

# Uncertainty & Information Topics

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EC327 Game Theory

# Outline

Topics and Definitions

Cheap Talk

Adverse Selection

# Topics and Definitions

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# What is Asymmetric Info?

- We already learned about *symmetric* uncertainty in the models where Nature makes a play that *neither* player can observe.
- But sometimes one player will know some things that other do not.

## Asymmetric Information

describes situations in which some players have **private information** that is not accessible to other players.

# What is Asymmetric Info?

If you are **better informed** than others:

- You might be able to *conceal* or *reveal misleading* information strategically in order to manipulate the beliefs of others about you
- You might instead want to *selectively reveal* the truth if it helps you.

If you are **less informed** than other players:

- You might want to *filter out the truth* from lies or misinformation.
- You could instead strategically *remain ignorant* in order to claim "credible deniability".

## Cheap Talk

I could let people in on my private info by directly talking to them. But if they know that I have potential incentives to *lie*, they might not believe my *cheap talk*.

*Actions Speak Louder Than Words*

# Behaviors in Asymmetric Info Games

## Signaling

When I know something about myself that would benefit me if *others* knew, I might send a **signal** through my actions

Examples:

- A 4.0 GPA might signal to potential employers that you are hard-working.
- If you're in the market for a product and you're uncertain of its quality, a money-back guarantee might *signal* that it works.

# Behaviors in Asymmetric Info Games

## Screening

When I want to know something about *someone else's* private info, I might get them to take an action that would **screen** out people of different *types*.

Examples:

- An employer might not know if a job candidate is a *lazy* or *industrious* type of worker, but they could try to screen out the *lazy* ones by requiring a portfolio of previous work.



# Effectiveness of Different Communication Strategies

When are different strategies effective in actually revealing private info?

- Sometimes direct communication works when players' interests align. But trust might break down when there are incentives to send false messages.
- A signal is only effective if not all types take the same action. We'll discuss breakdowns in signaling using the ideas of **Separating** vs **Pooling** equilibria

# Asymmetric Info in Market Games

- In 201 or 311 you may have learned about the **perfectly competitive** markets model.
- One of the assumptions of that model is **perfect information**.
- When this assumption breaks, we might see **Adverse Selection** or other types of market failures.

## Cheap Talk

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## Cheap Talk Equilibrium - When Interests Align

Suppose that I want to meet up with Jose at a coffee shop on campus.

		Jose	
		<i>Starbucks</i>	<i>Roma</i>
Dante	<i>Starbucks</i>	1, 1	0, 0
	<i>Roma</i>	0, 0	2, 2

We'll also add a first stage to this game where Dante can send Jose a text message saying either "I'm going to Starbucks" or "I'm going to Roma".

## Cheap Talk Equilibria - When Interests Align

The strategy profile where:

- I send the message "going to Starbucks"
- we both go to Starbucks if I send "going to Starbucks"
- or both go to Roma if I send "going to Roma"

is a **Nash Equilibrium** (specifically a subgame perfect NE).

- We'll call this a "cheap talk" equilibrium because it was in my best interest to communicate my actual strategy.
- It cost me nothing to send a *message*.

## Cheap Talk vs Babbling Equilibrium

However, this is not the only SPNE of this game. If are strategy profiles in the second stage are:

- Jose will go to Starbucks no matter what message Dante sends
- Dante will go to Starbucks no matter what message he sent

Then Dante will be indifferent between sending either message in the first place.

- We'll call this a "**babbling**" **equilibrium** because the initial message sends *no* information about what I will actually do.
- This equilibrium seems unlikely, but if I have an existing *reputation* for always going to Starbucks, this would be plausible and completely rational behavior.

## Cheap Talk Equilibria - When Interests are Conflicting

What about a zero-sum game?

		Navratilova	
		<i>DL</i>	<i>CC</i>
Evert	<i>DL</i>	50, 50	80, 20
	<i>CC</i>	90, 10	20, 80

- Should Navratilova believe what Evert says she will do?
- Should Navratilova believe that Evert will do *exactly the opposite* of what she says she'll do?

## Cheap Talk Equilibria - When Interests are Conflicting

What about a zero-sum game?

		Navratilova	
		<i>DL</i>	<i>CC</i>
Evert	<i>DL</i>	50, 50	80, 20
	<i>CC</i>	90, 10	20, 80

- The only equilibrium of this game is a **babbling** equilibrium.
- There is no message that Evert could send that would give Navratilova any more idea of what she will actually play.



## Cheap Talk Equilibria - Partially Aligned Interests

Many real life games have mixtures of conflict and common interest.

- The question of whether direct communication is *credible* or not will depend on the relative degree of each incentive.
- We will use our tools from the first half of the course to make testable predictions based on different ranges of assumptions.

