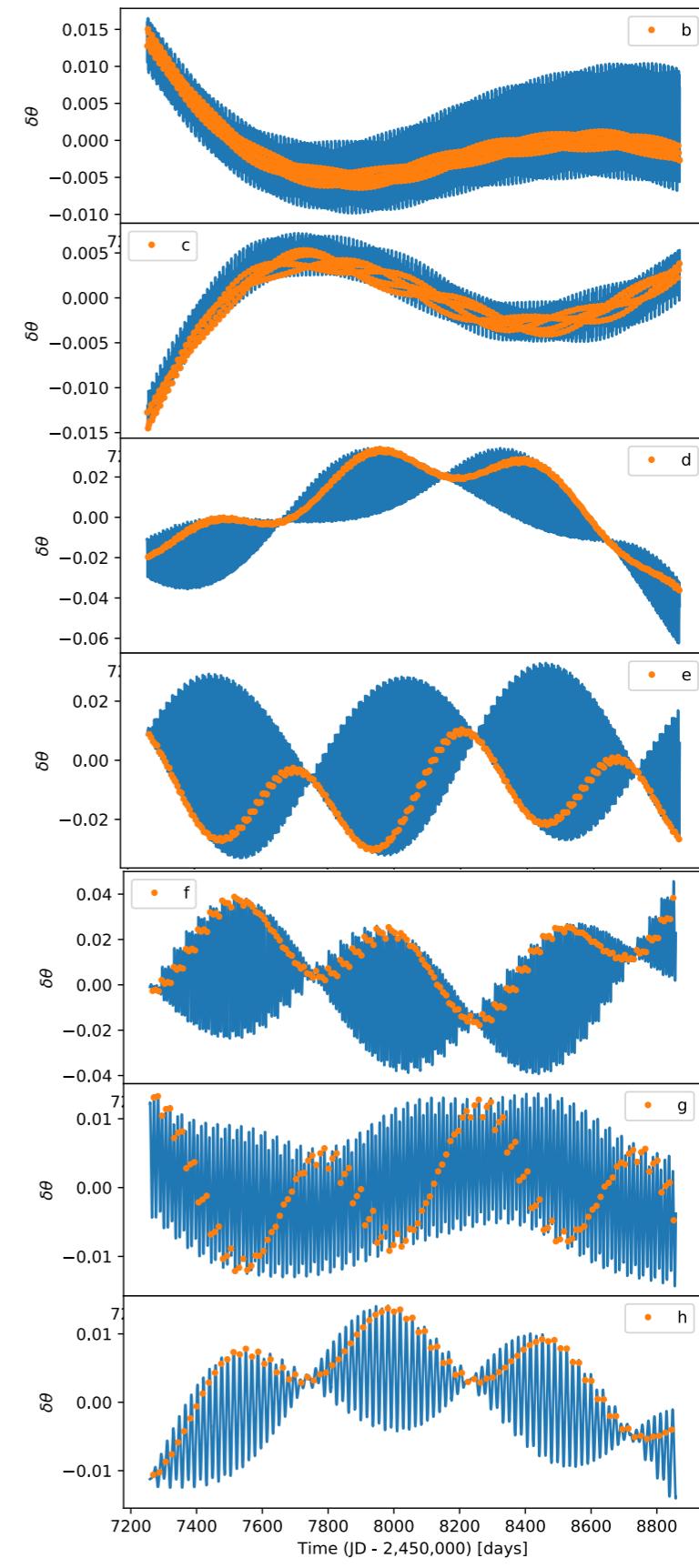
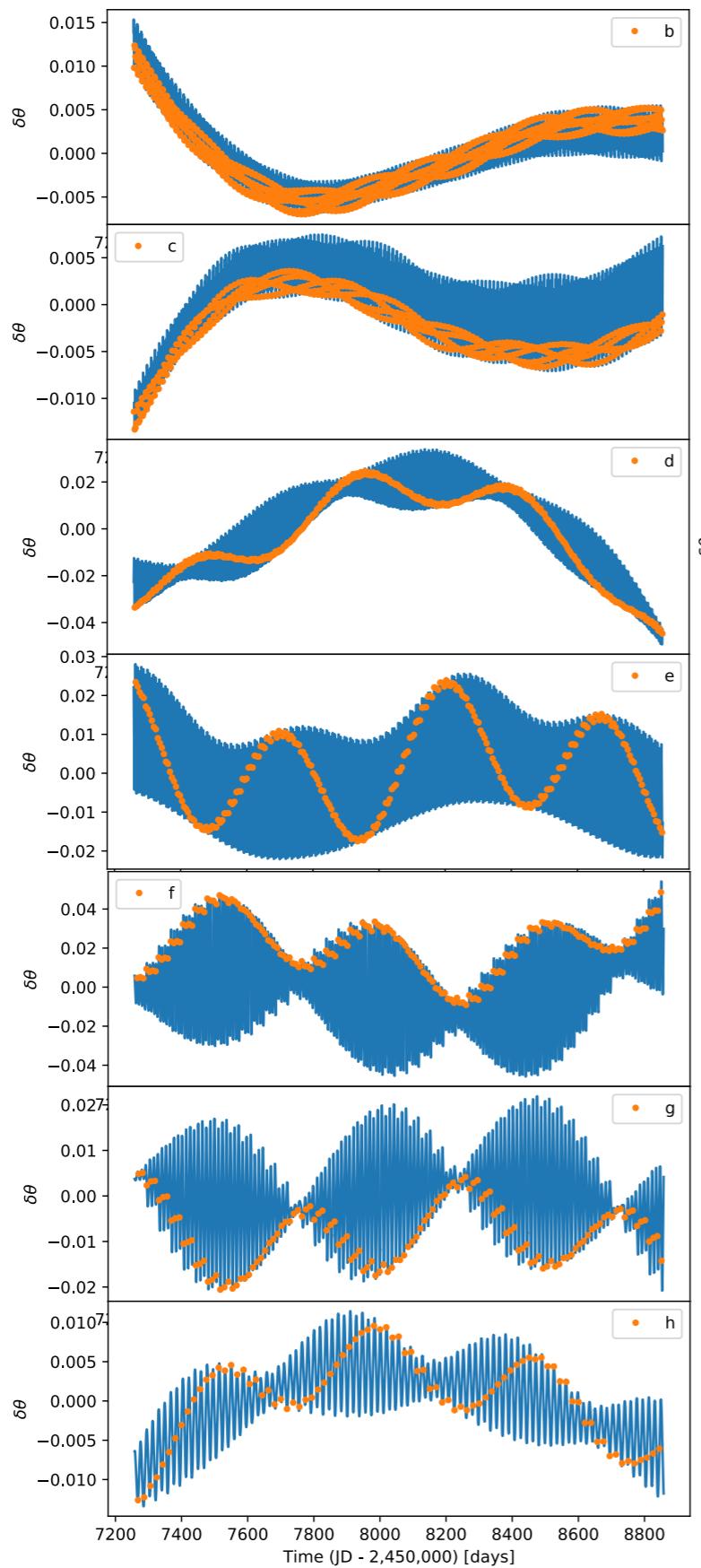
“Chopping” TTV: sensitive to mass-ratios



