Dylan C. Beck

EDUCATION

| The University of Kansas | M 0000 |
|--|---|
| Ph.D., mathematics | May 2022 |
| Ph.D. thesis: Combinatorial and Homological Aspect | $s\ of\ Monomial\ Algebras\ and\ Numerical\ Semigroups$ |
| M.A., mathematics | |
| Missouri State University B.S. with Honors, mathematics (minor in German) GPA: 4.00/4.00; member of Kappa Mu Epsilon (Ma | · · · · · · · · · · · · · · · · · · · |
| MPLOYMENT | |
| The University of Kansas | |
| Graduate Teaching Assistant | Aug 2016 to May 2022 |
| An asterisk (*) denotes instructor of record. | |
| \diamond MATH 002 (Intermediate Algebra) | \diamond MATH 115 (Applied Calculus I)* |
| ♦ MATH 101 (College Algebra) | ♦ MATH 125 (Calculus I) |
| ♦ MATH 104 (Precalculus)* | ♦ MATH 126 (Calculus II) |
| \diamond MATH 105 (Intro to Topics in Mathematics)* | ♦ MATH 127 (Calculus III) |
| Leader, Algebra Ph.D. Qualifying Exam Study Grou | up |
| Organizer, Graduate Student Algebra Seminar | |
| Leader, Probability and Statistics Ph.D. Qualifying | Exam Study Group Aug to Dec 2018 |
| Missouri State University | |
| Undergraduate Teaching Assistant | June 2015 to Aug 2016 |
| \diamond MTH 101 (Intermediate Algebra A) | |
| Mathematics Tutor, Bear CLAW (Center for Learni | ng and Writing) Aug 2013 to Aug 2016 |
| \diamond MTH 103 (Intermediate Algebra) | ♦ MTH 261 (Calculus I) |
| \diamond MTH 135 (College Algebra) | ♦ MTH 280 (Calculus II) |
| ♦ MTH 138 (Precalculus) | \diamond MTH 287/288 (Applied Calculus I/II) |
| ♦ MTH 181 (Trigonometry) | ♦ MTH 302 (Calculus III) |

AWARDS

Teaching

| finalist, Florence Black Award for Excellence in Teaching $\hdots \dots \dots Apr$ | 2021 |
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| Academic | |
| John Bunce Memorial Award | 2022 |
| Elbert Walker Graduate Scholarship in Mathematics | 2021 |
| Rashleigh Family Graduate Scholarship in Mathematics | 2020 |
| May Landis Graduate Scholarship in Mathematics | 2019 |
| U.G. Mitchell Graduate Scholarship in Mathematics | 2019 |
| first place in mathematics, MOState CNAS Undergraduate Research Symposium | 2014 |

RESEARCH

Research Interests

commutative algebra and its connections to combinatorics and additive number theory

Publications

On a generalization of two-dimensional Veronese subrings, in progress

ABSTRACT. If a is a positive integer and k is a field, then the ath Veronese subring of the twodimensional polynomial ring k[x,y] is the monomial subring $k[x,y]^{(a)} = k[x^iy^{a-i} \mid 1 \leq i \leq a]$. We demonstrate that for any nonempty subset $A \subseteq [a] = \{0,1,\ldots,a\}$, the properties of the monomial subring $k[x,y]^{(A)}$ are intimately intertwined with the properties of the r-fold sumsets of A.

Canonical blow-up of one-dimensional singularities (with Hailong Dao), in progress

ABSTRACT. We study the canonical blow-up $B(\omega_R)$ of an analytically unramified one-dimensional Cohen-Macaulay local ring (R, \mathfrak{m}, k) with infinite residue field k and canonical ideal ω_R . If $B(\omega_R)$ is Gorenstein, we say that R has the Gorenstein canonical blow-up (GCB) property. We provide equivalent conditions for GCB rings, and we show Arf rings, nearly Gorenstein rings of minimal multiplicity, farflung Gorenstein rings, and numerical semigroup rings of multiplicity three are GCB. We study related numerical semigroup rings and give examples.

