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## moneyiness == 0 二阶导数不连续

left parabolic ---  $dc < x \leq 0$

$$\text{In}[1]:= w[x_] = vc + sc * x + pc * x^2$$

$$\text{Out}[1]= vc + sc x + pc x^2$$

$$\text{In}[2]:= w'[x]$$

$$\text{Out}[2]= sc + 2 pc x$$

$$\text{In}[3]:= w''[x]$$

$$\text{Out}[3]= 2 pc$$

right parabolic ---  $0 < x \leq uc$

$$\text{In}[4]:= w[x_] = vc + sc * x + cc * x^2$$

$$\text{Out}[4]= vc + sc x + cc x^2$$

$$\text{In}[5]:= w'[x]$$

$$\text{Out}[5]= sc + 2 cc x$$

$$\text{In}[6]:= w''[x]$$

$$\text{Out}[6]= 2 cc$$

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## moneyiness == dc 二阶导数不连续

$$\text{In}[1]:= w[x_] = vc + sc * x + pc * x^2$$

$$\text{Out}[1]= vc + sc x + pc x^2$$

$$\text{In}[2]:= w[dc]$$

$$\text{Out}[2]= dc^2 pc + dc sc + vc$$

$$\text{In}[3]:= w'[x]$$

$$\text{Out}[3]= sc + 2 pc x$$

$$\text{In}[4]:= w'[dc]$$

$$\text{Out}[4]= 2 dc pc + sc$$

$$\text{In}[5]:= w''[x]$$

$$\text{Out}[5]= 2 pc$$

$$\text{In[6]}:= w[x_] = vc - \left(1 + \frac{1}{dsm}\right) * pc * dc^2 - \frac{sc * dc}{2 * dsm} +$$

$$\left(1 + \frac{1}{dsm}\right) * (2 * pc * dc + sc) * x - \left(\frac{pc}{dsm} + \frac{sc}{2 * dc * dsm}\right) * x^2$$

$$\text{Out[6]}= -dc^2 \left(1 + \frac{1}{dsm}\right) pc - \frac{dc sc}{2 dsm} + vc + \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) x - \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x^2$$

$$\text{In[7]}:= w[dc]$$

$$\text{Out[7]}= -dc^2 \left(1 + \frac{1}{dsm}\right) pc - \frac{dc sc}{2 dsm} + dc \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - dc^2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) + vc$$

$$\text{In[8]}:= \text{Simplify[}$$

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$$-dc^2 \left(1 + \frac{1}{dsm}\right) pc - \frac{dc sc}{2 dsm} + dc \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - dc^2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) + vc]$$

$$\text{Out[8]}= dc^2 pc + dc sc + vc$$

$$\text{In[9]}:= w'[x]$$

$$\text{Out[9]}= \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - 2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x$$

$$\text{In[10]}:= w'[dc]$$

$$\text{Out[10]}= \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - 2 dc \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right)$$

$$\text{In[11]}:= \text{Simplify}\left[\left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - 2 dc \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right)\right]$$

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$$\text{Out[11]}= 2 dc pc + sc$$

$$\text{In[35]}:=$$

$$\text{In[12]}:= w''[x]$$

$$\text{Out[12]}= -2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right)$$

$$\text{In[13]}:= w''[dc]$$

$$\text{Out[13]}= -2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right)$$

$$\text{In[14]}:= \text{Simplify}\left[-2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right)\right]$$

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$$\text{Out[14]}= -\frac{2 dc pc + sc}{dc dsm}$$

$$\text{In[15]}:= sc + 2 pc x == \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - 2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x$$

$$\text{Out[15]}= sc + 2 pc x == \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - 2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x$$

In[16]:= **Solve** $\left[sc + 2\ pc\ x == \left(1 + \frac{1}{dsm}\right) (2\ dc\ pc + sc) - 2\left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) x, \{x\}\right]$   
 解方程

Out[16]=  $\{\{x \rightarrow dc\}\}$

In[17]:=  $-2\left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) == 2\ pc$

Out[17]=  $-2\left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) == 2\ pc$

In[18]:= **Solve** $\left[-2\left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) == 2\ pc, \{dc, dsm, pc, sc\}\right]$   
 解方程

Out[18]=  $\{\{sc \rightarrow -2\ (dc\ pc + dc\ dsm\ pc)\}\}$

In[19]:= **FindInstance** $\left[-2\left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) == 2\ pc, \{dc, dsm, pc, sc\}\right]$   
 求解