Blue lines: TTV model with polynomial removed
Orange error bars: data.
Green dots: analytic chopping model



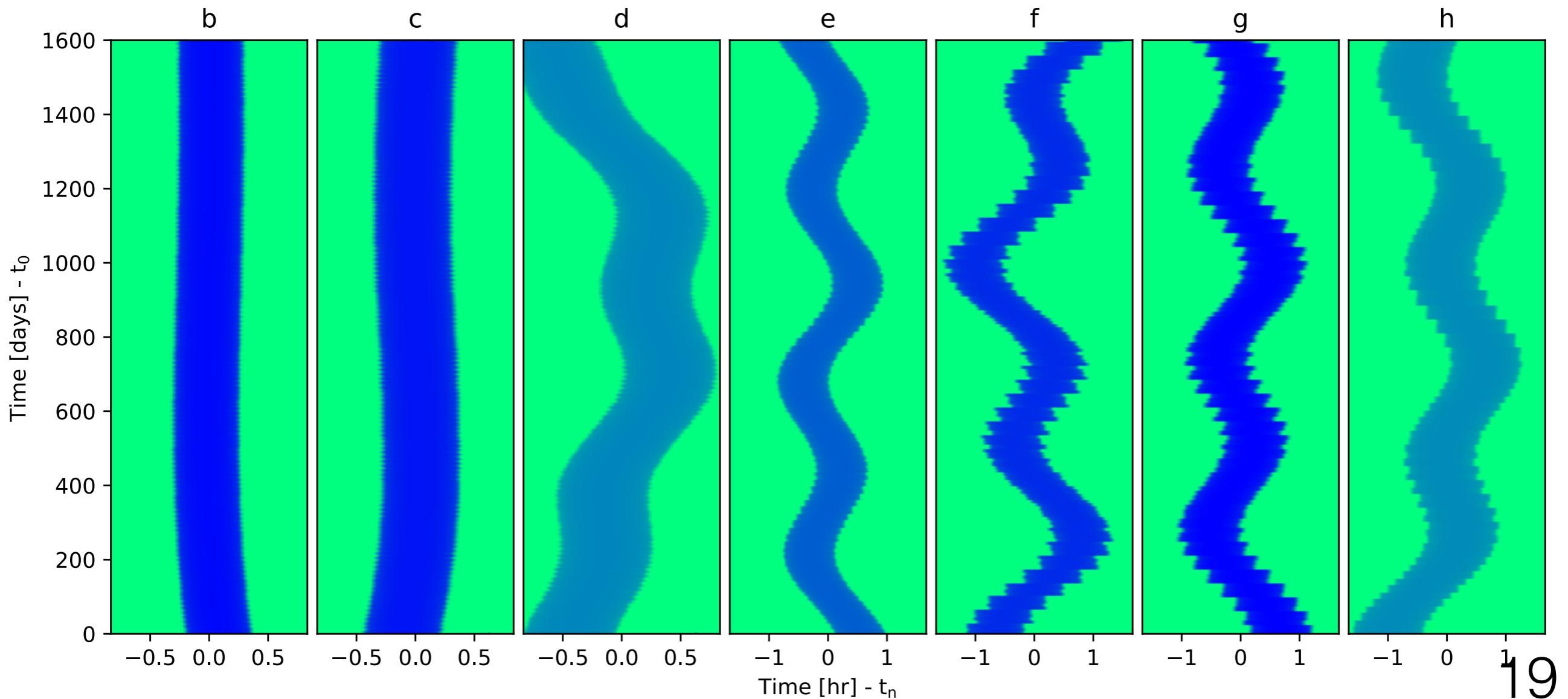
Aliasing



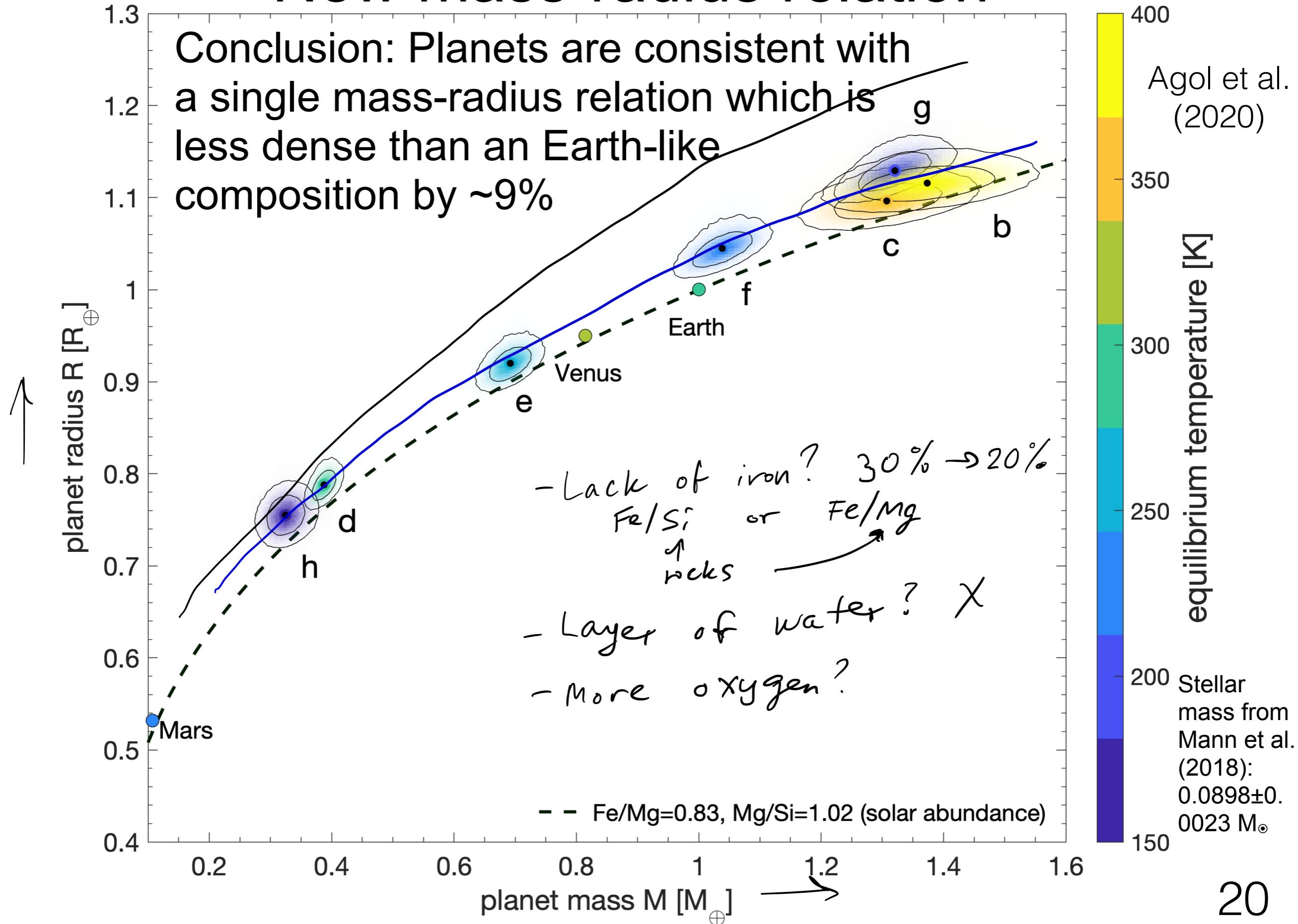
$$E = -\frac{GM_x}{2a_1} - \frac{GM}{2a_2}$$

