

**Fixed points for the nontrivial case  $g_1^* \neq 0$ ,  $u_1^* \neq 0$**

$$\beta_{g_1} = g_1(-y + 2\gamma_D - 2\gamma_v),$$

$$\beta_{g_2} = g_2(-\epsilon - \gamma_{g_2}),$$

$$\beta_{u_2} = -u_2\gamma_{u_2},$$

$$\beta_{u_1} = u_1(-\eta + \gamma_D),$$

$$\beta_a = -a\gamma_a,$$

anomalous dimensions

$$\begin{aligned}\gamma_D &= \frac{g_1}{4(1+u_1)} \left[ 3 + \alpha \frac{u_1-1}{u_1+1} + \frac{4\alpha a(1-a)}{(1+u_1)^2} \right] + \frac{g_2}{8}, \\ \gamma_a &= (1-2a) \left[ \frac{g_1\alpha(1-a)}{2(1+u_1)^3} + \frac{g_1u_2}{4a(1+u_1)} \left( 3 + \alpha - \frac{2\alpha}{1+u_1} \right) + \frac{g_2}{8a} \right], \\ \gamma_{u_2} &= \frac{g_1(1-2u_2)}{4(1+u_1)} \left[ 3 + \alpha \frac{u_1-1}{u_1+1} + \frac{2\alpha a(1-a)}{u_2(1+u_1)^2} \right] - \frac{g_2}{8}, \\ \gamma_{g_2} &= -\frac{3g_1}{2(1+u_1)} + \frac{g_1\alpha}{1+u_1} \left[ \frac{(1-2a)^2}{2} + \frac{1-3a(1-a)}{1+u_1} + \frac{2a(1-a)u_1}{(1+u_1)^2} \right] - \frac{3g_2}{2}, \\ \gamma_v &= \frac{g_1\alpha}{4(1+u_1)^2} \left[ \frac{4a(1-a)}{1+u_1} - 1 \right] + \frac{g_1u_2}{2(1+u_1)} \left[ 3 + \frac{\alpha u_1}{1+u_1} \right].\end{aligned}$$

**Fixed points**

• FP I

$$g_1^* = 0, \quad g_2^* = \frac{2\epsilon}{3} \wedge g_2^* = 8\eta, \quad u_1^* \text{ not fixed }, \quad a^* = \frac{1}{2}, \quad u_2^* = 0$$

• FP II

$$g_1^*, \quad g_2^* = 0, \quad u_1^*, \quad a^* = \frac{1}{2}, \quad u_2^*$$

equations to solve

$$\begin{aligned}\eta &= \frac{g_1}{4(1+u_1)} \left( 3 + \frac{\alpha u_1^2}{(1+u_1)^2} \right), \\ y &= \frac{g_1(1-2u_2)}{2(1+u_1)^2} \left( 3 + u_1(\alpha + 3) \right), \\ 0 &= \alpha \left( -1 + 4u_2 - 2u_1^2u_2 - 4u_2^2(1+u_1) \right) - 6u_2(1+u_1)^2\end{aligned}$$

- FP III

$$g_1^*, \quad g_2^*, \quad u_1^*, \quad a^* = \frac{1}{2}, \quad u_2^*$$

equations to solve

$$\begin{aligned} y &= \frac{g_2}{4} + g_1(1 - 2u_2) \left( \frac{\alpha u_1}{2(1 + u_1)^2} + \frac{3}{2(1 + u_1)} \right), \\ \epsilon &= \frac{3g_2}{2} + g_1 \left( -\frac{\alpha(1 + 3u_1)}{4(1 + u_1)^3} + \frac{3}{2(1 + u_1)} \right), \\ \eta &= \frac{g_2}{8} + \frac{g_1}{4(1 + u_1)^3} \left( 3(1 + u_1)^2 + \alpha u_1^2 \right), \\ 0 &= \frac{g_2 u_2}{8} - \frac{g_1 u_2(1 - 2u_2)}{4(1 + u_1)} \left( 3 + \alpha \frac{u_1 - 1}{u_1 + 1} + \frac{2\alpha a(1 - a)}{u_2(1 + u_1)^2} \right) \end{aligned}$$

- FP IV

$$g_1^*, \quad g_2^*, \quad u_1^*, \quad a^* \neq \frac{1}{2}, \quad u_2^* \neq \frac{1}{2}$$