

1) (5 pts) ANL (Algorithm Analysis)

What is the best and worst case runtime for the following algorithm, in terms of the input parameter n ? Give a brief explanation for your answers.

```
int foo(int * arr, int n){  
    if (n == 0)  
        return 0;  
  
    int j = 0, i;  
  
    for (i = 0; i < n; i++)  
        if (arr[i] > arr[j])  
            j = i;  
  
    int nLen = n - j - 1;  
    return arr[j] + foo(arr + j + 1, nLen);  
}
```

Best Case

The for loop runs and sets $j = n - 1$, which means that $nLen$ gets set to 0. In this case, the subsequent recursive call will immediately return 0 and the original recursive call will return the value of the last array element. The run time in this case is **$O(n)$** , since the entirety of the execution includes one for loop that runs n times and a few other simple statements. From a conceptual standpoint, the for loop identifies the index in between 0 and $n-1$ that stores the largest value within that range.

Worst Case

The worst case is when the array is sorted in reverse order. Every call eliminates only 1 value at the cost of n operations. The total runtime becomes **$O(n^2)$** .

Grading: 2 pts for each answer, 1 pt for all of the explanation.