Photodynamic model

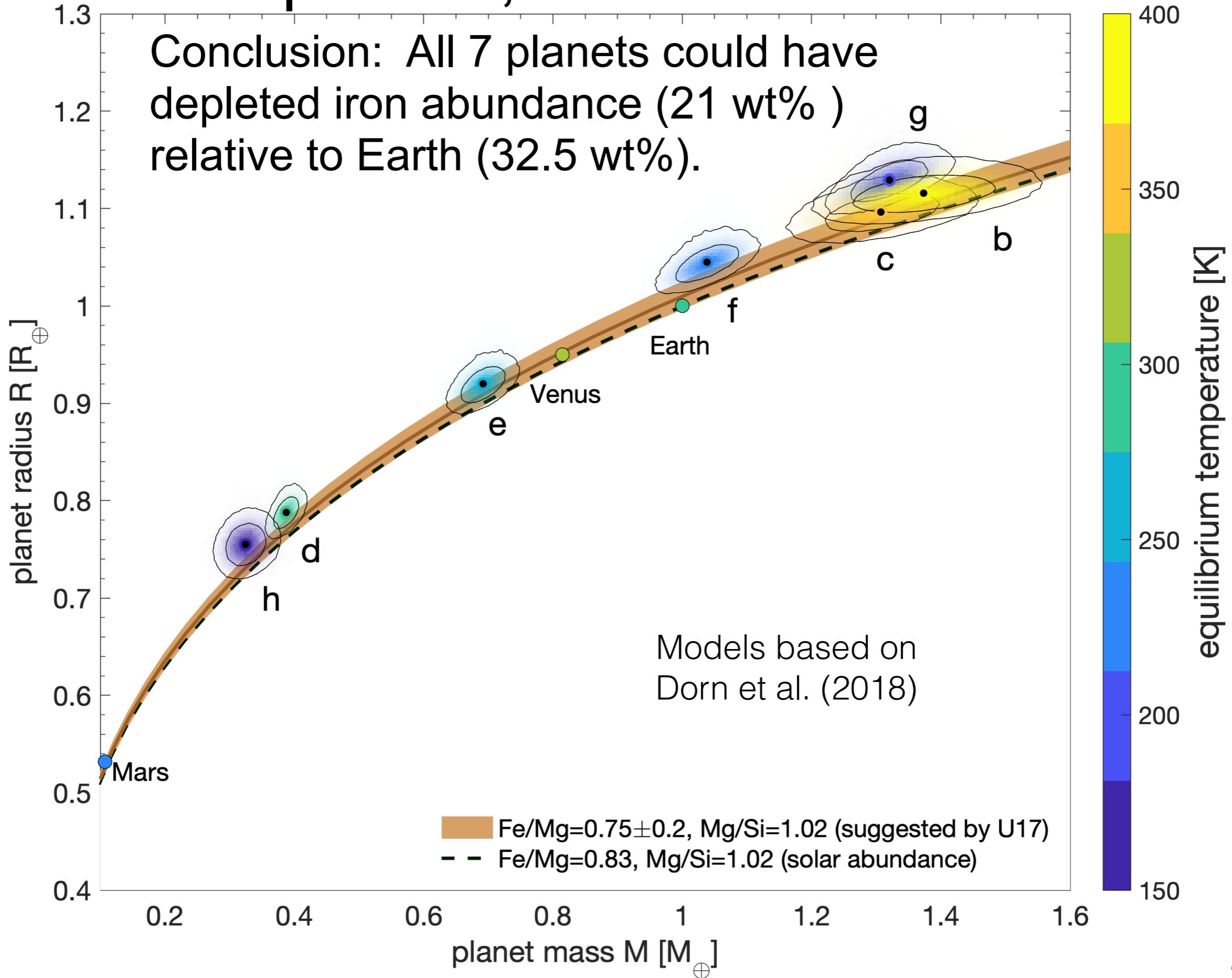
- Varied the stellar density, limb-darkening parameters, impact parameters, and radius-ratios.
- Held fixed the dynamical parameters at best-fit model.



