

# Introduction to Game Theory

## General Principles

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# Outline

- Introductions
- What is EC327?
  - Syllabus
  - Schedule & Assignments
  - Office Hours
- What is Game Theory?
  - What are strategic games?
  - How can we classify games?

# Introductions

# Welcome to the Class!

## About Me:

- **Preferred Name:** Dante
- **Preferred Pronouns:** he, him
- 4th year Econ Phd student
- Davis, CA -> Portland, OR -> Eugene, OR

# Introduce Yourselves

## IntroQuiz

- Your preferred name, pronouns; to help me get to know you
- Why did you choose this class?
- Song recommendation for class playlist

# What is EC327?

# Syllabus Document

- Most up to date version on github
- I will also upload to Canvas
- print, sign, and upload as your first assignment

# Class Expectations

## Prerequisites

- **Courses:** EC201 or EC202
- **Knowledge:** This class will require you to use some graphing skills. If you felt uncomfortable with the EC201, I recommend that you review how to solve equations, inequalities, and fractions.
  - There are great free resources out there like Khan Academy. You can always feel free to reach out for help or other resources.

# Student Expectations

- **Come to class**

- Pay attention to lectures, take notes, review to...
- Participate in group work & activities
- **Ask questions!**

- **Read the textbook**

- **Communicate respectfully**

- With your classmates
- With me & grader

- **Have academic integrity**<sup>1</sup>

- Verify that all submitted work is your own
- Provide sources for *all* information that you fo...

# Instructor Expectations

- **Provide course material**
  - Slides will be updated on github
  - I will also try to post them on Canvas, but not all
  - Assignments posted on Canvas w/ due dates,
- **Face-to-face Interaction**
  - **Classes**
    - Ask me to clarify if something doesn't make sense
    - Ask me to slow down if I'm going too fast
  - **Office Hours**
    - Use them!!

# Admin Stuff

## Problem Sets

You will practice what we learn in class on independent problem sets.

Each homework assignment will include a few problems that are similar to what you will see on exams.

- Learning something new takes practice, so these assignments help you keep up with the concepts
- You will be graded not only on whether you got the right answer, but also more importantly on how you communicate your work.
  - See Canvas rubric for more info

# Class Activities

- Sometimes I will ask you to play the types of games in lectures
  - Record the strategies you chose and the outcome
  - Reflect on how you played the game
  - Relate it to lecture concepts

# Exams

You will demonstrate how well you understand course material through  
a **midterm** and a **final** exam

- **Midterm**

- sometime around week 5 (Oct. 28th or 30th)
- Will test you on definitions, solution concepts, and critical thinking problems

- **Final**

- finals week of December 9 (check duckweb for details)
- Covers everything we learned in the quarter, with some concepts from the 2nd half

# Grading

<b>Problem Sets</b>	30%
<b>In-class Activities</b>	10%
<b>Midterm</b>	30%
<b>Final</b>	30%

# Policies

- **No make-up exams!**
  - if you absolutely cannot attend midterm, you final exam
- Problem set keys posted automatically after deadline
  - -> no late submissions accepted



# University Policies

# Campus Resources

- **Accessible Education Center**
  - [aec.uoregon.edu](http://aec.uoregon.edu)
- **Support for victims of assault, harassment, stalking, and discrimination**
  - [safe.uoregon.edu](http://safe.uoregon.edu)
  - 24/7 hotline: (+1) 541-346-SAFE (7244)
- **Health and Wellbeing**
  - University Counseling Services
  - Basic Needs Program
- **Religious Observance Accommodations**
  - Provost website

# Course Pages

<https://canvas.uoregon.edu/courses/251353> - submit assignments  
check deadlines

[github.com/dyasui/EC327](https://github.com/dyasui/EC327) - Find up-to-date version of assignments - *let me know if links are broken*

# What is Game Theory

# Motivation

What is the goal of **Game Theory**?

To understand social behavior

Why do economists study Game Theory?

We are *social* scientists

To make models, predictions, hypotheses, etc. of research

# Motivation

Why should **you** study game theory?

Practice your strategic decision-making in a safe environment.

Develop your intuition for social interactions in a structured way.

Feed your curiosity for economics, social science, and business questions!

# What is theory?

What is the point of *theory*?

**Simplify complex systems** - understanding one easier than trying to

**Generate *falsifiable* hypotheses** - good economy  
good theory

# Theory in a data-driven world?

“The theory of economics does not furnish a body of conclusions immediately applicable to policy. It is rather a method of approaching certain complex economic problems, one which helps its possessor to draw correct conclusions.”

# What are the limits to theory?

- Our models will never be perfect representation
- But we should know how well they *approximate* what we want to understand
- Theory is very useful for generating *falsifiable hypotheses* which can then be used to guide experimental or statistical analysis
- As we play games in class, we will observe the difference between our theoretical predictions

# What is a *game* of strategy?

Game theory: It's not all fun and games!

