

left parabolic --- $dc < x \leq 0$

$$In[1] := w[x_] = vc + sc * x + pc * x^2$$

$$Out[1] = vc + sc x + pc x^2$$

$$In[2] := g[x_] = \left(1 - \frac{x * w'[x]}{2 * w[x]}\right)^2 - \frac{w'[x]^2}{4} * \left(\frac{1}{w[x]} + \frac{1}{4}\right) + \frac{w''[x]}{2}$$

$$Out[2] = pc - \frac{1}{4} (sc + 2 pc x)^2 \left(\frac{1}{4} + \frac{1}{vc + sc x + pc x^2}\right) + \left(1 - \frac{x (sc + 2 pc x)}{2 (vc + sc x + pc x^2)}\right)^2$$

$$In[3] := \text{Simplify}\left[pc - \frac{1}{4} (sc + 2 pc x)^2 \left(\frac{1}{4} + \frac{1}{vc + sc x + pc x^2}\right) + \left(1 - \frac{x (sc + 2 pc x)}{2 (vc + sc x + pc x^2)}\right)^2\right]$$

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$$Out[3] = pc + \frac{(2 vc + sc x)^2}{4 (vc + x (sc + pc x))^2} - \frac{1}{4} (sc + 2 pc x)^2 \left(\frac{1}{4} + \frac{1}{vc + x (sc + pc x)}\right)$$

right parabolic --- $0 < x \leq uc$

$$In[4] := w[x_] = vc + sc * x + cc * x^2$$

$$Out[4] = vc + sc x + cc x^2$$

$$In[5] := g[x_] = \left(1 - \frac{x * w'[x]}{2 * w[x]}\right)^2 - \frac{w'[x]^2}{4} * \left(\frac{1}{w[x]} + \frac{1}{4}\right) + \frac{w''[x]}{2}$$

$$Out[5] = cc - \frac{1}{4} (sc + 2 cc x)^2 \left(\frac{1}{4} + \frac{1}{vc + sc x + cc x^2}\right) + \left(1 - \frac{x (sc + 2 cc x)}{2 (vc + sc x + cc x^2)}\right)^2$$

$$In[6] := \text{Simplify}\left[cc - \frac{1}{4} (sc + 2 cc x)^2 \left(\frac{1}{4} + \frac{1}{vc + sc x + cc x^2}\right) + \left(1 - \frac{x (sc + 2 cc x)}{2 (vc + sc x + cc x^2)}\right)^2\right]$$

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$$Out[6] = cc + \frac{(2 vc + sc x)^2}{4 (vc + x (sc + cc x))^2} - \frac{1}{4} (sc + 2 cc x)^2 \left(\frac{1}{4} + \frac{1}{vc + x (sc + cc x)}\right)$$

left smoothing range --- $dc(1+dsm) < x \leq dc$

$$In[7] := w[x_] = vc - \left(1 + \frac{1}{dsm}\right) * pc * dc^2 - \frac{sc * dc}{2 * dsm} +$$

$$\left(1 + \frac{1}{dsm}\right) * (2 * pc * dc + sc) * x - \left(\frac{pc}{dsm} + \frac{sc}{2 * dc * dsm}\right) * x^2$$

$$Out[7] = -dc^2 \left(1 + \frac{1}{dsm}\right) pc - \frac{dc sc}{2 dsm} + vc + \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) x - \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x^2$$

$$\begin{aligned}
In[] := & \mathbf{g}[x_] = \left(1 - \frac{x * w'[x]}{2 * w[x]}\right)^2 - \frac{w'[x]^2}{4} * \left(\frac{1}{w[x]} + \frac{1}{4}\right) + \frac{w''[x]}{2} \\
Out[] := & -\frac{pc}{dsm} - \frac{sc}{2 dc dsm} - \frac{1}{4} \left(\left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - 2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x \right)^2 \\
& \left(\frac{1}{4} + \frac{1}{-dc^2 \left(1 + \frac{1}{dsm}\right) pc - \frac{dc sc}{2 dsm} + vc + \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) x - \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x^2} \right) + \\
& \left(1 - \frac{x \left(\left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) - 2 \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x \right)}{2 \left(-dc^2 \left(1 + \frac{1}{dsm}\right) pc - \frac{dc sc}{2 dsm} + vc + \left(1 + \frac{1}{dsm}\right) (2 dc pc + sc) x - \left(\frac{pc}{dsm} + \frac{sc}{2 dc dsm}\right) x^2 \right)} \right)^2
\end{aligned}$$

In[] := Simplify[%2]