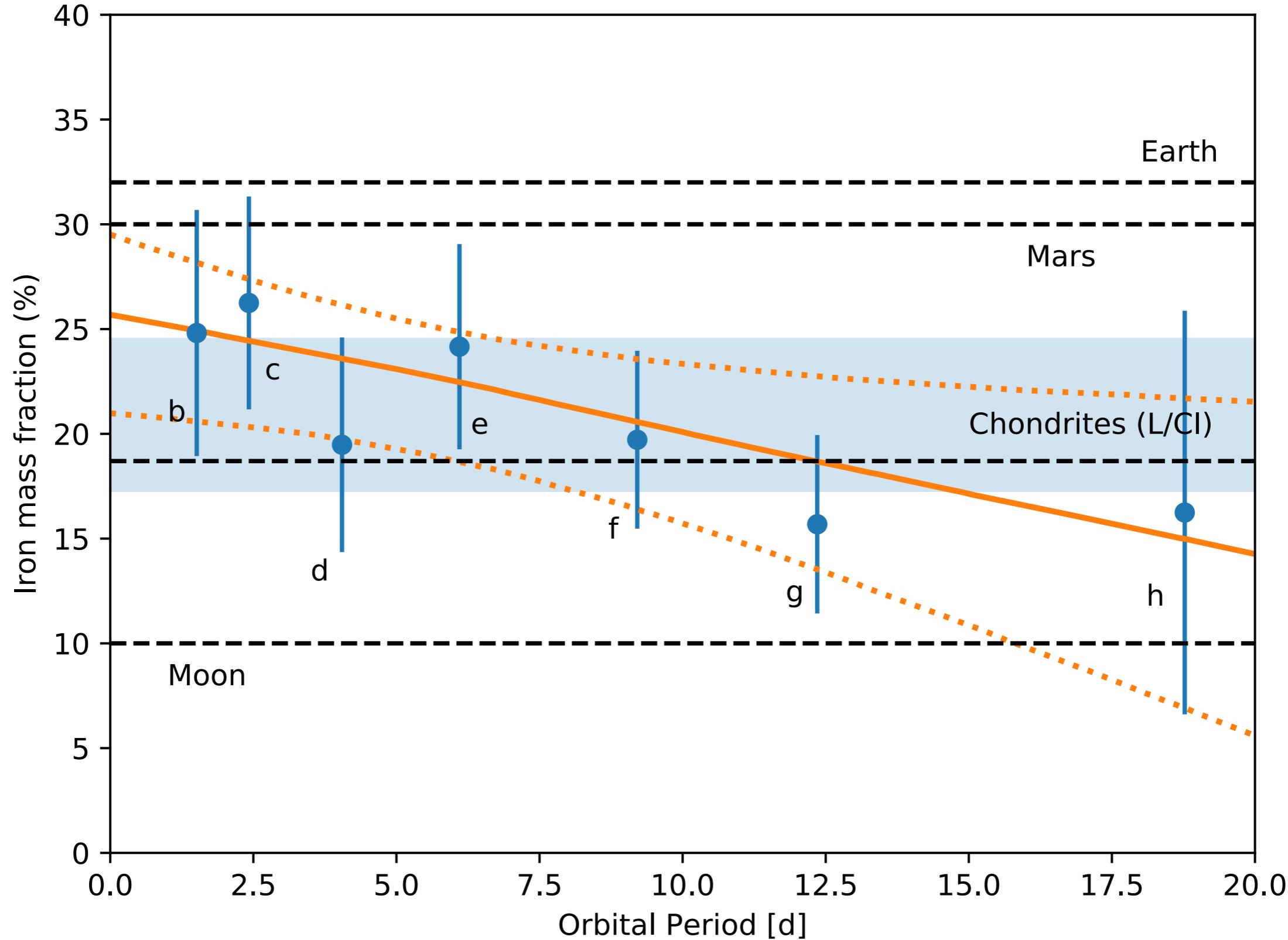
New mass-radius relation