Out[19]=  $\{\{dc \rightarrow -6, dsm \rightarrow -6, pc \rightarrow \frac{1}{15}, sc \rightarrow -4\}\}$

**moneyiness == dc(1+dsm)**

In[1]:=  $w[x_] = vc - \left(1 + \frac{1}{dsm}\right) * pc * dc^2 - \frac{sc * dc}{2 * dsm} +$   
 $\left(1 + \frac{1}{dsm}\right) * (2 * pc * dc + sc) * x - \left(\frac{pc}{dsm} + \frac{sc}{2 * dc * dsm}\right) * x^2$

Out[1]=  $-dc^2\left(1 + \frac{1}{dsm}\right) pc - \frac{dc\ sc}{2\ dsm} + vc + \left(1 + \frac{1}{dsm}\right) (2\ dc\ pc + sc) x - \left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) x^2$

In[2]:= **w** $[dc\ (1 + dsm)]$

Out[2]=  $-dc^2\left(1 + \frac{1}{dsm}\right) pc - \frac{dc\ sc}{2\ dsm} +$   
 $dc\left(1 + \frac{1}{dsm}\right) (1 + dsm) (2\ dc\ pc + sc) - dc^2 (1 + dsm)^2 \left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) + vc$

In[3]:= **Simplify** $\left[-dc^2\left(1 + \frac{1}{dsm}\right) pc - \frac{dc\ sc}{2\ dsm} +$   
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$dc\left(1 + \frac{1}{dsm}\right) (1 + dsm) (2\ dc\ pc + sc) - dc^2 (1 + dsm)^2 \left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) + vc]$

Out[3]=  $dc^2 (1 + dsm) pc + \frac{1}{2} dc (2 + dsm) sc + vc$

In[4]:= **w'** $[x]$

Out[4]=  $\left(1 + \frac{1}{dsm}\right) (2\ dc\ pc + sc) - 2\left(\frac{pc}{dsm} + \frac{sc}{2\ dc\ dsm}\right) x$

In[5]:= **Simplify**[ $\left(1 + \frac{1}{\text{dsm}}\right) (2 \text{ dc pc} + \text{sc}) - 2 \left(\frac{\text{pc}}{\text{dsm}} + \frac{\text{sc}}{2 \text{ dc dsm}}\right) x]$   
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Out[5]= 
$$\frac{(2 \text{ dc pc} + \text{sc}) (\text{dc} + \text{dc dsm} - x)}{\text{dc dsm}}$$

In[6]:= **w'**[**dc** (**1 + dsm**) ]

Out[6]= 
$$\left(1 + \frac{1}{\text{dsm}}\right) (2 \text{ dc pc} + \text{sc}) - 2 \text{ dc} (1 + \text{dsm}) \left(\frac{\text{pc}}{\text{dsm}} + \frac{\text{sc}}{2 \text{ dc dsm}}\right)$$

In[7]:= **Simplify**[ $\left(1 + \frac{1}{\text{dsm}}\right) (2 \text{ dc pc} + \text{sc}) - 2 \text{ dc} (1 + \text{dsm}) \left(\frac{\text{pc}}{\text{dsm}} + \frac{\text{sc}}{2 \text{ dc dsm}}\right)$ ]  
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Out[7]= 0

In[8]:= **w''**[**x**]

Out[8]= 
$$-2 \left(\frac{\text{pc}}{\text{dsm}} + \frac{\text{sc}}{2 \text{ dc dsm}}\right)$$

In[9]:= **w''**[**dc** (**1 + dsm**) ]

Out[9]= 
$$-2 \left(\frac{\text{pc}}{\text{dsm}} + \frac{\text{sc}}{2 \text{ dc dsm}}\right)$$

In[10]:= **Simplify**[ $-2 \left(\frac{\text{pc}}{\text{dsm}} + \frac{\text{sc}}{2 \text{ dc dsm}}\right)$ ]  
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Out[10]= 
$$-\frac{2 \text{ dc pc} + \text{sc}}{\text{dc dsm}}$$

In[11]:= **w**[**x\_**] = **vc** + **dc** \* (**2 + dsm**) \* (**sc** / **2**) + (**1 + dsm**) \* **pc** \* **dc** ^ **2**

Out[11]= 
$$\text{dc}^2 (1 + \text{dsm}) \text{pc} + \frac{1}{2} \text{dc} (2 + \text{dsm}) \text{sc} + \text{vc}$$

In[12]:= **w'**[**x**]

Out[12]= 0

In[13]:= **w''**[**x**]

Out[13]= 0