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$$\begin{aligned}
Out[] := & -\frac{pc}{dsm} - \frac{sc}{2 dc dsm} + \\
& \left(dc^2 \left(-2 dc^2 \left(1 + dsm\right) pc - dc sc + 2 dsm vc + 2 dc \left(1 + dsm\right) pc x + sc x + dsm sc x \right)^2 \right) / \\
& \left(2 dc^3 \left(1 + dsm\right) pc + sc x^2 + dc^2 \left(sc - 4 \left(1 + dsm\right) pc x \right) - \right. \\
& \left. 2 dc \left(x \left(sc - pc x \right) + dsm \left(vc + sc x \right) \right) \right)^2 - \frac{1}{4 dc^2 dsm^2} \\
& \left(2 dc pc + sc \right)^2 \left(dc + dc dsm - x \right)^2 \left(\frac{1}{4} - \left(2 dc dsm \right) / \left(2 dc^3 \left(1 + dsm\right) pc + sc x^2 + \right. \right. \\
& \left. \left. dc^2 \left(sc - 4 \left(1 + dsm\right) pc x \right) - 2 dc \left(x \left(sc - pc x \right) + dsm \left(vc + sc x \right) \right) \right) \right)
\end{aligned}$$

right smoothing range --- uc<x<=uc(1+usm)

$$\begin{aligned}
In[] := & \mathbf{w}[x_] = vc - \left(1 + \frac{1}{usm}\right) * cc * uc^2 - \frac{sc * uc}{2 * usm} + \\
& \left(1 + \frac{1}{usm}\right) * (2 * cc * uc + sc) * x - \left(\frac{cc}{usm} + \frac{sc}{2 * uc * usm}\right) * x^2 \\
Out[] := & -cc uc^2 \left(1 + \frac{1}{usm}\right) - \frac{sc uc}{2 usm} + vc + (sc + 2 cc uc) \left(1 + \frac{1}{usm}\right) x - \left(\frac{cc}{usm} + \frac{sc}{2 uc usm}\right) x^2 \\
In[] := & \mathbf{g}[x_] = \left(1 - \frac{x * w'[x]}{2 * w[x]}\right)^2 - \frac{w'[x]^2}{4} * \left(\frac{1}{w[x]} + \frac{1}{4}\right) + \frac{w''[x]}{2} \\
Out[] := & -\frac{cc}{usm} - \frac{sc}{2 uc usm} - \frac{1}{4} \left((sc + 2 cc uc) \left(1 + \frac{1}{usm}\right) - 2 \left(\frac{cc}{usm} + \frac{sc}{2 uc usm}\right) x \right)^2 \\
& \left(\frac{1}{4} + \frac{1}{-cc uc^2 \left(1 + \frac{1}{usm}\right) - \frac{sc uc}{2 usm} + vc + (sc + 2 cc uc) \left(1 + \frac{1}{usm}\right) x - \left(\frac{cc}{usm} + \frac{sc}{2 uc usm}\right) x^2} \right) + \\
& \left(1 - \frac{x \left((sc + 2 cc uc) \left(1 + \frac{1}{usm}\right) - 2 \left(\frac{cc}{usm} + \frac{sc}{2 uc usm}\right) x \right)}{2 \left(-cc uc^2 \left(1 + \frac{1}{usm}\right) - \frac{sc uc}{2 usm} + vc + (sc + 2 cc uc) \left(1 + \frac{1}{usm}\right) x - \left(\frac{cc}{usm} + \frac{sc}{2 uc usm}\right) x^2 \right)} \right)^2
\end{aligned}$$

In[*]:= Simplify[%2]

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$$\text{Out[*]} = -\frac{cc}{usm} - \frac{sc}{2 uc usm} + \left(uc^2 (2 usm vc - 2 cc uc (1 + usm) (uc - x) + sc (-uc + x + usm x))^2 \right) /$$

$$\left(sc (uc^2 - 2 uc (1 + usm) x + x^2) + \right.$$

$$\left. 2 uc (-usm vc + cc (uc^2 (1 + usm) - 2 uc (1 + usm) x + x^2)) \right)^2 - \frac{1}{4 uc^2 usm^2}$$

$$\left(sc + 2 cc uc \right)^2 (uc + uc usm - x)^2 \left(\frac{1}{4} - (2 uc usm) / (sc (uc^2 - 2 uc (1 + usm) x + x^2) + \right.$$

$$\left. 2 uc (-usm vc + cc (uc^2 (1 + usm) - 2 uc (1 + usm) x + x^2)) \right) \right)$$

left constant level --- $x < dc(1 + dsm)$

$$\text{In[*]} := w[x_] = vc + dc * (2 + dsm) * (sc / 2) + (1 + dsm) * pc * dc^2$$

$$\text{Out[*]} := dc^2 (1 + dsm) pc + \frac{1}{2} dc (2 + dsm) sc + vc$$

$$\text{In[*]} := g[x_] = \left(1 - \frac{x * w'[x]}{2 * w[x]} \right)^2 - \frac{w'[x]^2}{4} * \left(\frac{1}{w[x]} + \frac{1}{4} \right) + \frac{w''[x]}{2}$$

$$\text{Out[*]} := 1$$

right constant level --- $uc(1 + usm) < x$

$$\text{In[*]} := w[x_] = vc + uc * (2 + usm) * (sc / 2) + (1 + usm) * cc * uc^2$$

$$\text{Out[*]} := cc uc^2 (1 + usm) + \frac{1}{2} sc uc (2 + usm) + vc$$

$$\text{In[*]} := g[x_] = \left(1 - \frac{x * w'[x]}{2 * w[x]} \right)^2 - \frac{w'[x]^2}{4} * \left(\frac{1}{w[x]} + \frac{1}{4} \right) + \frac{w''[x]}{2}$$

$$\text{Out[*]} := 1$$