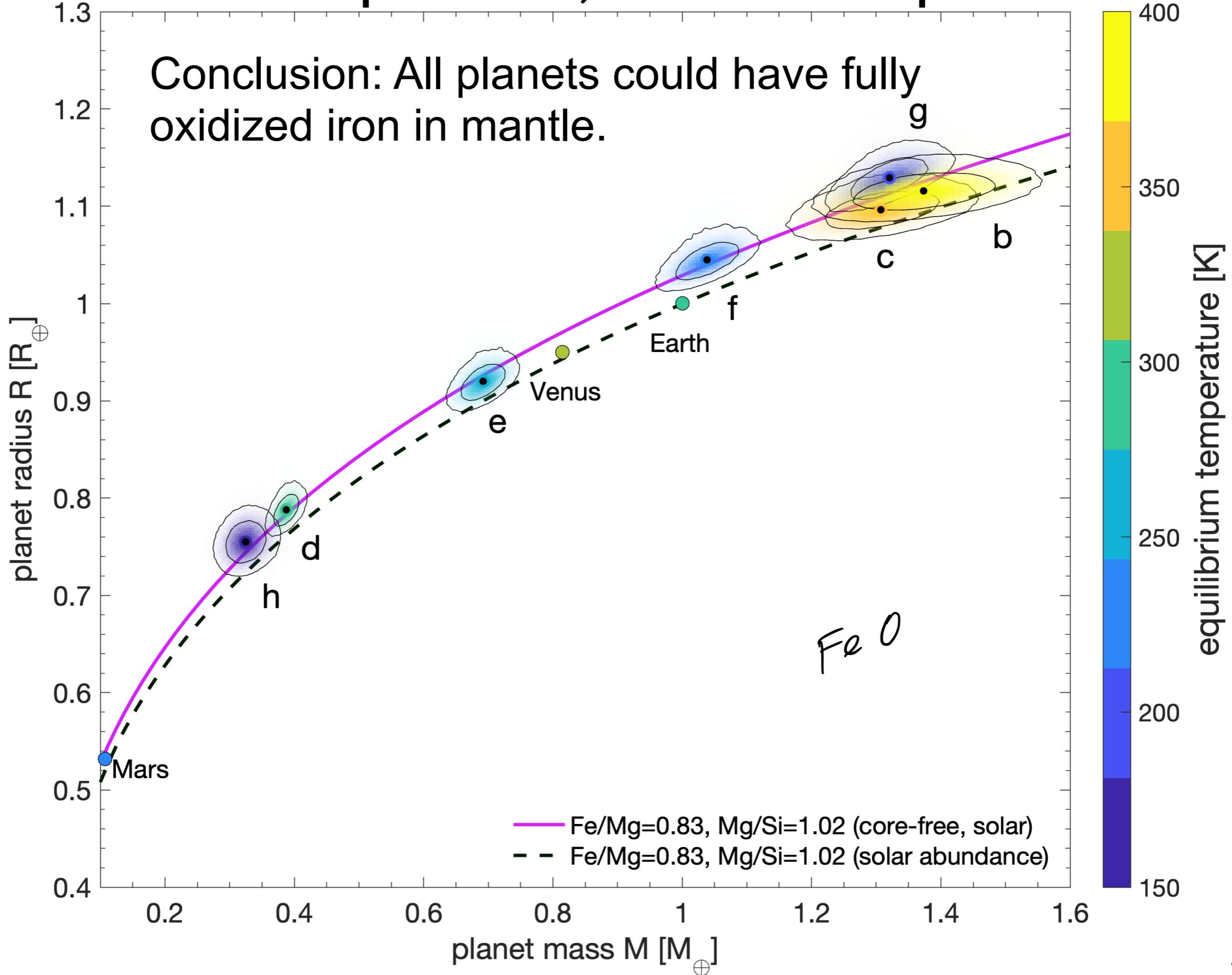
Cored planets, variable iron content