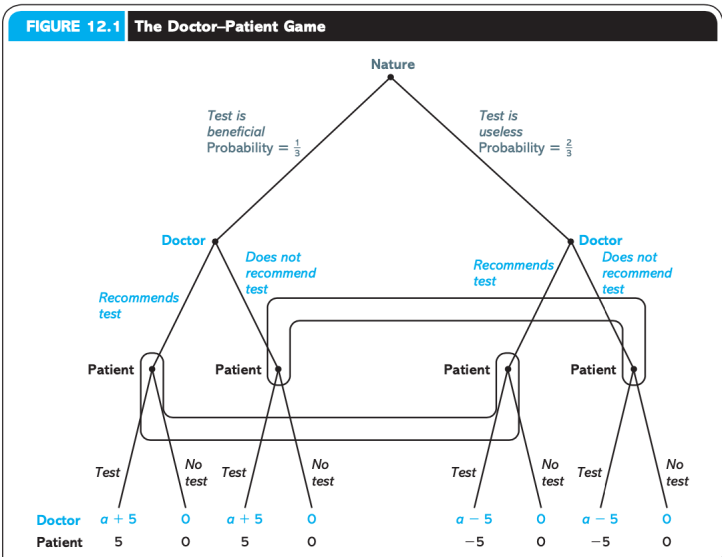
*In a recent survey of physicians, 93% reported altering their clinical behavior because of the threat of malpractice liability. Of them, 92% used “assurance behavior” such as ordering tests, performing diagnostic procedures, and referring patients for consultation; and 43% reported using imaging technology in clinically unnecessary circumstances.*

Harrington, pg. 461

# Defensive Medicine

- Consider a patient who goes to the doctor for an examination.
- The doctor can recommend an expensive test that is not fully covered by the patient's insurance.
- The doctor cares about the patient, but also doesn't want to be sued for malpractice if the patient *does* end up needing the test and the doctor didn't recommend it.
- The patients value  $v$  from a beneficial test is 5, and  $v = -5$  if the test is useless.
- We'll use  $a$  to stand in for the value of a test to a doctor from a malpractice standpoint.

**FIGURE 12.1** The Doctor–Patient Game



## Pooling Equilibrium

- Doctor's Strategy: Recommend the test whether or not it is beneficial.
  - Patient's Strategy: Ignore the doctor's recommendation.
  - Patient's Beliefs: Ignoring the doctors advice, the probability the test is effective is  $1/3$ .
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- This equilibrium is a *babbling equilibrium*.
  - The doctor's recommendation contains no real signal to the patient.

# Defensive Medicine - Babbling Strategy

## Pooling Equilibrium

- Doctor's Strategy: Recommend the test whether or not it is beneficial.
  - Patient's Strategy: Ignore the doctor's recommendation.
  - Patient's Beliefs: Ignoring the doctors advice, the probability the test is effective is  $1/3$ .
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- The patient's beliefs are consistent, and their expected utility from taking the test is  $\frac{1}{3} \cdot 5 + \frac{2}{3} \cdot (-5) = -\frac{5}{3}$ .
  - Given that the patient will never take the test, the doctor is indifferent between recommending the test or not.
  - So this situation in which the doctor always recommends the test and the patient always ignores their advice is *stable*.

The previous result was disappointing, but not unexpected.

### Insight

For every cheap talk game, there is always a babbling equilibrium.

- But let's now focus on the more interesting question of how to make the doctor's recommendation *meaningful*.

# Defensive Medicine - Separating Strategies

Consider the following strategy profile:

- Doctor's Strategy: Recommend the test if and only if it is beneficial.
- Patient's Strategy: Follow the doctor's recommendation.
- Patient's Beliefs:
  - If the doctor recommends the test, then the test is beneficial with 100% probability.
  - If the doctor does not recommend the test, then the test is beneficial with 0% probability.



## Defensive Medicine - Separating Strategies

When will the doctor follow the separating strategy?

1. When  $EU_d(\text{Rec. when beneficial}, (T, NT)) \geq EU_d(\text{Don't rec. when beneficial}, (T, NT))$
2. and when  $EU_d(\text{Don't rec. when useless}, (T, NT)) \geq EU_d(\text{Rec. when useless}, (T, NT))$

Solve for the range of  $a$  where this is a NE.

Interpreting our findings:

- When  $a = 0$ , the doctor's interests are *perfectly* aligned with the patient's.
- When  $a \leq 5$ , the doctor's interests are *partially* aligned with the patient's interests, and there is an equilibrium where the doctor gives truthful recommendations.
- When  $a > 5$ , there is only a babbling equilibrium because the doctor's incentives are to not be truthful. Even if they did give a truthful recommendation, the patient would have no reason to believe it would be *credible*.

# Defensive Medicine - Conclusions

Connecting with our real-world observations:

- We don't know what doctors' subjective costs of malpractice threats are ( $a$ ).
- But we can observe their *behaviors*.
- If we see that doctors recommend more tests than are beneficial, it might reveal that  $a$  is quite large.

## Revealed Preference

The idea that people reveal their true preferences by the choices they make.

# Adverse Selection

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