

Econ 327: Game Theory

Practice Final Exam

University of Oregon

December 8th, 2025

- Complete *all* questions and parts. All questions will be graded.
- Carefully explain all your answers on short and long answer questions.
An incorrect answer with clear explanation will earn partial credit, an incorrect answer with no work will get zero points.
- If you do not understand what a question is asking for, ask for clarification.

Allowed Materials:

- A single 5" by 3" note card
- A non-programmable calculator
- Pencils, color pens, eraser, etc.

Name _____

Answer the questions in the spaces provided on the question sheets. If you run out of room for an answer, continue on the back of the page or another sheet of paper.

Multiple Choice

Long Answer

Question 1. (12 P.)

Mixed Strategies: Consider the strategic form game below:

		P_2			
		Hall	Office	Library	Bathroom
P_1	Roof	0 , 2	1 , 1	0 , 2	5, 0
	Mezzanine	1 , 1	0 , 2	0 , 2	4, 0
	Ground	0 , 2	0 , 2	1 , 0	3, -1

a) (4 P.) Find any **pure strategy** Nash equilibria

b) (4 P.) Consider the following mixed strategy profile:

- Player 1 plays 1/3 **Roof**, 0 **Mezzanine**, and 2/3 **Ground**
- Player 2 plays 0 **Hall**, 1/2 **Office**, 1/2 **Library**, and 0 **Bathroom**

Check whether this is a **mixed strategy Nash equilibrium** and explain why or why not.

c) (4 P.) Now consider the strategy profile:

- Player 1 plays 2/5 **Roof**, 2/5 **Mezzanine**, and 1/5 **Ground**
- Player 2 plays 1/3 **Hall**, 1/3 **Office**, 1/3 **Library**, and 0 **Bathroom**

Check whether this is a **mixed strategy Nash equilibrium** and explain why or why not.

Screening: You are the Dean of the Faculty at St. Anford University. You hire Assistant Professors for a probationary period of 7 years, after which they come up for tenure and are either promoted and gain a job for life or turned down, in which case they must find another job elsewhere. Your Assistant Professors come in two types, Good and Brilliant. Any types worse than Good have already been weeded out in the hiring process, but you cannot directly distinguish between Good and Brilliant types. Each individual Assistant Professor knows whether he or she is Brilliant or merely Good. You would like to tenure only the Brilliant types. The payoff from a tenured career at St. Anford is \$6 million; think of this as the expected discounted present value of salaries, consulting fees, and book royalties, plus the monetary equivalent of the pride and joy that the faculty member and his or her family would get from being tenured at St. Anford. Anyone denied tenure at St. Anford will get a faculty position at Boondocks College, and the present value of that career is \$1 million. Your faculty can do research and publish the findings. But each publication requires effort and time and causes strain on the family; all these are costly to the faculty member. The monetary equivalent of this cost is \$25,000 per publication for a Brilliant Assistant Professor and \$50,000 per publication for a Good one. You can set a minimum number, N , of publications that an Assistant Professor must produce in order to achieve tenure.

- 3

Baysian Games: Consider a Wild West shootout between Earp and the Stranger. With probability .75, the Stranger is a Gunslinger type and the table shows Earp's and the Stranger's payoffs

		Gunslinger Stranger	
		Draw	Wait
Earp	Draw	2, 3	3, 1
	Wait	1, 4	8, 2

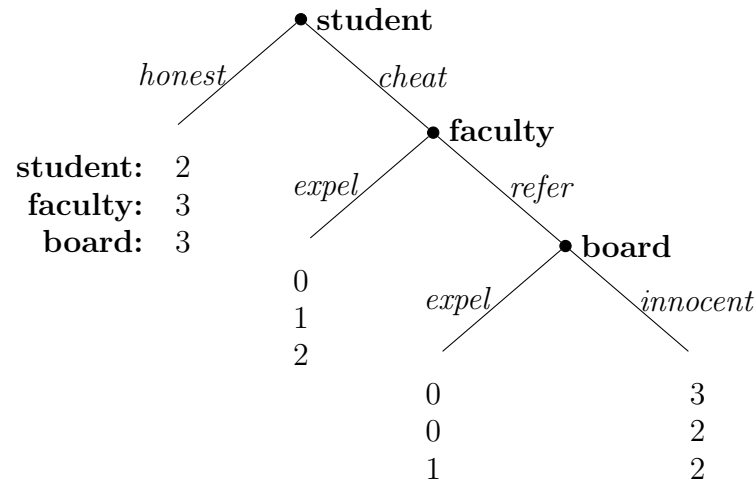
But with probability .25, the Stranger is a Cowpoke type and the table shows Earp's and the Stranger's payoffs

		Cowpoke Stranger	
		Draw	Wait
Earp	Draw	5, 2	4, 1
	Wait	6, 3	8, 4

- (4 P.) What is the Nash equilibrium **when the Stranger is always a Gunslinger**?
- (4 P.) What is the Nash equilibrium **when the Stranger is always a Cowpoke**?
- (4 P.) What is the Nash equilibrium when Earp believes the Stranger is a **Gunslinger with probability 0.75**?
- (4 P.) Consider a strategic move variation where the Gunslinger can commit to only playing Wait before Nature has assigned them a type.
Is this type of commitment *credible*? Why or why not?