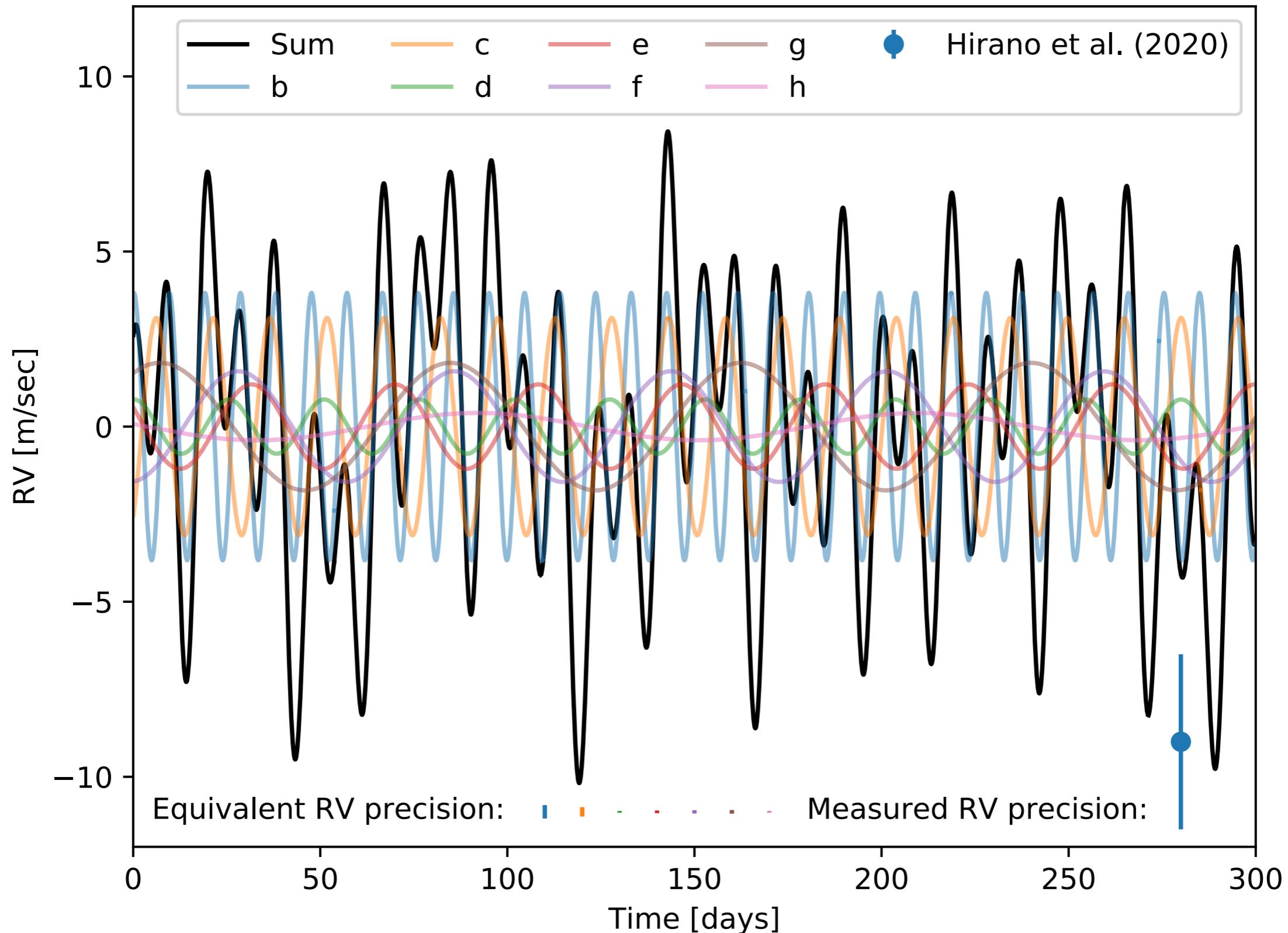
Iron mass fraction versus orbital period