# Examples of strategic games:

Where in the goal should you kick a penalty shot?



# Examples of *strategic games*:

Where in the goal should you kick a penalty shot?

- Left, Right, Center? Up or Down?
- Is there one best place to kick?
- What if you always choose top right corner?
- Besides soccer;
  - Which offensive play in football?
  - Where to serve in a tennis court?

# Examples of *strategic games*:

If 100% of your grade in this class is decided by a class average, should you study?

- If you can all agree to take a chill quarter and not study, will everyone get A's?
- But what if there's at least one try-hard?
- Now how much should you study, even if you already know you won't?
- Do you think everyone else will keep their promise?

# Examples of *strategic games*:

Should you give an engagement ring to the person

- Why buy an expensive trinket when you could save a house, etc?
- Does it matter if your recently engaged friends give engagement rings?
- Does your paycheck vs. how much your fiancee receives matter?

# Examples of *strategic games*:

In economics, why do we say there is a **law of one**

Imagine I set up a competing Starbucks franchise

- If they sell PSL for \$6.50, what happens if I sell the same?
- What if I sell for \$6.51?

This has been your EC201 review!

# Examples of *strategic games*:

Should the US try to defeat its rivals through global war?

- Why did the US and USSR amass massive nuclear arsenals?
- Why has a nuclear weapon never been used in a war?
- Are anti-ballistic missiles destabilizing to international relations?

'GAMES' REFERS TO MODELS, SIMULATIONS AND COMPUTER PROGRAMS WHICH HAVE TACTICAL AND STRATEGIC APPLICATIONS

#### List Games

FALKEN'S MAZE

BLACK JACK

GIN RUMMY

HEARTS

BRIDGE

CHECKERS

CHESS

POKER

FIGHTER COMBAT

GUERRILLA ENGAGEMENT

DESERT WARFARE

AIR-TO-GROUND ACTIONS

THEATERWIDE TACTICAL WARFARE

THEATERWIDE BIOTOXIC AND CHEMICAL WARFARE

GLOBAL THERMONUCLEAR WAR



# Examples of *strategic games*:

What do these examples have in common?

# What is a Game? Def

# What do all these questions have in common?

- They all involve people making choices which depend on the actions of others
- In other words, they are questions of **strategy**:

**Strategic interdependence** is present in a social situation if what is best for someone *depends* on what someone else does.

# A definition of a game<sup>1</sup>

A **Game** consists of:

- a collection of decision-makers, called **players**;
- the set of **information** available to each player;
- the **strategies** available to each player in each information set;
- a mapping from the intersection strategies of all players to payoffs;
- **preferences** of the individual players over all possible payoffs.

# Who are the players

# What defines a player?

- **Preferences:** Everyone has certain things they want.  
But you usually can't get everything you want; economic  
*constrained choices.*  
So its important to have priorities and to understand  
why people prefer to others.
- **Information:** Some people might be better informed than others.
- **Beliefs:** What do I think about when I have to make decisions?

# Preferences

**Preferences** describe the subjective ranking that we make among alternatives.

For example, on the set of Eugene boba stores, my ranking goes like this;

1. Day & Night - they have mango sago, cute location
2. Tea 4 - major chain, good quality and selection
3. Bobahead - no more campus location 😞
4. No boba
5. Rabbit Hole - no hate, just not for me

# Rational Preferences

The **rational model** of choice is the foundation of ...  
Its assumptions are that:

- People have **complete preferences**
  - for every pair of options, you can either tell me that you prefer one or that you are *indifferent*
  - for any pair of deserts,  $\{ \text{ice cream}, \text{donut} \}$ , either  $(\text{ice cream} > \text{donut})$  or  $(\text{ice cream} \sim \text{donut})$
- Preferences are **transitive**
  - if  $(\text{coffee} > \text{green tea})$  and  $(\text{green tea} > \text{soy milk})$ , then  $(\text{coffee} > \text{soy milk})$   
 $\{ \text{coffee}, \text{green tea}, \text{soy milk} \} \in \text{transitive}$

# Rational Preferences (cont.)

Another key assumption of rationality is that we can represent preferences by real numbers.

A **utility function** maps a choice to a single number.

For example, let  $u(\cdot)$  be the utility function from earlier.

- I can have  $u(\text{🍺}) = 5, u(\text{🍔}) = 10, u(\text{🤸}) = 25$
- I can also have  $u(\text{🍺}, \text{🍔}) = 20, u(\text{🍺}, \text{🍔}, \text{🤸}) = 30$

# Ordinal vs. Cardinal numbers

- **Cardinal:** amounts which can be measured in *magnitude*  
▪ examples: \$9.99, 80 students, 50:50 odds
- **Ordinal:** all that matters is the *relative ranking*  
▪ examples: utility; what does 100 utility mean?

# Don't worry!

- For this class, you won't need to worry about utility (if you want to, take EC311).
- I will almost always give you specific values of utility functions, called **payoffs**.
- The table on the previous page is a good example.

