

## 2) (5 pts) ANL (Algorithm Analysis)

A  $O(n^3)$  image processing algorithm took 125 milliseconds to index  $n = 400$  images. How long would it be expected for this algorithm to take to index **640** images, in milliseconds? **Please show all your work, including algebraic simplification, which is part of what is being tested with this question.**

Let  $T(n)$  be the run time of the algorithm. Then there is some constant  $c$  such that

$$T(n) = cn^3$$

$$T(400) = c(400^3) = 125ms \rightarrow c = \frac{125ms}{400^3}.$$

$$T(640) = c(640^3) = \frac{125ms}{400^3} \times 640^3 = (125ms) \times \left(\frac{640}{400}\right)^3 = (125ms) \times \left(\frac{8}{5}\right)^3 = 125ms \times \frac{512}{125} = \mathbf{512ms}$$

**Grading: 1 pt set up to solve for c**

**1 pt solve for c (no simplify)**

**1 pt plug in 640**

**2 pts to get to final answer**