Coreless planets, Solar composition

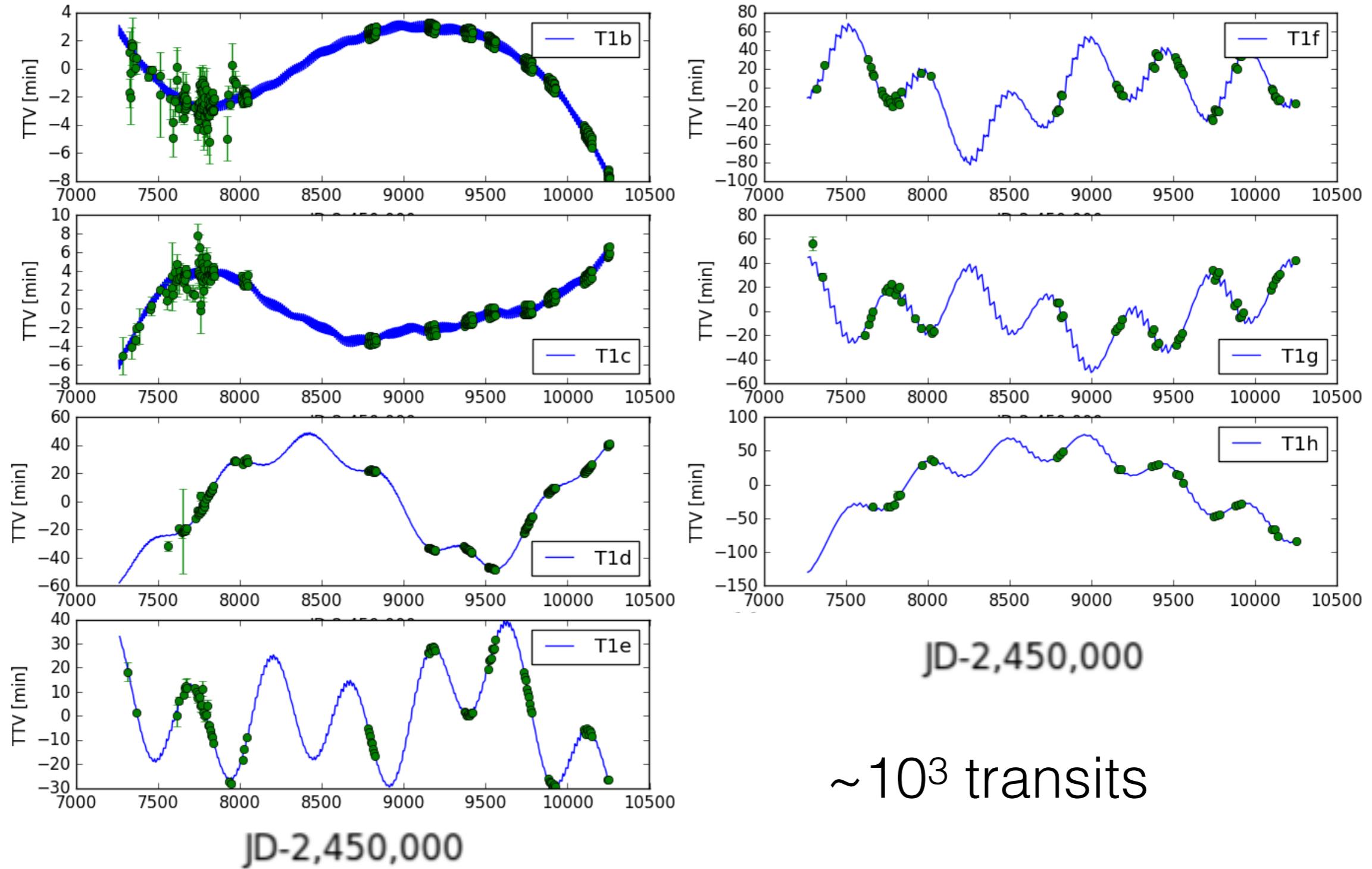


Radial velocity comparison



Simulate “pirated” JWST

~second timing precision → part-per-thousand mass ratios



Next time:

Astrometry & direct imaging

Reading:

“Direct Imaging of Exoplanets” Traub & Oppenheimer;

“Astrometric Detection and Characterization of Exoplanets”
Quirrenbach