Some new invariants of Noetherian local rings (with Souvik Dey), arXiv: 2205.01658

ABSTRACT. We introduce two new invariants of a Noetherian (standard graded) local ring (R, \mathfrak{m}) that measure the number of generators of certain kinds of reductions of \mathfrak{m} , and we study their properties. Explicitly, we consider the minimum among the number of generators of ideals I such that either $I^2 = \mathfrak{m}^2$ or $I \supseteq \mathfrak{m}^2$ holds. We investigate subsequently the case that R is the quotient of a polynomial ring $k[x_1, \ldots, x_n]$ by an ideal I generated by homogeneous quadratic forms, and we compute these invariants. We devote specific attention to the case that R is the quotient of a polynomial ring $k[x_1, \ldots, x_n]$ by the edge ideal of a finite simple graph G.

Academic Talks

Some New Invariants of Noetherian Local Rings (URiCA, May 2022)

Canonical Modules (Graduate Student Algebra Seminar, Mar 2022)

Some New Invariants of Edge Rings of Finite Simple Graphs (KU Combinatorics Seminar, Feb 2022)

A Small Survey of Topics in Commutative Algebra (Graduate Student Seminar, Feb 2022)

The Basics of Homological Algebra (Graduate Student Algebra Seminar, weekly from Feb to Apr 2022)

The Canonical Blow-Up of a Numerical Semigroup (KS Math Graduate Student Conference, Dec 2021)

Canonical Blow-Up of One-Dimensional Singularities (KU Local Algebra Conference, Nov 2021)

Serre's Condition and Cohen-Macaulayness (Graduate Student Algebra Seminar, Oct 2021)

Depth, Dimension, and Cohen-Macaulayness (Graduate Student Algebra Seminar, Oct 2021)

Numerical Semigroup Rings (Commutative Algebra Regional Expository Seminar, Feb 2021)

Loewy Length and the Rees Property (Graduate Student Algebra Seminar, Mar 2020)

Gorenstein Rings and the Canonical Module (Graduate Student Algebra Seminar, Nov 2019)

Cohen-Macaulay Rings and Their Properties (Graduate Student Algebra Seminar, Nov 2019)

Connecting Depth, Ext, and Projective Dimension (Graduate Student Algebra Seminar, Apr 2019)

Banach-Tarski Paradox and Equidecomposable Sets (Graduate Student Seminar, Nov 2018)

Cohen-Macaulay Rings, Depth, and Regular Sequences (Graduate Student Algebra Seminar, Oct 2018)

Ethics in Mathematics: a History of Mathematical Proofs (Graduate Student Seminar, Feb 2018)

Paradoxical Decompositions and the Banach-Tarski Paradox (Graduate Student Seminar, Oct 2016)

On a Quadratic Variant of a Problem of Berzsenyi (Missouri State University College of Natural and Applied Sciences Undergraduate Research Symposium, May 2014)

Conferences Attended

KUMUNU Commutative Algebra Conference (The University of Nebraska, May 2022)

URiCA: Upcoming Researchers in Commutative Algebra (The University of Nebraska, May 2022)

Kansas Mathematics Graduate Student Conference (The University of Kansas, Dec 2021)

KU Local Algebra Conference (The University of Kansas, Nov 2021)

KUMUNU Commutative Algebra Conference (The University of Nebraska, Sep 2019)

KUMUNUjr Commutative Algebra Conference (The University of Nebraska, Mar 2019)

Southwest Local Algebra Meeting (SLAM) (The University of Texas at El Paso, Feb 2019)

KUMUNU Commutative Algebra Conference (The University of Kansas, Oct 2018)

Great Plains Combinatorics Conference (GPCC) (Kansas State University, Apr 2018)

Graduate Student Combinatorics Conference (GSCC) (The University of Texas at Dallas, Apr 2018)

KUMUNU Commutative Algebra Conference (The University of Kansas, Oct 2017)

The Midwest Combinatorics Conference (University of Minnesota, May 2017)