# Payoffs

What is a player's goal in a game?

To maximize their expected **payoff**

- A payoff can represent many things.
- But for simplicity we will abstract them down to value.
- A payoff doesn't need to be abstract; it could be

# Payoffs

What is true of payoffs?

Higher numbers are more preferred

They are **Ordinal**; i.e., the relative units don't matter

They capture *everything* in a game that a player cares about

# *Strategic Choice* vs. other types

- Economics is the study of **constrained choice**; in the *utility maximization problem* as the workhorse
  - These types of problems usually only involve one consumer, who is only constrained by their budget
- We use the term **strategic games** to distinguish agent optimization problems
- A **game** is a type of problem featuring multiple agents in which their optimal choice **depends on the other players**.

# State-dependent utility table

- Sometimes my enjoyment of a thing depends on  
socially-dependent preferences

My choice	My friends' choice	M
Duck's game	Duck's game	3
Duck's game	Stay home	2
Stay home	Duck's game	1
Stay home	Stay home	2

- Is this an example of a **strategic** or **non-strategic** game?

# Common Knowledge

Our theories will have to make assumptions about  
All of our games will at least assume that **all players know the rules.**

# Rules of the Game

We will assume that all players know:

- Who else is playing,
- all of the strategies each player could *potentially* choose,
- everyone's payoffs for all possible combinations of players,
- and that everyone else is maximizing their payoff.

# Taxonomy of Games

# General Categorical Terms

- **Sequential** or **Simultaneous**?
- **Zero-sum** or not
- **Perfect** or **Imperfect** information?
  - is info **symmetric** or **asymmetric**?
- **One-shot** or **Repeated**?
- ‘**Noncooperative**’ or ‘**Cooperative**’?

# Sequential vs. Simultaneous

## **Sequential** Games

- players make their moves one after the other
- **Chapter 3**
- **Visual tool:** *game trees*
- **Solution Method:** *backwards induction*

...

## **Simultaneous** Games

- players make their moves at the same time
- **Chapter** 4 & 5
- **Visual tool:** *payoff tables*
- **Solution Method:** *best responses, deletion of dominated strats*

# Sequential Games

In **sequential** games, you have to think about how affect what your opponent will do in the **future**.

...

This hierarchy of thinking will make these types easier for us to think through, so they will be our games.

...

- We'll see that sometimes **moving first** can be ad
- ...
- While other times it's best to **wait and see** what

# Simultaneous Games

In **simultaneous** games, you have to figure out what your opponent is thinking about what your opponent is thinking you

...

This circular thinking can get confusing, so we'll learn new methods for organizing these games in chapter 2.

# Conflicting vs. Common Interests

Many games you are familiar with have distinct winners and losers.  
But in other types of games, it's possible for everyone to win ahead.

# Zero-sum (or constant-sum) Games

When the *total payoffs of all players sum to 0*<sup>1</sup>

- i.e, one player's gain is another player's loss
- Examples: NCAA Football Championship, Scrabble (technically constant-sum)

Not all games are fixed or zero sum;

- Examples: Hiring a tutor (mutual gains), International trade

# Are strategic interactions Repeated?

A **one-shot** game is played only once by the same players.

- If you've never played against someone before, you have **beliefs** about them
- Secrecy or surprise are potentially good strategies

A game is called **repeated** if the same players play many times.

- If you know your opponent, then your **reputation** matters. You want to cooperate

# Full or Equal Information

How much does each player know when they decide?

- **Perfect Information:** when players know all previous moves and external circumstances
  - players may have **imperfect info**; uncertainty about the world, previous' moves, or other player's 'type'
- **Asymmetric Info:** when one player has access to information that other players do not
  - Examples: hand in poker, used car salesmen
  - Topics: Signaling, Screening

# Can agreements be Enforced?

- Self-interest and common good can often conflict
- In these situations, players need to form agreements to achieve cooperative outcomes.

But can people actually be held to those agreements?

For example:

- Paris Climate accords; who polices nation-state's actions?
- Public goods; why do we need the Internal Revenue Service?

# Can agreements be Enforced?

Two broad categories of the field are **cooperative** game theory and **noncooperative** game theory<sup>1</sup>

**Cooperative** games are those in which agreements can be enforced

In **Noncooperative** games, no-one can be forced to keep their own self-interest

# Tentative Schedule

<b>Week</b>	<b>Chapter(s)</b>	<b>Topic</b>
1	1, 2	Intro & General Principles
2	3	Sequential Move Games
3	4	Simultaneous Move Games
4	6	Combining Sequential and S
5	6	Review & <b>Midterm</b>
6	5	Simultaneous Games: Conti Discussion, and Evidence
7	7	Mixed Strategies
8	8	Strategic Moves
9	9	Uncertainty and Information

<b>Week</b>	<b>Chapter(s)</b>	<b>Topic</b>
10	10	Repeated Games
<i>Finals</i>	<i>TBA</i>	<i>Exam</i>