Question 4. (12 P.)

Bayesian Game: Consider a situation in which a student can decide to cheat or be honest on an exam. If the faculty thinks the student has cheated, the faculty member has to decide whether to expel them from the college or refer them to the Honor Board. The Honor Board has to decide whether to expel the student or find them innocent. The payoffs are ordered, student, faculty, and college. Assume the board shares the college's payoffs.



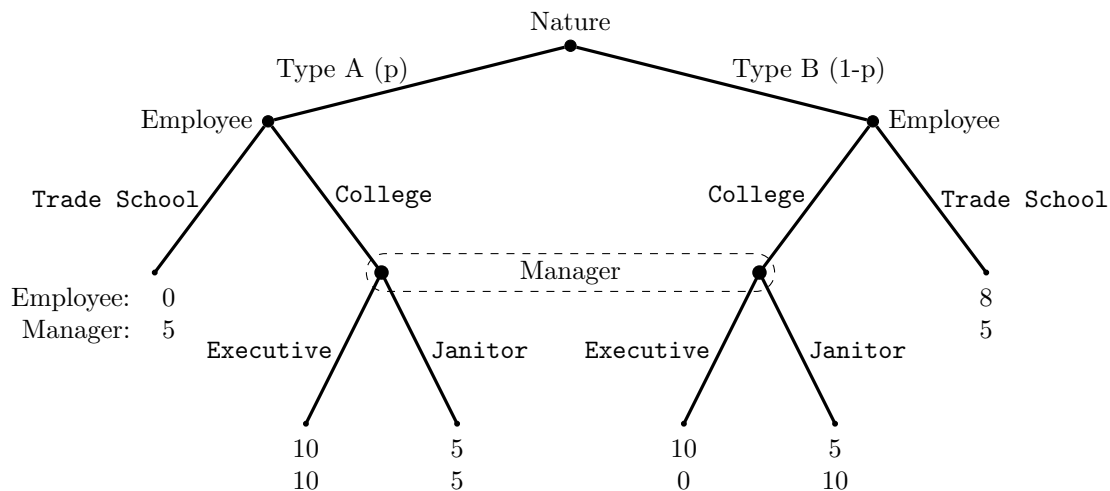
- a) (4 P.) Find the Subgame Perfect Nash Equilibrium.

- b) (4 P.) Assume now that the board acts like *Nature*, making no deliberate choice but instead expels a guilty student $q\%$ of the time. Solve for the range of q such that the student chooses *honest* in the SPNE.

- c) (4 P.) Relative to the pure threat of expulsion alone, who gains and who loses from the existence of an honor board that expels probabilistically?

Question 5. (16 P.)

Signaling: Consider a Bayesian game where Nature determines whether an employee is an A type and more suited for executive roles or a B type who are more suited for janitorial work. The Manager cannot observe the hidden type of an employee, but employees may choose to go to college or not. The extensive form game is shown below:



- a) (4 P.) Suppose that $p = 3/4$. Suppose that the Manager's pure strategy is to always hire College grads as *Executives*. Solve for the Subgame-perfect Bayes-Nash Equilibrium (SPBNE). Is this a *separating* or a *pooling* equilibrium?

- b) (4 P.) Suppose that $p = 3/4$. Is there a *separating equilibrium* in pure strategies where all A types go to college, and all B types go to trade schools?

- c) (4 P.) Suppose that now $p = 2/3$ so that Managers are indifferent between hiring a random employee as a **Executive** or as a **Janitor**.
Define mixed strategies for both players and use them to solve for a *semi-separating* equilibrium.

- d) (4 P.) What is the *signalling* value of an employee choosing **College**? Use Bayes rule to compare the ex-ante probability $p = 2/3$ of a Type A to the updated belief of a Manager as to the Employee being Type A conditional on observing college in the semi-separating equilibrium in part (c).

Question 6. (16 P.)

Repeated Games: Consider the strategic form game below:

		Column	
		Cooperate	Defect
Row	Cooperate	8 , 8	0, 10
	Defect	10 , 0	3 , 3

- a) (4 P.) What will happen when this game is a *one-shot* game and neither player can make any strategic moves?
- b) (2 P.) Will this outcome be *Pareto optimal*?
- c) (4 P.) What could you change about the structure of this game to ensure that a socially optimal outcome will be reached in equilibrium?
- d) (6 P.) Suppose that both players have a *discount factor* of $\delta = 3/4$. Can a strategy profile of both players using *grim trigger* strategies be sustained in the game where the strategic form game above is repeated infinitely?
Show all calculations and explain your answer.